Emotiq Yellowpaper

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ABSTRACT

We are nearing the future where scalability and high transaction throughput will be the baseline for blockchain technology. We are are not there yet and the race for an industrial-strength blockchain foundation is still on. We would like to present Emotiq, a decentralized public blockchain with strong consistency, fast transaction throughput, unlimited horizontal scalability through sharding, strong cryptography, privacy via non-interactive zero-knowledge proofs and natural language smart contracts.

1. INTRODUCTION

Emotiq is a public decentralized blockchain so anyone can join the network, become a validator and earn rewards for maintaining it. Emotiq uses the Proof-of-Stake (PoS) approach and all validators need to post a security bond of a fixed number of tokens which are forfeited if the validator is found cheating.

Emotiq uses a Byzantine consensus protocol with strong consistency which enables all validators to agree on the validity of blocks, without wasting computational power resolving inconsistencies (forks). Clients don?t need to wait more than a few seconds to be certain that a submitted transaction is committed; as soon as it appears in the blockchain, the transaction can be considered confirmed.

Emotiq provides unlimited horizontal scalability and throughput of thousands of transactions per second through sharding, as well as a cross-shard commit protocol.

Emotiq uses Boneh-Lynn-Shacham (BLS) pairing-based crypto (PBC). This enables short BLS signatures on public keys, as well as hierarchical deterministic wallets with all of the advantages promoted by BIP-32 but without the security risks.

We also cloak transactions through non-interactive zero-knowledge proofs and purge old and spent transactions. The former provides increased privacy by hiding transaction amounts and the latter drastically reduces the amount of data required to be maintained by validators.

Unlike most technical papers out there, this paper is designed to give the reader a technical overview of the platform using simple and plain language. We start with a look at networking and proceed to token economics and consensus, after which we review confidential transactions, blockchain pruning, real-time transactions validation and other parts of the system. We conclude with a forward outlook.

2. NETWORKING

The Emotiq network is composed of full nodes, called validators, and light clients, e.g. those running on mobile devices or in the or browser. Each validator maintains a full copy of the blockchain and associated data structures. Validators participate in the collective signing protocol and respond to queries by light clients.

Emotiq maintains the core of the network by running a number of validator nodes which both simplifies the bootstrap of new nodes and ensures continuity of the network. The addresses of the core nodes are hard-coded into each release of the Emotiq blockchain software.

Each node keeps a list of addresses of the nodes it knows about (peers) and adds new nodes to the list as it becomes aware of them. A new node starting up connects to one of the core nodes to fetch a list of peers. Each validator node quickly re-broadcasts each received transaction to a random subset of its peers, after only a few light checks. This both ensures that a node cannot be DDOS-ed with transactions to validate and that it does not re-broadcast junk transactions.

To discourage bad actors, we employ a mechanism to both throttle peers and punish peers for bad transactions, etc. by blocking them from further participation in the network.

3. CONSENSUS

3.1 Collective Signing

3.2 Bias-resistant Distributed Randomness

3.3 Leader Election

4. TRANSACTIONS

UTXO was first introduced by Bitcoin and, unlike Ethereum, aggregates spent and unspent coins, available across multiple wallets, into a single balance. Not only does UTXO offer simplicity, but also drastically increases Emotiq?s scaling capability, by enabling transactions to be processed independently and in parallel.

Emotiq transactions consist, at a minimum, of the sender?s signature and public key, the receiver address or addresses, as well as a smart contract that governs how the transaction may be used.

Emotiq uses zero-knowledge proofs to ensure transaction amounts, among other things, are not visible in the public ledger. For example, although blockchain addresses are represented by random strings, it is currently possible for mapping software to crawl Bitcoin?s ledger for spent and unspent (UTXO) coins, to identify the transactions of a single private key and determine a holder?s total wealth in Bitcoin. While non-interactive zero-knowledge proofs do not prevent such transaction graph analyses, they prevent the tracing party from seeing the amounts being transferred.

Emotiq builds upon MimbleWimble and strong cryptography to ensure that spent transactions can be pruned and new nodes can efficiently validate the blockchain without downloading any old or spent transactions. Unlike with Proof-of-Work (PoW), where transaction pruning can lower security by lowering the amount of work needed to be redone by an attacker, the approach does present an issue for our PoS blockchain.

5. TRANSACTION PRUNING

6. BLOCKS

Blocks consist of a header and a list of transactions. The block header contains a hash of the previous block, the collective signature and the list of public keys of co-signers, plus the Merkle root of the transactions stored in the block.

6.1 Rewards and incentives

7. CRYPTOGRAPHY

7.1 Pairing-based Cryptography

Emotiq utilizes advanced bilinear pairing-based cryptography[4][5] (PBC) for user keying, Boneh-Lynn-Shacham (BLS) Signatures[6], fast multi-party signatures, and for Randomness Generation. The advantages of PBC are numerous and include short signatures, fast signature generation, safe deterministic hierarchical wallet keying, and fast multiparty randomness generation.

A bilinear pairing uses pairs of Elliptic Curves, defined over two separate groups, such that their bilinear mappings produce homomorphic encryption in a resulting composite field. If we denote the two curve groups as G_1 and G_2 , their Tate pairing field G_T , and prime order finite field Z_q , then their pairing $e(G_1, G_2) \in G_T$ is such that

$$e(a U, V) = e(U, a V) = g^{a}$$

where $U \in G_1$, $V \in G_2$, $a \in Z_q$, and $g \in G_T$.

In our system, pairings are asymmetric. Group G_1 is always the smaller group, with the shortest representation. Pairings are ordered, and must be performed with a G_1 element as the first argument, and a G_2 element as second.

Specifically, our Z_q uses 256 bits, G_1 was chosen to have a 264-bit representation, G_2 has a 520-bit representation, G_T has a 3072-bit representation, and the prime order of the groups is $q \approx 2^{254}$, which gives us roughly 2^{127} security.

Private keys belong to the finite field Z_q with the same prime group order. Public keys are generated in G_2 , and

signatures are generated in G_1 . The embedding degree of our curves is 12, and correspond to $Type\ f$ asymmetric pairing curves in Lynn's Thesis[4]. Wherever they occur, we use compressed point representation for group elements from G_1 and G_2 .

The complete specification of the Emotiq cryptosystem requires knowledge of all curve pairing parameters, plus two chosen generators $U \in G_1$, and $V \in G_2$.

Hash values are first mapped to an element of Z_q before creating points in G_1 and G_2 as

$$G_1(H(x)) \equiv Z_q(H(x)) U$$

and

$$G_2(H(x)) \equiv Z_q(H(x)) V$$

In the following presentation we shall try to adhere to the convention that groups G_1 and G_2 are additive groups, while Z_q and G_T are both additive and multiplicative. Capitalized symbols denote groups and points from Elliptic curves, while lower cased symbols denote elements of finite fields. Field arithmetic in Z_q is implicitly performed $(mod \, q)$.

7.2 Boneh-Lynn-Shacham (BLS) Signatures

BLS signatures are the shortest possible, and enable multisignature generation in just one pass. A BLS signature on message msg is computed as

$$Sig = s G_1(H(msg))$$

where H(x) is the SHA3/256 hash of its argument, $s \in Z_q$ is the user's secret key value, and $G_1(H(x)) \in G_1$ is the group member that corresponds to that hash value. A signature is always accompanied by the public key of the signer, P = s V, for generator $V \in G_2$, producing a signed message as a triple

Because of homomorphism we can verify a signature by noting that a valid signature exhibits the pairing relationship

$$e(Sig, V) = e(s G_1(H(msg)), V)$$

= $e(G_1(H(msg)), s V)$
= $e(G_1(H(msg)), P)$

And also because of homomorphism, we can easily compute a multi-party signature by simply summing the individual signatures and also summing their corresponding public keys:

$$e(\sum_{i} s_i G_1(H(msg)), V) = e(G_1(H(msg)), \sum_{i} P_i)$$

producing the collective triple

$$(msg, \sum_{i} sig_{i}, \sum_{i} P_{i})$$

Therefore, during the computation of collective signatures, we need only a single pass through all participants as we gather and sum their signature components. A collective signature appears no different than a single signature.

7.2.1 Comparison with Schnorr Signatures

In contrast, conventional Schnorr signatures require two signature values, forming a quadruple with message and public key. For message msg the Schnorr signature is the pair (R, u) of an Elliptic Curve point R and a field value u, where R = rG, for generator point G, and

$$r = H(k_{rand}, msg, P)$$

is chosen as a random offset. Finally

$$u = r + H(R, P, msg) s$$

The Schnorr signature is validated by checking that

$$uG = R + H(R, P, msg)P$$

For collective Schnorr signing, all participants are asked to compute their own commitments $R_i = r_i G$. Those values are collected and summed to produce a global challenge value, $c_{glb} = H(\sum_i R_i, \sum_i P_i, msg)$. Then the participants are asked to produce their u_i values against that global challenge:

$$u_i = r_i + c_{qlb} s$$

and again the values are summed. Hence collective Schnorr signatures require two interactions with every signer of the message. Network traffic is approximately twice that required for BLS signatures, with a consequent window of opportunity for attackers to spoil the process during the second round.

7.3 Cosi Multisignatures

We use Cosi trees[9] to provide scalable, distributed, multisignature generation. Validator nodes are selected from among a group of stakeholder nodes, using random sortition to assign N of them to a position in a Cosi tree.

A Cosi tree is an n-way tree, where each node in the tree interior is a group leader over n subnodes, each of which may be group leaders over their own subtrees. At any one time, there may be several Cosi trees operating for different purposes, and some nodes might belong to more than one Cosi tree.

When a signature is requested from a Cosi tree, the message is distributed down through the tree to all participant nodes. Each node then attempts to validate the message and decides whether or not to add its BLS signature to the collective signature formed from the sum of all signatures of its subgroup, before passing the augmented signature back up to its parent node in the tree. Accompanying that signature is a composite public key consisting of the sum of participant node public keys, and a bitmap that represents which nodes actually signed the message.

Validation of a message requires varying computation based on the type of message. For randomness generation, it means validating all publicly verifiable quantities and producing decrypted shares. For block validation it means verifying the public keys of all signers of the block, validating all transactions, and so on.

At the top of the tree the bitmap is converted into a list of public keys for all participating nodes, which is used to verify the summed public key, and to gain a census count on how many nodes actually signed the message. That census count is checked against a pBFT threshold of 2f + 2, where $f = \lfloor \frac{N-2}{3} \rfloor$ is the tolerance for Byzantine failures among the nodes, to decide whether the multisignature is acceptable.

7.4 Consensus using Cosi

In and of itself, a single pass through a Cosi tree is insufficient to guarantee pBFT. Instead, we perform two passes. The first one sends a message to be validated by all member nodes of the Cosi network. On return the message has acquired some number of signatures. If that number exceeds the requisite pBFT threshold then we will have completed a successful *prepare* phase of pBFT.

The second pass sends the, now validated, message and its multisignature to all participant nodes in the Cosi network, to ensure that each node has seen the validated multisignature. Their new signatures attest that they will remember this message for future reference in efforts to deny double spending. This corresponds to the *commit* phase of consensus. Once all Cosi nodes have signed off on the validated message, and if the count remains above the pBFT threshold, the caller of this consensus round can be confident that pBFT consensus has been achieved.

7.5 Transaction Privacy

A simple technique for cloaking all transactions in a publicly verifiable manner does not need bilinear pairings, although an algorithm in bilinear pairings can also be developed.¹

We start with recognizing that a full transaction satisfies the following simple relation:

$$paid = cost + fees + change$$

where *paid* is the amount tendered in the transaction, *cost* is the cost of the product or service, *fees* are transaction fees that must be paid, and *change* is the amount returned to the buyer, due to overpayment.

Hence, if a spending transaction is rewritten in the form:

$$change - paid = -(cost + fees)$$

then when (cost+fees) is added to this transaction by the seller, the resulting full transaction will show a zero balance. It is very simple to advertise a zero balance, or some function of zero, such that everyone can recognize it.

To provide privacy for the transaction, the numeric value of (change-paid) is homomorphically encrypted to prove that only the sender could have encrypted it, yet the addition of (cost+fees) can be performed and produce the encoding of zero for all to see.

At the same time, we must also provide cryptographic proofs that the values of *change* and *paid* both lie within legitimate range, and that change < paid. That is the purpose of Bulletproofs, discussed in the next section.

A buyer cloaks his or her purchase offer by forming a quadruple $(P_{buy}, P_{sell}, t_{buy}, R_{sell})$, for public keys $P_{buy} = s_{buy} V \in G_2$, $P_{sell} = s_{sell} V \in G_2$, $s_{buy}, t_{buy}, s_{sell} \in Z_q$, and a point on an Elliptic Curve, $R_{sell} \in G_2$, for generator $V \in G_2$ on the curve, given as

$$t_{buy} = \frac{k_{rand}(change - paid)}{s_{buy}} \in Z_q$$

and

$$R_{sell} = k_{rand} P_{sell} \in G_2$$

 $^{^1}$ For single curve computations, we perform in field Z_q and group G_2 since that field already has our private keys, and the G_2 group has our public keys. Hence the same keying can be used over a single curve algorithm and for all of our pairing cryptography.

for k_{rand} a random cloaking factor, and buyer's secret key $s_{buy} \in Z_q.$

The random cloaking factor, k_{rand} , provides privacy by making each transaction appear different, even when the same currency values are involved. It also protects the secret keys, since the only other relation anyone knows about them comes from the public keys, and there is the ECDLP barrier of difficulty between them.

At the seller's end, we compute

$$C_{sell} = \frac{cost + fees}{s_{sell}} R_{sell} \in G_2$$

for seller's secret key $s_{sell} \in Z_q$, and check that

$$t_{buy} P_{buy} + C_{sell} = G_2(0)$$

Value $G_2(0)$ is the identity element in the curve group, and easily recognized by everyone. To accept the transaction, seller publishes the quadruple $(P_{buy}, P_{sell}, t_{buy}, C_{sell})$ so that everyone can verify the same $G_2(0)$ that represents a valid transaction.

The initial purchase offer cloaks its currency values from everyone, including the seller. The final published transaction is also cloaked with the same k_{rand} , and so hides all monetary values, except the zero balance that results from the check equation. Nobody but the intended seller can finish the transaction, and the check equation provides undeniable proof that the buyer created the offer. A zero balance proves that enough currency was supplied to cover net cost.

If a zero result is not produced, then it can only mean one or more of three things. First, the seller may be illegitimate and unable to decrypt the R_{sell} value with the secret key, s_{sell} . Second the transaction might not have been produced by the indicated buyer, P_{buy} . Or finally, the currency amounts may not match the seller's expectations. In any case, such a transaction would never be permitted into the blockchain.

7.5.1 Privacy without Encryption

There may be times when the (cost + fees) is publicly known, and there is no seller involved in a transaction. We can still achieve transactional privacy in that case. Simply make the substitutions

$$P_{sell} \to V \in G_2$$
$$s_{sell} \to 1$$

The buyer publishes the triple (P_{buy}, t_{buy}, R) , where t_{buy} is as before.

$$t_{buy} = \frac{k_{rand}(change-paid)}{s_{buy}} \in Z_q$$

and

$$R = k_{rand} V \in G_2$$

Then anyone knowing the value of (cost+fees) can verify the transaction using

$$C = (cost + fees) R \in G_2$$

and check that

$$t_{buy} P_{buy} + C = G_2(0)$$

The validation relation proves that the buyer formed the purchase offer, and that they forwarded enough money to cover net costs, while still cloaking the values involved. The cloaked values need to be accompanied by range proofs.

7.6 Bulletproofs

8. RANDOMNESS

Bias-resistant public randomness is a critical component of the Emotiq consensus protocol. Emotiq employs Rand-Herd, a large-scale distributed protocol that provides publicly-verifiable, unpredictable, and unbiasable randomness against Byzantine adversaries by implementing an efficient, decentralized randomness beacon. RandHerd arranges participants into verifiably unbiased random secret-sharing groups, which then repeatedly produce random output at predefined intervals. Emotiq uses RandHerd to elect leaders during each block-signing round, as well as to form shard groups.

8.1 Fast Randomness Generation with PVSS

The use of BLS Signatures allows an abbreviated form of PVSS randomness generation. Participants in randomness generation are given a list of neighboring group nodes in the network, with whom they carry out a pBFT protocol with publicly verifiable secret sharing (PVSS).

Within each group, a sharing threshold is set at $t = \lfloor \frac{N}{3} \rfloor + 1$ for group size N. Secret random seeds are generated by each participant, then encrypted shares are formed over that secret and distributed to other group members, along with cryptographic proofs on the shares.

For sharing threshold t, a random polynomial of order $t\!-\!1$ is generated

$$p(x) = a_0 + a_1 x + \dots + a_{t-1} x^{t-1}$$

with the secret value denoted by a_0 . Shares are constructed by computing the value of this polynomial for each member of the group, assigned successive ordinal values, i=1...N. The resulting share values, p(i), are then encrypted by multiplying the share value by the public key of each member, $E(share_i) = Z_q(p(i)) P_i \in G_2$, and proofs are generated by forming a point, $Proof_i = Z_q(p(i)) U \in G_1$, for generator $U \in G_1$.

A vector of shares and a vector of proofs is generated, one element for each member of the group, and these vectors are then transmitted to each group member.

$$(E(share_1), E(share_2), ..., E(share_N))$$

$$(Proof_1, Proof_2, ..., Proof_N)$$

As with any BLS signature, each share is validated against its proof by checking that the pairings match:

$$e(Proof_i, P_i) = e(U, E(share_i))$$

Every member of the group can also verify that all shares from another group member were consistently generated from the same sharing polynomial. To do so, we treat the share vector as a codeword from a Reed-Solomon encoding[1], compute a random polynomial of order N-t-1 and use that to compute a test vector from the dual-space of the original share generating polynomial:

$$f(x) = b_0 + b_1 x + \dots + b_{N-t-1} x^{N-t-1}$$

$$c_{\perp} = (\lambda_1 f(1), \lambda_2 f(2), ..., \lambda_N f(N))$$

where weights $\lambda_i = \prod_{j \neq i} \frac{1}{i-j}$, for i, j = 1...N. Then the consistency of the encrypted shares is verified by checking

that:

$$\sum_{i} c_{\perp i} \operatorname{Proof}_{i} = G_{1}(0)$$

This consistency check is absolutely certain for valid sharing vectors, and has an inconsequential probability of failing to detect an improper sharing set given as $\approx 1/q$, or about 1 chance in 2^{254} . There is a greater likelihood of finding a hash collision in SHA3/256 than in seeing a failure to detect an inconsistent sharing vector.

After performing consistency checks on the sharing set from one group member, the share directed at one node can be decrypted with its secret key to produce a decrypted share,

$$G_2(share_i) = \frac{1}{s_i} E(share_i) \in G_2$$

for secret key $s_i \in Z_q$.

This decrypted share is then broadcast to all group members. Decrypted shares can be verified from the pairing relation:

$$e(Proof_i, V) = e(U, G_2(share_i))$$

As soon as a sharing threshold number, $(n \ge t)$, of decrypted shares has been seen for any one sharing set, the secret randomness from that set can be discovered via Lagrange interpolation:

$$G_2(random) = \sum_i G_2(share_i) \prod_{j \neq i} \frac{i}{i-j}$$

Finally, after a supermajority of sharing sets has been decrypted, $(n \geq 2\lfloor \frac{N}{3} \rfloor + 1)$, their randomness is combined as a simple sum in G_2 , and forwarded to all other groups.

$$G_2(random_{grp}) = \sum_i G_2(random_i)$$

Proof of group randomness comes from the sum of Lagrange interpolations of the individual proof sets. Final randomness results from a supermajority sum of randomness obtained from each group, and its proof results from the sum of group proofs.

So the use of pairing-based cryptography shows great benefits, not only in minimizing network traffic, and by making immediate commitments to portions along the way, and also from the fact that proofs are so easily generated as simple sums of existing proofs.

Timing tests show that this approach scales linearly with number of group participants, ranging from about 5 seconds for 32 group members, to about 7 minutes for 1024 group members, on an ordinary iMac with an Intel i7 processor. The timings are dominated by compute load, not network communications.

8.1.1 The TPM Method

There is an alternate method for generating randomness with PVSS, which I call the TPM $Method.[11]^2$ It performs

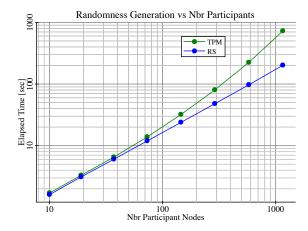


Figure 1: Comparison of performance between the TPM Method and the Reed-Solomon interpretation of proof vectors.

the same share generation procedure as seen above, but instead of sending along a vector of proofs on each encrypted share, it sends along proofs on the sharing polynomial coefficients, $a_i, i = 0..t-1$ using $Aproof_i = a_iU$ for generator $U \in G_1$.

Then, at each receiving node, the shares are verified by computing the sums

$$Proof_i = \sum_{j=0..t-1} i^j Aproof_j, i = 1..N$$

Then the pairing relation is checked

$$e(Proof_i, P_i) = e(U, E(share_i))$$

These proof sums correspond directly to the proofs presented in the previous section. And they also directly verify that every encrypted share came from the same polynomial. One advantage of this method is that instead of transmitting 2N vector elements, we now only need to transmit N+t elements.

However, we now also need to supply these proof sums along with any decrypted shares that we compute, and the method scales super-linearly. Timing tests have shown it to be a hair slower than the first method for N=32, and about half as fast when N=1024. But the method is equivalent in its information content, and every bit as secure.

8.2 Verifiable Random Functions

A verifiable random function (VRF)[7] uses a pseudorandom function (PRF) in such a way as to furnish proof that the resulting pseudo-random value came from a specific seed value mixed with the creator's secret key. And even though a secret key was involved in the generation of randomness, anyone can duplicate the calculation by knowing only the seed value and creator's public key. We follow the work of Dodis and Yampolskiy[2], to provide a PRF as follows:

For arbitrary input seeding values, form the hash H(seed) using SHA3/256. This converts arbitrary objects of any length into a 256-bit random-like, but reproducible, pattern. Then map that hash value into our Z_q field, which has dimension $q = |Z_q| \approx 2^{254}$, to produce $x = Z_q(H(seed))$.

²The paper has an error wherein it specifies that encrypted shares should be formed as the product of the share value and the generator of the curve. That is incorrect, as the encryption needs to incorporate information about the target node keying. It seems likely that the error crept in by way of fractured translation to English. I found the nomenclature terribly inconsistent and confusing.

Output of the VRF is a pseudo-random value in the pairing field (3072 bits)

$$y = VRF(x, s) = e(U, V)^{1/(x+s)} \in G_T$$

for secret key $s \in \mathbb{Z}_q$, generators $U \in G_1$, $V \in G_2$, and with proof

$$R = \frac{1}{x+s} U \in G_1$$

Output of the VRF is the quadruple (seed, x, y, R), i.e., the original seed, the seed deterministically reduced to an element of Z_q , the output of the VRF computation, and the point in G_1 that represents the proof.

Verification of proof checks the pairing

$$e(R, xV + P) = e(U, V) \in G_T$$

for public key $P = sV \in G_2$, and to verify that

$$y = e(R, V)$$

and that

$$x = Z_q(H(seed))$$

8.3 Blockchain Leader Election

Publicly verifiable randomness generation is used to perform leader elections for blockchain production. All public key holders can choose to participate in elections by depositing an amount of currency into escrow as their stake. Stakeholders also participate as members of Cosi and Randherd protocols.

The amount at stake is a hedge against misbehavior to thwart attacks. Requiring a stake helps prevent Sybil attacks. If a participant has staked some currency and is found to be misbehaving, that stake will be forfeited and the participant will be barred from future participation for some period of time. Conversely, members in good standing are rewarded for their services by sharing transaction fees with them in proportion to their stake.

Elections are stake-weighted lotteries. The larger your stake, the greater your chances of winning a round. After serving one round, the leader relinquishes his right to be re-elected until some number of rounds later. But former leaders can still serve as participants in other blockchain activities and receive rewards. The leader block is awarded a fixed fraction of the fee bounty, while the remainder is distributed to other participants in proportion to their stakes.

In order to produce a stake-weighted lottery, we could imagine dividing a circle into angular sections proportional to individual stakes, with the full circumference of the circle representing the sum of all stakes. A uniform random number over a finite interval acts as a spinner in a dial readout, and wherever it points after a spin, that member is selected as the next leader. Larger stakeholders occupy a larger portion of the circumference, and so have a more likely chance of winning.

In practice a binary tree of participants is formed, in arbitrary order, where each interior node represents the sum of all its sub-node stakes. The topmost node of the tree shows the full sum of all stakes represented in the tree, with all participants located in leafs. Branching decisions begin at the top node of the tree and descend toward leafs using the random value as a probe of the interval described by the partial sum at each node, with the division between left

and right based on the relative weights of its two subtrees. Descent continues until meeting a leaf node, and declaring that node the winner of the election.

If the random probe value is converted into a fractional value of its range, and each interior node is relabeled with its division fractional value, then it is simple to choose left or right subnodes based on a single comparison between the two fractional values.

Once elected, the leader forms the necessary Cosi trees and Randherd groups, and begins assembling a new block for the duration of the epoch until the next election round. There must be a balancing between the period between elections and the length of time it takes to assemble and validate blocks. The larger the block, in number of transactions to be verified, the longer it must take. At some size, that administrative duration will exceed the interval between Randherd beacon outputs.

(What happens if another Randherd random value arrives while everyone is busy validating blocks? Holding a new election right then could spoil the ongoing consensus, marking that block as a failure. And the same thing would happen again, or worse, during the next epoch, as it plays catch-up in block assembly.

Do we need consensus to hold a new election? Then consensus again to validate the election outcome? And so should nodes involved in consensus rounds be stateful so they know not to respond to elections until consensus has completed?

Is consensus nested? Can there be consensus rounds ongoing, inside of an outer consensus round?)

If a stakeholder wins an election but is absent or comes under attack, it may not respond to its election as leader, or block assembly activities will cease in that epoch. Any stakeholder can call for a new forced election, and after (2f+1) such calls have been seen, a new election cycle ensues. All other honest stakeholder nodes that have also seen the threshold number of calls for new election will eagerly grant consensus to newly elected leaders. Stakeholder nodes will typically register a complaint after seeing no activity for longer than an adaptive threshold based on recent past rates. An exponential average could be used for this purpose.

Calls for election are by gossip protocol, and the election protocol is performed in each stakeholder node. Whichever node notices its election as leader must gain the consensus of all other nodes in forming its own Cosi trees. Hence it must use the extant Cosi networks from the current epoch. Failed consensus constitutes a failed election cycle from the perspective of that node. The node can register a call for new election, or else respond to new gossip messages to participate in an epoch managed by some other node that also sees itself as winning the lottery.

If this happens, then it may be time to resynchronize its notion of stakeholder participants against the blockchain record. A stakeholder node so distracted in this manner constitutes just another example from the spectrum of Byzantine failures, and while distracted the node may fail to perform other duties it should have been doing. But the consensus protocol is adaptable to Byzantine failures and will proceed without the node.

8.4 Cryptographic Sortition

Sortition[3] is the process of randomly selecting members for Cosi networks and Randherd groups, based on stake weighting. We described one type of sortition event in the description of blockchain leader election. The process is repeated for selection of other duties. Random values for sortition probing are developed using VRF's to prove fairness in making selections.

As the outcome of selections becomes known, those stakeholders must be removed from the selection tree before holding additional rounds. The purpose of sortition rounds specifies roles, each of which may have different threshold requirements in number of selected participants. Roles specify the purpose of selection, such as for Cosi networks, Randherd groups, and so forth.

8.5 Safe Hierarchical Keying

In current blockchain designs which utilize simple Elliptic Curve cryptography, the possibility of producing subkeys from a master public key is presented. But that is wholly unsafe in the event that a decryption key is also generated for a derived public key. A simple bit of finite field arithmetic is all it takes to discover the original master private key.

With PBC we can safely generate both public and private keys without exposing our master private key. This is also known as Identity-Based Encryption (IBE). But unlike conventional presentations of IBE, we do not rely on a trusted third party for the generation of our keying. Rather, we view the master key holder as the only entity that should be entitled to generate new decryption keys.

Anyone can generate new public keys at any time, based on previously known public keys. But in order to obtain a decryption key for the new public keys, you must ask the primary secret key holder for a decryption key. Doing so puts the primary key holder at no risk for exposing his or her private key.

A new public key can be generated by asking for a subkey of a given public key, using an arbitrary identity value to identify that subkey. The new public key is computed as

$$P_{id} = Z_q(H(id)) V + P$$

for identity id, generator $V \in G_2$, public key $P \in G_2$, and where $Z_q(H(id)) \in Z_q$ is the element of the field that corresponds to the hash of the supplied identity.

You can use this public key to encrypt a message by making use of the hash of a pairing value as an XOR mask against a message

$$E(msg) = msg \oplus H(g^r)$$

where $r = Z_q(H(msg, id)) \in Z_q$, and pairing element

$$g^r = e(U, rV)$$

for generator $U \in G_1$, generator $V \in G_2$. The message is transmitted as the triple (E(msg), R, id), with $R = r P_{id} \in G_2$.

In order to produce a decryption key for that new public key, the primary key holder computes

$$S_{id} = \frac{1}{s + Z_q(H(id))} U \in G_1$$

for secret key $s \in Z_q$. Producing a decryption key in G_1 ensures, by difficulty of ECDLP, that our master private key remains safe against exposure.

Homomorphism allows us to see that the pairings

$$e(S_{id}, R) = e(\frac{1}{s + Z_q(H(id))} U, r(Z_q(H(id)) V + P))$$

= $e(U, rV) = g^r$

which allows us to recreate the XOR mask and decrypt to the original message

$$msg = E(msg) \oplus H(g^r)$$

Verification of the message is done by computing $r = Z_q(H(msg,id))$ and checking that

$$r\left(Z_q(H(id))V + P\right) = R \in G_2$$

In this form, a new private key cannot be used to sign messages in the usual manner as for BLS signatures with the master private key, because we have $P_{id} \neq s_{id} V$. But it does furnish a way to encrypt and decrypt messages by using the hash of the pairing result. This technique has been dubbed SAKKE by its authors Sakai-Kasahara[8]. We have extended SAKKE encryption to indefinite length by using successive SHA3 hashes on the pairing field result and an increasing index value.

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