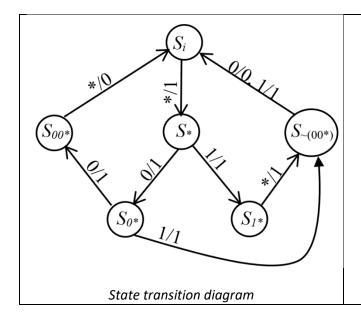
## Binary code assignment, more complicated FSMs

- 1. Optimal assignment of binary codes
  - a. Was implementing binary code checker last time
  - b. Drew naïve implementation of FSM, then minimized it



| Present State | Next   | State  | Output |      |  |
|---------------|--------|--------|--------|------|--|
|               | x = 0  | x = 1  | x = 0  | x =1 |  |
| i             | *      | *      | 1      | 1    |  |
| *             | 0*     | 1*     | 1      | 1    |  |
| 0*            | 00*    | ~(00*) | 1      | 1    |  |
| 1*            | ~(00*) | ~(00*) | 1      | 1    |  |
| 00*           | i      | i      | 0      | 0    |  |
| ~(00*)        | i      | i      | 0      | 1    |  |

State table

- c. Can assign binary codes for states randomly
- d. Rule of thumb for state binary code assignments

e. Assign using the rules above

| Binary Code |   | AB |    |    |    |  |  |
|-------------|---|----|----|----|----|--|--|
|             |   | 00 | 01 | 11 | 10 |  |  |
| C           | 0 |    |    |    |    |  |  |
| L           | 1 |    |    |    |    |  |  |

f. Note that there may potentially be more than one valid code assignment that minimizes distance



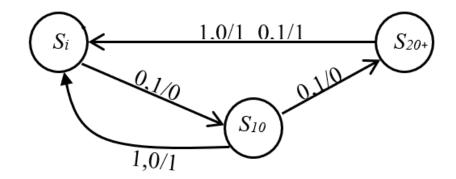
- 2. Debugging an FSM
  - a. Generally, much more efficient to put in effort to get it right to begin with
  - b. One good way of seeing if your FSM you drew was right
  - c. Examples
    - i. With the BCD checker
    - ii. With the vending machine below
- 3. More complicated FSMs
  - a. Design a vending machine
  - b. x<sub>1</sub>, x<sub>2</sub>
  - c. Will use a Mealy model
  - d. First, create state transition diagram

- e. Next, minimize the number of states using the Partition Minimization Procedure i.
  - ii.  $P_2$
  - iii. Draw new state transition diagram

f. Assign code words next

Binary Code  $\boldsymbol{A}$ 1 0 0 B1

## g. Next, create state transition table



Binary Code A

0 1

0 i 20+
1 10

| Drocont Pinom    |    | Present State |   | Inputs                |                | Next State |    | 0        |
|------------------|----|---------------|---|-----------------------|----------------|------------|----|----------|
| Present<br>State | •  | Α             | В | <b>X</b> <sub>1</sub> | X <sub>2</sub> | A'         | B' | Output z |
| i                | 00 | 0             | 0 | 0                     | 0              |            |    |          |
| i                | 00 | 0             | 0 | 0                     | 1              |            |    |          |
| i                | 00 | 0             | 0 | 1                     | 0              |            |    |          |
|                  |    | 0             | 0 | 1                     | 1              |            |    |          |
| 10               | 01 | 0             | 1 | 0                     | 0              |            |    |          |
| 10               | 01 | 0             | 1 | 0                     | 1              |            |    |          |
| 10               | 01 | 0             | 1 | 1                     | 0              |            |    |          |
|                  |    | 0             | 1 | 1                     | 1              |            |    |          |
| 20+              | 10 | 1             | 0 | 0                     | 0              |            |    |          |
| 20+              | 10 | 1             | 0 | 0                     | 1              |            |    |          |
| 20+              | 10 | 1             | 0 | 1                     | 0              |            |    |          |
|                  |    | 1             | 0 | 1                     | 1              |            |    |          |
|                  |    | 1             | 1 | 0                     | 0              |            |    |          |
|                  |    | 1             | 1 | 0                     | 1              |            |    |          |
|                  |    | 1             | 1 | 1                     | 0              |            |    |          |
|                  |    | 1             | 1 | 1                     | 1              |            |    |          |

## h. Finally, create K-maps from table above

| Drosent Binery   |    | Present State |   | Inputs                |                       | Next State |    | 0           |
|------------------|----|---------------|---|-----------------------|-----------------------|------------|----|-------------|
| Present<br>State |    | Α             | В | <b>X</b> <sub>1</sub> | <b>X</b> <sub>2</sub> | A'         | B' | Output<br>z |
| i                | 00 | 0             | 0 | 0                     | 0                     | 0          | 0  | 0           |
| i                | 00 | 0             | 0 | 0                     | 1                     | 0          | 1  | 0           |
| i                | 00 | 0             | 0 | 1                     | 0                     | 1          | 0  | 0           |
|                  |    | 0             | 0 | 1                     | 1                     | d          | d  | d           |
| 10               | 01 | 0             | 1 | 0                     | 0                     | 0          | 1  | 0           |
| 10               | 01 | 0             | 1 | 0                     | 1                     | 1          | 0  | 0           |
| 10               | 01 | 0             | 1 | 1                     | 0                     | 0          | 0  | 1           |
|                  |    | 0             | 1 | 1                     | 1                     | d          | d  | d           |
| 20+              | 10 | 1             | 0 | 0                     | 0                     | 1          | 0  | 0           |
| 20+              | 10 | 1             | 0 | 0                     | 1                     | 0          | 0  | 1           |
| 20+              | 10 | 1             | 0 | 1                     | 0                     | 0          | 0  | 1           |
|                  |    | 1             | 0 | 1                     | 1                     | d          | d  | d           |
|                  |    | 1             | 1 | 0                     | 0                     | d          | d  | d           |
|                  |    | 1             | 1 | 0                     | 1                     | d          | d  | d           |
|                  |    | 1             | 1 | 1                     | 0                     | d          | d  | d           |
|                  |    | 1             | 1 | 1                     | 1                     | d          | d  | d           |

| A'       |          | AB |    |    |    |  |  |
|----------|----------|----|----|----|----|--|--|
|          |          | 00 | 01 | 11 | 10 |  |  |
| $x_1x_2$ | 00       |    |    |    |    |  |  |
|          | 01<br>11 |    |    |    |    |  |  |
|          | 11       |    |    |    |    |  |  |
|          | 10       |    |    |    |    |  |  |

| B'       |    | AB |    |    |    |  |  |
|----------|----|----|----|----|----|--|--|
|          |    | 00 | 01 | 11 | 10 |  |  |
| $x_1x_2$ | 00 |    |    |    |    |  |  |
|          | 01 |    |    |    |    |  |  |
|          | 11 |    |    |    |    |  |  |
|          | 10 |    |    |    |    |  |  |

| $\boldsymbol{Z}$ |    | AB          |  |  |  |  |  |
|------------------|----|-------------|--|--|--|--|--|
|                  |    | 00 01 11 10 |  |  |  |  |  |
| $x_1x_2$         | 00 |             |  |  |  |  |  |
|                  | 01 |             |  |  |  |  |  |
|                  | 11 |             |  |  |  |  |  |
|                  | 10 |             |  |  |  |  |  |