1. More on Karnaugh maps

- a. Further example with don't cares and wrapping
 - i. $f_3 = m0 + D2 + D5 + D7 + m8 + m10 = \overline{BD}$

		AB			
		00	01	11	10
CD	00	1\	0	0	1
	01	þ	d	0	90
	11	0	d	0	0
	10	Q)	0	0 (1
					1

- b. Whether or not don't cares are included depends on your desired use case
 - i. Example: whenever we see an illegal input, raise a flag
 - ii. Wouldn't want to include don't cares in this case

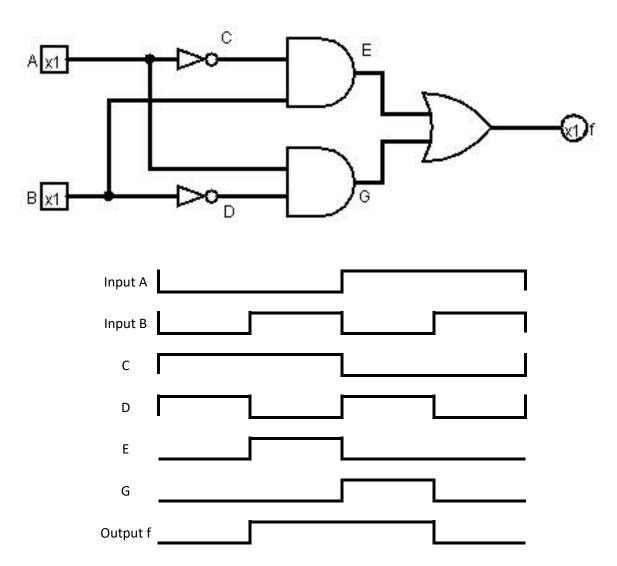
2. Timing

- a. Worst case path
 - i. Route through a circuit that takes the longest
 - 1. "Longest" can be number of gates or time, see below
 - ii. In the example on next page, worst case path is 3 gates
 - 1. Either A -> NOT -> AND -> OR or B -> NOT -> AND -> OR
 - 2. See below for time
 - iii. Worst case path determines clock speed
 - 1. Need to wait for all gates to finish to get output before we start new clock cycle
 - iv. Can also assign times to each type of gate to determine time output is generated
- b. Timing diagram
 - i. Visual representation of truth tables at different parts of a digital logic circuit
 - ii. Initial values of inputs iterate over all possible combinations (like a truth table)
 - iii. Truth values at later points are shown based on each of those combinations
- c. Example
 - i. Implementation of XOR using only AND, OR, NOT on next page

1.
$$A \oplus B = A * ^B + ^A B$$

- ii. Assume that we have the following gate delays
 - 1. NOT = 3 ns
 - 2. AND = 5 ns
 - 3. OR = 4 ns
- iii. What is the clock time of the circuit, if inputs become valid at time 0 ns?
 - 1. A -> NOT -> AND -> OR (other worst case path has identical times)
 - 2. 0 ns + 3 ns + 5 ns + 4 ns = 12 ns

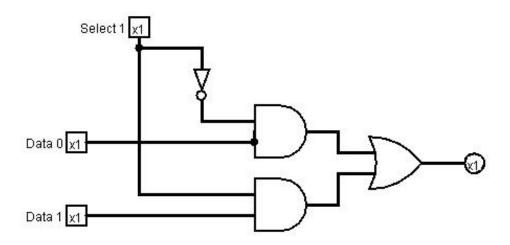




- 3. Combinational circuit building blocks
 - a. Talked about gates so far
 - b. We now move on to other important pieces of digital design
 - c. These pieces build upon the gates that we just learned

4. Multiplexors

- a. Also known as MUXes
- b. MUXes select one output from multiple inputs
 - i. Used to control signal and data routing
- c. For n data inputs, a MUX has $s = \lfloor \log_2 n \rfloor$ select bits that control which input we select
- d. Implementation
 - i. *n* AND gates
 - 1. Each one has one data input
 - 2. Also has s select inputs
 - 3. The select inputs are all true for only one AND gate at a time
 - ii. One OR gate
 - 1. *n* inputs from the AND gates
 - 2. Only one of the AND gates will have a non-zero output (unless that gate's output is all zeroes)
- e. Example
 - i. 2 to 1 MUX



ii. 4 to 1 MUX

