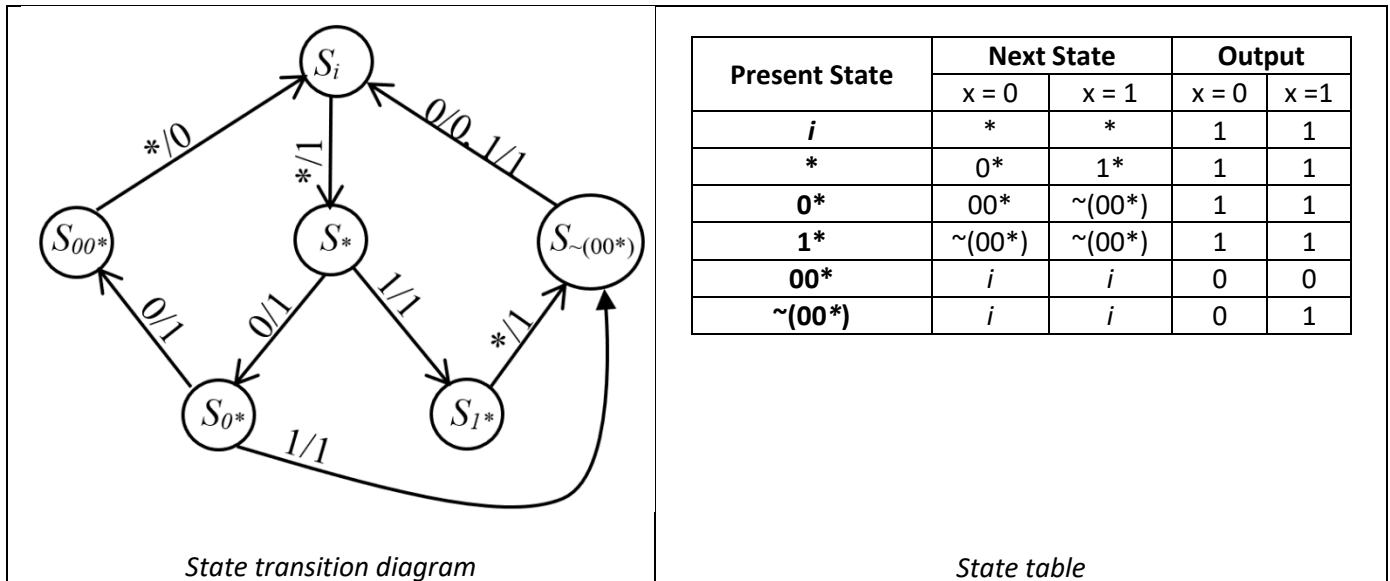


1. Optimal assignment of binary codes
 - a. Was implementing binary code checker last time
 - i. Previous lecture notes contain entire problem from start to finish
 - ii. This section describes the binary code assignment portion we didn't get to in lecture
 - b. Drew naïve implementation of FSM, then minimized it
 - i. Minimized version below



- c. Will need $\lceil \log_2 6 \rceil = 3$ flip flops to represent 6 states
- d. Can assign binary codes for states randomly
 - i. Random assignment works
 - ii. However, careful assignment reduces the combinational logic
- e. Rule of thumb for state binary code assignments
 - i. Try to assign adjacent (Hamming distance of 1) code words to a state and the state that follows it
 - ii. If two states have the same next state, assign those states code words adjacent to next state
 - iii. Creating a K-map helps immensely with this process
 - iv. Initial state *i* will always be all 0s
- f. Assign using the rules above
 - i. Place *i* at 000, will always do this
 - ii. Place * next to *i* at 010 since * is the successor to *i*
 - iii. Place 0* and 1* adjacent to * at 110 and 011 respectively
 - iv. 00* needs to be adjacent to *i* and 0*, which leaves 100 as the only place
 - v. Would like ~(00*) to be adjacent to 0*, 1*, and *i*, but that isn't possible
 1. These are rules of thumb, not fixed laws
 - vi. Can place ~(00*) at 001 to be adjacent to *i* and 1*, though
- g. Note that there may potentially be more than one valid code assignment that minimizes distance

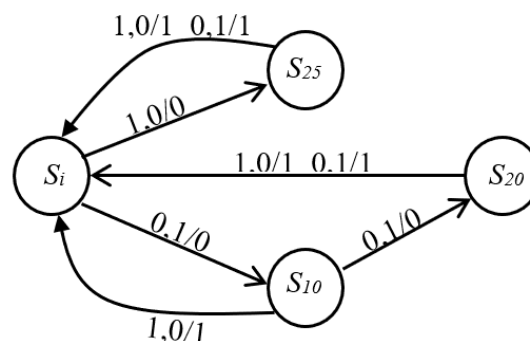
Binary Code		<i>AB</i>			
		00	01	11	10
<i>C</i>	0	<i>i</i>	*	0*	00*
	1	~(00*)	1*		

2. Debugging an FSM

- a. Generally, much more efficient to put in effort to get it right to begin with
 - i. Students tend to jump straight to coding without planning program layout
 - ii. Might work for smaller programs you write for classes... doesn't necessarily work in industry
 - iii. Same idea here—put in time drawing FSM right to begin with, save time later
 - iv. Nothing wrong with drawing a naïve FSM enumerating all states
 1. Once you've got that down, then minimize
 2. Trick is making sure that you draw that naïve FSM right to begin with
- b. One good way of seeing if your FSM you drew was right is to give a stream of inputs into your FSM
 - i. Starting from your initial state i , give inputs and track your progression through your diagram
 - ii. See what states you land at, and if those are what you expect
 - iii. Also see what outputs you get, and if those are what you expect as well
- c. Examples
 - i. With the BCD checker (both naïve and simplified) pass in 4 bit inputs and check output stream
 1. Outputs should be all 1s until you receive 4th bit
 2. On 4th bit, output 0 if input stream is 0-9 when interpreted as binary number
 - ii. With the vending machine below, give a dime, then a dime, then a quarter
 1. Vending machine shouldn't vend before enough money inserted
 2. Change should be appropriate once enough money is inserted into machine

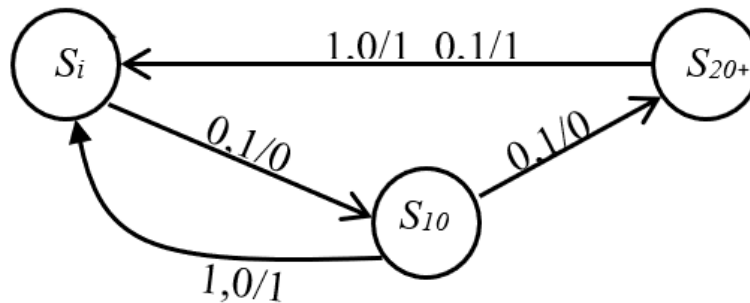
3. More complicated FSMs

- a. Design a vending machine that only takes dimes and quarters
 - i. Merchandise is dispensed ($z = 1$) when the sum of the inputs ≥ 30 cents
 - ii. No coin input results in no impact on machine
 - a. What kind of vending machine eats your money if you don't deposit it fast enough?
 - iii. Machine does not give change, no matter how much extra money gets deposited
- b. $x_1 = \text{quarter}$, $x_2 = \text{dime}$
 - i. Assume that it is not possible to input both quarters and dimes simultaneously
 - ii. Two input, single output
- c. Will use a Mealy model
 - i. Provides for simpler logic in the end
- d. First, create state transition diagram
 - i. Inputs are (x_1, x_2) for (quarter, dime)
 - ii. Input $(0, 0)$ is omitted, would just cause machine to stay in its current state



- e. Next, minimize the number of states using the Partition Minimization Procedure
 - i. $P_1 = (i, 10, 20, 25)$
 - ii. $P_2 = (i) (10) (20, 25)$
 1. 20 and 25 have same k-successors (i for both) so they stay together

- f. Draw new state transition diagram, with new state called 20+



- g. Assign code words next
- $\lceil \log_2 3 \rceil = 2$ flip flops
 - S_i starts in 00
 - No way to place all adjacent states 1 Hamming distance away
 - Do the best we can, though

		A	
		0	1
B	0	i	20+
	1	10	

- h. Next, create state transition table
- Don't have to create state table since this is simple enough
 - Will do the same as BCD checker and add empty rows to the table for don't cares

Present State	Binary Code	Present State		Inputs		Next State		Output z
		A	B	x_1	x_2	A'	B'	
i	00	0	0	0	0	0	0	0
i	00	0	0	0	1	0	1	0
i	00	0	0	1	0	1	0	0
		0	0	1	1	d	d	d
10	01	0	1	0	0	0	1	0
10	01	0	1	0	1	1	0	0
10	01	0	1	1	0	0	0	1
		0	1	1	1	d	d	d
20+	10	1	0	0	0	1	0	0
20+	10	1	0	0	1	0	0	1
20+	10	1	0	1	0	0	0	1
		1	0	1	1	d	d	d
		1	1	0	0	d	d	d
		1	1	0	1	d	d	d
		1	1	1	0	d	d	d
		1	1	1	1	d	d	d

- i. Finally, create K-maps from table above
 - i. Be careful when entering values into K-map!
 1. For example, $(A, B, x_1, x_2) = 0011$ is missing since we can't have $(x_1, x_2) = (1, 1)$
 2. Make those inputs don't cares like normal
 3. We added extra rows to the binary code table
 - a. This way, we know exactly where the don't cares go

A'		AB			
		00	01	11	10
x_1x_2	00	0	0	d	1
	01	0	1	d	0
	11	d	d	d	d
	10	1	0	d	0
$A' = A\bar{x}_1\bar{x}_2 + Bx_2 + \bar{A}\bar{B}x_1$					

B'		AB			
		00	01	11	10
x_1x_2	00	0	1	d	0
	01	1	0	d	0
	11	d	d	d	d
	10	0	0	d	0
$B' = B\bar{x}_1\bar{x}_2 + \bar{A}\bar{B}x_2$					

z		AB			
		00	01	11	10
x_1x_2	00	0	0	d	0
	01	0	0	d	1
	11	d	d	d	d
	10	0	1	d	1
$z = Ax_2 + Bx_1 + Ax_1$					