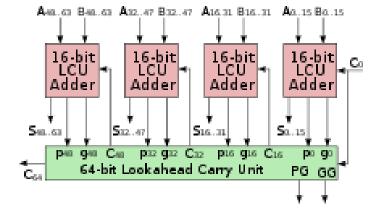
1. More on CLAs

- a. $C_{i+1} = G_i + P_iC_i$, where C is the carry
 - i. $G_i = A_i B_i$, $P_i = A_i \oplus B_i$
 - ii. Can expand this out
 - 1. $C_1 = G_0 + P_0 * C_0$
 - 2. $C_2 = G_1 + P_1 * C_1 = G_1 + P_1 * (G_0 + P_0 * C_0) = G_1 + P_1 * G_0 + P_1 * P_0 * C_0$
 - 3. $C_3 = G_2 + P_2 * C_2 = G_2 + P_2 * (G_1 + P_1 * C_1) = G_2 + P_2 * (G_1 + P_1 * (G_0 + P_0 * C_0))$ = $G_2 + (P_2 * G_1) + (P_2 * P_1 * G_0) + (P_2 * P_1 * P_0 * C_0)$
 - 4. $C_4 = G_3 + P_3 * C_3 = G_3 + P_3 * G_2 + (P_3 * P_2 * G_1) + (P_3 * P_2 * P_1 * G_0) + (P_3 * P_2 * P_1 * P_0 * C_0)$
 - iii. C₀ is the only carry that must be known for all these calculations
 - iv. All of these expressions can be implemented with two levels of gates
 - 1. Longest path could always be two gates
 - 2. However, more inputs in an AND gate means it takes longer for the gate to resolve, as there are more transistors in series
 - 3. For more than 7 inputs, binary tree of AND gates could be faster, even though path is longer

b. Process

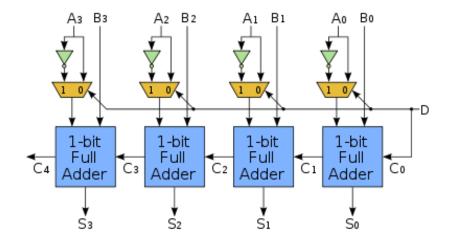
- i. Each bit adder i calculates its Pi and Gi
 - 1. Takes one gate delay
- ii. CLA unit simultaneously calculates all carry for its adders
 - 1. Takes two gate delays
 - 2. Also calculates the carry for the next group of adders (C₄ in the picture above)
- iii. With the calculated carries, each bit-adder in the group simultaneously calculates its sums
 - 1. Only takes one gate delay, as carry and the XOR was already calculated for $P = A_i \oplus B_i$
- c. Can expand this 4-bit adder to further levels, like a 64-bit unit





2. Subtractors

- a. Create the 2's complement of the number to be subtracted
 - i. Then add to other number
- b. Circuit below allows for that
 - i. When wanting to subtract, D is set to 1
 - ii. Multiplexers invert the entire number
 - iii. Add one by setting carry in C₀ to 1



3. Comparators

- a. See if two binary numbers are equal, output a 1 if true, 0 otherwise
- b. For an n bit comparison, use n 2-bit XNOR gates to compare if digits are equal
 - i. XNOR outputs a 1 if both are equal
- c. AND the results of all XNORs together to get final answer
- d. Example: 2 bit comparator

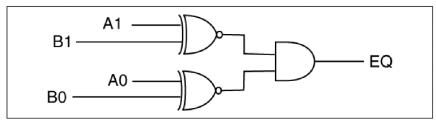


Figure 11.10: The final circuit for the 2-bit comparator as equation (e) in Figure 11.9.

4. Arithmetic logic unit (ALU)

- e. One unit that can perform multiple operations
 - i. Example: do ADD, NOT, AND, OR, XOR, equality check, so forth
- f. Each cell of the ALU has one of each type of gate in it
 - i. Performs operation on corresponding bits
 - ii. Use MUX to select which operation is chosen
 - iii. Control/select bits determine what operation is done
 - iv. Perform all operations at all time, discard results of operations not done
 - 1. Sounds wasteful, but it's cheaper to discard the results than attempt to disable/enable the unused pieces



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- 5. Error detection and correction
 - a. Error types
 - i. Hard failure permanent physical defect
 - ii. Soft error random non-destructive event that causes an error
 - 2. Example voltage spike
 - 3. Mario 64 upwarp glitch thought to be a soft error (bit flip)
 - iii. More common now that components are smaller
 - b. Will focus on errors that involve bits changing value
 - c. Measure of size of error Hamming distance between original and final values
 - d. Three possible outcomes
 - i. No errors detected
 - ii. Error detected, and location specified, so we can correct it
 - iii. Error detected, and location unspecified, so we can't correct it
 - e. Will look at SECDED Single Error Correction Double Error Detection
 - i. If the number of bits changed in a set is large enough, any error detection system will fail

