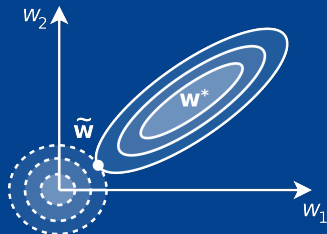


MACHINE LEARNING

LESSON 7: Optimization and Searching

CARSTEN EIE FRIGAARD
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L07: Optimization and Searching

Agenda

- ▶ BB | Hand-ins Deadlines | [Selected J1 hand-ins](#)
- ▶ GPU Cluster via EDUROAM or VPN/au-access (lost port 22)
- ▶ Break-out session 15:00: on J1 or Linear Algebra?
- ▶ J3: as journal or poster+session?
- ▶ Regularization and Optimization
 - Preprocessing of data (no-exe),
 - Optimizers (no-exe),
 - Regularizers,
 - Exercise: [L07/regulizers.ipynb](#)
- ▶ Searching
 - Model selection and model searching (no-exe),
 - Gridsearch,
 - Randomsearch,
 - Exercise: [L07/gridsearch.ipynb](#)

Preprocessing of Data

Scaling, Standardization, Normalization...

Why the need for preprocessing?

*Standardization of datasets is a **common requirement for many machine learning estimators** [..]; they might **behave badly** if the individual features do not more or less look like standard normally distributed data. [..]*

[<https://scikit-learn.org/stable/modules/preprocessing.html>]

Standardization of a feature vector \mathbf{x} , giving \mathbf{x}' mean zero, and standard deviation one

$$\mathbf{x}' = \frac{\mathbf{x} - \mu_{\mathbf{x}}}{\sigma_{\mathbf{x}}}$$

What kind of estimators needs standardization?

→ **Neural networks (NNs) in particular!**

Regularization and optimization:

→ **WARM-UP** for the coming use of NNs!

Preprocessing of Data

Scaling, Standardization, Normalization...

Common preprocessing methods

- ▶ standardization, aka mean/std scaling, $\frac{x-\mu}{\sigma}$
`sklearn.preprocessing.StandardScaler`
- ▶ min/max, or abs scaling, say $x \in [0; 1]$
`sklearn.preprocessing.MinMaxScaler`
`sklearn.preprocessing.MaxAbsScaler`
- ▶ normalization, giving unit norm
`sklearn.preprocessing.normalize`

Potential problems:

- ▶ outliers,
- ▶ NaNs (Not-a-Number)

Preprocessing of Data

Scaling, Standardization, Normalization in a Pipeline

Use preprocessing as first state in a fit-predict **pipeline**

```
1  from sklearn.preprocessing import StandardScaler
2  from sklearn.pipeline import make_pipeline
3  from sklearn.naive_bayes import GaussianNB
4
5  mypipeline = make_pipeline(
6      StandardScaler(),
7      GaussianNB()
8  )
9
10 ..
11 mypipeline.fit(X_train, y_train)
12 ..
13 mypipeline.predict(X_test)
```

[[GITMAL],L07/Extra/standardization_demo.ipynb]

Remember: scale train and test equally!

Regularization

Adding a Penalty to the Cost Function

For a linear regressor, our cost function was

$$J(\mathbf{X}, \mathbf{y}; \mathbf{w}) = ||\mathbf{X}\mathbf{w} - \mathbf{y}||_2^2 \propto \text{MSE}(\mathbf{X}, \mathbf{y}; \mathbf{w})$$

But now enters a **penalty factor**, Ω , that scaled with α adds extra cost to J ,

$$\tilde{J}(\mathbf{X}, \mathbf{y}; \mathbf{w}) = ||\mathbf{X}\mathbf{w} - \mathbf{y}||_2^2 + \alpha\Omega(\mathbf{w})$$

so this becomes **a-tug-of-war** between the two terms in \tilde{J} .

The effect of the added penalty is to:

- ▶ put a **constraint** on the norm of the weights, \mathbf{w} , disallowing 'em to grow wildly,
- ▶ leading to **reduced overfitting**, disabling the model to learn the background noise in the data.

\mathcal{L}_2 Regularization

Ridge Penalisation

Aka Weight Decay, aka Tikhonov regularization

$$\Omega(\mathbf{w}) = \|\mathbf{w}\|_2^2 = \mathbf{w}^\top \mathbf{w}$$

$$\tilde{J}_{\text{ridge}}(\mathbf{X}, \mathbf{y}; \mathbf{w}) = J(\mathbf{X}, \mathbf{y}; \mathbf{w}) + \alpha \mathbf{w}^\top \mathbf{w}$$

with $\mathbf{w} = [w_1 \ w_2 \ \cdots \ w_n]^\top$ without the bias element w_0 in the regularizer term, Ω , and recalling the Euclidean norm

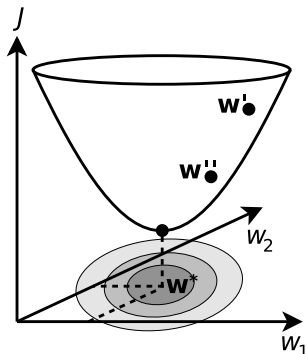
$$\mathcal{L}_2^2 : \|\mathbf{x}\|_2^2 = \mathbf{x}^\top \mathbf{x}$$

and give-or-take some additional $1/2$ or $1/n$ constant, that we do not care about.

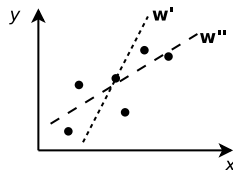
\mathcal{L}_2 Regularization

Ridge Penalization

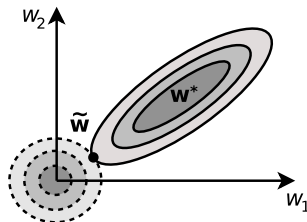
A graphical view for a linear regressor



3D: ideal convex loss in $J - \mathbf{w}$ space.



2D $y - x$ space,
here only 1D shown.



2D: flat $w_2 - w_1$ view with
some feature scaling.

The-tug-of-war: what happens with $\tilde{\mathbf{w}}$,
if \mathbf{w}^* is far from the origin $[w_1, w_2] = (0, 0)$?

\mathcal{L}_1 Regularization

Lasso penalization

Now, just replace the \mathcal{L}_2 with \mathcal{L}_1 and we have the Lasso regularizer

$$\Omega(\mathbf{w}) = \|\mathbf{w}\|_1$$

$$\tilde{J}_{\text{lasso}}(\mathbf{X}, \mathbf{y}; \mathbf{w}) = J(\mathbf{X}, \mathbf{y}; \mathbf{w}) + \alpha \|\mathbf{w}\|_1$$

with the Manhattan norm

$$\mathcal{L}_1 : \|\mathbf{x}\|_1 = \sum_{i=1}^n \text{abs}(x_i)$$

\mathcal{L}_1 and \mathcal{L}_2 Regularization

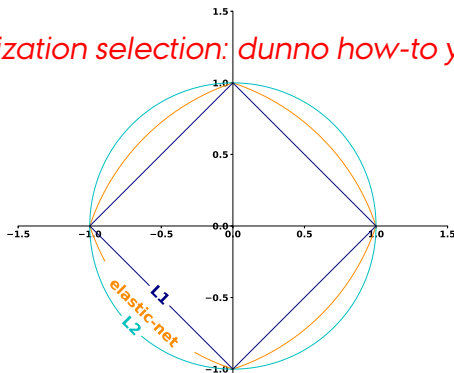
Elastic-net Penalisation

And finally a combination of the two: an Elastic-net regularizer

$$\Omega(\mathbf{w}) = \beta \|\mathbf{w}\|_1 + (1 - \beta) \|\mathbf{w}\|_2^2$$

$$\tilde{J}_{\text{elastic}}(\mathbf{X}, \mathbf{y}; \mathbf{w}) = J(\mathbf{X}, \mathbf{y}; \mathbf{w}) + \alpha (\beta \|\mathbf{w}\|_1 + (1 - \beta) \|\mathbf{w}\|_2^2)$$

Regularization selection: dunno how-to yet!??



Optimizers

Momentum Optimization

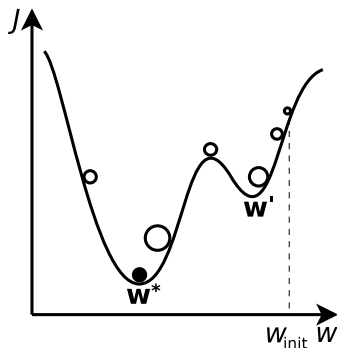
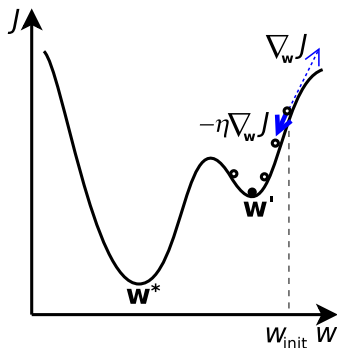
Normal GD algo

$$\mathbf{w} \leftarrow \mathbf{w} - \eta \nabla_{\mathbf{w}} J$$

but now with added (physical) momentum

$$\mathbf{m} \leftarrow \beta \mathbf{m} - \eta \nabla_{\mathbf{w}} J$$

$$\mathbf{w} \leftarrow \mathbf{w} - \mathbf{m}$$



ML Models

Models encountered so far

Some classifiers and regressors..

```
sklearn.neighbors.KNeighborsRegressor  
sklearn.linear_model.LinearRegression  
sklearn.linear_model.SGDClassifier  
sklearn.linear_model.SGDRegressor
```

Perhaps...

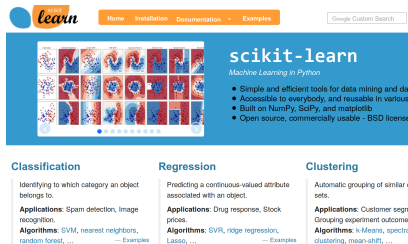
```
sklearn.naive_bayes.GaussianNB  
sklearn.naive_bayes.MultinomialNB
```

Not really or not in depth

```
sklearn.linear_model.Perceptron  
sklearn.linear_model.LogisticRegression  
sklearn.svm.SVC  
sklearn.svm.SVR  
sklearn.neural_network.MLPClassifier  
sklearn.neural_network.MLPRegressor
```

Or even more exotic models like..

- ▶ supervised ensemble: AdaBoost, Bagging, DecisionTree, RandomForest,...
- ▶ semi-supervised: ??
- ▶ unsupervised: K-means, manifolds, restricted Boltzmann machines,...
- ▶ clustering: K-means



The screenshot shows the scikit-learn website. At the top, there's a navigation bar with links: Home, Installation, Documentation, and Examples. A Google Custom Search bar is on the right. The main header features the scikit-learn logo and the tagline "Machine Learning in Python". Below this, a grid of 12 small images shows various machine learning visualizations. To the right of the grid, a list of bullet points highlights key features: "Simple and efficient tools for data mining and data analysis", "Accessible to everybody, and reusable in various contexts", "Built on NumPy, SciPy, and matplotlib", and "Open source, commercially usable - BSD license". The page is divided into three columns: "Classification", "Regression", and "Clustering". Each column contains a brief description, applications, and algorithms. For example, the "Classification" column describes identifying object categories, lists applications like spam detection and image recognition, and mentions algorithms like SVM, nearest neighbors, and random forest. The "Regression" column describes predicting continuous-valued attributes, lists applications like drug response and stock prices, and mentions algorithms like SVR, ridge regression, and Lasso. The "Clustering" column describes automatic grouping of similar sets, lists applications like customer segmentation and grouping experiment outcomes, and mentions algorithms like k-means, spectral clustering, and mean-shift.



ML Model Selection and Searching

What ML model to choose?

Model selection

► manual:

model characteristics, \mathcal{O} complexity, etc.
browsing through Scikit-learn documentation,
...and also based on data assumptions.

► semi-automatic:

model search, and fun with python!

```
1 models = {  
2     SVC(gamma="scale"),  
3     SGDClassifier(tol=1e-3, eta0=0.1),  
4     GaussianNB()  
5 }  
6  
7 for i in models:  
8     i.fit(X_train, y_train)  
9     y_pred_test = i.predict(X_test)  
10    p = precision_score(y_test, y_pred_test, average='micro')  
11    print(f'{type(i).__name__:13s}: precision={p:0.2f}')
```

prints..

GaussianNB:	p=1.00
SGDClassifier:	p=0.93
SVC:	p=0.98

NOTE: Python dictionary= {a:x, b:y}

Grid Search

The hyperparameter-set for SGD linear regressor

```
1 class sklearn.linear_model.SGDRegressor(  
2     loss      = 'squared_loss', penalty      = 'l2',  
3     alpha     = 0.0001,               l1_ratio    = 0.15,  
4     tol       = None,                 shuffle     = True,  
5     verbose   = 0,                   epsilon     = 0.1,  
6     eta0      = 0.01,                power_t     = 0.25,  
7     n_iter_no_change=5,              warm_start  = False,  
8     fit_intercept = True,            max_iter    = None,  
9     average     = False,            n_iter      = None  
10    random_state  = None,            learning_rate='invscaling',  
11    early_stopping=False,           validation_fraction=0.1  
12 )
```



Search best hyperparameters in a (smaller) set, say

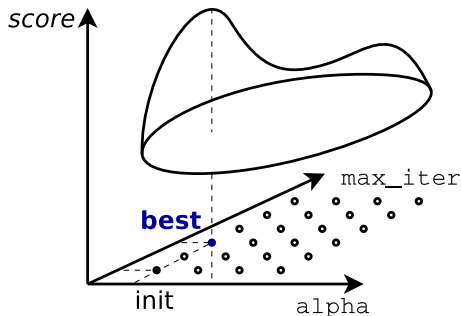
```
1 model = SGDClassifier()  
2 tuning_parameters = {  
3     'alpha': [ 0.001, 0.01, 0.1],  
4     'max_iter': [1, 10, 100, 100],  
5     'learning_rate': ('constant', 'optimal', 'invscaling', 'adaptive')  
6 }  
7 ..  
8 grid_tuned = GridSearchCV(model, tuning_parameters, ..
```

Grid Search

How to set hyperparameters optimally?

Gridsearch seen in 3D for the two hyperspace dimensions:

- ▶ $\alpha \in [1, 2, 3..]$ (NOTE: linear range for this plot only!),
- ▶ $\text{learnig_rate} \in [1, 2, 3..]$



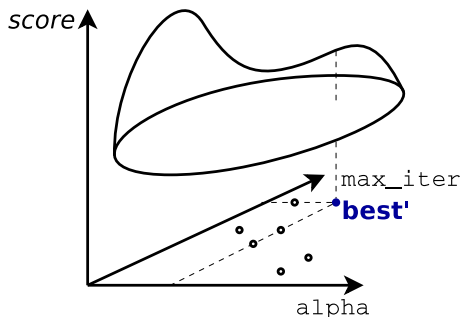
But, what if there are many hyperparameters and many combinations? → Zzzzzzz!

Randomized Search

How to set hyperparameters faster but less optimally?

Replace `GridSearchCV()` with

`RandomizedSearchCV(n_iter=100,...)`



Faster, but will not yield the optimal score maximum,
...but does it matter in a huge hyperparameter search-space?