## Università degli Studi di Napoli Federico II Dipartimento di Ingegneria Elettrica e delle Tecnologie dell'Informazione



## Parallel and Distributed Computing submissions

Giuliano Aiello

2024

# Contents

1	Prolusion			
	1.1	Goal	1	
	1.2	Environment	1	
	1.3	Project directory layout	2	
	1.4	Build	3	
		1.4.1 Libraries	3	
		1.4.2 Xcode	3	
	1.5	Run	4	
		1.5.1 Network Requirement	4	
2	Max	asum	5	
	2.1	Problem at a glance	5	
	2.2	Algorithm	5	
		2.2.1 Parallelization	5	
		2.2.2 Pseudocode	5	
		2.2.3 Performance Analysis	7	
3	Lap	lace	11	
	3.1	Problem at a glance	11	
	3.2	Algorithm	11	
	_	3.2.1 Parallelization	11	
		3.2.2 Pseudocode	11	
4	MatMatThread			
	4.1	Problem at a glance	13	
	4.2	Algorithm	13	
		4.2.1 Parallelization	13	
		4.2.2 Pseudocode	13	
5	Fur	ther Algorithms	15	
Acronyms			19	

iv CONTENTS

# **Prolusion**

### 1.1 Goal

A comprehensive overview of a Parallel and Distributed Computing project developed in C is presented. The project consists of multiple modules delivered in incremental phases. Every algorithm is implemented within the **Single Program Multiple Data** parallel model.

This report is not intended as a user guide, but rather aims to describe the project's exploration of Parallel and Distributed Computing techniques, leveraging High Performance Computing in certain instances.

### 1.2 Environment

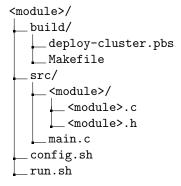
The project was entirely developed on macOS with the help of Xcode IDE. Naturally, this will mainly impact the build process.

## 1.3 Project directory layout

The structure of the project's root directory is outlined below.

common package serves as a library of utility functions designed to support and be reused by various modules across the project.

The remaining directories represent the individual project modules, which constitute the deliverables of the project. Within each module, the directory structure follows a standard format:



Most parts of the main.c files are provided by the project supervisor.

1.4. BUILD 3

#### 1.4 Build

The project was primarily compiled using the Clang compiler.

The build process was carried out either through the Makefile (some of which support compilers other than Clang) or via Xcode.

Regardless of the build process, every module of the project was compiled with:

 $\bullet\,$  -03 optimization flag to maximize performance.

#### 1.4.1 Libraries

The following are the dynamically linked libraries integrated into the project.

- math.h
- mpi.h
- omp.h
- stdio.h
- stdbool.h
- stdlib.h
- sys/time.h
- unistd.h

#### 1.4.2 Xcode

When it came to build with the Xcode, the development process adhered to the workflow and conventions defined by the chosen IDE, leveraging its built-in tools and features to organize and manage the project. Particularly, this includes:

- Xcode targets
- Xcode schemes
- Xcode .entitlements file

### 1.5 Run

## 1.5.1 Network Requirement

Running an MPI module with no internet connection, makes the following error occur:

[Giulianos-MacBook-Pro.local:05355] ptl\_tool: problems getting address for index 0 (kernel index -1)

\_\_\_\_\_\_

The PMIx server's listener thread failed to start. We cannot continue.

-----

Program ended with exit code: 213

## Maxsum

### 2.1 Problem at a glance

Given a matrix, the objective is to identify the row with the maximum squared root sum.

### 2.2 Algorithm

#### 2.2.1 Parallelization

The algorithm employs a multithreaded approach, each thread can compute indipendently its local maximum squared root sum. Once a thread has completed its task, a synchronization is needed with the other threads in order to determine the overall maximum squared root sum.

#### 2.2.2 Pseudocode

#### Input:

- global matrix
- number of thread(s) for parallel execution

#### Steps:

- 1. Compute the indices of the global matrix corresponding to the local matrix of the thread.
- $2. \ \,$  Compute the local maximum squared root sum.
- 3. Perform a thread-safe update of the overall maximum squared root sum variable.

#### Algorithm 1: Maxsum

```
Input: matrix, numThreads
Output: maxSumOverall

STARTTHREADS (numThreads)

startRow \leftarrow getStartingRowIndex(threadRank)
endRow \leftarrow getEndingRowIndex(threadRank)

for currRow \leftarrow startRow to endRow do

currSum \leftarrow squareRootSum(currRow)

if currSum > maxSum then

maxSum \leftarrow currSum

end

CRITICAL

if maxSumOverall < maxSum then

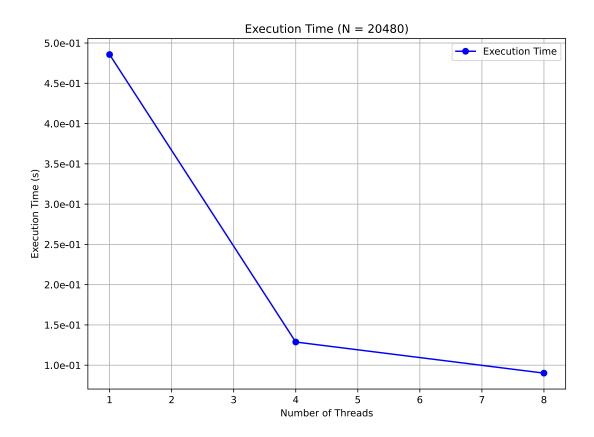
maxSumOverall \leftarrow maxSum

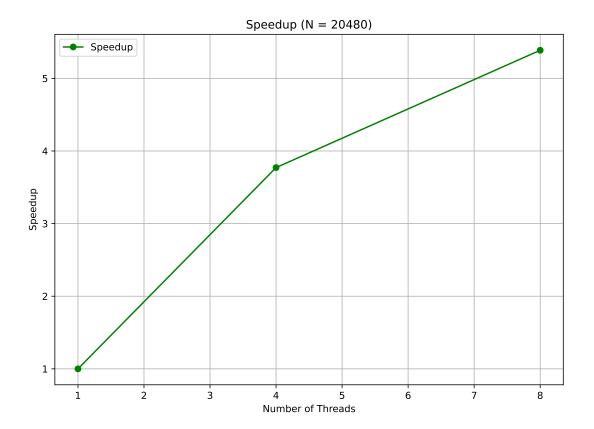
end

end
```

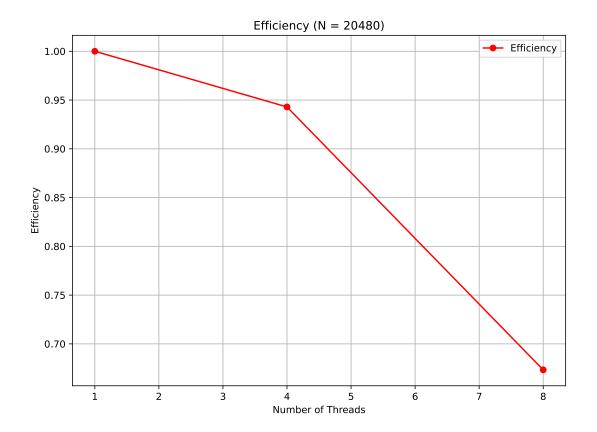
2.2. ALGORITHM 7

## 2.2.3 Performance Analysis





2.2. ALGORITHM 9



# Laplace

### 3.1 Problem at a glance

Given a matrix and a number of iterations, the objective is to compute the discrete Laplacian of the matrix over the specified iterations.

### 3.2 Algorithm

#### 3.2.1 Parallelization

The algorithm employs a multiprocess approach. A synchronization between processes is needed from the outset.

The global matrix is distributed among the processes, harnessing the advantages of parallelism, representing a spatial advantage other than a temporal one.

#### 3.2.2 Pseudocode

#### Input:

- local process matrix
- number of iteration(s)

#### Steps:

For each iteration:

- 1. If  $P_i \neq P_1$  Then
  - (a) Send to  $P_{i-1}$  the local first row
  - (b) Receive from  $P_{i-1}$  its last row
- 2. If  $P_i \neq P_n$  Then
  - (a) Receive from  $P_{i+1}$  its first row
  - (b) Send to  $P_{i+1}$  the local last row
- 3. Compute the Laplacian considering only the local inner matrix, the matrix boundaries are left out.

- 4. If  $P_i \neq P_1$ 
  - (a) Compute the Laplacian considering only the local top row, with the auxiliary last row from the previous process.
- 5. If  $P_i \neq P_n$ 
  - (a) Compute the Laplacian considering only the local bottom row, with the auxiliary first row from the next process.

An auxiliary matrix is involved to facilitate the computation.

#### Algorithm 2: Laplace

```
Input: matrix, iterations
Output: matrix

for iter \leftarrow 1 to iterations do

if P_i \neq P_1 then

SEND(P_{i-1}, localFirstRow)
RECV(P_{i-1}, receivedLastRow)
end

if P_i \neq P_n then

RECV(P_{i+1}, receivedFirstRow)
SEND(P_{i+1}, localLastRow)
end

laplacian(inner(matrix))

if P_i \neq P_1 then

| laplacian(matrix, receivedLastRow)
end

if P_i \neq P_n then

| laplacian(matrix, receivedLastRow)
end

if P_i \neq P_n then

| laplacian(matrix, receivedFirstRow)
end

end

end
```

# MatMatThread

## 4.1 Problem at a glance

Given matrices A, B, C, the goal is to perform a multithreaded MatMatBlock algorithm to compute C = C + AB.

- 4.2 Algorithm
- 4.2.1 Parallelization
- 4.2.2 Pseudocode

# Further Algorithms

The project includes additional modules not part of the presented submissions, such as two parallel summation algorithms: **Ringsum** and **Cascadesum**.

The latter is more efficient with respect to time complexity, requiring only  $\log_2(P)$  steps for message passing, as opposed to P-1, where P denotes the number of processes involved.

# Acronyms

 ${f HPC}$  High Performance Computing 1

 ${\bf IDE}$  Integrated Development Environment 1, 3

 $\mathbf{MPI}\,$  Message Passing Interface 4

 ${\bf PDC}\,$  Parallel and Distributed Computing 1

 ${\bf SPMD}\,$  Single Program Multiple Data 1