Squashed c x let a library writer provide *x* in "*c*-irrelevant" way to a library user.

```
newtype Squashed c x = Squash { getSquashed :: \forall r.c \ r \Rightarrow (x \rightarrow r) \rightarrow r }
```

Squashed is almost like *Cont*¹ or *Codensity* ², so *Squashed* is a *Monad*:

```
instance Monad (Squashed c) where return x = Squash ($x) m \gg k = Squash $ \lambda bx \rightarrow getSquashed m $ \lambda a \rightarrow getSquashed (k a) bx instance Applicative (Squashed c) where pure = return liftA2 = liftM2 instance Functor (Squashed c) where fmap = liftM
```

Monad-instance allows to work on the wrapped value, for example

```
squashedTree' :: Squashed Monoid (Tree String)
squashedTree' = pure Node "x" [pure "yz", pure "foo"]
squashedTree :: Squashed Monoid (Tree Int)
squashedTree = \mathbf{do}
x \leftarrow \text{squashedTree'}
return (fmap length x)
```

However, we cannot *extract* the original value, only as much as the constraint let us:

```
-- 6
example_1 :: Int
example_1 = getSum (getSquashed squashedTree (foldMap Sum))
-- [1,2,3]
example_2 :: [Int]
example_2 = getSquashed squashedTree (foldMap pure)
```

This restriction maybe be useful to enforce correctness, without relying on the module system! Squash c x is a generalised notion of "free c over x", e.g. Monoid as described in Free Monoids in Haskell³. It should be possible to write c (Squashed c x) instances for all (reasonable) c. Or actually ($\forall x.c' \ x \Rightarrow c \ x$) $\Rightarrow c$ (Squashed c' a) after Quantified Constraints -proposal⁴ is implemented. (TODO: amend when we have the extension in released GHC).

```
instance Semigroup (Squashed Semigroup x) where a \diamond b = Squash \$ \lambda k \rightarrow getSquashed a <math>k \diamond getSquashed b k instance Monoid (Squashed Monoid x) where mempty = Squash \$ \lambda_- \rightarrow mempty mappend a b = Squash \$ \lambda k \rightarrow getSquashed a k'mappend' getSquashed b k
```

As with Singleton containers⁵, tell me if you have seen this construction in the wild! *Addendum*: As Iceland_jack pointed on Twitter⁶⁷there is a free-functors⁸ package on Hackage, and more is written about *Squash*:

```
1https://hackage.haskell.org/package/transformers-0.5.5.0/docs/Control-Monad-Trans-Cont.html#t:ContT
2http://hackage.haskell.org/package/kan-extensions-5.1/docs/Control-Monad-Codensity.html#t:Codensity
3http://comonad.com/reader/2015/free-monoids-in-haskell/
4https://github.com/ghc-proposals/ghc-proposals/blob/master/proposals/0018-quantified-constraints.rst
5http://oleg.fi/gists/posts/2018-05-12-singleton-container.html
6https://twitter.com/Iceland_jack/status/1001081879045525504
7https://twitter.com/Iceland_jack/status/1001083326965407745
8https://hackage.haskell.org/package/free-functors
```

- http://comonad.com/reader/2015/domains-sets-traversals-and-applicatives/
- https://www.cs.ox.ac.uk/ralf.hinze/Kan.pdf

Note, that Squash doesn't let us turn a thing into something it isn't...

```
newtype Squashed1 \ c \ f \ x = Squash1
         \{getSquashed1 :: \forall g.c \ g \Rightarrow (\forall y.f \ y \rightarrow g \ y) \rightarrow g \ x\}
      squash1:: f x \rightarrow Squashed1 c f x
      squash1 fx = Squash1 (\$fx)
      instance Monad (Squashed1 Monad f) where
         return \ x = Squash1 \ \$ \ \lambda_- \rightarrow return \ x
         m \gg k = Squash1 \$ \lambda f \rightarrow
            getSquashed1 \ m \ f \gg \lambda y \rightarrow
            getSquashed1 (k y) f
      instance Applicative (Squashed1 Monad f) where
         pure = return
         liftA2 = liftM2
       instance Functor (Squashed1 Monad f) where
         fmap = liftM
... though we can foolishly think so:
      intSet' :: Squashed1 Monad Set Int
      intSet' = squash1 $ Set.fromList [1,2,3]
      intSet :: Squashed1 Monad Set Int
      intSet = intSet' \gg \lambda_{-} \rightarrow return 5
         -- [5,5,5]
      intList :: [Int]
```

So Squash let's only forget, not to "remember" anything new.

intList = getSquashed1 intSet Set.toList

By the way, this post is genuine Literate Haskell file, using LaTeX, not Markdown. If interested on how, check the gists repository⁹. I'm weird, as after some point of markup complexity, I actually prefer LaTeX.

 $^{^{9} \}verb|https://github.com/phadej/gists|$