

PROGRAMMING IN HASKELL⁰



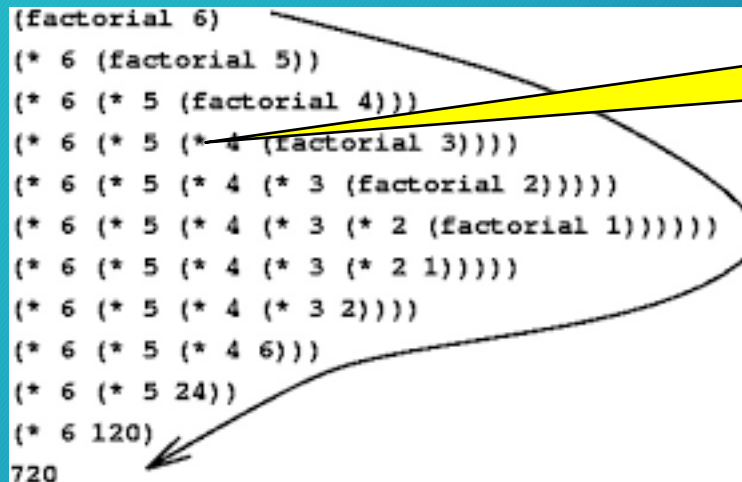
Chapter 6.2 - Tail Recursion

Recursion – why we need tail recursion

1

```
factRec :: Int -> Int
factRec 0 = 1
factRec n = n*factRec (n-1)
```

```
{factorial 6}
(* 6 (factorial 5))
(* 6 (* 5 (factorial 4)))
(* 6 (* 5 (* 4 (factorial 3)))
(* 6 (* 5 (* 4 (* 3 (factorial 2))))
(* 6 (* 5 (* 4 (* 3 (* 2 (factorial 1)))))
(* 6 (* 5 (* 4 (* 3 (* 2 1))))
(* 6 (* 5 (* 4 (* 3 2)))
(* 6 (* 5 (* 4 6)))
(* 6 (* 5 24))
(* 6 120)
720
```



Pending
'multiply's

This is expensive and prone to stack overflows..

Tail recursion

2

- In tail recursion, the information that needs to be stored on the call stack is much smaller
- We use the base case in such a way that once it is called, the work is done (no pending operations)
- We use a helper function that in turn uses an accumulator

Example 1 – tail recursion

3

```
factTailRec :: Int -> Int
factTailRec n = helper n 1 where
    helper 1 acc = acc
    helper x acc = helper (x-1) (acc*x)
```

```
factTailRec 4
```

```
= helper 4 1
```

```
= helper 3 (4*1)
```

```
= helper 2 (3 * 4)
```

```
= helper 1 (2 * 12)
```

```
= 24
```

General template

4

Some updated
value

```
foo :: Int -> Int
foo x = foohelper x initial solution
where foohelper
      | base case = solution (based on accum)
      | otherwise = fooHelper (n-1) (updated accum)
```


Example 2 – tail recursion

5

```
sumInts :: [Int] -> Int
sumInts [] = 0
sumInts (n:ns) = n + sumInts ns
```

e.g. `sumInts [1,3,5] = 9`

We will rewrite this using tail recursion.

Exercise: Convince yourself that it is not currently tail recursive

Example 2 – tail recursion

6

```
sumIntsTail :: [Int] -> Int
sumIntsTail ns = helper ns 0 where
  helper [] acc = acc
  helper (n:ns) acc = helper ns (acc + n)
```

sumIntsTail [1,3,5]

= helper [1,3,5] 0

= helper [3,5] (1+0)

= helper [5] (3+1)

= helper [] (5+4)

= 9

Example 3 – tail recursion

myAdd takes two integers and returns their sum.
Note : we can only use +1 and -1

```
myAdd :: Int -> Int -> Int
myAdd x 0 = x
myAdd 0 y = y
myAdd x y = myAdd (x-1) (y+1)
```

Is this tail recursive?

Example 3 – tail recursion

8

```
myAdd :: Int -> Int -> Int
myAdd x 0 = x
myAdd 0 y = y
myAdd x y = myAdd (x-1) (y+1)
```

Is this tail recursive?

```
myAdd 3 4
= myAdd 2 5
= myAdd 1 6
= myAdd 0 7 = 7
```

No pending
ops after base
case is called

This is tail
recursive

