

# PROGRAMMING IN HASKELL<sup>0</sup>



Chapter 6.2 - Tail Recursion

# Recursion – why we need tail recursion

1

```
factRec :: Int -> Int
factRec 0 = 1
factRec n = n*factRec (n-1)
```

```
(factorial 6)
(* 6 (factorial 5))
(* 6 (* 5 (factorial 4)))
(* 6 (* 5 (* 4 (factorial 3))))
(* 6 (* 5 (* 4 (* 3 (factorial 2)))))
(* 6 (* 5 (* 4 (* 3 (* 2 (factorial 1))))))
(* 6 (* 5 (* 4 (* 3 (* 2 1))))))
(* 6 (* 5 (* 4 (* 3 2))))
(* 6 (* 5 24))
(* 6 120)
720
```

Pending  
'multiply's

This is expensive and prone to stack overflows..

# Tail recursion

2

- In tail recursion, the information that needs to be stored on the call stack is much smaller
- We use the base case in such a way that once it is called, the work is done (no pending operations)
- We use a helper function that in turn uses an accumulator

## Example 1 – tail recursion

```
factTailRec :: Int -> Int
factTailRec n = helper n 1 where
    helper 1 acc = acc
    helper x acc = helper (x-1) (acc*x)
```

factTailRec 4

$$= \text{helper } 4 \ 1$$

$$= \text{helper } 3 \ (4 * 1)$$

$$= \text{helper } 2 \ (3 * 4)$$

$$= \text{helper } 1 \ (2 * 12)$$

$$= 24$$

## General template

Some updated  
value

```
foo :: Int -> Int
foo x = foohelper x initial solution
where foohelper
      | base case = solution (based on accum)
      | otherwise = fooHelper (n-1) (updated accum)
```

## Example 2 – tail recursion

5

```
sumInts :: [Int] -> Int
sumInts [] = 0
sumInts (n:ns) = n + sumInts ns
```

e.g. sumInts [1,3,5] = 9

We will rewrite this using tail recursion.

**Exercise:** Convince yourself that it is not currently tail recursive

## Example 2 – tail recursion

```
sumIntsTail :: [Int] -> Int
sumIntsTail ns = helper ns 0 where
    helper [] acc = acc
    helper (n:ns) acc = helper ns (acc + n)
```

sumIntsTail [1,3,5]

= helper [1,3,5] 0

= helper [3,5] (1+0)

= helper [5] (3+1)

= helper [] (5+4)

= 9

## Example 3 – tail recursion

myAdd takes two integers and returns their sum.  
Note : we can only use +1 and -1

```
myAdd :: Int -> Int -> Int  
myAdd x 0 = x  
myAdd 0 y = y  
myAdd x y = myAdd (x-1) (y+1)
```

Is this tail recursive?

# Example 3 – tail recursion

`myAdd :: Int -> Int -> Int`

`myAdd x 0 = x`

`myAdd 0 y = y`

`myAdd x y = myAdd (x-1) (y+1)`

No pending  
ops after base  
case is called

Is this tail recursive?

`myAdd 3 4`

`= myAdd 2 5`

`= myAdd 1 6`

`= myAdd 0 7`

`= 7`

This is tail  
recursive

