

exercises

Functors and I/O

Exercise 1:

Give a definition of the function

```
fmap :: (a-> b) -> IO a -> IO b
```

the effect of which is to transform an interaction by applying the function to its result. You should define it using the

do

construct.

Solution 1:

```
fmap :: (a-> b) -> IO a -> IO b
```

```
fmap f m  
= do x <- m  
     return (f x)
```

Exercise 2:

Define the function

```
repeat :: IO Bool -> IO () -> IO ()
```

so that

```
repeat test oper
```

has the effect of repeating *oper* until the condition *test* is *True*.

Solution 2:

```
repeat :: IO Bool -> IO () -> IO ()
```

```
repeat test m  
= do res <- test  
     if res  
         then return ()  
     else do m  
             repeat test m
```

Exercise 3:

Define the higher-order function ***whileG*** in which the condition and the operation work over values of type ***a***. Its type should be:

whileG :: (***a*** → **IO Bool**) → (***a*** → **IO a**) → (***a*** → **IO a**)

so that

whileG cond op x

has the effect of repeating ***op x*** while the condition ***cond x*** is ***True***.

Solution 3:

```
whileG :: (a → IO Bool) → (a → IO a) → (a → IO a)
whileG cond op x
= do test <- cond x
    if test
        then do op x
                whileG cond op x
        else return x
```

Exercise 4:

Using the function ***whileG*** or otherwise, define an interaction which reads a number, ***n***, say, and then reads a further ***n*** numbers and finally returns their average.

Solution 4:

```
findAvg :: IO Integer
findAvg
= do n <- getInt
    s <- sumInts n 0
    return (s `div` n)

sumInts :: Integer → Integer → IO Integer
sumInts n s
= if n>0
    then do m <- getInt
            sumInts (n-1) (s+m)
    else return s
```

Exercise 5:

1. Define a function

```
accumulate :: [IO a] -> IO [a]
```

which performs a sequence of actions and accumulates their result in a list.

You can test this using (see testf below), e.g.:

```
> accumulate [readLn, testf "hi", readLn]
```

2. Also define a function :

```
sequence' :: [IO a] -> IO ()
```

which performs the interactions in turn, but discards their results.

You can test this using (see testf below), e.g.:

```
> sequence' [putStrLn "hello" , putStrLn "goodbye"]
```

3. Finally show how you would sequence a series, passing in values from one to the next :

```
seqList :: [a -> IO a] -> a -> IO a
```

Hint: Use a simple function e.g

```
testf :: String -> IO String
testf x = do
    putStrLn x
    return (x ++ x)
```

(which takes a parameter and appends it to itself. It works on Strings).

So, you could call it as

```
> seqList [testf, testf, testf] "hello" — and get back
  hello                               —from first call (as IO effect)
  hellohello                            —from second call
  hellohellohellohello                  —from third call
  "hellohellohellohellohellohello"      — returned from function
```

Solution 5:

```
accumulate :: [IO a] -> IO [a]
accumulate [] = return []
accumulate (a:as) = do
    x <- a
    xs <- accumulate as
    return (x:xs)
```

```

—test this using
> accumulate [readLn, testf "hi", readLn]

sequence' :: [IO a] -> IO ()
sequence' [] = return ()
sequence' (a:as) = do
    a
    sequence' as
    return ()

—test this with
> sequence' [putStrLn "hello" , putStrLn "goodbye"]

seqList :: [a-> IO a] -> a -> IO a
seqList [] elem = return elem

seqList (a:as) elem = do
    x <- a elem
    seqList as x

```

Exercise 6:

Given the type definition

```
data Result a = Succeed a | Fail
```

show how **Result** can be made into a monadic type.

Solution 6:

```

data Result a = Succeed a | Fail deriving (Eq, Show)

instance Functor Result where
    fmap f (Succeed x) = Succeed (f x)
    fmap _ _ = Fail

instance Applicative Result where
    pure = Succeed
    Fail <*> _ = Fail
    (Succeed f) <*> something = fmap f something

instance Monad Result where
    return = Succeed
    Succeed x >>= f = f x
    Fail >>= _ = Fail

— to test this

```

```
divBy :: Int -> Int -> Result Int
divBy 0 _ = Fail
divBy x y = Succeed (y `div` x)
```