

```

O(1) def euclidean_distance(town1:tuple, town2:tuple):
O(1)     return ((town1[0] - town2[0])**2 + (town1[1] - town2[1])**2)**0.5

```

$O(N+N*(N+N)) = O(N^2)$

```

    def glouton(size:int, towns:dict):
O(N)         to_visit = [i for i in range(1, size)]
O(1)         result = [0]

O(N)         while len(to_visit) > 0:
O(1)             min_found, index = float('inf'), float('inf')
O(N)             for i in to_visit:
O(1)                 distance = euclidean_distance(towns[result[-1]], towns[i])
O(1)                 if distance < min_found:
O(1)                     min_found, index = distance, i
O(1)                 result.append(index)
O(N)             to_visit.remove(index)
O(1)         return result

```

$O(n \log(n))$ car selon théorème maitre $k=1$, $b=1$ et $l=1$. Plus formellement $T(n) = 1*T(n-1) + 2*(n^1)$

```

    def powerset(seq):
O(1)         if len(seq) <= 1:
O(1)             yield seq
O(1)             yield []
        else:
O(N-1)         for item in powerset(seq[1:]):
O(1)             yield [seq[0]]+item
O(1)             yield item

```

$O(2N + N! + N*\log(N) + N + (N-1)!*N*(N-1) + N + N + N + N) = O(N!*N^2)$

```

def progdyn(size:int, towns:dict):

```

```

O(N)      town_indexes = list(towns.keys())
O(N)      town_indexes.remove(0)
O(N!+N*log(N)) = (next line)
O(N!)     cols = [set(x) for x in powerset(town_indexes)]
O(N*log(N)) cols.sort(key=lambda x: len(x))
O(1)      cols.pop()
O(1)      dyn_table = dict()

O(N)      for k in town_indexes:
O(1)      dyn_table[(k, frozenset(cols[0]))] = euclidean_distance(towns[0], towns[k]), 0

O((N-1)!) for subset in cols[1:]:
O(N)      for k in town_indexes:
O(1)      if k in subset:
O(1)      dyn_table[(k, frozenset(subset))] = None
            else:
O(1)      min_found, min_found_index = float('inf'), float('inf')
O(N-1)    for j in subset:
O(1)      distance = euclidean_distance(towns[k], towns[j]) + dyn_table[(j, frozenset(subset - {j}))][0]
O(1)      if distance < min_found:
O(1)      min_found, min_found_index = distance, j
O(1)      dyn_table[(k, frozenset(subset))] = min_found, min_found_index

O(1)      min_path, min_path_index = float('inf'), float('inf')
O(N)      town_indexes_set = set(town_indexes)
O(N)      for k in town_indexes_set:
O(1)      distance = euclidean_distance(towns[0], towns[k]) + dyn_table[(k, frozenset(town_indexes_set - {k}))][0]
O(1)      if distance < min_path:
O(1)      min_path, min_path_index = distance, k

```

$O(N)$ car on passe dans toutes les valeurs de `town_indexes_set` avec une taille égale à N

```
def get_path(k:int, town_indexes_set:set):
```

```
O(1)         if len(town_indexes_set) == 1:
```

```
O(1)         return [k]
```

```
O(1)         return [k] + get_path(dyn_table[(k, frozenset(town_indexes_set - {k}))][1], town_indexes_set - {k})
```

```
O(N)         result = get_path(min_path_index, town_indexes_set)
```

```
O(1)         result.append(0)
```

```
O(N)         result.reverse()
```

```
O(1)         return result
```

```
class Graph():
```

```
O(1)         def __init__(self, vertices, towns:dict):
```

```
O(1)         self.V = vertices
```

```
O(1)         self.nodes = {}
```

```
O(1)         self.towns = towns
```

$O(N+N*M) = O(N*M)$ où M est le nombre d'enfant par noeuds

```
def printMST(self, parent):
```

```
O(N)         for i in range(1, self.V):
```

```
O(1)         if parent[i] not in self.nodes:
```

```
O(1)         self.nodes[parent[i]] = []
```

```
O(1)         self.nodes[parent[i]].append({"child":i, "weight":euclidean_distance(self.towns[i],  
                                          self.towns[parent[i]])})
```

```
O(1)         stack = [0]
```

```
O(1)         result = []
```

```
O(N)         while len(stack) > 0:
```

```
O(1)         current = stack.pop()
```

```
O(1)         result.append(current)
```

```
O(1)         if current in self.nodes:
```

```
O(M)         for child in self.nodes[current]:
```

O(1) stack.append(child["child"])

O(1) return result

O(N) def minKey(self, key, mstSet):

O(1) min = sys.maxsize

O(N) for v in range(self.V):

O(1) if key[v] < min and mstSet[v] == False:

O(1) min = key[v]

O(1) min_index = v

O(1) return min_index

$O(N*(N+N) + N*M) = O(N^2)$, car $N*M < N^2$ car $M < N$

def primMST(self):

O(1) key = [sys.maxsize] * self.V

O(1) parent = [None] * self.V

O(1) key[0] = 0

O(1) mstSet = [False] * self.V

O(1) parent[0] = -1

O(N) for cout in range(self.V):

O(N) u = self.minKey(key, mstSet)

O(1) mstSet[u] = True

O(N) for v in range(self.V):

O(1) uv_distance = euclidean_distance(self.towns[u], self.towns[v])

O(1) if uv_distance > 0 and mstSet[v] == False \ and key[v] > uv_distance:

O(1) key[v] = uv_distance

O(1) parent[v] = u

O(N*M) return self.printMST(parent)

$O(N^2)$ `def approx(size:int, towns:dict):`

$O(1)$ `g = Graph(size, towns)`

$O(N^2)$ `return g.primMST()`