

Recursion (Basic)

1) fn calling itself directly or indirectly.

2) 2 Parts 
→ Base case.
→ Recursive call.

3) Every recursive problem can be solved with iteration and vice versa.

4) Multiple Activation records are formed for recursion due to fn calls.

c)

Disadv

- Uses more space and memory.
- Also has greater time req.

Adv

- Is clean and simple.

Basic 1 finding a number

```
bool recursiveSearch(int arr[],
                    int l, int r,
                    int x)
{
    if (x < l) { return false; }
    if (arr[l] == x) { return true; }
    if (arr[r] == x) { return true; }
    return recursiveSearch(arr,
                          l+1, r-1,
                          x);
}
```

Basic 2 Palindrome

```
bool isPalindrome(char str[], int s, int e)
{
    if (s == e) { return true; }
    if (str[s] != str[e]) { return false; }
    if (s < e) { return isPalindrome(str, s+1, e-1); }
    return true;
}
```

7) Tail Recursion

→ When the recursive call is at the end of the fn. and doesn't use the current fn anymore.

↳ Easier for compiler to correct.

Eg:- Factorial

fact(int N, int a)

```
{
    if (N == 0) return a;
    return fact(N-1, N*a);
}
```

↓
Tail

fact(int N)

```
{
    if (N == 0) return 1;
    return N * fact(N-1);
}
```

Non-Tail.

8) Application

→ Dynamic Prog

Backtracking

Divide and Conquering (Quick Sort, Merge Sort) etc.

Binary Search.

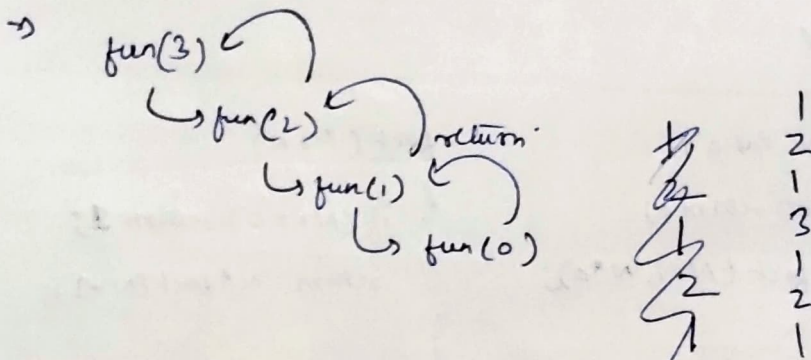
Inherently Recursive → Tower of Hanoi
Traversals
DFS/BFS
Josephus problem.

Problems

Guess the output →

```
void fun(int n)
{
    if (n == 20) return;
    fun(n-1);
    cout << n << endl;
    fun(n-1);
}

int main() {
    fun(3);
    return 0;
}
```



Always try to draw a tree
to solve recursion problems.

① Print n to 1 using recursion.

```
Print_n_to_1(int n) {
    if (n == 0) { return; } → Base case.
    Print(n);
    Print_n_to_1(n-1);
}
```

Space → $O(n)$ but if we
use tail recursion
i.e. use modern compiler it can reduce to
 $O(1)$.

② Natural numbers sum.

First n natural num sum.

firstN (int n)

```
{  
    if (n == 0) return 0;  
    return n + firstN(n-1);  
}
```

③ Find nth Fibonacci number (where $n \geq 0$).

inta
fibo (int n) {

(5th, 2)

if (a == n) return a;

a = f(a-1) + f(a-2);

if (n == 1) return 1;

} My
trial.

Ans
int fib (int n)

{ if (n == 0) return 0;

if (n == 1) return 1;

return fib(n-1) + fib(n-2);

}

④ Palindrome already discussed.