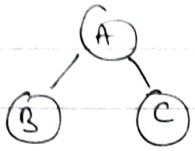
More on complexity later

* We can use a type of binary search tech from searching an element in set.

BST (Binary Search Tree).



Binary → 0, 1, 2 branches [Duplicate elements not allowed].

C → Always greater than A

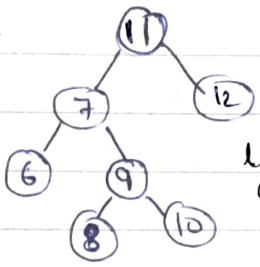
B → Always less than A

Even the subtree of B will be < A.

vice versa for C.

B Case → O(1)
Avg → $O(\log_2 n) = O(h)$ ← h is to the height.
Worst → O(n)

Eg:-



logical ins & deletion explained.

Coding will remain the same as in Binary Tree just data will change.

AVL Tree

(1) → It is a BST. $O(\log_2 n)$ - Always.

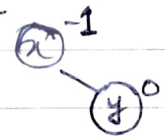
(2) → Height of left subtr − Height of right subtr = {-1, 0, +1}.

This is known as balance factor.

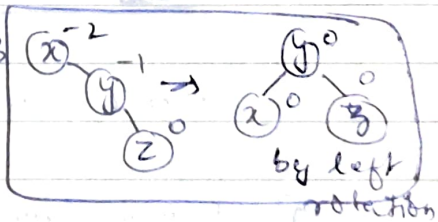
Balance factor = No. of nodes of a nodes. (children)

Case 1 →

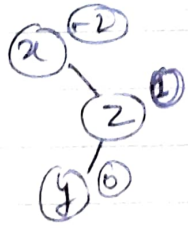
Case 2



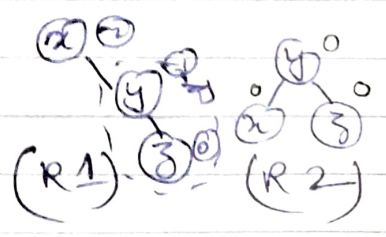
Case 3



Case 4 →



→ Simple 1 rotation not possible → 2 rotation req



Case 5 → Vice versa of case 4.

Rotations → LL, RR (single)
LR, RL (double)

Code Remains same for it too

Red - Black Trees

(1) ⇒ It is a BST.

(2) ⇒ It is a self balancing tree like AVL, but AVL requires many rotations.

In Red-Black only recolouring & max 2 rotation req.

(3) ⇒ Used when insertion & deletion operations are req frequently. for Searching req the AVL trees. are best. (RBTr best)

Props of RBTr

(1) ⇒ Every node is either Black or Red.

(2) ⇒ A storage req for storing colour of tree also.

(3) ⇒ Root node is always Black.

(4) ⇒ Every leaf which is Nil is Black.

(5) ⇒ If node is Red, children are Black.

(6) ⇒ Every path from a node to any of it's descendent Null node has same number of Black nodes.

* AVL tree is a subset of Red-Black Tree.

(7) Extreme (longest) branch should not be > than smallest branch.

Insertion in Red-Black Trees.

Steps:

(1) ⇒ If tree is empty, create newnode as root node with colour black.

(2) ⇒ If not empty, create it as Red.

(3) ⇒ If parent of newnode is black then exit.

(3) ⇒ If parent of newnode is Red, then check colour of parent's sibling.

Cases:

a) If colour is black (or) null then do suitable rotation and recolour

b) If Red, then recolour & also check if Grand parent of newnode is not root node, if yes, then recolour the parent of newnode.