

(4) Probability

(i) \rightarrow Relationship b/n prob & stats?

\rightarrow Probability is a mathematical concept used in statistics and vice versa, \therefore They are interconnected fields.

(ii) \rightarrow Probability is measure of how likely event will occur.

\Rightarrow b/n 0 & 1.

$$\Rightarrow P(E) = \frac{\text{desired outcomes}}{\text{Total outcomes}}$$

(iii) Terminologies

\rightarrow Random experiment

\rightarrow An exp where outcome cannot be predicted with certainty.

\rightarrow Sample space

\rightarrow Possible set of outcomes.

\rightarrow Event

\rightarrow Outcome that actually happened.

(iv) Types of events

\rightarrow Disjoint  \rightarrow King & Queen (cards)

\rightarrow Non-disjoint  \rightarrow no ball & six (cricket)

(v) Types of distribution

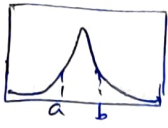
\rightarrow Probability density function (pdf)

\rightarrow Normal distribution

\rightarrow Central limit theorem.

→ Probability Density Function.

→ An equation describing continuous probability ~~curve~~ ^{distribution}

→ Bell Curve graph. 

→ Has 3 properties

- Graph of pdf is continuous.
- Area bounded by pdf and x-axis = 1
- $P(E) = \text{area b/n } a \text{ \& } b$ i.e. it depends on $a \text{ \& } b$.

∴ Probability of finding a cont random var b/n $a \text{ \& } b$.

→ Normal Distribution (Optional).

→ Depends of mean & std dev.

→ Mean determines where center of graph will be.

→ Std dev determines what the height will be.

→ Also a bell curve.

∴ Main idea is data around mean describes population more than data away from it.

→ Central Limit Theorem (Optional)

→ Sampling distribution of mean of any independent, random variable will be normal (or) nearly normal, if sample size is large enough.

(vii) Types of Probability

- ↳ marginal.
- ↳ Joint.
- ↳ Conditional.

Marginal Probability

→ Probability of occurrence of single event.

Eg:- Card drawn is heart or not? $13/52$

Joint Probability

→ Probability of 2 events happening at the same time.

Eg:- $P(A \& B)$ = Intersection of a & b.

→ $P(\text{Card is heart \& a 4}) = 1/52$

Conditional Probability

→ CP of event B is prob that it will occur given that A has already occurred.

$$P(B|A) = \frac{P(A \cap B)}{P(A)} \rightarrow \begin{matrix} \text{'n' means} \\ A \text{ and } B \end{matrix} \left\{ \begin{array}{l} \text{if } A \& B \\ \text{are dependent} \end{array} \right.$$

$$P(B|A) = P(B) \rightarrow \text{if } A \& B \text{ are independent.}$$

(viii) Bayes Theorem

→ Mainly used in naive bayes algo (a supervised algo).
→ Used in Gmail Spam.

→ Shows relation b/w
one conditional prob
& its inverse.

$$P(A|B) = \frac{P(B|A) \times P(A)}{P(B)}$$