



HOW TO KILL TWO BIRDS WITH ONE STONE: LEARNING TO RANK WITH MULTIPLE OBJECTIVES

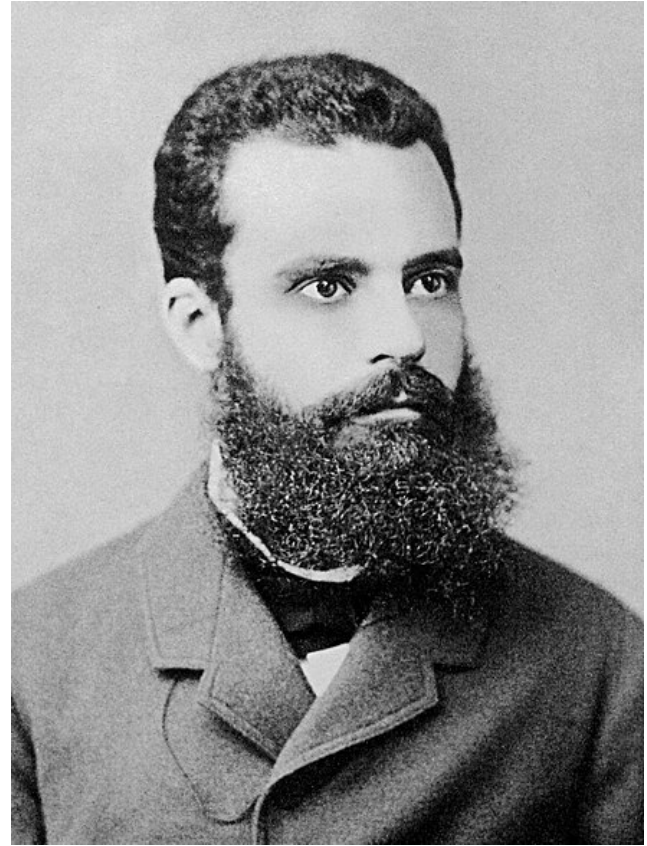
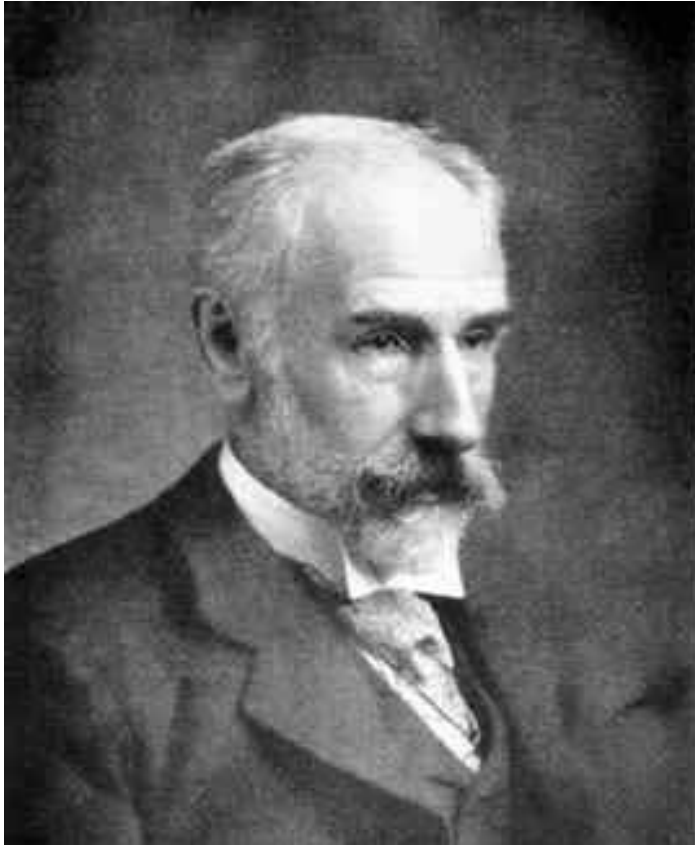
HAYSTACK EU 2019



ALEXEY KURENNOY

28-10-2019





MULTI-OBJECTIVE OPTIMISATION IN EVERYDAY LIFE

- Product quality vs price
- Hotel location vs facilities
- Job satisfaction vs compensation
- ...

ZALANDO AT A GLANCE

~ **5.4** billion EUR
revenue 2018

> **300**
million

visits
per
month

> **400,000**
product choices

> **15,500**

employees in
Europe

> **80%**

of visits via
mobile devices

> **27**

million
active customers

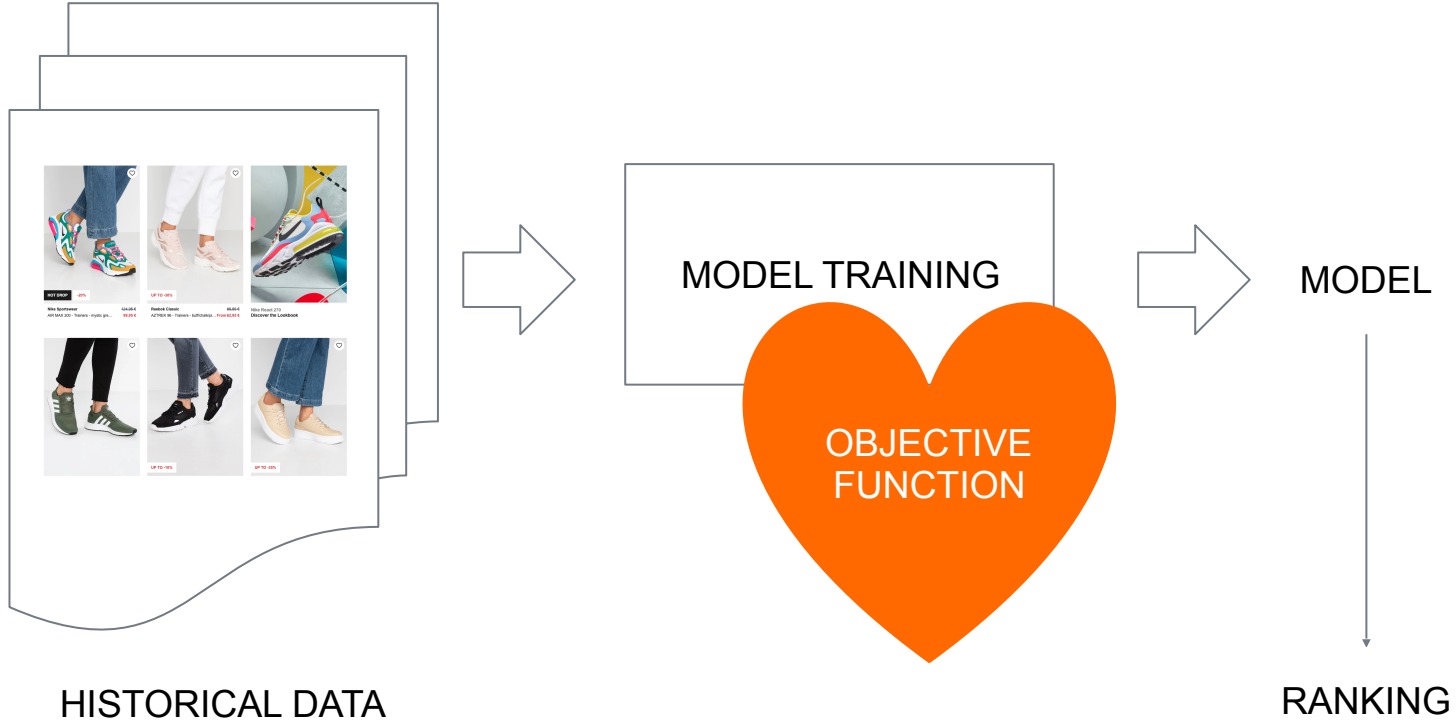
~ **2,000**
brands

17
countries

OUTLINE

- Introduction
- Learning to Rank recap
- Multi-objective optimisation
- LambdaMART recap
- Multi-objective Learning to Rank with LambdaMART
- Experiments
- Conclusion and further steps

LTR RECAP



EXAMPLE: NDCG OBJECTIVE

Interaction	r_{ij}
purchase	3
click	1
no interaction	0

$$i = 1, \dots, N,$$
$$j = 1, \dots, n_i.$$

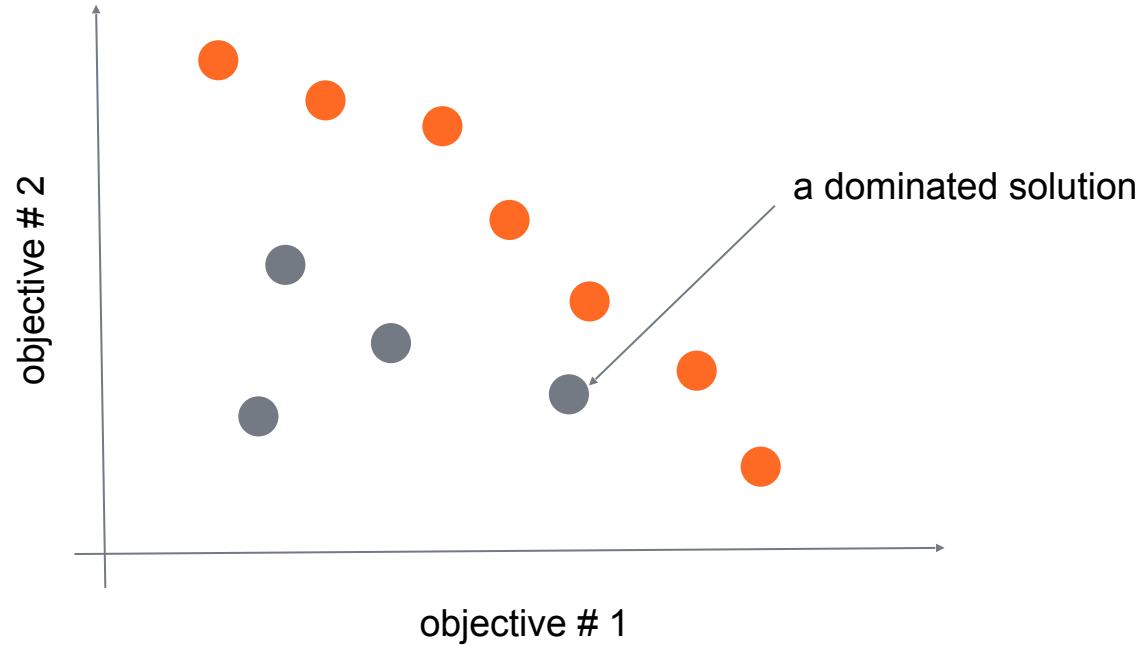
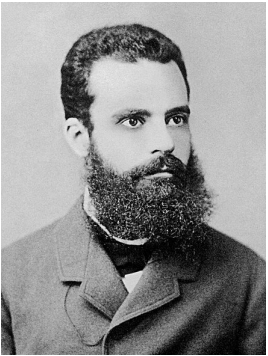
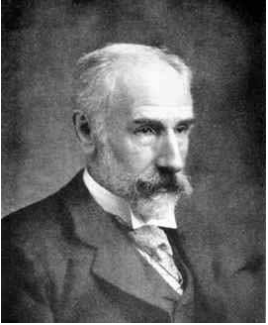
$$DCG_i = \sum_{j=1}^{n_i} \frac{r_{ij}}{\log_2(j+1)}$$

$$NDCG = \sum_{i=1}^N \frac{DCG_i}{\max DCG_i}$$

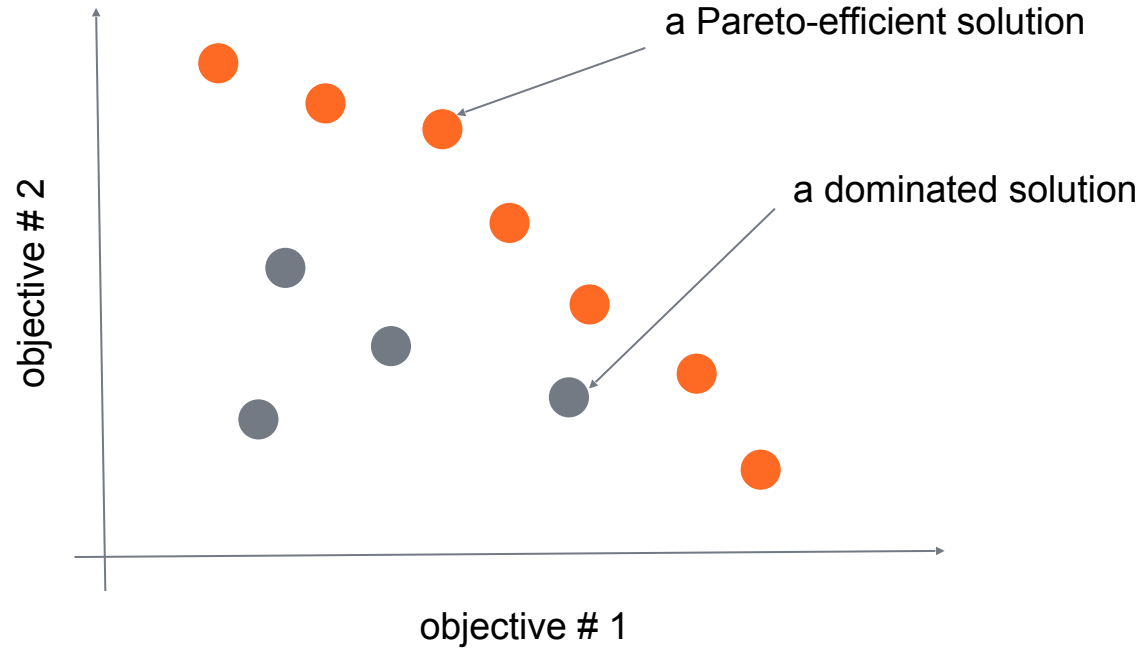
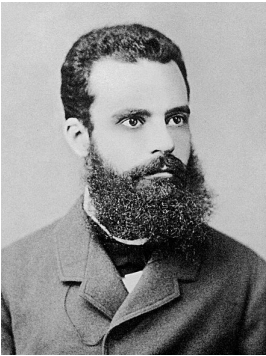
WHY A SINGLE OBJECTIVE MAY BE NOT ENOUGH?

- Different types of user feedback (implicit vs explicit)
- Different sources of feedback (user vs annotator)
- E-Commerce: engagement vs post-order experience
- E-Commerce: engagement vs fashionability

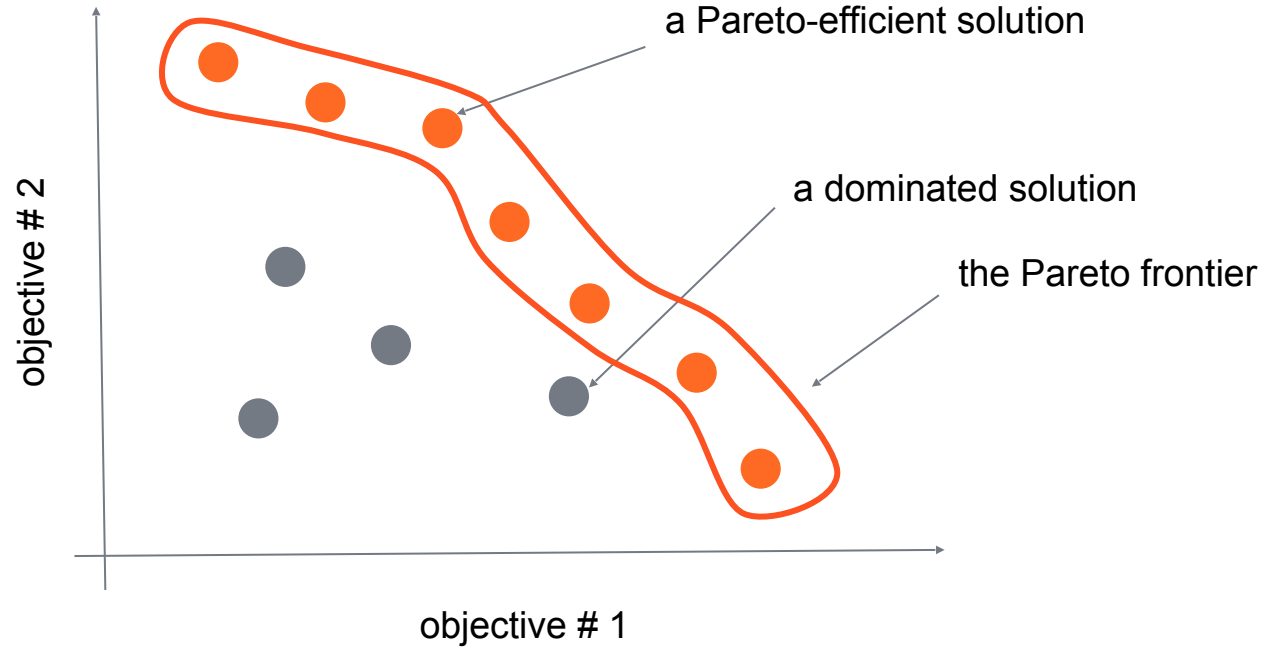
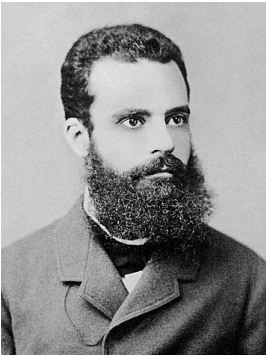
MULTI-OBJECTIVE OPTIMISATION



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MULTI-OBJECTIVE OPTIMISATION



HOW TO SEARCH FOR PARETO SOLUTIONS?

$$r', r'', F_{r'}, F_{r''}$$

HOW TO SEARCH FOR PARETO SOLUTIONS?

$$r', r'', F_{r'}, F_{r''}$$

- Post-augmentation of the sorting rule

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- Redefining the relevance

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$$r', r'', F_{r'}, F_{r''}$$

- Post-augmentation of the sorting rule
- Redefining the relevance

Interaction	r_{ij}
purchase, fashionable	7
purchase, non-fashionable	3
click	1
no interaction	0

$$i = 1, \dots, N, \\ j = 1, \dots, n_i.$$

HOW TO SEARCH FOR PARETO SOLUTIONS?

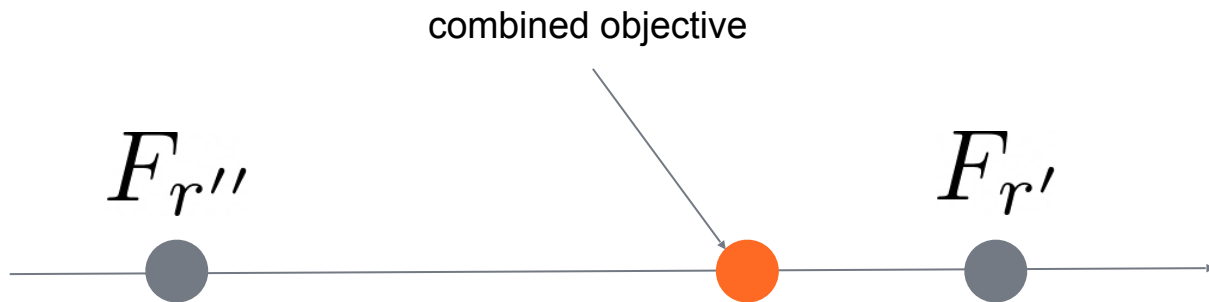
$$r', r'', F_{r'}, F_{r''}$$

- Post-augmentation of the sorting rule
- Redefining the relevance
- **Scalarization**

$$\alpha F_{r'} + (1 - \alpha) F_{r''} \rightarrow \max$$
$$\alpha \in (0, 1)$$

SCALARIZATION

$$\alpha F_{r'} + (1 - \alpha) F_{r''} \rightarrow \max$$
$$\alpha \in (0, 1)$$

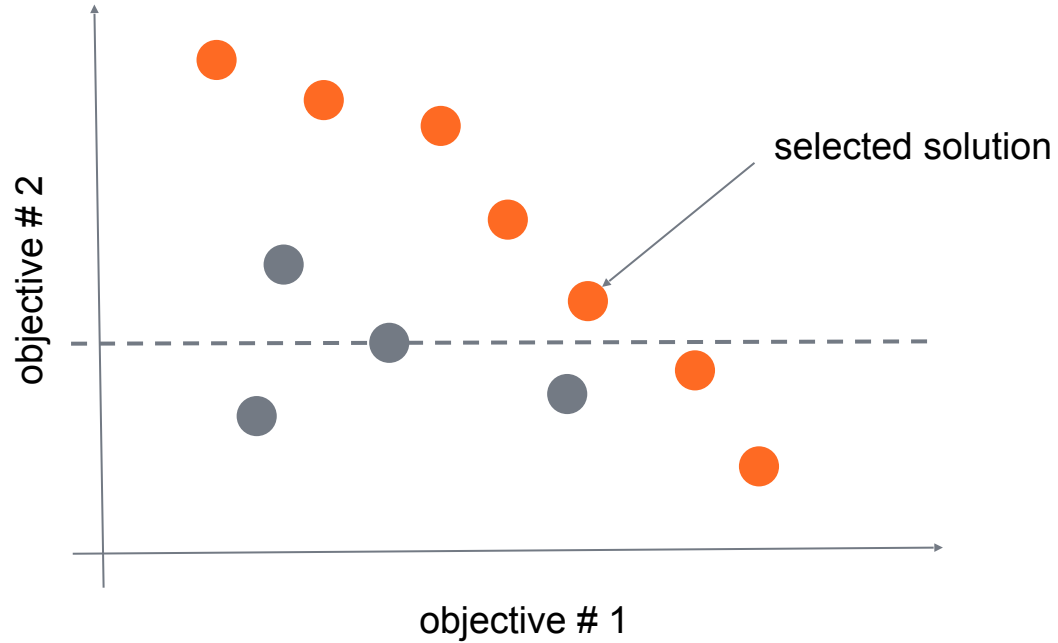


SCALARIZATION

$$\alpha F_{r'} + (1 - \alpha) F_{r''} \rightarrow \max$$
$$\alpha \in (0, 1)$$

- Produces only Pareto optimal solutions
- Allows finding any Pareto optimal solution (under certain assumptions)
- Straightforward to apply when there are more than two objectives

HOW TO CHOOSE AMONG PARETO SOLUTIONS?



HOW TO SEARCH FOR PARETO SOLUTIONS?

$$r', r'', F_{r'}, F_{r''}$$

- Post-augmentation of the sorting rule
- Redefining the relevance
- Scalarization
- Constrained optimisation
(Momma et. al. [Multi-objective Relevance Ranking](#). SIGIR 2019)

$$F_{r'} \rightarrow \max \text{ s.t. } F_{r''} \geq c$$

LAMBDMART RECAP

- A boosting algorithm for optimising ranking metrics (such as NDCG)
- Iteration:
 - compute the lambda-gradient

$$\Delta s_{ij}(r)$$

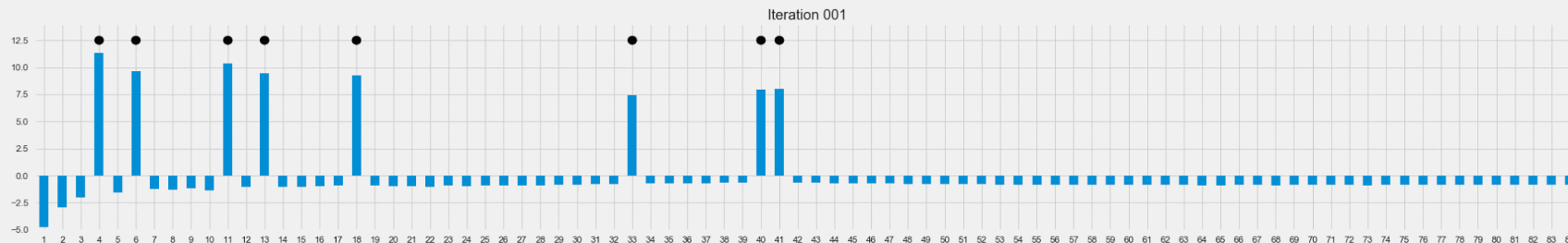
- construct a tree that approximates the lambda-gradient and add it to the ensemble

LAMBDMART RECAP

- A boosting algorithm for optimising ranking metrics (such as NDCG)
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 - compute the lambda-gradient

$$\Delta s_{ij}(r)$$

- construct a tree that approximates the lambda-gradient and add it to the ensemble



MULTI-OBJECTIVE OPTIMISATION WITH LAMBDAMART

$$\Delta s_{ij}(r)$$

$$r', r''$$

$$\Delta s_{ij} = \alpha \Delta s_{ij}(r') + (1 - \alpha) \Delta s_{ij}(r'')$$

IMPLEMENTATION

`lightgbm.train(..., fobj=...)`

- Used Cython
- Parallelisation by means of OpenMP
~5x speed-up (Dual-Core Intel Core i5)
- The speed is on par with the original implementation

```
cimport cython
cimport openmp
from cython.parallel import prange

...

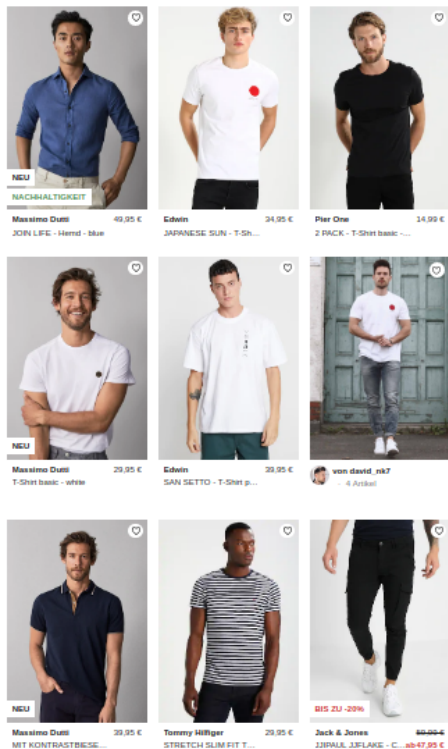
cdef int cnt
cnt = <int>(end - start)

...

cdef int i
cdef int j
for high in range(cnt):
    label_high = labels[start + high]
    score_high = preds[start + high]
    for low in range(cnt):
        label_low = labels[start + low]
        score_low = preds[start + low]
        if label_high > label_low:
            sigmoid = get_sigmoid(score_high - score_low, ...)
            abs_delta_ndcg = get_abs_delta_ndcg(...)

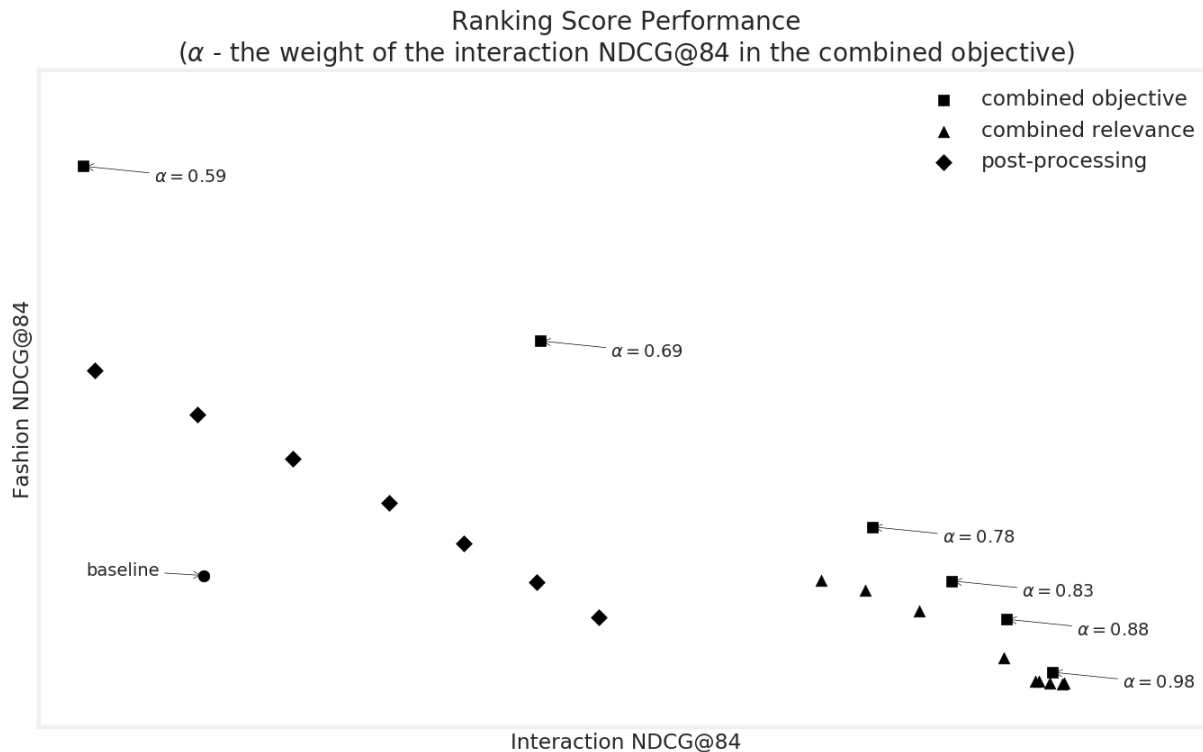
            grad[start + high] += -abs_delta_ndcg * sigmoid
            grad[start + low] -= p_lambda
```


OFFLINE EXPERIMENTS: SETUP



- Result pages from Zalando catalog (~50K pages)
- Two objectives:
 - Interaction NDCG
$$r_{ij} = \begin{cases} 3 & \text{if purchased}_{ij}, \\ 1 & \text{if clicked}_{ij}, \\ 0 & \text{otherwise.} \end{cases} \quad \begin{matrix} i = 1, \dots, N, \\ j = 1, \dots, n_i. \end{matrix}$$
 - Fashionability NDCG (relevance = fashion score)
- Goal: up-sort popular *but fashionable* articles

OFFLINE EXPERIMENTATION: RESULTS



OFFLINE EXPERIMENTATION: RESULTS

- Visibility of popular but non-fashionable articles went UP
- Visibility of fashionable but unpopular articles went UP
- Visibility of fairly popular and relatively fashionable articles went DOWN

CONCLUSIONS

- A Pareto-efficient solution in ranking can lead to a “mixed” effect
- Evaluation in the “multi-objective” space may not be reliable

FUTURE STEPS

- Experimenting with the “combined” relevance
- Experimenting with dataset augmentation

P.S.

No birds were killed during the preparation of this talk.