



The Evolution of a Haskell Programmer

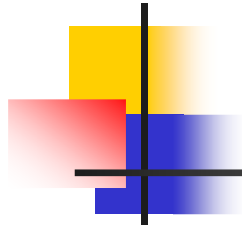
Inšpirovaný rôznymi technikami programovania v Haskellu riešime nasledujúce zadania:

`fac n = 1.2.n`

`sum n = 1+2+ ... +n`

`sumsq n = 1^2 + 2^2 + ... + n^2`

`triangle n = [[1,2,..n],[1,2,..,n-1],...,[1,2],[1]]`



Freshman Haskell programmer

```
fac n = if n == 0 then 1 else n * fac (n-1)
```

```
suma n = if n == 0 then 0 else n + suma (n-1)
```

```
sumsq n = if n == 0 then 0 else (n*n) + sumsq (n-1)
```

```
triangle n = if n == 0 then [] else [1..n] : triangle (n-1)
```



Haskell programmer, at MIT

fac1 =

```
(\n) -> (if (==) n 0) then 1 else ((*) n (fac1 ((-) n 1))))
```

suma1 =

```
(\n) -> (if (==) n 0) then 0 else ((+) n (suma1 ((-) n 1))))
```

sumsq1 =

```
(\n) -> (if (==) n 0) then 0 else ((+) ((*) n n) (sumsq1 ((-) n 1))))
```

triangle1 =

```
(\n) -> (if (==) n 0) then [] else (:) [1..n] (triangle ((-) n 1))))
```



Junior Haskell programmer

fac2 0 = 1
fac2 (n+1) = (n+1) * fac2 n

sum2 0 = 0
sum2 (n+1) = (n+1) + sum2 n

sumsq2 0 = 0
sumsq2 (n+1) = (n+1)*(n+1) + sumsq2 n

triangle2 0 = []
triangle2 (n+1) = [1..n] : triangle2 n

■ Another junior Haskell programmer

fac 0 = 1
fac n = n * fac (n-1)



Senior Haskell programmer

(voted for John McCain — “leans right”)

```
fac3 n = foldr (*) 1 [1..n]
```

```
sum3 n = foldr (+) 0 [1..n]
```

```
sumsq3 n = foldr (+) 0 (map (\x->x*x) [1..n])
```

```
sumsq33 n = foldr (\x y->x*x+y) 0 [1..n]
```

```
triangle3 n =
```

```
  foldr (\x y->[1..x]:y) []
```

```
    (enumFromThenTo n (n-1) 1)
```



Another senior Haskell programmer

(voted for McGovern Barack Obama — “leans left”)

```
fac4 n = foldl (*) 1 [1..n]
```

```
sum4 n = foldl (+) 0 [1..n]
```

```
sumsq4 n = foldl (\x y->y*y+x) 0 [1..n]
```

```
triangle4 n = foldl (\x y->[1..y]:x) [] [1..n]
```



Yet another senior Haskell programmer

(leaned so far right he came back left again!)

-- using foldr to simulate foldl

```
fac5 n = foldr (\x g n -> g (x*n)) id [1..n] 1
```

```
sum5 n = foldr (\x g n -> g (x+n)) id [1..n] 0
```

```
sumsq5 n = foldr (\x g n -> g (x*x+n)) id [1..n] 0
```

```
triangle5 n = foldr (\x g n -> g ([1..x]:n)) id [1..n] []
```

fac6 n = facs !! n

```
facs = scanl (*) 1 [1..]
```

```
scanl (*) 1 [1..] !! 10
```

sum6 n = sums !! n

```
sums = scanl (+) 0 [1..]
```

sumsq6 n = sumsq5 !! n

```
sumsq = scanl (\x y -> y*y+x) 0 [1..]
```

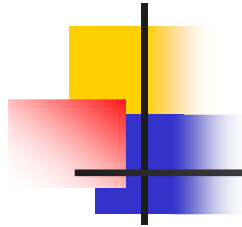
```
triangle6 n = triangles !! n
```

```
triangles = scanl (\x y -> [1..y]:x) [] [1..]
```

```
scanl :: (a -> b -> a) -> a -> [b] -> [a]
```

```
scanl f q xs = q : (case xs of [] -> [])
```

```
x:xs -> scanl f (f q x) xs)
```

Oxford Haskell programmer

fac = foldr (*) 1 . enumFromTo 1

(foldr (*) 1 . enumFromTo 1) 10
(foldr (*) 1 . enumFromTo 1) 10

fac7 = foldr (*) 1 . enumFromTo 1

foldr (*) 1 (enumFromTo 1 10)

sum7 = foldr (+) 0 . enumFromTo 1

sumsq7 = foldr (+) 0 . map (\x->x*x) . enumFromTo 1

triangle7 = foldr (:) [] . map (\x->[1..x]) . enumFromTo 1



Accumulating Haskell programmer


facAcc a 0 = a
facAcc a n = facAcc (n*a) (n-1)
fac8 = facAcc 1

sumAcc a 0 = a
sumAcc a n = sumAcc (n+a) (n-1)
sum8 = sumAcc 0

sumsqAcc a 0 = a
sumsqAcc a n = sumsqAcc (n*n+a) (n-1)
sumsq8 = sumsqAcc 0

triangleAcc a 0 = a
triangleAcc a n = triangleAcc ([1..n]:a) (n-1)
triangle8 = triangleAcc []

Iterative Haskell programmer (Pascal programmer)



```
fac n = result (for init next done)
  where   init = (0,1)
         next (i,m) = (i+1, m * (i+1))
         done (i,_) = i==n
         result (_,m) = m
```

```
for i n d = until d n i
```

```
until :: (a -> Bool) -> (a -> a) -> a -> a
until p f x = if p x then x else until p f (f x)
```

```
triangle9 n = result (for init next done)
  where init = (0,[])
        next (i,m) = (i+1, [1..(i+1)]:m)
        done (i,_) = i==n
        result (_,m) = m
```



Iterative one-liner Haskell (APL or C) programmer

```
fac10 n =  
    snd (until ((>n) . fst) (\(i,m) -> (i+1, i*m)) (1,1))
```

```
sumsq10 n =  
    snd (until ((>n) . fst) (\(i,m) -> (i+1, i*i+m)) (1,0))
```

```
triangle10 n =  
    snd (until ((>n) . fst) (\(i,m) -> (i+1, [1..i]:m)) (1,[]))
```



Boy Scout Haskell programmer

`y f` = `f (y f)`

`fac11` = `y (\f n -> if (n==0) then 1 else n * f (n-1))`

`sumsq11` = `y (\f n -> if (n==0) then 0 else n*n + f (n-1))`



Tenured professor

```
fac12 n = product [1..n]
```

```
sumsq12 n = n*(n+1)*(2*n+1) `div` 6
```

```
triangle11 n = map (\x -> [1..x]) (enumFromThenTo n (n-1) 1)
```



Cvičenie

Rôznymi spôsobmi definujte funkciu, ktorej výsledkom je jednotková matica rozmeru n

- jednotkova $n = [[1,0,\dots,0],[0,1,\dots,0],\dots,[0,\dots,1,0],[0,\dots,0,1]]$

Definujte rôzne algoritmy pre triedenie zoznamu:

- bubbleSort
- insertSort
- selectionSort