Chapter 8

Prove the following statements.

Exercise (16). If A, B and C are sets, then $A \times (B \cup C) = (A \times B) \cup (A \times C)$.

Proof: $\square$

Exercise (22). Let A and B be sets. Prove that $A \subseteq B$ if and only if $A \cap B = A$.

Proof: $\square$

Exercise (26). Prove that $\{4k + 5 : k \in \mathbb{Z}\} = \{4k + 1 : k \in \mathbb{Z}\}$.

Proof: $\square$

Chapter 9

Each of the following statements is either true or false. If a statement is true, prove it. If a statement is false, disprove it.

Exercise (3). If $n \in \mathbb{Z}$ and $n^5 - n$ is even, then n is even.

Proof: $\square$

Exercise (5). If A, B, C and D are sets, then $(A \times B) \cup (C \times D) = (A \cup C) \times (B \cup D)$.

Proof: $\square$

Exercise (8). If A, B and C are sets, and $A - (B \cup C) = (A - B) \cup (A - C)$.

Proof: $\square$

Exercise (9). If A and B are sets, then $\mathcal{P}(A) - \mathcal{P}(B) \subseteq \mathcal{P}(A \setminus B)$.

Proof: $\square$

Exercise (12). If $a, b, c \in \mathbb{N}$ and ab, bc and ac all have the same parity, then a, b and c all have the same parity.

Proof: $\square$

Exercise (30). There exist integers a and b for which $42a + 7b = 1$.

Proof: $\square$

Exercise (34). If $X \subseteq A \cup B$, then $X \subseteq A$ or $X \subseteq B$.

Proof: $\square$

Exercise (Reflection Problem). Answer the following questions:

Proof:

- How long did it take you to complete each problem?

  Write your answer here.

- What was easy?

  Write your answer here.

- What was challenging? What made it challenging?

  Write your answer here.

- Compare your answers to the odd numbered exercises to those in the back of the textbook. What did you learn from this comparison?

  Write your answer here.

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