# CSE419 – Artificial Intelligence and Machine Learning 2018

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https://github.com/FurkanGozukara/CSE419 2018

# Lecture 3 Decision Trees

Based on Asst. Prof. Dr. David Kauchak (Pomona College) Lecture Slides

# Representing examples

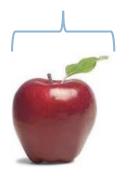
#### examples



What is an example? How is it represented?

### Features

#### examples









#### features

$$f_1, f_2, f_3, ..., f_n$$

How our algorithms actually "view" the data

Features are the questions we can ask about the examples

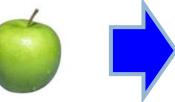
### Features

#### examples

#### features



red, round, leaf, 3oz, ...



green, round, no leaf, 4oz, .

yellow, curved, no leaf, 4oz,

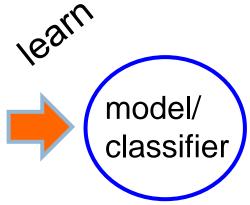
green, curved, no leaf, 5oz, ...

How our algorithms actually "view" the data

Features are the questions we can ask about the examples

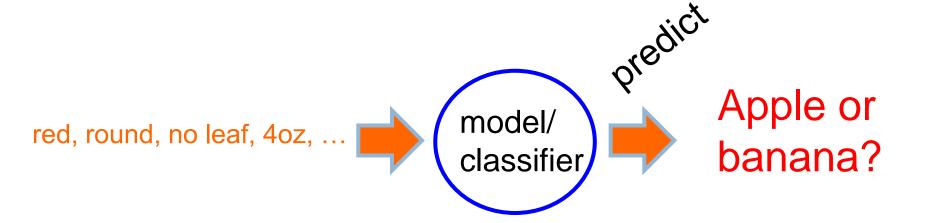
examples label red, round, leaf, 3oz, ... apple green, round, no leaf, 4oz, ... apple

yellow, curved, no leaf, 4oz, ...banana

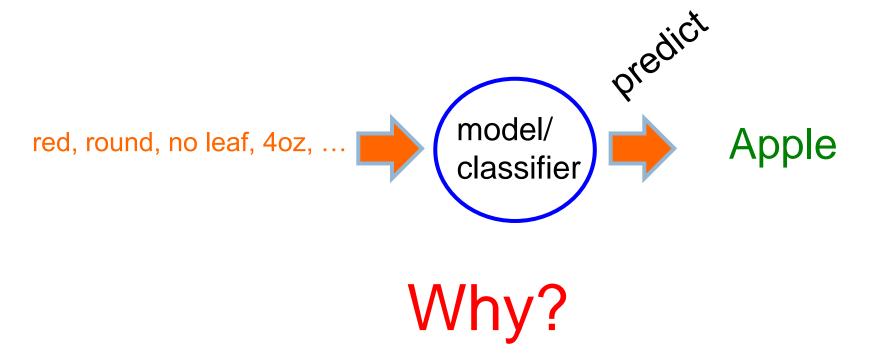


green, curved, no leaf, 5oz, ...banana

During learning/training/induction, learn a model of what distinguishes apples and bananas based on the features



The model can then classify a new example based on the features



The model can then classify a new example based on the features

Training data

Test set

examples

label

red, round, leaf, 3oz, ...

apple

green, round, no leaf, 4oz, ... apple

red, round, no leaf, 4oz, ...?

yellow, curved, no leaf, 4oz, ...banana

green, curved, no leaf, 5oz, ...banana

Training data

Test set

examples

label

red, round, leaf, 3oz, ...

apple

green, round, no leaf, 4oz, ... apple

red, round, no leaf, 4oz, ...?

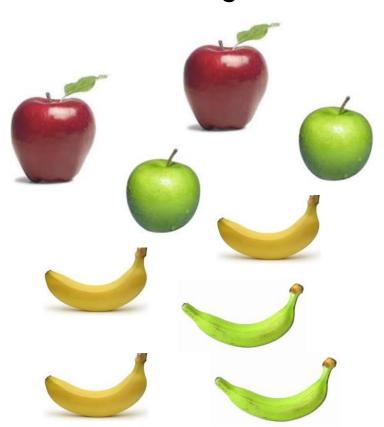
yellow, curved, no leaf, 4oz, ...banana

green, curved, no leaf, 5oz, ...banana

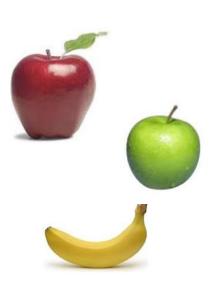
Learning is about generalizing from the training data What does this assume about the training and test set?

# Past predicts future

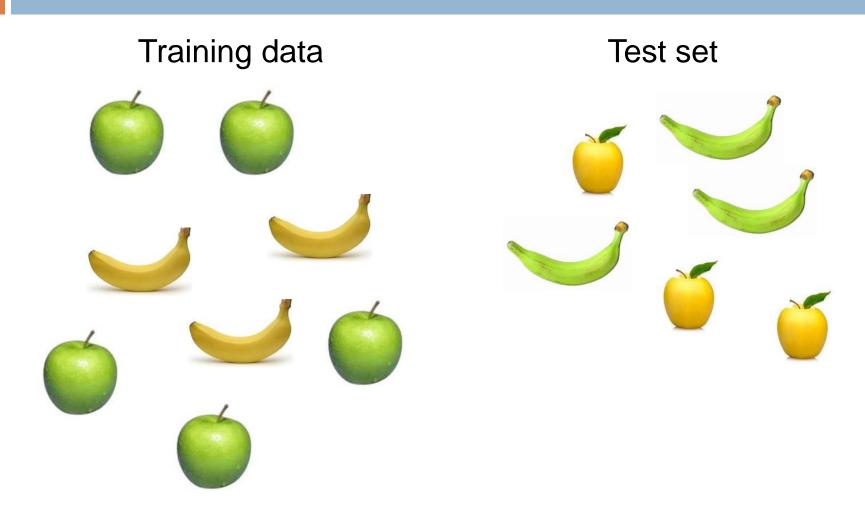
Training data



Test set

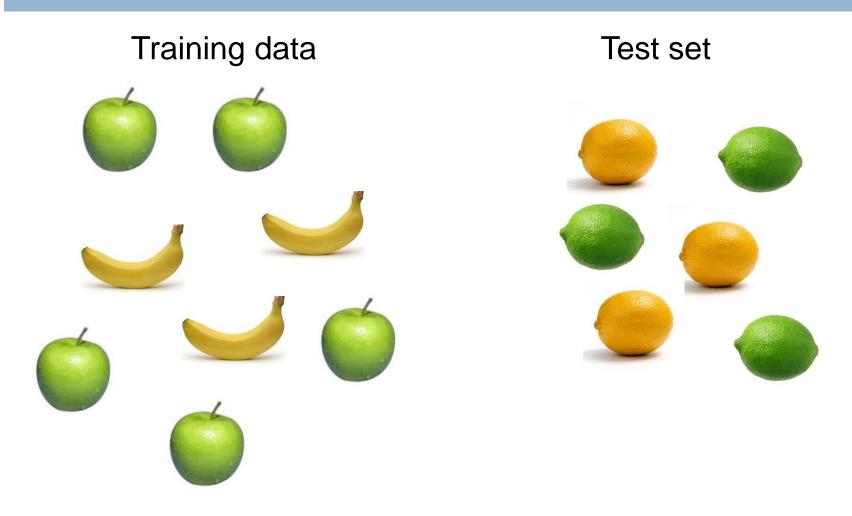


# Past predicts future



Not always the case, but we'll often assume it is!

# Past predicts future



Not always the case, but we'll often assume it is!

# More technically...

We are going to use the *probabilistic model* of learning

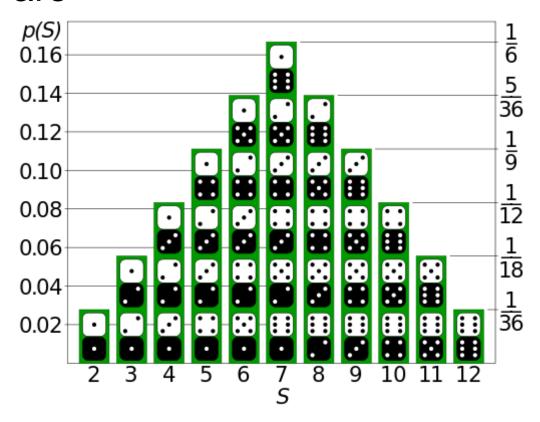
There is some probability distribution over example/label pairs called the *data generating distribution* 

**Both** the training data **and** the test set are generated based on this distribution

What is a probability distribution?

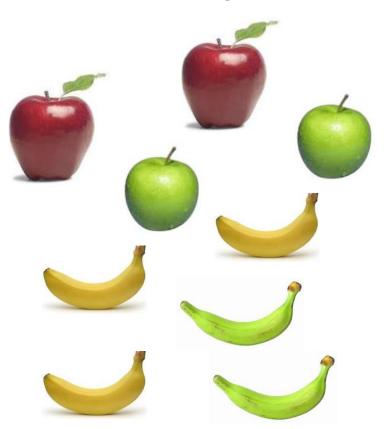
# Probability distribution

Describes how likely (i.e. probable) certain events are



# Probability distribution

#### Training data



#### High probability

round apples

curved bananas

apples with leaves

. . .

#### Low probability

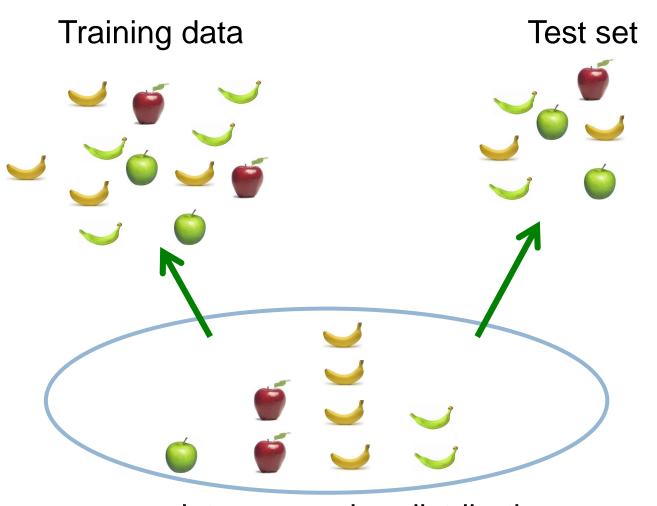
curved apples

red bananas

yellow apples

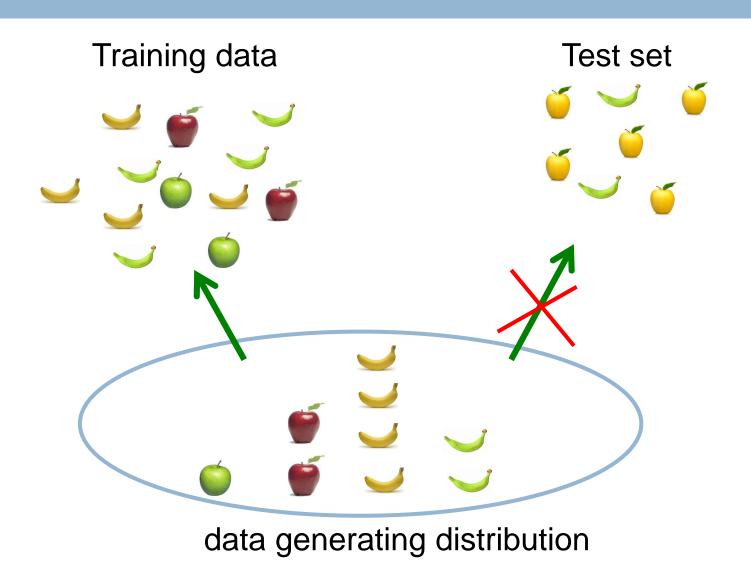
. . .

# data generating distribution

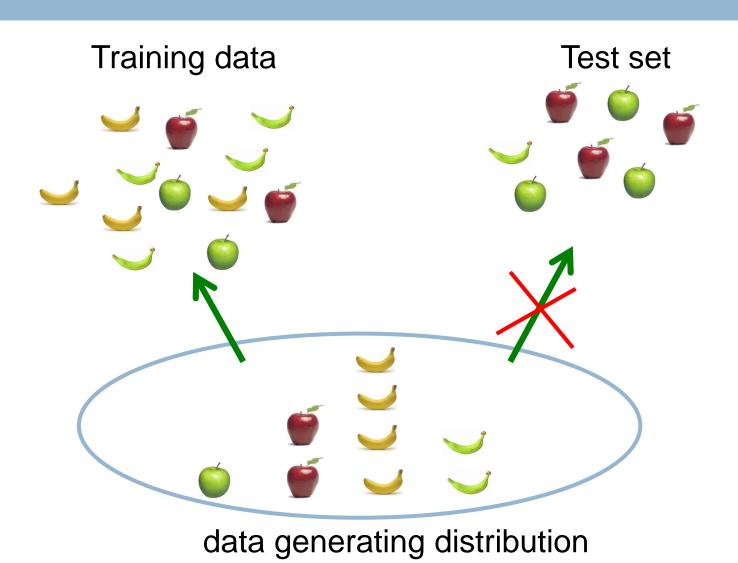


data generating distribution

# data generating distribution



# data generating distribution

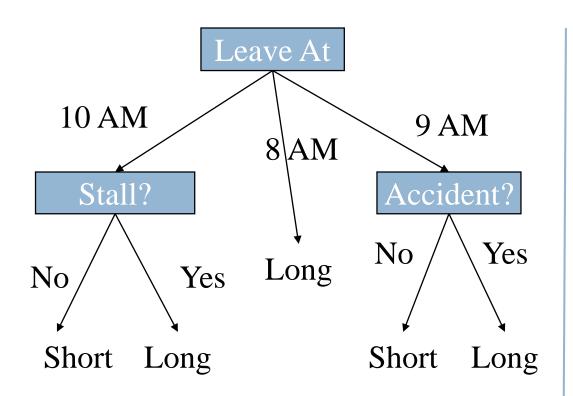


# A sample data set

Features				Label
Hour	Weather	Accident	Stall	Commute
8 AM	Sunny	No	No	Long
8 AM	Cloudy	No	Yes	Long
10 AM	Sunny	No	No	Short
9 AM	Rainy	Yes	No	Long
9 AM	Sunny	Yes	Yes	Long
10 AM	Sunny	No	No	Short
10 AM	Cloudy	No	No	Short
9 AM	Sunny	Yes	No	Long
10 AM	Cloudy	Yes	Yes	Long
10 AM	Rainy	No	No	Short
8 AM	Cloudy	Yes	No	Long
9 AM	Rainy	No	No	Short

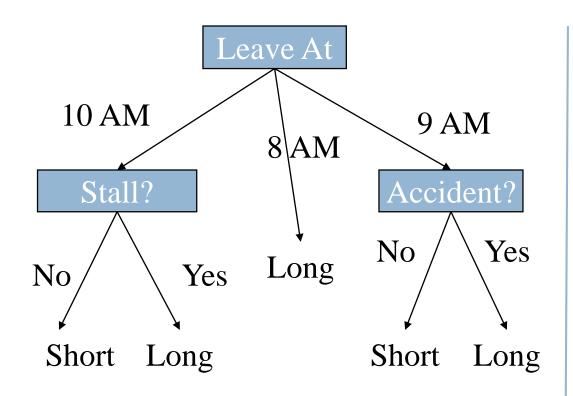
8 AM, Rainy, Yes, No? 10 AM, Rainy, No, No?

Can you describe a "model" that could be used to make decisions in general?



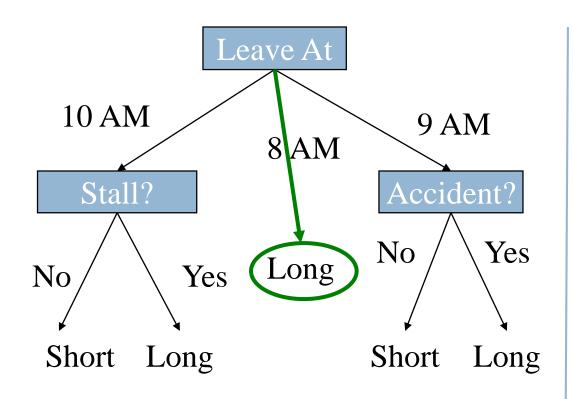
Tree with internal nodes labeled by features

Branches are labeled by tests on that feature



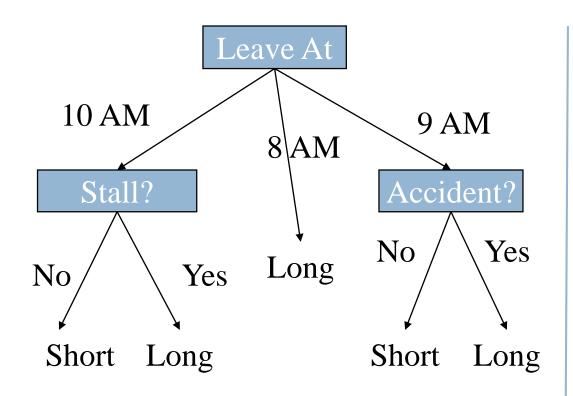
Leave = 8 AM Accident = Yes Weather = Rainy Stall = No Tree with internal nodes labeled by features

Branches are labeled by tests on that feature



Leave = 8 AM Accident = Yes Weather = Rainy Stall = No Tree with internal nodes labeled by features

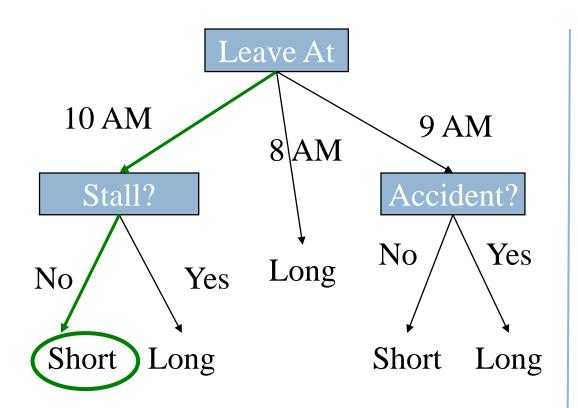
Branches are labeled by tests on that feature



Leave = 10 AM Accident = No Weather = Rainy Stall = No

Tree with internal nodes labeled by features

Branches are labeled by tests on that feature



Leave = 10 AM Accident = No Weather = Rainy Stall = No

Tree with internal nodes labeled by features

Branches are labeled by tests on that feature

# To ride or not to ride, that is the question...

Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Normal	Rainy	NO
Road	Normal	Sunny	YES
Trail	Mountain	Sunny	YES
Road	Mountain	Rainy	YES
Trail	Normal	Snowy	NO
Road	Normal	Rainy	YES
Road	Mountain	Snowy	YES
Trail	Normal	Sunny	NO
Road	Normal	Snowy	NO
Trail	Mountain	Snowy	YES

Build a decision tree

# Recursive approach

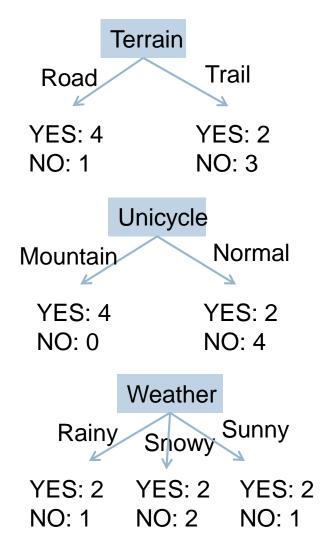
Base case: If all data belong to the same class, create a leaf node with that label

#### Otherwise:

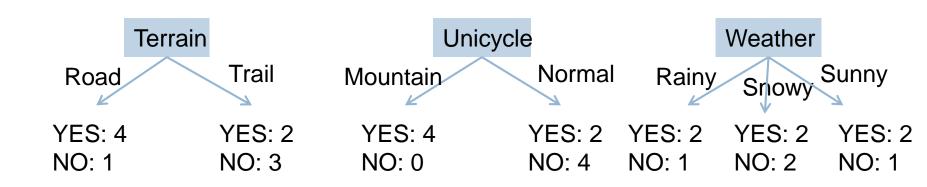
- calculate the "score" for each feature if we used it to split the data
- pick the feature with the highest score, partition the data based on that data value and call recursively

# Partitioning the data

Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Normal	Rainy	NO
Road	Normal	Sunny	YES
Trail	Mountain	Sunny	YES
Road	Mountain	Rainy	YES
Trail	Normal	Snowy	NO
Road	Normal	Rainy	YES
Road	Mountain	Snowy	YES
Trail	Normal	Sunny	NO
Road	Normal	Snowy	NO
Trail	Mountain	Snowy	YES



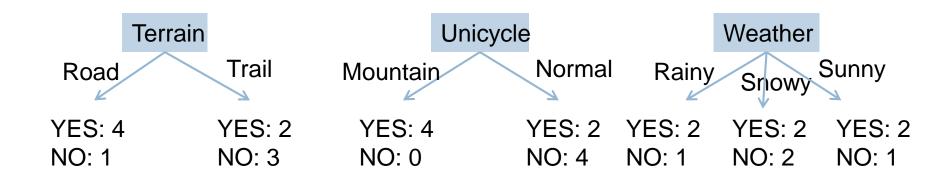
# Partitioning the data



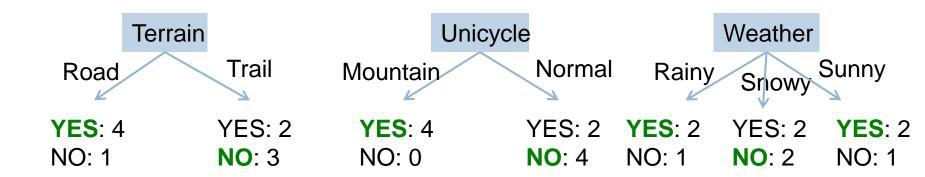
calculate the "score" for each feature if we used it to split the data

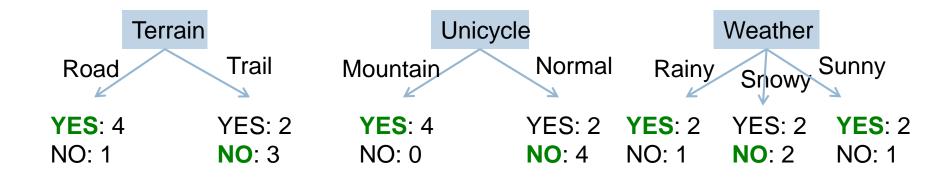
What score should we use?

If we just stopped here, which tree would be best? How could we make these into decision trees?



How could we make these into decision trees?

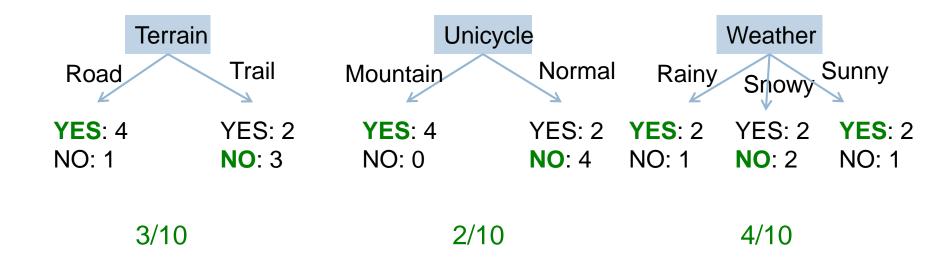




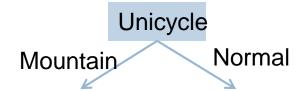
Training error: the average error over the training set

For classification, the most common "error" is the number of mistakes

Training error for each of these?



Training error: the average error over the training set



YES: 4

NO: 0

YES: 2

NO: 4

Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Mountain	Sunny	YES
Road	Mountain	Rainy	YES
Road	Mountain	Snowy	YES
Trail	Mountain	Snowy	YES

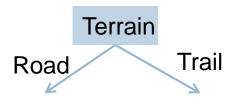
Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Normal	Rainy	NO
Road	Normal	Sunny	YES
Trail	Normal	Snowy	NO
Road	Normal	Rainy	YES
Trail	Normal	Sunny	NO
Road	Normal	Snowy	NO

Unicycle Mountain Normal

**YES**: 4 YES: 2

NO: 0 NO: 4

Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Normal	Rainy	NO
Road	Normal	Sunny	YES
Trail	Normal	Snowy	NO
Road	Normal	Rainy	YES
Trail	Normal	Sunny	NO
Road	Normal	Snowy	NO



YES: 2 YES: 0 NO: 1 NO: 3

Weather
Rainy Snowy Sunny

YES: 1 YES: 0 YES: 1

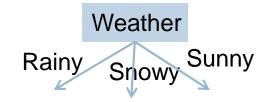
NO: 1 NO: 2 NO: 1

Unicycle Mountain Normal

**YES**: 4 YES: 2 NO: 4

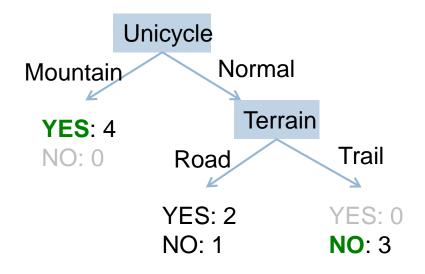
**Terrain** Unicycle-Weather Go-For-Ride? type Normal Trail Rainy NO **Normal** Road YES Sunny Trail Normal Snowy NO Road Normal Rainy YES Trail Normal Sunny NO Road Normal Snowy NO

Terrain
Road Trail
YES: 2
NO: 1
NO: 3

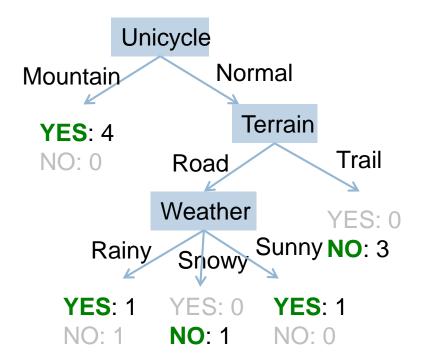


**YES**: 1 YES: 0 **YES**: 1 NO: 1 **NO**: 2 NO: 1

2/6



Terrain	Unicycle- type	Weather	Go-For- Ride?
Road	Normal	Sunny	YES
Road	Normal	Rainy	YES
Road	Normal	Snowy	NO



## Building decision trees

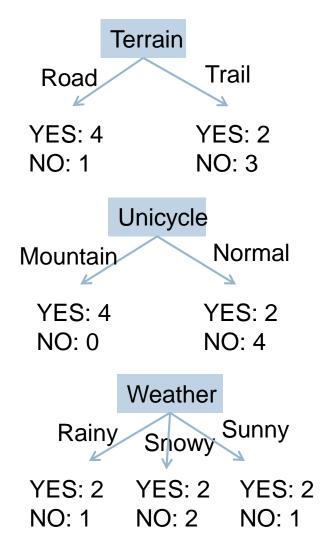
Base case: If all data belong to the same class, create a leaf node with that label

#### Otherwise:

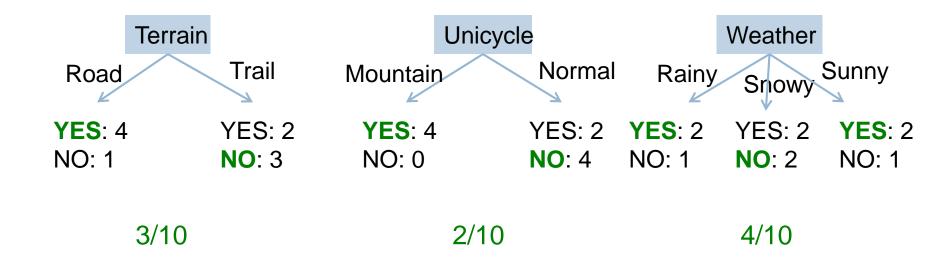
- calculate the "score" for each feature if we used it to split the data
- pick the feature with the highest score, partition the data based on that data value and call recursively

## Partitioning the data

Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Normal	Rainy	NO
Road	Normal	Sunny	YES
Trail	Mountain	Sunny	YES
Road	Mountain	Rainy	YES
Trail	Normal	Snowy	NO
Road	Normal	Rainy	YES
Road	Mountain	Snowy	YES
Trail	Normal	Sunny	NO
Road	Normal	Snowy	NO
Trail	Mountain	Snowy	YES

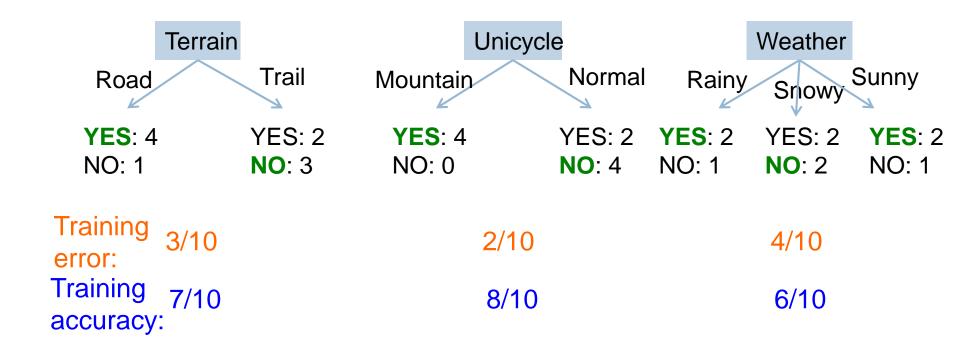


#### Decision trees



Training error: the average error over the training set

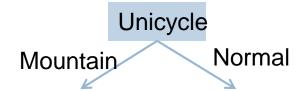
## Training error vs. accuracy



training error = 1-accuracy (and vice versa)

Training error: the average error over the training set

Training accuracy: the average percent correct over the training set



YES: 4

NO: 0

YES: 2

NO: 4

Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Mountain	Sunny	YES
Road	Mountain	Rainy	YES
Road	Mountain	Snowy	YES
Trail	Mountain	Snowy	YES

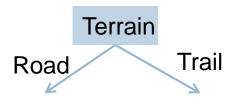
Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Normal	Rainy	NO
Road	Normal	Sunny	YES
Trail	Normal	Snowy	NO
Road	Normal	Rainy	YES
Trail	Normal	Sunny	NO
Road	Normal	Snowy	NO

Unicycle Mountain Normal

**YES**: 4 YES: 2

NO: 0 NO: 4

Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Normal	Rainy	NO
Road	Normal	Sunny	YES
Trail	Normal	Snowy	NO
Road	Normal	Rainy	YES
Trail	Normal	Sunny	NO
Road	Normal	Snowy	NO



YES: 2 YES: 0 NO: 1 NO: 3

Weather
Rainy Snowy Sunny

YES: 1 YES: 0 YES: 1

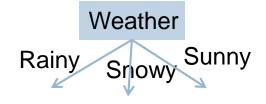
NO: 1 NO: 2 NO: 1

Unicycle Mountain Normal

**YES**: 4 YES: 2 NO: 4

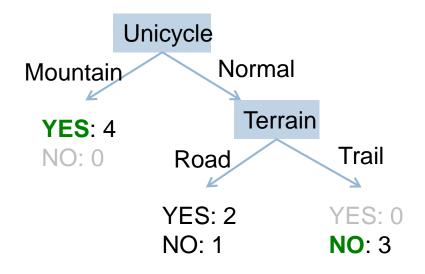
**Terrain** Unicycle-Weather Go-For-Ride? type Normal Trail Rainy NO **Normal** Road YES Sunny Trail Normal Snowy NO Road Normal Rainy YES Trail Normal Sunny NO Road Normal Snowy NO

Terrain
Road Trail
YES: 2
NO: 1
NO: 3

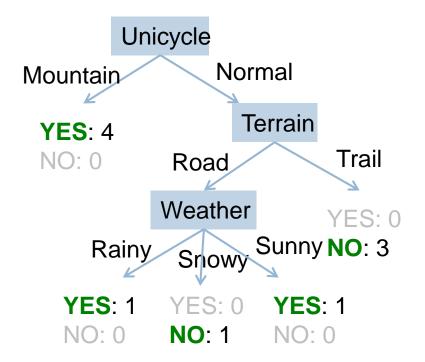


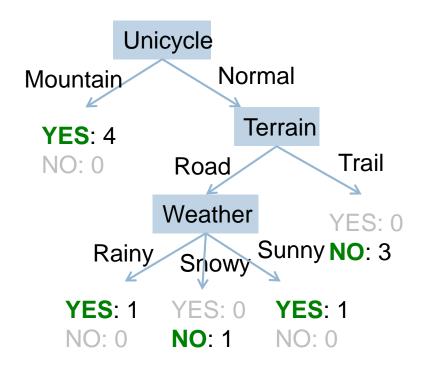
**YES**: 1 YES: 0 **YES**: 1 NO: 1 **NO**: 2 NO: 1

2/6



Terrain	Unicycle- type	Weather	Go-For- Ride?
Road	Normal	Sunny	YES
Road	Normal	Rainy	YES
Road	Normal	Snowy	NO





Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Normal	Rainy	NO
Road	Normal	Sunny	YES
Trail	Mountain	Sunny	YES
Road	Mountain	Rainy	YES
Trail	Normal	Snowy	NO
Road	Normal	Rainy	YES
Road	Mountain	Snowy	YES
Trail	Normal	Sunny	NO
Road	Normal	Snowy	NO
Trail	Mountain	Snowy	YES

Are we always guaranteed to get a training error of 0?

Training error?

#### Problematic data

Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Normal	Rainy	NO
Road	Normal	Sunny	YES
Trail	Mountain	Sunny	YES
Road	Mountain	Snowy	NO
Trail	Normal	Snowy	NO
Road	Normal	Rainy	YES
Road	Mountain	Snowy	YES
Trail	Normal	Sunny	NO
Road	Normal	Snowy	NO
Trail	Mountain	Snowy	YES

When can this happen?

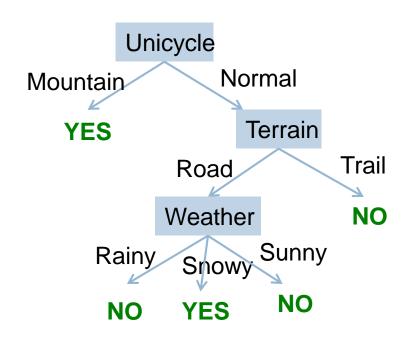
## Recursive approach

Base case: If all data belong to the same class, create a leaf node with that label *OR* all the data has the same feature values

Do we always want to go all the way to the bottom?

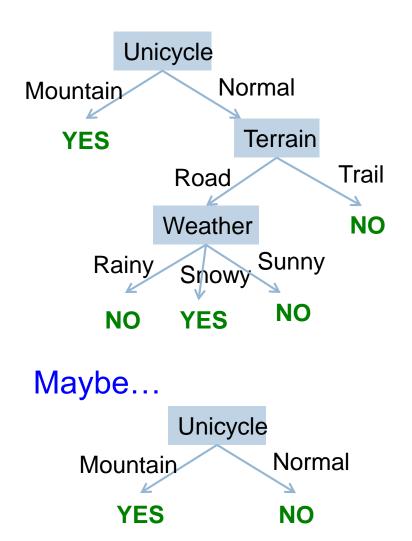
Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Mountain	Rainy	YES
Trail	Mountain	Sunny	YES
Road	Mountain	Snowy	YES
Road	Mountain	Sunny	YES
Trail	Normal	Snowy	NO
Trail	Normal	Rainy	NO
Road	Normal	Snowy	YES
Road	Normal	Sunny	NO
Trail	Normal	Sunny	NO

Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Mountain	Rainy	YES
Trail	Mountain	Sunny	YES
Road	Mountain	Snowy	YES
Road	Mountain	Sunny	YES
Trail	Normal	Snowy	NO
Trail	Normal	Rainy	NO
Road	Normal	Snowy	YES
Road	Normal	Sunny	NO
Trail	Normal	Sunny	NO



Is that what you would do?

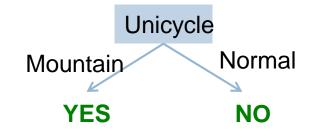
Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Mountain	Rainy	YES
Trail	Mountain	Sunny	YES
Road	Mountain	Snowy	YES
Road	Mountain	Sunny	YES
Trail	Normal	Snowy	NO
Trail	Normal	Rainy	NO
Road	Normal	Snowy	YES
Road	Normal	Sunny	NO
Trail	Normal	Sunny	NO



Terrain	Unicycle-type	Weather	Jacket	ML grade	Go-For-Ride?
Trail	Mountain	Rainy	Heavy	D	YES
Trail	Mountain	Sunny	Light	C-	YES
Road	Mountain	Snowy	Light	В	YES
Road	Mountain	Sunny	Heavy	Α	YES
	Mountain				YES
Trail	Normal	Snowy	Light	D+	NO
Trail	Normal	Rainy	Heavy	B-	NO
Road	Normal	Snowy	Heavy	C+	YES
Road	Normal	Sunny	Light	A-	NO
Trail	Normal	Sunny	Heavy	B+	NO
Trail	Normal	Snowy	Light	F	NO
	Normal				NO
Trail	Normal	Rainy	Light	С	YES

## Overfitting

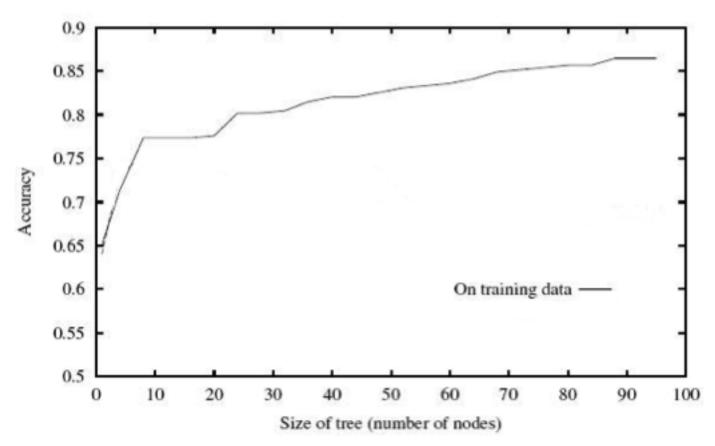
Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Mountain	Rainy	YES
Trail	Mountain	Sunny	YES
Road	Mountain	Snowy	YES
Road	Mountain	Sunny	YES
Trail	Normal	Snowy	NO
Trail	Normal	Rainy	NO
Road	Normal	Snowy	YES
Road	Normal	Sunny	NO
Trail	Normal	Sunny	NO



Overfitting occurs when we bias our model too much towards the training data

Our goal is to learn a **general** model that will work on the training data as well as other data (i.e. test data)

## Overfitting

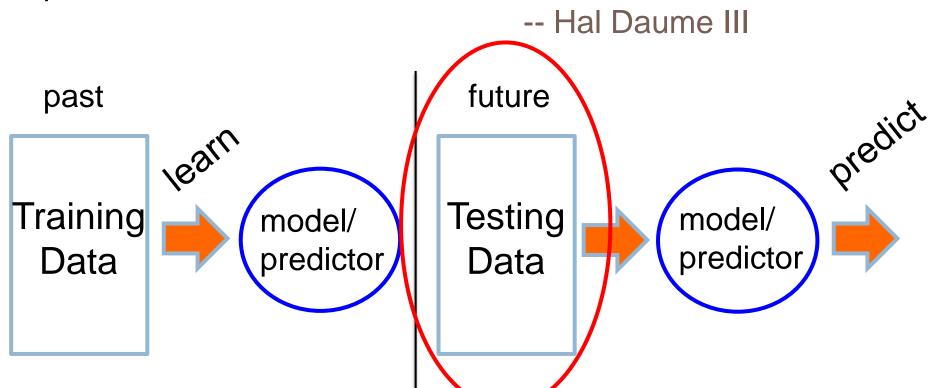


Our decision tree learning procedure always decreases training error

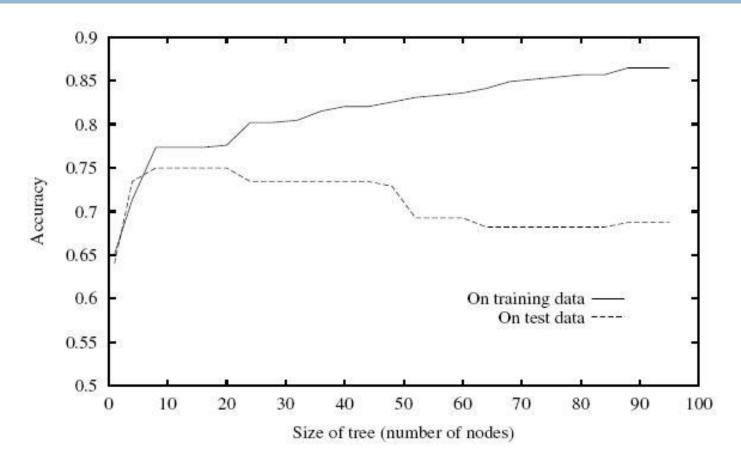
Is that what we want?

#### Test set error!

Machine learning is about predicting the future based on the past.



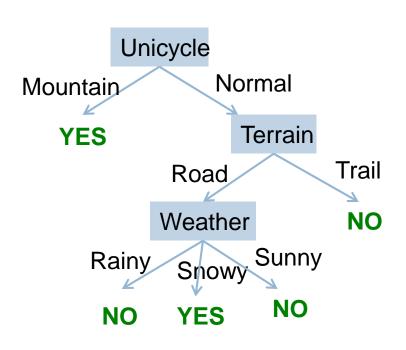
## Overfitting



Even though the training error is decreasing, the testing error can go up!

## Overfitting

Terrain	Unicycle- type	Weather	Go-For- Ride?
Trail	Mountain	Rainy	YES
Trail	Mountain	Sunny	YES
Road	Mountain	Snowy	YES
Road	Mountain	Sunny	YES
Trail	Normal	Snowy	NO
Trail	Normal	Rainy	NO
Road	Normal	Snowy	YES
Road	Normal	Sunny	NO
Trail	Normal	Sunny	NO



How do we prevent overfitting?

## Preventing overfitting

Base case: If all data belong to the same class, create a leaf node with that label *OR* all the data has the same feature values *OR* 

- We've reached a particular depth in the tree
- ?

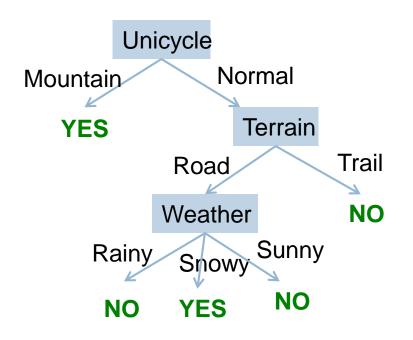
One idea: stop building the tree early

## Preventing overfitting

Base case: If all data belong to the same class, create a leaf node with that label *OR* all the data has the same feature values *OR* 

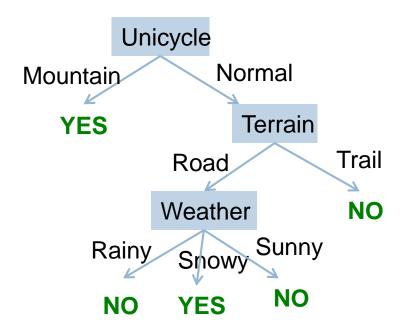
- We've reached a particular depth in the tree
- We only have a certain number/fraction of examples remaining
- We've reached a particular training error
- Use development data (more on this later)

- ...

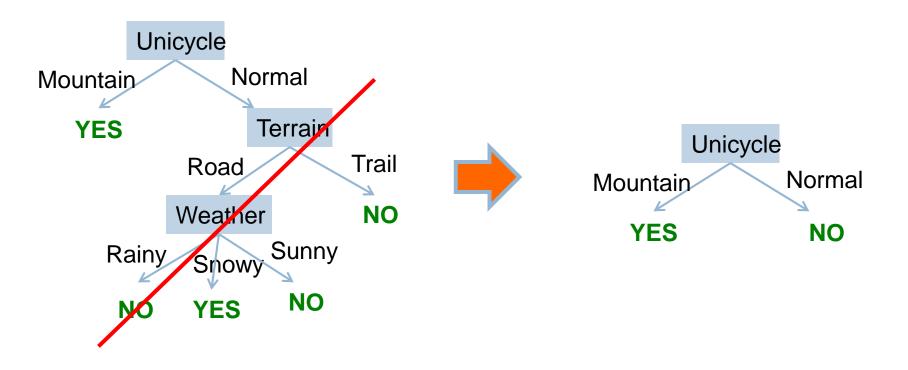


Pruning: after the tree is built, go back and "prune" the tree, i.e. remove some lower parts of the tree

Similar to stopping early, but done after the entire tree is built

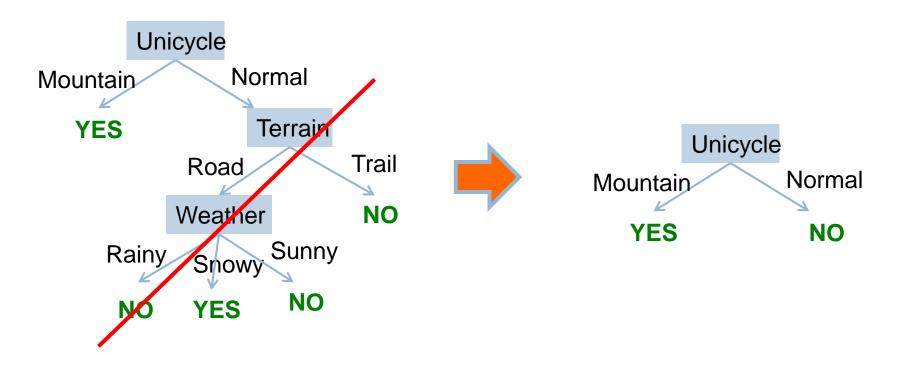


Build the full tree



Build the full tree

Prune back leaves that are too specific



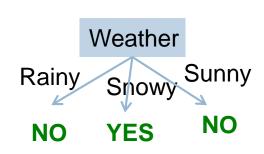
Pruning criterion?

## Handling non-binary attributes

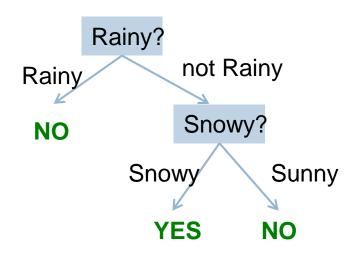
PassengerId	Polace	Sex	Age	SibSp	Parch	Ticket	Fare	Embarked	Survived
804	3			•	1			O	
					1			0	1
756	2	0	0.67		1	250649		2	1
470	3	1	0.75	2	1	2666	19.2583	0	1
645	3	1	0.75	2	1	. 2666	19.2583	0	1
79	2	0	0.83	0	2	248738	29	2	1
832	2	0	0.83	1	1	29106	18.75	2	1
306	1	0	0.92	. 1	2	113781	151.55	2	1
165	3	0	1	. 4	1	3101295	39.6875	2	0
173	3	1	1	. 1	1	347742	11.1333	2	1
184	2	0	1	. 2	1	230136	39	2	1
382	3	1	1	. 0	2	2653	15.7417	0	1
387	3	0	1	. 5	2	2144	46.9	2	0
789	3	0	1	. 1	2	2315	20.575	2	1
828	2	0	1	. 0	2	2079	37.0042	0	1
8	3	0	2	2 3	1	349909	21.075	2	0
17	3	0	2	2 4	1	382652	29.125	1	0
120	3	1	2	2 4	2	347082	31.275	2	0
206	3	1	2	2 0	1	347054	10.4625	2	0
298	1	1	2	. 1	2	113781	151.55	2	0
341	2	0	2	. 1	1	230080	26	2	1
480	3	1	2	2 0	1	3101298	12.2875	2	1

What do we do with features that have multiple values? Real-values?

### Features with multiple values



Treat as an n-ary split

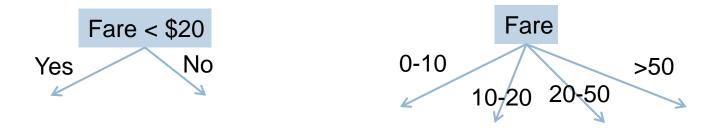


Treat as multiple binary splits

#### Real-valued features

Use any comparison test (>, <, ≤, ≥) to split the data into two parts

Select a range filter, i.e. min < value < max



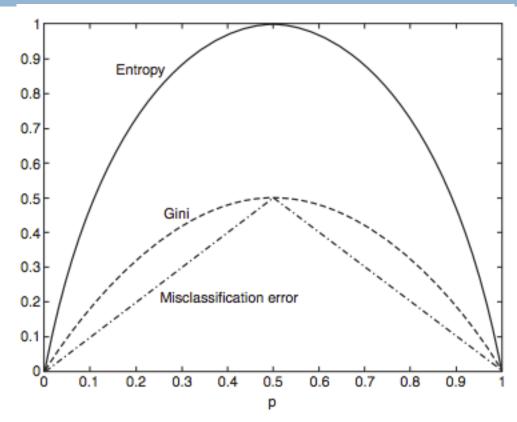
## Other splitting criterion

#### Otherwise:

- calculate the "score" for each feature if we used it to split the data
- pick the feature with the highest score, partition the data based on that data value and call recursively

We used training error for the score. Any other ideas?

## Other splitting criterion



- Entropy: how much uncertainty there is in the distribution over labels after the split
- Gini: sum of the square of the label proportions after split
- Training error = misclassification error

### Decision trees

#### Good? Bad?



## Decision trees: the good

Very intuitive and easy to interpret

Fast to run and fairly easy to implement (Assignment 2 ©)

Historically, perform fairly well (especially with a few more tricks we'll see later on)

No prior assumptions about the data

#### Decision trees: the bad

#### Be careful with features with lots of values

Which feature would be at the top here?

ID	Terrain	Unicycle- type	Weather	Go-For- Ride?
1	Trail	Normal	Rainy	NO
2	Road	Normal	Sunny	YES
3	Trail	Mountain	Sunny	YES
4	Road	Mountain	Rainy	YES
5	Trail	Normal	Snowy	NO
6	Road	Normal	Rainy	YES
7	Road	Mountain	Snowy	YES
8	Trail	Normal	Sunny	NO
9	Road	Normal	Snowy	NO
10	Trail	Mountain	Snowy	YES

#### Decision trees: the bad

Can be problematic (slow, bad performance) with large numbers of features

Can't learn some very simple data sets (e.g. some types of linearly separable data)

Pruning/tuning can be tricky to get right

## Final DT algorithm

#### Base cases:

- If all data belong to the same class, pick that label
- If all the data have the same feature values, pick majority label
- If we're out of features to examine, pick majority label
- If the we don't have any data left, pick majority label of *parent*
- 5. If some other stopping criteria exists to avoid overfitting, pick majority label

#### Otherwise:

- calculate the "score" for each feature if we used it to split the data
- pick the feature with the highest score, partition the data based on that data value and call recursively

# Alternative Score Calculation – Information Gain

- Why information gain is better over accuracy?
  - Decision trees are generally prone to over-fitting and accuracy doesn't generalize well to unseen data.
  - One advantage of information gain is that -- due to the factor ¬p\*log(p) in the entropy definition -- leafs with a small number of instances are assigned less weight (limp→0+p\*log(p)=0) and it favors dividing data into bigger but homogeneous groups.
  - This approach is usually more stable and also chooses the most impactful features close to the root of the tree.

To illustrate, imagine the task of <u>learning</u> to <u>classify</u> first-names into male/female groups. That is given a list of names each labeled with either m or f, we want to learn a <u>model</u> that fits the data and can be used to predict the gender of a new unseen first-name.

First step is <u>deciding</u> what <u>features</u> of the data are relevant to the target class we want to predict. Some example features include: first/last letter, length, number of vowels, does it end with a vowel, etc.. So after feature extraction, our data looks like:

Ashley	1	3	6	f
Brian	0	2	5	m
Caroline	1	4	8	f
David	0	2	5	m

The goal is to build a <u>decision tree</u>. An example of a <u>tree</u> would be:

```
length<7
| num-vowels<3: male
| num-vowels>=3
| ends-vowel=1: female
| ends-vowel=0: male
length>=7
| length=5: male
```

basically each node represent a test performed on a single attribute, and we go left or right depending on the result of the test. We keep traversing the tree until we reach a leaf node which contains the class prediction ( m or f )

So if we run the name *Amro* down this tree, we start by testing "is the length<7?" and the answer is yes, so we go down that branch. Following the branch, the next test "is the number of vowels<3?" again evaluates to true. This leads to a leaf node labeled m, and thus the prediction is male (which I happen to be, so the tree predicted the outcome correctly).

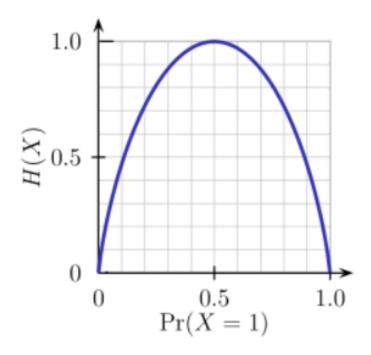
The decision tree is <u>built in a top-down fashion</u>, but the question is how do you choose which attribute to split at each node? The answer is find the feature that best splits the target class into the purest possible children nodes (ie: nodes that don't contain a mix of both male and female, rather pure nodes with only one class).

This measure of *purity* is called the <u>information</u>. It represents the <u>expected</u> amount of <u>information</u> that would be needed to specify whether a new instance (first-name) should be classified male or female, given the example that reached the node. We calculate it based on the number of male and female classes at the node.

**Entropy** on the other hand is a measure of *impurity* (the opposite). It is defined for a <u>binary class</u> with values a / b as:

Entropy = - 
$$p(a)*log(p(a)) - p(b)*log(p(b))$$

This <u>binary entropy function</u> is depicted in the figure below (random variable can take one of two values). It reaches its maximum when the probability is p=1/2, meaning that p(X=a)=0.5 or similarly p(X=b)=0.5 having a 50%/50% chance of being either a or b (uncertainty is at a maximum). The entropy function is at zero minimum when probability is p=1 or p=0 with complete certainty (p(X=a)=1 or p(X=a)=0 respectively, latter implies p(X=b)=1).



Of course the definition of entropy can be generalized for a discrete random variable X with N outcomes (not just two):

$$H(X) = -\sum_{i=1}^{n} p(x_i) \log_b p(x_i)$$

(the Log in the formula is usually taken as the logarithm to the base 2)

Back to our task of name classification, lets look at an example. Imagine at some point during the process of constructing the tree, we were considering the following split:

As you can see, before the split we had 9 males and 5 females, i.e. P(m)=9/14 and P(f)=5/14. According to the definition of entropy:

```
Entropy_before = -(5/14)*log2(5/14) - (9/14)*log2(9/14) = 0.9403
```

Next we compare it with the entropy computed after considering the split by looking at two child branches. In the left branch of ends-vowel=1, we have:

```
Entropy_left = -(3/7)*log2(3/7) - (4/7)*log2(4/7) = 0.9852
```

and the right branch of ends-vowel=0, we have:

```
Entropy_right = -(6/7)*log2(6/7) - (1/7)*log2(1/7) = 0.5917
```

We combine the left/right entropies using the number of instances down each branch as <u>weight</u> <u>factor</u> (7 instances went left, and 7 instances went right), and get the final entropy after the split:

```
Entropy_after = 7/14*Entropy_left + 7/14*Entropy_right = 0.7885
```

## Information Gain Example

Now by comparing the entropy before and after the split, we obtain a measure of <u>information gain</u>, or how much information we gained by doing the split using that particular feature:

```
Information_Gain = Entropy_before - Entropy_after = 0.1518
```

You can interpret the above calculation as following: by doing the split with the end-vowels feature, we were able to reduce uncertainty in the sub-tree prediction outcome by a small amount of 0.1518 (measured in bits as units of information).

At each node of the tree, this calculation is performed for every feature, and the feature with the *largest information gain* is chosen for the split in a <u>greedy</u> manner (thus favoring features that produce *pure* splits with low uncertainty/entropy). This process is applied recursively from the root-node down, and stops when a leaf node contains instances all having the same class (no need to split it further).

Note that I skipped over some <u>details</u> which are beyond the scope of this post, including how to handle <u>numeric features</u>, <u>missing values</u>, <u>overfitting</u> and <u>pruning</u> trees, etc..

#### Source of Information Gain Example >

https://stackoverflow.com/questions/1859554/what-is-entropy-and-information-gain