



# Data acquisition and conversion

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- Introduction
- Sampling
- Signal reconstruction
- Data converters
- Sample and hold gates
- Multiplexing





28.1

# Introduction

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- Digital techniques have several advantages over analogue methods:
  - They are less affected by noise
  - Processing, transmission and storage is often easier
- However, we often produce or use analogue signals
- Therefore, we often have the need to translate between analogue and digital representations

28.2

# The sampling system

Abbreviations:

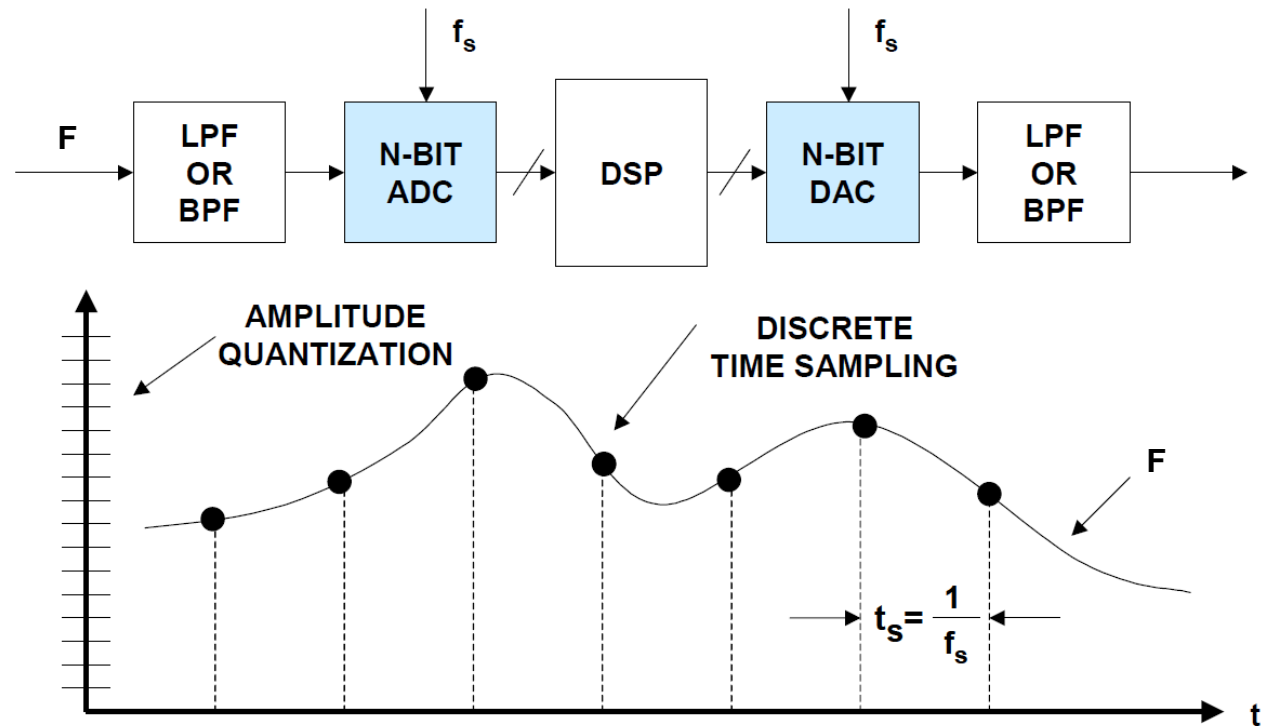
LPF = low pass filter

BPF = band pass filter

ADC = analogue to digital converter

DSP = digital signal processor

DAC = digital to analogue converter



Signal with maximum frequency  $F$  is filtered, sampled at frequency  $f_s$ , digitized, stored and then output as an analogue signal that is filtered.

28.3

# The sampling system

Have talked about the DSP  
Now we will first talk about the sampling  
and the filters  
Then the ADC/DAC

Abbreviations:

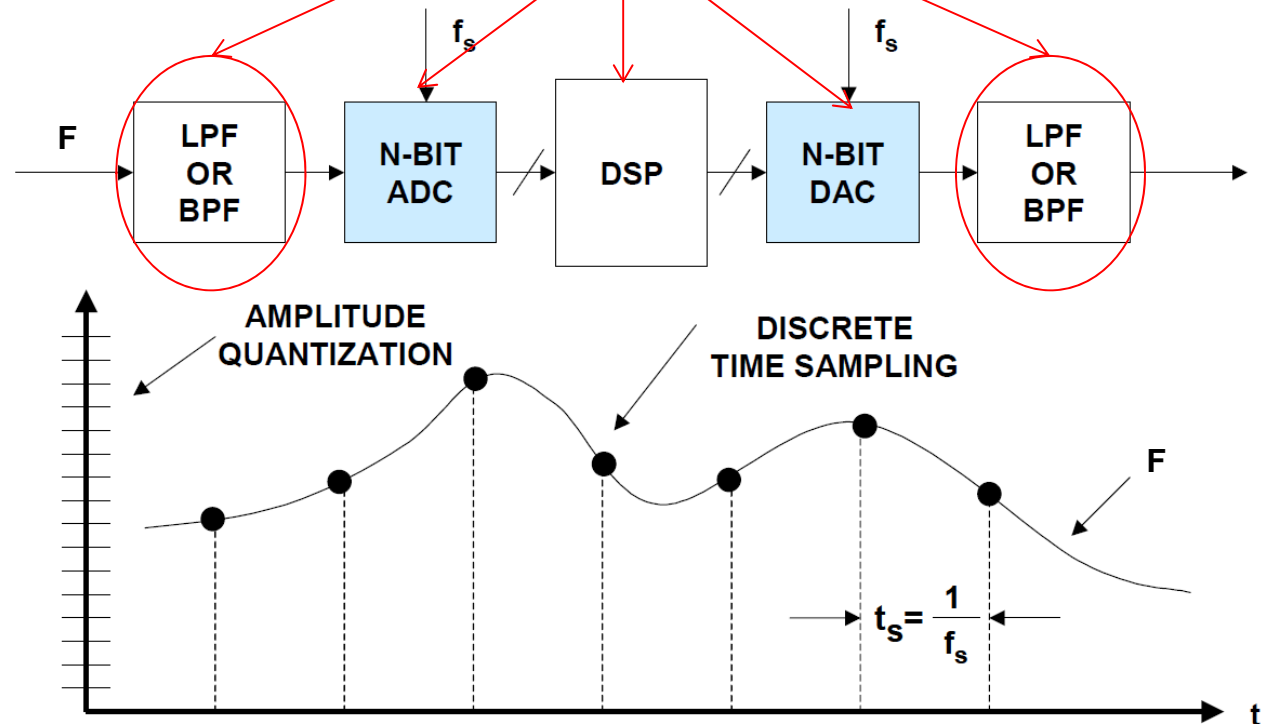
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28.4



Video 28A



28.2

## Why the filters: Sampling

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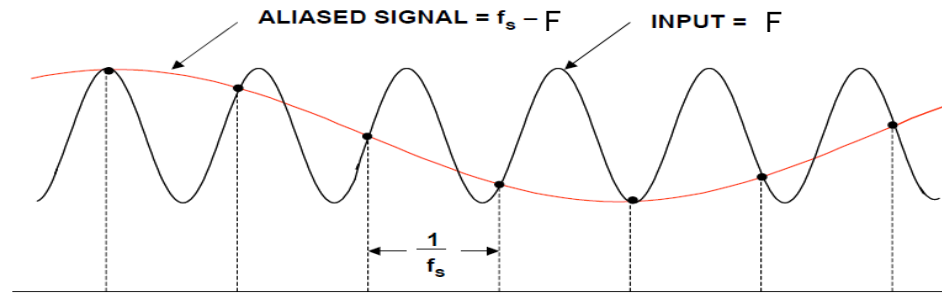
- In order to obtain a picture of a varying quantity we need to take regular measurements
  - this process is called **sampling**
  - but how often do we need to sample?

- The answer is given by the **Nyquist sampling theorem** which says that:

*the sampling rate must be greater than twice the highest frequency present in the signal being sampled.*

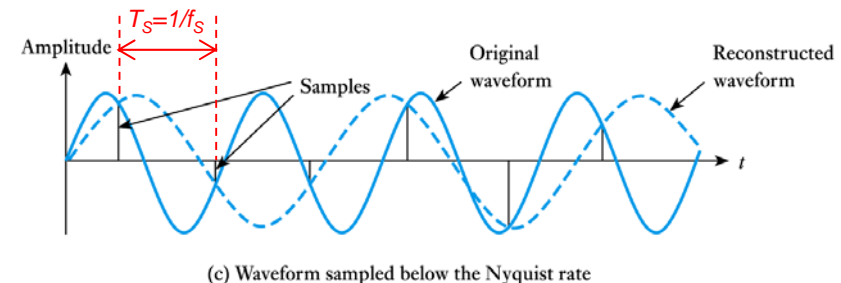
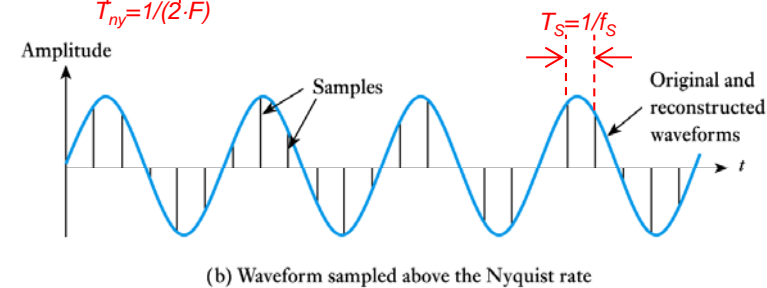
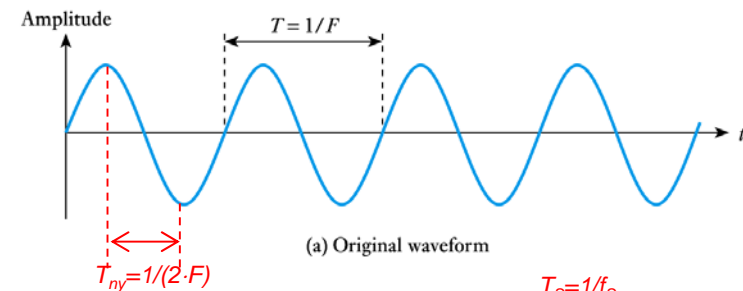
- this minimum sampling rate is the **Nyquist rate**

28.5



So a high-frequency signal at  $F$  is read as a low frequency signal at  $f_s - F$

- The effects of sampling rate are illustrated here:
    - (a) shows the original signal
    - (b) shows the effects of sampling at a rate *above* the Nyquist rate
    - (c) shows the effects of sampling at a rate *below* the Nyquist rate ( $f_{ny} = F/2$ )
    - (d) Sample at the frequency of the sine wave,  $F$ , interpret as  $f=0$  again!
- Second harmonic



# “Negative” frequencies or harmonics

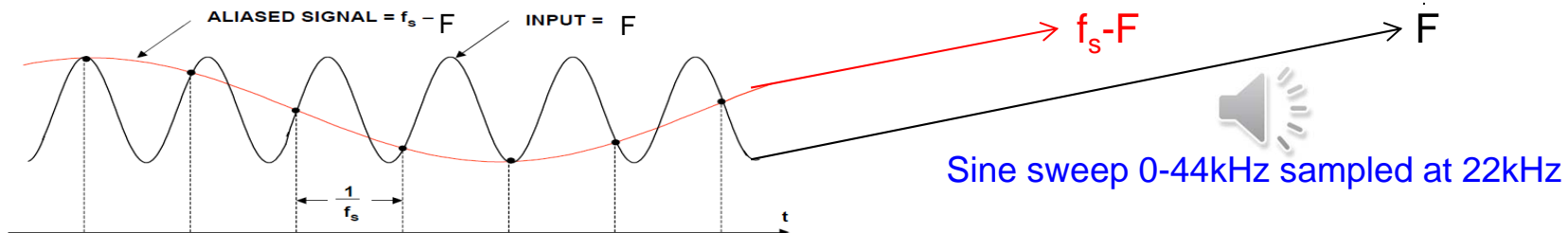
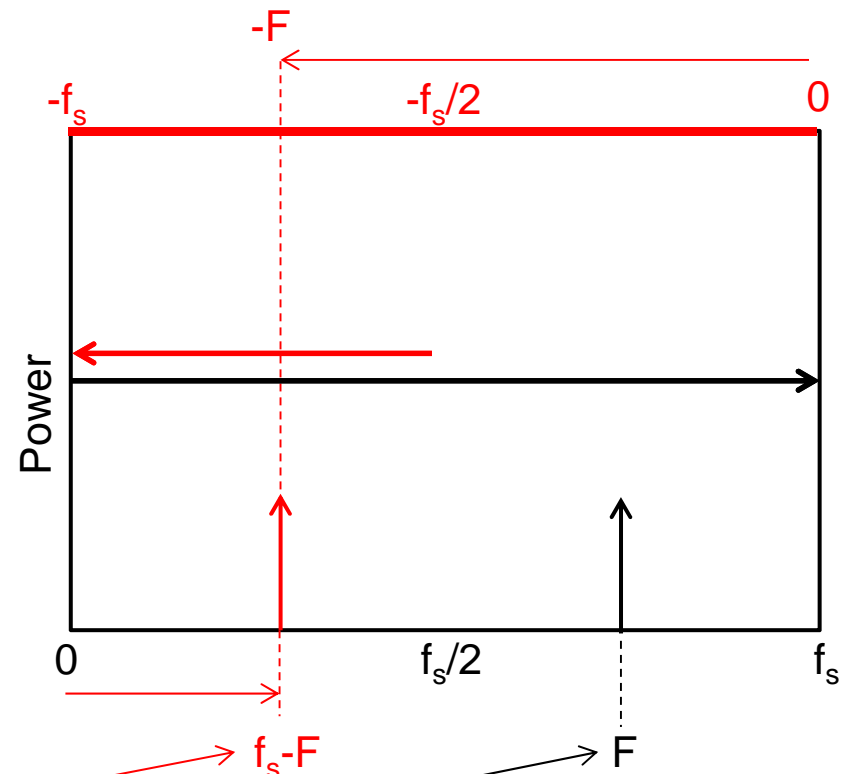
## Fourier Transform

Shows power vs. frequency of sine wave at frequency  $F$

Add a reverse scale of negative frequencies

A sine wave with high, negative frequency  $-F$

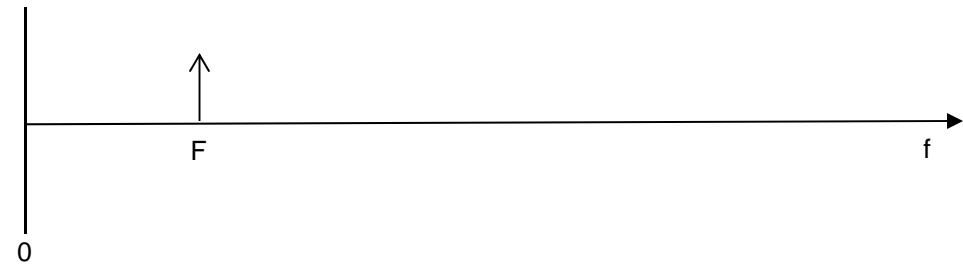
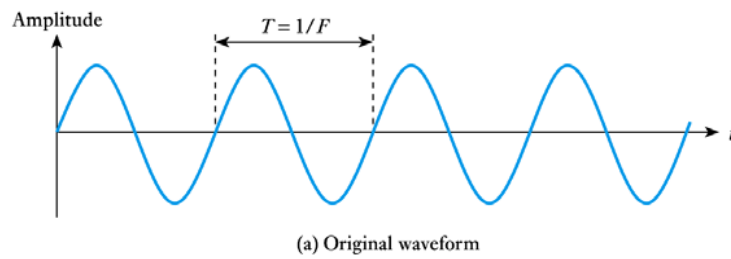
Is heard as a low frequency sine wave at  $f_s - F$



Sine sweep 0-44kHz sampled at 22kHz

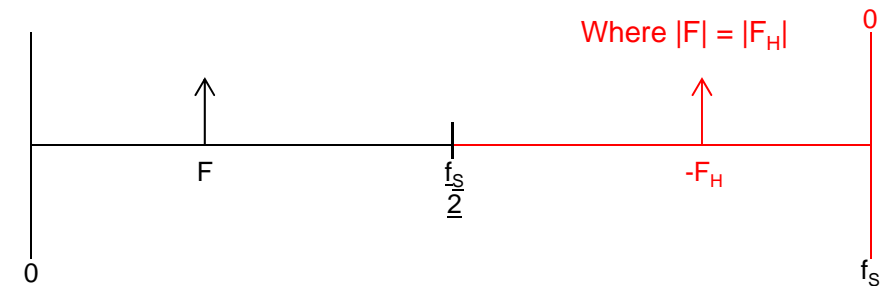
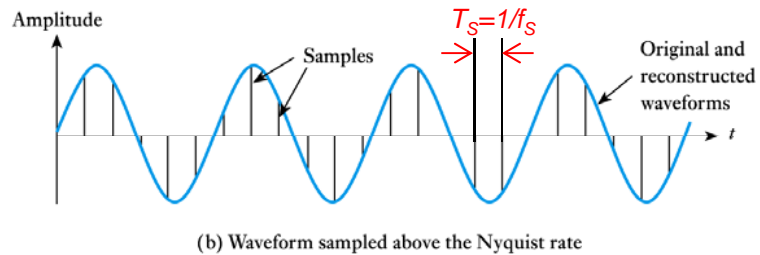
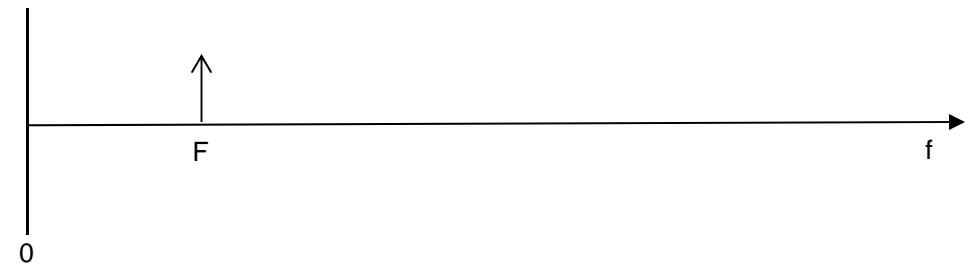
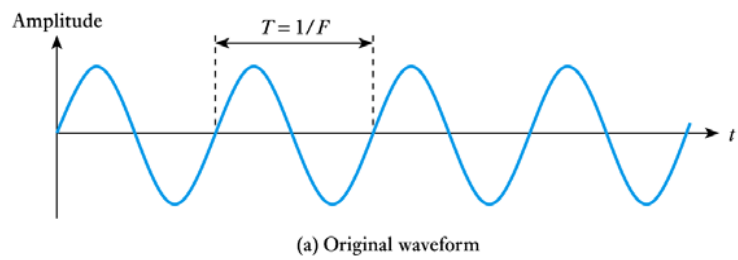
# How does this look in frequency?

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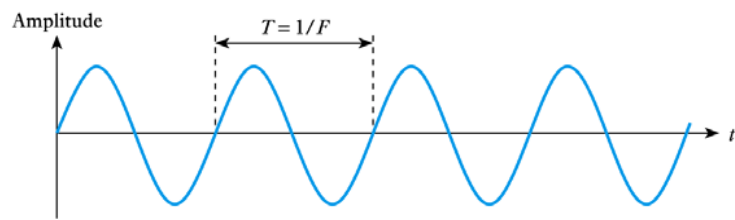




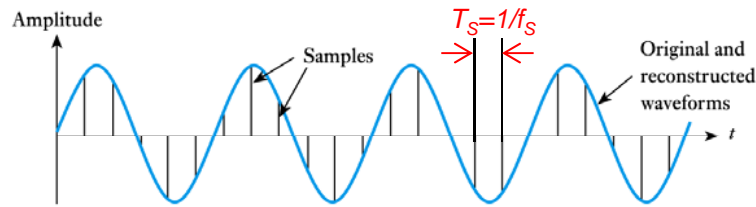
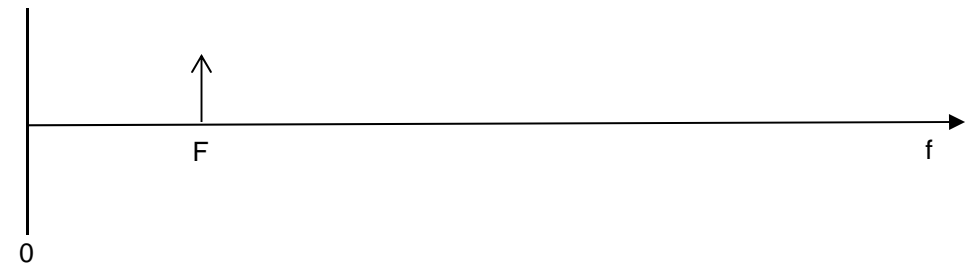
# How does this look in frequency?



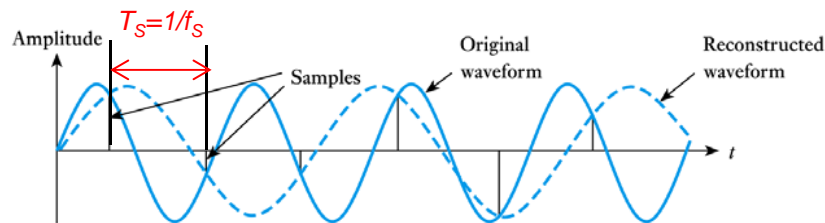
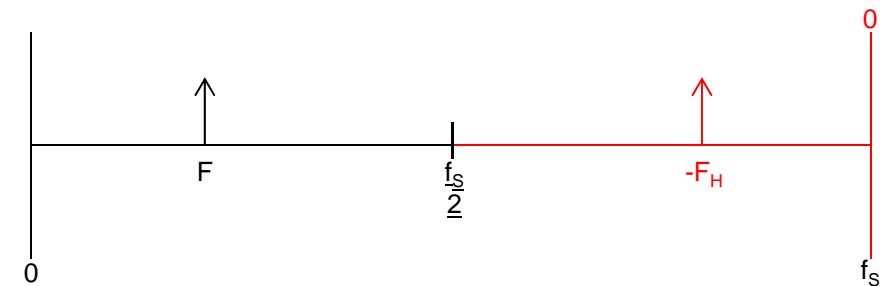
# How does this look in frequency?



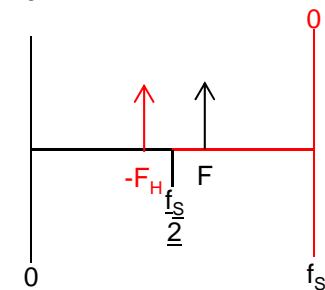
(a) Original waveform



(b) Waveform sampled above the Nyquist rate



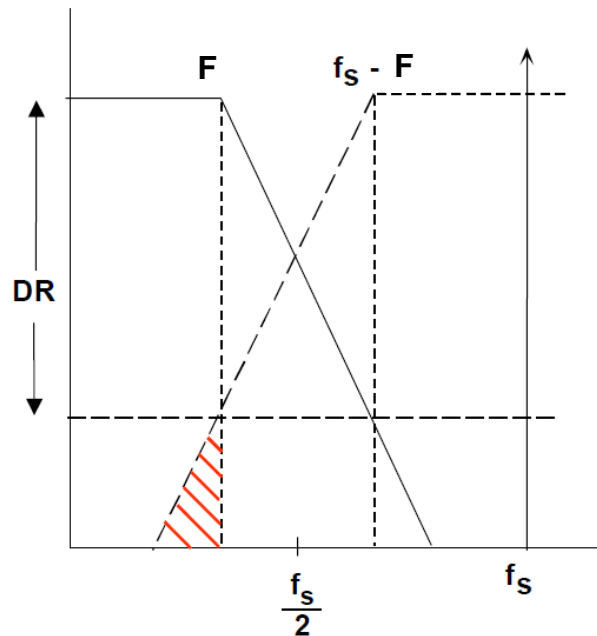
(c) Waveform sampled below the Nyquist rate



Now the 1<sup>st</sup> harmonic (at  $-F_H$ ) appears at  $f_a = f_s - F$   
It is "aliased" about the Nyquist frequency  $= f_s/2$   
We only really see  $0-f_{Ny}$

- 
- **Note:** the sampling rate is determined by the highest frequency present in the signal, *not* the highest frequency of interest
  - If a signal contains unwanted high frequency components, *we will see these as aliased frequencies*. So they should be removed before sampling
    - this is done using a low-pass filter
    - such a filter is called an **anti-aliasing filter**
  - It is common to sample at about 20% or more above the Nyquist rate to allow for imperfect filtering

## Example of filtering



STOPBAND ATTENUATION = DR  
TRANSITION BAND:  $F$  to  $f_s - F$   
CORNER FREQUENCY:  $F$

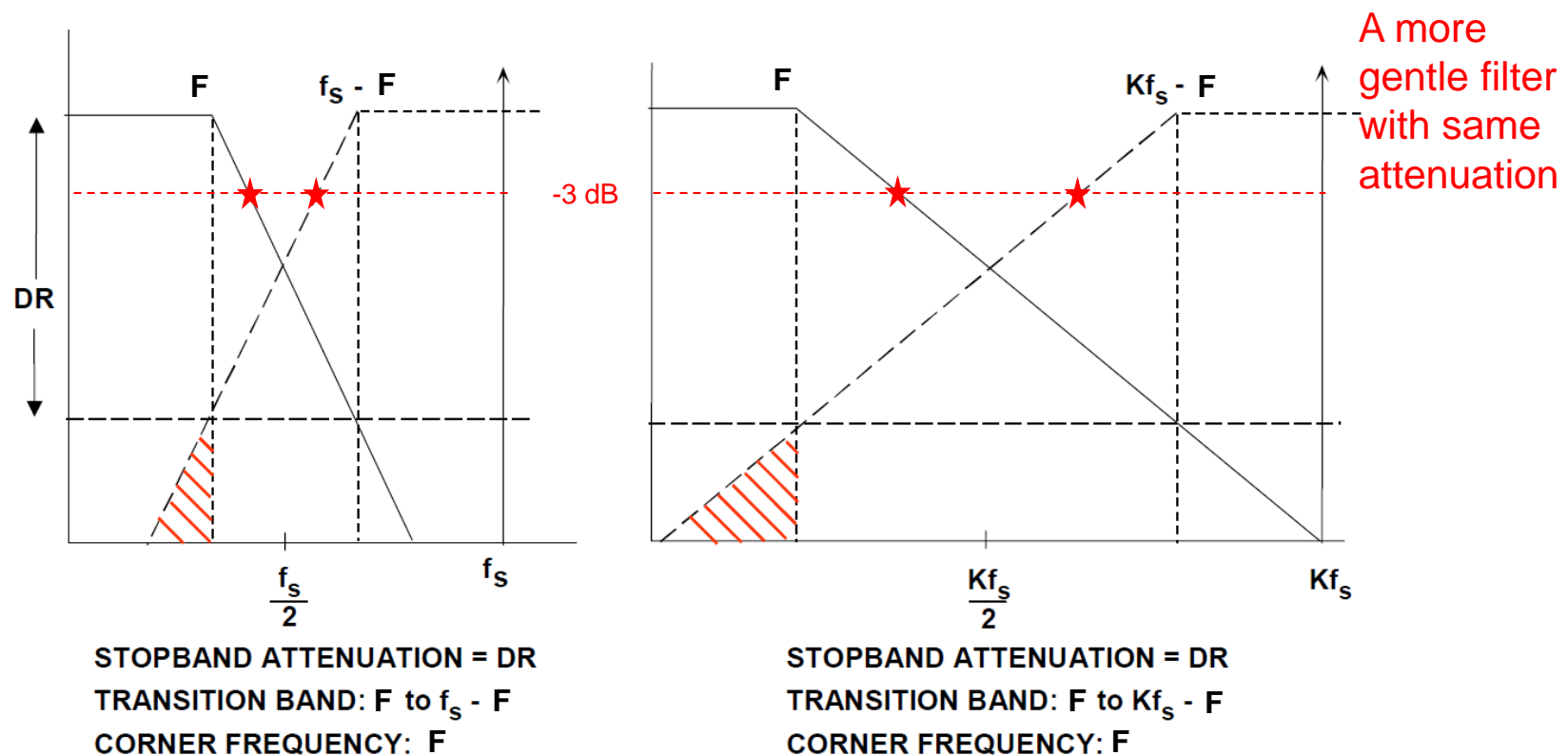
Specify the attenuation of the first harmonic in our “signal” band,  $0 \rightarrow F$ .  
( $F \approx 0.8 \cdot f_s / 2 = 0.8 \cdot f_{ny}$ )

Will still have those frequencies, but at an attenuation of DR.

Usually want as many frequencies as possible ( $F \rightarrow f_s / 2$ ), but that would require a sharp filter (“brick wall”),

Relax to  $\sim 80\%$  of  $f_{ny}$

# Example of filtering and “oversampling”

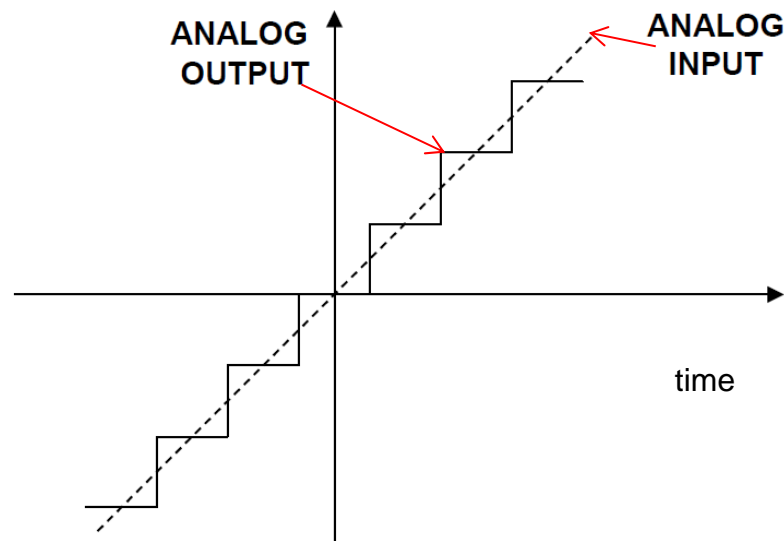


Remember, a LPF will have a  $-45^\circ$  phase shift at the -3 dB point  
 If you want the violin at the same time as the bass, move this as far out as possible

28.13

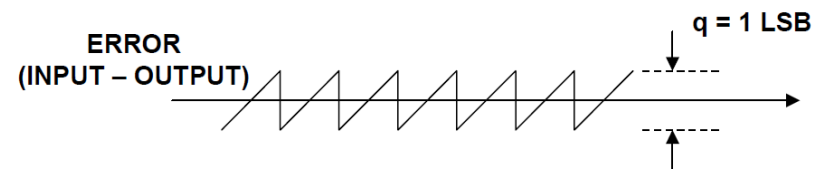
## Assume we have digitized and now want to follow steps to reconstruct the signal.

- Have anti-aliased the input (some band playing)
- Converted it to digital numbers (and stored on computer)
- Now reconvert to analogue signal (to play back on speakers)



The input ramp has been “quantized” into a digital signal

These “quanta” appear at the output giving us steps



28.14



28.3

## Signal reconstruction

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- In many cases it is necessary to reconstruct an analogue signal from a series of sample
  - typically after they have been processed, transmitted or stored
- This requires the removal of the step transitions in the sampled waveform (step  $\Rightarrow$  high frequencies)
- Reconstruction is achieved using a low-pass filter to remove these unwanted frequencies
  - this filter is called a **reconstruction filter**

28.15

# Hence, the sampling system

Abbreviations:

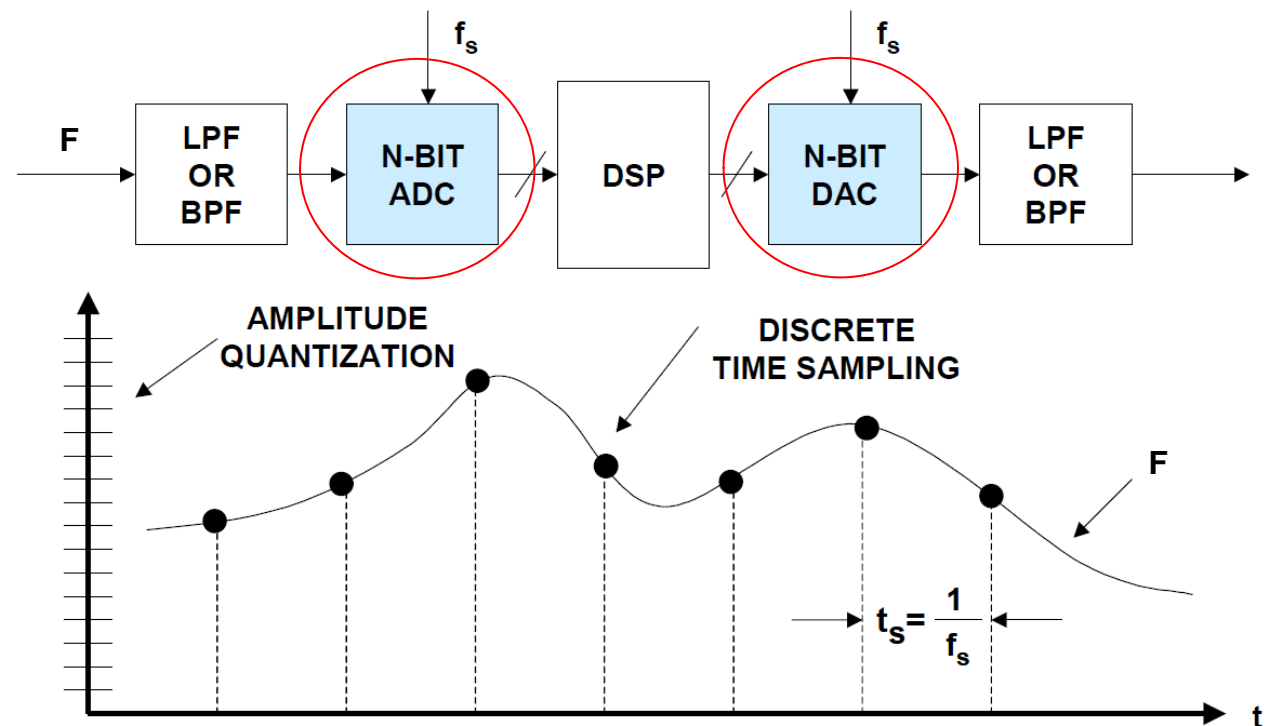
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ADC = analogue to digital converter

DSP = digital signal processor

DAC = digital to analogue converter



Signal with maximum frequency  $F$  is filtered, sampled at frequency  $f_s$ , digitized, stored and then output as an analogue signal and filtered.

28.16



## What about the data converters!

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- *Sampling* involves taking a series of instantaneous measurements of a signal and converting these into a digital form
- *Reconstruction* involves taking a series of digital readings and converting these back into their analogue equivalents
- These two operations are performed by **data converters** which can be of two basic types:
  - **Analogue-to-digital converters (ADC'S)**
  - **Digital-to-analogue converters (DAC'S)**

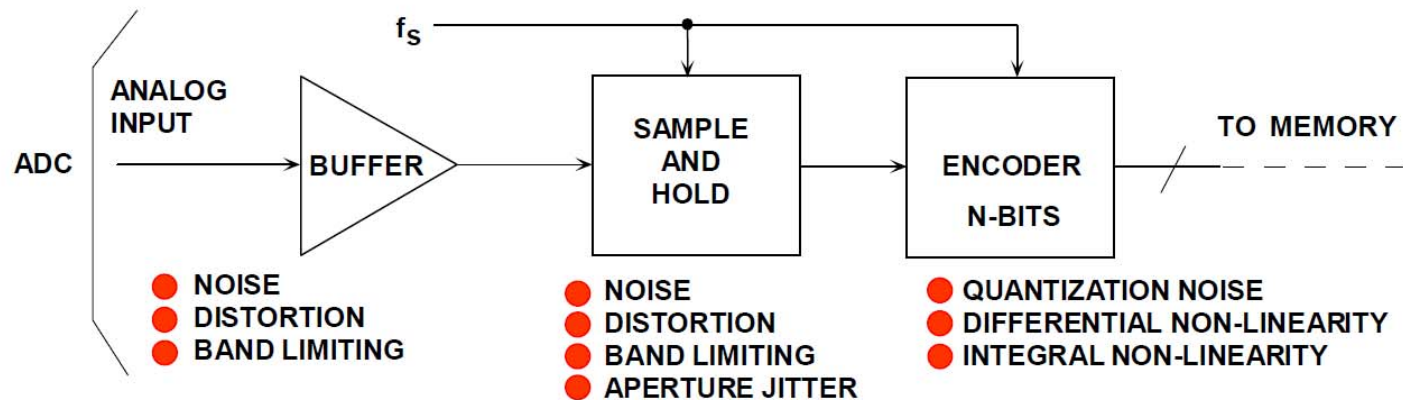
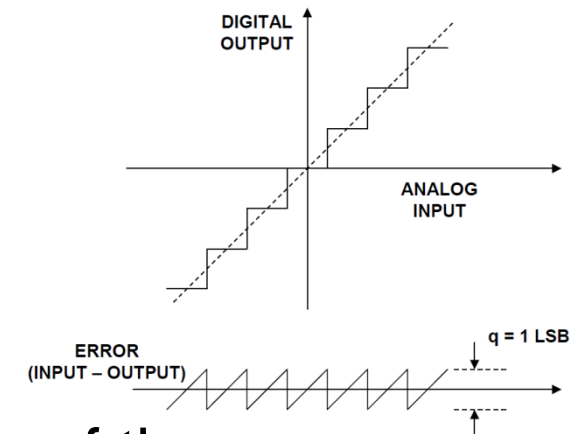
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## ■ Resolution of data converters

- a range of converters is available, each providing conversion to a particular **resolution**
- this determines the number of **quantization levels** used
- an  $n$ -bit converter uses  $2^n$  discrete steps
  - e.g. an 8-bit converter uses  $2^8$  or 256 levels
  - a 10-bit converter uses  $2^{10}$  or 1024 levels
- an 8-bit converter gives a resolution of about 0.4%  
(volts/step = FullScaleVolts/ $2^8$ . Resolution = volts/step/FSV \*100)
- where greater resolution is required converters with up to 20-bit resolution or more are available

# Resolution vs. accuracy

- The resolution represents a “quantization” noise
- Frequently quoted as  $\pm 1/2$  LSB
- Accuracy will depend upon the total noise of the process, which depends on the entire chain (typically  $\pm 1.5$  LSB)



Reverse the chain through DAC for output

## How fast can we digitize or reconstruct a signal?

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- Determines what frequencies we can sample
- **Speed of conversion**
  - conversions of ADC's or DAC's take a finite time
  - this is referred to as the **conversion time** or **settling time** of the converter
  - the time taken depends on the converter
  - DACs are usually faster than ADCs



Video 28B

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- **Digital-to-analogue converters (DACs)**

- wide range of resolutions, but in general, conversion time *increases with resolution*
- a typical general-purpose 8-bit DAC would have a settling time of between 100 ns and 1  $\mu$ s
- a typical 16-bit converter would have a settling time of a few milliseconds
- for specialist applications high-speed converters have settling times of a few nanoseconds
- a video DAC might have a resolution of 8 bits and a maximum sampling rate of 100 MHz

28.21

## – a binary-weighted resistor DAC

A “1” on an input tries to draw current from the op amp junction (must come from  $V_o$  since input of op amp does not draw or source current)

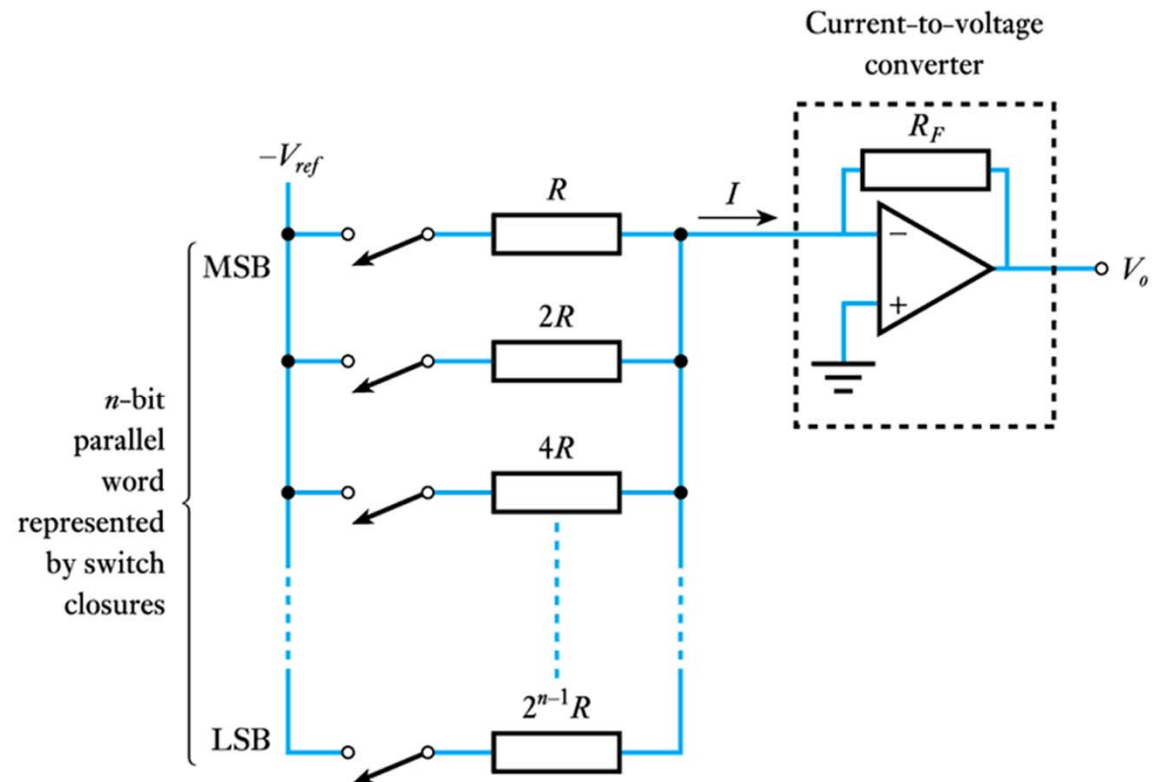
Op amp changes  $V_o$  to null the current at the input

Just an inverting amplifier whose gain depends on which bits are 1.

Gain decreases from MSB to LSB

So for a binary input number  $m$ :

$$V_o = m \times \frac{V_{ref} R_F}{2^{n-1} R}$$



## Same idea, but same resistors for better thermal control

### – an $R$ - $2R$ resistor chain DAC

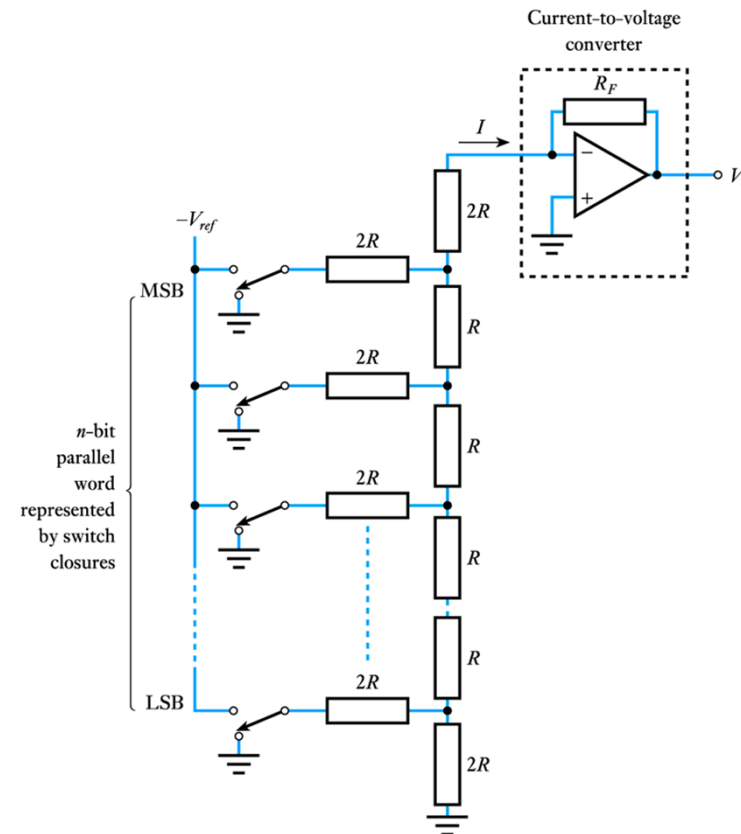
A 1 on an input will cause a current to flow through the  $2R$  resistor attached to the switch.

At the junction, this current sees an equivalent resistance  $2R$  in each direction and is split equally

As it travels up the chain, it is split again at each junction

Coming from LSB it sees the most splits  $\Rightarrow$  this gives the least current at op-amp

Op amp changes  $V_o$  to offset (null) the current at the input



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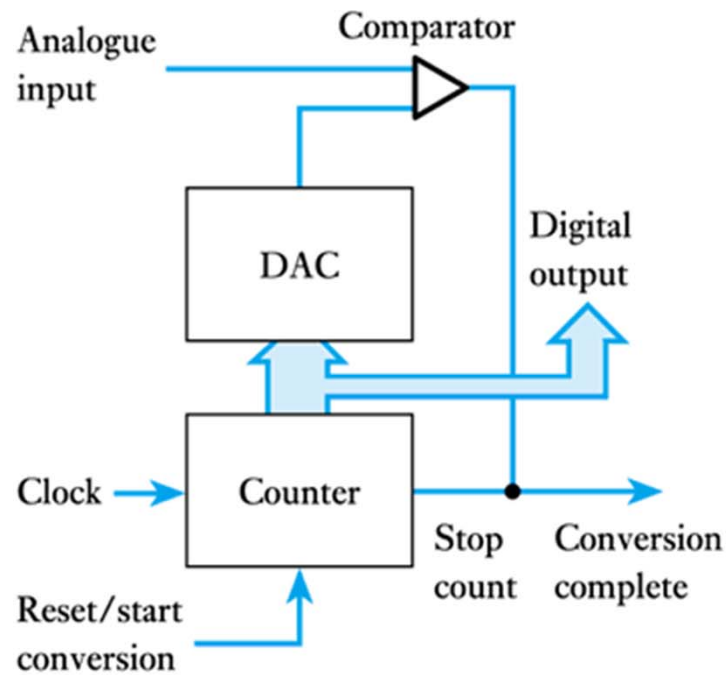
- **Analogue-to-digital converters (ADCs)**

- again available in a range of resolutions and speeds
- a typical 8-bit converter might have a settling time of between 1 and 10  $\mu\text{s}$  (~10x longer than a DAC)
- a typical 12-bit converter might have a settling time of 10 to 100  $\mu\text{s}$
- But, high speed converters can exceed 150 million samples per second

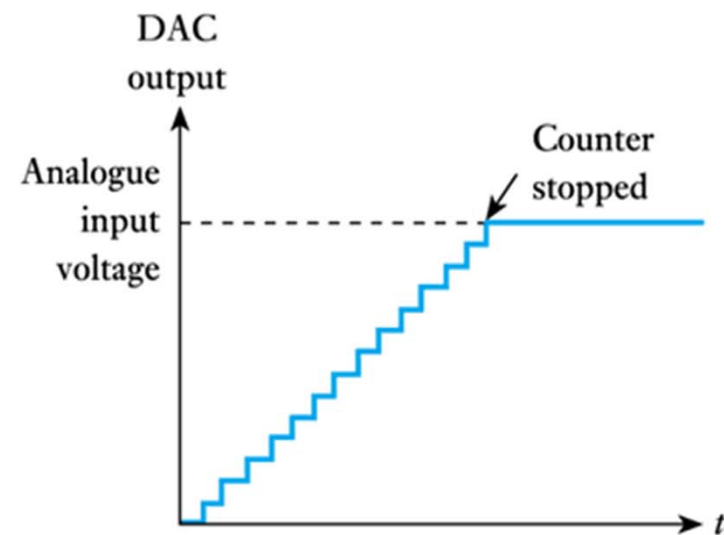


## – a counter or servo ADC

Slow but cheap-few ms



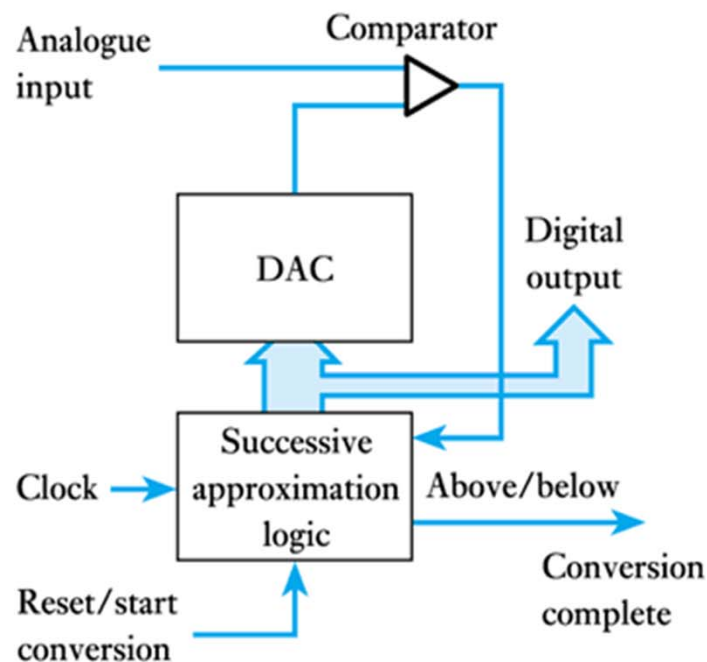
(a) Block diagram



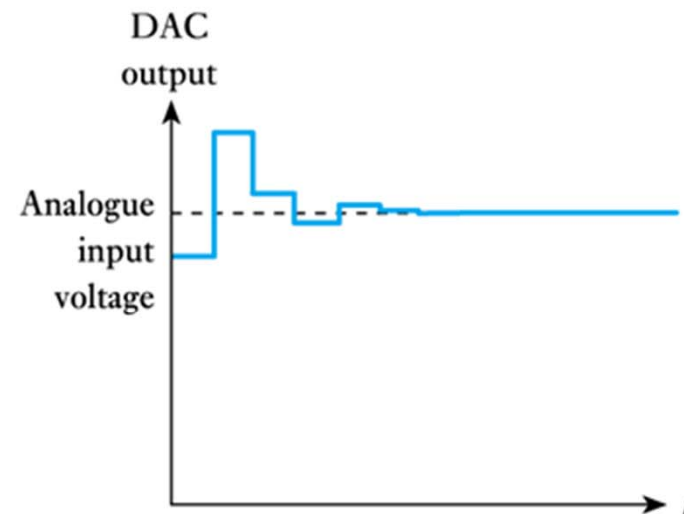
(b) DAC waveform

Fast and still cheap  
1-100  $\mu\text{s}$  for 8-12 bits  
Most common type

- a successive approximation ADC (**bisection**)
- MSB=1, DAC =  $\frac{1}{2}$  scale, if less than input, keep MSB=1 & turn on next bit
- If more than input, reset bit to 0 and turn next bit on, keep going



(a) Block diagram



(b) DAC waveform

28.26

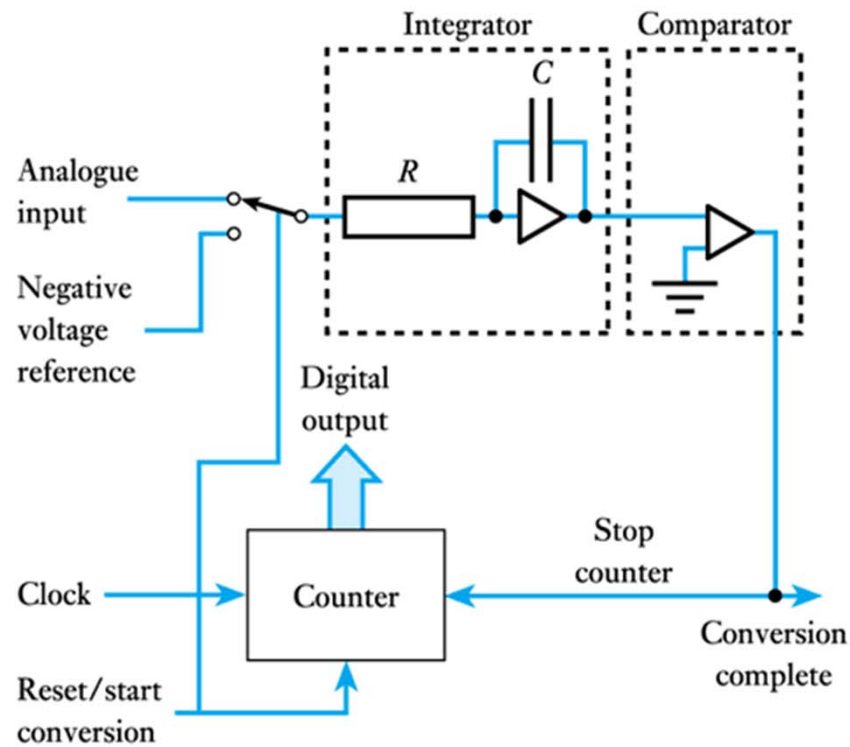
$V_i$  charges capacitor

Discharge at constant rate

Counter starts at start of discharge and stops at full discharge

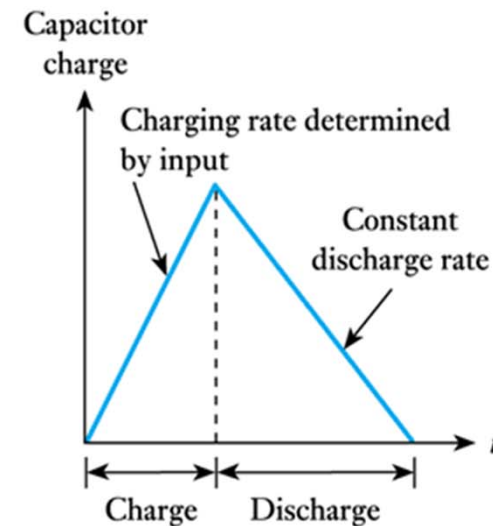
Time = count =  $V_i$

## – a dual-slope ADC



(a) Block diagram

Slow (10-100 ms)  
but very accurate



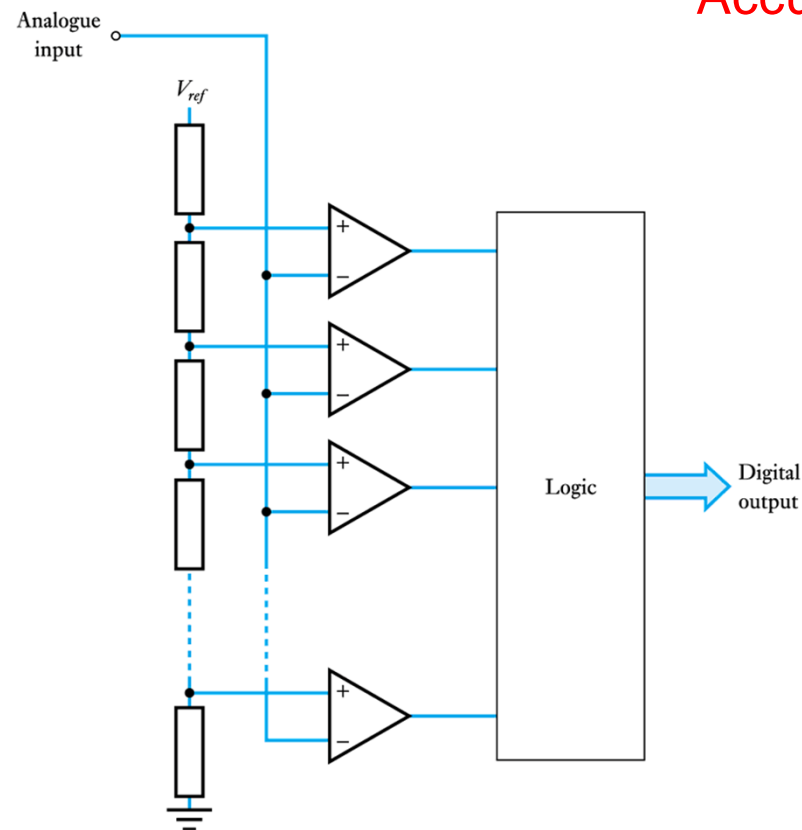
(b) Capacitor waveform

Comparators connected to voltages with  $V > V_i$  produce one polarity,  
All connected to  $V < V_i$  produce the opposite polarity.  
Combinational logic is then used to determine the value of the input  
voltage from this pattern.

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## – a parallel or flash ADC

Go fast converter (ns)  
Accurate and expensive



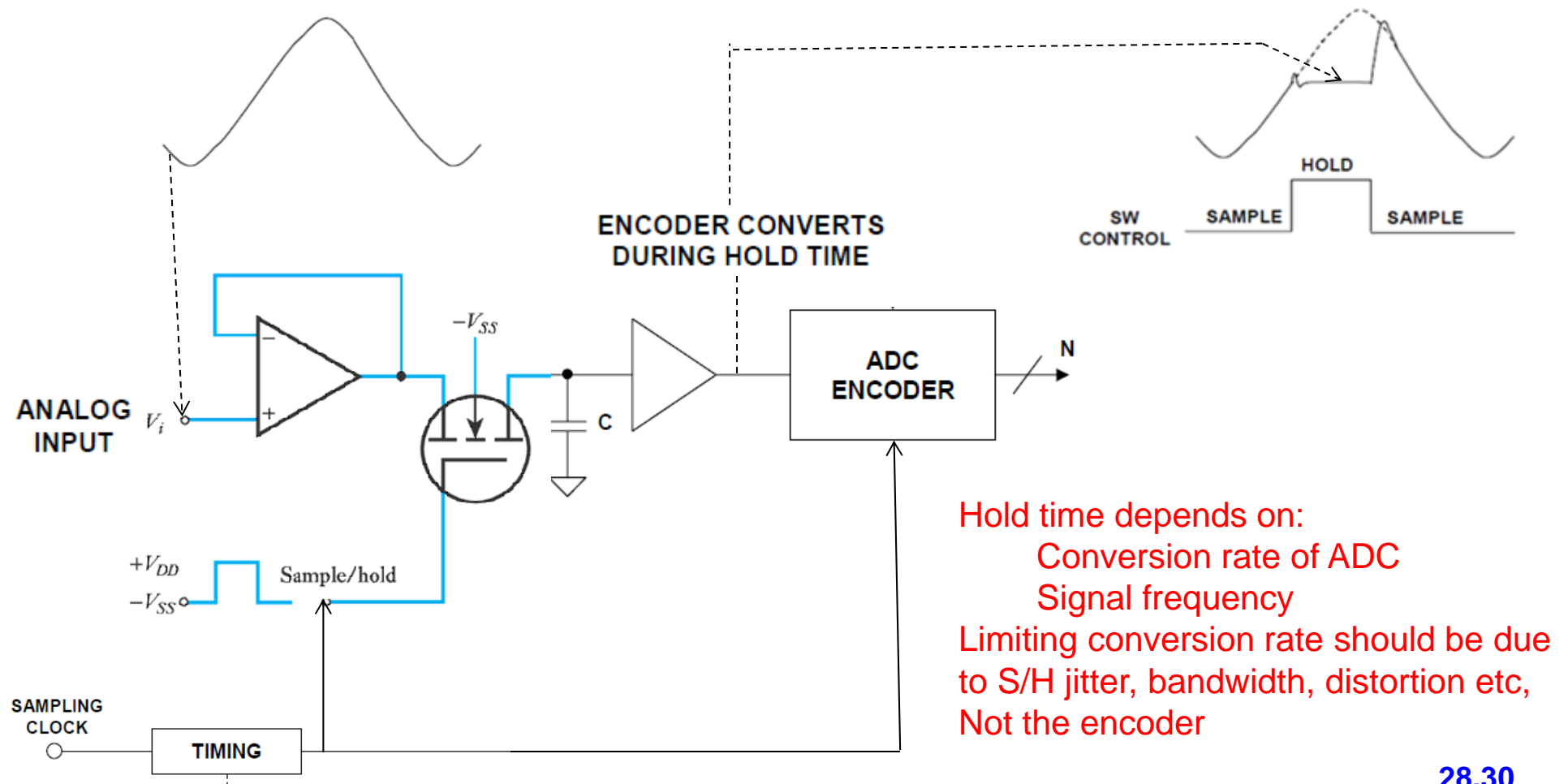
28.28

## Sample and hold gates

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- It is often useful to be able to *sample* a signal and then *hold* its value constant
  - this is useful when performing analogue-to-digital conversion so that the signal does not change during conversion
  - it is also useful when doing digital-to-analogue conversion to maintain the output voltage constant between conversions
- This task is performed by a **sample and hold gate**
  - we have looked at such circuits in earlier lectures

## ■ A FET sample and hold gate

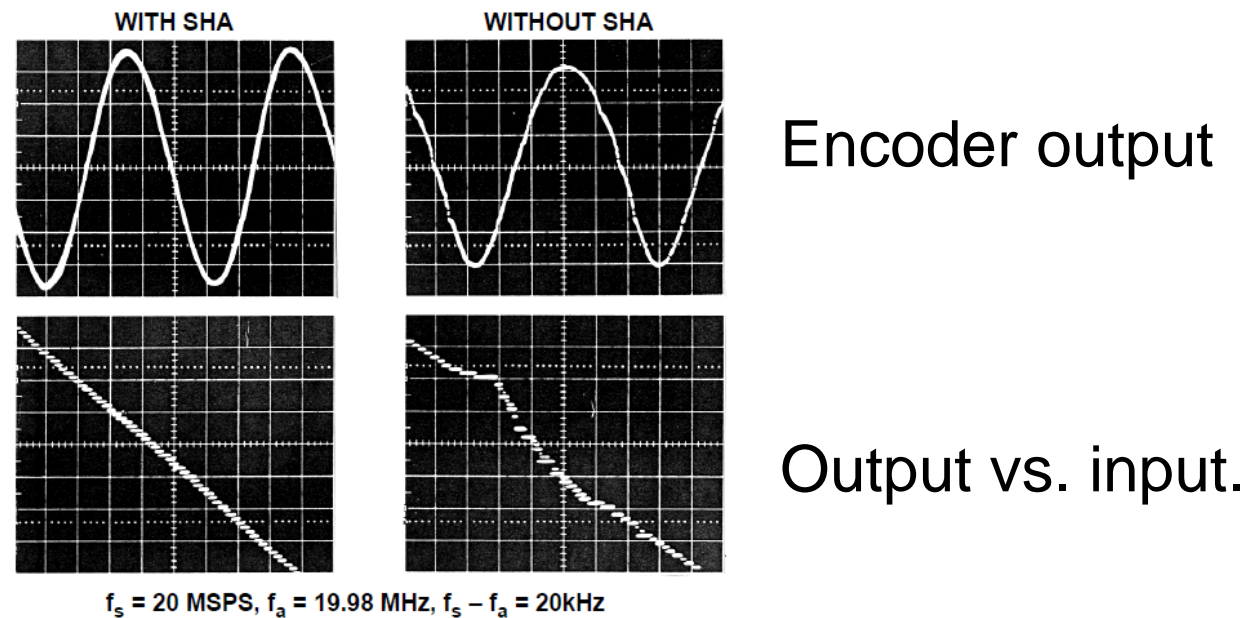


28.30

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- Most sample and hold gates are constructed using integrated circuits
  - Typical devices require a few microseconds to sample the incoming waveform, which then decays (or **droops**) at a rate of a few millivolts per millisecond
  - High speed devices, such as those used for video applications, can sample an input in a few nanoseconds, so droop must be limited to a few millivolts per microsecond

## Advantage of S/H

- If signal is changing during conversion, increases bit errors, missing codes, and accentuates timing mismatches in comparators of flash ADC.



**Figure 2.28:** 8-bit, 20-MSPS Flash ADC With and Without Sample-and-Hold



# Multiplexing

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Video 28C



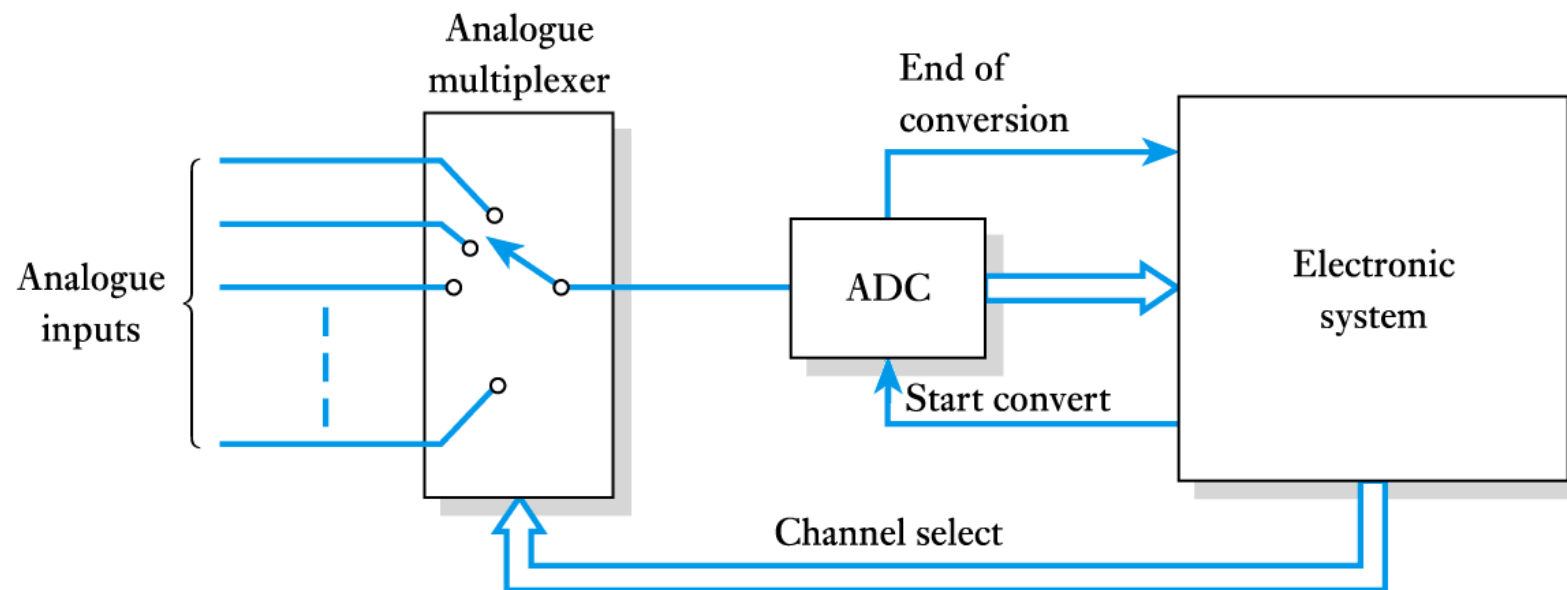
28.6

- While some systems have a single input and a single output, often there are multiple inputs and outputs
- Rather than have separate converters for each input and output, we often use **multiplexing**
  - multiplexers make use of **electrically operated switches** to control the routing of signals
  - these can be used at the input or output of a system
  - normally separate anti-aliasing and/or reconstruction filters would be used with each input

**28.33**

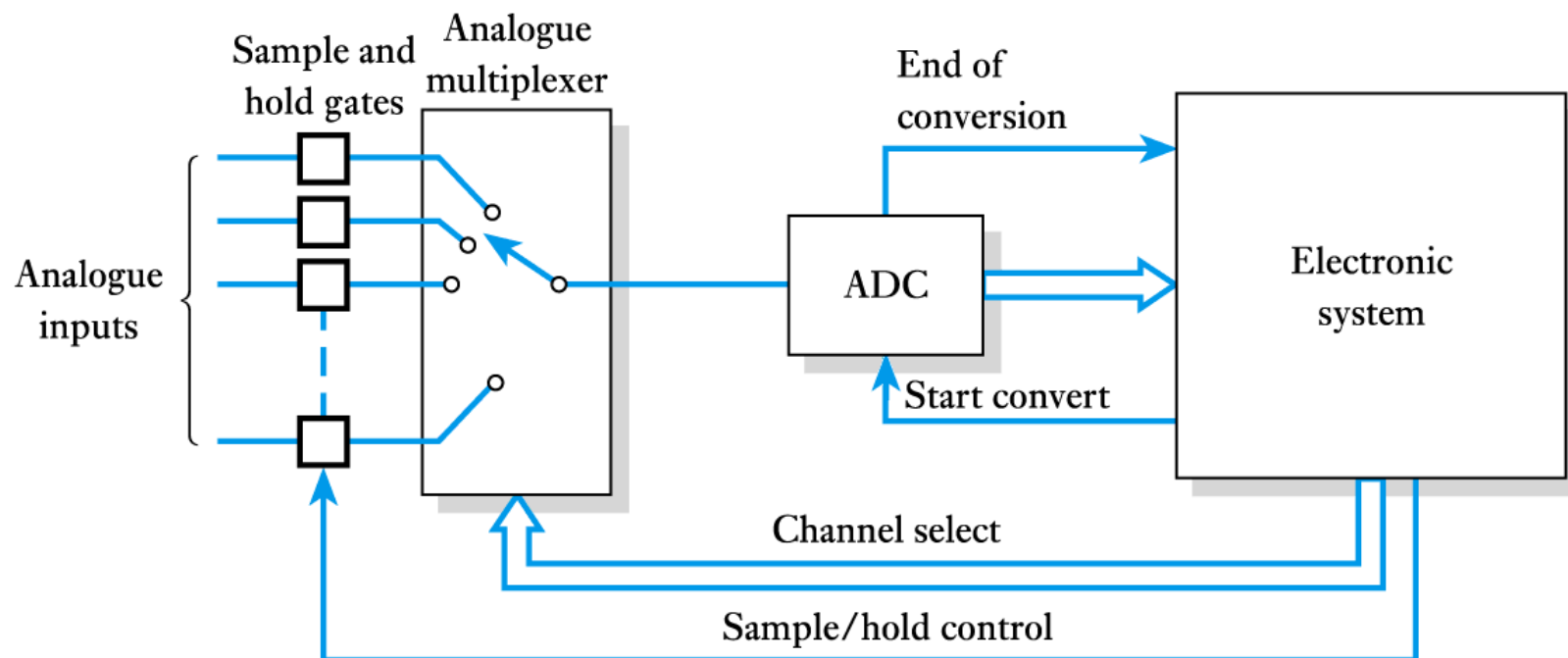
## Time delay between sampled inputs

- **Input multiplexing**



All inputs sampled simultaneously—only droop to worry about (last one read has largest droop)

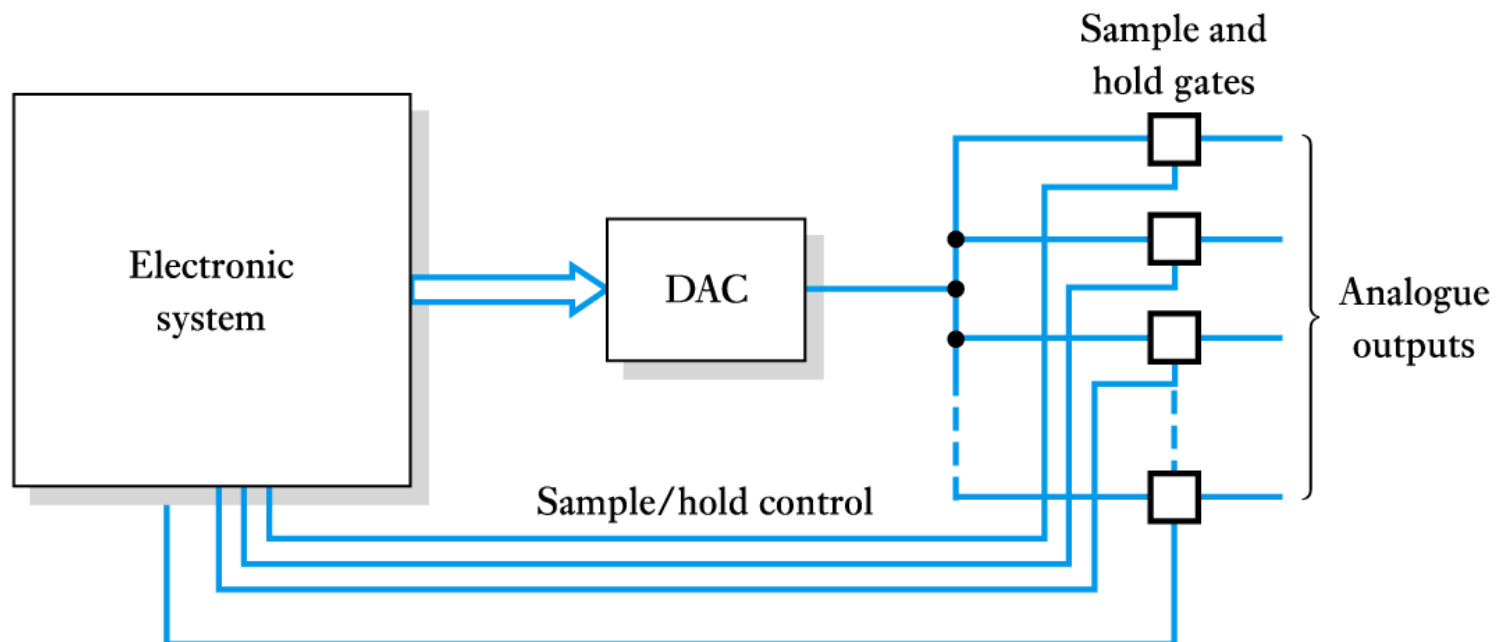
- **Input multiplexing with sample and hold gates**



Convert input 1-hold output 1

Get new input, convert new input, hold output on ch 2 ...

- **Output multiplexing**



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- **Single-chip data acquisition systems**

- these are a combination of an ADC and a multiplexer within a single integrated circuit
- usually designed for use with microprocessor-based systems, and provide all the control lines necessary for simple interfacing

- More info in the analogue devices analogue to digital conversion handbook on It's Learning [analog\\_digital\\_conversion.zip](#)



Video 28D Further Study

## Further Study

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- The Further Study section at the end of Chapter 28 looks at the use of analogue sensors within smartphones.
- Consider what novel sensors could be added to a smartphone and suggest some applications that might make use of them.
- When you have given this some thought, take a look at the video.



## Key points

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- Converting an analogue signal to a digital form is achieved by sampling the waveform and then performing analogue to digital conversion
- As long as the sampling rate is above the Nyquist rate ( $>$  twice the highest frequency present), no information is lost as a result of sampling
- When sampling broad spectrum signals we make use of anti-aliasing filters to remove unwanted components
- When reconstructing signals, filters are used to remove the effects of the sampling
- A wide range of ADCs and DACs is available
- Sample and hold gates may be useful at the input or output
- Multiplexers can reduce the number of converters required

28.39