



TMT4320 Nanomaterials, fall 2015

## EXERCISE 4

**Guidance:** Wednesday 16<sup>th</sup> September, 18:15-20:00, H3  
**Due date:** Friday 18<sup>th</sup> September, 14:00, boxes outside R7 or in It's learning

### PROBLEM 1

The energy  $\Delta G$  of a nucleus of a new phase of size  $r$  appearing in a homogeneous mixture can be described as a sum of a volume term and a surface term:

$$\Delta G = \Delta\mu_v + \Delta\mu_s = \frac{4}{3}\pi r^3 \Delta G_v + 4\pi r^2 \gamma$$

where  $\Delta G_v$  is the change of Gibbs energy per unit volume of the solid phase and  $\gamma$  is the surface energy. Use this equation to derive expressions for the critical size of a stable nucleus ( $r^*$ ) and the critical energy (energy barrier for nucleation,  $\Delta G^*$ ) as functions of  $\Delta G_v$  and  $\gamma$ .

### PROBLEM 2

- a) Use Figure 1 below to explain in your own words (not copy paste from a book) the concept of nucleation and growth in the transition from a single phase to two phases, for instance the formation of solid nanoparticles in a solution. Fill in the appropriate axes, areas and limits.

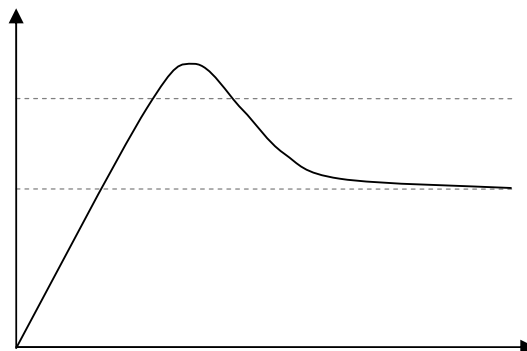
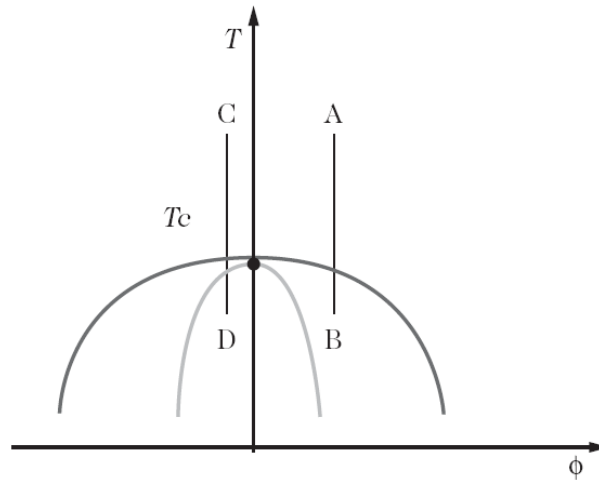


Figure 1.

- b) What is the main difference between nucleation-and-growth and spinodal decomposition?
- c) In Figure 2 below, which of the two lines A-B and C-D represents nucleation-and-growth and which line represents spinodal decomposition? Assume the material is quenched.



**Figure 2.** Phase diagram of a system with order parameter  $\phi$ .  $T$ : temperature. *Black curve*: boundary for coexistence of the two phases (binodal curve). *Grey curve*: spinodal curve.

- d) During the transition from the homogeneous phase to the spinodal region of the two-phase region, is it possible to observe nucleation-and-growth? Explain how and why.

### PROBLEM 3

- Draw the molecular structure of a cationic surfactant, an anionic surfactant and a non-ionic surfactant and name the three surfactants.
- What is the difference between a micelle and a reverse micelle? Draw the two structures.
- How can reverse micelles be used for synthesis of nanoparticles? As an example, explain how you would produce cobalt (Co) nanoparticles if you have these compounds available: Water, hexane,  $\text{CoCl}_2$ ,  $\text{NaBH}_4$ , and  $\text{Na(AOT)}$  (sodium bis(2-ethylhexyl)-sulfosuccinate).
- How can we control the size of nanoparticles synthesized in reverse micelles?