



# Sorting in Arrays



# Array

Previously, we **initialized** an integer array for 5 numbers.

```
int num[5] = {5,4,1,11,6};
```



|    |        |
|----|--------|
| 5  | num[0] |
| 4  | num[1] |
| 1  | num[2] |
| 11 | num[3] |
| 6  | num[4] |

Memory



# Unsorted Array

The data in this **num** array is **not** in an order.

```
int num[5] = {5,4,1,11,6};
```

|    |        |
|----|--------|
| 5  | num[0] |
| 4  | num[1] |
| 1  | num[2] |
| 11 | num[3] |
| 6  | num[4] |

Memory



# Sorting

The process of **ordering data elements** in the array is called **Sorting**.

There are two types of orders in Sorting.

1. **Ascending** Order
2. **Descending** Order

# Sorting

```
int num[5] = {5,4,1,11,6};
```

The process of **ordering data elements** in the array is called **Sorting**.

There are two types of orders in Sorting.

1. **Ascending** Order

```
int num[5] = {1,4,5,6,11};
```

2. **Descending** Order

```
int num[5] = {11,6,5,4,1};
```

# Working Example

Write a **C++** program that **Sorts** the array in **Descending Order**.

```
int num[5] = {5,4,1,11,6};
```



# Algorithm for Sorting

**Step 1:** Make a new array and set the index to 0.

**Step 2:** Find the Largest Element in the original array

**Step 3:** Place the largest Element on the available index of the new array.

**Step 4:** Replace the largest element in the original array with a lowest number (i.e., -1)

**Step 5:** Update the index of the new array.

**Step 6:** Repeat Step 2, 3, 4 and 5

# Algorithm for Sorting: Step 1

Original Array

|   |   |   |    |   |
|---|---|---|----|---|
| 5 | 4 | 1 | 11 | 6 |
|---|---|---|----|---|

New Array

|  |  |  |  |  |
|--|--|--|--|--|
|  |  |  |  |  |
|--|--|--|--|--|



# Algorithm for Sorting: Step 2

Original Array

|   |   |   |    |   |
|---|---|---|----|---|
| 5 | 4 | 1 | 11 | 6 |
|---|---|---|----|---|

New Array

|  |  |  |  |  |
|--|--|--|--|--|
|  |  |  |  |  |
|--|--|--|--|--|

# Algorithm for Sorting: Step 3

Original Array

|   |   |   |    |   |
|---|---|---|----|---|
| 5 | 4 | 1 | 11 | 6 |
|---|---|---|----|---|

New Array

|    |  |  |  |  |
|----|--|--|--|--|
| 11 |  |  |  |  |
|----|--|--|--|--|

# Algorithm for Sorting: Step 4

Original Array

|   |   |   |    |   |
|---|---|---|----|---|
| 5 | 4 | 1 | -1 | 6 |
|---|---|---|----|---|

New Array

|    |  |  |  |  |
|----|--|--|--|--|
| 11 |  |  |  |  |
|----|--|--|--|--|

# Algorithm for Sorting: Step 5

Original Array

|   |   |   |    |   |
|---|---|---|----|---|
| 5 | 4 | 1 | -1 | 6 |
|---|---|---|----|---|

New Array

|    |  |  |  |  |
|----|--|--|--|--|
| 11 |  |  |  |  |
|----|--|--|--|--|

# Algorithm for Sorting: 2nd Iteration

Original Array

|   |   |   |    |   |
|---|---|---|----|---|
| 5 | 4 | 1 | -1 | 6 |
|---|---|---|----|---|

New Array

|    |  |  |  |  |
|----|--|--|--|--|
| 11 |  |  |  |  |
|----|--|--|--|--|

# Algorithm for Sorting: 2nd Iteration

Original Array

|   |   |   |    |    |
|---|---|---|----|----|
| 5 | 4 | 1 | -1 | -1 |
|---|---|---|----|----|

New Array

|    |   |  |  |  |
|----|---|--|--|--|
| 11 | 6 |  |  |  |
|----|---|--|--|--|

# Algorithm for Sorting: 3rd Iteration

Original Array

|   |   |   |    |    |
|---|---|---|----|----|
| 5 | 4 | 1 | -1 | -1 |
|---|---|---|----|----|

New Array

|    |   |  |  |  |
|----|---|--|--|--|
| 11 | 6 |  |  |  |
|----|---|--|--|--|

# Algorithm for Sorting: 3rd Iteration

Original Array

|    |   |   |    |    |
|----|---|---|----|----|
| -1 | 4 | 1 | -1 | -1 |
|----|---|---|----|----|

New Array

|    |   |   |  |  |
|----|---|---|--|--|
| 11 | 6 | 5 |  |  |
|----|---|---|--|--|



# Algorithm for Sorting: 4th Iteration

Original Array

|    |   |   |    |    |
|----|---|---|----|----|
| -1 | 4 | 1 | -1 | -1 |
|----|---|---|----|----|

New Array

|    |   |   |  |  |
|----|---|---|--|--|
| 11 | 6 | 5 |  |  |
|----|---|---|--|--|

# Algorithm for Sorting: 4th Iteration

Original Array

|    |    |   |    |    |
|----|----|---|----|----|
| -1 | -1 | 1 | -1 | -1 |
|----|----|---|----|----|

New Array

|    |   |   |   |  |
|----|---|---|---|--|
| 11 | 6 | 5 | 4 |  |
|----|---|---|---|--|

# Algorithm for Sorting: 5th Iteration

Original Array

|    |    |   |    |    |
|----|----|---|----|----|
| -1 | -1 | 1 | -1 | -1 |
|----|----|---|----|----|

New Array

|    |   |   |   |  |
|----|---|---|---|--|
| 11 | 6 | 5 | 4 |  |
|----|---|---|---|--|

# Algorithm for Sorting: 5th Iteration

Original Array

|    |    |    |    |    |
|----|----|----|----|----|
| -1 | -1 | -1 | -1 | -1 |
|----|----|----|----|----|

New Array

|    |   |   |   |   |
|----|---|---|---|---|
| 11 | 6 | 5 | 4 | 1 |
|----|---|---|---|---|

# Solution

Let's make a function that searches an array and finds the largest element from the array and then returns it.

```
#include <iostream>
using namespace std;

// Global Array and its Size
int o_arr[5] = {5, 4, 1, 11, 6};
const int arr_length = sizeof(o_arr) / sizeof(o_arr[0]);

// Function Definition
int largest()
{
    int large = -1;
    int large_index;
    for (int idx = 0; idx < arr_length; idx = idx + 1)
    {
        if (large < o_arr[idx])
        {
            large = o_arr[idx];
            large_index = idx;
        }
    }
    o_arr[large_index] = -1;
    return large;
}
```

# Solution

Now, use that function and make a new array and populate its elements in descending order.

```
main()
{
    int n_arr[arr_length];
    for (int idx = 0; idx < arr_length; idx = idx + 1)
    {
        n_arr[idx] = largest();
    }
}
```

# Solution

Now, print the new array.

```
main()
{
    int n_arr[arr_length];
    for (int idx = 0; idx < arr_length; idx = idx + 1)
    {
        n_arr[idx] = largest();
    }
    for (int idx = 0; idx < arr_length; idx = idx + 1)
    {
        cout << n_arr[idx] << ", ";
    }
}
```

# Algorithm for Sorting

There are different methods for sorting. Lets see another one which sorts the elements in the same array.

|   |   |   |    |   |
|---|---|---|----|---|
| 5 | 4 | 1 | 11 | 6 |
|---|---|---|----|---|



# Algorithm for Sorting

**Step 1:** Sort the 0th index by swapping with the largest element.

|   |   |   |    |   |
|---|---|---|----|---|
| 5 | 4 | 1 | 11 | 6 |
|---|---|---|----|---|

# Algorithm for Sorting

**Step 1:** Sort the 0th index by swapping with the largest element.



# Algorithm for Sorting

**Step 1:** Sort the 0th index by swapping with the largest element.



# Algorithm for Sorting

**Step 2:** Sort the 1st index by swapping with the largest element in the rest of unsorted array.



# Algorithm for Sorting

**Step 2:** Sort the 1st index by swapping with the largest element in the rest of unsorted array.



# | Algorithm for Sorting

**Step 2:** Sort the 1st index by swapping with the largest element in the rest of unsorted array.



# Algorithm for Sorting

**Step 3:** Sort the 2nd index by swapping with the largest element in the rest of unsorted array.



# Algorithm for Sorting

**Step 3:** Sort the 2nd index by swapping with the largest element in the rest of unsorted array.





# Algorithm for Sorting

**Step 3:** Sort the 2nd index by swapping with the largest element in the rest of unsorted array.



# Algorithm for Sorting

**Step 4:** Sort the 3rd index by swapping with the largest element in the rest of unsorted array.



# Algorithm for Sorting

**Step 4:** Sort the 3rd index by swapping with the largest element in the rest of unsorted array.



# Algorithm for Sorting

**Step 4:** Sort the 3rd index by swapping with the largest element in the rest of unsorted array.



# | Algorithm for Sorting

**Step 5:** Sort the 4th index by swapping with the largest element in the rest of unsorted array.

|    |   |   |   |   |
|----|---|---|---|---|
| 11 | 6 | 5 | 4 | 1 |
|----|---|---|---|---|

# Algorithm for Sorting

**Step 5:** Sort the 4th index by swapping with the largest element in the rest of unsorted array.



# | Algorithm for Sorting

**Step 5:** Sort the 4th index by swapping with the largest element in the rest of unsorted array.

|    |   |   |   |   |
|----|---|---|---|---|
| 11 | 6 | 5 | 4 | 1 |
|----|---|---|---|---|

# Solution

Let's make a function that searches an array from a **specific index** and **finds the largest index** from the array.

```
#include <iostream>
using namespace std;

// Global Array and its Size
int o_arr[5] = {5, 4, 1, 11, 6};
const int arr_length = sizeof(o_arr) / sizeof(o_arr[0]);

// Function Definition
int largest(int s)
{
    int large = -1;
    int large_index;
    for (int idx = s; idx < arr_length; idx = idx + 1)
    {
        if (large < o_arr[idx])
        {
            large = o_arr[idx];
            large_index = idx;
        }
    }
    return large_index;
}
```



# Solution

Now, use that function to get the index of the largest element.

```
main()
{
    int largest_idx;
    int temp;
    for (int idx = 0; idx < arr_length; idx = idx + 1)
    {
        largest_idx = largest(idx);
    }
}
```

# Solution

Now, we have to swap the largest element with the index on which we are present. For that we have to use a temporary variable. So our data doesn't get lost.

```
main()
{
    int largest_idx;
    int temp;
    for (int idx = 0; idx < arr_length; idx = idx + 1)
    {
        largest_idx = largest(idx);
        temp = o_arr[largest_idx];
        o_arr[largest_idx] = o_arr[idx];
        o_arr[idx] = temp;
    }
}
```

# Solution

Now, print the new array.

```
main()
{
    int largest_idx;
    int temp;
    for (int idx = 0; idx < arr_length; idx = idx + 1)
    {
        largest_idx = largest(idx);
        temp = o_arr[largest_idx];
        o_arr[largest_idx] = o_arr[idx];
        o_arr[idx] = temp;
    }
    for (int idx = 0; idx < arr_length; idx = idx + 1)
    {
        cout << o_arr[idx] << ", ";
    }
}
```

# Algorithm for Sorting

## 1st Method

Original Array

|    |    |    |    |    |
|----|----|----|----|----|
| -1 | -1 | -1 | -1 | -1 |
|----|----|----|----|----|

New Array

|    |   |   |   |   |
|----|---|---|---|---|
| 11 | 6 | 5 | 4 | 1 |
|----|---|---|---|---|

## 2nd Method

Original Array

|    |   |   |   |   |
|----|---|---|---|---|
| 11 | 6 | 5 | 4 | 1 |
|----|---|---|---|---|

# Algorithm for Sorting

## 1st Method

Original Array

|    |    |    |    |    |
|----|----|----|----|----|
| -1 | -1 | -1 | -1 | -1 |
|----|----|----|----|----|

New Array

|    |   |   |   |   |
|----|---|---|---|---|
| 11 | 6 | 5 | 4 | 1 |
|----|---|---|---|---|

Out of Place Sorting

## 2nd Method

Original Array

|    |   |   |   |   |
|----|---|---|---|---|
| 11 | 6 | 5 | 4 | 1 |
|----|---|---|---|---|

In Place Sorting

# Algorithm for Sorting

Which one is better?

1st Method

Original Array

|    |    |    |    |    |
|----|----|----|----|----|
| -1 | -1 | -1 | -1 | -1 |
|----|----|----|----|----|

New Array

|    |   |   |   |   |
|----|---|---|---|---|
| 11 | 6 | 5 | 4 | 1 |
|----|---|---|---|---|

Out of Place Sorting

2nd Method

Original Array

|    |   |   |   |   |
|----|---|---|---|---|
| 11 | 6 | 5 | 4 | 1 |
|----|---|---|---|---|

In Place Sorting

# Algorithm for Sorting

Which one is better?

1st Method

Original Array

|    |    |    |    |    |
|----|----|----|----|----|
| -1 | -1 | -1 | -1 | -1 |
|----|----|----|----|----|

New Array

|    |   |   |   |   |
|----|---|---|---|---|
| 11 | 6 | 5 | 4 | 1 |
|----|---|---|---|---|

Out of Place Sorting

2nd Method

Original Array

|    |   |   |   |   |
|----|---|---|---|---|
| 11 | 6 | 5 | 4 | 1 |
|----|---|---|---|---|



In Place Sorting

# Learning Objective

In this lecture, we learnt how to use **arrays** to solve real world problems of **sorting the data** elements of the array in an order





# Conclusion

- The process of ordering data elements in the array is called **Sorting**. There are two types of orders in Sorting.
  - Ascending Order
  - Descending Order
- If one arranges the data elements in order of **increasing number** then it is called the array is Sorted in **Ascending order**. If one arranges the data elements in order of **decreasing number** then it is called the array is Sorted in **Descending order**.

# Self Assessment

1. Write a program that takes nine numbers between 1 and 10 (excluding one number) and returns the missing number.  
Note: The array of numbers will be **unsorted** (**not in order**). Only one number will be missing.

| Input                        | Output |
|------------------------------|--------|
| [1, 2, 3, 4, 6, 7, 8, 9, 10] | 5      |
| [7, 2, 3, 6, 5, 9, 1, 4, 8]  | 10     |
| [10, 5, 1, 2, 4, 6, 8, 3, 9] | 7      |



# Self Assessment

2. Write a C++ program that takes an **unsorted array** and returns the  $n$ th smallest integer entered by the user. (the smallest integer is the **first smallest**, the second smallest integer is the **second smallest**, etc).

Note:

- $n$  will always be  $\geq 1$ .
- Each number in the array will be **distinct** (no duplicates will be there).
- Given an **out of bounds parameter** (e.g. an array is of size  $k$ ), and you are asked to find the  $m > k$  smallest integer, **return -1**.



# Self Assessment

## Test Cases:

| Input             | Output |
|-------------------|--------|
| [1, 3, 5, 7]<br>1 | 1      |
| [1, 3, 5, 7]<br>3 | 5      |
| [7, 3, 5, 1]<br>2 | 3      |



# Self Assessment

3. Given a sequence of integers as an array, determine whether it is possible to obtain a **strictly increasing** sequence by removing no more than one element from the array.

**Note:** sequence  $a_0, a_1, \dots, a_n$  is considered to be a strictly increasing if  $a_0 < a_1 < \dots < a_n$ . Sequence containing only one element is also considered to be strictly increasing.



# Self Assessment

## Example:

- For sequence = [1, 3, 2, 1], the output should be `solution(sequence) = false`.

There is no one element in this array that can be removed in order to get a strictly increasing sequence.

- For sequence = [1, 3, 2], the output should be `solution(sequence) = true`.

As you can remove 3 from the array to get the strictly increasing sequence [1, 2]. Alternately, you can remove 2 to get the strictly increasing sequence [1, 3].



# Self Assessment

## Test Cases:

| Input                                         | Output |
|-----------------------------------------------|--------|
| sequence: [3, 5, 67, 98, 3]                   | 1      |
| sequence: [123, -17, -5, 1, 2, 3, 12, 43, 45] | 1      |
| sequence: [0, -2, 5, 6]                       | 1      |
| sequence: [1, 2, 1, 2]                        | 0      |

