## Convolutional neural network layers

In this notebook, we will build the convolutional neural network layers. This will be followed by a spatial batchnorm, and then in the final notebook of this assignment, we will train a CNN to further improve the validation accuracy on CIFAR-10.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, their layer structure, and their implementation of fast CNN layers. This also includes nndl.fc\_net, nndl.layers, and nndl.layer\_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

```
In []: ## Import and setups
        import time
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl.conv_layers import *
        from utils.data_utils import get_CIFAR10_data
        from utils gradient_check import eval_numerical_gradient, eval_numerical_gra
        from utils.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ik
        %load_ext autoreload
        %autoreload 2
        def rel_error(x, y):
          """ returns relative error """
          return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

The autoreload extension is already loaded. To reload it, use: %reload\_ext autoreload

## Implementing CNN layers

Just as we implemented modular layers for fully connected networks, batch normalization, and dropout, we'll want to implement modular layers for convolutional neural networks. These layers are in <a href="mailto:nndl/conv\_layers.py">nndl/conv\_layers.py</a>.

#### Convolutional forward pass

Begin by implementing a naive version of the forward pass of the CNN that uses for loops. This function is conv\_forward\_naive in nndl/conv\_layers.py . Don't worry about efficiency of implementation. Later on, we provide a fast implementation of

these layers. This version ought to test your understanding of convolution. In our implementation, there is a triple for loop.

After you implement conv\_forward\_naive, test your implementation by running the cell below.

```
In []: x_{shape} = (2, 3, 4, 4)
        w_{\text{shape}} = (3, 3, 4, 4)
        x = np.linspace(-0.1, 0.5, num=np.prod(x_shape)).reshape(x_shape)
        w = np.linspace(-0.2, 0.3, num=np.prod(w_shape)).reshape(w_shape)
        b = np.linspace(-0.1, 0.2, num=3)
        conv_param = {'stride': 2, 'pad': 1}
        out, = conv forward naive(x, w, b, conv param)
        correct_out = np.array([[[[-0.08759809, -0.10987781],
                                    [-0.18387192, -0.2109216]],
                                   [[ 0.21027089, 0.21661097],
                                    [ 0.22847626, 0.23004637]],
                                   [[ 0.50813986, 0.54309974],
                                    [ 0.64082444, 0.67101435]]],
                                  [[-0.98053589, -1.03143541],
                                    [-1.19128892, -1.24695841]],
                                   [[ 0.69108355, 0.66880383],
                                    [ 0.59480972, 0.56776003]],
                                   [[ 2.36270298, 2.36904306],
                                    [ 2.38090835, 2.38247847]]])
        # Compare your output to ours; difference should be around 1e-8
        print('Testing conv_forward_naive')
        print('difference: ', rel_error(out, correct_out))
```

Testing conv\_forward\_naive difference: 2.2121476417505994e-08

#### Convolutional backward pass

Now, implement a naive version of the backward pass of the CNN. The function is conv\_backward\_naive in nndl/conv\_layers.py . Don't worry about efficiency of implementation. Later on, we provide a fast implementation of these layers. This version ought to test your understanding of convolution. In our implementation, there is a quadruple for loop.

After you implement conv\_backward\_naive , test your implementation by running the cell below.

```
In []: x = np.random.randn(4, 3, 5, 5)
w = np.random.randn(2, 3, 3, 3)
b = np.random.randn(2,)
dout = np.random.randn(4, 2, 5, 5)
conv_param = {'stride': 1, 'pad': 1}

out, cache = conv_forward_naive(x,w,b,conv_param)

dx_num = eval_numerical_gradient_array(lambda x: conv_forward_naive(x, w, b, dw_num = eval_numerical_gradient_array(lambda w: conv_forward_naive(x, w, b, db_num = eval_numerical_gradient_array(lambda b: conv_forward_naive(x, w, b, db_num = eval_numerical_gradient_array(lambda b: conv_forward_naive(x, w, b, db_num = eval_numerical_gradient_array(lambda b: conv_forward_naive(x, w, b, conv_param)
dx, dw, db = conv_backward_naive(dout, cache)
```

```
# Your errors should be around 1e-9'
print('Testing conv_backward_naive function')
print('dx error: ', rel_error(dx, dx_num))
print('dw error: ', rel_error(dw, dw_num))
print('db error: ', rel_error(db, db_num))
```

```
Testing conv_backward_naive function dx error: 1.0862986065211766e-09 dw error: 1.0424739064656239e-08 db error: 9.37090619514303e-12
```

#### Max pool forward pass

In this section, we will implement the forward pass of the max pool. The function is max\_pool\_forward\_naive in nndl/conv\_layers.py. Do not worry about the efficiency of implementation.

After you implement max\_pool\_forward\_naive, test your implementation by running
the cell below.

```
In [ ]: x_shape = (2, 3, 4, 4)
        x = np.linspace(-0.3, 0.4, num=np.prod(x_shape)).reshape(x_shape)
        pool_param = {'pool_width': 2, 'pool_height': 2, 'stride': 2}
        out, = max pool forward naive(x, pool param)
        correct_out = np.array([[[[-0.26315789, -0.24842105]
                                   [-0.20421053, -0.18947368]],
                                  [[-0.14526316, -0.13052632],
                                   [-0.08631579, -0.07157895]],
                                  [[-0.02736842, -0.01263158],
                                   [ 0.03157895, 0.04631579]]],
                                 [[[ 0.09052632, 0.10526316],
                                   [ 0.14947368, 0.16421053]],
                                  [[ 0.20842105, 0.22315789],
                                   [ 0.26736842,
                                                  0.28210526]],
                                  [[ 0.32631579,
                                                  0.34105263],
                                   [ 0.38526316,
                                                  0.4
                                                            1111)
        # Compare your output with ours. Difference should be around 1e-8.
        print('Testing max_pool_forward_naive function:')
        print('difference: ', rel_error(out, correct_out))
```

Testing max\_pool\_forward\_naive function: difference: 4.1666665157267834e-08

## Max pool backward pass

In this section, you will implement the backward pass of the max pool. The function is max\_pool\_backward\_naive in nndl/conv\_layers.py . Do not worry about the efficiency of implementation.

After you implement max\_pool\_backward\_naive, test your implementation by running the cell below.

```
In []: x = np.random.randn(3, 2, 8, 8)
dout = np.random.randn(3, 2, 4, 4)
pool_param = {'pool_height': 2, 'pool_width': 2, 'stride': 2}
```

```
dx_num = eval_numerical_gradient_array(lambda x: max_pool_forward_naive(x, pout, cache = max_pool_forward_naive(x, pool_param)
dx = max_pool_backward_naive(dout, cache)

# Your error should be around 1e-12
print('Testing max_pool_backward_naive function:')
print('dx error: ', rel_error(dx, dx_num))
```

Testing max\_pool\_backward\_naive function:
dx error: 1.0

## Fast implementation of the CNN layers

Implementing fast versions of the CNN layers can be difficult. We will provide you with the fast layers implemented by cs231n. They are provided in cs231n/fast\_layers.py.

The fast convolution implementation depends on a Cython extension; to compile it you need to run the following from the cs231n directory:

```
python setup.py build_ext --inplace
```

**NOTE:** The fast implementation for pooling will only perform optimally if the pooling regions are non-overlapping and tile the input. If these conditions are not met then the fast pooling implementation will not be much faster than the naive implementation.

You can compare the performance of the naive and fast versions of these layers by running the cell below.

You should see pretty drastic speedups in the implementation of these layers. On our machine, the forward pass speeds up by 17x and the backward pass speeds up by 840x. Of course, these numbers will vary from machine to machine, as well as on your precise implementation of the naive layers.

```
In [ ]:
       from utils.fast_layers import conv_forward_fast, conv_backward_fast
        from time import time
        x = np.random.randn(100, 3, 31, 31)
        w = np.random.randn(25, 3, 3, 3)
        b = np.random.randn(25,)
        dout = np.random.randn(100, 25, 16, 16)
        conv_param = {'stride': 2, 'pad': 1}
        t0 = time()
        out_naive, cache_naive = conv_forward_naive(x, w, b, conv_param)
        t1 = time()
        out_fast, cache_fast = conv_forward_fast(x, w, b, conv_param)
        t2 = time()
        print('Testing conv_forward_fast:')
        print('Naive: %fs' % (t1 - t0))
        print('Fast: %fs' % (t2 - t1))
        print('Speedup: %fx' % ((t1 - t0) / (t2 - t1)))
        print('Difference: ', rel_error(out_naive, out_fast))
        t0 = time()
```

```
dx_naive, dw_naive, db_naive = conv_backward_naive(dout, cache_naive)
         t1 = time()
         dx_fast, dw_fast, db_fast = conv_backward_fast(dout, cache_fast)
         t2 = time()
         print('\nTesting conv_backward_fast:')
         print('Naive: %fs' % (t1 - t0))
         print('Fast: %fs' % (t2 - t1))
         print('Speedup: %fx' % ((t1 - t0) / (t2 - t1)))
         print('dx difference: ', rel_error(dx_naive, dx_fast))
        print('dw difference: ', rel_error(dw_naive, dw_fast))
print('db difference: ', rel_error(db_naive, db_fast))
        Testing conv forward fast:
        Naive: 1.668772s
        Fast: 0.003283s
        Speedup: 508.340257x
        Difference: 1.1453941607283845e-10
        Testing conv backward fast:
        Naive: 2.635268s
        Fast: 0.007747s
        Speedup: 340.169113x
        dx difference: 4.338719039146703e-12
        dw difference: 4.886114125336343e-13
        db difference: 8.907336046324406e-14
In []: from utils.fast layers import max pool forward fast, max pool backward fast
        x = np.random.randn(100, 3, 32, 32)
         dout = np.random.randn(100, 3, 16, 16)
         pool_param = {'pool_height': 2, 'pool_width': 2, 'stride': 2}
         t0 = time()
         out naive, cache naive = max pool forward naive(x, pool param)
         t1 = time()
         out fast, cache fast = max pool forward fast(x, pool param)
         t2 = time()
         print('Testing pool_forward_fast:')
         print('Naive: %fs' % (t1 - t0))
         print('fast: %fs' % (t2 - t1))
         print('speedup: %fx' % ((t1 - t0) / (t2 - t1)))
         print('difference: ', rel_error(out_naive, out_fast))
         t0 = time()
         dx_naive = max_pool_backward_naive(dout, cache_naive)
         t1 = time()
         dx_fast = max_pool_backward_fast(dout, cache_fast)
         t2 = time()
         print('\nTesting pool_backward_fast:')
         print('Naive: %fs' % (t1 - t0))
         print('speedup: %fx' % ((t1 - t0) / (t2 - t1)))
         print('dx difference: ', rel_error(dx_naive, dx_fast))
```

```
Testing pool_forward_fast:
Naive: 0.175092s
fast: 0.001499s
speedup: 116.792144x
difference: 0.0

Testing pool_backward_fast:
Naive: 0.181028s
speedup: 35.130986x
dx difference: 1.0
```

## Implementation of cascaded layers

We've provided the following functions in nndl/conv\_layer\_utils.py :

```
conv_relu_forwardconv_relu_backwardconv_relu_pool_forwardconv_relu_pool_backward
```

These use the fast implementations of the conv net layers. You can test them below:

```
In [ ]: from nndl.conv_layer_utils import conv_relu_pool_forward, conv_relu_pool_bac
        x = np.random.randn(2, 3, 16, 16)
        w = np.random.randn(3, 3, 3, 3)
        b = np.random.randn(3,)
        dout = np.random.randn(2, 3, 8, 8)
        conv_param = {'stride': 1, 'pad': 1}
        pool_param = {'pool_height': 2, 'pool_width': 2, 'stride': 2}
        out, cache = conv_relu_pool_forward(x, w, b, conv_param, pool_param)
        dx, dw, db = conv_relu_pool_backward(dout, cache)
        dx_num = eval_numerical_gradient_array(lambda x: conv_relu_pool_forward(x, v
        dw_num = eval_numerical_gradient_array(lambda w: conv_relu_pool_forward(x,
        db_num = eval_numerical_gradient_array(lambda b: conv_relu_pool_forward(x, v
        print('Testing conv_relu_pool')
        print('dx error: ', rel_error(dx_num, dx))
        print('dw error: ', rel_error(dw_num, dw))
        print('db error: ', rel_error(db_num, db))
        Testing conv_relu_pool
        dx error: 7.219458272573818e-09
        dw error: 6.087323464150389e-10
        db error: 6.544846206436092e-11
In [ ]: | from nndl.conv_layer_utils import conv_relu_forward, conv_relu_backward
        x = np.random.randn(2, 3, 8, 8)
        w = np.random.randn(3, 3, 3, 3)
        b = np.random.randn(3,)
        dout = np.random.randn(2, 3, 8, 8)
        conv_param = {'stride': 1, 'pad': 1}
        out, cache = conv_relu_forward(x, w, b, conv_param)
        dx, dw, db = conv_relu_backward(dout, cache)
        dx_num = eval_numerical_gradient_array(lambda x: conv_relu_forward(x, w, b,
```

```
dw_num = eval_numerical_gradient_array(lambda w: conv_relu_forward(x, w, b,
db_num = eval_numerical_gradient_array(lambda b: conv_relu_forward(x, w, b,

print('Testing conv_relu:')
print('dx error: ', rel_error(dx_num, dx))
print('dw error: ', rel_error(dw_num, dw))
print('db error: ', rel_error(db_num, db))
```

Testing conv\_relu:

dx error: 9.794782245421235e-10 dw error: 2.1483016236566917e-10 db error: 6.71836478000241e-11

#### What next?

We saw how helpful batch normalization was for training FC nets. In the next notebook, we'll implement a batch normalization for convolutional neural networks, and then finish off by implementing a CNN to improve our validation accuracy on CIFAR-10.

2024/2/29 13:46 CNN-BatchNorm

## Spatial batch normalization

In fully connected networks, we performed batch normalization on the activations. To do something equivalent on CNNs, we modify batch normalization slightly.

Normally batch-normalization accepts inputs of shape (N, D) and produces outputs of shape (N, D), where we normalize across the minibatch dimension N. For data coming from convolutional layers, batch normalization accepts inputs of shape (N, C, H, W) and produces outputs of shape (N, C, H, W) where the N dimension gives the minibatch size and the (H, W) dimensions give the spatial size of the feature map.

Since spatial batch norm and batch normalization are similar, it'd be good to at this point also copy and paste our prior implemented layers from HW #4. Please copy and paste your prior implemented code from HW #4 to start this assignment. If you did not correctly implement the layers in HW #4, you may collaborate with a classmate to use their implementations from HW #4. You may also visit TA or Prof OH to correct your implementation.

You'll want to copy and paste from HW #4:

- layers.py for your FC network layers, as well as batchnorm and dropout.
- layer\_utils.py for your combined FC network layers.
- optim.py for your optimizers.

Be sure to place these in the <a href="nndl/">nndl/</a> directory so they're imported correctly. Note, as announced in class, we will not be releasing our solutions.

If you use your prior implementations of the batchnorm, then your spatial batchnorm implementation may be very short. Our implementations of the forward and backward pass are each 6 lines of code.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, their layer structure, and their implementation of fast CNN layers. This also includes nndl.fc\_net, nndl.layers, and nndl.layer\_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

2024/2/29 13:46 CNN-BatchNorm

```
In []: ## Import and setups
        import time
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl.conv layers import *
        from utils.data_utils import get_CIFAR10_data
        from utils.gradient_check import eval_numerical_gradient, eval_numerical_gra
        from utils.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload-of-modules-in-ik
        %load ext autoreload
        %autoreload 2
        def rel_error(x, y):
          """ returns relative error """
          return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

# Spatial batch normalization forward pass

Implement the forward pass, spatial\_batchnorm\_forward in nndl/conv\_layers.py . Test your implementation by running the cell below.

```
In [ ]: # Check the training—time forward pass by checking means and variances
         # of features both before and after spatial batch normalization
        N, C, H, W = 2, 3, 4, 5
         x = 4 * np.random.randn(N, C, H, W) + 10
         print('Before spatial batch normalization:')
         print(' Shape: ', x.shape)
         print(' Means: ', x.mean(axis=(0, 2, 3)))
         print(' Stds: ', x.std(axis=(0, 2, 3)))
         # Means should be close to zero and stds close to one
         gamma, beta = np.ones(C), np.zeros(C)
         bn_param = {'mode': 'train'}
         out, _ = spatial_batchnorm_forward(x, gamma, beta, bn_param)
         print('After spatial batch normalization:')
         print(' Shape: ', out.shape)
print(' Means: ', out.mean(axis=(0, 2, 3)))
print(' Stds: ', out.std(axis=(0, 2, 3)))
         # Means should be close to beta and stds close to gamma
         gamma, beta = np.asarray([3, 4, 5]), np.asarray([6, 7, 8])
         out, _ = spatial_batchnorm_forward(x, gamma, beta, bn_param)
         print('After spatial batch normalization (nontrivial gamma, beta):')
         print(' Shape: ', out.shape)
         print(' Means: ', out.mean(axis=(0, 2, 3)))
         print(' Stds: ', out.std(axis=(0, 2, 3)))
```

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```
Before spatial batch normalization:
    Shape: (2, 3, 4, 5)
    Means: [10.50357688 10.51030877 11.43714596]
    Stds: [3.77219514 4.29569943 4.05931067]

After spatial batch normalization:
    Shape: (2, 3, 4, 5)
    Means: [-1.66533454e-17 -8.32667268e-17 -2.22044605e-16]
    Stds: [0.99999965 0.99999973 0.9999997]

After spatial batch normalization (nontrivial gamma, beta):
    Shape: (2, 3, 4, 5)
    Means: [6. 7. 8.]
    Stds: [2.99999895 3.99999892 4.99999848]
```

## Spatial batch normalization backward pass

Implement the backward pass, spatial\_batchnorm\_backward in nndl/conv\_layers.py . Test your implementation by running the cell below.

```
In []: N, C, H, W = 2, 3, 4, 5
        x = 5 * np.random.randn(N, C, H, W) + 12
        gamma = np.random.randn(C)
        beta = np.random.randn(C)
        dout = np.random.randn(N, C, H, W)
        bn_param = {'mode': 'train'}
        fx = lambda x: spatial batchnorm forward(x, gamma, beta, bn param)[0]
        fg = lambda a: spatial batchnorm forward(x, gamma, beta, bn param)[0]
        fb = lambda b: spatial_batchnorm_forward(x, gamma, beta, bn_param)[0]
        dx_num = eval_numerical_gradient_array(fx, x, dout)
        da_num = eval_numerical_gradient_array(fg, gamma, dout)
        db_num = eval_numerical_gradient_array(fb, beta, dout)
        _, cache = spatial_batchnorm_forward(x, gamma, beta, bn_param)
        dx, dgamma, dbeta = spatial_batchnorm_backward(dout, cache)
        print('dx error: ', rel_error(dx_num, dx))
        print('dgamma error: ', rel_error(da_num, dgamma))
        print('dbeta error: ', rel_error(db_num, dbeta))
```

dx error: 1.543416794185354e-08 dgamma error: 3.7746163369837325e-12 dbeta error: 2.275653908839388e-12

## Convolutional neural networks

In this notebook, we'll put together our convolutional layers to implement a 3-layer CNN. Then, we'll ask you to implement a CNN that can achieve > 65% validation error on CIFAR-10.

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, their layer structure, and their implementation of fast CNN layers. This also includes nndl.fc\_net, nndl.layers, and nndl.layer\_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

If you have not completed the Spatial BatchNorm Notebook, please see the following description from that notebook:

Please copy and paste your prior implemented code from HW #4 to start this assignment. If you did not correctly implement the layers in HW #4, you may collaborate with a classmate to use their layer implementations from HW #4. You may also visit TA or Prof OH to correct your implementation.

You'll want to copy and paste from HW #4:

- layers.py for your FC network layers, as well as batchnorm and dropout.
- layer\_utils.py for your combined FC network layers.
- optim.py for your optimizers.

Be sure to place these in the <a href="nndl/">nndl/</a> directory so they're imported correctly. Note, as announced in class, we will not be releasing our solutions.

```
In [ ]: # As usual, a bit of setup
        import numpy as np
        import matplotlib.pyplot as plt
        from nndl.cnn import *
        from utils.data_utils import get_CIFAR10_data
        from utils.gradient_check import eval_numerical_gradient_array, eval_numeric
        from nndl.layers import *
        from nndl.conv_layers import *
        from utils.fast_layers import *
        from utils.solver import Solver
        %matplotlib inline
        plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
        plt.rcParams['image.interpolation'] = 'nearest'
        plt.rcParams['image.cmap'] = 'gray'
        # for auto-reloading external modules
        # see http://stackoverflow.com/questions/1907993/autoreload—of—modules—in—ik
        %load_ext autoreload
```

```
%autoreload 2

def rel_error(x, y):
    """ returns relative error """
    return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
```

```
In []: # Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
    for k in data.keys():
        print('{}: {} '.format(k, data[k].shape))

X_train: (49000, 3, 32, 32)
    y_train: (49000,)
    X_val: (1000, 3, 32, 32)
    y_val: (1000,)
    X_test: (1000, 3, 32, 32)
    y_test: (1000,)
```

## Three layer CNN

In this notebook, you will implement a three layer CNN. The <a href="ThreeLayerConvNet">ThreeLayerConvNet</a> class is in <a href="nndl/cnn.py">nndl/cnn.py</a>. You'll need to modify that code for this section, including the initialization, as well as the calculation of the loss and gradients. You should be able to use the building blocks you have either earlier coded or that we have provided. Be sure to use the fast layers.

The architecture of this CNN will be:

```
conv - relu - 2x2 max pool - affine - relu - affine - softmax
```

We won't use batchnorm yet. You've also done enough of these to know how to debug; use the cells below.

Note: As we are implementing several layers CNN networks. The gradient error can be expected for the eval\_numerical\_gradient() function. If your W1 max relative error and W2 max relative error are around or below 0.01, they should be acceptable. Other errors should be less than 1e-5.

```
In [ ]:
         num_inputs = 2
         input_dim = (3, 16, 16)
         reg = 0.0
         num classes = 10
         X = np.random.randn(num inputs, *input dim)
         y = np.random.randint(num_classes, size=num_inputs)
         model = ThreeLayerConvNet(num_filters=3, filter_size=3,
                                      input_dim=input_dim, hidden_dim=7,
                                      dtype=np.float64)
         loss, grads = model.loss(X, y)
         for param_name in sorted(grads):
             f = lambda _: model.loss(X, y)[0]
             param_grad_num = eval_numerical_gradient(f, model.params[param_name], vertical_gradient(f, model.params[param_name])
             e = rel_error(param_grad_num, grads[param_name])
             print('{} max relative error: {}'.format(param_name, rel_error(param_grame))
```

```
W1 max relative error: 0.0002363098827308143
W2 max relative error: 0.012834558109218656
W3 max relative error: 5.944032603719739e-05
b1 max relative error: 6.925269117802639e-05
b2 max relative error: 1.1801826476487836e-07
b3 max relative error: 5.831459607789406e-10
```

#### Overfit small dataset

To check your CNN implementation, let's overfit a small dataset.

```
num train = 100
In [ ]:
        small data = {
          'X_train': data['X_train'][:num_train],
          'y_train': data['y_train'][:num_train],
          'X_val': data['X_val'],
          'y_val': data['y_val'],
        model = ThreeLayerConvNet(weight scale=1e-2)
        solver = Solver(model, small data,
                         num_epochs=10, batch_size=50,
                         update_rule='adam',
                         optim_config={
                           'learning_rate': 1e-3,
                         },
                         verbose=True, print every=1)
        solver.train()
        (Iteration 1 / 20) loss: 2.362546
        (Epoch 0 / 10) train acc: 0.170000; val acc: 0.117000
        (Iteration 2 / 20) loss: 3.979359
        (Epoch 1 / 10) train acc: 0.170000; val acc: 0.119000
        (Iteration 3 / 20) loss: 3.316965
        (Iteration 4 / 20) loss: 2.733217
        (Epoch 2 / 10) train acc: 0.260000; val_acc: 0.119000
        (Iteration 5 / 20) loss: 2.562140
        (Iteration 6 / 20) loss: 2.161792
        (Epoch 3 / 10) train acc: 0.380000; val_acc: 0.160000
        (Iteration 7 / 20) loss: 2.253736
        (Iteration 8 / 20) loss: 1.859916
        (Epoch 4 / 10) train acc: 0.400000; val_acc: 0.098000
        (Iteration 9 / 20) loss: 1.753295
        (Iteration 10 / 20) loss: 1.646840
        (Epoch 5 / 10) train acc: 0.520000; val_acc: 0.119000
        (Iteration 11 / 20) loss: 1.546418
        (Iteration 12 / 20) loss: 1.308756
        (Epoch 6 / 10) train acc: 0.570000; val_acc: 0.186000
        (Iteration 13 / 20) loss: 1.267099
        (Iteration 14 / 20) loss: 1.214133
        (Epoch 7 / 10) train acc: 0.660000; val_acc: 0.190000
        (Iteration 15 / 20) loss: 1.129290
        (Iteration 16 / 20) loss: 1.203855
        (Epoch 8 / 10) train acc: 0.700000; val_acc: 0.203000
        (Iteration 17 / 20) loss: 0.843799
        (Iteration 18 / 20) loss: 0.974359
        (Epoch 9 / 10) train acc: 0.750000; val_acc: 0.172000
        (Iteration 19 / 20) loss: 0.854074
        (Iteration 20 / 20) loss: 0.625796
        (Epoch 10 / 10) train acc: 0.800000; val_acc: 0.196000
```

```
plt.subplot(2, 1, 1)
In [ ]:
         plt.plot(solver.loss_history, 'o')
         plt.xlabel('iteration')
         plt.ylabel('loss')
          plt.subplot(2, 1, 2)
          plt.plot(solver.train_acc_history, '-o')
         plt.plot(solver.val_acc_history, '-o')
         plt.legend(['train', 'val'], loc='upper left')
         plt.xlabel('epoch')
          plt.ylabel('accuracy')
         plt.show()
            4.0
            3.5
            3.0
           2.5
            2.0
           1.5
            1.0
            0.5
                           2.5
                                     5.0
                                               7.5
                                                                  12.5
                 0.0
                                                        10.0
                                                                           15.0
                                                                                     17.5
                                                    iteration
            0.8
                   train
                    val
            0.7
            0.6
           0.5
           0.4
            0.3
            0.2
            0.1
                                                                                            10
                                                      epoch
```

#### Train the network

Now we train the 3 layer CNN on CIFAR-10 and assess its accuracy.

```
(Iteration 1 / 980) loss: 2.304323
(Epoch 0 / 1) train acc: 0.136000; val_acc: 0.136000
(Iteration 21 / 980) loss: 2.207954
(Iteration 41 / 980) loss: 1.798766
(Iteration 61 / 980) loss: 2.064802
(Iteration 81 / 980) loss: 1.861099
(Iteration 101 / 980) loss: 1.855049
(Iteration 121 / 980) loss: 1.658991
(Iteration 141 / 980) loss: 1.815817
(Iteration 161 / 980) loss: 1.326318
(Iteration 181 / 980) loss: 2.022595
(Iteration 201 / 980) loss: 1.641709
(Iteration 221 / 980) loss: 1.877826
(Iteration 241 / 980) loss: 1.631371
(Iteration 261 / 980) loss: 1.531714
(Iteration 281 / 980) loss: 1.780931
(Iteration 301 / 980) loss: 1.527178
(Iteration 321 / 980) loss: 1.604898
(Iteration 341 / 980) loss: 1.758340
(Iteration 361 / 980) loss: 1.561351
(Iteration 381 / 980) loss: 1.527699
(Iteration 401 / 980) loss: 1.850302
(Iteration 421 / 980) loss: 1.766610
(Iteration 441 / 980) loss: 1.990235
(Iteration 461 / 980) loss: 1.544909
(Iteration 481 / 980) loss: 1.832894
(Iteration 501 / 980) loss: 1.741829
(Iteration 521 / 980) loss: 1.813254
(Iteration 541 / 980) loss: 2.070675
(Iteration 561 / 980) loss: 1.631089
(Iteration 581 / 980) loss: 1.598499
(Iteration 601 / 980) loss: 1.402315
(Iteration 621 / 980) loss: 1.830516
(Iteration 641 / 980) loss: 1.582647
(Iteration 661 / 980) loss: 1.710053
(Iteration 681 / 980) loss: 1.641495
(Iteration 701 / 980) loss: 1.408017
(Iteration 721 / 980) loss: 1.378994
(Iteration 741 / 980) loss: 1.896228
(Iteration 761 / 980) loss: 1.525349
(Iteration 781 / 980) loss: 1.287301
(Iteration 801 / 980) loss: 1.543243
(Iteration 821 / 980) loss: 1.866409
(Iteration 841 / 980) loss: 1.753571
(Iteration 861 / 980) loss: 1.728755
(Iteration 881 / 980) loss: 1.578095
(Iteration 901 / 980) loss: 1.547145
(Iteration 921 / 980) loss: 1.493463
(Iteration 941 / 980) loss: 1.406413
(Iteration 961 / 980) loss: 1.725868
(Epoch 1 / 1) train acc: 0.462000; val_acc: 0.451000
```

# Get > 65% validation accuracy on CIFAR-10.

In the last part of the assignment, we'll now ask you to train a CNN to get better than 65% validation accuracy on CIFAR-10.

## Things you should try:

• Filter size: Above we used 7x7; but VGGNet and onwards showed stacks of 3x3 filters are good.

- Number of filters: Above we used 32 filters. Do more or fewer do better?
- Batch normalization: Try adding spatial batch normalization after convolution layers and vanilla batch normalization aafter affine layers. Do your networks train faster?
- Network architecture: Can a deeper CNN do better? Consider these architectures:
  - [conv-relu-pool]xN conv relu [affine]xM [softmax or SVM]
  - [conv-relu-pool]XN [affine]XM [softmax or SVM]
  - [conv-relu-conv-relu-pool]xN [affine]xM [softmax or SVM]

#### Tips for training

For each network architecture that you try, you should tune the learning rate and regularization strength. When doing this there are a couple important things to keep in mind:

- If the parameters are working well, you should see improvement within a few hundred iterations
- Remember the coarse-to-fine approach for hyperparameter tuning: start by testing
  a large range of hyperparameters for just a few training iterations to find the
  combinations of parameters that are working at all.
- Once you have found some sets of parameters that seem to work, search more finely around these parameters. You may need to train for more epochs.

```
(Iteration 1 / 366) loss: 2.304626
(Epoch 0 / 6) train acc: 0.098000; val_acc: 0.105000
(Iteration 21 / 366) loss: 1.760903
(Iteration 41 / 366) loss: 1.561822
(Iteration 61 / 366) loss: 1.403849
(Epoch 1 / 6) train acc: 0.509000; val_acc: 0.502000
(Iteration 81 / 366) loss: 1.353386
(Iteration 101 / 366) loss: 1.360045
(Iteration 121 / 366) loss: 1.198331
(Epoch 2 / 6) train acc: 0.566000; val acc: 0.581000
(Iteration 141 / 366) loss: 1.176595
(Iteration 161 / 366) loss: 1.101311
(Iteration 181 / 366) loss: 1.077048
(Epoch 3 / 6) train acc: 0.655000; val_acc: 0.622000
(Iteration 201 / 366) loss: 1.035905
(Iteration 221 / 366) loss: 1.099724
(Iteration 241 / 366) loss: 0.928033
(Epoch 4 / 6) train acc: 0.706000; val_acc: 0.650000
(Iteration 261 / 366) loss: 0.974193
(Iteration 281 / 366) loss: 0.901123
(Iteration 301 / 366) loss: 0.867813
(Epoch 5 / 6) train acc: 0.730000; val_acc: 0.634000
(Iteration 321 / 366) loss: 0.819308
(Iteration 341 / 366) loss: 0.796763
(Iteration 361 / 366) loss: 0.777600
(Epoch 6 / 6) train acc: 0.713000; val_acc: 0.653000
```

In []:

```
import numpy as np
# Now you can import your modules
from .layers import *
from .conv layers import *
from utils.fast_layers import *
from .layer_utils import *
from .conv layer utils import *
import pdb
,,,,,,,
This code was originally written for CS 231n at Stanford University
(cs231n.stanford.edu). It has been modified in various areas for use in the
ECE 239AS class at UCLA. This includes the descriptions of what code to
implement as well as some slight potential changes in variable names to be
consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
permission to use this code. To see the original version, please visit
cs231n.stanford.edu.
class ThreeLayerConvNet (object):
 A three-layer convolutional network with the following architecture:
 conv - relu - 2x2 max pool - affine - relu - affine - softmax
 The network operates on minibatches of data that have shape (N, C, H, W)
 consisting of N images, each with height H and width W and with C input
 channels.
 def init (self, input dim=(3, 32, 32), num filters=32, filter size=7,
              hidden_dim=100, num_classes=10, weight_scale=1e-3, reg=0.0,
              dtype=np.float32, use_batchnorm=False):
   Initialize a new network.
   Inputs:
   - input_dim: Tuple (C, H, W) giving size of input data
   - num filters: Number of filters to use in the convolutional layer
   - filter_size: Size of filters to use in the convolutional layer
    - hidden dim: Number of units to use in the fully-connected hidden layer
    - num classes: Number of scores to produce from the final affine layer.
   - weight scale: Scalar giving standard deviation for random initialization
     of weights.
    - reg: Scalar giving L2 regularization strength
    - dtype: numpy datatype to use for computation.
   self.use batchnorm = use batchnorm
   self.params = {}
   self.reg = reg
   self.dtype = dtype
    # YOUR CODE HERE:
      Initialize the weights and biases of a three layer CNN. To initialize:
```

```
# - the biases should be initialized to zeros.
      - the weights should be initialized to a matrix with entries
         drawn from a Gaussian distribution with zero mean and
         standard deviation given by weight scale.
  # ------ #
  C,H,W = input dim
  size w1 = (num filters, C, filter size, filter size)
  size b1 = num filters
  size w2 = (hidden dim, (H//2)*(W//2)*num filters)
  size_b2 = hidden dim
  size w3 = (num classes, hidden dim)
  size b3 = num_classes
  self.params['W1'] = np.random.normal(loc=0.0, scale=weight scale, size = size w1)
  self.params['b1'] = np.zeros(size b1)
  self.params['W2'] = np.random.normal(loc=0.0, scale=weight scale, size = size w2).T
  self.params['b2'] = np.zeros(size b2)
  self.params['W3'] = np.random.normal(loc=0.0, scale=weight scale, size = size w3).T
  self.params['b3'] = np.zeros(size b3)
  # ----- #
  # END YOUR CODE HERE
  # ______ #
  for k, v in self.params.items():
   self.params[k] = v.astype(dtype)
def loss(self, X, y=None):
  Evaluate loss and gradient for the three-layer convolutional network.
  Input / output: Same API as TwoLayerNet in fc_net.py.
  11 11 11
  W1, b1 = self.params['W1'], self.params['b1']
  W2, b2 = self.params['W2'], self.params['b2']
  W3, b3 = self.params['W3'], self.params['b3']
  # pass conv param to the forward pass for the convolutional layer
  filter_size = W1.shape[2]
  conv_param = {'stride': 1, 'pad': (filter_size - 1) / 2}
  # pass pool param to the forward pass for the max-pooling layer
  pool param = {'pool height': 2, 'pool width': 2, 'stride': 2}
  scores = None
  # ----- #
  # YOUR CODE HERE:
    Implement the forward pass of the three layer CNN. Store the output
    scores as the variable "scores".
  # Forward pass
  out pool fast, cache pool fast = conv relu pool forward(X, W1, b1, conv param, pool param)
  out_affine_Relu_fast, cache_affine_Relu_fast = affine_relu_forward(out_pool_fast, W2, b2)
  scores, cache affine fast = affine forward(out affine Relu fast, W3, b3)
  # ----- #
  # END YOUR CODE HERE
  if y is None:
   return scores
```

```
loss, grads = 0, {}
   # YOUR CODE HERE:
     Implement the backward pass of the three layer CNN. Store the grads
     in the grads dictionary, exactly as before (i.e., the gradient of
     self.params[k] will be grads[k]). Store the loss as "loss", and
    don't forget to add regularization on ALL weight matrices.
   # ----- #
   # Compute the loss
   loss, dscores = softmax loss(scores, y)
   # Backward pass: compute gradients
   dout affine Relu fast, grads['W3'], grads['b3'] = affine backward(dscores,
cache affine fast)
   dout pool fast, grads['W2'], grads['b2'] = affine relu backward(dout affine Relu fast,
cache affine Relu fast)
   dx, grads['W1'], grads['b1'] = conv relu pool backward(dout pool fast, cache pool fast)
   \# Add regularization to the loss and gradients for W1, W2, and W3
   loss += 0.5 * self.reg * (np.sum(W1 * W1) + np.sum(W2 * W2) + np.sum(W3 * W3))
   grads['W1'] += self.reg * W1
   grads['W2'] += self.reg * W2
   grads['W3'] += self.reg * W3
   # END YOUR CODE HERE
   # ----- #
   return loss, grads
```

pass

```
from nndl.layers import *
import pdb
This code was originally written for CS 231n at Stanford University
(cs231n.stanford.edu). It has been modified in various areas for use in the
ECE 239AS class at UCLA. This includes the descriptions of what code to
implement as well as some slight potential changes in variable names to be
consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
permission to use this code. To see the original version, please visit
cs231n.stanford.edu.
def conv forward naive(x, w, b, conv param):
 A naive implementation of the forward pass for a convolutional layer.
  The input consists of N data points, each with C channels, height H and width
  W. We convolve each input with F different filters, where each filter spans
  all C channels and has height HH and width HH.
 Input:
  - x: Input data of shape (N, C, H, W)
  - w: Filter weights of shape (F, C, HH, WW)
  - b: Biases, of shape (F,)
  - conv param: A dictionary with the following keys:
   - 'stride': The number of pixels between adjacent receptive fields in the
     horizontal and vertical directions.
   - 'pad': The number of pixels that will be used to zero-pad the input.
  Returns a tuple of:
  - out: Output data, of shape (N, F, H', W') where H' and W' are given by
   H' = 1 + (H + 2 * pad - HH) / stride
   W' = 1 + (W + 2 * pad - WW) / stride
  - cache: (x, w, b, conv_param)
  11 11 11
 out = None
 pad = conv_param['pad']
  stride = conv param['stride']
  # ------ #
  # YOUR CODE HERE:
  # Implement the forward pass of a convolutional neural network.
  # Store the output as 'out'.
  # Hint: to pad the array, you can use the function np.pad.
  # ----- #
  N, C, H, W = x.shape
  F, _, HH, WW = w.shape
  out height = 1 + (H + 2 * pad - HH) // stride
 out width = 1 + (W + 2 * pad - WW) // stride
  out = np.zeros((N, F, out_height, out_width))
  # Pad the input
  x \text{ pad} = \text{np.pad}(x, ((0, 0), (0, 0), (pad, pad), (pad, pad)), mode='constant',
constant values=0)
  for n in range(N):
       for f in range(F):
           for i in range(out height):
               for j in range(out width):
                   h start = i * stride
                   w_start = j * stride
                   h end = h start + HH
                   w = m = w = m + WW
                   x_slice = x_pad[n, :, h_start:h_end, w_start:w_end]
                   out[n, f, i, j] = np.sum(x_slice * w[f, :, :, :]) + b[f]
```

import numpy as np

```
# END YOUR CODE HERE
    cache = (x, w, b, conv param)
   return out, cache
def conv_backward_naive(dout, cache):
   A naive implementation of the backward pass for a convolutional layer.
   Inputs:
   - dout: Upstream derivatives.
   - cache: A tuple of (x, w, b, conv param) as in conv forward naive
   Returns a tuple of:
   - dx: Gradient with respect to x
   - dw: Gradient with respect to w
    - db: Gradient with respect to b
   dx, dw, db = None, None, None
   N, F, out height, out width = dout.shape
   x, w, b, conv param = cache
   stride, pad = [conv_param['stride'], conv_param['pad']]
   xpad = np.pad(x, ((0,0), (0,0), (pad,pad), (pad,pad)), mode='constant')
   num filts, , f height, f width = w.shape
    # ------ #
    # YOUR CODE HERE:
        Implement the backward pass of a convolutional neural network.
    # Calculate the gradients: dx, dw, and db.
    # ----- #
   dx = np.zeros_like(x)
   dw = np.zeros like(w)
   db = np.zeros like(b)
       # Pad x and dx for the gradient computation
   x_{padded} = np.pad(x, ((0, 0), (0, 0), (pad, pad), (pad, pad)), mode='constant',
constant values=0)
   dx_{padded} = np.pad(dx, ((0, 0), (0, 0), (pad, pad), (pad, pad)), mode='constant',
constant_values=0)
   for n in range(N): # For each image in the input batch
           for f in range(F): # For each filter
                  for i in range(out_height):
                         for j in range(out_width):
                                    h start = i * stride
                                     w_start = j * stride
                                     h end = h start + f height
                                     w = nd = w start + f width
                                     # Calculate gradients
                                     dx_{padded[n, :, h_start:h_end, w_start:w_end]} += w[f, :, :, :] * dout[n, the double of the doubl
f, i, j]
                                     dw[f, :, :, :] += x_padded[n, :, h_start:h_end, w_start:w_end] * dout[n,
f, i, j]
                                     db[f] += dout[n, f, i, j]
       # Unpad dx to get the correct shape
   dx = dx padded[:, :, pad:-pad, pad:-pad]
    # ----- #
    # END YOUR CODE HERE
```

```
return dx, dw, db
def max pool forward naive(x, pool param):
 A naive implementation of the forward pass for a max pooling layer.
 Inputs:
 - x: Input data, of shape (N, C, H, W)
 - pool_param: dictionary with the following keys:
   - 'pool height': The height of each pooling region
   - 'pool width': The width of each pooling region
   - 'stride': The distance between adjacent pooling regions
 Returns a tuple of:
 - out: Output data
  - cache: (x, pool_param)
 out = None
 # YOUR CODE HERE:
   Implement the max pooling forward pass.
 # ----- #
 N, C, H, W = x.shape
 pool height, pool width, stride = pool param['pool height'], pool param['pool width'],
pool param['stride']
   # Calculate output dimensions
 out_height = (H - pool_height) // stride + 1
 out width = (W - pool width) // stride + 1
 out = np.zeros((N, C, out height, out width))
 for n in range(N):
     for c in range(C):
        for i in range(out height):
            for j in range(out width):
                 h start = i * stride
                 w start = j * stride
                 h end = h_start + pool_height
                 w_end = w_start + pool_width
                 x_pooling_region = x[n, c, h_start:h_end, w_start:w_end]
                 out[n, c, i, j] = np.max(x_pooling_region)
  # END YOUR CODE HERE
 # ----- #
 cache = (x, pool_param)
 return out, cache
def max pool backward naive(dout, cache):
 A naive implementation of the backward pass for a max pooling layer.
 Inputs:
 - dout: Upstream derivatives
 - cache: A tuple of (x, pool param) as in the forward pass.
 Returns:
  - dx: Gradient with respect to x
  mmm
 dx = None
 x, pool param = cache
 pool height, pool width, stride = pool param['pool height'], pool param['pool width'],
```

```
pool_param['stride']
  # YOUR CODE HERE:
   Implement the max pooling backward pass.
 # ----- #
 N, C, H, W = x.shape
 out_height = (H - pool_height) // stride + 1
 out width = (W - pool width) // stride + 1
 dx = np.zeros_like(x)
 for n in range(N):
     for c in range(C):
        for i in range(out height):
           for j in range(out_width):
                 h start = i * stride
                 w start = j * stride
                 h end = h start + pool_height
                 w_end = w_start + pool_width
                 # Find the max value in the input region
                 x pooling region = x[n, c, h start:h end, w start:w end]
                 max value = np.max(x pooling region)
                 for i in range(pool height):
                    for j in range(pool width):
                       if x pooling region[i, j] == max value:
                           dx[n, c, h start + i, w start + j] += dout[n, c, i, j]
  # END YOUR CODE HERE
  return dx
def spatial batchnorm forward(x, gamma, beta, bn param):
 Computes the forward pass for spatial batch normalization.
 Inputs:
 - x: Input data of shape (N, C, H, W)
 - gamma: Scale parameter, of shape (C,)
 - beta: Shift parameter, of shape (C,)
  - bn param: Dictionary with the following keys:
   - mode: 'train' or 'test'; required
   - eps: Constant for numeric stability
   - momentum: Constant for running mean / variance. momentum=0 means that
    old information is discarded completely at every time step, while
    momentum=1 means that new information is never incorporated. The
    default of momentum=0.9 should work well in most situations.
   - running mean: Array of shape (D,) giving running mean of features
   - running var Array of shape (D,) giving running variance of features
 Returns a tuple of:
  - out: Output data, of shape (N, C, H, W)
  - cache: Values needed for the backward pass
 out, cache = None, None
  # ----- #
  # YOUR CODE HERE:
    Implement the spatial batchnorm forward pass.
   You may find it useful to use the batchnorm forward pass you
```

```
# implemented in HW #4.
  N, C, H, W = x.shape
 mode = bn param['mode']
 eps = bn param.get('eps', 1e-5)
 momentum = bn param.get('momentum', 0.9)
 running mean = bn param.get('running mean', np.zeros(C, dtype=x.dtype))
 running_var = bn_param.get('running_var', np.zeros(C, dtype=x.dtype))
 if mode == 'train':
       mean = np.mean(x, axis=(0, 2, 3), keepdims=True)
       var = np.var(x, axis=(0, 2, 3), keepdims=True)
       # Update the running mean and variance
       running_mean = momentum * running_mean + (1 - momentum) * mean.squeeze()
       running var = momentum * running var + (1 - momentum) * var.squeeze()
       # Normalize the batch
       x normalized = (x - mean) / np.sqrt(var + eps)
       # Scale and shift
       out = gamma.reshape(1, C, 1, 1) * x normalized + beta.reshape(1, C, 1, 1)
       cache = (x, x normalized, mean, var, gamma, beta, eps)
       # Update bn param
       bn param['running mean'] = running mean
       bn param['running var'] = running var
 elif mode == 'test':
       # Use the running mean and variance to normalize during inference
       x \text{ normalized} = (x - running mean.reshape(1, C, 1, 1)) /
np.sqrt(running var.reshape(1, C, 1, 1) + eps)
       out = gamma.reshape(1, C, 1, 1) * x normalized + beta.reshape(1, C, 1, 1)
       cache = None
 else:
       raise ValueError ('Invalid forward batchnorm mode "%s"' % mode)
  # END YOUR CODE HERE
  # ======================= #
 return out, cache
def spatial batchnorm backward (dout, cache):
 Computes the backward pass for spatial batch normalization.
 Inputs:
 - dout: Upstream derivatives, of shape (N, C, H, W)
 - cache: Values from the forward pass
 Returns a tuple of:
 - dx: Gradient with respect to inputs, of shape (N, C, H, W)
 - dgamma: Gradient with respect to scale parameter, of shape (C,)
  - dbeta: Gradient with respect to shift parameter, of shape (C,)
 dx, dgamma, dbeta = None, None, None
  # ----- #
  # YOUR CODE HERE:
     Implement the spatial batchnorm backward pass.
   You may find it useful to use the batchnorm forward pass you
     implemented in HW #4.
```

```
# ============== #
 x, x_normalized, mean, var, gamma, beta, eps = cache
 N, C, H, W = dout.shape
   # Reshape gamma and dout for easier computation
 gamma reshaped = gamma.reshape(1, C, 1, 1)
 dout_reshaped = dout * gamma_reshaped
   # Compute gradients with respect to the normalized input
 dx normalized = dout reshaped
 dvar = np.sum(dx_normalized * (x - mean) * -0.5 * np.power(var + eps, -1.5), axis=(0, 2, 3),
keepdims=True)
 dmean = np.sum(dx normalized * -1 / np.sqrt(var + eps), axis=(0, 2, 3), keepdims=True) + \
          dvar * np.mean(-2 * (x - mean), axis=(0, 2, 3), keepdims=True)
 dx = dx \text{ normalized / np.sqrt(var + eps) + }
       dvar * 2 * (x - mean) / (N * H * W) + 
       dmean / (N ^{\star} H ^{\star} W)
 dgamma = np.sum(dout * x normalized, axis=(0, 2, 3))
 dbeta = np.sum(dout, axis=(0, 2, 3))
   # Reshape gradients back to their original shapes
 dx = dx.reshape(N, C, H, W)
 dgamma = dgamma.reshape(C,)
 dbeta = dbeta.reshape(C,)
 # ------ #
 # END YOUR CODE HERE
 return dx, dgamma, dbeta
```

```
import numpy as np
import pdb
This code was originally written for CS 231n at Stanford University
(cs231n.stanford.edu). It has been modified in various areas for use in the
ECE 239AS class at UCLA. This includes the descriptions of what code to
implement as well as some slight potential changes in variable names to be
consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for
permission to use this code. To see the original version, please visit
cs231n.stanford.edu.
def affine forward(x, w, b):
 Computes the forward pass for an affine (fully-connected) layer.
 The input x has shape (N, d 1, \ldots, d k) and contains a minibatch of N
 examples, where each example x[i] has shape (d_1, \ldots, d_k). We will
 reshape each input into a vector of dimension D = d \ 1 \ * \ldots \ * \ d \ k, and
 then transform it to an output vector of dimension M.
 Inputs:
 - x: A numpy array containing input data, of shape (N, d 1, ..., d k)
 - w: A numpy array of weights, of shape (D, M)
  - b: A numpy array of biases, of shape (M,)
 Returns a tuple of:
 - out: output, of shape (N, M)
  - cache: (x, w, b)
  # ----- #
  # YOUR CODE HERE:
   Calculate the output of the forward pass. Notice the dimensions
    of w are D x M, which is the transpose of what we did in earlier
    assignments.
  out = np.dot(x.reshape(x.shape[0], -1), w) + b
 pass
  # ------ #
  # END YOUR CODE HERE
  # ------ #
 cache = (x, w, b)
 return out, cache
def affine backward(dout, cache):
 Computes the backward pass for an affine layer.
 Inputs:
 - dout: Upstream derivative, of shape (N, M)
  - cache: Tuple of:
   - x: Input data, of shape (N, d 1, ... d k)
   - w: Weights, of shape (D, M)
 Returns a tuple of:
 - dx: Gradient with respect to x, of shape (N, d1, ..., d k)
  - dw: Gradient with respect to w, of shape (D, M)
  - db: Gradient with respect to b, of shape (M,)
  11 11 11
 x, w, b = cache
 dx, dw, db = None, None, None
```

```
# ------ #
 # YOUR CODE HERE:
 # Calculate the gradients for the backward pass.
 # ============== #
 dx = np.dot(dout, w.T).reshape(x.shape)
 dw = np.dot(x.reshape(x.shape[0], -1).T, dout)
 db = np.sum(dout, axis=0)
 # ------ #
 # END YOUR CODE HERE
 # ------ #
 return dx, dw, db
def relu forward(x):
 Computes the forward pass for a layer of rectified linear units (ReLUs).
 Input:
 - x: Inputs, of any shape
 Returns a tuple of:
 - out: Output, of the same shape as x
 - cache: x
 # ----- #
 # YOUR CODE HERE:
   Implement the ReLU forward pass.
 out = np.maximum(0, x)
 # ======================= #
 # END YOUR CODE HERE
 # ------ #
 cache = x
 return out, cache
def relu backward(dout, cache):
 Computes the backward pass for a layer of rectified linear units (ReLUs).
 - dout: Upstream derivatives, of any shape
 - cache: Input x, of same shape as dout
 Returns:
 - dx: Gradient with respect to x
 11 11 11
 x = cache
 # ------ #
 # YOUR CODE HERE:
   Implement the ReLU backward pass
 # ------ #
 dx = (x > 0) * dout
 # ------ #
 # END YOUR CODE HERE
```

```
def batchnorm forward(x, gamma, beta, bn param):
 Forward pass for batch normalization.
 During training the sample mean and (uncorrected) sample variance are
 computed from minibatch statistics and used to normalize the incoming data.
 During training we also keep an exponentially decaying running mean of the mean
 and variance of each feature, and these averages are used to normalize data
  at test-time.
 At each timestep we update the running averages for mean and variance using
  an exponential decay based on the momentum parameter:
 running mean = momentum * running mean + (1 - momentum) * sample mean
 running_var = momentum * running_var + (1 - momentum) * sample_var
 Note that the batch normalization paper suggests a different test-time
 behavior: they compute sample mean and variance for each feature using a
  large number of training images rather than using a running average. For
  this implementation we have chosen to use running averages instead since
  they do not require an additional estimation step; the torch7 implementation
 of batch normalization also uses running averages.
 Input:
  - x: Data of shape (N, D)
  - gamma: Scale parameter of shape (D,)
  - beta: Shift paremeter of shape (D,)
  - bn param: Dictionary with the following keys:
   - mode: 'train' or 'test'; required
   - eps: Constant for numeric stability
   - momentum: Constant for running mean / variance.
   - running mean: Array of shape (D,) giving running mean of features
   - running var Array of shape (D,) giving running variance of features
  Returns a tuple of:
  - out: of shape (N, D)
  - cache: A tuple of values needed in the backward pass
 mode = bn param['mode']
  eps = bn param.get('eps', 1e-5)
 momentum = bn param.get('momentum', 0.9)
 N, D = x.shape
  running mean = bn param.get('running mean', np.zeros(D, dtype=x.dtype))
  running var = bn param.get('running var', np.zeros(D, dtype=x.dtype))
  out, cache = None, None
  if mode == 'train':
   # ----- #
   # YOUR CODE HERE:
      A few steps here:
         (1) Calculate the running mean and variance of the minibatch.
         (2) Normalize the activations with the running mean and variance.
         (3) Scale and shift the normalized activations. Store this
            as the variable 'out'
         (4) Store any variables you may need for the backward pass in
          the 'cache' variable.
    # ------ #
   sample mean = np.mean(x, axis=0)
   sample var = np.var(x, axis=0)
   x 	ext{ normalized} = (x - sample mean) / np.sqrt(sample var + eps)
   out = gamma * x normalized + beta
   running_mean = momentum * running_mean + (1 - momentum) * sample_mean
```

```
running_var = momentum * running_var + (1 - momentum) * sample_var
      cache = (x, x_normalized, gamma, beta, sample_mean, sample_var, eps)
      # ----- #
      # END YOUR CODE HERE
       elif mode == 'test':
      # ----- #
      # YOUR CODE HERE:
      # Calculate the testing time normalized activation. Normalize using
          the running mean and variance, and then scale and shift appropriately.
      # Store the output as 'out'.
      x normalized = (x - running mean) / np.sqrt(running var + eps)
      out = np.expand dims(gamma, axis=0) * x normalized + np.expand dims(beta, axis=0)
      cache = None
      # ----- #
      # END YOUR CODE HERE
      # ----- #
   else:
      raise ValueError ('Invalid forward batchnorm mode "%s"' % mode)
   # Store the updated running means back into bn param
   bn param['running mean'] = running mean
   bn_param['running_var'] = running_var
   return out, cache
def batchnorm backward(dout, cache):
   Backward pass for batch normalization.
   For this implementation, you should write out a computation graph for
   batch normalization on paper and propagate gradients backward through
   intermediate nodes.
   Inputs:
   - dout: Upstream derivatives, of shape (N, D)
   - cache: Variable of intermediates from batchnorm forward.
   Returns a tuple of:
   - dx: Gradient with respect to inputs x, of shape (N, D)
   - dgamma: Gradient with respect to scale parameter gamma, of shape (D,)
   - dbeta: Gradient with respect to shift parameter beta, of shape (D,)
   dx, dgamma, dbeta = None, None, None
   # ----- #
   # YOUR CODE HERE:
   # Implement the batchnorm backward pass, calculating dx, dgamma, and dbeta.
   # ----- #
   x, x_normalized, gamma, beta, sample_mean, sample_var, eps = cache
   N, D = dout.shape
   dbeta = np.sum(dout, axis=0)
   dgamma = np.sum(dout * x normalized, axis=0)
   dx normalized = dout * gamma
   dvar = np.sum(dx normalized * (x - sample mean) * -0.5 * np.power(sample var + eps, -1.5),
axis=0)
   dmean = np.sum(dx_normalized * -1 / np.sqrt(sample_var + eps), axis=0) + dvar * np.mean(-2 * open to the context of the cont
```

```
(x - sample_mean), axis=0)
 dx = dx_normalized / np.sqrt(sample_var + eps) + dvar * 2 * (x - sample_mean) / N + dmean /
 # ============== #
 # END YOUR CODE HERE
 return dx, dgamma, dbeta
def dropout_forward(x, dropout_param):
 Performs the forward pass for (inverted) dropout.
 Inputs:
 - x: Input data, of any shape
 - dropout param: A dictionary with the following keys:
  - p: Dropout parameter. We drop each neuron output with probability p.
   - mode: 'test' or 'train'. If the mode is train, then perform dropout;
    if the mode is test, then just return the input.
   - seed: Seed for the random number generator. Passing seed makes this
    function deterministic, which is needed for gradient checking but not in
    real networks.
 Outputs:
 - out: Array of the same shape as x.
 - cache: A tuple (dropout param, mask). In training mode, mask is the dropout
  mask that was used to multiply the input; in test mode, mask is None.
 p, mode = dropout param['p'], dropout param['mode']
 if 'seed' in dropout param:
  np.random.seed(dropout param['seed'])
 mask = None
 out = None
 if mode == 'train':
   # YOUR CODE HERE:
    Implement the inverted dropout forward pass during training time.
     Store the masked and scaled activations in out, and store the
    dropout mask as the variable mask.
  # ----- #
  mask = (np.random.rand(*x.shape) < (1 - p)) / (1 - p)
  out = x * mask
   # END YOUR CODE HERE
   elif mode == 'test':
   # ----- #
   # YOUR CODE HERE:
    Implement the inverted dropout forward pass during test time.
   out = x
   # ----- #
   # END YOUR CODE HERE
   # ----- #
 cache = (dropout param, mask)
 out = out.astype(x.dtype, copy=False)
```

```
def dropout backward(dout, cache):
 Perform the backward pass for (inverted) dropout.
 Inputs:
 - dout: Upstream derivatives, of any shape
 - cache: (dropout_param, mask) from dropout_forward.
 dropout param, mask = cache
 mode = dropout_param['mode']
 dx = None
 if mode == 'train':
   # ----- #
   # YOUR CODE HERE:
    Implement the inverted dropout backward pass during training time.
  # ----- #
  dx = dout * mask
   # END YOUR CODE HERE
   # ----- #
 elif mode == 'test':
   # YOUR CODE HERE:
    Implement the inverted dropout backward pass during test time.
  # ------ #
  dx = dout
   # END YOUR CODE HERE
   return dx
def svm loss(x, y):
 Computes the loss and gradient using for multiclass SVM classification.
 Inputs:
 - x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
  for the ith input.
 - y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
  0 <= y[i] < C
 Returns a tuple of:
 - loss: Scalar giving the loss
 - dx: Gradient of the loss with respect to x
 N = x.shape[0]
 correct class scores = x[np.arange(N), y]
 margins = np.maximum(0, x - correct class scores[:, <math>np.newaxis] + 1.0)
 margins[np.arange(N), y] = 0
 loss = np.sum(margins) / N
 num_pos = np.sum(margins > 0, axis=1)
 dx = np.zeros like(x)
 dx[margins > 0] = 1
 dx[np.arange(N), y] -= num pos
 dx /= N
 return loss, dx
def softmax loss(x, y):
```

return out, cache

```
Computes the loss and gradient for softmax classification.
Inputs:
- x: Input data, of shape (N, C) where x[i, j] is the score for the jth class
 for the ith input.
- y: Vector of labels, of shape (N,) where y[i] is the label for x[i] and
 0 <= y[i] < C
Returns a tuple of:
- loss: Scalar giving the loss
- dx: Gradient of the loss with respect to x
probs = np.exp(x - np.max(x, axis=1, keepdims=True))
probs /= np.sum(probs, axis=1, keepdims=True)
N = x.shape[0]
loss = -np.sum(np.log(probs[np.arange(N), y])) / N
dx = probs.copy()
dx[np.arange(N), y] -= 1
dx /= N
```

return loss, dx

```
import numpy as np
```

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This code was originally written for CS 231n at Stanford University (cs231n.stanford.edu). It has been modified in various areas for use in the ECE 239AS class at UCLA. This includes the descriptions of what code to implement as well as some slight potential changes in variable names to be consistent with class nomenclature. We thank Justin Johnson & Serena Yeung for permission to use this code. To see the original version, please visit cs231n.stanford.edu.

.....

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This file implements various first-order update rules that are commonly used for training neural networks. Each update rule accepts current weights and the gradient of the loss with respect to those weights and produces the next set of weights. Each update rule has the same interface:

def update(w, dw, config=None):

#### Inputs:

- w: A numpy array giving the current weights.
- dw: A numpy array of the same shape as w giving the gradient of the loss with respect to w.
- config: A dictionary containing hyperparameter values such as learning rate, momentum, etc. If the update rule requires caching values over many iterations, then config will also hold these cached values.

#### Returns

- next w: The next point after the update.
- config: The config dictionary to be passed to the next iteration of the update rule.

NOTE: For most update rules, the default learning rate will probably not perform well; however the default values of the other hyperparameters should work well for a variety of different problems.

For efficiency, update rules may perform in-place updates, mutating w and setting next\_w equal to w.

```
def sgd(w, dw, config=None):
```

Performs vanilla stochastic gradient descent.

```
config format:
    - learning_rate: Scalar learning rate.
"""
if config is None: config = {}
config.setdefault('learning_rate', 1e-2)
w -= config['learning_rate'] * dw
return w, config
```

#### def sgd\_momentum(w, dw, config=None):

....

Performs stochastic gradient descent with momentum.

#### config format:

- learning rate: Scalar learning rate.
- momentum: Scalar between 0 and 1 giving the momentum value. Setting momentum = 0 reduces to sgd.
- velocity: A numpy array of the same shape as w and dw used to store a moving average of the gradients.

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```
if config is None: config = {}
 config.setdefault('learning rate', 1e-2)
 config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
 v = config.get('velocity', np.zeros_like(w)) # gets velocity, else sets it to zero.
 # ============== #
 # YOUR CODE HERE:
 # Implement the momentum update formula. Return the updated weights
   as next w, and the updated velocity as v.
 # ============ #
 v = config['momentum'] * v - config['learning_rate'] * dw
 next w = w + v
 # ------ #
 # END YOUR CODE HERE
 config['velocity'] = v
 return next w, config
def sgd nesterov momentum(w, dw, config=None):
 Performs stochastic gradient descent with Nesterov momentum.
 config format:
 - learning rate: Scalar learning rate.
 - momentum: Scalar between 0 and 1 giving the momentum value.
  Setting momentum = 0 reduces to sgd.
 - velocity: A numpy array of the same shape as w and dw used to store a moving
   average of the gradients.
 if config is None: config = {}
 config.setdefault('learning rate', 1e-2)
 config.setdefault('momentum', 0.9) # set momentum to 0.9 if it wasn't there
 v = config.get('velocity', np.zeros_like(w)) # gets velocity, else sets it to zero.
 # ------ #
 # YOUR CODE HERE:
   Implement the momentum update formula. Return the updated weights
   as next w, and the updated velocity as v.
 # ------ #
 v old = v
 v = config['momentum'] * v - config['learning rate'] * dw
 next w = w + v + config['momentum']*(v - v old)
 # ----- #
 # END YOUR CODE HERE
 config['velocity'] = v
 return next w, config
def rmsprop(w, dw, config=None):
 Uses the RMSProp update rule, which uses a moving average of squared gradient
 values to set adaptive per-parameter learning rates.
 config format:
 - learning rate: Scalar learning rate.
 - decay rate: Scalar between 0 and 1 giving the decay rate for the squared
  gradient cache.
 - epsilon: Small scalar used for smoothing to avoid dividing by zero.
 - beta: Moving average of second moments of gradients.
```

```
if config is None: config = {}
 config.setdefault('learning_rate', 1e-2)
 config.setdefault('decay rate', 0.99)
 config.setdefault('epsilon', 1e-8)
 config.setdefault('a', np.zeros like(w))
 next w = None
 # ----- #
 # YOUR CODE HERE:
    Implement RMSProp. Store the next value of w as next_w. You need
   to also store in config['a'] the moving average of the second
 # moment gradients, so they can be used for future gradients. Concretely,
 # config['a'] corresponds to "a" in the lecture notes.
 # ----- #
 config['a'] = config['decay rate'] * config['a'] + (1-config['decay rate']) * dw * dw
 next w = w - config['learning rate'] * dw / (np.sqrt(config['a']) + config['epsilon'])
 # ------ #
 # END YOUR CODE HERE
 # ----- #
 return next w, config
def adam(w, dw, config=None):
 Uses the Adam update rule, which incorporates moving averages of both the
 gradient and its square and a bias correction term.
 config format:
 - learning rate: Scalar learning rate.
 - betal: Decay rate for moving average of first moment of gradient.
 - beta2: Decay rate for moving average of second moment of gradient.
 - epsilon: Small scalar used for smoothing to avoid dividing by zero.
 - m: Moving average of gradient.
 - v: Moving average of squared gradient.
 - t: Iteration number.
 if config is None: config = {}
 config.setdefault('learning rate', 1e-3)
 config.setdefault('beta1', 0.9)
 config.setdefault('beta2', 0.999)
 config.setdefault('epsilon', 1e-8)
 config.setdefault('v', np.zeros_like(w))
 config.setdefault('a', np.zeros like(w))
 config.setdefault('t', 0)
 next w = None
 # ------ #
 # YOUR CODE HERE:
 # Implement Adam. Store the next value of w as next w. You need
 # to also store in config['a'] the moving average of the second
 # moment gradients, and in config['v'] the moving average of the
 # first moments. Finally, store in config['t'] the increasing time.
 # ----- #
 config['t'] += 1
 config['v'] = config['beta1'] * config['v'] + (1 - config['beta1']) * dw
 config['a'] = config['beta2'] * config['a'] + (1 - config['beta2']) * (dw**2)
 v corrected = config['v'] / (1 - config['beta1'] ** config['t'])
 a_corrected = config['a'] / (1 - config['beta2'] ** config['t'])
 next_w = w - config['learning_rate'] * v_corrected / (np.sqrt(a_corrected) +
config['epsilon'])
 # ------ #
```