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! Skeleton 2-1/2D Electromagnetic GPU-MPI PIC code
! written by Viktor K. Decyk, UCLA
      program gpupbpic2
     use gpulib2_h
     use gpupbpush2 h
     use gpupfft2 h
     use pbpush2 h
                   ! use with pplib2.f90
     use pplib2
!
     use pplib2 h
                     ! use with pplib2.f
     use gpplib2
     implicit none
     integer, parameter :: indx = 9, indy =
     integer, parameter :: npx = 3072, npy =
                                                 3072
     integer, parameter :: ndim = 3
     real, parameter :: tend = 10.0, dt = 0.04, qme = -1.0
     real, parameter :: vtx = 1.0, vty = 1.0, vx0 = 0.0, vy0 = 0.0
     real, parameter :: vtz = 1.0, vz0 = 0.0
     real :: ax = .912871, ay = .912871, ci = 0.1
! idimp = dimension of phase space = 5
! relativity = (no, yes) = (0,1) = relativity is used
      integer :: idimp = 5, ipbc = 1, relativity = 1
! idps = number of partition boundaries
      integer :: idps = 2
      real :: wke = 0.0, we = 0.0, wf = 0.0, wm = 0.0, wt = 0.0
! sorting tiles
      integer :: mx = 16, my = 16
! fraction of extra particles needed for particle management
     real :: xtras = 0.2
! declare scalars for standard code
      integer :: nx, ny, nxh, nyh, nxh1, nxe, nye, nxeh
      integer :: nxyh, nxhy, nyl, mxl, ntime, nloop, isign, ierr
     real :: qbme, affp, dth
     real, dimension(1) :: ssum
     double precision :: np
! declare scalars for MPI code
      integer :: nvp, idproc, kstrt, npmax, kxp, kyp, nypmx, nypmn
      integer :: nyp, noff, npp, nps
      integer :: myp1, mxyp1, kxpp, kypp
!
! declare scalars for GPU code
      integer :: nblock = 128
! nscache = (0,1,2) = (no,small,big) cache size
      integer :: nscache = 1
      integer :: mmcc, nppmx, nppmx0, nbmaxp, ntmaxp, npbmx
      integer :: nxhd, kxpd, idev, ndev
      integer, dimension(1) :: irc
! declare arrays for standard code
      real, dimension(:,:), pointer :: part
      complex, dimension(:,:), pointer :: ffct
      integer, dimension(:), pointer :: mixup
     complex, dimension(:), pointer :: sct
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real, dimension(7) :: wtot, work
! declare arrays for MPI code
     real, dimension(:,:), pointer :: sbufl, sbufr, rbufl, rbufr
     real, dimension(:), pointer :: edges
     real, dimension(:), pointer :: scs, scr
     integer, dimension(:), pointer :: locl
! declare arrays for GPU code
     integer, dimension(2) :: g_qe = 0.0
     integer, dimension(2) :: g cue = 0.0, g fxyze = 0.0, g bxyze = 0.0
     integer, dimension(2) :: g ffct = 0.0
     integer, dimension(2) :: g_mixup = 0.0, g_sct = 0.0
     integer, dimension(2) :: q q = 0.0, q cu = 0.0
     integer, dimension(2) :: g_qt = 0.0, g_cut = 0.0
     integer, dimension(2) :: g_fxyz = 0.0, g_hxyz = 0.0
     integer, dimension(2) :: q fxyzt = 0.0, q hxyzt = 0.0
     integer, dimension(2) :: g_exyzt = 0.0, g_bxyzt = 0.0
     integer, dimension(2) :: q wke = 0.0, q we = 0.0
     integer, dimension(2) :: g_wf = 0.0, g_wm = 0.0
     integer, dimension(2) :: g ppart = 0.0, g ppbuff = 0.0
     integer, dimension(2) :: g kpic = 0.0
     integer, dimension(2) :: g_sbufl = 0.0, g_sbufr = 0.0
     integer, dimension(2) :: g_ncl = 0.0, g_ihole = 0.0
     integer, dimension(2) :: g_ncll = 0.0, g_nclr = 0.0
     integer, dimension(2) :: g_bsm = 0.0, g_brm = 0.0
     integer, dimension(2) :: g_scs = 0.0
     integer, dimension(2) :: g sum = 0.0
     integer, dimension(2) :: g_irc = 0.0
     complex, dimension(:,:), pointer :: qt
     complex, dimension(:,:,:), pointer :: fxyzt
     real, dimension(:,:,:), pointer :: ppart
     integer, dimension(:), pointer :: kpic
     integer, dimension(:,:), pointer :: ncll, nclr, mcll, mclr
     complex, dimension(:,:), pointer :: bsm, brm
! declare and initialize timing data
     real :: time
     integer, dimension(4) :: itime
     real :: tdpost = 0.0, tguard = 0.0, tsort = 0.0
     real :: tfield = 0.0, tdjpost = 0.0, tpush = 0.0
     real :: tmov = 0.0
     real, dimension(2) :: tmsort = 0.0
     real, dimension(2) :: tfft = 0.0
     double precision :: dtime
! initialize scalars for standard code
     np = dble(npx)*dble(npy)
     nx = 2**indx; ny = 2**indy; nxh = nx/2; nyh = ny/2
     nxh1 = nxh + 1
     nxe = nx + 2; nye = ny + 2; nxeh = nxe/2
     nxyh = max(nx,ny)/2; nxhy = max(nxh,ny); ny1 = ny + 1
     mx1 = (nx - 1)/mx + 1
     nloop = tend/dt + .0001; ntime = 0
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qbme = qme
      affp = dble(nx)*dble(ny)/np
      dth = 0.0
! set size for FFT arrays
      nxhd = nxh1
! nvp = number of distributed memory nodes
! initialize for distributed memory parallel processing
      call PPINIT2(idproc,nvp)
      kstrt = idproc + 1
! check if too many processors
      if (nvp > ny) then
         if (kstrt==1) then
        write (*,*) 'Too many processors requested: ny, nvp=', ny, nvp
         endif
        go to 3000
      endif
! initialize data for MPI code
      allocate(edges(idps))
! calculate partition variables: edges, nyp, noff, nypmx
! edges(1:2) = lower:upper boundary of particle partition
! nyp = number of primary (complete) gridpoints in particle partition
! noff = lowermost global gridpoint in particle partition
! nypmx = maximum size of particle partition, including guard cells
! nypmn = minimum value of nyp
      call PDICOMP2L(edges,nyp,noff,nypmx,nypmn,ny,kstrt,nvp,idps)
      if (nypmn < 1) then
         if (kstrt==1) then
            write (*,*) 'combination not supported nvp, ny =',nvp,ny
         endif
        go to 3000
      end i f
! initialize additional scalars for MPI code
! kxp = number of complex grids in each field partition in x direction
      kxp = (nxh - 1)/nvp + 1
! set size for FFT arrays
      kxpd = (nxh1 - 1)/nvp + 1
! kyp = number of complex grids in each field partition in y direction
      kyp = (ny - 1)/nvp + 1
! npmax = maximum number of electrons in each partition
      npmax = (np/nvp)*1.25
! myp1 = number of tiles in y direction
      myp1 = (nyp - 1)/my + 1; mxyp1 = mx1*myp1
! kxpp/kypp = actual size of GPU field partition
      kxpp = min(kxpd,max(0,nxhd-kxpd*idproc))
      kypp = min(kyp,max(0,ny-kyp*idproc))
! allocate and initialize data for standard code
      allocate(part(idimp, npmax))
      allocate(ffct(nyh,kxpd))
      allocate(mixup(nxhy),sct(nxyh))
      allocate(kpic(mxyp1))
      allocate(qt(ny,kxpd),fxyzt(ny,ndim,kxpd))
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! allocate and initialize data for MPI code
      allocate(locl(nvp))
!
! set up GPU
      irc = 0
! get unique GPU device ids
      call PPFNDGRP(loc1,kstrt,nvp,idev,ndev)
      if (idev < 0) then
         write (*,*) kstrt, 'GPU device id error!'
         call PPABORT()
         stop
      endif
      call gpu_setgbsize(nblock)
      call init_cu(idev,irc(1))
      if (irc(1) /= 0) then
         write (*,*) kstrt, 'CUDA initialization error!'
         call PPABORT()
         stop
      endif
! obtain compute capability
      mmcc = getmmcc()
      if (mmcc < 20) then
         write (*,*) kstrt, 'compute capability 2.x or higher required'
         call PPABORT()
         stop
      endif
! set cache size
      call gpu_set_cache_size(nscache)
! create asynchronous streams
      call gpu_initstream(1)
      call gpu initstream(2)
      call gpu initstream(3)
! allocate and initialize data for GPU code
      call gpu_fallocate(g_qe,nxe*nypmx,irc(1))
      call gpu_fallocate(g_cue,ndim*nxe*nypmx,irc(1))
      call gpu_fallocate(g_fxyze,ndim*nxe*nypmx,irc(1))
      call gpu_fallocate(g_bxyze,ndim*nxe*nypmx,irc(1))
      call qpu callocate(q ffct,nyh*kxpd,irc(1))
      call gpu_iallocate(g_mixup,nxhy,irc(1))
      call gpu_callocate(g_sct,nxyh,irc(1))
      call gpu_callocate(g_q,nxhd*kyp,irc(1))
      call gpu_callocate(g_cu,nxhd*ndim*kyp,irc(1))
      call gpu_callocate(g_qt,ny*kxpd,irc(1))
      call gpu_callocate(g_cut,ny*ndim*kxpd,irc(1))
      call gpu_callocate(g_fxyz,nxhd*ndim*kyp,irc(1))
      call gpu_callocate(g_hxyz,nxhd*ndim*kyp,irc(1))
      call gpu_callocate(g_fxyzt,ny*ndim*kxpd,irc(1))
      call gpu_callocate(g_hxyzt,ny*ndim*kxpd,irc(1))
      call qpu callocate(q exyzt,ny*ndim*kxpd,irc(1))
      call gpu_callocate(g_bxyzt,ny*ndim*kxpd,irc(1))
      call gpu_fallocate(g_wke,mxyp1,irc(1))
      call gpu_fallocate(g_we,kxpd,irc(1))
      call gpu_fallocate(g_wf,kxpd,irc(1))
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call gpu fallocate(g wm,kxpd,irc(1))
      call gpu_fallocate(g_sum,1,irc(1))
      if (irc(1) /= 0) then
        write (*,*) kstrt, 'GPU allocate error!'
         call PPABORT()
         stop
      endif
1
! prepare fft tables
      call WPFFT2RINIT(mixup,sct,indx,indy,nxhy,nxyh)
! prepare NVIDIA ffts
      call gpupfft2rrcuinit(nx,kypp,ndim)
      call gpupfft2cuinit(kxpp,ny,ndim)
! calculate form factors
      isign = 0
      call PPOIS23T(qt,fxyzt,isign,ffct,ax,ay,affp,we,nx,ny,kstrt,ny,
     &kxpd, nyh)
! copy in solver arrays to GPU
      call gpu_icopyin(mixup,g_mixup,nxhy)
      call gpu_ccopyin(sct,g_sct,nxyh)
      call gpu_ccopyin(ffct,g_ffct,nyh*kxpd)
! initialize electrons
      nps = 1
      npp = 0
      call PDISTR2H(part,edges,npp,nps,vtx,vty,vtz,vx0,vy0,vz0,npx,npy, &
     &nx,ny,idimp,npmax,idps,ipbc,ierr)
! check for particle initialization error
      if (ierr /= 0) then
         if (kstrt==1) then
            write (*,*) 'particle initialization error: ierr=', ierr
        endif
        go to 3000
      endif
! initialize transverse electromagnetic fields
      call gpu_zcmem(g_exyzt,ny*ndim*kxpd)
      call gpu_zcmem(g_bxyzt,ny*ndim*kxpd)
! find number of particles in each of mx, my tiles: updates kpic, nppmx
      call PPDBLKP2L(part,kpic,npp,noff,nppmx,idimp,npmax,mx,my,mx1,
     &mxyp1,irc(1))
      if (irc(1) /= 0) then
        write (*,*) kstrt, 'PPDBLKP2L error, irc=', irc(1)
         call PPABORT()
         stop
      endif
! allocate vector particle data
      nppmx0 = (1.0 + xtras)*nppmx
      ntmaxp = 0.5*xtras*nppmx
      npbmx = 0.5*xtras*nppmx
      nbmaxp = 0.25*mx1*npbmx
! align data to warp size
      nppmx0 = 32*((nppmx0 - 1)/32 + 1)
      ntmaxp = 32*(ntmaxp/32 + 1)
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npbmx = 32*((npbmx - 1)/32 + 1)
      nbmaxp = 32*((nbmaxp - 1)/32 + 1)
     call gpu_fallocate(g_ppart,nppmx0*idimp*mxyp1,irc(1))
     call gpu_fallocate(g_ppbuff,npbmx*idimp*mxyp1,irc(1))
     call gpu_iallocate(g_kpic,mxyp1+1,irc(1))
     call gpu fallocate(g sbufl,nbmaxp*idimp,irc(1))
     call gpu_fallocate(g_sbufr,nbmaxp*idimp,irc(1))
      call gpu_iallocate(g_ncl,8*mxyp1,irc(1))
     call gpu_iallocate(g_ihole,2*(ntmaxp+1)*mxyp1,irc(1))
     call gpu_iallocate(g_ncl1,3*mx1,irc(1))
     call gpu_iallocate(g_nclr,3*mx1,irc(1))
     call gpu_callocate(g_bsm,kxpd*ndim*kyp*nvp,irc(1))
     call gpu_callocate(g_brm,kxpd*ndim*kyp*nvp,irc(1))
     call gpu_fallocate(g_scs,nxe*ndim,irc(1))
     call gpu_iallocate(g_irc,1,irc(1))
      if (irc(1) /= 0) then
        write (*,*) kstrt, 'GPU allocate error!'
         call PPABORT()
         stop
      endif
      allocate(ppart(nppmx0,idimp,mxyp1))
      allocate(ncl1(3,mx1),nclr(3,mx1),mcl1(3,mx1),mclr(3,mx1))
! allocate data for GPU-MPI buffers
!
     allocate(scs(nxe*ndim),scr(nxe*ndim))
!
      allocate(sbufl(idimp,nbmaxp),sbufr(idimp,nbmaxp))
!
      allocate(rbufl(idimp,nbmaxp),rbufr(idimp,nbmaxp))
!
      allocate(bsm(kxpd*ndim*kyp,nvp),brm(kxpd*ndim*kyp,nvp))
! allocate host page-locked memory for GPU-MPI buffers
      call hpl flallocate(scs,nxe*ndim,irc(1))
      call hpl_f1allocate(scr,nxe*ndim,irc(1))
     call hpl_f2allocate(sbufl,idimp,nbmaxp,irc(1))
     call hpl_f2allocate(sbufr,idimp,nbmaxp,irc(1))
     call hpl_f2allocate(rbufl,idimp,nbmaxp,irc(1))
     call hpl_f2allocate(rbufr,idimp,nbmaxp,irc(1))
     call hpl_c2allocate(bsm,kxpd*ndim*kyp,nvp,irc(1))
     call hpl_c2allocate(brm,kxpd*ndim*kyp,nvp,irc(1))
      if (irc(1) /= 0) then
        write (*,*) kstrt, 'hpl allocate error, irc=', irc(1)
        call PPABORT()
         stop
     endif
! copy ordered particle data for GPU code: updates ppart, kpic
     call PPPMOVIN2LT(part,ppart,kpic,npp,noff,nppmx0,idimp,npmax,mx,my&
    &, mx1, mxyp1, irc(1))
      if (irc(1) /= 0) then
        write (*,*) kstrt, 'PPPMOVIN2LT overflow error, irc=', irc(1)
         call PPABORT()
         stop
     endif
! sanity check
     call PPPCHECK2LT(ppart,kpic,noff,nyp,idimp,nppmx0,nx,mx,my,mx1,
    &myp1,irc(1))
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```
if (irc(1) /= 0) then
        write (*,*) kstrt, 'PPPCHECK2LT error: irc=', irc(1)
         call PPABORT()
         stop
      endif
! copy to GPU
      call gpu_icopyin(irc,g_irc,1)
      call gpu_fcopyin(ppart,g_ppart,nppmx0*idimp*mxyp1)
      call gpu_icopyin(kpic,g_kpic,mxyp1)
      call gpu_zfmem(g_we,kxpd)
      call gpu zfmem(g wf,kxpd)
      call gpu zfmem(g wm,kxpd)
!
      if (dt > 0.45*ci) then
         if (kstrt==1) then
            write (*,*) 'Warning: Courant condition may be exceeded!'
         endif
      endif
!
! * * * start main iteration loop * * *
 500 if (nloop <= ntime) go to 2000
      if (kstrt==1) write (*,*) 'ntime = ', ntime
!
! deposit current with GPU code: updates g_ppart, g_cue
      call dtimer(dtime,itime,-1)
      call gpu_zfmem(g_cue,ndim*nxe*nypmx)
      if (relativity==1) then
         call cgpu2pprjppost21(g_ppart,g_cue,g_kpic,noff,qme,dth,ci,
     &nppmx0,idimp,nx,ny,mx,my,nxe,nypmx,mx1,mxyp1,ipbc)
         call cgpu2ppjppost21(g_ppart,g_cue,g_kpic,noff,qme,dth,nppmx0, &
     &idimp,nx,ny,mx,my,nxe,nypmx,mx1,mxyp1,ipbc)
      endif
      call dtimer(dtime, itime, 1)
      time = real(dtime)
      tdjpost = tdjpost + time
! reorder particles by tile with GPU code:
! updates g_ppart, g_ppbuff, g_kpic, g_ncl, g_ihole, and g_irc,
! as well as various buffers
      call GPPORDER2L(g_ppart,g_ppbuff,g_sbuf1,g_sbufr,g_kpic,g_ncl,
     &g_ihole,g_ncll,g_nclr,sbufl,sbufr,rbufl,rbufr,ncll,nclr,mcll,mclr,&
     &tmsort,noff,nyp,kstrt,nvp,idimp,nppmx0,nx,ny,mx,my,mx1,myp1,npbmx,&
     &ntmaxp,nbmaxp,q irc)
     tsort = tmsort(1)
      tmov = tmsort(2)
!
! deposit charge with GPU code: updates g_qe
      call dtimer(dtime, itime, -1)
      call gpu_zfmem(g_qe,nxe*nypmx)
      call cgpu2ppppost21(g_ppart,g_qe,g_kpic,noff,qme,idimp,nppmx0,mx,&
     &my,nxe,nypmx,mx1,mxyp1)
      call dtimer(dtime,itime,1)
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time = real(dtime)
      tdpost = tdpost + time
! add and copy guard cells with GPU code: updates g_cu, g_q
      call dtimer(dtime,itime,-1)
      call GPPCACGUARD2L(q cu,q cue,g scs,scs,scr,nx,nyp,kstrt,nvp,ndim,&
     &nxe,nypmx,nxhd,kyp)
      call GPPCAGUARD2L(g_q,g_qe,g_scs,scs,scr,nx,nyp,kstrt,nvp,nxe,
     &nypmx, nxhd, kyp)
      call dtimer(dtime,itime,1)
      time = real(dtime)
      tquard = tquard + time
!
! transform charge to fourier space with GPU code: updates q q, q qt,
! as well as various buffers
      isign = -1
      call WAPPFFT2RCS(q q,q qt,g bsm,g brm,bsm,brm,isiqn,q mixup,q sct,&
     &tfft, indx, indy, kstrt, nvp, kxpd, kyp, nxhd, ny, kyp, nxhy, nxyh)
! NVIDIA fft
!
     call GPUPPFFT2RRCU(g_q,g_qt,g_bsm,g_brm,bsm,brm,isign,tfft,indx, &
     &indy, kstrt, nvp, kxpd, kyp, nxhd, ny, kyp)
! transform current to fourier space with GPU code: updates q cu, q cut,
! as well as various buffers
      isign = -1
      call WAPPFFT2RCSN(g_cu,g_cut,g_bsm,g_brm,bsm,brm,isign,g_mixup,
     &g_sct,tfft,indx,indy,kstrt,nvp,ndim,kxpd,kyp,nxhd,ny,kyp,nxhy,nxyh&
     &)
! NVIDIA fft
      call GPUPPFFT2RRCUN(g_cu,g_cut,g_bsm,g_brm,bsm,brm,isign,tfft,indx&
!
     &, indy, kstrt, nvp, ndim, kxpd, kyp, nxhd, ny, kyp)
! take transverse part of current with GPU code: updates q cut
      call dtimer(dtime,itime,-1)
      call cgpuppcuperp2t(g_cut,nx,ny,kstrt,ny,kxpd)
      call dtimer(dtime,itime,1)
      time = real(dtime)
      tfield = tfield + time
1
! calculate electromagnetic fields in fourier space with GPU code:
! updates g_exyzt, g_bxyzt, g_wf, g_wm
      call dtimer(dtime,itime,-1)
      if (ntime==0) then
         call cgpuippbpoisp23t(g_cut,g_bxyzt,g_ffct,ci,g_wm,nx,ny,kstrt,&
     &ny, kxpd, nyh)
         wf = 0.0
         dth = 0.5*dt
      else
         call cgpuppmaxwe12t(g_exyzt,g_bxyzt,g_cut,g_ffct,affp,ci,dt,
     &q wf,q wm,nx,ny,kstrt,ny,kxpd,nyh)
      endif
      call dtimer(dtime, itime, 1)
      time = real(dtime)
      tfield = tfield + time
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! calculate force/charge in fourier space with GPU code:
! updates g_fxyzt, g_we
     call dtimer(dtime,itime,-1)
     call cgpuppois23t(g_qt,g_fxyzt,g_ffct,g_we,nx,ny,kstrt,ny,kxpd,nyh&
     call dtimer(dtime,itime,1)
     time = real(dtime)
     tfield = tfield + time
! add longitudinal and transverse electric fields with with GPU code:
! updates g_fxyzt
     call dtimer(dtime,itime,-1)
     isign = 1
     call cgpuppemfield2t(g_fxyzt,g_exyzt,g_ffct,isign,nx,ny,kstrt,ny, &
    &kxpd, nyh)
! copy magnetic field with GPU code: updates q hxyzt
     isign = -1
     call cgpuppemfield2t(g_hxyzt,g_bxyzt,g_ffct,isign,nx,ny,kstrt,ny, &
    &kxpd, nyh)
     call dtimer(dtime,itime,1)
     time = real(dtime)
     tfield = tfield + time
! transform force to real space with GPU code: updates g_fxyz, g_fxyzt
! as well as various buffers
     isign = 1
     call WAPPFFT2RCSN(g_fxyz,g_fxyzt,g_bsm,g_brm,bsm,brm,isign,g_mixup&
    &,g_sct,tfft,indx,indy,kstrt,nvp,ndim,kxpd,kyp,nxhd,ny,kyp,nxhy,
    &nxyh)
! NVIDIA fft
     call GPUPPFFT2RRCUN(g_fxyz,g_fxyzt,g_bsm,g_brm,bsm,brm,isign,tfft,&
    &indx,indy,kstrt,nvp,ndim,kxpd,kyp,nxhd,ny,kyp)
!
! transform magnetic field to fourier space with GPU code:
! updates g_hxyz, g_hxyzt, as well as various buffers
     isign = 1
     call WAPPFFT2RCSN(g_hxyz,g_hxyzt,g_bsm,g_brm,bsm,brm,isign,g_mixup&
    &,g_sct,tfft,indx,indy,kstrt,nvp,ndim,kxpd,kyp,nxhd,ny,kyp,nxhy,
    &nxyh)
     call GPUPPFFT2RRCUN(g_hxyz,g_hxyzt,g_bsm,g_brm,bsm,brm,isign,tfft,&
!
!
    &indx,indy,kstrt,nvp,ndim,kxpd,kyp,nxhd,ny,kyp)
! copy guard cells with GPU code: updates g_fxyze, g_bxyze
     call dtimer(dtime,itime,-1)
     call GPPCBGUARD2L(g_fxyz,g_fxyze,g_scs,scs,scr,nx,nyp,kstrt,nvp, &
    &ndim,nxe,nypmx,nxhd,kyp)
     call GPPCBGUARD2L(g_hxyz,g_bxyze,g_scs,scr,nx,nyp,kstrt,nvp,
    &ndim, nxe, nypmx, nxhd, kyp)
     call dtimer(dtime, itime, 1)
     time = real(dtime)
     tguard = tguard + time
! push particles with GPU code: updates g_ppart, g_wke
```

```
call dtimer(dtime, itime, -1)
      if (relativity==1) then
        call cgpuppgrbppush231(g_ppart,g_fxyze,g_bxyze,g_kpic,noff,nyp,&
     &qbme,dt,dth,ci,g_wke,idimp,nppmx0,nx,ny,mx,my,nxe,nypmx,mx1,mxyp1,&
     &ipbc)
     else
         call cgpuppgbppush231(g_ppart,g_fxyze,g_bxyze,g_kpic,noff,nyp, &
     &qbme,dt,dth,g_wke,idimp,nppmx0,nx,ny,mx,my,nxe,nypmx,mx1,mxyp1,
     &ipbc)
     endif
     call dtimer(dtime, itime, 1)
     time = real(dtime)
     tpush = tpush + time
! reorder particles by tile with GPU code:
! updates g_ppart, g_ppbuff, g_kpic, g_ncl, g_ihole, and g_irc,
! as well as various buffers
     call GPPORDER2L(g_ppart,g_ppbuff,g_sbufl,g_sbufr,g_kpic,g_ncl,
     &g_ihole,g_ncll,g_nclr,sbufl,sbufr,rbufl,rbufr,ncll,nclr,mcll,mclr,&
     &tmsort,noff,nyp,kstrt,nvp,idimp,nppmx0,nx,ny,mx,my,mx1,myp1,npbmx,&
     &ntmaxp,nbmaxp,g_irc)
     tsort = tmsort(1)
     tmov = tmsort(2)
! sanity check
     call gpu_icopyout(irc,g_irc,1)
      if (irc(1) /= 0) then
        write (*,*) kstrt, 'GPPORDER2L error: irc=', irc(1)
        call PPABORT()
         stop
     endif
! energy diagnostic
      if (ntime==0) then
        call gpu_zfmem(g_sum,1)
        call cgpusum2(g_we,g_sum,kxpd)
        call gpu_fcopyout(ssum,g_sum,1); we = ssum(1)
        call gpu_zfmem(g_sum,1)
        call cqpusum2(q wf,q sum,kxpd)
        call gpu_fcopyout(ssum,g_sum,1); wf = ssum(1)
        call gpu_zfmem(g_sum,1)
        call cgpusum2(g_wm,g_sum,kxpd)
        call gpu_fcopyout(ssum,g_sum,1); wm = ssum(1)
        call gpu_zfmem(g_sum,1)
        call cgpusum2(g_wke,g_sum,mxyp1)
        call gpu_fcopyout(ssum,g_sum,1); wke = ssum(1)
        wt = we + wf + wm
        wtot(1) = wt
        wtot(2) = wke
        wtot(3) = 0.0
        wtot(4) = wke + wt
        wtot(5) = we
        wtot(6) = wf
        wtot(7) = wm
```

```
call PPSUM(wtot,work,7)
        wke = wtot(2)
        we = wtot(5)
        wf = wtot(6)
        wm = wtot(7)
         if (kstrt==1) then
            wt = we + wf + wm
            write (*,*) 'Initial Total Field, Kinetic and Total Energies&
     &:'
            write (*,'(3e14.7)') wt, wke, wke + wt
            write (*,*) 'Initial Electrostatic, Transverse Electric and &
     &Magnetic Field Energies: '
            write (*,'(3e14.7)') we, wf, wm
         endif
      endif
      ntime = ntime + 1
      go to 500
2000 continue
!
! * * * end main iteration loop * * *
! energy diagnostic
      call gpu_zfmem(g_sum,1)
      call cgpusum2(g_we,g_sum,kxpd)
      call gpu_fcopyout(ssum,g_sum,1); we = ssum(1)
      call gpu_zfmem(g_sum,1)
      call cgpusum2(g_wf,g_sum,kxpd)
      call gpu fcopyout(ssum, g sum, 1); wf = ssum(1)
      call gpu_zfmem(g_sum,1)
      call cgpusum2(g_wm,g_sum,kxpd)
      call gpu_fcopyout(ssum,g_sum,1); wm = ssum(1)
      call gpu_zfmem(g_sum,1)
      call cgpusum2(g_wke,g_sum,mxyp1)
      call gpu_fcopyout(ssum,g_sum,1); wke = ssum(1)
     wt = we + wf + wm
     wtot(1) = wt
     wtot(2) = wke
     wtot(3) = 0.0
     wtot(4) = wke + wt
     wtot(5) = we
     wtot(6) = wf
     wtot(7) = wm
      call PPSUM(wtot,work,7)
     wke = wtot(2)
     we = wtot(5)
     wf = wtot(6)
     wm = wtot(7)
      if (kstrt==1) then
        write (*,*) 'ntime, relativity = ', ntime, relativity
        write (*,*) 'MPI nodes nvp = ', nvp, ', GPUs per host = ', ndev
        wt = we + wf + wm
        write (*,*) 'Final Total Field, Kinetic and Total Energies:'
        write (*,'(3e14.7)') wt, wke, wke + wt
        write (*,*) 'Final Electrostatic, Transverse Electric and Magne&
```

```
&tic Field Energies:'
        write (*,'(3e14.7)') we, wf, wm
        write (*,*)
1
        write (*,*) 'deposit time = ', tdpost
        write (*,*) 'current deposit time = ', tdjpost
        tdpost = tdpost + tdjpost
        write (*,*) 'total deposit time = ', tdpost
        write (*,*) 'guard time = ', tguard
        write (*,*) 'solver time = ', tfield
        write (*,*) 'fft times = ', sum(tfft), tfft
        write (*,*) 'push time = ', tpush
        write (*,*) 'move time = ', tmov
        write (*,*) 'sort time = ', tsort
        tfield = tfield + tguard + sum(tfft)
        write (*,*) 'total solver time = ', tfield
        time = tdpost + tpush + tsort + tmov
        write (*,*) 'total particle time = ', time
        wt = time + tfield
        write (*,*) 'total time = ', wt
        write (*,*)
!
        wt = 1.0e+09/(real(nloop)*real(np))
        write (*,*) 'Push Time (nsec) = ', tpush*wt
        write (*,*) 'Deposit Time (nsec) = ', tdpost*wt
        write (*,*) 'Sort Time (nsec) = ', tsort*wt
        write (*,*) 'Move Time (nsec) = ', tmov*wt
        write (*,*) 'Total Particle Time (nsec) = ', time*wt
     endif
! close down NVIDIA fft
     call gpupfft2cudel()
     call gpupfft2rrcudel()
! deallocate memory on GPU
     call gpu_deallocate(g_irc,irc(1))
     call gpu_deallocate(g_scs,irc(1))
     call gpu_deallocate(g_brm,irc(1))
     call gpu_deallocate(g_bsm,irc(1))
     call gpu deallocate(g nclr,irc(1))
     call gpu_deallocate(g_ncll,irc(1))
     call gpu_deallocate(g_ihole,irc(1))
     call gpu_deallocate(g_ncl,irc(1))
     call gpu_deallocate(g_sbufr,irc(1))
     call gpu_deallocate(g_sbufl,irc(1))
     call gpu_deallocate(g_kpic,irc(1))
     call gpu_deallocate(g_ppbuff,irc(1))
     call gpu_deallocate(g_ppart,irc(1))
     call gpu_deallocate(g_sum,irc(1))
     call gpu_deallocate(g_wm,irc(1))
     call gpu deallocate(g wf,irc(1))
     call gpu_deallocate(g_we,irc(1))
     call gpu_deallocate(g_wke,irc(1))
     call gpu_deallocate(g_bxyzt,irc(1))
     call gpu_deallocate(g_exyzt,irc(1))
```

```
call gpu_deallocate(g_hxyzt,irc(1))
      call gpu_deallocate(g_fxyzt,irc(1))
      call gpu_deallocate(g_hxyz,irc(1))
      call gpu_deallocate(g_fxyz,irc(1))
      call gpu_deallocate(g_cut,irc(1))
      call gpu deallocate(g gt,irc(1))
      call gpu_deallocate(g_cu,irc(1))
      call gpu deallocate(g q,irc(1))
      call gpu_deallocate(g_sct,irc(1))
      call gpu_deallocate(g_mixup,irc(1))
      call gpu deallocate(g ffct,irc(1))
      call gpu_deallocate(g_bxyze,irc(1))
      call gpu_deallocate(g_fxyze,irc(1))
      call gpu_deallocate(g_cue,irc(1))
      call gpu_deallocate(g_qe,irc(1))
! deallocate host page-locked memory
      call hpl deallocate(scs,irc(1)); nullify(scs)
      call hpl_deallocate(scr,irc(1)); nullify(scr)
      call hpl deallocate(sbufl,irc(1)); nullify(sbufl)
      call hpl_deallocate(sbufr,irc(1)); nullify(sbufr)
      call hpl deallocate(rbufl,irc(1)); nullify(rbufl)
      call hpl deallocate(rbufr,irc(1)); nullify(rbufr)
      call hpl deallocate(bsm,irc(1)); nullify(bsm)
      call hpl_deallocate(brm,irc(1)); nullify(brm)
3000 continue
!
! delete asynchronous streams
      call gpu delstream(3)
      call gpu_delstream(2)
      call gpu delstream(1)
! close down GPU
      call end cu()
! close down MPI
      call PPEXIT()
!
      stop
      end program
!
      subroutine getfcptr(cref,carray,nx)
! set reference to C data in 1d real Fortran pointer object
      implicit none
      integer :: nx
      real, dimension(nx), target :: carray
      real, dimension(:), pointer :: cref
      cref => carray
      end subroutine
      subroutine getf2cptr(cref,carray,nx,ny)
! set reference to C data in 2d real Fortran pointer object
      implicit none
      integer :: nx, ny
      real, dimension(nx,ny), target :: carray
      real, dimension(:,:), pointer :: cref
      cref => carray
```

```
end subroutine
!
    subroutine getc2cptr(cref,carray,nx,ny)
! set reference to C data in 2d complex Fortran pointer object
    implicit none
    integer :: nx, ny
    complex, dimension(nx,ny), target :: carray
    complex, dimension(:,:), pointer :: cref
    cref => carray
    end subroutine
```