

Vacuum Technology

PHY451
October 22, 2014

Some References

- [http://uspas.fnal.gov/materials/13Duke/
Duke_VacuumScience.shtml](http://uspas.fnal.gov/materials/13Duke/Duke_VacuumScience.shtml)
- [http://physics.ucsd.edu/~tmurphy/phys121/lectures/
06_vacuum.ppt](http://physics.ucsd.edu/~tmurphy/phys121/lectures/06_vacuum.ppt)
- [http://www.oerlikon.com/ecomaxL/files/
oerlikon_FUNDAMENTALS.PDF&download=1](http://www.oerlikon.com/ecomaxL/files/oerlikon_FUNDAMENTALS.PDF&download=1)

Vacuum – [1]

Vacuum when gas has the density of the particles less than atmospheric pressure

Vacuum systems necessary to remove and maintain removal of gases in some volume

- **Vacuum used e.g.**
 - Oxygen removed from light bulb to protect filament & in food processing to preserve
 - Create force for forming plastic sheets
 - Deposition to create insulators, conductors, etc
 - Electron beam microscope
 - Particle accelerators
 - Cryogenic system insulation

Vacuum - [2]

Pressure Ranges

- Atmosphere ~760 torr
- Rough Vacuum ~ 10^{-3} torr
- High Vacuum ~ 10^{-3} to 10^{-6} torr
- Very High Vacuum ~ 10^{-6} to 10^{-9} torr
- Ultra High Vacuum ~ 10^{-9} to 10^{-12} torr

Example Values

- Deep space ~ $<10^{-17}$ torr
- Mars surface ~5 torr
- Lunar surface ~ 10^{-11} torr
- Geosynchronous satellites ~ 10^{-11} torr
- Space station ~ 10^{-9} torr
- Above earth – [12 km (airline) ~140 torr], [32 km ~8torr], [80.5 km ~ 10^{-3} torr]

Vacuum – [3]

- Gas composition and pressure can have wide variance.
 - Depending on application – acceptable residual gas density can vary from 10^{10} to 10^4 molecules per cm^3
 - Initial gas composition initially air but later largely driven by pumping technique and source of gas
 - » Initial “vacuum” – mainly air N_2 (78.08%), O_2 (20.95%), CO_2 (0.037%)

General Gas Equation

- P = pressure [Pa; N / m²]
- T = thermodynamic temperature [K]
- n = molecular number density [1 / m³]
- k = Boltzmann's constant $k = 1.380 \cdot 10^{-23}$ J/K

$$P = n \cdot k \cdot T$$

Pressure Units

- Pressure = Force/Area
 - E.G., 6 inch diameter plate with vacuum / atmosphere interfaces
→~416 pounds force
- Pressure units
 - Pascal (N/m^2) = Pa, bar = 10^5 Pa, Torr = mmHg,
 - micron = μmHg , psi = lbs/inch²
 - 1 atmosphere (atm) →
 - » $1.01325 \text{ bar} = 1.01325 \times 10^5 \text{ Pa}$
 - » $760 \text{ torr} = 760 \text{ mmHg} = 760 \times 10^3 \text{ micron}$
 - » 14.7 psi (pounds per square inch)
 - 1 torr = 133.32 Pa = 1.3332 mbar
- At standard temperature (273.15 K = 0°C) & pressure (1atm) → 22.414 liters contains 6.02×10^{23} particles (molecular weight in grams) → molecular density (1/cm³) = 6.02×10^{23} particles / 22414 cm³= 2.7×10^{19} molecules/cm³
- At 10^{-3} torr → $2.7 \times 10^{19} / 760 \times 10^3 = 3.6 \times 10^{13}$ molecules/cm³

Maxwell Boltzman – [1]

Gas particles move randomly but with specific velocity given by Maxwell-Boltzmann Distribution = f

- f is probability distribution that is function of particle velocity (v), mass, and temperature T – *velocity does not depend on pressure*

$$f(v, \text{mass}, T) := 4\pi \left(\frac{\text{mass}}{2\pi k T} \right)^{\frac{3}{2}} v^2 e^{-\frac{\text{mass} v^2}{2k T}}$$

- k= Boltzman Constant = $1.380650424 \times 10^{-23}$ (joule/K)
- T = temperature (K)
- Mass = kg = molecular weight in AMU $\times 1.6605402 \times 10^{-27} \text{ kg/AMU}$

- Most probable velocity = v_p

$$\left(2k \frac{T}{\text{mass}} \right)^{0.5}$$

- Mean velocity = v_{ave}

$$\left(\frac{8k}{\text{mass} \pi} \frac{T}{\text{mass}} \right)^{0.5}$$

$$v_{ave} = 1.1284 \times v_p$$

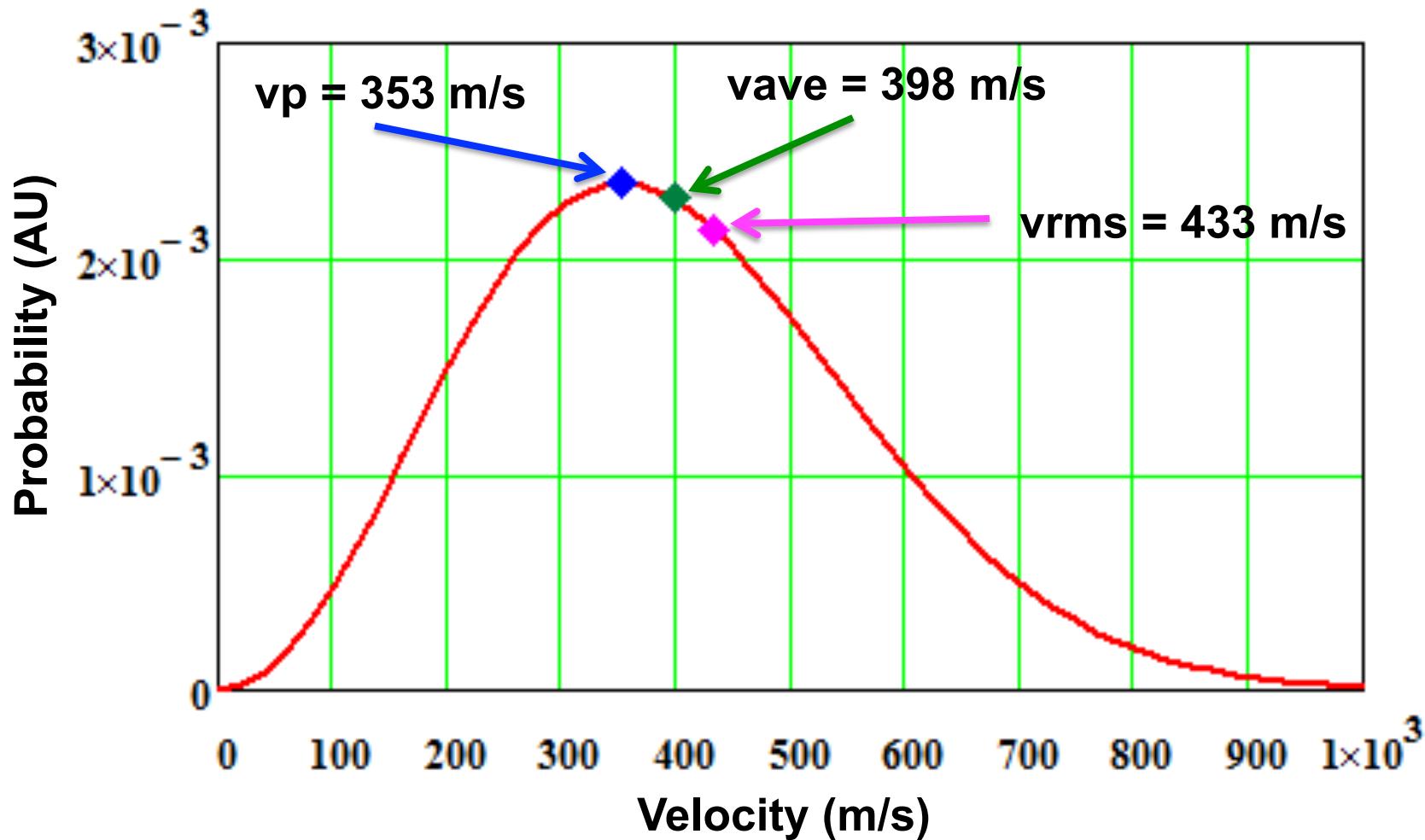
- RMS velocity = v_{rms}

$$\left(3k \frac{T}{\text{mass}} \right)^{0.5}$$

$$v_{rms} = 1.2247 \times v_p$$

Maxwell-Boltzmann – [2]

Probability velocity distribution for ^{40}Ar at 300 K



Maxwell-Boltzmann – [3]

Velocity mass dependent ($T = 300$ K)

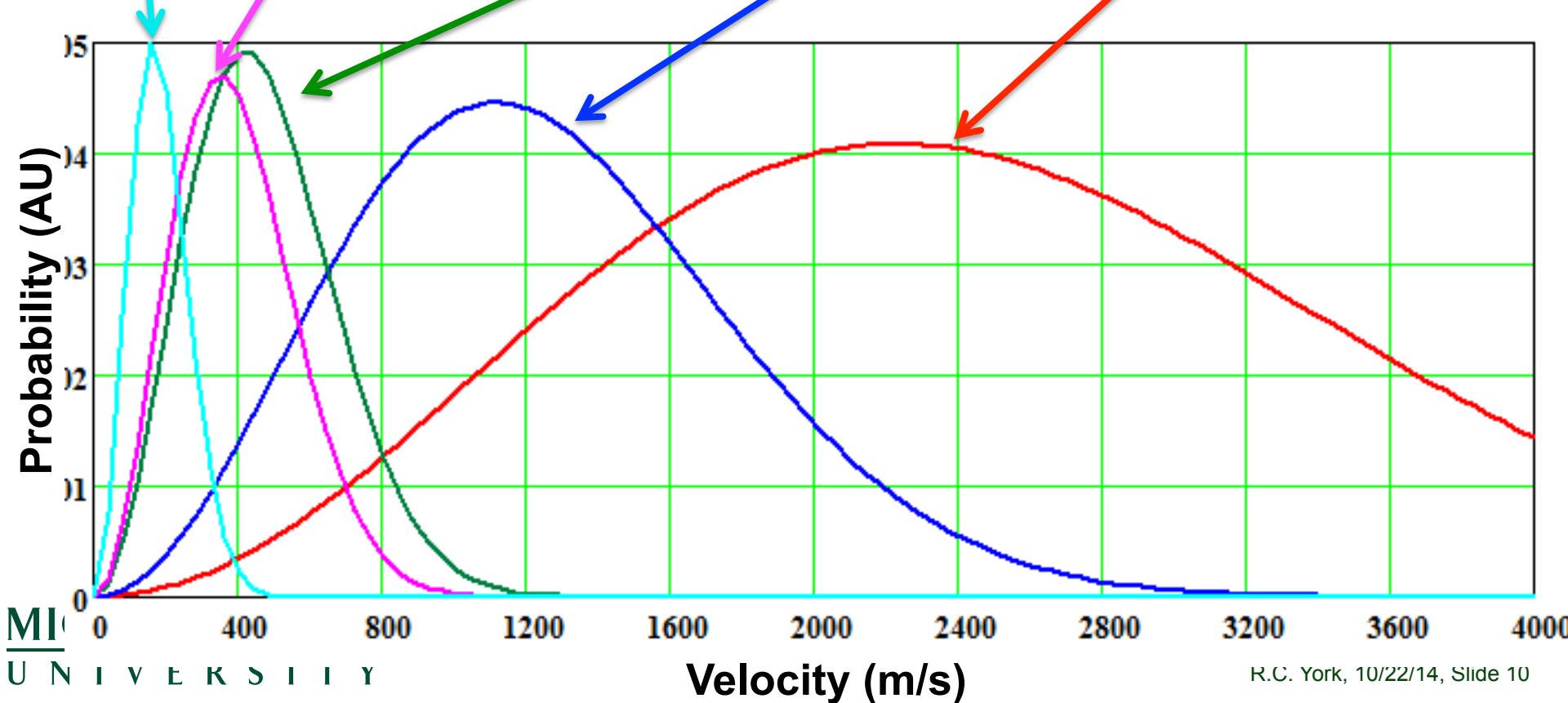
Ar (40 amu)

Xe (181 amu)

N₂ (28 amu)

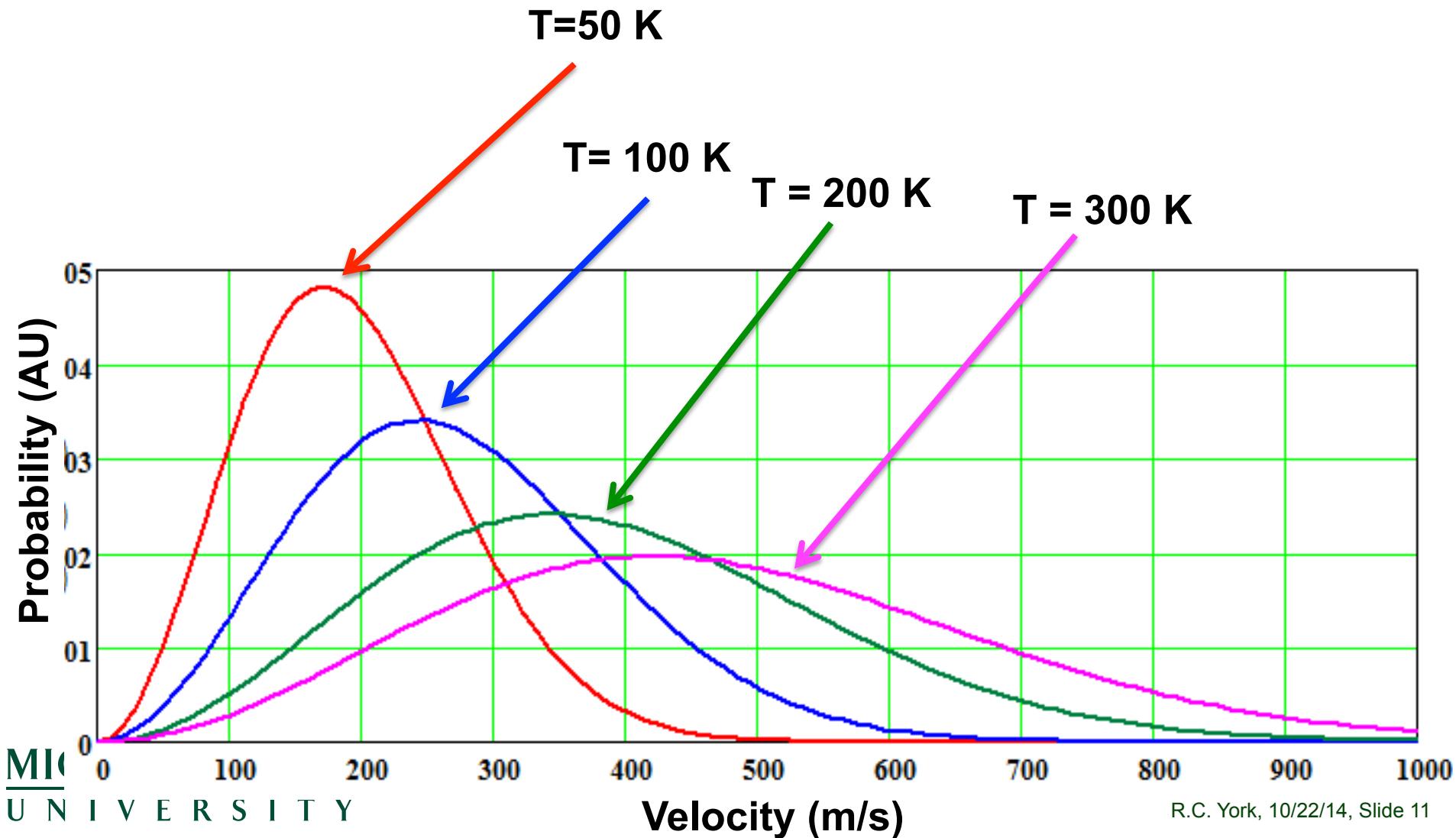
He (4 amu)

H (1 amu)



Maxwell-Boltzmann – [4]

Velocity temperature (T) dependent (N_2 mass = 28 amu)



Maxwell Boltzman – [5]

Energy depends only on T

- Average energy = $E_{ave} = \text{mass} \times v_{rms}^2/2 = 3kT/2$
- $E(T=50K)=6.5 \text{ meV}$, $E(T=100K)=12.9 \text{ meV}$, $E(T=300K)=38.8 \text{ meV}$
- Most probable energy = $E_p = \text{mass} \times v_p^2/2 = kT/2$

Mean Free Path – [1]

Mean free path (λ) is average distance before colliding with another molecule

$$\bullet \lambda = 1 / [(2)^{0.5} \pi d_o^2 n] = k T / [(2)^{0.5} \pi d_o^2 P]$$

– λ = mean free path (m)

– d_o = diameter of molecule (m)

» For Air – average diameter $\sim 3.74 \times 10^{-10}$ m

– n = molecular density (m^{-3})

» n (stand. temp. & pressure – STP) = $n_{\text{stp}} * T_{\text{stp}} * P / (T * P_{\text{stp}})$

– n_{stp} (T_{stp} , P_{stp}) = 2.7×10^{19} molecules/cm³

– T = Temperature (K)

– P = Pressure (Pa)

– k = Boltzmann constant = 1.38×10^{-23} m² kg s⁻² K⁻¹

Mean Free Path – [2]

Mean free path (λ) is average distance before colliding with another molecule - values shown for air T=303.15 K (30 °C)

- λ (cm) = $1.646 \times 10^{-5}T$ (K)/P(torr)
- λ (cm) = $2.1945 \times 10^{-3}T$ (K)/P(Pa)
- Once λ similar to vacuum vessel dimension – only collisions with vacuum walls dominate – not molecules colliding with molecules
 - i.e. <10⁻³ torr

P(torr)	760	1	10 ⁻³	10 ⁻⁶	10 ⁻⁹
λ (cm)	6.6×10^{-6}	5.0×10^{-3}	5.0	5.0×10^3	5.0×10^6

Molecular Collisions

Rate of gas striking surface – Γ (molecules per $m^{-2}s^{-1}$):

- $\Gamma(m^{-2}s^{-1}) = n \text{ vave}/4 = n (kT/(2\pi m)^{0.5}$ where n = gas density
- Since for Air – average diameter $\sim 3.74 \times 10^{-10} \text{ m}$
 - Area $\sim 1.1 \times 10^{-19} \text{ m}^2$
- Then for N_2 at 10^{-6} torr
 - get monolayer in $1.1 \times 10^{-19} \times 3.9 \times 10^{18} \sim 0.4 \text{ s}$

P (torr)	n (m^{-3})	Particle Flux ($m^{-2}s^{-1}$)		
		H_2	H_2O	N_2
760	2.5×10^{25}	1.1×10^{28}	3.7×10^{27}	2.9×10^{27}
10^{-6}	3.2×10^{16}	1.4×10^{19}	4.8×10^{18}	3.9×10^{18}

Gas Flow – [1]

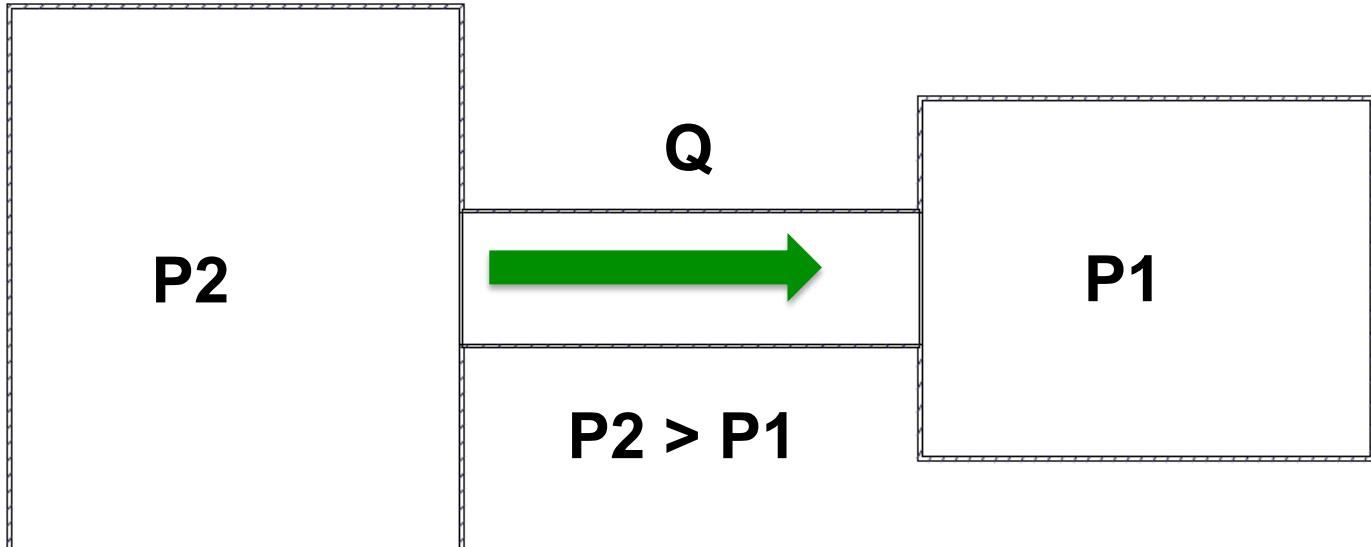
Knudsen number (Kn) is ratio of mean free path and flow channel diameter (a)

$$Kn = \lambda / a$$

- If $Kn < 0.01$ flow driven by molecule-molecule collisions
 - Molecules travel in uniform motion toward lower pressure
 - Can be laminar or turbulent
- If $0.01 < Kn < 1$ flow is in transition
- If $Kn > 1$ flow driven by molecule-wall collisions

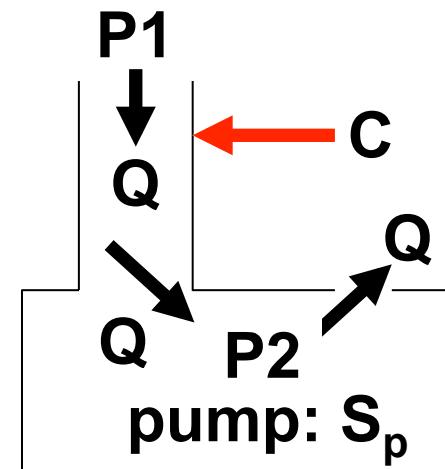
Gas Flow – [2]

- Throughput = Q = gas flow rate = $d(PV)/dt$
 - Q in $\text{Pa}\cdot\text{m}^3/\text{s}$ ($= 7.5 \text{ torr-liter/s}$)
- Gas conductance = C = $Q/(P_2 - P_1)$
 - P_1 = pressure outlet, P_2 = pressure inlet
 - C in m^3/s ($= 1000 \text{ liter/s}$)
- Pumping speed = S = dV/dt (liters/second)
- $Q = (P_2 - P_1) \times C$



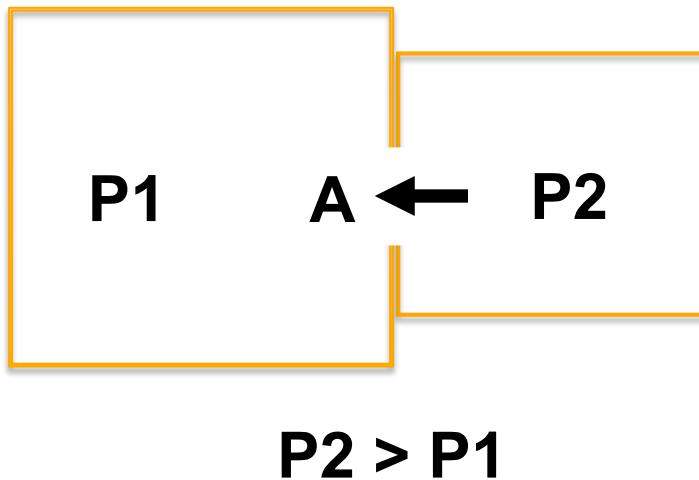
Evacuation Rate

- Evacuation rate at chamber $S_{eff} = Q/P_1$
- Evacuation rate at pump is $S_p = Q/P_2$
- $Q = \text{constant (mass conserved)} = (P_1 - P_2)C$
- Combining get $1/S_{eff} = 1/S_p + 1/C$ (like resistors in parallel)
 - Most restrictive will dominate
- E.G.
 - if pump has $S_p = 100 \text{ liter/s}$
 - C for round tube is $C = 12.1 D^3/L$ (liter/sec), $D = \text{ID of tube (cm)}$, $L = \text{length of tube (cm)}$ – NOTE diameter dependence to 3rd power
 - » For $ID = 6, L = 30 \text{ cm}$ then $C = 86 \text{ liter/sec}$
 - » $S_{eff} = 46 \text{ liter/sec}$ or pumping speed reduced to 46% by tube conductance!



Conductance

- Round Tube of diameter D, Length L $\rightarrow C(m^3/s) \propto (T/Mamu)^{0.5} D^3/L$
 - For Air (Mamu=29 at 22 °C) $C = 12.1 D^3/L$ (liters/sec)
- For aperture A $\rightarrow C(m^3/s) \propto (T/Mamu)^{0.5} A(m^2)$
 - For Air (Mamu=29 at 22 °C) $C(\text{liters/sec}) = 11.6 A (\text{cm}^2)$



Pump-down time

To go from pressure P₁ to P₂ takes time t

- $t = V(\text{liters})/S(\text{liter/s}) \times \ln(P_1/P_2)$
 - E.G., If V = 10 liters, S = 10 liter/sec P₁ = 760 torr, P₂ = 10⁻⁶ torr
 - t ~ 18 s
- **BUT other sources to vacuum load – e.g. water evaporating from vacuum surfaces – make time dramatically longer – e.g. hours**

Mechanical Pumps

Roughing pump

- To begin process from ~ atmosphere down to ~ 10^{-3} torr
- Uses oil to seal between rotating blade to push molecules from inlet to outlet

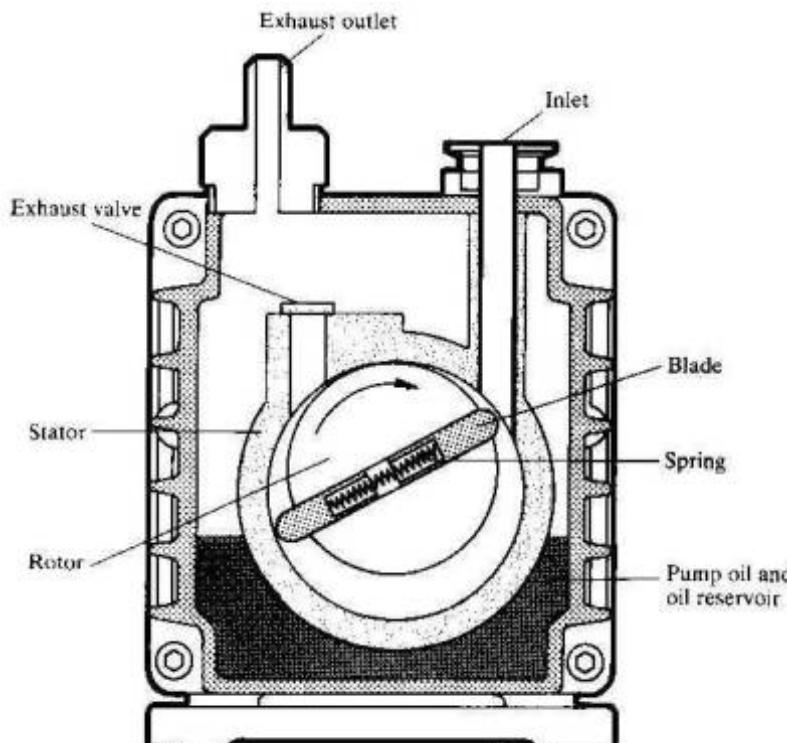
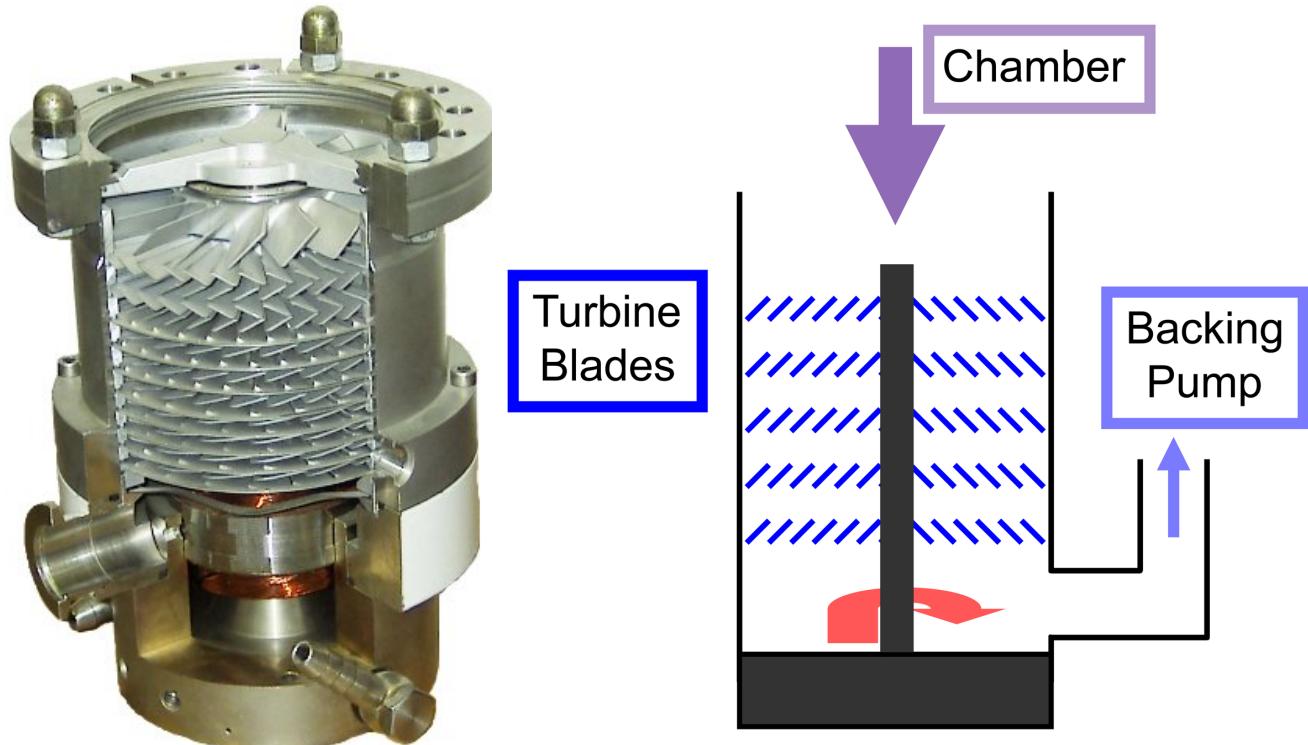


Figure from: http://physics.ucsd.edu/~tmurphy/phys121/lectures/06_vacuum.ppt

Turbomolecular Pumps

- Turbomolecular pumps often used at $<10^{-2}$ torr as next stage pumping after mechanical (roughing) pump
- Turbomolecular pump is connected to mechanical (backing) pump so that pressure differential is between chamber vacuum and $\sim 10^{-3}$ torr of roughing (backing) pump
- Rotating blades ($\sim 24,000$ rpm) push molecules from chamber to backing pump get vacuums $<\sim 10^{-6}$ torr



Cryogenic Pumps

- Cryogenic pumps have surface cooled to LN₂ (77 K) or He (4 K)
- Pumping action is “freezing” molecules on cold surface
- Pumping speed determined by surface area
- Can be very fast and remove largest components of gas (e.g. H₂O and N₂)
- BUT – requires cryogenics to make/maintain temperature
- BUT – additional surface layers of “frozen molecules” makes pump increasingly less effective
 - Then needs to be “regenerated” – warmed up to release frozen molecules
 - If not isolated from vacuum system before regeneration – then full accumulated gas load dumped back into system
- Also used as “cold trap” to prevent e.g. carbon-based (oil from roughing pump) from contaminating vacuum chamber

Ion Pump

- Removes molecules by ionizing molecules that are then driven by voltage to chemically active surface
- Typically for Ultra-High Vacuum applications (10^{-11} torr)
 - Used after Turbomolecular or when vacuum $\sim 10^{-5}$ torr
 - Mechanically simple – but only for very low pressures
- Current from ionized molecules is proportional to pressure – so can use current as pressure gauge

