



# Cellular Networks: Concepts and Theory

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# Overview of Telecommunication Systems

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- **1G:** Basic mobile telephony service
  - Based on **analog** cellular technology
  - e.g., American Mobile Phone (AMPS) and NMT in Europe
- **2G:** Mobile telephony services for mass users with improved ciphering and efficient utilization of the radio spectrum
  - **Digital** cellular technology
  - e.g., GSM (Global System for Mobile communications) and CDMA
- **2.5G:** Mobile **Internet/data services** together with voice services
  - Packet switching technology adding into 2G
  - Providing mobile data services over 2G networks
  - e.g., GPRS (General Packet Radio Service) and EDGE
- **3G:** enhanced 2.5G services with improved mobile internet services and emerging new applications
  - e.g., CDMA2000 and UMTS (Universal Mobile Telecom System)



# Overview of Telecommunication Systems

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- **4G (LTE/WiMAX)**: IP-based voice, data, and multimedia phones
  - faster than 3G
- **5G** : New Radio (NR) and LTE
  - millimeter wave bands (e.g., 26, 28, 38, 60 GHz)
  - OFDM, SCMA (Sparse Code MA), and NOMA (Non-Orthogonal MA) are candidates of standards
  - massive MIMO antennas (64 ~ 256 antennas) & beamforming
  - offering as high as 20 Gbps



# Telecommunication Services

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- **TRADITIONALLY**, a mobile phone is used for talking with another person: point-to-point voice service
- **NOW**, mobile phones are more than phones. They are computing devices with networking capabilities
- What can be done with them?



# Telecommunication Services

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- Emails
  - Emails may be sent to other mobile phone users
  - Instant messages (SMS), WeChat...
  - What are differences in communication technology between emails and voice?
- Web browsing
  - 2G provides limited text-based web browsing services with low-resolution graphics. 3G is better but has still many limitations
  - Trans-coding and adaptation of web contents to fit into handheld devices
- Location-dependent services
  - Identify subscriber locations based on the connection points (base stations) and GPS network
  - Location-specific web contents/services



# Telecommunication Services

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- Mobile game applications
  - Download and store a variety of dynamic applications and execute the applications in the mobile devices
  - Require a better operating environment and higher CPU power
- Video applications
  - 3G enables mobile users to obtain video contents
  - Real-time playback of videos (video stream data transmission)
- Other services
  - Tracking of mobile objects, vehicular networks, self-driving cars
  - Remote control and surveillance, e.g., home and field management
  - Shopping, marketing, logistic services, inventory control, IoT (Internet of Things)
  - .....

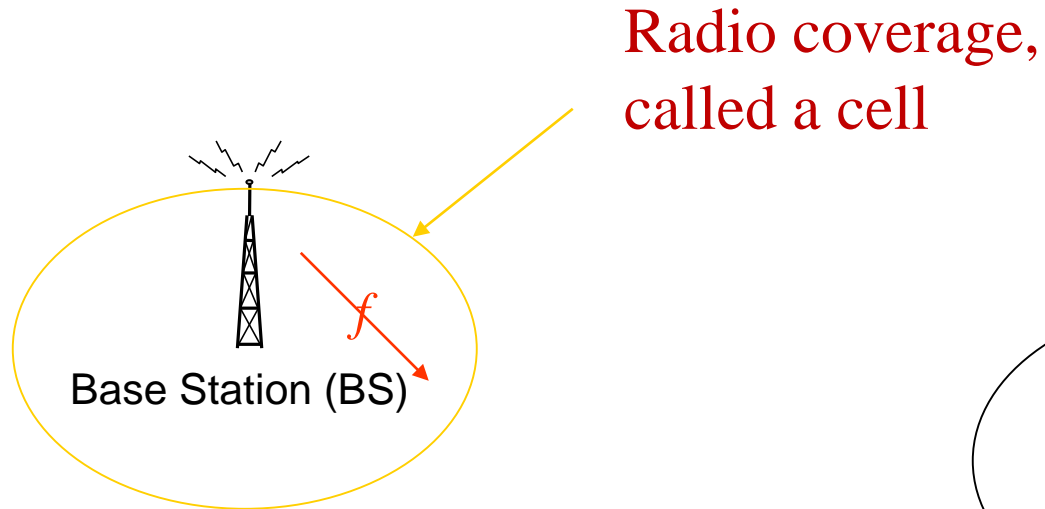


# Cellular Networks

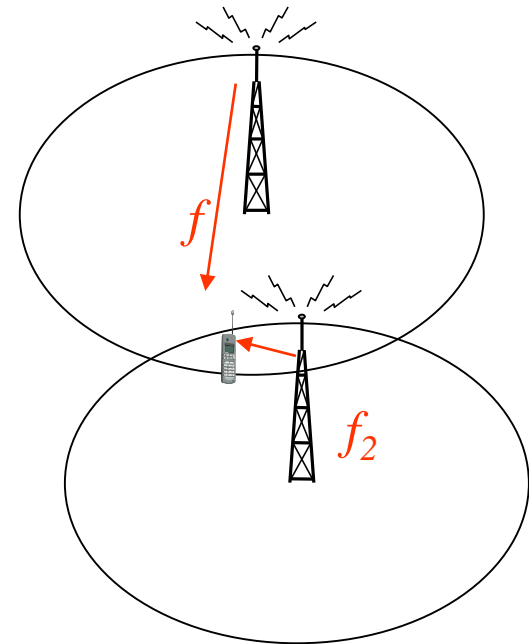
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- In a cellular network, service area is divided into a number of cells
  - Each cell has a BS that connects all MSs in the cell to the system
  - BS does channel allocation and management of MSs
  - One cell  $\Rightarrow$  one BS  $\Rightarrow$  multiple channels  $\Rightarrow$  many MSs
- Do you see the cell boundaries?
  - How to define the boundary of a cell?
  - No physical boundary, but there is a service boundary (no service signal)
- One particular location normally belongs to only one cell
  - Can it belong to more than one cell? Yes
  - Does it allow overlapping in cell area? Yes

# Signal Coverage in Cellular Networks



- If a MS is far away from any BS, it cannot receive any signal from BSs, it is out of service area
- A MS may receive signals from more than one BS







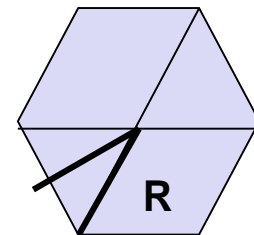
# Why Cellular?

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- Why cellular?
  - A cell is allocated with a number of channels (each channel has a fixed bandwidth and frequency band).
  - A frequency band **can be reused** after a separation of distance
    - but “Near-by” cells should not use the same frequency band due to interference
  - For a given service area, smaller size cells => more channel reuse. **Why?**

# Modeling of a Cell

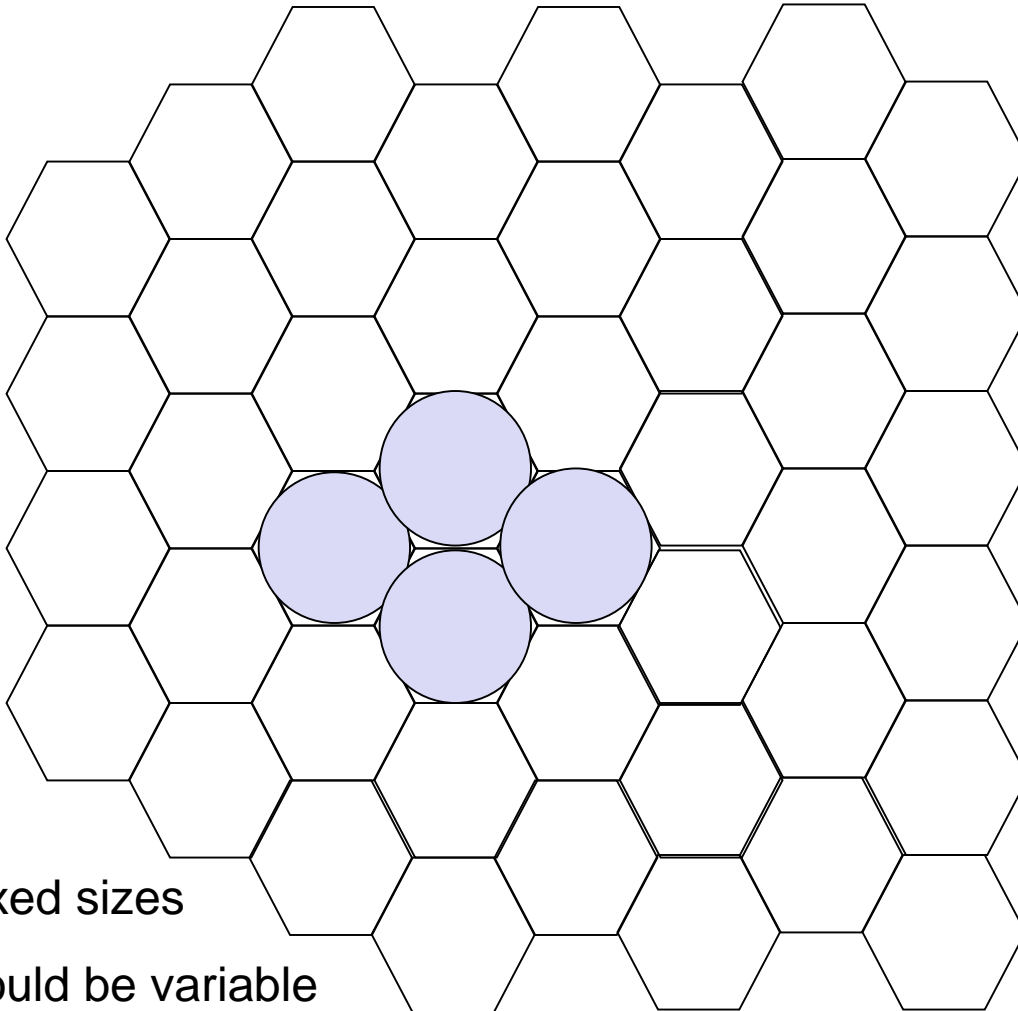
- Cells are modeled as polygons conceptually.
- Can it be circular?
  - Yes, the transmission range is more like a circle in open space, rather than a polygon.
- What is the distance from the center of the cell (location of the BS) to the edge (furthest MS in the cell)?
  - Transmission radius



# Hexagonal cells cover all areas

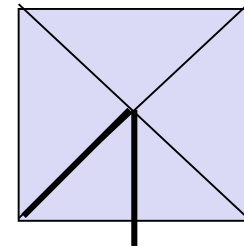
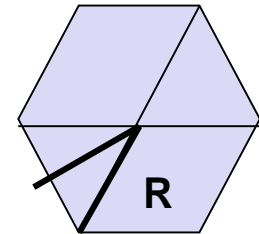
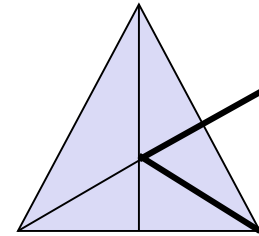
## Circular cells have some gaps (uncovered areas)

Why triangles or squares are no good?



Fixed sizes

Could be variable



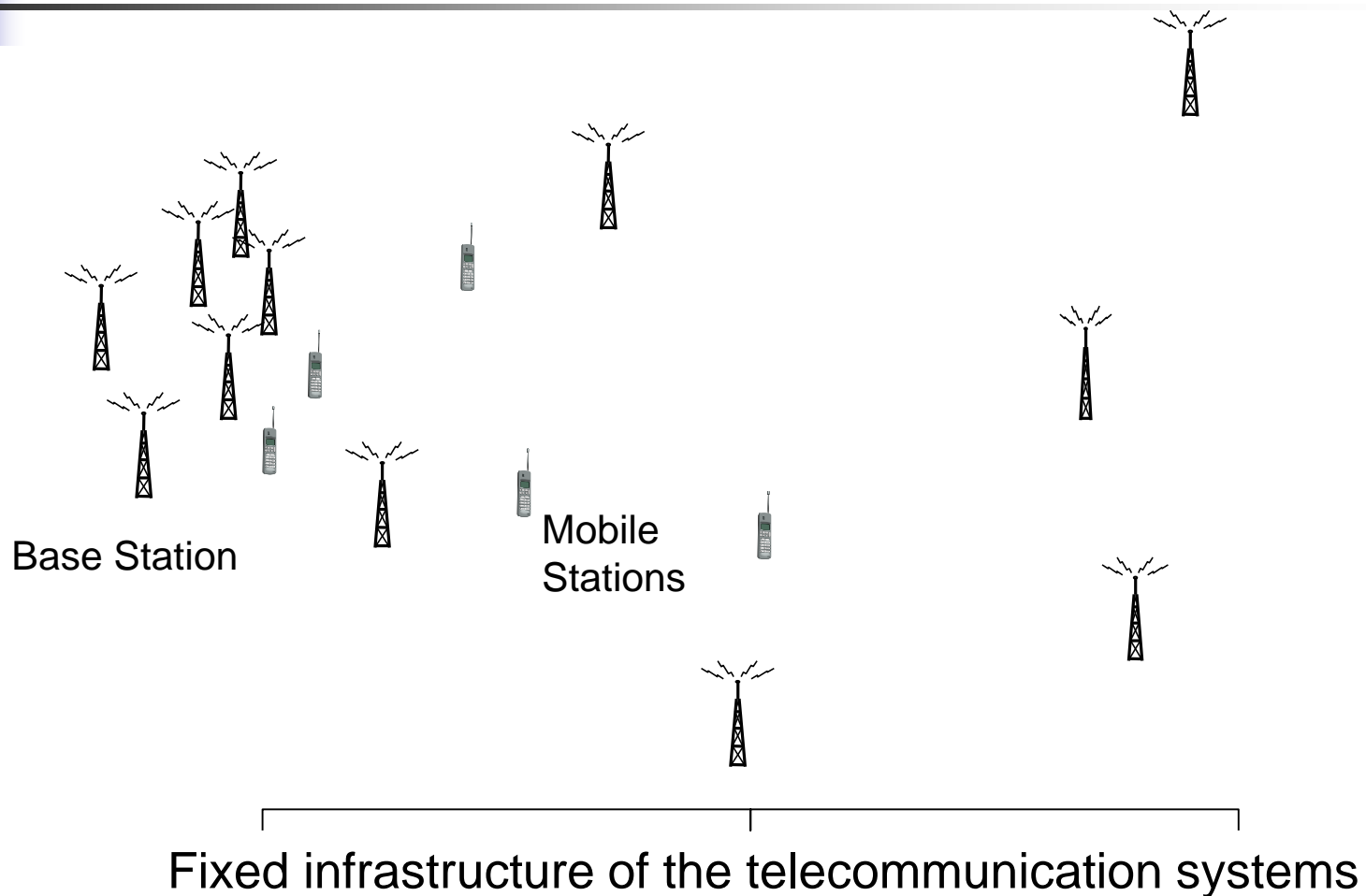


# Handoff/Handover in Cellular Networks

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- Handoff/handover
  - When a MS moves from one cell into another, handoff occurs where the MS is connected to a new BS
  - The new BS allocates a new channel to the MS and the connection is smoothly handed over to the new cell

# Distribution of BSs in Cellular Networks



Uneven distribution of BSs → Why?



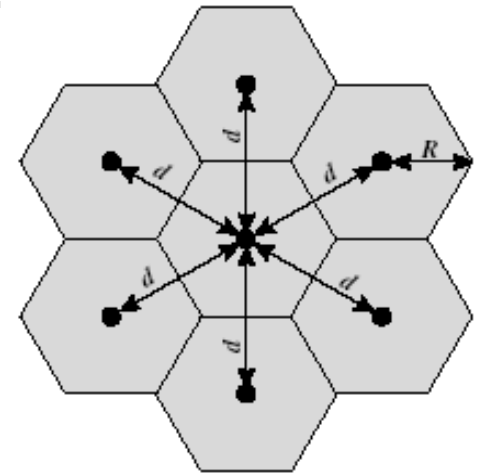
# Cell Sizes

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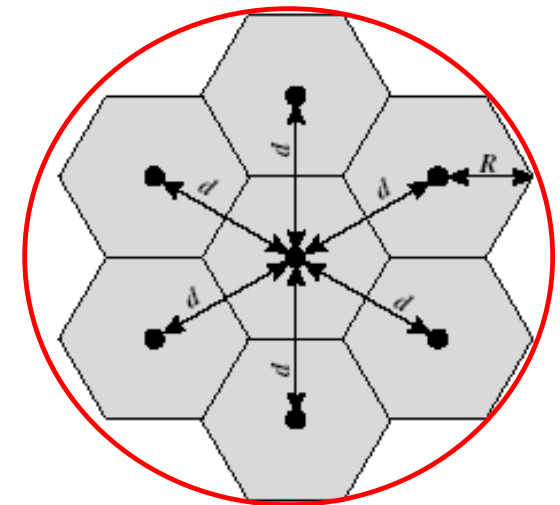
- Cell size: 0.1 – 30 Km (radius). Not a constant. **How to determine?**
  - Determined according to connection load (density of users)
- Macro cell
  - Large cell for sparsely populated area (lesser users)
- Micro cell
  - Small cell for densely populated area (more users)
  - Smaller cells => lower transmission power => more channel reuse
  - **What happens if macro cells are used for highly populated area?**
- Umbrella cell (hierarchical cell)
  - Two (or more) levels: macro cell over multiple micro-cells
    - Macro cell for fast moving users, micro-cells for slow users
  - Reduce number of handoffs for fast moving users (in vehicles)
  - A tradeoff solution for channel reuse and frequent handoffs

# Umbrella Cell

- Purpose of umbrella cells: support both users with high mobility and users with high density
- An Umbrella cell: A macro cell on top of 7 micro cells.
- The macro cell need to use different set of channels from micro cells, i.e., macro cell channels + micro cell channels
- When a new call arrives, should it be assigned to the micro cell channel or macro cell channel?



7 cells with similar size



a macro cell on top of 7 micro cells



# Pros and Cons of Cellular Networks

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- Advantages of cellular networks
  - Higher capacity: **space division multiplexing** to allow frequency reuses to support more users and higher bandwidth
  - Less transmission power: MSs are not far away from BSs. The power consumption of mobile device is minimized
  - Local interference: shorter distance between MS and BS leads to low transmission power => less interference
  - Robustness: Decentralized system with multiple BSs for connection with MSs => more fault tolerant
- Disadvantages of cellular networks
  - Infrastructure: require a complex infrastructure to have full coverage of the whole service area and connect all base stations
  - Handoff: moving from one cell into another





# Area Planning & Frequency Assignment

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- Goal: Min the number of call blocking, Max channel utilizations, Min handoffs (reduce ping-pong effect)
  - Call blocking: a call-request from a MS is rejected due to no free channel available
- Two directions to maximize system throughput at low cost:
  - 1) Divide the area into cells according to the distribution of users and traffic load
  - 2) Find the minimal channel-reuse distance, subject to the satisfactory signal quality (i.e., good SIR)



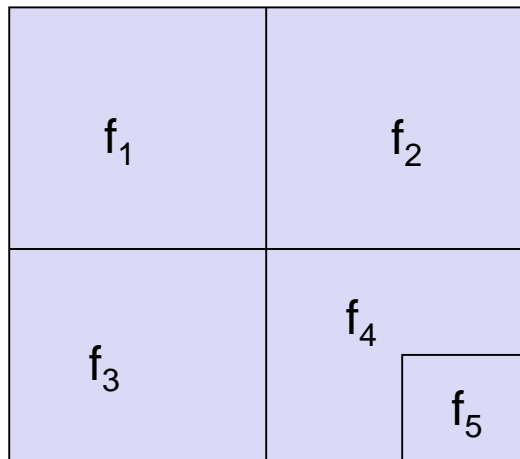
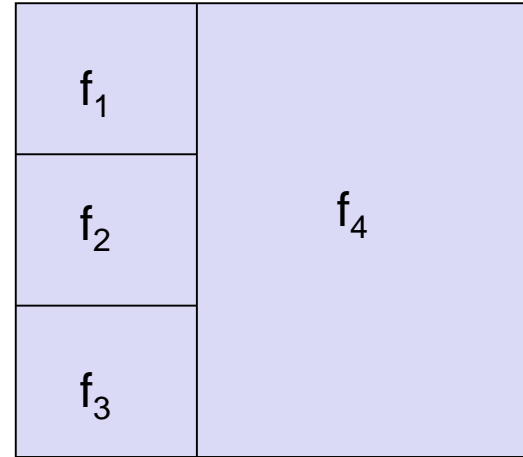
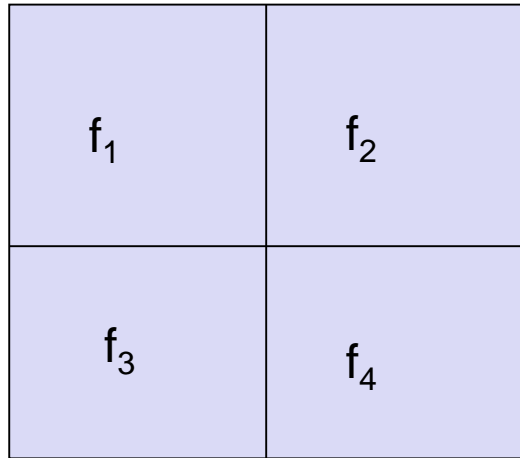
# How to divide an area to cells?

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- What is the right size of a cell?
  - Smaller cells => more cells => more BSs
    - More operational and management cost, but
    - More channel reuse and more users can be supported
  - Large cells => less BSs
    - Less operational cost of BSs, but
    - Poor channel utilization



# Which cell division is better?



Suppose frequency bands can be reused in non-neighboring cells:

- Which cell division has better usage of frequencies?
- Suppose there are 12 channels in total and all cells have the same number of users. How many users a cell division can support?



# Frequency Assignment and Reuses

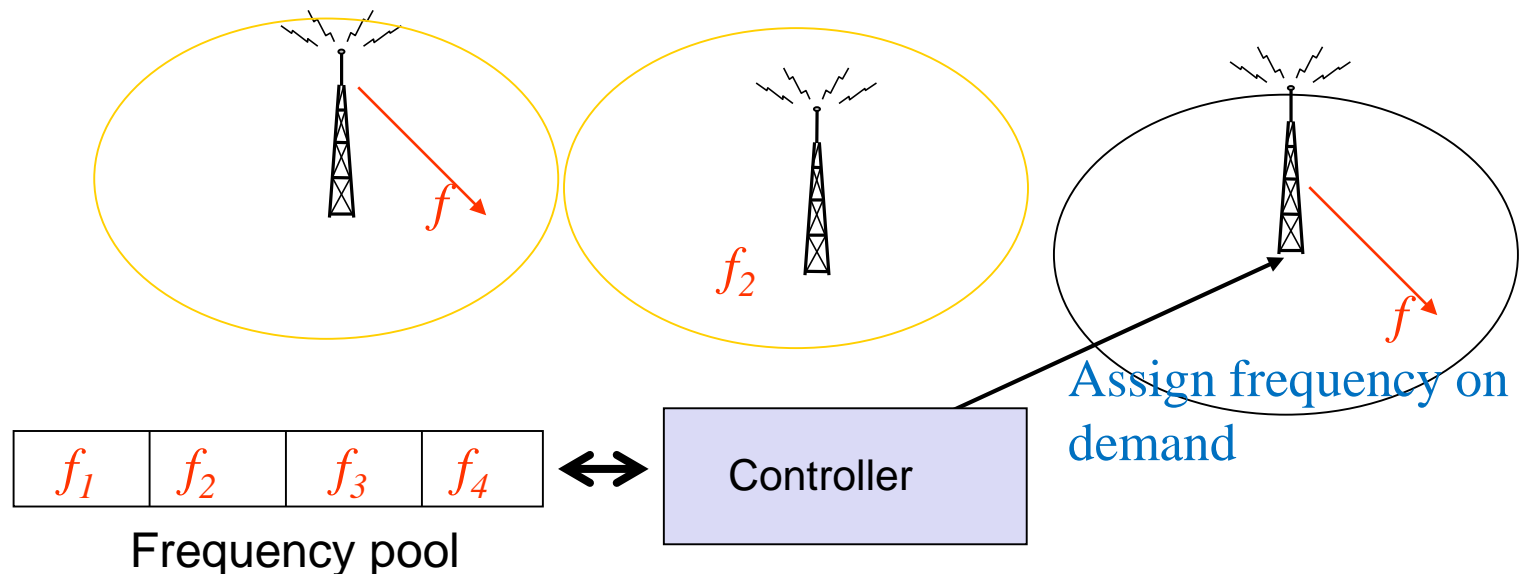
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How to allocate frequency bands to a BS? Two basic ways to allocate frequencies to a BS, given the frequency bands of the system:

- Fixed frequency assignment:
  - Certain frequencies are assigned to a certain cell
  - Problem: Cells have different traffic load and this load changes from time to time
- Dynamic frequency assignment:
  - Any BS can assign the entire bands of frequencies that are currently free for use. (it needs to consider interference, i.e., frequencies currently used in neighbor cells.)
  - The cells with more traffic can use more frequencies
- **How can a BS know the current free channels for assignment?**
  - Coordination among BSs for assignment, or
  - A Central controller maintains a pool of free-channels

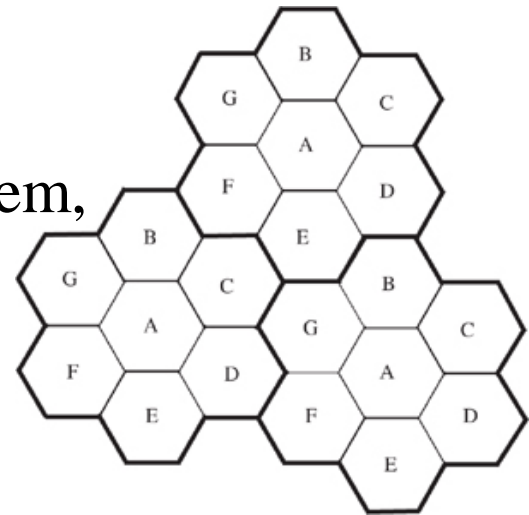
# Dynamic Frequency Assignment

- A central controller maintains the pool of free frequencies
- Each BS needs to request the controller for assignment of a frequency for a newly arrived user
  - BS needs to interact with the controller for every new user, leading to longer time for handoff



# Analysis of Channel Reuse in Cellular Networks

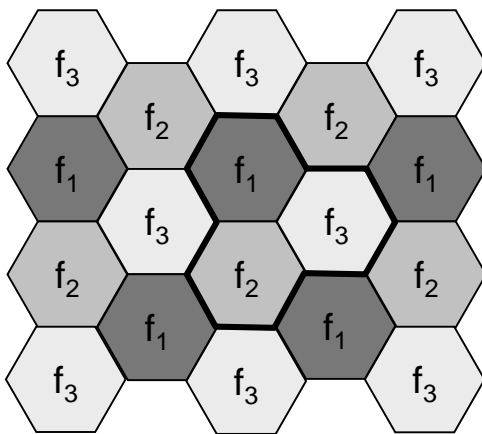
- Divide cells into clusters
  - Cells within a cluster all use different set of channels
  - The same set of channels are reused in cells in different clusters
- The size of the cluster (number of cells in a cluster),  $K$ , is called reuse factor
- The entire system only uses  $K$  sets of different channels
  - Given  $C$ , total number of channels in the system, the number of channels per cell is:  $C/K$



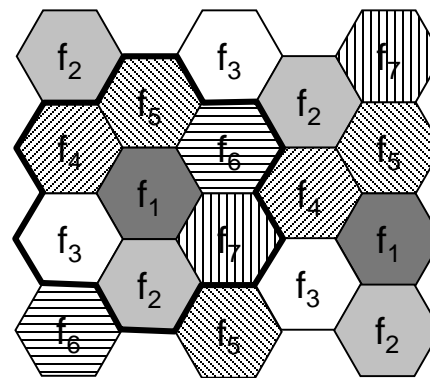
# Frequency Planning

Which one is better,  $K = 3$  or  $7$ ?

- When  $K = 3$ , only neighboring cells use different frequency sets (separated by one cell distance), but in practical, it requires larger separation distance
- With a strong transmission power, the separation distance should be larger (e.g.,  $K = 7$ )



3 cell cluster



7 cell cluster



# Reuse Factor K

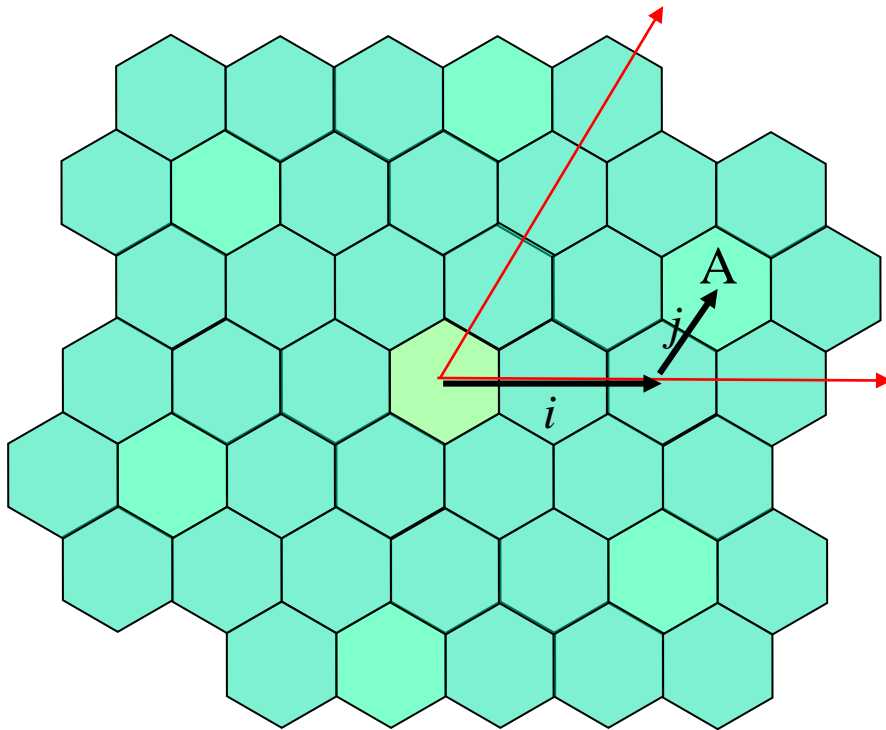
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- Consider a cluster with C duplex channels for K cells
  - $C = c \times K$ , where  $c$  is the number channels for each cell
  - C is the total frequency bands used by the whole system (including guard space)
- The cluster is replicated across the space to cover the whole area
- K, the reuse factor, is the size (no. of cells) of each cluster
  - With a smaller K is (e.g., from 7 reduced to 3), more channels can be allocated to each cell
  - But, a smaller K leads to higher interference. Why?
  - $C = 105$ :  $K = 7 \Rightarrow c = 15$ ;  $K = 3 \Rightarrow c = 35$

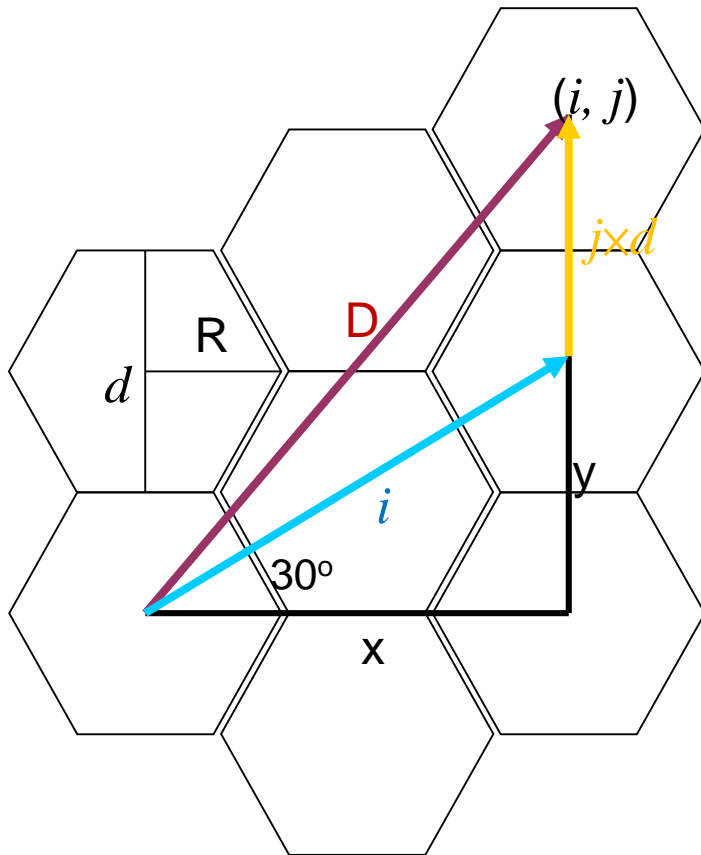
What is the right number of K?



# Hexagon Cell Coordinate System



- A cell is denoted by coordinate  $(i, j)$ . The center cell is  $(0,0)$
- $i$  and  $j$  are integers, called **shift parameters**, i.e., the number of cells being shifted from the center to the current cell
- $i$ : number of cells moved horizontally
- $j$ : number of cells moved vertically from the center cell
- Coordinate of cell A is  $(2,1)$ , relative to the center cell



$$d = \sqrt{3}R$$

$$x = i \times d \cos 30^\circ$$

$$= i \sqrt{3} R \cos 30^\circ = 3/2 i R$$

$$y = i \sqrt{3} R \sin 30^\circ = \sqrt{3} / 2 i R$$

$$D^2 = x^2 + (y + j)^2 \quad \boxed{j \times d}$$

$$= (3/2 i R)^2 + (\sqrt{3}/2 i R + j \sqrt{3} R)^2$$

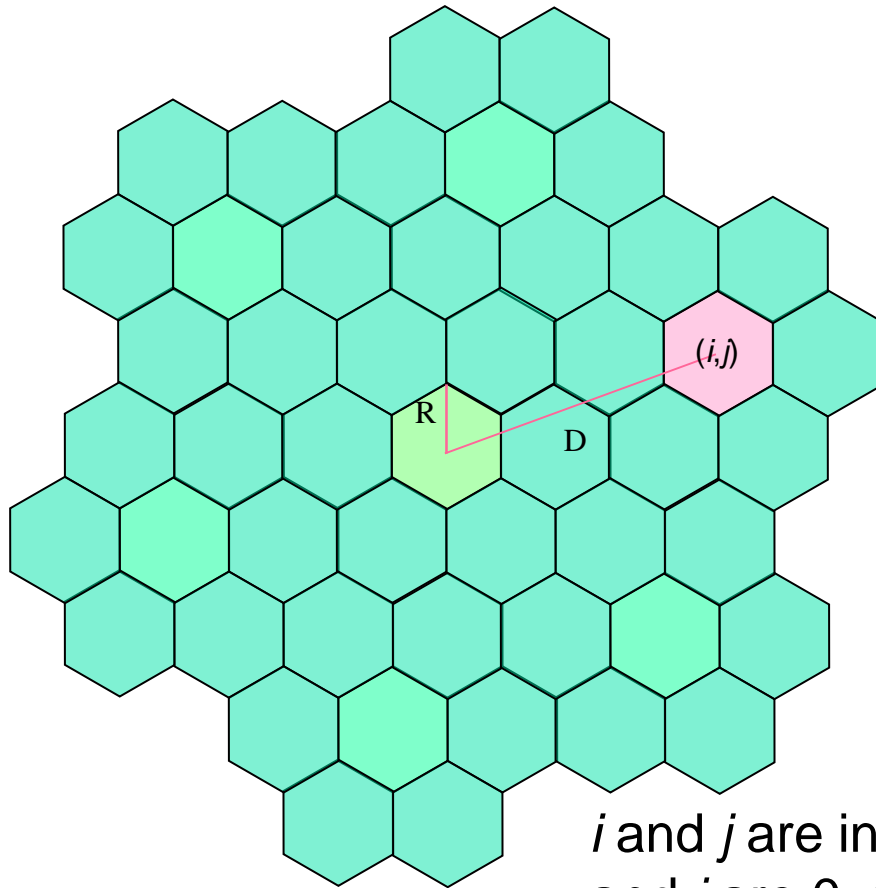
$$= 9/4 \, i^2 R^2 + 3R^2 \, (i^2/4 + i j + j^2)$$

$$= 3R^2 (i^2 + j^2 + ij)$$

$$D = \sqrt{3R^2 (i^2 + j^2 + ij)}$$

$$= R \sqrt{3(i^2 + j^2 + ij)}$$

# Distance & Reuse Factor



$$D = \sqrt{3(i^2 + ij + j^2)}R$$
$$= \sqrt{3K}R$$

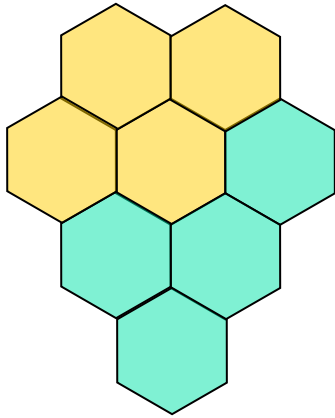
where

$$K = i^2 + ij + j^2$$

Reuse factor: number of cells in the cluster within distance from  $(0,0)$  to  $(i,j)$

$i$  and  $j$  are integers. The possible values for  $i$  and  $j$  are 0, 1, 2, 3, ... Then,  $K = 1, 3, 4, 7, 9, \dots$

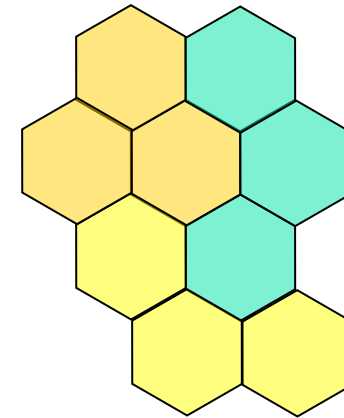
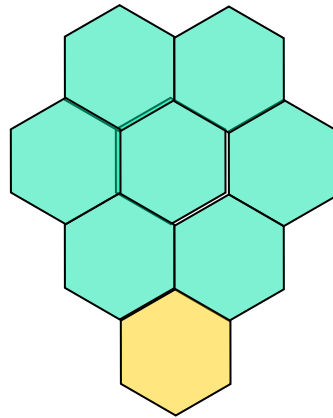
# K and No. of Channels per Cell



Each cell =  $C / K$

$K = 7$

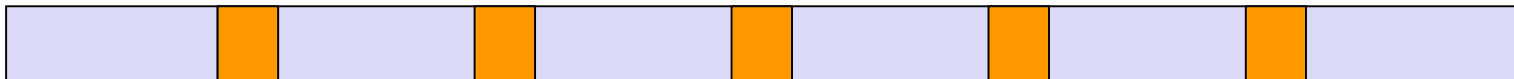
Each cell =  $C / 7$



$K = 3$

Each cell =  $C / 3$

C is a constant for the entire system. It is divided into K groups of channels separated by guard frequencies





# Signal Quality

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- The signal quality depends on the ratio between signal power and interference (noise) power

$$\frac{S}{I} = \frac{S}{\sum_i I_i} \quad \longleftarrow \text{Interference from the } i^{\text{th}} \text{ BS}$$

- This is called **signal-to-interference ratio** (SIR) or Signal-to-noise ratio (SNR)



# Signal-to-Interference Ratio (SIR)

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- Signal-to-noise ratio (SNR, or SIR)

$$(SNR)_{\text{dB}} = 10 \log_{10} \frac{\text{signal power}}{\text{noise power}}$$

- SNR is typically measured at a receiver
- SNR sets the upper bound on achievable data rate
  - High SNR => high-quality signal, high data rate
  - Low SNR => low data rate (802.11 Auto Rate Fallback)



# Calculation of SIR/SNR

- SIR is measured in dB (decibel) .
- SIR in dB =  $10 \cdot \log_{10}(P_{\text{Signal}}/P_{\text{Noise}})$ .
- Example: Given SIR = 20dB, **what is ratio of  $P_{\text{Signal}}/P_{\text{noise}}$ ?**

$$P_{\text{Signal}}/P_{\text{Noise}} = 10^2 = 100$$

SIR = 20 ~ 25 dB	Strong Signal
SIR = 15 ~ 20 dB	Good Signal
SIR < 12 dB	Poor Signal



- $$P_r = P_0 d^{-\alpha}$$

- 
- A diagram of a hexagonal lattice. A central hexagon is highlighted with a double border. Two vectors,  $\mathbf{i}$  (cyan) and  $\mathbf{j}$  (yellow), originate from the bottom-left vertex of this central hexagon. Vector  $\mathbf{i}$  points to the top-right vertex, and vector  $\mathbf{j}$  points to the top vertex. A vector  $\mathbf{D}$  (purple) also originates from the same point and points to the top-right vertex of the hexagon immediately to the right of the central one. A right-angled triangle is formed by the horizontal distance  $x$  and vertical distance  $y$  between the origin and the tip of  $\mathbf{D}$ . The angle between the horizontal axis and vector  $\mathbf{i}$  is  $30^\circ$ . The distance from the origin to the tip of  $\mathbf{D}$  is labeled  $R$ . The distance from the origin to the tip of  $\mathbf{j}$  is labeled  $d$ .



# SIR Analysis in Cellular Networks

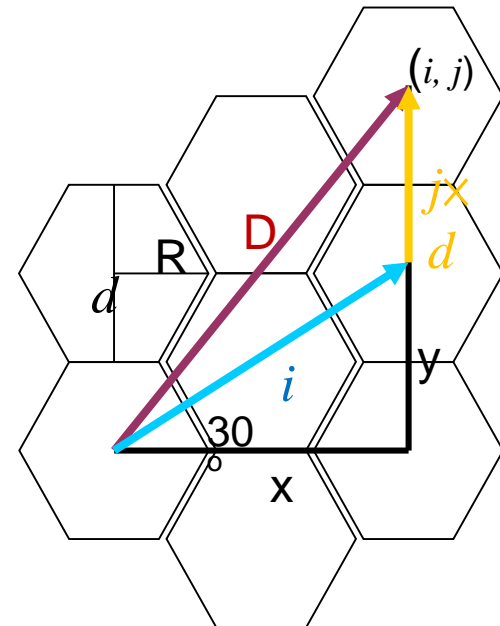
## ■ Assumption:

- The user is located at the corner of a cell, i.e.,  $d = R$
- Interference from all other BSs using the same channel
- All BSs use the same power

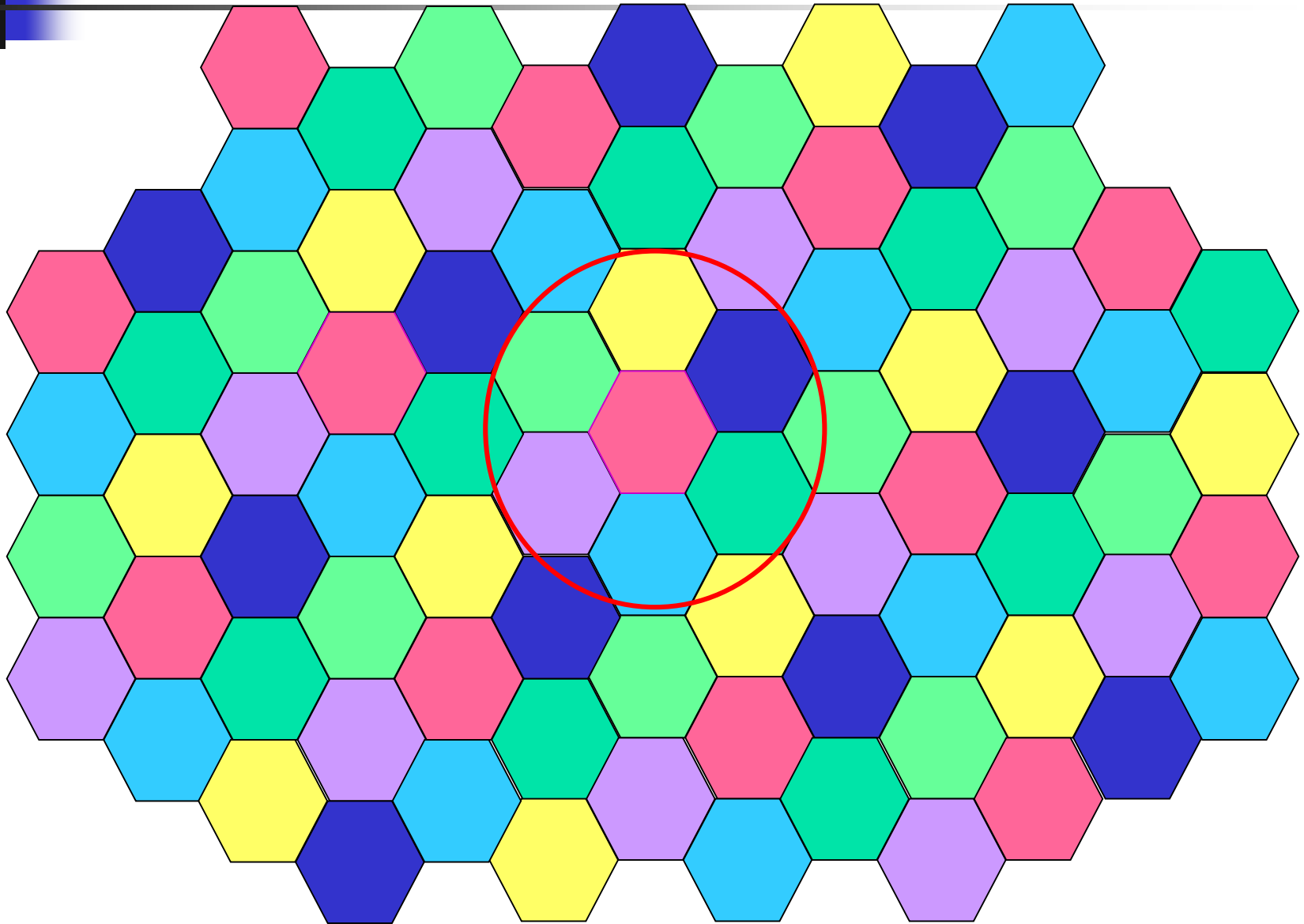
$$S = P_0 R^{-\alpha}$$

$$\frac{S}{I} = \frac{P_0 R^{-\alpha}}{\sum_i P_0 D_i^{-\alpha}} = \frac{R^{-\alpha}}{\sum_i D_i^{-\alpha}}$$

$D_i$  is the distance between the centers of the reference cell and the  $i$ -th interfering cell



# Reuse Factor $K = 7$

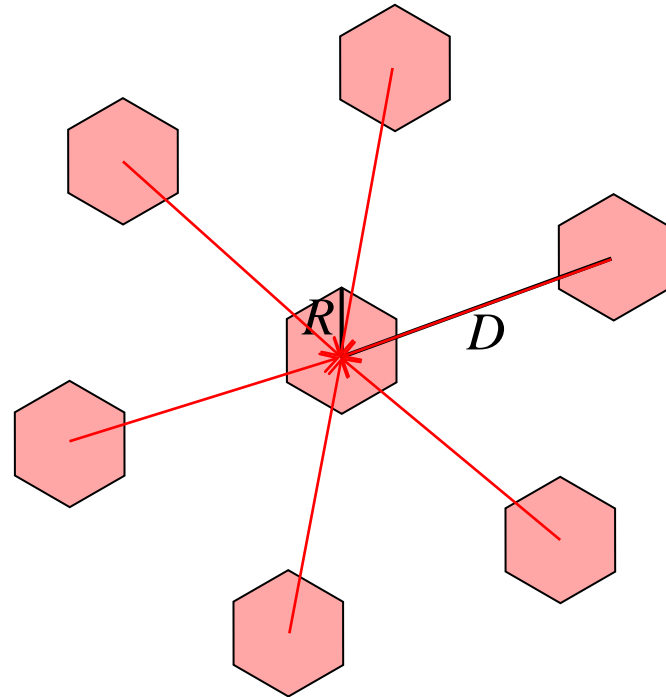


# SIR Calculation for $K = 7$

- Consider only the 1<sup>st</sup> tier of interfering cells
- Note: in real cases, more factors need to be considered. **What are these factors?**

$$S/I = R^{-\alpha} / 6D^{-\alpha}$$

$$\frac{S}{I} = \frac{1}{6} \left( \frac{D}{R} \right)^{\alpha}$$





# Calculate K for a Required SIR Value

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- Suppose at least  $SIR = 18$  dB.
- What is the minimum reuse factor?  
(assume  $\alpha = 4$ )
- We need to find the minimum distance D from the 1<sup>st</sup> tier of interfering BSs...



# What is the right K?

$$10\log_{10}S/I \geq 18\text{dB}$$

$$\frac{S}{I} = \frac{1}{6} \left( \frac{D}{R} \right)^\alpha \geq 10^{18\text{dB}/10} = 10^{1.8} \approx 63$$

$$D \geq 4.4R$$

$$D = \sqrt{3KR}$$

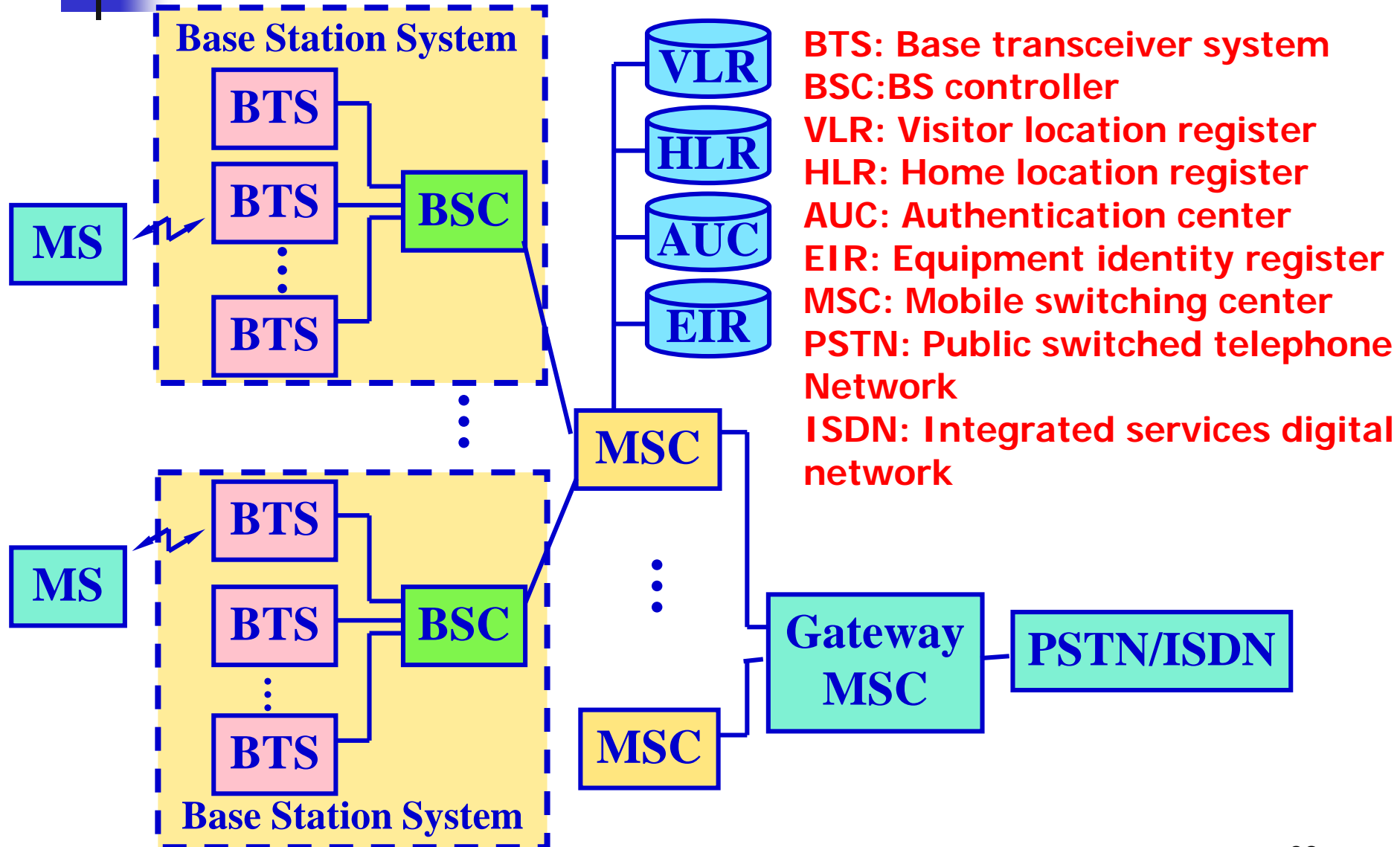
$$\sqrt{3K} \geq 4.4$$

$$K \geq 6.5$$

Choose  $i = 2, j = 1$  or  $i = 1, j = 2$

Ans:  $K = 7$

# Cellular System Infrastructure



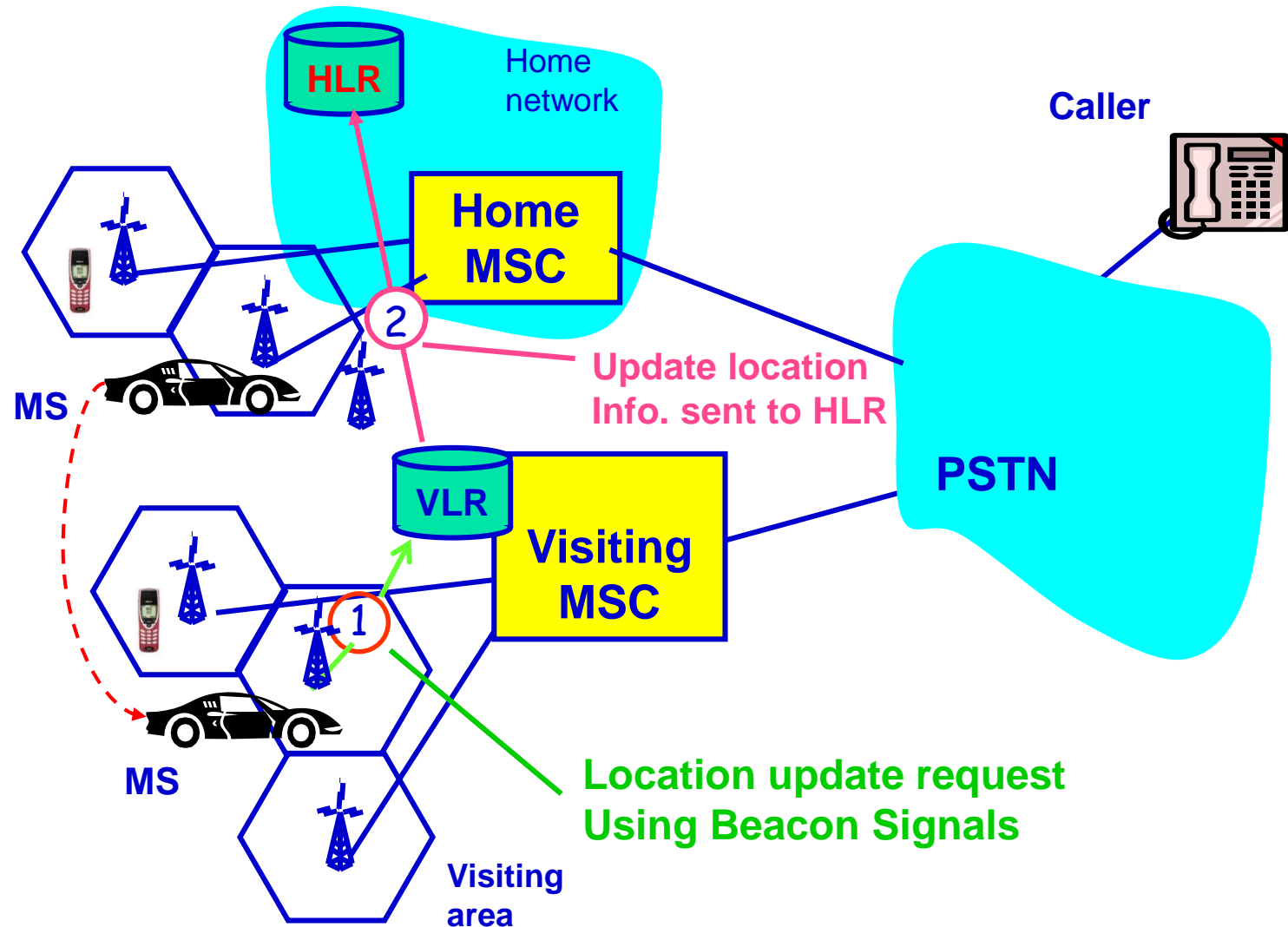


# VLR/HLR/AUC/EIR

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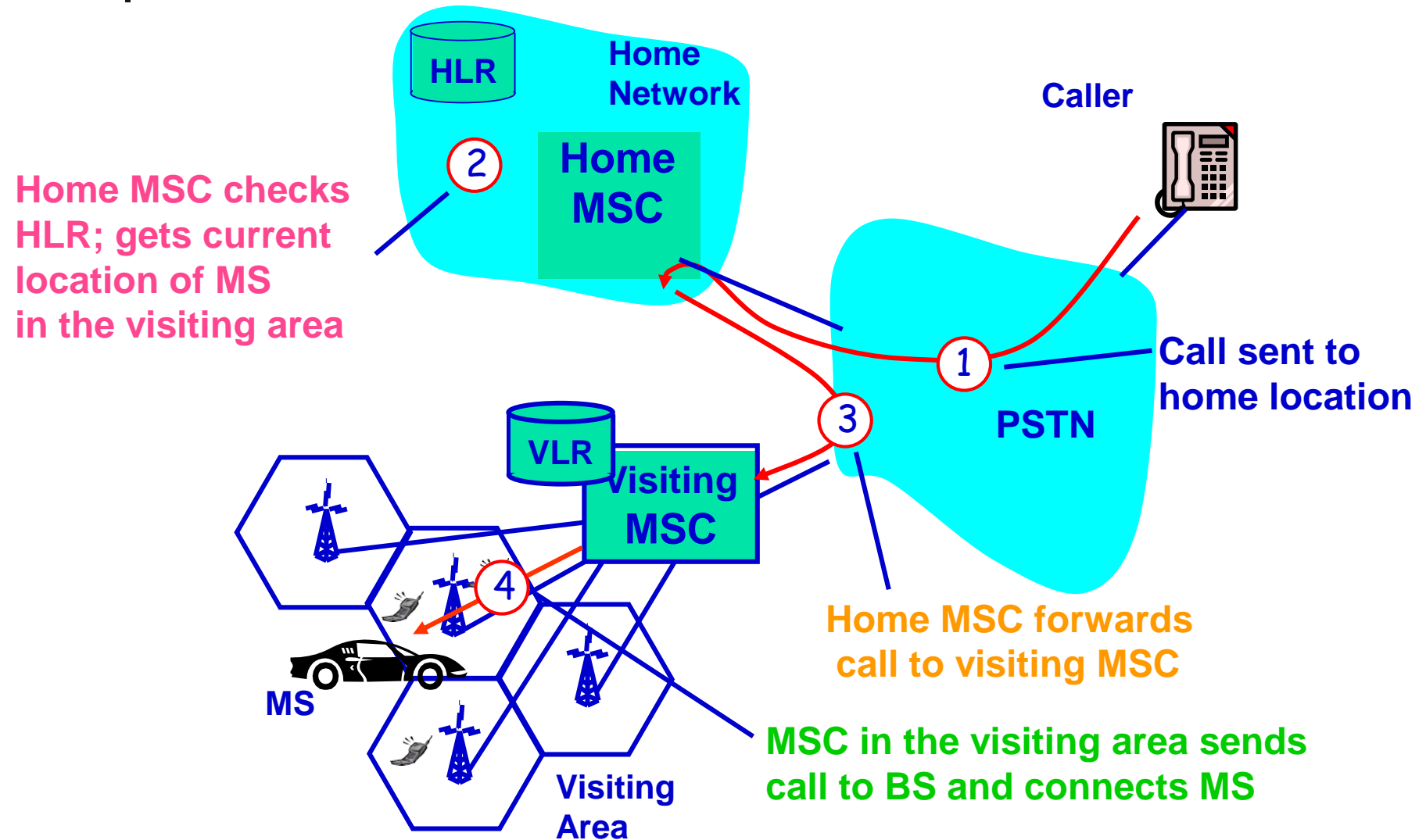
- VLR contains information about all visiting MSs in the particular area of MSC
  - VLR has pointers to the HLR's of visiting MS
  - VLR helps in billing and access permission to the visiting MS
- AUC provides authentication and encryption parameters
- EIR contains identity of equipment that prevents service to unauthorized MSs

# Automatic Location Update





# Automatic Call Forwarding using HLR-VLR





# Tracking MS Location & Handoff

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- Wireless system needs to know whether MS is currently located in its **home area** or some other area (for routing incoming calls)
  - This is done by periodically exchanging signals between BS and MS known as **beacons**
- BS periodically broadcasts beacon signal (e.g., 1 per second) to detect the MS around
- Each MS listens to beacons, when it hears signal from a new BS, it adds it to the **active beacon kernel table**
  - This information is used by the MS to locate the nearest BS
- Information carried by beacon signal: cell ID, gateway ID of the paging area, timestamp, etc.

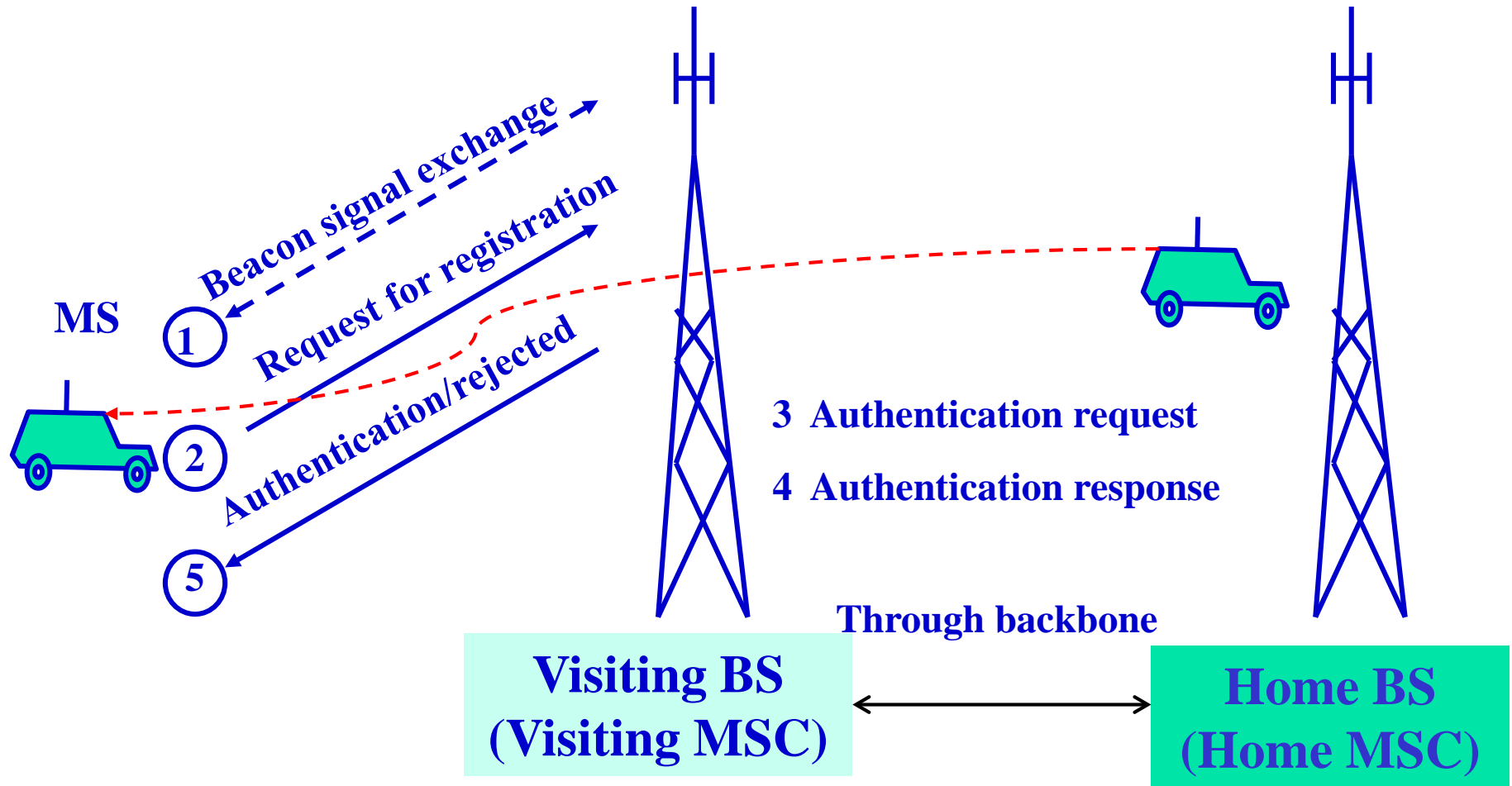


# Steps for MS moving to a new MSC

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- When MS decides that it needs to connect to a new BS (a new subscription area), it initiates the handoff process
  - The new BS performs the user level processing by contacting the home MSC of the MS to find:
    - Who is the user?
    - What are its access permissions?
    - Keeping track of billing
- (no need of this operation if the MS is within the same MSC)
- The home MSC sends appropriate authentication response to the current serving BS (visiting MSC)
  - The visiting MSC (via the visiting BS) approves/disapproves the user access

# a MS moving outside its subscription area





# Summary

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- Cells are modelled as Hexagons
  - Channel reuse
  - Umbrella cells
- Cell size and density of users
  - Frequency assignment
- Channel reuse factor
  - Calculating interference distance in hexagon model
  - SIR in hexagon model
  - Calculating reuse factor  $K$  to meet required SIR
- Cellular system infrastructure
  - Keeping track of users and handoff



# Exercise

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- Suppose the system requires  $SIR \geq 20$  dB. What is the minimum reuse factor? Assume  $\alpha = 3$ .