## **Lab 8 K-Means Clustering**

## Overview of algorithm

- 1. Randomly choose K centroids (in practice we often choose them from the existing data points)
- 2. Calculate the distance of all instances to the K centroids and assign instances to closest centroid
- 3. Calculate new centroid for each of the K clusters
- 4. Repeat Step 2 and 3 until clusters assignments are stable or centroids are not changing

The MNIST dataset is a dataset of  $28 \times 28$  images of hand-written digits (http://yann.lecun.com/exdb/mnist/). To read these images in Python, you can use the following script.

## from sklearn.datasets import fetch\_openml

```
mnist = fetch_openml('mnist_784', version=1)
```

X = mnist["data"]

Since the dataset is quite large, restrict yourself to the first 2000 training images. The data should be a  $2000 \times 784$  matrix.

## Requirements

- a. Write a function my\_kmeans to perform a k-means clustering of the 2000 images of digits.
- b. Your function should take 3 arguments, the data matrix, the number of clusters K, and the number of initializations M.
  - (1) Your code should consist of 3 nested loops.
  - (2) The outermost (from 1 to M) cycles over random centroids initializations (i.e. you will call k-means M times with different initializations).
  - (3) The second loop is the actual k-means algorithm for that initialization, and cycles over the iterations of k-means.
  - (4) Inside this are the actual iterations of k-means. Each iteration can have 2 successive loops from 1 to K: the first assigns observations to each cluster and the second recalculates the means of each cluster.
- c. Your function should return:
  - (1) the K centroids and cluster assignments for the best solution with the lowest loss function (recall that the k-means loss function is the sum of the squared distances of observations from their assigned means)
  - (2) the sequence of values of the loss-function over k-means iterations for the best solution (this should be non-increasing)
  - (3) the set of M terminal loss-function values for all initializations
- d. Run your code on the 2000 digits for K = 10 and M = 15. Plot the sequence of values of the loss-function over k-means iterations for the best solution.
- e. Plot the M terminal loss-function values for all initializations.