Template

November 14, 2019

$\operatorname{GummyBear}$

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.vimrc

```
void init() { memset(f, -1, sizeof(f)); }
                                                       while(x) dig[pos++] = \times \% 10, \times /= 10;
                                                                                       return dfs(pos -1, ..., 1);
                                                                                                                                                                                                    init();
// 可调用 solve(x) 多次
11 solve(11 x) {
                             int pos = 0;
                                                                                                                                                                       void solve()
                                                                                                                                          nmap<F9> : :w <CR> :!g++ % -0 %< -02 -g -std=c++11 -wall <CR>
                             sts=2 sw=2
                                                                                                             nmap<F8> : !time ./%< < %<.in <CR>
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```

if (!lim) f[] = res;

return res;

DataStructure 3

2DST

#define rep(i, a, b) for(int i=(a); i<(b); i++) #define per(i, a, b) for(int i=(b)-1; i>=(a); i--)

#define pb push_back

#**define** mp make_pair

#define se second #define fi first

#include<bits/stdc++.h>

Head

1.2

using namespace std;

#define de(a) cout << #a << " = " << a << endl #define dd(a) cout << #a << " = " << a << " "

#define sz(a) (int)a.size()

#define all(a) a.begin(), a.end()

#define pw(x) (111<<(x))

#define endl "\n"

typedef pair<int, int> pii;

typedef vector<int> vi; typedef long long ll;

typedef double db;

int main() {

```
rep(i, 1, dep1+1) rep(j, p[i], n+1) rep(k, 0, dep2+1) rep(l, p[k], m+1) st[i][k][j][l]=max(st[i-1][k][j-p[i-1]][l]], st[i-1][k][j][l]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int l1 = Log[x2-x1+1], l2 = Log[y2-y1+1];
int res1 = max(st[l1][l2][x1+p[l1]-1][y1+p[l2]-1], st[l1][l2][x2][y2]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int res2 = max(st[l1][l2][x1+p[l1]-1][y2], st[l1][l2][x2][y1+p[l2]-1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(i, 1, n + 1) rep(j, 1, dep2 + 1) rep(k, p[j], m + 1) st[0][j][i][k] = max(st[0][j-1][i][k], st[0][j-1][i][k - p[j-1]]);
                                                                                                                                                                                                                                                                                for(dep1 = 0; (1 << dep1) < n; dep1++);
                                                                                                                                                                                                                                                                                                                      For(dep2 = 0; (1 << dep2) < m; dep2++);
                                                                                                                                                                                                                                                                                                                                                                                                       st[0][0][i][j] = a[i][j]; // modify
                                                                                                                                                                                                  rep(i, 0, M) p[i] = 1 << i;
rep(i, 2, N) Log[i] = Log[i >> 1] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int qry(int x1, int y1, int x2, int y2){
                                                                                                                                                            void build(int n, int m, short a[][N]){
                                                                                                                                                                                                                                                                                                                                                               rep(i, 1, n+1) rep(j, 1, m+1)
                                                                              int Log[N], p[M], dep1, dep2;
short st[M][M][N][N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  //attention to range of k
                                     const int N = 1010, M = 11;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return max(res1, res2);
namespace ST_2D{
```

2DSegTree3.2

```
void upd(int L,int R,int C,int l=0,int r=m,int rt=1) {
// 修改: 将区域内的值修改为区域最大值 + h
                                                                                                 struct seg {
   int ma[N<<2], la[N<<2];</pre>
                        // 询问:求区域最大值
                                                   const int N=1010;
                                                                            int n, m, q;
```

DP

// cout << setiosflags(ios::fixed); std::ios::sync_with_stdio(**false**);

std::cin.tie(0);

// cout << setprecision(3)

return 0;

DigDP

```
if (...) res += dfs(pos - 1, ..., lim & (i == up));
                                                                       if (!lim && ~f[...]) return f[...];
                       dfs(int pos, ..., bool lim) {
                                                                                                                          int up = lim ? dig[pos] : 9;
                                                  if (pos == -1) return ?;
                                                                                                                                                 rep(i, 0, up + 1)
                                                                                               11 res = 0;
11 f[];
```

```
else if (p2 > r) {tmp[i] = a[p1]; p1++;}
else if (a[p1], y <= a[p2],y) {tmp[i] = a[p1]; p1++;}</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, l, pos) fen.add(fen.a1, a[i].z, —a[i].num);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 1, n+1) cin >> a[i].x >> a[i].y >> a[i].z;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // desc : bud a cartesion tree from a[0] .. a[n-1]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 1, n+1) {
    if (i > 1 && a[i] == a[i-1]) { a[nn].num++;
                                                                                                                                                                                                                                                   while (pos <= mid && a[pos].y <= a[i].y) {
   fen.add(fen.a1, a[pos].z, a[pos].num);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(i, 1, nn+1) ans[a[i].ans] += a[i].num;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(i, l, r+1){
    if (p1 > mid) {tmp[i] = a[p2]; p2++;}
                                                                                                                                                                                                                                                                                                                                                                   a[i].ans += fen.sum(fen.a1, a[i].z);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // !!!! : return rt, a[n] will be rewrite
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, 0, n) cout << ans[i] << endl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             else {tmp[i] = a[p2]; p2++;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(i, l, r+1) a[i] = tmp[i];
                                                     a[1].ans = a[1].num - 1;
                                                                                                                                                                      CDQ(1, mid); CDQ(mid+1, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           CartesianTree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            sort(a+1, a+n+1, cmp);
                                                                                                                                     int mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           a[++nn] = a[i];
void CDQ(int 1, int r){
                                                                                                                                                                                                                       rep(i, mid+1, r+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           a[nn].num = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                   p1 = 1; p2 = mid+1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   cin >> n >> k;
                                if (1 == r) {
                                                                                                                                                                                                                                                                                                                  :++sod
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // time : 0(N)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           fen.ini(N);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CDQ(1, nn);
                                                                                      return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return 0;
                                                                                                                                                                                               pos = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int main(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   nn = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         3.4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(x2>=mid+1) ans=max(ans, qry(x1, x2, y1, y2, mid+1, r, rt<<1|1));</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void upd(int x1, int x2, int y1, int y2, int c, int l=0, int r=n, int rt=1) {
```

if(x1<=mid) ans=max(ans, qry(x1, x2, y1, y2, 1, mid, rt<<1));</pre>

if(x1<=1&&r<=x2) return ans=max(ans, ma[rt].qry(y1, y2));</pre>

int mid=l+r>>1;

return ans;

CDO

3.3

}T;

ans=max(ans, la[rt].qry(y1, y2));

int ans=0;

int qry(int x1,int x2,int y1,int y2,int l=0,int r=n,int rt=1) {

if(x2>=mid+1) upd(x1, x2, y1, y2, c, mid+1, r, rt<<1|1);</pre>

 $if(x1 \le mid) upd(x1, x2, y1, y2, c, 1, mid, rt \le 1);$

if(x1<=1&&r<=x2) return la[rt].upd(y1, y2, c), void();</pre>

ma[rt].upd(y1, y2, c);

seg ma[N<<2], la[N<<2];

struct Seg {

if(L<=mid) ans=max(ans, qry(L, R, 1, mid, rt<<1));
if(R>=mid+1) ans=max(ans, qry(L, R, mid+1, r, rt<<1|1));</pre>

if(L<=l&&r<=R) return ans=max(ans, ma[rt]);

int mid=l+r>>1;

return ans;

ans=max(ans, la[rt]);

int ans=0;

int

if(L<=l&&r<=R) return la[rt]=max(la[rt], c), void();</pre>

ma[rt]=max(ma[rt], c);

if(R>=mid+1) upd(L, R, c, mid+1, r, rt<<1|1);</pre> qry(int L,int R,int l=0,int r=m,int rt=1) {

if(L<=mid) upd(L, R, c, l, mid, rt<<1);</pre>

int mid=1+r>>1

```
return x == b.x & y == b.y & z == b.z;
                                                                                                      bool operator == (const node & b) const{
                                                                                                                                                                                                                                                                                                                                                                                   //if (a.y != b.y) return a.y < b.y;
                                                                                                                                                                                                                                           if (a.x != b.x) return a.x < b.x;
                                                                                                                                                                                                                                                                      if (a,y) = b,y return a,y < b,y;
                         int p1, p2, pos, n, k, nn, ans[N];
                                                                                                                                                                                                                                                                                                                                                      bool cmp2(node a, node b){
                                                                                 int x, y, z, num, ans;
                                                                                                                                                                                                                 bool cmp(node a, node b){
                                                                                                                                                                                                                                                                                                                                                                                                            //return a.z < b.z;
const int N = 200005,
                                                                                                                                                                                                                                                                                                     return a.z < b.z;
                                                                                                                                                                                                                                                                                                                                                                                                                                        return a.y < b.y;
                                                                                                                                                                                      } a[N], tmp[N];
                                                      struct node{
```

a[n] = INT_MAX; vi v(1, n); fill_n(1s, n, -1), fill_n(rs, n, -1);

int cartesionTree(int a[], int n) {

int ls[N], rs[N];

```
r, rt); }
 Ľ
 ۲,
   ó
= 0; cnt[rt][o] = qry(1, r, v,
rep(o, 0, 2) { 11 v
                                               KDT
                                                                                      // init
                                                3.7
                while (a[v.back()] < a[i]) 1s[i] = v.back(), v.pop_back();</pre>
                                  v.pb(rs[v.back()] = i);
 rep(i, 0, n) {
                                                                   return v[1];
```

Fenwick

3.5

```
T sum(T *a, int p) { T r=0; for(; p>=1; p-=p & -p) r+=a[p]; return r; } T pre(int p) { return !p ? 0 : sum(a1, p) * p - sum(a2, p);} T qry(int 1,int r) {return pre(r)-pre(1-1); }
                                                                                                                                                                                                                                                                                                                                      void add(T *a, int p,T d) { for(; p<=n; p+=p & -p) a[p]+=d; }</pre>
                                                                                                                                                                                                                                                                                                void ini(int _n){ fill_n(a1+1, n=_n, 0); fill_n(a2+1, n=_n, 0);
                                                                                                                                                                                                                                                                                                                                                                                                            add(a1, 1, d), add(a1, r+1, -d); add(a2, 1, d*(1-1)), add(a2, r+1, -d*r);
                                                                   // support : segment add, sum
                                                                                                                                                                                                                       static const int N =2e5+7;
                                                                                                                                                                                                                                                                                                                                                                            void add(int l,int r,T d)
                                                                                                        // !!!! : use before init()!
                                                                                                                                                                                                                                                             int n;T a1[N],a2[N];
                                                                                                                                                 template<class T>
// index : [1, n]
                                // time : nlogn
                                                                                                                                                                                       struct Fenwick{
```

3.6 IntervalMaximumChangeTimes

```
o`
                                                                                                                                                                                                                                                                                                                                       R, v, o, 0, 1, mid, 1s)
                                                                                                                                                                                                                                                                    if(ma[ls | o] < v) return o ? qry(L, R, v, o, 0, 1, mid, ls) : qry(L, R, v, o,</pre>
inline int qry(int L, int R, 11 \, \&v, int O, bool spe, int 1, int r, int rt) { if(L > R) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(o == 0 && L <= mid) ans += qry(L, R, v, o, 0, 1, mid, 1s);
if(R > mid) ans += qry(L, R, v, o, 0, mid + 1, r, rs);
if(o == 1 && L <= mid) ans += qry(L, R, v, o, 0, 1, mid, 1s);</pre>
                                                                                                                                                                                                                                                                                                                                     == 0 ? qry(L,
                                                                                                                                                                                                                                                                                                                                int ans = cnt[rt][o] - cnt[ls | o][o] + (o
                                                                                                                                                                                                                                                                                                                                                                      qry(L, R, v, o, 0, mid + 1, r, rs));
                                                                                                                                                                  if(1 == r) return v = ma[rt], 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int mid = 1 + r >> 1, ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void up(int 1, int r, int rt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ma[rt] = max(ma[ls], ma[rs])
                                                                                                                                                                                                                                                                                                                                                                                                     return \ v = ma[rt], ans;
                                                                                                    if(ma[rt] < v) return 0;
                                                                                                                                                                                                      int mid = 1 + r >> 1;
                                                                                                                                   if(L <= 1 && r <= R) {
                                                                                                                                                                                                                                        down(l, r, mid, rt);
                                                                                                                                                                                                                                                                                                      mid + 1, r, rs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         down(l, r, mid, rt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return ans;
                                                                   if(!spe) {
```

```
struct P\{T \times [D]; bool operator < (const P &c) const \{ return \times [W] < c. \times [W]; \} p[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(!k) {k=newnode(),nd[k].val=p,nd[k].son[0]=nd[k].son[1]=0,up(k);return;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, 2) if(al * nd[k].sz < nd[nd[k].son[i]].sz) o = 1;
if(o) { int cnt = 0; pia(k,cnt), k = build(1,cnt,w); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     nd[k].sz = 1; rep(i, 0, 2) nd[k].sz += nd[nd[k].son[i]].sz;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ins(p, nd[k].son[nd[k].val.x[w] < p.x[w]], (w + 1) % D);
                                                                                                                                                                                                                                                                                      struct Node{ T mi[D], ma[D]; int son[2], sz; P val; }nd[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   nd[k].mi[i] = min(nd[k].mi[i], nd[s].mi[i]);
nd[k].ma[i] = max(nd[k].ma[i], nd[s].ma[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      w=w,nth_element(p+1,p+mid,p+r+1),nd[k].val=p[mid];
                                                                                                                                                                                                                                                                                                                                                            void init() { rt = L = top = 0; } 
int newnode() { return top ? sta[top—] : ++L;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     nd[k].son[0] = build(1,mid-1, (w + 1) % D);
nd[k].son[1] = build(mid+1,r, (w + 1) % D);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 0, D) {
nd[k].m1[i]=nd[k].ma[i]=nd[k].val.x[i]}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // 抄上面这部分就好了,下面部分是视具体题目定的
// 最近点(曼哈顿距离)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(nd[k].son[0]) pia(nd[k].son[0],cnt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(nd[k].son[1]) pia(nd[k].son[1],cnt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int mid = 1 + r >> 1, k = newnode();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(o, 0, 2) if(nd[k].son[o])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             p[++cnt]=nd[k].val,sta[++top]=k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int s = nd[k].son[o];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int build(int l,int r,int w)
                                                                      const int N = 1e6 + 7, D = 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void ins(P p, int &k, int w) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void check(int &k, int w) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void pia(int k, int &cnt) {
                                                                                                                                                                                                                     int rt, L, top, W, sta[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(1 > r) return 0;
                                                                                                       const T INF = 1e9 + 7;
typedef int T; // modify
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \mathsf{up}(\mathsf{k}), \mathsf{check}(\mathsf{k},\mathsf{w});
                                                                                                                                            const db al = 0.75;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   up(k); return k;
                                                                                                                                                                                                                                                                                                                                                                                                                                        void up(int k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            bool 0 = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // O(nsqrt(n))
                                 namespace KDT
```

```
void down(int x) { if(nd[x].rev) gao(nd[x].son[0]), gao(nd[x].son[1]), nd[x].rev =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void access(int x) { for(int y = 0; x; y = x, x = nd[x].fa) splay(x), nd[x].son[1]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int 1 = id(x), r = (1 ^ 1), s = nd[x].son[r];
if(nrt(y)) nd[z].son[id(y)] = x; nd[x].son[l] = s;
                                                                                                                                                                                                                                                                                                                                                                                                                nd[x].rev ^= 1, swap(nd[x].son[0], nd[x].son[1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(nrt(y)) (id(x) \land id(y)) ? rot(x) : rot(y);
                                                                                                                                              == x \mid \mid nd[fa].son[1] == x;
                                                                                                                                                                                                                                                                                            nd[x].sum = nd[ls].sum + nd[rs].sum + nd[x].val;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void makeroot(int x) { access(x); splay(x); gao(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(s) nd[s].fa = y; nd[y].fa = x; nd[x].fa = z;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            while(\operatorname{id}[x].\operatorname{son}[0]) down(x), x = \operatorname{nd}[x].\operatorname{son}[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int id(int u) { return nd[nd[u].fa].son[1] == u;
                                                                                                                                                                                                                                                             int ls = nd[x].son[0], rs = nd[x].son[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int y = nd[x] fa, z = nd[y] fa;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for(int i = x; ; i = nd[i].fa)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            while(top) down(sta[top—]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(!nrt(i)) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void link(int x, int y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                while(nrt(x)) {
int y = nd[x].fa;
static const int N = ::N;
                                                                                                                                            return nd[fa].son[0]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        access(x); splay(x)
                                                          // if(no root) return 1
                               Node nd[N]; int sta[N];
                                                                                                                   int fa = nd[x].fa;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int findroot(int x)
                                                                                                                                                                                                                                    if(!x) return ;
                                                                                                                                                                                                                                                                                                                                                                                  if(!x) return ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void splay(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         sta[++top]
                                                                                                                                                                                                                                                                                                                                                       void gao(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 nb(y), up(x);
                                                                                   bool nrt(int \times) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int top = 0;
                                                                                                                                                                                                         void up(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void rot(int x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            splay(x);
return x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       = x' \cdot nb(x); 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // 换根
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // 找根
                                                        rep(i, 0, D) ans += max(0, p.x[i] - nd[k].ma[i]) + max(0, nd[k].mi[i] - p.x[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(d, 0, D) ans += max(sqr(nd[u].mi[d] - p.x[d]), sqr(nd[u].ma[d] - p.x[d]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ll dis = 0; rep(d, 0, D) dis += sqr(nd[u].val.x[d] - p.x[d]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, 2) if(nd[u].son[i]) qry(nd[u].son[i], ans);
                                                                                                                                                                                                         0, D) ans += abs(a.x[i] - b.x[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(all_in) { ans = max(ans, ma); return; }
                                                                                                                                                                                                                                                                                                                                                       int ls = nd[k].son[0], rs = nd[k].son[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ans.push(-dis), ans.pop();
int ls = nd[u].son[0], rs = nd[u].son[1]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(d1 > dr) swap(d1, dr), swap(ls, rs);
                                                                                                                                                                                                                                                                                                                                                                                                                                           if(d1 > dr) swap(d1, dr), swap(ls, rs);
if(d1<ans) qry(p,1s,ans);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              sqr(int \times) \{ return 111 * \times * \times; \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(dr > -ans.top()) qry(p, rs);
if(dl > -ans.top()) qry(p, ls);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(u_in) ans = max(ans, u_val);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      while(!ans.empty()) ans.pop();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(no_in || ma < ans) return;
                                                                                                                                                                                                                                                                                                                     ans=min(ans,dis(p,nd[k].val));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ll dr = rs ? Dis(p, rs) : -1;
                                                                                                                                                                                                                                                                                                                                                                                  T dl = 1s ? dis(p, 1s) : INF;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           11 d1 = 1s ? Dis(p, 1s) : -1;
                                                                                                                                                                                                                                                                                                                                                                                                                T dr = rs ? dis(p, rs) : INF;
                                                                                                                                                                                                                                                                                            void qry(P p, int k, T &ans) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 0, k) ans.push(1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(dr<ans) qry(p, rs, ans)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       void qry(int u, int &ans) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   J 矩形区域的最大值(伪代码)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              priority_queue<11> ans;
void init() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void qry(P p, int u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // 0(n \wedge (2-1/D))
                                                                                                                                                                       dis(P a, P b) {
T ans = 0; rep(i,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Dis(P p, int u) {
T dis(P p, int k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // 距离点 ロ 第 k 远
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         11 ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return ans;
                                                                                                                     return ans;
                                                                                                                                                                                                                                        return ans;
                                 T ans = 0;
                                                                                     // modify
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             LCT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     3.8
```

if(findroot(y) != x) nd[x].fa = y;

makeroot(x)

struct Node { int val, sum, fa, son[2]; bool rev; };
struct LCT {

```
if(findroot(y) != x) makeroot(y), nd[x].fa = y, add(y, x), up(y);
                                                                                                                                                                                                                                                                                                             int getAns() { access(1); splay(1); return nd[1].mxs; }
For(int y = 0; x; y = x, x = nd[x].fa) {
                                                  int &rs = nd[x].son[1];
                                                                                                                                                                                                         void link(int x, int y) {
                                                                                                    if(rs) add(x, rs);
                                                                          if(y) del(x, y);
                                                                                                                              rs = y, up(x);
                              splay(x);
                                                                                                                                                                                                                                       makeroot(x);
                                                                            if(findroot(y) == x \& nd[y].fa == x \& ind[y].son[0]) nd[y].fa = nd[x].son[1]
                                                                                                                                                                                void path(int x, int y) { makeroot(x); access(y); splay(y);
                                                                                                                                                                                                                                     void upd(int x, int c) { splay(x); nd[x].val = c; up(x); }
                        void cut(int x, int y) {
                                                                                                                                                                                                                                                                                                                 diameter
                                                                                                                                }
// nd[y]: 路径信息
                                                      makeroot(x);
                                                                                                        0, up(x);
                                                                                                                                                                                                           // 单点修改
                                                                                                                                                                                                                                                                                                               \GammaCT
  / 黒法
                                                                                                                                                                                                                                                                                                                 3.9
```

3.10 PerTrie

int sec(multiset<int> st) { return sz(st) > 1 ? *(++st.rbegin()) : 0; }

void Era(multiset<int> &s, int x) { s.erase(s.find(x)); }

int fir(multiset<int> st) { return sz(st) ? *(st.rbegin()) : 0;

}lct;

```
per(i, 0, M) {
   int c = val >> i & 1;
                                                                                                                                                                                                                                                                           ne[now][1] = ne[pre][1];
                                                                                                                                                                                                                                                                                                                  cnt[now] = cnt[pre] + 1;
                                                                                                                                                                                                                                                  ne[now][0] = ne[pre][0]
                                                                                                                                                                                                                                                                                                                                                                                                                int c = val >> dep & 1;
                                                                                                                                            // 将当前数的信息存在叶子
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          using namespace __gnu_cxx;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rp.insert(cur, 字符数组 );
                                                                                                             void init() { L = 0; }
                                                                                                                                                                                                                                                                                                                                                   ed[now] = ed[pre];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rp.erase(cur, len);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         #include <ext/rope>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return ed[R];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rp.push_back(ch);
                                                                                                                                                                                                                   now = ++L;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          Rope
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ropecchar> rp;
               struct Trie {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          3.11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     }ac;
                                                                                                                                                              void del(int x, int y) { Era(nd[x].chain, nd[y].lmx), Era(nd[x].path, nd[y].mxs); }
void add(int x, int y) { nd[x].chain.insert(nd[y].lmx), nd[x].path.insert(nd[y].mxs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Ma(nd[p].mxs, nd[ls].rmx + R); // 经过 p 父边的答案
Ma(nd[p].mxs, nd[rs].lmx + L); // 经过 u 向下实边的答案
Ma(nd[p].mxs, cha + sec(nd[p].chain) + (p > n)); // 處子树中到根路径最长的两条拼起来
struct Node { int fa, son[2], lmx, rmx, mxs, sum; bool rev; multiset<int> chain, path;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    nd[p].lmx = max(nd[ls].lmx, nd[ls].sum + R); // 从链顶出发的最远距离nd[p].rmx = max(nd[rs].rmx, nd[rs].sum + L); // 从链底出发的最远距离nd[p].mxs = max(nd[ls].mxs, nd[rs].mxs); // mxs[p] 表示当前范围的直径
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               nd[p] .sum = nd[1s] .sum + nd[rs] .sum + (p > n); // 当前链的长度 int cha = fir(nd[p] .chain); // 从 p 沿處儿子走的最远距离 int L = max(cha, nd[1s].rmx) + (p > n); // 从 p 沿父亲走的最远距离 int R = max(cha, nd[rs].lmx) + (p > n); // 从 p 沿突光上的最远距离
                                                                                                                                                                                                                                                                                                  rep(i, 1, n + m + 1) {
    nd[i].fa = nd[i].son[0] = nd[i].son[1] = nd[i].rev = 0;
    nd[i].lmx = nd[i].rmx = nd[i].mxs = nd[i].sum = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    \inf p = x, Is = nd[x].son[0], rs = nd[x].son[1]; // 以下考虑的都是链 p 与链 p 的所有虚子树
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Ma(nd[p].mxs, fir(nd[p].path)); // 虚子树的直径
                                                                                                                                                                                                                                                                                                                                                                                                 nd[i].chain.clear(), nd[i].path.clear(),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      swap(nd[x].son[0], nd[x].son[1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          swap(nd[x].lmx, nd[x].rmx);
                                                                                              static const int N = 30303;
                                                                                                                                  Node nd[N]; int sta[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(!x) return ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void access(int \times)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(!x) return ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          nd[x].rev ^{-1}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void gao(int \times) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void up(int \times) {
                                                                                                                                                                                                                                                               void init() {
                                                             struct LCT {
```

```
#include <ext/rope>
using namespace __gnu_cxx;
rope<br/>cchar> rp;
rp.bush_back(ch);
rp.insert(cur, 字符数组 ); // 在 cur 处插入字符<br/>rp.erase(cur, 1en);
// 刪除 cur 开始的 len 个字符<br/>rp.replace(cur, 字符数组 ); // 刪除 cur 处的字符, 换成字符数组<br/>rp.copy(cur, len, 字符数组 ); // 复制 cur 处开始的 len 个字符到字符数组
```

```
if(L > R) return ;
if(L <= 1 && r <= R && c < mi[rt][1]) return gao(rt, c), void();</pre>
                                                                                                                                                                                                                                                            void down(int rt) { gao(ls, mi[rt][0]); gao(rs, mi[rt][0]); }
void upd(int L, int R, int c, int l, int r, int rt) {
                                                                            build(1, mid, 1s); build(mid + 1, r, rs); up(rt);
                                                                                                                                                                                 sum[rt] += 111 * cnt[rt] * (c - mi[rt][0]);
                                                                                                                                                                                                                                                                                                                                                                                             if(L <= mid) upd(L, R, c, l, mid, ls);
if(R > mid) upd(L, R, c, mid + 1, r, rs);
                                                                                                                                                                                                                                                                                                                                                                       int mid = 1 + r >> 1; down(rt);
                                                                                                                                                           if(c <= mi[rt][0]) return ;</pre>
                                                  int mid = 1 + r >> 1;
                                                                                                                               void gao(int rt, int c)
                                                                                                                                                                                                             mi[rt][0] = c;
    return ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                     up(rt);
// 取第 cur 个字符
// 取第 cur 个字符
// 提取从 cur 处开始的 1en 个字符
// 可持久化, 0(1),直接拷贝根节点
                                                                                                                                                                                                                                                                    ^
                                                                                                                                                     * 1. 维护一正一反两个 rope
* 2. 翻转等价于交换两个子串
* 二)区间循环位移
* 1. 拆成多个子串, 重新安排它们的位置
* 三)区间 a -> b, b -> c, c -> d ....
* 1. 维护 26 个 rope
                                                      rp.substr(cur, len);
                                                                          rp[i] = rp[i - 1];
                                                                                                                                 * 一)翻转操作
```

 \mathbf{S}

3.12

rp.at(cur);

rp[cur];

Splay

```
struct Node { int val, fa, son[2], cnt, sz; bool rev; };
                                                                                                                                                                                                                                         // if go to vertex p, must splay(p)
                                                                                                                                                                                                               // id starts from 1
                                                                                                                                                                                                                                                                                                    struct Splay {
                                                                                                                                                                                       // init
                                                                                                                     3.14
                                                                   }sed;
                                                                                                                                   rep(i, 2, n + 1) lg[i] = lg[i >> 1] + 1;
rep(i, 0, n) a[0][i] = v[i];
rep(i, 1, lg[n] + 1) rep(j, 0, n - (1 << i) + 1) {
a[i][j] = max(a[i - 1][j], a[i - 1][j + (1 << i >> 1)]);
                                                                                                                                                                                                                                                                                                                                                                                              return max(a[i][1], a[i][r + 1 - (1 << i)]);
                                                      static const int N = 101010;
                                                                                int a[20][N], lg[N];
void build(int *v, int n){
                                                                                                                                                                                                                                                                                                                                       if(1 > r) swap(1, r);
int i = lg[r - 1 + 1];
                                                                                                                                                                                                                                                                                                             int qry(int 1, int r){
                          struct ST{
// [0,n)
```

SegIntervalMax 3.13

```
if(mi[rt][0] == mi[ls | i][0]) cnt[rt] += cnt[ls | i];
                                                                                                                                                                                rep(i, 0, 2) mi[rt][i] = min(mi[1s][i], mi[rs][i]);
cnt[rt] = 0;
rep(i, 0, 2) {
                                                                                                                                                                                                                                                                                      else mi[rt][1] = min(mi[rt][1], mi[ls | i][0]);
                                                                                                                                                                                                                                                                                                                                                                                                   if(1 == r) {
    sum[rt] = mi[rt][0] = a[1]; //modify
    mi[rt][1] = inf; cnt[rt] = 1;
                                                                                                                                                                                                                                                                                                                                                                      void build(int l, int r, int rt) {
                                                                                                      11 sum[N]; int mi[N][2], cnt[N];
                                                                                                                                                       sum[rt] = sum[ls] + sum[rs];
                                                                         static const int N = ::N << 2;
                    区间求和
                                                                                                                                   void up(int rt) {
                      // 区间取 max,
                                                 struct Seg {
// 0(nlogn)
```

if(nd[u].rev) gao(nd[u].son[0]), gao(nd[u].son[1]), nd[u].rev = 0;

void down(int u)

int id(int u) { return nd[nd[u].fa].son[1] == u; nd[u].sz = nd[1s].sz + nd[rs].sz + nd[u].cnt;

void rot(int x)

int ls = nd[u].son[0], rs = nd[u].son[1];

if(!u) return ;

void up(int u) {

int y = nd[x].fa, z = nd[y].fa;
int l = id(x), r = (1 ^ 1), s = nd[x].son[r];

nd[u].rev ^= 1, swap(nd[u].son[@], nd[u].son[1]);

void init(int n) { rt = L = 0;

eturn L;

void gao(int u) {

if(!u) return

nd[L].son[0] = nd[L].son[1] = nd[L].rev = 0; nd[L].cnt = nd[L].sz = 1;

6

= 0, int 0 =

int newnode(int c, int fa static const int N = ::N;

nd[fa].son[o] = L;nd[++L].fa = fa;

nd[L].val = c;

int rt, L; Node nd[N];

```
if(nd[x].r < nd[y].r) \ \{ down(x), nd[x].rs = merge(nd[x].rs, y), up(x); return x \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(\min(nd[rt].getf(v[1]), nd[rt].getf(v[r])) >= \max(k.getf(v[1]), k.getf(v[r])))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(max(mi[rt].getf(v[1]), mi[rt].getf(v[r])) <= min(k.getf(v[1]), k.getf(v[r])))</pre>
                                                                                                                                                                                                                                                                                                                               else { down(y), nd[y].ls = merge(x, nd[y].ls), up(y); return y;
                                                         if(sz < k) \times = u, splitk(nd[u].rs, k - sz - 1, nd[u].rs, y); else y = u, splitk(nd[u].ls, k, x, nd[u].ls);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(k.getf(v[mid]) > nd[rt].getf(v[mid])) swap(k, nd[rt]);
if(1 == r) return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(k.getf(v[mid]) < mi[rt].getf(v[mid])) swap(k, mi[rt]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void upd(int L, int R, Node c, int l, int r, int rt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Node nd[N], mi[N]; // nd: max val; mi: min val; void _upd(Node k, int l, int r, int rt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(mi[rt].k \le k.k)_min(k, l, mid, ls);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(nd[rt].k > k.k) _upd(k, l, mid, ls);
else _upd(k, mid + 1, r, rs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        o;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(L <= mid) upd(L, R, c, l, mid, ls);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void _min(Node k, int l, int r, int rt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Node(11 k, 11 b) : k(k), b(b) {}
11 getf(int x) const { return k * x +
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        else _min(k, mid + 1, r, rs);
  down(u);
int sz = nd[nd[u].ls].sz;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              static const int N = ::N << 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(L > R) return ;
if(L <= 1 && r <= R) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         _upd(c, l, r, rt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  _min(c, 1, r, rt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int mid = 1 + r >> 1;
                                                                                                                                                                                                            int merge(int x, int y) {
                                                                                                                                                                                                                                                                                                                                                             } else return x + y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        Node(): k(0), b(0) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(1 == r) return
                                                                                                                                                     else x = y = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                lcSegTree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return ;
                                                                                                                                                                                                                                        if(x && y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return ;
                                                                                                                         (n)dn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 struct Node {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             struct Seg {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               11 k, b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   3.16
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // init
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void down(int x) { if(nd[x].rev) gao(nd[x].ls), gao(nd[x].rs), nd[x].rev = 0; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int rt, L; Node nd[N];
void init() { rt = L = 0; srand(time(0)); }
11 Rand() { return ((rand() * 111 << 32) ^ (rand() * 111 << 16) ^ rand()); }</pre>
if(z) nd[z].son[id(y)] = x; nd[x].son[r] = y; nd[y].son[1] = s;
if(s) nd[s].fa = y; nd[y].fa = x; nd[x].fa = z;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(nd[u].val \le c) \times = u, splitc(nd[u].rs, c, nd[u].rs, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            struct Node { int val, cnt, sz, ls, rs; ll r; bool rev;};
                                                                                                                                                                                                        if(z != g) (id(x) ^ id(y)) ? rot(x) : rot(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             else y = u, splitc(nd[u].ls, c, x, nd[u].ls);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               nd[x].sz = nd[ls].sz + nd[rs].sz + nd[x].cnt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     nd[x].rev ^= 1, swap(nd[x].ls, nd[x].rs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void splitc(int u, int c, int &x, int &y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            void splitk(int u, int k, int &x, int &y) {
  if(u) {
                                                                                                                                                                              int y = nd[x].fa, z = nd[y].fa;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                nd[L].1s = nd[L].rs = nd[L].rev =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int ls = nd[x].ls, rs = nd[x].rs;
                                                                                                                     void splay(int x, int g = 0) {
  while(nd[x].fa != g) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                nd[L].cnt = nd[L].sz = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          struct fhqTreap {
   static const int N = ::N;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // u -> (1 - k) (k+1 - L)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              nd[++L].r = Rand();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // !!!: nd[].cnt == 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int newnode(int c) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 (2 <) (2 =>) <- n //
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           } else \times = y = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(!x) return ;
                                                                                                                                                                                                                                                                                                                                                                                                                       fhqTreap
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // 不要修改 の 节点的值
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         nd[L].val = c;
                                                                                                                                                                                                                                                                                                    if(!g) rt = x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void gao(int \times) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(!x) return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // id starts from 1
                                                                (x)), up(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void up(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      down(u);
                                                                                                                                                                                                                                          rot(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return L;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (n)dn
                                                                                                                                                                                                                                                                                                                                                                                                                         3.15
```

```
else { y = newcopy(y), down(y), nd[y].ls = merge(x, nd[y].ls), up(y); return y;
                                                                                                                                                                                                                                                                                                                                                                                       if(nd[x].r < nd[y].r) { x = newcopy(x), down(x), nd[x].rs = merge(nd[x].rs, y), up(x); return x; }
                                                                      \begin{array}{l} \textbf{int} \ sz = nd[nd[u].ls].sz; \\ \textbf{if}(sz < k) \ \times = u, \ splitk(nd[u].rs, \ k-sz-1, \ nd[u].rs, \ y); \end{array} 
                                                                                                                                          else y = u, splitk(nd[u].ls, k, x, nd[u].ls);
                                                                                                                                                                                                                                                                                      // sometimes do not need to newcopy
                                   u = newcopy(u), down(u);
                                                                                                                                                                                                                                                                                                                          int merge(int x, int y) {
                                                                                                                                                                                                                    } else x = y = 0;
                                                                                                                                                                                                                                                                                                                                                                 if(× && y) {
                                                               il qry(int p, int l, int r, int rt) {
    ll ans = max(abs(nd[rt].getf(v[p])), abs(mi[rt].getf(v[p])));
                                                                                                                                                                                                               if(p \le mid) ans = max(ans, qry(p, 1, mid, 1s));
                                                                                                                                                                                                                                                        else ans = max(ans, qry(p, mid + 1, r, rs));
  rs);
if(R > mid) upd(L, R, c, mid + 1, r,
                                                                                                                                            if(1 == r) return ans;
                                                                                                                                                                              int mid = 1 + r >> 1
                                                                                                                                                                                                                                                                                                                                                                                                                                   perTreap
                                                                                                                                                                                                                                                                                         return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                   3.17
                                                                                                                                                                                                                                                                                                                                                                 }sed:
```

3.18 **动态** dp_bst

struct Node { int val, cnt, sz, ls, rs; ll r, sum; bool rev; };

// 不要修改 の 节点的值

// id starts from 1

static const int N = 3e7;

struct fhqTreap {

} else return $\times + y$;

```
int n, m, a[N], sz[N], wson[N], f[N][2], h[N][2];
int to[N << 1], ne[N << 1], hd[N], _;
inline void ae(int u, int v) { to[++_] = v, ne[_] = hd[u], hd[u] = _; }</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, l, r + 1) tot += sz[sta[i]] – sz[wson[sta[i]]];
rep(i, l, r + 1) {
                                                                                                                                                                                     for(int i = hd[u]; i; i = ne[i]) if(to[i] i = fa) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(son[x][0]) sum[x] = sum[son[x][0]] * sum[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(son[x][1])    sum[x] = sum[x] * sum[son[x][1]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           now += sz[sta[i]] — sz[wson[sta[i]]],
                                                                                                                                                                                                                                                                                                                                          (sz[v] > sz[wson[u]]) && (wson[u] = v)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ċ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int fa[N], son[N][2], rt, sta[N], top,
inline void up(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 inline int sbuild(int 1, int r)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if((now << 1) >= tot) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int tot = 0, now = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int \times = sta[i];
                                                                                                                          void dfs(int u, int fa) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(1 > r) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              sum[x] = val[x];
                                                                                                                                                                                                                                                                                                           sz[u] += sz[v];
                                                                                                                                                                                                                 int v = to[i];
                                                                                                                                                                                                                                                                                                                                                                                                       int s = wson[u];
                                                                                                                                                                                                                                                                                 // nbd f[u]
                                                                                                                                                                                                                                                                                                                                                                                                                                   // h[u] = f[u]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   [n]y pdn //
                                                                                                                                                                                                                                                  dfs(v, u);
                                                                                                                                                           sz[u] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(s)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void down(int x) { if(nd[x].rev) gao(nd[x].ls), gao(nd[x].rs), nd[x].rev = 0; }
int rt[::N], L; Node nd[N];
void init() { fill_n(rt, L + 1, 0); L = 0; srand(time(0)); }
11 Rand() { return ((rand() * 111 << 32) ^ (rand() * 111 << 16) ^ rand()); }</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(nd[u].val \le c) \times u, splitc(nd[u].rs, c, nd[u].rs, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     else y = u, splitc(nd[u].ls, c, x, nd[u].ls);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                nd[x].sum = nd[ls].sum + nd[rs].sum + nd[x].val;
                                                                                                                                                                                                                                                                                                                int newcopy(int x) { nd[++L] = nd[x]; return L; }
                                                                                                                                                                                                                                                                                                                                                                                                                                   nd[x].sz = nd[ls].sz + nd[rs].sz + nd[x].cnt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       nd[x].rev \land = 1, swap(nd[x].ls, nd[x].rs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void splitk(int u, int k, int &x, int &y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void splitc(int u, int c, int &x, int &y)
                                                                                                                                                                                                                      0
                                                                                                                                                                                                                 nd[L].1s = nd[L].rs = nd[L].rev =
                                                                                                                                                                                                                                                                                                                                                                                                       int ls = nd[x].ls, rs = nd[x].rs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     u = newcopy(u), down(u);
                                                                                                                                                    nd[L].val = nd[L].sum = c;
                                                                                                                                                                                     nd[L].cnt = nd[L].sz = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // u \rightarrow (1 - k) (k+1 - L)
                                                                                                                            nd[++L].r = Rand();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // !!!: nd[].cnt == 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              (c < c) (c = c) < c / (c < c)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                } else x = y = 0;
                                                                                                int newnode(int c) 
                                                                                                                                                                                                                                                                                                                                                                           if(!x) return ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void gao(int \&x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             x = newcopy(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(!x) return
                                                                                                                                                                                                                                                                                                                                              void up(int \times) \{
                                                                                                                                                                                                                                                     return L;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ;(n)dn
```

```
Fuzhou University
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int sz[N], wson[N], top[N], dep[N], id[N], _, par[N], who[N], leaf[N];
11 f[N][2], F[N][2];
struct Mat {
                                                                                                                                                                                                                                                                 access(x); splay(x); nd[x].val.a[1][0] += y - a[x];
                                                                                                                                                                                                                                                                                                        return max(nd[x].sum.a[0][0], nd[x].sum.a[1][0]);
                        for(int y = 0; x; y = x, x = nd[x].fa) {
                                                                                                                                                                                                                                             inline int upd(int x, int y) {
                                                                                                                                                                                   nd[x].son[1] = y; up(x);
       inline void access(int \times) {
                                                                                                                                                                                                                                                                                                                                                                                                       对态 dp 对链剖分
                                            splay(x);
if(nd[x].son[1]) {
// upd val[x]
                                                                                                                                             // upd val[x]
                                                                                                                                                                                                                                                                                    up(x); a[x] = y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                     int n, a[N]; vi g[N];
namespace DP {
                                                                                                                         if(y) {
                                                                                                                                                                                                                                                                                                                                                 }lct;
                                                                                                                                                                                                                                                                                                                                                                                                        3.20
                                                                                                                                                                                   for(int u = tp; u; f = u, u = wson[u]) {
  for(int i = hd[u]; i; i = ne[i]) if(to[i] != f && to[i] != wson[u]) {
    fa[build(to[i], u)] = u;
}
```

fa[son[x][0]] = fa[son[x][1]] = x;

return x;

(x)dn

int build(int tp, int f) {

// upd val[u]

son[x][0] = sbuild(1, i - 1); son[x][1] = sbuild(i + 1, r);

```
inline void e() { rep(i, 0, 3) rep(j, 0, 3) a[i][j] = (i != j) * (-inf); }
                                                                                                                                                                                                                                                                                                                                                                           rep(k, 1, 3) r.a[i][j] = max(r.a[i][j], a[i][k] + c.a[k][j]);
                                                                                                                                                                                                                                                                                                       inline Mat operator * (const Mat &c) const
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       inline void build(int 1, int r, int rt) {
                                                                                                                                                                                                                                                                                                                            Mat r; rep(i, 0, 3) rep(j, 0, 3) {
    r.a[i][j] = a[i][0] + c.a[0][j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int u = who[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // set m[rt]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // calc F, f
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(1 == r) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return ;
                                                                                                                                                                                                                                                                                                                                                                                                  } return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Mat m[N << 2];
                                                                                                                                                                                                                                                                                  11 a[3][3];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         struct Seg {
                                                                                                          n = _n; rt = build(1, 0);
rep(i, 1, n + 1) isr[i] = (son[fa[i]][0] != i && son[fa[i]][1] != i);
                     for(int u = tp; u; u = wson[u]) sta[++top] = u;
                                                                                                                                                                                                                                                                                                                                                // u = fa[x], get h[u], val[u]
                                                                                                                                                                                inline int upd(int x, int y) {
// upd h[x], a[x] = y, val[x]
                                                                                                                                                                                                                                                   if(isr[x] && fa[x]) {
    // get old f[x]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // get dp[1] by sum[rt]
                                          return sbuild(1, top);
                                                                                                                                                                                                                                                                                                                   // get new f[x]
                                                                                       void build(int _n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                         x = fa[x];
                                                                                                                                                                                                                                                                                                     (x)dn
                                                                                                                                                                                                                                                                                                                                                                                            (x)dn
                                                                                                                                                                                                                                                                                                                                                                     else {
                                                                                                                                                                                                                                while(x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  dfs(1, 0);
bst.build(n);
top = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void init() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      }bst;
```

动态 dp_lct 3.19

int mid = 1 + r >> 1; build(mid + 1, r, rs); build(1, mid, ls);

m[rt] = m[ls] * m[rs];

inline void upd(int u, int l, int r, int rt) {

// set m[rt]

return ;

if(1 == r) {

(id[u] <= mid) ? upd(u, l, mid, ls) : upd(u, mid + 1, r, rs);

int mid = 1 + r >> 1;

```
if(ls) nd[x].sum = nd[ls].sum * nd[x].sum;
                                                                                                                                                                                     if(rs) nd[x].sum = nd[x].sum * nd[rs].sum;
                                                   struct Node { int fa, son[2]; Mat val, sum; };
                                                                                                                                nd[x].sum = nd[x].val;
                                                                                                inline void up(int x) {
int n, m, a[N], f[N][2];
namespace DP {
                                                                               struct LCT {
```

```
void upd(int L, int R, 11 c, int 1 = 1, int r = n, int rt = 1) sum[rt] += c * (min(R, r) - max(L, 1) + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                  if(L <= 1 && r <= R) return la[rt] += c, void();</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ll ans = la[rt] * (min(R, r) - max(L, l) + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(L <= mid) ans += qry(L, R, 1, mid, 1s);
if(R > mid) ans += qry(L, R, mid + 1, r, rs);
                                  int mid = 1 + r >> 1;
build(1, mid, 1s); build(mid + 1, r, rs);
                                                                                                                                                                                                                                                                                                               if(L <= mid) upd(L, R, c, l, mid, ls);
if(R > mid) upd(L, R, c, mid + 1, r, rs);
if(1 == r) return sum[rt] = a[1], void();
                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(L <= 1 && r <= R) return sum[rt];</pre>
                                                                                                   sum[rt] = sum[ls] + sum[rs]
                                                                                                                                                                                                                                                                            int mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         }sed;
                                                                   inline void qry(int L, int R, int l, int r, int rt, Mat &ans) {
   if(rt == 1) ans.e();
```

// if(s) top[s] = top[c], dfs2(s, c, g), leaf[c] = leaf[s],

// else leaf[c] = c;

struct HeavyChain{

inline pair<11, 11> qry(int x) {
 Mat tmp; seg.qry(id[x], id[leaf[x]], 1, n, 1, tmp);
 11 f0 = max(tmp.a[0][0], tmp.a[0][1], tmp.a[0][2]); 11 f1 = max(tmp.a[1][0], tmp.a[1][1], tmp.a[1][2]);

F[p][1] += c - a[p], a[p] = c;

int v = p;

void upd(int p, int c) {

return mp(f0, f1);

 $if(L \le 1 \& R r \le R) return$ ans = ans * m[rt], void(),

int mid = 1 + r >> 1;

m[rt] = m[ls] * m[rs];

if(L <= mid) qry(L, R, l, mid, ls, ans);
if(R > mid) qry(L, R, mid + 1, r, rs, ans);

线段树优化建图 3.23

```
#define ls (rt << 1)
                                                              #define rs (ls | 1)
                             struct SegGraph {
                                                                                                                                        f[u][0] = _f.fi, f[u][1] = _f.se, v = fa;
while(v) {
  int u = top[v], fa = par[u];
                                                          pair<ll, ll> _f = qry(u);
                                         seg.upd(v, 1, n, 1);
                                                                                                                                                                                                                                        seg.build(1, n, 1);
                                                                                                  // upd F[fa]
                                                                                                                                                                                                                      hc.Build(g);
                                                                                 if(fa) {
                                                                                                                                                                                                     void work() {
```

```
void build(int \bar{1} = 1, int r = n, int rt = 1) {
                         struct Seg {
    static const int N = ::N << 2;</pre>
                                                                           11 sum[N], la[N];
                                                                                                                                 la[rt] = 0;
int n; ll a[N];
```

```
void link(int l, int r, int rt, int L, int R, int w, int o) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void link(int li, int ri, int l2, int r2, int w, int n) {
                                                                                                                                                                                                               t[0] = ++tim, t[1] = ++tim, liu(t[0], t[1], 0);
if (rt / 2) liu(fa[0], t[0], 0), liu(t[1], fa[1], 0);
if (l == r) { p[1] = t[0]; return; }
build(l, mid, ls); build(mid+1, r, rs);
                                                          vectorpii> g[M];
void init() { rep(i, 0, tim+1) g[i].clear(); tim = 0; }
void liu(int u, int v, int w) { g[u].pb(mp(v, w)); }
void build(int l, int r, int rt) {
   int *t = id[rt], *fa = id[rt / 2], mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (R > mid) link(mid+1, r, rs, L, R, w, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (L <= mid) link(l, mid, ls, L, R, w, 0);</pre>
static const int N = :: N \ll 2, M = N + Q;
                                                                                                                                                                                                                                                                                                                                                                                                              int *t = id[rt], mid = 1 + r >> 1;
if (L <= 1 && R >= r) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // [11, r1] \rightarrow [12, r2] weight = w
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (0) liu(t[0], tim, w);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    link(1, n, 1, 12, r2, 0, 0);
link(1, n, 1, 11, r1, w, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             else liu(tim, t[o], w);
                               int id[N][2], p[::N], tim;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            top
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     * 单点修改,区间查询 -> 单点修改,前缀查询 -> 后缀修改,单点查询
* 树剖路径问题:重链区间修改,轻边暴力维护。轻边深度小的点一定在重链上,深度大的一定是
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         区回加区回水型
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         标记不下传
                                                                                                                                                                                                                                                                                                                                                                            常见转化
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           3.22
                                                                                                                                                                                                                                                                                                                                                                                3.21
```

```
len[0][rt] = (1 == r) ? 0 : len[0][ls] + len[0][rs]; len[1][rt] = (1 == r) ? 0 : len[1][ls] + len[1][rs];
                                                                                                                                                                                                                                                                                                              len[1][rt] = (1 == r) ? 0 : len[0][ls] + len[0][rs];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void upd(int L, int R, int c, int l, int r, int rt) {
覆盖大于 k 次的矩形面积
                                                                                                                                                               void up(int rt, int 1, int r) {
                                                                                                            static const int N = ::N << 2;
                                                                                                                                                                                                           len[0][rt] = r - 1 + 1; len[1][rt] = r - 1 + 1;
                                                                                                                                                                                                                                                                                         len[0][rt] = r - 1 + 1;
                                                                                                                                                                                                                                                              else_if(la[rt] >= 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(L <= 1 && r <= R) {
                                                            // 这里是覆盖次数大于 1 次的
                                                                                                                                   int la[N], len[2][N];
                                                                                                                                                                                      if(la[rt] >= 2) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         up(rt, 1, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      la[rt] += c;
                                                                                                                                                                                                                                                                                                                                             } else ·
                                                                                   struct Seg {
 3.24
```

} };

Game

Nim 积 4.1

if(L <= mid) upd(L, R, c, 1, mid, 1s);
if(R > mid) upd(L, R, c, mid + 1, r, rs);

up(rt, 1, r);

int mid = 1 + r >> 1;

return ;

const int N = :: N, M = Sqrt(N) + 5, K = 7;

int n, k, B, pos[K][N];

bitset<N> s[K][M];

vectorpii> V[K];
struct node { int d[K]; } a[N];
void init(int _n, int _k) {

n = _n; k = _k;

// 如果有 02 比较快, 不然可能比较慢要手写 bitset

namespace PX{

高维偏序

3.25

}seg;

```
while (x < (1 << (1 << a)) || x >= (1 << (1 << (a + 1)))) a++; int m = 1 << (1 << (a + 1))) a++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        while (x < (1 << a)) || x >= (1 << (1 << (a + 1)))) a++;
int m = 1 << (1 << a), p = x / m, q = x%m, s = y / m, t = y%m;
int c1 = Mul(p, s), c2 = Mul(p, t) ^ Mul(q, s), c3 = Mul(q, t);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return (m*(c1^c2)) ^ c3^nimPow(m / 2, c1);
                                                                                                                                                                                                                                                               int d1 = nimPow(p, s), d2 = nimPow(p, t);
                                                                                                                                                                                                                                                                                                       return (m^*(d1^{\wedge}d2)) \wedge nimPow(m / 2, d1);
                                                                                                                                                                                                                                                                                                                                                                                                             if (x < y) return Mul(y, x);
if (x < 2) return x & y; int a = 0;</pre>
                                                                                                                                                      if (x < 2) return x &   y ; int a = 0;
                                                                                                                 int nimPow(int x, int y) {
                                                                                                                                                                                                                                                                                                                                                                                int Mul(int x, int y) {
* 注: 高维硬币游戏
                                                                                 namespace Nim {
```

SurNum 4.2

```
11 x, k; inf op;
SurNum() { x = k = op = 0; }
SurNum(11 x, 11 k, 11 op = 0) :x(x), k(k), op(op) { }
SurNum(const SurNum &a) { *this = a; }
inline SurNum Simplify() {
                                                                                                        int sgn(11 \times) { return !x ? 0 : (x > 0 ? 1 : -1);
                                                                                                                                              struct SurNum {
                                                                                                                                         a[i].d[j] = lower_bound(all(V[j]), mp(a[i].d[j], i)) - V[j].begin();
rep(i, 1, n+1) rep(j, 0, k) cin >> a[i].d[j];
rep(i, 1, n+1) rep(j, 0, k) V[j].pb(mp(a[i].d[j], i));
rep(j, 0, k) sort(all(V[j]));
rep(j, 1, n+1) rep(j, 0, k) {
                                                                                                                                                                                                                                                                                                                       bitset<N> tmp; int id = 1;
                                                                                                                                                                         pos[j][a[i].d[j]] = i;
                                                                                                                                                                                                                                                                                  rep(j, 0, k) {
                                                                                                                                                                                                                                                    = sqrt(n);
```

```
rep(j, 0, k) {
   int ed = lower_bound(all(V[j]), mp(V[j][a.d[j]].fi, n+1)) - V[j].begin() - 1;
                                                                                                                                                                                                                                                                                                                           bitset<N> tmp;int id = ed / B, st = id ? (id - 1) * B : 0;
                                                              if (i == id * B - 1) s[j][id++] = tmp;
                                                                                                                                                                                                                                                                                                                                                                                            rep(i, st, ed+1) tmp[pos[j][i]] = 1;
                                                                                                                                                                                                                                                                                                                                                         if (id) tmp = s[j][id - 1];
                                tmp.set(pos[j][i]);
                                                                                                                                                                                                                                 bitset<N> ans; ans.set();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return ans.count();
rep(i, 0, n) {
                                                                                                                                                                                                int qry(node a) {
                                                                                                                                                                                                                                                                                                                                                                                                                            ans &= tmp;
```

```
while (op = getDir(S, a, b)) S = ((op == 1) ? S.goRight() : S.goLeft());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Η,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              SurNum y; if (x.x \le 0 \& x.k == 0) y = x, y.x—; else y = p + x >>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (x, x) >= 0 \& x, k == 0 y = x, y, x++; else y = x + q >>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \Leftrightarrow
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              SurTri(SurNum p, SurNum x, SurNum q) :p(p), x(x), q(q) SurTri(const SurTri &a) { *this = a; }
friend inline SurNum operator -= (SurNum &a, SurNum b)
                                                                                    Ş
                                                                                                                                                                    friend inline SurNum getMid(SurNum a, SurNum b)
                                                                                                                                                                                                                                                                                                           if (op == 1) { printf("+inf\n"); return; }
                                                                                                                                                                                                                                                                                                                                       if (op == -1) { printf("-inf\n"); return;
                                                                                  friend inline SurNum operator >> (SurNum a,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int getDir(SurTri Š, SurNum a, SurNum b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return SurNum(a1, a2, a3).Simplify();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    &a1, &a2, &a3);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (a <= S.x && b <= S.x) return -1;
if (a >= S.x && b >= S.x) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (a < S.x && S.x < b) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              SurNum getValue(SurNum a, SurNum b)
                                                                                                                                                                                                                                                                                                                                                                   printf("%lld/%lld\n'', x, 1 << k),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 p.print(), x.print(), q.print();
                                                                                                              return a.k += k, a.Simplify();
                                                                                                                                                                                                                                                                                                                                                                                                                         inline static SurNum read() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    printf("\n\nSurTri:\n\n");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  SurTri S(—_inf, _0, _inf);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             SurNum p, x, q;
SurTri() { p = x = q = \_0; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    _0(0, 0, 0), _inf(0, 0, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return SurTri(p, y, x);
                                                                                                                                                                                                                                                     inline void print() const
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return SurTri(x, y, q);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    scanf("%11d%11d%11d",
                                                                                                                                                                                                                                                                                   printf("SurNum:\n");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           printf("\nend\n\n");
                                                                                                                                                                                              return a + b \gg 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               struct SurCalculator {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       SurTri goRight() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             SurTri goLeft() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                        11 a1, a2, a3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void print() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return S.x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            assert(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              struct SurTri {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   SurNum y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int op;
```

```
friend inline bool operator >= (const SurNum &a, const SurNum &b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       friend inline bool operator == (const SurNum &a, const SurNum &b) return compare(a, b) == \theta;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          friend inline bool operator <= (const SurNum &a, const SurNum &b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              &b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    friend inline bool operator < (const SurNum &a, const SurNum &b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   friend inline bool operator > (const SurNum &a, const SurNum &b)
return compare(a, b) == 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              const SurNum
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              grow(a, b); return SurNum(a.x + b.x, a.k, 0).Simplify();
                                                                                            friend inline int sgn(const SurNum &a) { return sgn(a.x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if (a.op == -1 || b.op == -1) return SurNum(0, 0, -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               friend inline SurNum operator += (SurNum &a, SurNum b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               friend inline SurNum operator + (SurNum a, SurNum b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (a.op == 1 || b.op == 1) return SurNum(0, 0, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   SurNum b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           friend inline SurNum operator — (const SurNum &a)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         friend inline bool operator != (const SurNum &a,
                                                                                                                                                                                                                                                                                                                                friend inline void grow(SurNum &a, SurNum &b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                   friend inline int compare(SurNum a, SurNum b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      – (SurNum a,
while (x \% 2 == 0 \&\& k > 0) \times /= 2,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return SurNum(—a.x, a.k, —a.op)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int opa = sgn(a), opb = sgn(b);
if (opa < opb) return -1;
if (opa > opb) return 1;
                                                                                                                                                                                                                                 ⊩ KK;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (a.op < b.op) return -1;
if (a.op > b.op) return 1;
if (a.op != 0) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              friend inline SurNum operator
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return compare(a, b) ==-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return compare(a, b) <= 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return compare(a, b) i = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return compare(a, b) >= 0;
                                                                                                                                                            Simplify();
if (kk < k) return 0;
x *= 111 << kk - k, k</pre>
                                                                                                                                                                                                                                                                                                                                                                    int k = max(a.k, b.k);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return sgn(a.x - b.x);
                                                                                                                           inline bool Grow(int kk)
                                                                                                                                                                                                                                                                                                                                                                                                a.Grow(k), b.Grow(k);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return a = a + b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return a + (-b);
                              return *this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  grow(a, b);
                                                                                                                                                                                                                                                                     return 1;
```

```
if(sign(a[i] * a[i] - a[j] * a[j] - a[k] * a[k] - a[j] * a[k]) >= 0) return p[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               P proj(L 1, P p) { return 1.a + (1.b - 1.a) * (dot(p-1.a, 1.b-1.a) / (1.b-1.a).
                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 0, 3) a[i] = (p[(i + 2) % 3] - p[(i + 1) % 3]).len();
rep(i, 0, 3) {
  int j = (i + 1) % 3, k = (i + 2) % 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 auto Rand = [&] () { return rand() % 10000 / 5000 * pi; }; P ans(0, 0); rep(i, 0, n) ans = ans + p[i]; ans = ans / n; db len = 0; rep(i, 0, n) len += (ans - p[i]).len();
                                                                                                                                                            // sqrt((a ^ 2 + b ^ 2 + c ^ 2 + 4 * sqrt(3) * area) / 2)
// 如果有重点,大于 2 的直接用模拟退火法
o = outC(p[i], p[j], p[k]), r = abs(o-p[k]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            P np(ans.x + t * sin(ang), ans.y + t * cos(ang));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(det(p[0], p[1], p[2]) < 0) swap(p[1], p[2]);
P q1 = (p[2] - p[0]).rot(pi / 3) + p[0];
P q2 = (p[0] - p[1]).rot(pi / 3) + p[1];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             c = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        isLL(db a0, db b0, db c0, db a1, db b1, db c1) { db d = a0 * b1 - a1 * b0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          db k = 0; rep(i, 0, n) \dot{k} += (np - p[i]).len(); if(sign(len - k) > 0) ans = np, len = k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            db s2 = -\det(12.b - 12.a, 11.b - 12.a);
return (11.a * s2 + 11.b * s1) / (s1 + s2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        isLL(L 1, db a, db b, db c) \{ // ax + by \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return isLL(L(q1, p[1]), L(q2, p[2]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         db s1 = det(12.b - 12.a, 11.a - 12.a);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return (1.a * v + 1.b * u) / (u + v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      db \dot{u} = a * 1.a.x + b * 1.a.y + c;
db v = -(a * 1.b.x + b * 1.b.y + c);
                                                                                                                                                                                                                                                                                                                       if(n = 2) return (p[0] + p[1]) / 2;

if(n = 3) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       由线
                                                                                                                                                                                                                                                           int n = sz(p); assert(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       直线、
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  db t = 10000; // modify
                                                                                                                                                                                                                                                                                              if(n == 1) return p[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // 【点到直线投影(垂足)】
                                                                                                                                                                                                                        P fermat(vector<P> p)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         P isLL(L 11, L 12) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                db ang = Rand();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       线段、
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  while(t > eps) {
                                                                   return C(o,r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // 【直线交点】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return ans;
                                                                                                                                                                                                                                                                                                                                                                                          db a[3];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  len2()); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ર્સ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            5.2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     db Xm = p[m].x, lim = min(solve(1, m, p), solve(m + 1, r, p)); inplace_merge(p.begin() + 1, p.begin() + m + 1, p.begin() + r + 1, [&](P a, P b){
                                                                                                                                                                                                                                                                                                                                                                                                                                      };
db rad(P p1, P p2) { return atan2l(det(p1, p2), dot(p1, p2)); } // p1 与 p2 的夹角,有方
                                                                                                                                                                                                                                                                                                        int quad() const { return sign(y) > 0 || (sign(y) == 0 && sign(x) >= 0); }
                                                                                                                                                                                                                                                                                                                                        P rot90() { return P(-y, x); }
P rot(db a) { return P(cos(a) * x - sin(a) * y, cos(a) * y + sin(a) * x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(i, 1, r + 1) if(fabs(p[i].x - Xm) <= lim) V.pb(p[i]);
rep(i, 0, sz(V)) rep(j, i + 1, sz(V)) {
   if(fabs(V[j].y - V[i].y) >= lim) break;
   T dis = (V[i] - V[j]).len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               sort(all(A), [\&](P a, P b)\{return a.x < b.x;\});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           bool cmp(const pii &a, const pii &b) { // 级角排序
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     o = (p[i] + p[j]) / 2, r = abs(o-p[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(sgn(abs(o-p[k])-r) \leftarrow 0) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(sgn(abs(o-p[j])-r) \leftarrow 0) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int o = a > pii(0, 0), t = b > pii(0, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(sgn(abs(o-p[i])-r) \leftarrow 0) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           namespace NearestPoints \{ // sz(A) <= 1e5 \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         db solve(int 1, int r, vector<P> &p) {
                                                                                                                                                                                                                                                                                                                                                                                                      P norm() { return *this / len(); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return solve(0, sz(A) - 1, A);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(1 == r) return 1e100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          random_shuffle(p , p + n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     lim = min(lim, dis);
                                                                                                                                                                                          向量
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(0) = t return 0 < t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   }
db solve(vector<P> A) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return a.y < b.y;});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int m = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return det(a, b) > 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         0 = p[i], r = 0; r = 0; r = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          P o = p[0]; db r = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              C Mincir(P *p, int n){
                                                                                                                                                                                        1、基础点、
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // 【点集中最近点对】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           vector<P> V;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return lim;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // 【最小圆覆盖】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(i,1,n) {
                                                                                                                                                                                                                                                                               struct P {
```

```
return (b.y - a.y) * 111 * (c.x - b.x) <= (c.y - b.y) * 111 * (b.x - a.x);
                                                                                                     \label{eq:control_dos} \begin{subarray}{ll} $\bf do (++(det(A[(i+1)\ %\ n]-A[i]), A[(i+1)\ %\ n] - A[i]) >= 0\ ?\ j\ :\ i))\ \% = n, \\ res = max(res,\ (A[i]-A[i]).len()); \end{subarray}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void ins(int x, int y) { ins(h1, P(x, y)); ins(h2, P(x, -y)); } bool in(int x, int y) { return in(h1, P(x, y)) && in(h2, P(x, -y)); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(!sz(h)) return 0;
if(p.x < h.begin()->se.x || p.x > h.rbegin()->se.x) return 0;
rep(i, 1, n) (A[i] < A[1]) & (1 = i), (A[r] < A[i]) & (r = i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(sgn(b.x - a.x)) return (p.x - a.x) / (b.x - a.x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(ao(11->se, 1->se, p)) h.erase(1); else break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               auto rr = r; rr++; if(rr == h.end()) break;
if(ao(p, r\rightarrow se, rr\rightarrow se) h.erase(r); else break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            while(1) {
    auto 1 = pos; if(1 == h.begin()) break; --1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    auto 11 = 1; if(11 == h.begin()) break; —11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       auto r = pos; r++; if(r == h.end()) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 P operator [] (const int&n) {return d[n];}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  <= 1->se.y;
                                                                                                                                                                                                                                                                                                                  // 0(nlogn)
// 插入点,询问点在不在凸包内部(包括边界)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return (p.y - a.y) / (b.y - a.y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               P d[10]; int dn; // d[dn] = d[0]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(p.x == 1->se.x) return p.y
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void ins(map<int, P> &h, P p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         namespace ConvecIntersection{ // ?
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          bool in(map<int, P> &h, P p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  auto 1 = h.lower_bound(p.x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return ao(1—>se, p, r—>se);
                                     db res = (A[1]-A[r]).len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(in(h, p)) return;
h[p.x] = p;
auto pos = h.find(p.x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    typedef pair<db, int> pdi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                     bool ao(P a, P b, P c) {
                                                                                                                                                                          while(i != 1 || j != r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int n;pdi res[1000005];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       db getLoc(P a,P b,P p){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // 包括边界: 小等于
                                                                                                                                                                                                                                                                                                                                                                                                                  map<int, P> h1, h2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               const int N = 1005
                                                                          int i = 1, j = r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       auto r = 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    while(1) {
                                                                                                                                                                                                                                                                                                                                                                               namespace DCH {
                                                                                                                                                                                                                  return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            struct Rec
                                                                                                                                                                                                                                                                             // 【动态凸包】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    //【凸包交】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            sort(all(ps)); vector<P> qs;
for(int i = 0; i < n; qs.pb(ps[i++])) {
    while(sz(qs) > 1 && sign(det(qs[sz(qs) - 2], qs.back(), ps[i])) <= 0) qs.pop_back();</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    while(sz(qs) > t \& sign(det(qs[sz(qs) - 2], qs.back(), ps[i])) <= 0) qs.pop_back();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return min(min(disToSeg(b, a.s), disToSeg(b, a.t)), min(disToSeg(a, b.s), disToSeg(a,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return sign(dot(1.a, p, 1.b)) * sign(dot(1.b, p, 1.a)) == 1 ? disToL(1, p) : min((p 1.a).len(), (p-1.b).len());
                                                                                                     bool isSSr(const L &a, const L &b){ db c1 = det(a.t - a.s, b.s - a.s), c2 = det(a.t - a.s, b.t - a.s); db c3 = det(b.t - b.s, a.s - b.s), c4 = det(b.t - b.s, a.t - b.s);
                                                                                                                                                                                                                                                                                                               db c1 = det(a.t - a.s, b.s - a.s), c2 = det(a.t - a.s, b.t - a.s);
db c3 = det(b.t - b.s, a.s - b.s), c4 = det(b.t - b.s, a.t - b.s);
return sign(c1) * sign(c2) <= 0 && sign(c3) * sign(c4) <= 0 &&
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       bool isLS(P a1, P a2, P b1, P b2) { // 判断直线线段是否相交(端点也算)
db c1 = det(a2 - a1, b1 - a1), c2 = det(a2 - a1, b2 - a1);
                                                                                                                                                                                                     return sign(c1) * sign(c2) < 0 && sign(c3) * sign(c4) < 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for(int i = n - 2, t = sz(qs); i >= 0; qs.pb(ps[i-])) {
                                                                                                                                                                                                                                                                                                                                                                                                                     sign(max(a.s.x, a.t.x) - min(b.s.x, b.t.x)) >= 0 &&
                                                                                                                                                                                                                                                                                                                                                                                                                                                       sign(max(b.s.x, b.t.x) - min(a.s.x, a.t.x)) >= 0 &&
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       sign(max(a.s.y, a.t.y) - min(b.s.y, b.t.y)) >= 0 &&
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          sign(max(b.s.y, b.t.y) - min(a.s.y, a.t.y)) >= 0;
  - a0 * c1) / d;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return fabs(det(1.a, p, 1.b) / (1.b - 1.a).len());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int n = sz(ps); if(n \le 1) return ps;
     a1 * c0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            vector<P> convexHull(vector<P> ps) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return sign(c1) * sign(c2) <= 0;
     b1 * c0,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               disSS(L a, L b){
if(isSS(a, b)) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    diameter(vector<P> A)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         qs.pop_back(); return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(n <= 1) return 0;</pre>
     return P(b0 * c1 -
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  db disToL(L l, P p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       db disToS(L l, P p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int 1 = 0, r = 0;
                                                                                                                                                                                                                                                                          bool isSS(L a,L b){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int n = sz(A);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // 【凸包最远点对】
                                                                     // 【线相交判定】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // 【线到线距离】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // 【点到线距离】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    / 【求凸句】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            b.t)));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               က်
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               5.3
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GEO
Fuzhou University
                                                                                                                                                                                                                                                                                                                                                                                                                         = 1;
                                                                                                                                                                                                                                                                                                                    = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                       if(det(q[0], q1, q2) < 0) swap(q1, q2), f2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       db res = f1 == f2 ? area(ps) : —area(ps);
                                                                                                                                                                                                                                                                                                                  Ţ
                                                                                                                                                                                                                                                                                                                  if(det(p[0], p1, p2) < 0) swap(p1, p2),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(sign(dis - (A.r + B.r)) == 1) return 4;
if(sign(dis - (A.r + B.r)) == 0) return 3;
                                                                              polyInter(vector<P> &p, vector<P> &q) {
                                                                                                                                                         // if(area(p) < 0) reverse(all(p));
                                                                                                                                                                                 // if(area(q) < 0) reverse(all(q));
                                                                                                                                                                                                                                                                                                                                                                                                                                                 vector<P> ps(\{p[0], p1, p2\});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           convexCut(ps, L(q[0], q1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           convexCut(ps, L(q2, q[0]));
                                                                                                                                                                                                                                                                                                                                                                P q1 = q[j], q2 = q[j + 1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // 相离4: 外切3: 相交2: 内切1: 内含0:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     convexCut(ps, L(q1, q2));
                                                                                                                                                                                                                                 rep(i, 1, n - 1) {
P p1 = p[i], p2 = p[i + 1];
                            <u>=</u> =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int relCC(C A, C B) { // 两圆关系
                                                                                                        int n = sz(p), m = sz(q);
if(n < 3 || m < 3) return 0;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            db \ dis = (A.0 - B.0).len();
                          // 【平面图欧拉定理】 N + F -
                                                  【简单多边形求面积交】
                                                                                                                                                                                                                                                                                                                                            rep(j, 1, m-1)
                                                                                                                                                                                                                                                                                                                                                                                            bool f2 = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ans += res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return fabs(ans);
                                                                                                                                                                                                                                                                                      bool f1 = 0;
                                                                                                                                                                                                               db ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // 注意相等关系
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         國
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // 【两圆关系】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             5.6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  \mathsf{rt} \; + = \; \big( (\mathsf{r[i][j+1]} - \mathsf{r[i][j]}) \; \; \mathsf{a} \; + \; \mathsf{r[i][j]}) \; / \; \big( (\mathsf{r[i][j+1]} - \mathsf{r[i][j]}) \; \; \mathsf{b} \; + \; \\
                                                                                                                                                                                                                                                                                                                        if(sgn((r[i][j+1] - r[i][j]) * (r[t][g+1] - r[t][g])) < 0 || i < t)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         else if(du < 0 && dv >= 0) res[sz++] = pdi(s1 / (s1 + s2) , -1);
                                                                                                                                                                                                                                                                                                                                              res[sz++] = pdi(getLoc(r[i][j], r[i][j+1], r[t][g]), 1);
res[sz++] = pdi(getLoc(r[i][j], r[i][j+1], r[t][g+1]), -1);
                                                                                                                                                                                                                                                                                                                                                                                                    else {
    db s1 = (r[i][j] - r[t][g]) / (r[t][g+1] - r[t][g]);
    db s2 = (r[t][g+1] - r[t][g]) / (r[i][j+1] - r[t][g]);
    if(du >= 0 && dv < 0) res[sz++] = pdi(s1 / (s1 + s2) , 1);</pre>
                                                                                                                                                                                                                                           int du = sgn((r[i][j+1] - r[i][j]) / (r[t][g] - r[i][j]));
int dv = sgn((r[i][j+1] - r[i][j]) / (r[t][g+1] - r[i][j]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(cnt == 0 && sgn(res[t].fi - res[t+1].fi)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(b < 0) continue; if(b > 1) b = 1;
                                                                                                                                      res[sz++] = pdi(0,0);res[sz++] = pdi(1,0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(a < 0) a = 0; if(a > 1) break
                                                                                    rep(i,0,n) rep(j,0,r[i].dn){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               db b = res[t+1].fi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            db \ a = res[t].fi;
                                                                                                                                                                                       if(t == i) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           sort(res , res + sz);
                                                                                                                                                                                                                   rep(g,0,r[t].dn) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        cnt += res[t].se;
                                                                                                                                                                                                                                                                                                if(!du && !dv)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int cnt = 0; —sz;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(t,0,sz) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return rt / 2;}}
                                                                                                                                                                   rep(t,0,n) {
                                                                                                                int sz=0;
        }
db work() {
                                                              db rt=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    5.4
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三角形 4

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db dB = b.len2(), dC = c.len2(), d = 2 * det(b, c); return A - P(b.y * dC - c.y * dB, c.x * dB - b.x * dC) / d;
                                                                                                                                                                                                                                                                                                                               fz = fz + (p[0] + p[i] + p[i + 1]) * t / 3;
                                                                                                                                                                          baryC(P p[], int n) { // 重心 P fz(0, 0); db fm = 0; rep(i, 1, n - 1) { db t = det(p[0], p[i], p[i + 1]);
                         P outC(P A, P B, P C) { // 外心
                                                        P \ b = B - A, C = C - A;
                                                                                                                                                                                                                                                                                                                                                                                               return fz / fm
                                                                                                                                                                                                                                                                                                      fm += t;
(心)
|
|
```

P det = $((p_0 - c.o)^* (-c.r * sqrt(d) / x)).rot90();$

p1 = c.o + p + det;p2 = c.o + p - det;

P p = (p0 - c.0) * (c.r * c.r / x);

if(d < eps) return 0;</pre>

vector<P> tanCC(const C &c1, const C &c2) {

db dis = (c1.0 - c2.0).len();

vector<P> res

// 【圆圆切点】

return 1;

bool tanCP(0 c, P p0, P &p1, P &p2) { db $x = (p\theta - c.o).len2(), d = x - c.r * c.r; }$

// 【点圆切点】

ceturn 0;

if(sign(dis - fabs(A.r - B.r)) == 1) return 2; if(sign(dis - fabs(A.r - B.r)) == 0) return 1;

```
2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ans[cnt] += ang * c[i].r * c[i].r / 2 - \sin(ang) * c[i].r * c[i].r /
                            if(sign(dot(s - p1, t - p1)) \le 0 \& sign(dot(s - p2, t - p2) \le 0))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(j,0,i) if(c[i]==c[j]) cnt++;
rep(j,0,n) if(j!=i&&!(c[i]==c[j])&&overlap(c[j],c[i])) cnt++;
                                                        return r * r * (rad(s, p1) + rad(p2, t)) + det(p1, p2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         P p,T ang;int delta;
E(){} E(P p,T ang,int delta):p(p),ang(ang),delta(delta){}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  bool overlap(C a,C b) {return sgn(a.r\rightarrowb.r\rightarrowabs(a.o\rightarrowb.o))>=0;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           bool operator < (const E&b) const {return ang<b.ang;}</pre>
                                                                                  else return r * r * rad(s, t);
} else if(b1) return r * r * rad(s, p1) + det(p1, t);
else if(b2) return r * r * rad(p2, t) + det(s, p2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ans[cnt] += evt[j].p / evt[j+1].p / 2;
db ang = evt[j + 1].ang - evt[j].ang;
if(ang < 0) ang += pi * 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(j,0,2) a[j]=(pts[j]-c[i].0).arg();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(!sz(evt)) ans[cnt] += pi*c[i].r*c[i].r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              memset(ans , 0 , sizeof(T) * (n + 1)); rep(i,0,n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                 ans += areaCT(c.r, u - c.0, v - c.0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 vector<P> pts=insCC(c[i],c[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         evt.pb(E(pts[0],a[0],1));
evt.pb(E(pts[1],a[1],-1));
                                                                                                                                                                                                                                                                                                                                                                                             P u = p[i], v = p[(i + 1) % n];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   namespace CircleIntersection{ // ?
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      cnt += a[0] > a[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  cnt+=evt[j].delta;
                                                                                                                                                                                                                                                                        db areaCPoly(C c, vector<P> p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   void solve(C *c,int n,T *ans)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         evt.pb(evt.front());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(j, 0, sz(evt)-1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(j,0,n) if(j!=i){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      sort(all(evt));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(sz(pts)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return fabs(ans) / 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               vector<E> evt;
                                                                                                                                                                                                               }
// 【圆与多边形交面积】
                                                                                                                                                                                return det(s, t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int cnt=1;
                                                                                                                                                                                                                                                                                                                                                                    rep(i, 0, n) {
if(b1 && b2) {
                                                                                                                                                                                                                                                                                                           int n = sz(p);
                                                                                                                                                                                                                                                                                                                                     db ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    struct E{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  / 【國交】
```

```
bool b1 = sign(s.len2() - r * r) == 1, b2 = sign(t.len2() - r * r) == 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     P p = l.a - ((1.b - 1.a) * (x / y)), det = (1.b - 1.a) * (sqrt(d) / y); p1 = p - det, p2 = p + det; // dir : l.a \rightarrow l.b
                          res.pb(c1.0 + (c2.0 - c1.0) * c1.r / (c1.r + c2.r));
                                                                                                                     res.pb(c1.0 + (c2.0 - c1.0) * c1.r / (c1.r - c2.r));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                P p = (c1.0 * -c2.r + c2.0 * c1.r) / (c1.r - c2.r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) {
  if(c1.r < c2.r) swap(p1, p2), swap(q1, q2);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     db x = dot(1.a - a.o, 1.b - 1.a);
db y = (1.b - 1.a).len2();
db d = x * x - y * ((1.a - a.o).len2() - a.r * a.r);
if(sign(d) < 0) return 0;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(tanCP(c1, p, p1, p2) && tanCP(c2, p, q1, q2)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       P p = (c1.0 * c2.r + c2.0 * c1.r) / (c1.r + c2.r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  bool f = iscL(C(P(0, 0), r), L(s, t), p1, p2);
if(!f) return r * r * rad(s, t);
                                                                                                                                                                                                                                                                                                                                                                                                      dir = (dir * (c1.r / dir.len())).rot90();
                                                                                                                                                                                                                                                                                                                                                                                                                                     ret.pb(L(c1.0 + dir, c2.0 + dir));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ret.pb(L(c1.0 - dir, c2.0 - dir))
if(sign(dis - (c1.r + c2.r)) == 0)  {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        areaCT(db r,P s,P t) { // 需要除
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           bool isCL(0 a, L l, P &p1, P &p2) {
                                                                                           if(sign(dis - fabs(c1.r - c2.r))
                                                                                                                                                                                                                                                                            vector<L> extanCC(C c1, C c2) {
                                                                                                                                                                                                                                                                                                                                          if(sign(c1.r - c2.r) == 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                vector<L> intanCC(C c1, C c2) \{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ret.pb(L(p1, q1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ret.pb(L(p2, q2));
                                                                                                                                                                                                                                                                                                                                                                         P \text{ dir} = c2.0 - c1.0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ret.pb(L(p2, q2));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ret.pb(L(p1, q1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                p1, p2, q1, q2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // 【 國与三角形交面积】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         P p1, p2, q1, q2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  d = max(d, 0.);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // 【直线和圆求交】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               vector<L> ret;
                                                                                                                                                                                                                                                                                                                vector<L> ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return ret;
                                                                                                                                                                                          return res
                                                                                                                                                                                                                                                  // 【外公切线】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // 【内公切线】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return 1;
```

0 0 0

b, c));

```
3D
```

```
db 1 = s.len(), x = s.x / 1, y = s.y / 1, z = s.z / 1, si = sin(a), co = cos(a); db p[4][4] = \{
                                          int quad() const { return sign(y) > 0 \mid | (sign(y) == 0 \& sign(x) >= 0); }
                                                                                                                                                   4) rep(j, 0, 4) r.a[i][j] = p[i][j]; return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       this \rightarrow a=P(0,0); this \rightarrow b=P(sign(b), sign(b)*(-a/b));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int x=sign(c)*sign(det(P(-c/a,0), P(0,-c/b)));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(x==1) this->a=P(-c/a,0), this->b=P(0,-c/b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     else this->a=P(0,-c/b), this->b=P(-c/a,0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              this\rightarrowa=P(-c/a, 0);this\rightarrowb=P(-c/a,-sign(a));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               this->a=P(0,-c/b);this->b=P(Sign(b),-c/b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         dba, dbb, dbc) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(d1 * d2 < 0) q.pb(isLL(L(p1, p2), 1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(d1 * d2 < 0) q.pb(isLL(L(p1, p2), a,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 0, sZ(p)) {
   P p1 = p[i], p2 = p[(i + 1) % sZ(p)];
   int d1 = sign(a * p1.x + b * p1.y + c);
   int d2 = sign(a * p2.x + b * p2.y + c);
                                                                                                                                                                                                                                                                                                                                                               rep(i, 0, sz(p)) {
   P p1 = p[i], p2 = p[(i + 1) % sz(p)];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // ax + by + c >= 0, (a != 0 || b != 0)
L(db a, db b, db c) {
                                                                                                                                                                                                                                                                                                                                                                                                                                      int d2 = sign(det(l.a, l.b, p2));
if(d1 >= 0) q.pb(p1);
                                                                                                                                                                                                                                                                                                                                                                                                                 int d1 = sign(det(l.a, l.b, p1));
                                                                                                                                                                                                                                                                                                                void convexCut(vector<P> &p, L l) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         HalfPlane_nlogn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void convexCut(vector<P> &p,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(d1 >= 0) q.pb(p1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      } else if(sign(b)==0)
                                                                                                                                                                                                                                 HalfPlane n2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(sign(c)!=0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(sign(a)==0)
                                                                                                                                                                                                                                                                                         // 1: a->b 逆时针方向
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // ax + by + c >= 0
                                                                                                                                                     Mat r; rep(i, 0,
                                                                                                                                                                                                                                                                                                                                        vector<P> q;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      vector<P> q
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   p = q
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             struct L {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      struct P {
                                                                                                                                                                                                                                 .
დ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         5.9
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(i, 0, 4) rep(j, 0, 4) rep(k, 0, 4) r.a[i][j] += a[i][k] * c.a[k][j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Mat r; rep(i, 0, 4) rep(j, 0, 4) r.a[i][j] = p[i][j]; return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                4) rep(j, 0, 4) r.a[i][j] = p[i][j]; return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         db ty, db tz) { // 平移,以下矩阵均为左乘
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void set() { rep(i, 0, 4) rep(j, 0, 4) a[i][j] = 0; }
void e() { rep(i, 0, 4) a[i][i] = 1; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            Mat rotate(P3 s, db a) { // 绕 s 为轴旋转 a 度, 右手方向
                                                                                                                            db t = 1; P3 ans(0, 0, 0);
rep(i, 0, n) ans = ans + p[i]; ans = ans / n;
                                                                                                                                                                                                                                                                                 if(ret < tmp) ret = tmp, j = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Mat scale(db a, db b, db c) { // 缩放
db p[4][4] = {
                                                                                                                                                                                                                                                      db tmp = (p[i] - ans).len();
                                                                                                                                                                                                                                                                                                                                 ans = ans + (p[j] - ans) * t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Mat operator * (const Mat &c)
                                                                              P3 MinSphere(vector<P3> p) {
                                                                                                                                                                               while(t > eps) {
  int j = -1; db ret = -1;
                                                                                                       int n = sz(p); assert(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Mat kpow(Mat a, int b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(b & 1) r = r * a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Mat r; r.set(); r.e();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Mat translate(db tx,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Mat r; r.set();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Mat r; rep(i, 0,
                                                                                                                                                                                                                                                                                                                                                                                                                                                       // 【三维向量变换】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         1, 0, 0, tx, 0, 1, 0, ty, 0, 0, 1, tz, 0, 0, 0, 1, tz, 0, 0, 0, 1};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i, 0, n)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      db p[4][4] = {
                                                       【最小球覆盖】
                                                                                                                                                                                                                                                                                                                                                          t^* = 0.999
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 a = a * a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           db a[4][4];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return r;
                                                                                                                                                                                                                                                                                                                                                                                                           return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             while(b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               b >>= 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    struct Mat {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return r;
```

```
for (int 1 : vals) area += 1d(1) * sqrt(1d(D) * 1d(D) - 1d(1) * 1d(1)) / 4; 1d hiArea = 1d(hi) * sqrt(1d(D) * 1d(D) - 1d(hi) * 1d(hi)) / 4;
                                                                                                                                                                                                                                                    while (tooSmall(ma)) numExpand++, ma += (ma - mi);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    P &b, P &c) {
                                                             ld hiAng = 2 * asin(ld(hi) / ld(D));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      tmb;
                                                                                                                          else return ang + hiAng >= 2 * PI;
                                                                                       if (isReflex) return ang < hiAng;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               T res = area(a, b, c), cur = res,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void maxAreaTri(P *p, int n, P &a,
int i = 0, j = 1, k = 2;
a = p[i], b = p[j], c = p[k];
                                                                                                                                                                                                                                                                                   rep(tim, 0, 50 + numExpand) { Id md = mi + (ma - mi) / 2;
                                                                                                                                                                                                                                                                                                                                              if (tooSmall(md)) mi = md;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (isReflex) area —= hiArea;
auto tooSmall = [\&](ld D)
                                                                                                                                                                                       Id mi = hi, ma = hi + 1;
                               ld ang = getAngle(D);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              MaxAreaTri
                                                                                                                                                                                                                                                                                                                                                                                                                                             Id D = mi, area = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            else area += hiArea;
                                                                                                                                                                                                                         int numExpand = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                else break;
                                                                                                                                                                                                                                                                                                                                                                                     else ma = md;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              while(1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return area;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // 0(n ^ 2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              5.11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              bool includer(const P &p) const { return sign(det(b - a, p - a)) > 0; bool include(const P &p) const { return sign(det(b - a, p - a)) >= 0; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        while(sz(q) > 2 && !check(q[sz(q) - 2], q.back(), q[0])) q.pop_back();
while(sz(q) > 2 && !check(q[1], q[0], q.back())) q.pop_front();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          while(sz(q) > 1 && !check(q[1], q[0], 1[1])) q.pop_front();
q.pb(1[1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    bool check(L u, L v, L w) { return w.include(isLL(u, v)); }
                                                                                                                                                                                                                                                                                                                                                                                return sign(det(a, b)) == 0 \& sign(dot(a, b)) == 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(a.quad() != b.quad()) return a.quad() < b.quad();
return sign(det(a, b)) > 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       bool operator < (const L &l0, const L &l1) {
   if(sameDir(l0, l1)) return l1.includer(l0.a);
   return (l0.b - l0.a) < (l1.b - l1.a);</pre>
                                                                                                                                                                                         P det = (b - a).rot90().norm() * len;
                                                                                                                                                                                                                                                                                                                                                                                                                                             bool operator < (const P &a, const P &b)
                                                                                                                                                                                                                                                                                                                   bool sameDir(L 10, L 11) {
   P a = 10.a - 10.b, b = 11.a - 11.b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 deque<L> halfPlane(vector<L> 1) {
                                                                                                                                                                                                                      return L(a + det, b + det);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 sort(all(l)); dequeL> q;
                                                                                                                            // 向内(右手方向)推
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(i, 0, sz(l)) {
                                                                                                                                                            L push(db len) {
```

```
while(cur <= (tmp = area(p[i], p[j], p[(k + 1) % n]))) (++k) %= n, cur = tmp; if(cur <= (tmp = area(p[i], p[(j + 1) % n], p[k]))) (++j) %= n, cur = tmp;
                                                                                                                                                     if(cur > res) a = p[i], b = p[i], c = p[k], res = cur;
                                                                                                                                                                                                                                                                                                           cur = area(p[i], p[j], p[k]);
                                                                                                                                                                                                                                 if(i == j) (++j) %= n;
if(j == k) (++k) %= n;
                                                                                                                                                                                              (++i) %= n;
                                                                                                                                                                                                                                                                                                                                                 } while(i);
```

MinAreaTri 5.12

if (cur > hi) swap(cur, hi);

rep(i, 1, sz(S)) { **int** cur = S[i];

MaxAreaPoly

5.10

int sum = 0, hi = S[0];

vi vals;

solve_poly(vi &S) { assert(sz(S) > 0);

19

if (sum <= hi) return 0;

ld tot = 0;return tot;

vals.pb(cur); sum += cur;

```
bool cmp(const P &x, const P &y) { return det(x, y) < \theta; }
                                                            struct P { int x, y, ind, u, v; };
                                                                                                                                                const 11 inf = 4e18;
                                                                                          namespace MinAreaTri {
                                                                                                                       const int N = 2020;
                                                                                                                                                                             int n, m, pos[N];
                                                                                                                                                                                                          P p[N], 1[N * N];
// 无重点、三点共线
                                 // 0(n^2 10g_2n)
                                                                                                                                                  for (int 1 : vals) tot += 2 * asin(ld(1) / ld(D));
                                                                                                                                                                                                            };
bool isReflex = (getAngle(hi) < PI);</pre>
                                                                                       auto getAngle = [\&](ld D) \rightarrow ld\{
```

```
}
C fy1(P o, db r, C c) { // 不过反演中心的圆反演后还是圆
                                                                                                                                                                                                                                                                                                                          fy0(b o, db r, C c) { // 过反演中心的圆反演后是直线
                                                                                                                                                                                                                        return C((p1 + p2) / 2, (p1 - p2).len() / 2);
                                                                                                                                                                             P p1, p2; isCL(c, L(o, c.o), p1, p2);
p1 = fy(o, r, p1);
p2 = fy(o, r, p2);
                                                                                                                                                                                                                                                                                P p1 = fy(o, r, p);
P p2 = p1 + (o - p1).rot90();
                                                                                          return (p - o) * ro / d + o;
                                                                                                                                                                                                                                                                 P p = c.0 + c.0 - 0;
                                                                                                                                                                                                                                                                                                            return L(p1, p2);
return ans
                                                        圆反演
                                                          5.14
```

平面图转对偶图 5.15

== 0 && a.x >= 0); }

bool gao(P a) { **return** a.y > 0 || (a.y **bool** cmp(P a, P b) {

int n; P p[N], q[N]; 11 s[N];
namespace CNT {

const int N = 1010;

凹四边形计数

5.13

bool o = gao(a), t = gao(b); if(o != t) return o > t;

return det(a, b) > 0;

```
static const int N = 101010, M = 101010
                                                                                                                                                                                                                                                                               rep(i, 0, sz(ps)) g[i].clear();
                                                                                                                                                                                                                                                                                                   fill_n(vis, cnte, false);
ps.clear(); cnte = 0;
                                                                                                                                                                                                                                                                                                                                                                                   void adde(int u, int v)
                                                                                                                                                                                                                                                                                                                                                                                                            g[u].pb(mp(v, cnte));
E[cnte++] = mp(u, v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                   g[v].pb(mp(u, cnte));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         E[cnte++] = mp(v, u);
                                          // ps id starts from 0
                                                                                   // cnte id starts from
                                                                                                                                                                                                                                                                                                                                               areas.clear();
                                                                                                                                                    // u -> (v, cnte)
                                                                                                                                                                                                                  vector<db> areas;
                                                                                                                                                                       vector<pii> g[N];
                                                                                                       int cnte, ne[M];
                                                                                                                                                                                                                                                      void init() {
                                                                vector<P> ps;
                                                                                                                         bool vis[M];
struct Planar {
                                                                                                                                                                                           pii E[M];
```

while(j >= 2 && det(q[j], q[i]) > 0) — j, ++cnt;

s[i] = s[i + 1] + cnt;

per(i, k + 1, n + 1) {

int j = k, cnt = 0;

rep(i, 1, n + 1) q[i] = p[i]; swap(q[1], q[u]); rep(i, 2, n + 1) q[i] = q[i] - p[u];

void solve(int u, ll &ans) {

int k = n; **while**(k >= 2 && q[k].y <= 0)

sort(q + 2, q + n + 1, cmp);

*111 * (c - k - 1);

ll ans = 0; rep(i, 1, n + 1) solve(i, ans);

} 11 solve() {

int c = j = k + 1; rep(i, 2, k + 1) {
 while(c <= n && det(q[i], q[c]) > 0) ++c; while(j <= n && det(q[i], q[j]) >= 0) ++j; ans += s[j] + (n - j + 1) * 111 * (c - k -

19/93

```
mi = min(mi, area(p[pu - 1], p[pu], p[pv + 1], p[v]));
ma = max(ma, area(p[1], p[pu], p[n], p[v]));
                                                                                                                                                if(1[m].x \le 0) 1[m].x *= -1, 1[m].y *= -1;
else if(1[m].x == 0 \&\& 1[m].y < 0) 1[m].y *= -1
                                                      rep(i, 1, n + 1) p[i].ind = i, pos[i] = i;

m = 0; rep(i, 1, n + 1) rep(j, i + 1, n + 1) {

l[++m] = p[i] - p[j];
                                                                                                                                                                                                                                                                                                                                                                                                                               if(pu > pv) swap(u, v), swap(pu, pv);
                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(pu == 1 || pv == n) continue;
                                                                                                                                                                                                                                                                                                                                                                                                   int pu = pos[u], pv = pos[v];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                cout << mi << " " << ma << endl;
                                                                                                                                                                                                                                                                                                         mi = inf, ma = 0;
rep(i, 1, m + 1) {
  int u = l[i].u, v = l[i].v;
                                                                                                                                                                                                                                                                          Sort(1 + 1, 1 + 1 + m, cmp);
                                                                                                                                                                                                              l[m].u = i, l[m].v = j;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       swap(pos[u], pos[v]);
                            sort(p + 1, p + 1 + n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           swap(p[pu], p[pv]);
void solve() {
```

```
else ans = min(ans, disSS(L(p[o], p[(o + 1) % n]), L(q[t], q[(t + 1) % m])));
                                                                                                                                                                                                                                                                                                                                                                                                       while(det(t, ps[(p + 1) % n] - ps[p]) > 0) (++p) %= n, while(dot(t, ps[(1 + 1) % n] - ps[1]) < 0) (++1) %= n,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           while(dot(t, ps[(r + 1) % n] - ps[r]) > 0) (++r) %= n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        11 et = abs(det(ps[p], ps[i], ps[(i + 1) % n]));
11 ot = abs(dot(t, ps[1] - ps[r]));
                                                                                                                                                                           p, n));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ans = min(ans, (db)et * ot / t.len2());
                                                                                                                                                                         return min(solve(p, n, q, m), solve(q, m,
                                                                                                                                            work(P p[], int n, P q[], int m) {
                                                                                                                                                                                                                                                                                                                  int p = 1, l = 1, r;
rep(i, 0, n) {
  P t = ps[i] - ps[(i + 1) % n];
                                                                                                                                                                                                                                                                                        int n = sz(ps); T ans = 1e18;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // 【凸包最小周长外接矩形】
                                                                                                                                                                                                                              // 【凸包最小面积外接矩形】
                                                                                                                                                                                                                                                               T solve(vector<P> ps) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                               r = (p + 1) \% n;
                               :u =% (0++)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Graph
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return ans;
                                                                                      return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ဗ
                                                                                                                                                                                                                                                                                                                                                                                                                                    void solve(const vector<P> &_ps, const vector<pii> init(); ps = _ps;
                                                                                                                                                                                                                                                                                      res += det(ps[E[e].se], ps[E[e].fi]); vis[e] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(j, 0, sz(g[i])) {
ne[g[i][j].se] = g[i][(j + 1) % sz(g[i])].se;
                                                       P a = ps[i.fi] - ps[V], b = ps[i.fi] - ps[V];
int o = P(0, 0) < a, t = P(0, 0) < b;
                            bool cmp(const pii &i, const pii &j) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for(auto e : es) adde(e.fi, e.se);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(i, 0, cnte) if(!vis[i]) go(i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, sz(ps)) {
    V = i; sort(all(g[i]), cmp);
                                                                                                                                                                                                                                                                                                                                                                            if(res > 0) areas.pb(res / 2);
                                                                                                               if(0 != t) return 0 < t;
                                                                                                                                              return det(a, b) > 0;
                                                                                                                                                                                                                                                               while(!vis[e]) {
                                                                                                                                                                                                                                                                                                                       e = ne[e \land 1]
                                                                                                                                                                                                 void go(int e) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              旋转卡壳
                                                                                                                                                                                                                              db res = 0;
```

2-sat

6.1

```
void add_set(int a, int va) { a = a << 1 | va; g[a ^ 1].pb(a); } // va 必选
void add_then(int a, int va, int b, int vb) { // va 和 vb 不能同时取
addedge(a, va, b, vb ^ 1);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            void add_xor(int a, int va, int b, int vb) { // va 和 vb 同时取或同时不取
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            void add_or (int a, int va, int b, int vb) { // va 和 vb 不能同时不取
                                                                                                                                                                                                                                                                                                        void addedge(int a, int va, int b, int vb) { // va 选了 vb 必选
                                                                                                                                                                                        void init(int _n) { per(i, 0, (n = _n << 1)) g[i].clear(); }
int new_node() { rep(i, 0, 2) g[n++].clear(); return n / 2 -
/// optionals begin</pre>
                                                                        int dfn[N], low[N], id[N], st[N], _st,
                                                                                                                                                                                                                                                                                                                                               a = a \ll 1 \mid va; b = b \ll 1 \mid vb;
                                                                                                                                                                                                                                                                                                                                                                                      g[a].pb(b); g[b ^ 1].pb(a ^ 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     }
// 需要 sz(vu) 个额外的 dp 变量
                                    static const int N = ::N << 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   addedge(a, va ^ 1, b, vb);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            addedge(a, va, b, vb);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        addedge(b, vb, a, va)
                                                                                                                                                    int mark[N], n;
struct TwoSat
                                                                                                                  vi g[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               while((tmp = det(a, q[(t + 1) % m] - q[t])) < 0) (++t) %= m; 
if(sign(tmp)) ans = min(ans, disToSeg(L(p[o], p[(o + 1) % n]), q[t]));
                                                                                                                                                                                                                                                                   while(\det(t, ps[(p + 1) % n] - ps[p]) > 0) (++p) % = n;
                                                                                                                                                                                                                                                                                                                                                  ans = max(ans, (ps[(i + 1) % n] - ps[p]).len());
                                                                                                                                                                                                                                                                                                        ans = max(ans, (ps[i] - ps[p]).len());
                                                                                                               if(n <= 1) return 0;
if(n == 2) return (ps[1] - ps[0]).len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        P a = p[(o + 1) % n] - p[o]; db tmp;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int o = 0, t = 0; T ans = inf;
rep(i, 1, n) if(p[i].y > p[o].y) o = i;
rep(i, 1, m) if(q[i].y < q[t].y) t = i;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         T solve(P p[], int n, P q[], int m) {
```

P t = ps[i] - ps[(i + 1) % n];

rep(i, 0, n) {

T diameter(vector<P> ps) n = sz(ps); T ans = 0;

// 【凸包直径】点 − 点

// 凸包都是顺时针给出

5.16

1

凸包间的最大距离】点

【凸包宽度】点 **return** ans;

【凸包间的最小距离】

rep(i, 0, n) {

-1;}

```
if (idfs(i ^ 1)) return 0;
}
return 1;
```

6.2 BCC

```
rep(i, 0, n) if(!dfn[i]) dfs(i, 1, g);
rep(i, 0, n) for(auto j:g[i]) if(id[i]!=id[j.fi])
bcc[id[i]].pb(id[j.fi]);
                                                                                                                                                                                                                                                                                                                                              low[c]=min(low[c],low[t]);
if(low[t]>dfn[c]) key.pb(e.se);
} else if(dfn[t] != dfn[c] - 1 || cc++)
                                                                                                                                 int dfn[N] , low[N] , id[N] , st[N] , _st , _;
void dfs(int c,int dep,vector<pii> g[]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         do{id[st[---st]]=_;}while(st[_st]!=c);
                                                                                                                                                                                                                                                                                                                                                                                                                         low[c] = min(low[c], dfn[t]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int solve(int n, vector<pii> g[]){
// key contains the id of edges
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              fill_n(bcc, n, key=vi());
                                                                                                                                                                                                                                                                                                                       dfs(t, dep+1, g);
                                                                                                                                                                                      int cc=0;st[_st++]=c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     fill_n(low,n,_st=0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(low[c]==dfn[c]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          fill_n(dfn,n,_=0);
                                                                                                                                                                                                            dfn[c]=low[c]=dep;
                                                                                                                                                                                                                                         for(auto e:g[c]){
                                                                           const int N = 202020;
                                                                                                                                                                                                                                                                                        if(!dfn[t]){
                                                                                                                                                                                                                                                                    int t=e.fi;
                                                                                                      vi key, bcc[N];
                            // _ starts from 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return _;
                                                     namespace BCC{
```

```
6.3 CircleCount
```

```
| struct circle4 {
| static const int N = 1e5 + 7;
| int n, m, u, v, x, y;
| bool vis[N];
| // cnt3,4 中为包含 i 号点的三,四元环数量
| 11 f[N][5], du[N], D[N], cnt4[N], cnt3[N], cnt1[N], t, ans;
| priority_queuepriority_queuepriority_queuepriority_queuepriority_queuepriority_queuepriority_queuepriority_queuepriority_queuepriority_queuepriority_queuepriority_queuepriority_queuepriority_queuepriority_queuepriority_queuepriority_queuepriority_queuepriority_queuepriority_queue
```

```
if(!dfn[t]) dfs(t, g), low[c] = min(low[c], low[t]);
else if(!id[t]) low[c] = min(low[c], dfn[t]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (!dfs(i)) {
    rep(j, 0, tot) col[ans[j]] = col[ans[j] ^ 1] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       bool solve2() { // 构造字典序最小解
for (int i = 0; i < n; i += 2) if (!col[i])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           do{id[st[--st]]=_;}while(st[_st] != c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       col[u] = 1; col[u \land 1] = -1;
for (auto v : g[u]) if (!dfs(v)) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (id[i] == id[i + 1]) return 0;
mark[i >> 1] = (id[i] > id[i + 1]);
void add_at_most_one(vector<pii> vu) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(i, 0, n) if(!dfn[i]) dfs(i, g);
                                              rep(i, 0, sz(vu)) {
    int a = vu[i].fi, va = vu[i].se;
                                                                                                                                                                                                addedge(pre, 1, a, va \wedge 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        for (int i = 0; i < n; i += 2) {
                                                                                                                                                                         addedge(pre, 1, dpi, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (col[u] == -1) return 0;
if (col[u] == 1) return 1;
                                                                                                                          addedge(a, va, dpi, 1);
                                                                                                   int dpi = new_node();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      bool solve() { // 构造任意解
                                                                                                                                                                                                                                                                                                                                                                          dfn[c] = low[c] = ++cc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    fill_n(low, n, _st=0);
                                                                                                                                                                                                                                                                                                                                                      void dfs(int c, vi g[]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(low[c] == dfn[c]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        fill_n(dfn, n, cc=0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int col[N], ans[N], tot;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 0, n) —id[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             fill_n(id, n, _=0);
                                                                                                                                                                                                                                                                                                                                                                                                                            for(auto t : g[c])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ans[tot++] = u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      bool dfs(int u) {
                                                                                                                                                                                                                                                                                                                                                                                                       st[\_st++] = c;
                                                                                                                                                                                                                                                                                                                             // optionals end
                           int pre = -1;
                                                                                                                                                                                                                                                     pre = dpi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void find(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 find();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return;
```

```
for(auto j : g[i]) if(dp[j.se] > md) md = dp[j.se], ne[0][i] = j.se, col = j.fi
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  per(i, 0, M) if(ne[i][u] && cnt[i][u] < k && k <= cnt[i][u] + dp[ne[i][u]]) {
                                                                                                                                                                                                                                                                                                                                                                                        pre[i][j] = (j == 0 ? sp[i] : pre[i][j - 1]) + dp[t.se];
if(t.fi < col) cnt[0][i] = min((11)lim, cnt[0][i] + dp[t.se]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // can handle isolate point and not connected graph and muti edge
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             cn\bar{t}[\bar{i}][\bar{j}] = m\bar{i}n((l1)\bar{l}i\bar{m}, cnt[i-1][j] + cnt[i-1][t]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int p = lower_bound(all(pre[u]), k) - pre[u].begin(); k -= (p == 0 ? sp[u] : pre[u][p - 1]);
                                                                                                                                                                                                                                                                                                 cnt[0][i] = sp[i]; pre[i] = vector<11>(sz(g[i]));
rep(j, 0, sz(pre[i])) {
    pii t = g[i][j];
                                                                                       int ne[M][N]; ll cnt[M][N]; vector<ll> pre[N];
                                                                                                                                                                                const int N = ::N, M = 18, lim = 1e9;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // dcc i->j , i(points) , j(bcc_block)
// st is stack
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, 1, M) rep(j, 1, n + 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(k == 1 && sp[u]) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ne[i][j] = ne[i - 1][t];
                                                    bool sp[N]; 11 dp[N]; // init
                                                                                                                                                  void build(vector<pii> g[]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int t = ne[i - 1][j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // can handle self circle ?
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            k = cnt[i][u];

u = ne[i][u];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int ans = 0, u = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ans += pw(i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          u = g[u][p].se;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // _st is top of stack
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // cactus: n multi by
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     _ is number of dcc
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int qry(int k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  while(1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return ans
  namespace DAG {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // key is cuts
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ++ans
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              namespace DCC{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    DCC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      6.5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ans == 2 * cnt3[i] * D[i]; for (auto v : gg[i]) ans == (D[v] - 1) * D[v]; //第一次重复为第 2 步
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for (auto v : gg[i]) ans3 -= D[v] \dot{} i, ans \dot{} = ans3; // 边数为 3 的链数 for (auto v : gg[i]) ans -= 2 * cnt3[v]; ans += 4 * cnt3[i];
                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 1, 5) rep(j, 1, n+1) for (auto v : gg[j]) f[j][i] += f[v][i-1];
while (!q.empty()) {
    x = q.top().se; y = q.top().fi; q.pop();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ans -= cnt4[i] * 2; 11 ans3 = f[i][3] - D[i] * D[i] - 2 * cnt3[i]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for(auto u : d1) vis[u] = 0; d1.clear(); d2.clear();
                                                                                                                                                                                                     f(', ', ', ', ', ')
D[i] = du[i] = sz(gg[i]); cnt3[i] = cnt4[i] = 0;
for (auto v : gg[i]) g[i].insert(v);
                                                                                  for (auto v : g[u]) if (v != fa) dfs(v, d+1, u);
void dfs(int u, int d, int fa) {
   if (d == 2) { d2.pb(u); w[u].pb(fa); return; }
   if (d == 1) d1.pb(u), vis[u] = 1;
                                                                                                                                                                                                                                                                                                                                                 rt, ±, ...±, r
rep(j, 1, 5) f[i][j] = 0; f[i][0] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 1, n+1) { // 计算边数为 4 的链数
ans = f[i][4];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (vis[u]) cnt3[v]++, t++;
                                                                                                                                                                                                                                                                                                   rep(i, 1, n+1) q.push(mp(du[i], i));
rep(i, 1, n+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  cnt4[x] += s * (s - 1) / 2;

cnt4[u] += s * (s - 1) / 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 d.push(mp(——du[u], u));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (du[x] != y) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 //以第一次产生重复位置分类计数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     cnt3[x] += t / 2; t = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for (auto v : w[u]) {
                                                                                                                                                void solve(int n, vi gg[]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  cnt4[v] += s - 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for (auto u : g[x]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ans -= D[i] * f[i][2];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        //第一次重复为第 4 步
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           //第一次重复为第3步
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             dfs(x, 0, -1);
for (auto u : d2) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         11 s = sz(w[u]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            g[u].erase(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  w[u].clear();
                                                                                                                                                                                     rep(i, 1, n+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  cnt1[i] = ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            } c4;
```

6.4 DAG 割分

vi key , dcc[N];
int dfn[N] , low[N] , st[N] , _st , _;

const int N = 202020;

```
int p = ans[i], x = pos[p].fi.fi, y = pos[p].fi.se, c = pos[p].se;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(j, 1, len+1) {
   if (ss[i][j-1] == '-') rep(k, 1, len+1) ins(i, j, k);
                                                                                                                                                                                                                                                                                                                                     //cout << ans[i] << " \n"[i == ansd - 1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           else ins(i, j, ss[i][j-1] - 'A' + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(i, 1, len+1) cout << ss[i] << endl;
                                                                                              FOR(i, r, 0) if (s[c] > s[i]) c = i;
                                                             Η
                                                                                                                                                                                                                  FOR(j, l, i) restore(col[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       SS[X][y - 1] = C + 'A'
                                                                                                                                                                              FOR(j, r, i) remove(col[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           n = 0; init(len * len * 4);
rep(i, 1, len+1) {
   if (i > 1) cin >> ss[i];
                                                                                                                                                                                                if (dance(dep+1)) return 1;
                                                        if (!r[0]) return ansd = dep,
                                                                                                                                                                                                                                                                                                                   void ins(int x, int y, int c) {
   ပ်
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, 1, ansd) {
1[r[c]] = c; r[1[c]] =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         while (cin >> ss[1]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       bool ok = dance(1);
                                                                                                                                    FOR(i, d, c) {
 ans[dep] = row[i];
                                                                                                                                                                                                                                                          restore(c); return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   cout << endl;
                                    bool dance(int dep) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     tmp.resize(4);
                                                                            int c = r[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (ok) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                              add(n, tmp);
                                                                                                                     remove(c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void work() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    DMST
                                                                                                                                                                                                                                                                                                vi tmp;
```

while(st[--_st]!=t) dcc[st[_st]].pb(_);
dcc[c].pb(_);dcc[t].pb(_++);

if(++out==2) key.pb(c);

low[c]=min(low[c],low[t]);

dfs(t,dep+1,g);

if(low[t]>=dfn[c]){

void dfs(int c,int dep,const vi g[]){ int cc=0, out=1<dep; st[_st++]=c;</pre>

dfn[c]=low[c]=dep; if(!dfn[t]){ for(auto t:g[c])

int solve(int n, const vi g[]){// n is size of points

} else if(dfn[t] != dfn[c] - 1 || cc++) $low[c] = min(low[c]^{'}, dfn[t]);$ rep(i,0,n) **if**(sz(dcc[i]) == 0) dcc[i].pb(_++),

return _;

DLX

6.6

rep(i,0,n) **if**(!dfn[i]) dfs(i,1,g);

fill_n(dcc, n, key=vi());

fill_n(low,n,_st=0);

fill_n(dfn,n,_=0);

```
struct edge {int u, v, d, U, V;bitset<1005> b;};
                             // can handle multi edge,
// id starts from 0
                                                                   FOR(i, u, c) FOR(j, l, i) u[d[j]] = j, d[u[j]] = j, ++s[col[j]]
```

self ring

```
static const int N = 2e4 + 8, D = 4, len = 16;
int n, m, tim, ansd, row[N], col[N], s[N], ans[N], l[N], r[N], u[N], d[N];
pair<pii, int> pos[N]; string ss[100];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    inline void remove(int c) {
    l[r[c]] = l[c]; r[l[c]] = r[c];
    FOR(i, d, c) FOR(j, r, i) u[d[j]] = u[j], d[u[j]] = d[j], --s[col[j]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   l[tim] = tim-1, r[tim] = tim+1, u[tim] = u[c], d[tim] = c;
                                                                                                                                                                                                                      rep(i, 0, m+1) l[i] = i-1, r[i] = i+1, u[i] = d[i] = i; l[0] = m, r[m] = 0, tim = m+1;
                              #define FOR(i, ne, t) for(int i = ne[t]; i := t; i = ne[i])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (sz(tmp)) 1[first] = tim-1, r[tim-1] = first;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  u[c] = tim; d[u[tim]] = tim;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              row[tim] = R, col[tim] = C;
                                                                                                                                                                                                                                                                                                                                                              void add(int R, const vi &tmp){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    inline void restore(int c) {
                                                                                                                                                                                                                                                                                                rep(i, 0, m+1) s[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(i, 0, sz(tmp)) {
    int c = tmp[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    tim++, s[c]++;
                                                                                                                                                              void init(int _m) {
                                                                                                                                                                                                                                                                                                                                                                                               int first = tim;
struct DLX{
```

if (~mins[v] && dfn[sem[mins[v]]] < dfn[sem[mins[u]]]) mins[u] = mins[v];

fs[u] = find(fs[u]);

return fs[u];

int s , t , n , h[N] , cur[N] , 1v[N] , q[N] , e , ne[M] , to[M];
T cap[M] , flow;

const static int N = 10101 , M = N * 10;

struct Dinic{

 $int v = fs[\bar{u}];$

```
/oid liu(int u,int v,T w){ to[e] = v;ne[e] = h[u];cap[e] = w;h[u] = e++;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        T flow = dfs(to[k] , min(mx , cap[k])); ret += flow;cap[k] -= flow , cap[k^1] += flow;mx -= flow;
                       void link(int u,int v,T w){ liu(u , v , w);liu(v , u , \bar{0});}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      vis[u] = stamp; dfn[u] = sz(ord); ord.pb(u);

for (auto v : g[u]) if (vis[v] != stamp) fa[v] = u, dfs(v);
                                                   void ini(int _{-}n = N) { fill(h , h + (n=_n) , -1);e = 0;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(1v[to[k]] == 1v[c] + 1 \&\& cap[k] > 0)
                                                                                                                                                                                                                                            for(int k = h[c]; -k ; k = ne[k])
if(cap[k] > 0 && !~lv[to[k]])
lv[q[R++] = to[k]] = lv[c] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for(int \&k = cur[c]; ~k; k = ne[k]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int fs[N], mins[N], dom[N], sem[N], buf2[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(!mx) return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         flow += dfs(s, ~0U>>1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             copy(h, h + n, cur);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         vi revg[N], g[N], buf[N], ord;
int stamp, vis[N], dfn[N], fa[N];
                                                                                                                                   fill(lv , lv + n , -1);
lv[q[R++] = s] = 0;
while(L < R && !~lv[t]){
                                                                                                                                                                                                                                                                                                                                                                                                                                           if(c == t) return mx;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (u == fs[u]) return u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      DominatorTree
                                                                                                          int L = 0, R = 0;
                                                                                                                                                                                                                    int c = q[L++]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              T run(int _s,int _t){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            S = \_S, t = \_t;
f1Ow = 0;
                                                                                                                                                                                                                                                                                                                                                            return ~lv[t];
                                                                                                                                                                                                                                                                                                                                                                                                                    T dfs(int c,T mx){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               while(bfs()){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    const int N = 1e5 + 7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return flow;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              [v[c] = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         T ret = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void dfs(int u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int find(int u) {
                                                                            bool bfs(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      6.9
                                                                                                                                                                     II
                                                                                                                                        void ini(int n) {this->n = n, m = 0;}
void addedge(int u, int v, int d) {e[m] = edge({u, v, d, u, v}); e[m].reset();e[m].b[m]
                                                                                                                                                                                                                                                                                                                                                                                      if(e[i].d < in[v] && u != v) in[v] = e[i].d, pre[v] = u, index[v] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       while(vis[v] != i && id[v] == -1 && v!=root) vis[v] = i, v = pre[v];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             e[i].u = id[e[i].u]; e[i].v = id[e[i].v];
if(e[i].u != e[i].v) {e[i].d -= in[v];e[i].b ^= e[index[v]].b;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(v != root && id[v] == -1) {
    for(int u=pre[v];u != v;u = pre[u]) id[u] = cnt;
                                                     edge e[M];int n, m, vis[N], pre[N], id[N], index[N], Pre[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(i, 0, n) if(id[i] == -1) id[i] = cnt++;
                           static const int N = ::N, M = N * N, inf = 2e9;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           memset(vis, -1, sizeof(*vis)*n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(in[i] == inf) return -1;
                                                                                                                                                                                                                                                                                                                                                          int u = e[i].u, v = e[i].v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             memset(id, -1, sizeof(*id)*n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ans += in[i]; int v= i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(i == root) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                fang \wedge= e[index[i]].b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int cnt = 0;in[root] = 0;
                                                                                                                                                                                                                                                                                                 rep(i, 0, n) in[i] = inf;
rep(i, 0, m){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    n = cnt; root = id[root];
                                                                                                                                   void ini(int n) {this->n = n,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int t = index[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        id[v] = cnt++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(cnt == 0) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int v=e[i].v;
                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(i, 0, n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i, 0, m) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 0, n){
                                                                                                                                                                                                                    int run(int root){
                                                                              bitset<1005> fang;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // double need eps
                                                                                                                                                                                                                                                    int ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      template<class T>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return ans;
                                                                                                                                                                                                                                                                            while(1){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // [0,n) init!!
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Dinic
                                                                                                            int in[N];
  struct DMST{
                                                                                                                                                                                                 1;m++;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                dmst;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    6.8
```

```
if (sz(cir[k]) > 1 && ne[cir[k][0]] != cir[k][1]) reverse(all(cir[k]));
                                                                                                                                                                                                                                                                                                                if (!dfn[v]) {fa[v] = u; d[v] = d[u] + w; dfs(v, g[u][i].se);}
                                                                                                   int p = u; cir[k].pb(p); id[p] = k;
if (p != v) {do { p = fa[p]; cir[k].pb(p); id[p] = k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            static const int N = 1e5 + 100, M = 17; // (1 << M) > n
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int id[N], tmp[N], n, f[N][M], h[N][M], dep[N];
int v = g[u][i].fi.fi, w = g[u][i].fi.se;
                                   if (dfn[v] && dfn[v] <= dfn[u]) .
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Gomory-HuTree
                                                                                                                                                                         } while (p != v);}
                                                                                                                                                                                                                                                     continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        Dinic<int> G;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         struct GHT{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               6.13
                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (sem[v] == sem[mins[v]]) dom[v] = sem[v]; else buf2[v] = mins[v];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (auto u : ord) if (\sim buf2[u]) dom[u] = dom[buf2[u]];
                                                                      ord.clear(); ++stamp; dfs(s); for (auto u : ord) fs[u] = u, mins[u] = buf2[u] = -1;
                                                                                                                                                                                                                                          if (dfn[v] > dfn[u]) find(v), v = sem[mins[v]];
                                                                                                                                                                       int u = ord[i], p = fa[u]; sem[u] = p;
for(auto v : revg[u]) if (vis[v] == stamp) {
                                                                                                                                                                                                                                                                                                                                                 buf[sem[u]].pb(u); mins[u] = u; fs[u] = p;
per(j, 0, sz(buf[p])) {
   int v = buf[p][j]; find(v);
                                                                                                                                                                                                                                                                             if (dfn[v] < dfn[sem[u]]) sem[u] = v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                dom[ord[0]] = ord[0];
                                                                                                                                      per(i, 1, sz(ord)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             buf[p].clear();
                                void mark(int s) {
```

DualMST

6.10

对偶图最小生成树,等于平面图所有边边权和减去平面图最大生成树

6.11 EulerianPath

5.12 FindCircle

```
// 支持基环树森林和自环重边
const int N = 1e5 + 7;
vector<pair<pre>rector<pair</pre>
// 支持基环树森林和自环重边
const int N = 1e5 + 7;
vector<pair</pre>
int tim, dfn[N], fa[N], M;
vi cir[N];
vi cir[N];
int ne[N]; // 有向图的出度
int id[N]; // 点属于的环编号
void dfs(int u, int pre) { // pre 为边编号
dfn[u] = ++tim;
rep(i, 0, sz(g[u])) {
   if (g[u][i].se == pre) continue;
}
```

```
void ini(int_n) { n = _n; G.ini(n + 5); rep(i, 1, n+1) id[i] = i, g[i].clear(); }
void link(int u, int v, int w) { G.link(u, v, w); G.link(v, u, w);}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (dep[u] < dep[v]) swap(u, v); per(i, 0, M) if (dep[f[u][i]] >= dep[v]) res = min(res, h[u][i]), u = f[u][i];
                                                                                         void solve(int 1, int r) {
   if (1 == r) return;
   int s = id[1], t = id[1+1];
   for(int i = 0; i < 6.e; i += 2) 6.cap[i] += 6.cap[i+1], 6.cap[i+1] = 0;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            h[v.fi][i] = min(h[v.fi][i-1], h[f[v.fi][i-1]][i-1]);
                                                                                                                                                                                                                                                                                                                                                   rep(i, l, r+1) {
if (G.lv[id[i]] != -1) id[cl++] = id[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(i, 1, M) {
f[v.fi][i] = f[f[v.fi][i-1]][i-1],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void build() { solve(1, n); dfs(1, 0); } int get(int u, int v) { // 注意 long long
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for (auto v : g[u]) if (v.fi != fa) {
  f[v.fi][0] = u; h[v.fi][0] = v.se;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 0, cr) id[cl + i] = tmp[i];
                                                                                                                                                                                                                                                                                                                                                                                                                           else tmp[cr++] = id[i]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void dfs(int u, int fa) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   dep[u] = dep[fa] + 1;
                                                                                                                                                                                                                            int w = G.run(s, t);
                                                                                                                                                                                                                                                                                                                     int cl = 1, cr = 0;
                                                                                                                                                                                                                                                          g[s].pb(mp(t, w));
                                                                                                                                                                                                                                                                                               g[t].pb(mp(s, w));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    solve(1, c1 - 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int res = pw(30);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             dfs(v.fi, u);
vector<pii> g[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       solve(cl, r);
```

```
* 对于一张无边权的 DAG 图, 给定 n 个起点和对应的 n 个终点,这 n 条不相交路径的方案数为矩阵
                              * e(a1, b1), e(a1, b2)...e(a1, bn)
                                                                 * e(a2, b1), e(a2, b2)...e(a2, bn)
                                                                                                                                                                 * e(an, b1), e(an, b2)...e(an, bn)
                                                                                                                                                                                                  的行列式
per(i, 0, M) if (f[u][i] != f[v][i]) res = min(res, min(h[u][i], h[v][i])), u = f[\ |\ ]
                                                               if (u != v) res = min(res, min(h[u][0], h[v][0]));
                                   u][i], v = f[v][i];
                                                                                                    return res;
                                                                                                                                                              } tr;
```

KM6.14

```
* 即 M[i][j]=e(ai,bj)
* e(a,b) 为 a 到 b 的路径方案数
                                                                                                                                                      × × × ×
                                                                                                6.16
                                                                                                                                                                                                                            6.17
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 0, m+1) if (used[i]) Lx[left[i]] = d, Ly[i] += d;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     T tmp = Lx[left[u]] + Ly[i] - g[left[u]][i];
if (tmp < slack[i]) slack[i] = tmp, pre[i] = u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for(; u != m; left[u] = left[pre[u]], u = pre[u]);
                                                                                                                                                                                                                                                                                                                                    void go(int now) {
    rep(i, 0, m+1) used[i] = 0, slack[i] = inf;
                                                                                                                                                                                                                                                                                      rep(i, 0, n) rep(j, 0, m) g[i][j] = -inf;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (slack[i] < d) d = slack[v = i]
                                                                                                                                                                                               int n, m, left[N], pre[N], used[N];
                                                                                                                                                                                                                       T g[N][N], Lx[N], Ly[N], Slack[N]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 0, m) if(!used[i]) {
                                                                                                                                                                                                                                                                                                                                                                                                                           for(u = m; ~left[u]; u = v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(i, 0, n) ans += Lx[i];
rep(i, 0, m) ans += Ly[i];
                                                                                                                                                                        static const T inf = ~0U>>2;
                                                                                                                                                                                                                                              void ini(int _n, int _m) {
                                        // init!! , id starts from 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     else slack[i] -= d;
                                                                                                                                                      static const int N = 505;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             fill_n(left, m, -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, n) go(i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  fili_n(Lx, n, 0);
fill_n(Ly, m, 0);
                                                                                                                                                                                                                                                                 n = _n, m = _m;
                                                                                                                                                                                                                                                                                                                                                                                                                                                      used[u] = 1;
                                                                                                                                                                                                                                                                                                                                                                                     left[m] = now;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            T d = inf;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return ans;
                                                                                                          template<class T>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                T ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                          int u, v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              T run() {
                                                                                                                               struct KM {
                                                                // n <= m
```

Manhattan distance --> Chebyshev distance Chebyshev distance --> Manhattan distance - y >> 1(x + y, x - y) (x + y > 1, x)

ManhattanDistance

ManhattanDistanceMST

```
rep(i, 0, sz(v)) v[i].fi.se -= v[i].fi.fi, V.pb(v[i].fi.se);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int F(int x) { return lower_bound(all(V), x) - V.begin() + 1;
                                                                                                                                                                                                                                                                                                                                                                                                           void init() { rep(i, 1, sz(V) + 1) mi[i] = mp(inf, inf);
void upd(int p, pii c) {
    p = sz(V) + 1 - p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for( ; p <= SZ(V); p += Ib(p)) mi[p] = min(mi[p], c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          For( ; p >= 1; p ^{-1} lb(p)) ans = min(ans, mi[p]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void _solve(vector<pair<pre>ctor<pair</pre>ctor<pair</pre>ctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctorctor</pr
                                                                                                                                                                                                                                                                                                         // 最大只要把这里所有 mi 改成 ma 就行了
                                                                                                                                                        const int N = 101010, inf = 1e9 + 7;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          V.erase(unique(all(V)), V.end());
// 曼哈顿最小距离生成树(可以求最大)
// 这份代码处理的区域是 Y 轴右转 45
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        p = sz(V) + 1 - p;
pii ans = mp(inf, inf);
                                                                                                                                                                                                       vector<pair<int, pii> > E;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            reverse(all(v));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      pii qry(int p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   sort(all(V));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             sort(all(v))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return ans;
                                                                                                     namespace MMST {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             V.clear();
                                                                                                                                                                                                                                                                                                                                                                    pii mi[N];
```

Lindstrom Gessel Viennot Lemma 6.15

if(t.se != inf) E.pb(mp(t.fi - s, mp(t.se, u.se)));

upd(F(u.fi.se), mp(s, u.se));

pii t = qry(F(u.fi.se));
int s = u.fi.fi * 2 + u.fi.se;

For (auto u : v) {

init();

for(int u = ctz(z); u < n; u + ctz(z >> (u + 1)) + 1) {

gao(cur | (1ull << u), can & g[u], ban & g[u]), can ^= 1ull << u, ban |= 1ull << u;

```
6.19 Max clique BK
                                                                                                        g[i][i] should be
                                                                                                                          // g[i] is i's edge
                                                                                                                                                  // index [0..N)
// 0(3 ^ (n / 3))
                                    rep(i, 0, sz(v)) swap(v[i].fi.fi, v[i].fi.se);
_solve(v);
                                                                                                     _solve(v);
rep(i, 0, sz(v)) swap(v[i].fi.fi, v[i].fi.se);
void solve(vector<pair<pii, int> > v) {
                                                                               rep(i, 0, sz(v)) v[i].fi.fi *= -1;
                   solve(v);
                                                                                                                                                   solve(v);
```

6.18 MaxMatch

```
if(!link[v] || dfs(link[v], g)) { return link[v] = u, 1; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     fill_n(vis, n+1, 0);
per(i, 1, n+1) link[link[i]] = i;
rep(i, 1, n+1) if (!link[i]) vis[i] = use[i] = 1, Q.push(i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 1, n+1) if (link[i] && !use[link[i]]) use[i] = 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (!vis[v]) vis[v] = 1, 0.push(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (!vis[v]) vis[v] = 1, 0.push(v);
                                            int link[N], vis[N], use[N], in[N];
                                                                                                                                                                                                                                                                                                              int solve(int n, int m, vi g[]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int u = Q.front(); Q.pop();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for (auto v : g[u]) { use[v] = 2;
                                                                                                                                                                                                                                                                                                                                                                               rep(i, 1, n+1) {
fill_n(vis, m+1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void MVC(int n, vi g[]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int v = link[u];
                                                                                        int dfs(int u, vi g[]) {
                                                                                                              for(auto v : g[u]) {
   if(!vis[v]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (use[u] == 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           while (!Q.empty()) {
                                                                                                                                                                                                                                                                                                                                                                                                                               ret += dfs(i, g);
                                                                                                                                                                                                                                                                                                                                    fill_n(link, m+1,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           use[v] = 1;
                                                                                                                                                                    vis[v] = 1;
                      const int N = 1050;
namespace MaxMatch {
                                                                                                                                                                                                                                                                                                                                                            int ret = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return ret;
                                                                       queue<int> 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 }else {
                                                                                                                                                                                                                                                                return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return;
```

```
// g[i][i] should be 0
// g[i] is i's edge
// index [0..N)
// o(3 ^ (n / 3))

typedef unsigned long long T;

struct BK {
    static const int N = 100; T g[N];
    inline int ctz(T s){    return s ? __builtin_ctzll(s) : 64;}
    int n, ans;

    void ini(int _n) {
        //per(i, 0, n = _n) g[i] = 0;
        rep(i, 0, n) g[i] = 0;
        rep(i, 0, n) rep(j, 0, n) if (a[i][i]) g[i] |= 1ull << j;
    }

    void gao(T cur, T can, T ban) {
        if (!can && !ban) { ans = max(ans, __builtin_popcountll(cur)); return; inf piv = ctz(can | ban), ret = 0;
        T z = can & ~g[piv];
</pre>
```

$6.20~{ m Max_clique_fastest}$

int run() { gao(ans = 0, (1ull << n) - 1, 0); **return** ans; }

```
Maxclique(BB *conn, int sz, const db tt = 0.025): pk(0), lv(1), Tlimit(tt) {
                                                                                                                                                        //cc : ColorClass
                                                                                  //ves: Vertices
                                                                                                                                                                                                                                                                                                                                                                                                                          void deg_sort(ves &R) { set_deg(R); sort(all(R), desc_deg); }
                                                                                                                                                                                                                                                rep(i, 0, sz) V.pb(ve(i)); e = conn;
                                                                                                                                    typedef vector<ve> ves; ves V;
typedef vector<int> cc; cc Q, QMAX;
                                                             const BB *e; int pk, lv; db Tlimit;
                                                                                                                                                                                                                                                                   C.resize(sz + 1);
                                                                                                                                                                                                                                                                                         S.resize(sz + 1)
                      typedef bool BB[N];
const int N = 130
                                            struct Maxclique
                                                                                                                                                                             vector<cc> C;
                                                                                                                                                                                                   vector<sc> S;
```

```
for(p = t;p != s;p = to[k^1]) pl = min(pl, cap[k = pre[p]]);

for(p = t;p != s;p = to[k^1]) cap[k = pre[p]] -= pl, cap[k^1] += pl;
int c = Q.front(); Q.pop(); ing[c] = 0;
for(int k = h[c]; -k; k = ne[k]) if (cap[k] > 0) {
                                                                                                                                                                                    if(!ing[v]) Q.push(v) , ing[v] = 1;
                                                                                   if(dis[c] + cost[k] < dis[v]){
  dis[v] = dis[c] + cost[k];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int dfn[N], low[N], id[N], st[N],_st,_,cc;
                                                                                                                                                                                                                                                                                                                                                                                                 _t){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                U pl = inf; int p, k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return mp(flow, mincost);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      mincost += pl * dis[t];
                                                                                                                                                   pre[v] = k;
                                                                int v = to[k];
                                                                                                                                                                                                                                                                                                                                                                                             s, int
                                                                                                                                                                                                                                                                                                     return dis[t] != inf;
                                                                                                                                                                                                                                                                                                                                                                                                                             s = \_s, t = \_t;
flow = mincost = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            void dfs(int c,vi g[]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          dfn[c]=low[c]=++cc
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                const int N = 100050
                                                                                                                                                                                                                                                                                                                                                                                             pair<U, V> run(int
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        flow += pl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    while(spfa()){
                                                                                                                                                                                                                                                                                                                                                                 U flow; V mincost;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      st[_st++]=c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // _ starts from 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       namespace SCC{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        6.22
  bool cut1(int pi , cc &va) { rep(i, 0, sz(va)) if (e[pi][va[i]]) return true; return |
                                                            void cut2(ves &va, ves &vb) { rep(i, 0, sz(va) - 1) if (e[va.back().i][va[i].i]) vb.
                                                                                                                                                                                                                                                                                                                                                                                                                        rep(k, min_k, maxno + 1) rep(i, 0, sz(C[k])) R[j].i = C[k][i], R[j++].d = k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void mcqdyn(int *mxc, int &sz) { // mcqdyn(int maxclique, int &siz)
                                                                                                                                                                                                                                                                                                     if (k > maxno) C[(maxno = k) + 1].clear(); C[k].pb(pi);
if (k < min_k) R[j++].i = pi;</pre>
                                                                                                                                                 int j = 0, maxno = 1, min_k = max(sz(QMAX) - sz(Q) + 1,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       set_deg(V); sort(all(V), desc_deg);
ini_col(V); rep(i, 0, sz(V) + 1) S[i].a = S[i].b = 0;
exp_dyn(V); per(i, 0, sz(QMAX)) mxc[i] = QMAX[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (sz(Rp)) {
   if ((db) S[lv].a / ++pk < Tlimit) deg_sort(Rp);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for (; sz(R); Q.pop_back(), R.pop_back()) {
   if (sz(Q) + R.back().d <= sz(QMAX)) return;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 else if (sz(Q) > sz(QMAX)) QMAX = Q;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                co_sort(Rp); S[lv++].a++;
                                                                                                                                                                                                                                                                       while (cut1(pi, C[k])) k++;
                                                                                                                                                                               rep(i, 1, 3) C[i].clear();
rep(i, 0, sz(R)) {
int pi = R[i].i, k = 1;
                                                                                                                                                                                                                                                                                                                                                                                          if (j > 0) R[j - 1].d = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        exp_dyn(Rp); —1v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            S[1v].b = S[1v - 1].a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ves Rp; cut2(R, Rp);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Q.pb(R.back().i);
                                                                                                                        void co_sort(ves &R) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   sz = sz(QMAX);
                                                                                       pb(va[i].i); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       6.21
```

```
rep(i,0,n) for(auto j:g[i]) if(id[i]!=id[j]) ng[id[i]].pb(id[j]);
for(auto t:g[c])
   if(!dfn[t]) dfs(t,g),low[c]=min(low[c],low[t]);
   else if(!id[t]) low[c] =min(low[c],dfn[t]);
if(low[c]==dfn[c]){
                                                                                                                                    do{id[st[---st]]=_;}while(st[_st]!=c);
                                                                                                                                                                                                                                                                                                                                                rep(i,0,n) if(!dfn[i]) dfs(i,g);
                                                                                                                                                                                                                                         int solve(int n, vi g[]){
                                                                                                                                                                                                                                                                                               fill_n(low, n, _st=0);
                                                                                                                                                                                                                                                                                                                                                                             rep(i, 0, n) \longrightarrow id[i]
                                                                                                                                                                                                                                                                      fill_n(dfn, n, cc=0)
                                                                                                                                                                                                                                                                                                                       fill_n(id,n,_=0);
                                                                                                                                                                                                                                                                                                                                                                                                          fill_n(ng, _, vi())
                                                                                                                                                                                                                                                                                                                                                                                                                                                            return _;
                                                                                                                                                                                                                vi ng[N];
                                                                                                                                                                                                                                                                                                   П
```

```
MinCostMaxFlow
```

```
int h[N], ing[N], pre[N], to[M], ne[M], e, s, t, n;
U cap[M]; V dis[N], cost[M];
void ini(int _n = N){ fill(h , h + (n=_n) , -1);e = 0;}
void liu(int u,int v,U c,V w){ to[e] = v;ne[e] = h[u];cap[e] = c;cost[e] = w;h[u]
                                                                                                                                                                                                                                                                                                                                      void link(int u,int v,U c,V w){ liu(u,v,c,w);liu(v,u,0,-w);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Q.push(s), ing[s] = 1, dis[s] = 0;
                                                                                                          static const int N = 6000, M = 201010,
// [\mathtt{0},\mathtt{n}) , init!! , inf modify
                                                                                                                                                                                                                                                                                                                                                                                                                                                   fill(dis, dis+n, inf);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            while(!Q.empty()){
                                     template<class U, class V>
                                                                                                                                                                                                                                                                                                                                                                                                                    queue<int> 0;
                                                                                                                                                                                                                                                                                                                                                                              bool spfa().
                                                                             struct MCMF{
```

```
t1), node(i, j, t2));
                                                                                                                                for (int t = msk \& (msk - 1); t > 0; t = (t - 1) \& msk)
                                                                                                                                                                                                                                  if (z > w) z = w, pre[msk][i][j] = mp(node(i, j,
                                                                                                                                                               int t1 = t | st[i][j], t2 = msk ^ t | st[i][j];
int w = dp[t1][i][j] + dp[t2][i][j] - a[i][j];
                                                                                                                                                                                                                                                                                                   if (z < inf) q.push(mp(i, j)), vis[msk][i][j] = 1;
                              rep(j, 1, m+1) {
    if (st[i][j] && !(st[i][j] & msk)) continue;
    int &z = dp[msk][i][j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 1, n+1) rep(j, 1, m+1) if (ans > dp[S][i][j]]) ans = dp[S][i][j], now = node(i, j, S);
rep(i, 1, n+1)
                                                                                                                                                                                                                                                                                                                                                                        spfa(msk);
                                                                                                                                                                                                                                                                                                                                                                                                                                      ans = inf;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          dfs(now);
```

SteinerTree

6.23

```
rep(i, 1, n+1) if (!vis[i] && !use[i] && val[i] >= ma) ma = val[i], t = i;
                                                                                                                                                                                                                            void add_edge(int u, int v, int w) { g[u][v] += w; g[v][u] += w; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(i, 1, n+1) if (!vis[i] && !use[i]) val[i] += g[t][i];
                                                                                                                                                                                                                                                                                                                                                                                                                                  int MinimumCutPhase(int cnt, int &s, int &t) {
                     static const int N = 305, INF = 0x3f3f3f3f;
                                                                                                                                                                        rep(i, 1, n+1) fill_n(g[i] + 1, n, 0);
                                                                                                                           n = _n;
fill_n(use + 1, n, 0);
                                                                                                                                                                                                                                                                                                     g[v][i] += g[u][i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                           fill_n(val + 1, n, 0);
fill_n(vis + 1, n, 0);
                                                                                                                                                                                                                                                                                                                              g[i][v] += g[i][u];
                                                                                                                                                                                                                                                      void merge(int u, int v)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (!ma) return 0;
                                                int n, g[N][N], val[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             vis[s = t] = 1;
                                                                        bool vis[N], use[N];
                                                                                               void init(int _n) {
                                                                                                                                                                                                                                                                                 rep(i, 1, n+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    while (—cnt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int ma = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int res = INF;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return val[t];
struct StoerWagner{
                                                                                                                                                                                                                                                                                                                                                                                 use[u] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int solve() {
```

for (**int** i = n, s, t; i > 1; —i) {

```
StoerWagner\_O(n3)
```

return ans == inf ? -1 : ans;

```
z = w, pre[t][nx][ny] = mp(node(x, y, msk), node(x, y, 0));
if (t == msk && ivis[msk][nx][ny]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i, 0, 4) {
   int nx = x + dx[i], ny = y + dy[i], t = msk | st[nx][ny];
   if (nx > n || nx < 1 || ny > m || ny < 1) continue;
   if (nx > n || nx < 1 || ny > m || ny < 1)</pre>
                                                                                                                                                                                                                                                                               node(int \times = 0, int y = 0, int msk = 0):x(x), y(y), msk(msk){}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int &z = dp[t][nx][ny], w = dp[msk][x][y] + a[nx][ny];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         pre[pw(k++)][ij[j] = mp(node(0, 0, 0), node(0, 0, 0));
                                                             int n, m, k, a[N][N], st[N][N], dp[1 << M][N][N][N], S,
bool use[N][N], vis[1 << M][N][N];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               pair<node, node> t = pre[now.msk][now.x][now.y];
// 要视图的情况使用 spfa, dijstra, 多源 bfs
const int N = 11, M = 10, inf = 0x3f3f3f3f
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              vis[msk][nx][ny] = 1;
                                                                                                                                                                                                                                                                                                                                            pair<node, node> pre[1 << M][N][N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               d.push(mp(nx, ny));
                                                                                                                                                                                                                                                                                                                                                                                                                                   pii u = q.front(); q.pop();
int x = u.fi, y = u.se;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(i, 1, n+1) rep(j, 1, m+1)
cin >> a[i][j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        memset(dp, 0x3f, sizeof(dp))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int SteinerTree(int n, int m)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             dp[pw(k)][i][j] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      node t1 = t.fi, t2 = t.se
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (!a[i][j]) {
    st[i][j] = pw(k);
                                                                                                                        int dx[] = {1, -1, 0, 0};
int dy[] = {0, 0, 1, -1};
queue<pii> q;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              vis[msk][x][y] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   use[now.x][now.y] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                    while (!q.empty()) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (t2.msk) dfs(t2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(msk, 1, S+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (!t1.x) return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     \mathbf{if} (z > w) 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void dfs(node now) {
                                                                                                                                                                                                                                                                                                                                                                          void spfa(int msk)
                                                                                                                                                                                                                                                  int x, y, msk;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     S = pw(k) - 1;
                                                                                                                                                                                                               struct node {
```

```
void ini(int _n = N){ fill(h , h + (n=_n) , -1);e = 0;}
void liu(int u,int v,U c,V w){ to[e] = v;ne[e] = h[u];cap[e] = c;cost[e] = w;h[u] =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(!v[t] \& cap[k] > 0) Min = min(Min , dis[t] + cost[k] - dis[c]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(c == t) return flow += mx , mincost += mx * dis[s] , mx;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(!v[t] \& act[k] > 0 \& dis[c] - cost[k] == dis[t])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   void link(int u,int v,U c,V w){ liu(u,v,c,w);liu(v,u,0,-w);
                                                                                                                                                                                                                                                                                                                                                                                                                     int h[N] , ing[N] , v[N] , to[M] , ne[M] , e , s , t , n;
U cap[M];V dis[N] , cost[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(!ing[v]) Q.push(v), ing[v] = true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              U tmp = dfs(t , min(cap[k] , mx - ret));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(c,0,n) if(v[c]) for(int k=h[c];-k;k=ne[k]){
int t=to[k];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int c = Q.front();Q.pop();ing[c] = false;
res = min(res, MinimumCutPhase(i, s, t));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(cap[k^1] <= 0) continue;
if(dis[c] + cost[k^1] < dis[v]){
    dis[v] = dis[c] + cost[k^1];</pre>
                                                                                                                                                                                                                                                                                                                                                                                     static const int N = 1010, M = 40404;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(i, 0, n) if(v[i]) dis[i] += Min;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for(int k=h[c]; \sim k; k=ne[k]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(Min == inf) return false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for(int k=h[c];~k;k=ne[k]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ing[t] = true, dis[t] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        v[c] = true; U ret = 0;
                                                                                                                                                                                                                                                                                                      // [0,n) , init!! , inf modify
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int v = to[k]
                           if (res == 0) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           fill(dis,dis+n,inf);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int t = to[k];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    while(!Q.empty()){
                                                                                                                                                                                                                                                                                                                                   template<class U, class V>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               U dfs(int c,U mx){
                                                          merge(s, t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              queue<int> 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       U flow;V mincost;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                bool modlable(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  V Min = inf
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Q.push(t);
                                                                                                                   return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   void spfa(){
                                                                                                                                                                                                                                    ZKW
                                                                                                                                                                                                                                                                                                                                                              struct ZKW{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            6++;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         while (!q.empty() && (vis[q.top().se] || val[q.top().se] != q.top().fi)) q.pop
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int findset(int u) { return u == fa[u] ? u : fa[u] = findset(fa[u]); }
                                                                                                                                                                                                                                                                                                                                                            int head[N], val[N], e, n, to[M], ne[M], data[M], fa[N], link[N];
                                                                                                                                                                                                                                                                                                                               static const int N = 3005, M = 1000005 * 2, INF = 0x3f3f3f3f
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       to[e] = v; data[e] = w; ne[e] = head[u]; head[u] = e++; to[e] = u; data[e] = w; ne[e] = head[v]; head[v] = e++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (!vis[v]) q.push(mp(val[v] += data[p], v));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (int p = head[u]; -p; p = ne[p]) {
   int v = findset(to[p]);
res = min(res, MinimumCutPhase(i, s, t));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int MinimumCutPhase(int cnt, int &s, int &t) {
                                                                                                                                                                                                                                    {
m StoerWagner\_O(nmlog(m))}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for (int u = s; ~u; u = link[u]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for (int i = n, s, t; i > 1; —i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void add_edge(int u, int v, int w) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     while (-link[p]) p = link[p];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (q.empty()) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               t = q.top().se; q.pop();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 1, n+1) fa[i] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           fill_n(link + 1, n, -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                      n = _n;
fill_n(head + 1, n, -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void merge(int u, int v) {
                           if (res == 0) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    fill_n(val + 1, n, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               fill_n(vis + 1, n, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              priority_queue<pii> q;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         while (—cnt) {
   vis[s = t] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                     void init(int _n) {
                                                        merge(s, t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int solve() {
  int res = INF;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return val[t];
                                                                                                                                                                                                                                                                                                      struct StoerWagner{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  link[p] = v;
                                                                                                                     return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  fa[v] = u;
                                                                                                                                                                                                                                                                                                                                                                                         bool vis[N]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        6.25
                                                                                                                                                                           } SW;
```

```
val[p] = val[ori], id[p] = id[ori], ht[p] = ht[ori];
                                                                                                                                                                                                                          inline int newnode(db _val, int _id, int _dis = 0){
                                                                                                                                                                          int ls[M*B], rs[M*B], ht[M*B], id[M*B], tot;
                                                                                                                                                                                                                                                                          val[p] = _val, id[p]=_id, ht[p] = _dis;
                                                                                                                                                                                                                                                                                                                                                                                                                                                    ls[p] = ls[ori], rs[p] = rs[ori];
fa[v] = u; tree[i] = 1;
                                                                                                                                                                                                                                                                                                                                                                           inline int _copy(int ori){
                                                                                                                                                                                                                                                                                                  ls[p] = rs[p] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                      int p = ++tot;
                                                                                                                                                                                                                                                     int p = ++tot;
                          dfs(v);
                                                                                                                                                                                                 db val[M*B];
                                                                                                                                                                                                                                                                                                                               return p;
                                                                                                                                                     namespace LT{
                                                                                                                          int rt[N];
 cap[k] —= tmp , cap[k^1] += tmp;
                                                 if(ret == mx) return ret;
                                                                                                                                                                                                                                                   flow = mincost = 0;
do do memset(v,0,sizeof(v[0])*n);
                                                                                                                                                                                                                                                                                                                                                    return make_pair(flow , mincost)
                                                                                                                                                                          pair<U,V> run(int _s,int _t){
                                                                                                                                                                                                                                                                                                      while(dfs(s,inf));
                          ret += tmp;
                                                                                                                                                                                                                                                                                                                             while(modlable());
                                                                                                                                                                                                   s = _{-}s , t = _{-}t;
                                                                                                                            return ret;
                                                                                                                                                                                                                              spfa();
```

k短路 6.27

```
if (!tree[i] && dis[v] < inf) LT::ins(rt[u], dis[v] - dis[u] + g.w[i], v);
                                                                                                                                                                                                                                                                                                                                        inline void ins(int &rt, db val, int id){ rt = merge(rt, newnode(val, id)); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (rt[o]) pq.push(mp(w + LT::val[rt[o]], rt[o]));
if (ls) pq.push(mp(w + LT::val[ls] - LT::val[u], ls));
                                                                                                                                                                                                           if(ht[ls[now]] < ht[rs[now]]) swap(ls[now],rs[now]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (rt[S]) pq.push(mp(dis[S] + LT::val[rt[S]], rt[S]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              priority_queue<pdi, vector<pdi>, greater<pdi> > pq;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     E -= w; if (E >= 0) ++ans; else return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   db w = t.fi; int u = t.se, o = LT::id[u];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for (int i = g.h[u]; i ; i = g.ne[i]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int ls = LT::ls[u], rs = LT::rs[u];
                                                                                                                     if(val[a] > val[b]) swap(a, b);
                                                       inline int merge(int a, int b){
                                                                                                                                               int now = _copy(a);
rs[now] = merge(rs[now], b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    pdi t = pq.top(); pq.pop();
                                                                                                                                                                                                                                             ht[now] = ht[rs[now]] + 1;
                                                                                      if(!a || !b) return a|b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int ans = 1; E = dis[S];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    typedef pair<db, int> pdi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rt[u] = rt[fa[u]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int v = g.to[i]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       while(!pq.empty()) {
                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(j, 1, top+1) {
    int u = st[j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           inline int calc_K(){
                                                                                                                                                                                                                                                                                                                                                                                                 void build_heap(){
                                                                                                                                                                                                                                                                              return now;
return p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ф
Е;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (!vis[v] && fabs(dis[v] - dis[u] - rg.w[i]) <= eps) {</pre>
                                                                                                                                                                                                                                                                                                                                                                           ne[++e] = h[u], h[u] = e, to[e] = v, w[e] = val;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int v = rg.to[i];
if (dis[v] > dis[u] + rg.w[i] + eps) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for (int i = rg.h[u]; i; i = rg.ne[i]) {
                                                           // time : O(klogk + mlogn) space : O(nlogn)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int i = rg.h[u]; i; i = rg.ne[i]) {
                                                                                                                                                                                                                                                                                                                                            inline void add(int u, int v, db val){
                                                                                                                                                                                     bool vis[N], tree[M];
int n, m, S, T, fa[N], st[N], top, u, v;
struct Graph{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if (vis[u]) continue; vis[u] = 1;
                                                                                          const int N = 5050, M = 200005, B = 20,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       dis[v] = dis[u] + rg.w[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  priority_queue<pair<db, int> > pq;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int u = pq.top().se; pq.pop();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   pq.push(mp(-dis[v], v));
                                                                                                                          const db eps = 1e-9, inf = 1e16;
                          // S -> T 可重复经过点的第 K 短路
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(i, 1, n+1) dis[i] = inf;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    pq.push(mp(dis[T] = 0, T));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       st[++top] = u; vis[u] = 1;
                                                                                                                                                                                                                                                                                int h[N], ne[M], to[M], e;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              while(!pq.empty()){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int v = rg.to[i]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void dfs(int u){
                                                                                                                                                           db dis[N], w;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void Dij(){
                                                                                                                                                                                                                                                                                                                    db w[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                               } g, rg;
```

1a 有源汇额外增加的 t->s 的边编号

o = -1 有源汇最小流

/* o = 0 无源汇可行流 0 = 1 有源汇最大流

```
rep(i, 0, n) if (a[i] < 0) link(i, tt, -a[i]); else link(ss, i, a[i]), need += a[i
                                                                                                                                                                                                                                                                               void link(int u, int v, T wl, T wr) { // wl \le wr
                                                                                                                                                                                                                                                                                                                         use[++m] = wl; id[m] = e + 1;
                                                                                                                                                    copy(h , h + n , cur);
flow += dfs(s, ~0U>>1);
                                                                                                                                                                                                                                                                                                                                                                                                                ss = n - 2; tt = ss + 1;
                                                                                                                                                                                                                                                                                                        a[u] = wl; a[v] += wl;
                                                                                                                                                                                                                                                                                                                                                link(u, v, wr - wl);
                                                               T run(int _s,int _t){
                                                                                   S = _{-}S, t = _{-}t;
flow = 0;
                                                                                                                              while(bfs()){
                                                                                                                                                                                                                   return flow;
lv[c] = -1;
                       return ret;
                                                                                                                                                                                                                                                                                                                                                                                       void build() {
if (rs) pq.push(mp(w + LT::val[rs] - LT::val[u], rs));
                                                                                                                                                                                                                                                                                                                       rep(i, 1, n+1) vis[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                          cout << calc_K() << endl;
                                                                                                     ios::sync_with_stdio(0);
                                                                                                                                                                                                                cin >> u >> w;
                                                                                                                                                                                                                                                                rg.add(v, u, w);
                                                                                                                                                    cin >> n >> m >> E;
                                                                                                                                                                                                                                         g.add(u, v, w);
                                                                                                                                                                                          rep(i, 1, m+1) {
                                                                                                                                                                          S = 1; T = n;
                                                                                                                                                                                                                                                                                                                                                                    build_heap();
                                                                                                                              cin.tie(0);
                                             return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                 return 0;
                                                                                   int main(){
                                                                                                                                                                                                                                                                                                                                                  dfs(T);
                                                                                                                                                                                                                                                                                                   Dij();
```

上下界网络流 6.28

```
void link(int u, int v,T w){ liu(u, v, w);liu(v, u, 0);}
void ini(int _n = N) { fill(h, h + (n=_n), -1); fill(a, a + n, 0); e = m = need =
                                                      const static int N = 10101 , M = N * 50;
int s, t, n, h[N], cur[N], lv[N], q[N], e, ne[M], to[M], m, ss, tt, id[M];
T cap[M], flow, use[M], need, a[N];
                                                                                                                                                    void liu(int u,int v,T w){ to[e] = v;ne[e] = h[u];cap[e] = w;h[u] = e++;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         T flow = dfs(to[k] , min(mx , cap[k])); ret += flow;cap[k] -= flow , cap[k^1] += flow;mx -= flow;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(lv[to[k]] == lv[c] + 1 && cap[k] > 0){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               lv[q[R++] = to[k]] = lv[c] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for(int k = h[c]; ~k; k = ne[k])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(cap[k] > 0 && !~lv[to[k]])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for(int &k = cur[c]; \simk; k = ne[k]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(!mx) return ret;
                                                                                                                                                                                                                                                                                                                                              fill(lv , lv + n , -1);
lv[q[R++] = s] = 0;
while(L < R && !~lv[t]){
int c = q[L++];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(c == t) return mx;
                                                                                                                                                                                                                                                                                                                     int L = 0, R = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           T dfs(int c,T mx){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return ~lv[t];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              T ret = 0;
template<class T>
                                                                                                                                                                                                                                                                                  bool bfs(){
                             struct Dinic{
```

仙人掌最短路 6.29

if (0 == 1) flow += run(:: s, :: t);

else flow -= run(::t, ::s);

 $cap[::1a] = cap[::1a \land 1] = 0;$

if (flow != need) return -1; flow = cap[::la ^ 1];

if (0 != 0) {

T flow = run(ss, tt);

int run(int 0) {

build();

rep(i, 1, m+1) use[i] += cap[id[i]];

return flow;

```
B)
                                                                                          如果是方点, ans = dep[a] + dep[b] - dep[A] - dep[B] + dis(A)
                             圆圆边边权不变,圆方边边权是圆点到它所在环的根的最短距离。
如果询问两点的 1ca 是圆点, ans = dep[a] + dep[b] - dep[1ca]
* 建出圆方树, 选任意圆点作为根, 环的根指的是环上深度最小的点。
```

前向星 6.30

per(i, 1, n+1) { // 色数 for (auto v : g[a[i]]) use[col[v]] = i;

ans = 0;

for (auto v : g[u]) {
 ins(++lab[v], v);
 ma = max(lab[v], ma);

a[i] = u, vis[u] = 1;

static int rk[N][N], d[N][N];
rep(i, 0, n) rep(j, 0, n) d[i][i] = g[i][i], rk[i][i] = j;
rep(k, 0, n) rep(i, 0, n) rep(j, 0, n)
d[i][i] = min(d[i][i], d[i][k] + d[k][i]);
rep(i, 0, n) sort(rk[i], rk[i] + n, [&](int a, int b) {return d[i][a] < d[i][b];});</pre>

u = to[h[ma]]; del(ma);

while (1) {

if (!vis[u]) break

e = ma = 0; // 完美消除序列

rep(i, 1, n+1) ins(0, i); per(i, 1, n+1) $\{$

const int N = 1e3 + 7, inf = 1e9 + 7;

// g[i][i] should be 0

// id : 0 .. n-1// time : $0(n \wedge 3)$

图绝对中心

6.31

int n, m, g[N][N], u, v, w;

pii GraphCenter(int n, int g[][N]) {

(n)qd.[v]b; (v)qd.[n]b

rep(i, 0, m) { cin >> u >> v;

cin >> n >> m;

rep(j, 1, n+1) if (use[j] != i) col[a[i]] = j;

ans = max(ans, col[a[i]])

break;

```
ma;
                                 int ans, use[N], col[N], lab[N], vis[N], a[N], e, m, ne[M], h[N], to[M], u, v, n,
                                                                                                                                                     void ins(int p, int v) \{ ++e; to[e] = v; ne[e] = h[p]; h[p] = void ins(int p, int v) \}
const int N = 1e5 + 7, M = 2e6 + 7
                                                                                                                                                                                                                                                                            while (!h[ma]) ma—;
                                                                                                                                                                                                                                    h[p] = ne[h[p]];
                                                                                                                                                                                            void del(int p)
                                                                                                                                                                                                                                                                                                                                                  int solve(){
                                                                            vi g[N];
                                                                                              int L, hd[::N], ne[N], to[N]; 11 val[N];
inline void init(int n) { L = 0; rep(i, 1, n + 1) hd[i] = -1; }
inline void _add(int u, int v, 11 w) { to[L] = v; val[L] = w; ne[L] = hd[u]; hd[u]
                                                                                                                                                                                                                                                            inline void add(int u, int v, 11 w) { _add(u, v, w); _add(v, u, w);
                                                            static const int N = ::N << 1;
                           struct Gra {
```

return ans;

for (int k = n - 1, i = n - 2; i >= 0; —i) { int x = rk[u][i], y = rk[u][k];

if (d[v][x] > d[v][y]) {

rep(v, 0, n) **if** (g[u][v] != inf) {

if $(d[u][rk[u][n-1]] * 2 < ret) {$

int ret = inf, $s_1 = -1$, $s_2 = -1$;

db ds1 = 0, ds2 = 0;

rep(u, 0, n) {

ret = d[u][rk[u][n-1]] * 2;

ds1 = ds2 = 0;

s1 = s2 = u;

```
// time : 0(n^3)
                                                                                                                             struct blossom {
                                   6.33
int tmp = d[u][x] + d[v][y] + g[u][v];
                                        ret = tmp, s1 = u, s2 = v;

ds1 = 0.5 * tmp - d[u][x];
                                                                                     ds2 = g[u][v] - ds1;
                     if (tmp < ret) {</pre>
                                                                                                                                                                                                                                          cout << ret / 2.0 << endl;
                                                                                                                                 = i;
                                                                                                                                                                                                                                                              return mp(s1, s2);
```

带花树

```
vi g[N];
int u, v, n, match[N], q[N], L, R, pred[N], b[N], s, t, newb;
bool inq[N], inb[N], inp[N];
                                                                                                                                                                        void init(int _n) { n = _n; rep(i, 0, n) g[i].clear();
void link(int u, int v) { g[u].pb(v); g[v].pb(u); }
void push(int u) { q[R++] = u; inq[u] = 1; }
int pop() { return q[L++]; }
                                                           static const int N = 5005;
                                                                                                                                                                                                                                                                                                                            rep(i, 0, n) inp[i]=0;
while(1) {
                                                                                                                                                                                                                                                                                            int LCA(int u,int v) {
// id : 0 .. n-1
```

完美消除序列 6.32

```
v = pred[u], w = match[v];
match[v] = u, match[u] = v;
u = w;
u = w;

lu = w;

}
int solve() {
    int res = 0;
    rep(i, 0, n) match[i] = -1;
    // random_shuffle maybe faster
    rep(i, 0, n) if (match[i] == -1) if (Find(i)) AugmentPath();
    rep(i, 0, n) if (match[i] != -1) res++;
    return res / 2;
}

fracturn res / 2;
}
```

6.34 **最短路矩阵中**第 k 小

```
⊐
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            pq.push(data(u.w - g[u.last][u.id].fi + g[u.last][u.id + 1].fi, u.st, u.last,
                                                                                                                                             data(11 W, int S, int L, int I) { w = W; st = S; last = L; id = I; } bool operator < (const data &c) const { return w > c.w; }
                                                                                                                                                                                                     ];
// 连通图的话 k <= n * (n – 1)
// 复杂度最坏应该是 O( min(nmlogn, k^2logk) ) 正常应该是 O(klogk + nlogn)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (sz(g[v])) pq.push(data(u.w + g[v][0].fi, u.st, v, 0));
                                                                                                                                                                                                                                                                                                                                                                            rep(i, 1, n+1) {
    if (sz(g[i])) pq.push(data(g[i][0].fi, i, i, 0));
                                                          int n, m, k, u, v, w;
struct data { // 距离起点当前点当前扩展过的边编号
                        vectorctorctorctorctorcpii> g[N]; // ( 边权 , 终点 ) 需要排序
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            k—; if (k == 0) return u.w;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (!vis.count(mp(u.st, v))) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          }
if (u.id + 1 < sz(g[u.last]))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          data u = pq.top(); pq.pop();
int v = g[u.last][u.id].se;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 vis.insert(mp(u.st, v));
                                                                                                                                                                                                                                                                                                                                                                                                                                           vis.insert(mp(i, i));
                                                                                                                  11 w; int st, last, id;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 while (!pq.empty()) {
const int N = 2e5 + 7;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ;((1 + pi));
                                                                                                                                                                                                                                                                                                                                                      set<pii>set<pii>s;
```

6.35 生成树计数与欧拉回路方案数

 $i==j d[i][j]=in_deg(i)$

// b[][]:

i!=j d[i][j]=0

// d[][]:

```
if(v == s \mid | (match[v] >= 0 \& pred[match[v]] >= 0))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(i, 0, n) pred[i] = -1, b[i] = i, inq[i] = 0; s = u, t = -1, L = R = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (match[v] >= 0) push(match[v]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (b[u] \stackrel{!}{=} \stackrel{!}{=} \stackrel{!}{b}[\stackrel{v}{v}] && match[u] \stackrel{!}{=} v)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      else if(pred[v] == -1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         else return t = v, 1;
                                                                                                                                                                                                                                                                                                             inb[b[u]] = inb[b[v]] = 1;
u = pred[v];
if(b[u] != newb) pred[u] = v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(i, 0, n) if (inb[b[i]]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(b[u] != newb) pred[u] = v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 pred[v] = u;
                                                                                                            if (inp[v = b[v]]) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Blossom(u, v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         per(i, 0, sz(g[u])) {
                                                                                                                                                                                                                                                                                                                                                                                                                           void Blossom(int u,int v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (!inq[i]) push(i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 0, n) inb[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            pred[v]=u;
                                           u = pred[match[u]];
                                                                                                                                  v = pred[match[v]];
                                                                                                                                                                                                                       void ResetTrace(int u) {
                                                                                                                                                                                                                                                                  while(b[u] != newb) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int v = g[u][i]
inp[u = b[u]] = 1;
                      if (u == s) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int u = pop();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void AugmentPath() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(b[v]] != newb)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int u = t, v, w;
while (u >= 0) {
                                                                                                                                                                                                                                                                                        v = match[u];
                                                                                                                                                                                                                                                                                                                                                                                                                                                   newb = LCA(u, v)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             bool Find(int u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   bool found = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          b[i] = newb;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              while(L < R) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ResetTrace(u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ResetTrace(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return found;
                                                                                    while(1) {
                                                                                                                                                                               return v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        (s)ysnd:
```

```
int C[N][N], B[N];
void ini() {
    rep(i, 0, N) C[i][0] = 1;
    rep(i, 0, N) rep(j, 1, i + 1) C[i][j] = add(C[i - 1][j - 1], C[i - 1][j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(j, 0, i) B[i] = add(B[i], MOD - mul(C[i+1][j], B[j])); B[i] = mul(B[i], qpow(C[i+1][i], MOD - 2)) % MOD;
                                                                                                                                                                                                                                                                                                                                                    rep(i, 0, sz(B)) C[i + m] = add(C[i + m], mul(c, B[i]));
if(2 * L <= n) L = n + 1 - L, B = T, b = d, m = 1;
                                       rep(i, 0, L+1) (d += 111 * C[i] * s[n-i]) \% P;
                                                                                                                                                                                                                                                                                                   11 c = P - d * kpow(b, P - 2) % P;
while(sz(C) < sz(B) + m) C.pb(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // desc : 0^{\Lambda}k + 1^{\Lambda}k + 2^{\Lambda}k + ... + (n-1)^{\Lambda}k
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return vi(C.begin(\bar{)}, C.end(\bar{)} = \bar{1});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(i, 0, sz(C)) C[i] = P - C[i]
                                                                                         vi C(1, 1), B(1, 1);

int L = 0, m = 1, b = 1;

rep(n, 0, sz(s)) {

11 d = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int cal(int n, int k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           const int N = 1000;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // time_cal : k + log
                                                                                                                                                                                                                           if(d == 0) ++m;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(i, 1, N) {
B[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 namespace Bernoulli
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // time_ini : O(n^2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      reverse(all(C));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          Bernoulli
                                                                                                                                                                                                                                                                           viT = C;
                                                                                                                                                                                                                                                                                                                                                                                                              else ++m;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           B[0] = 1;
                                                                   vi BM(vi s) {
                                                                                                                                                                                                                                                   else {
                   // 0(1en^2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          7.2
                                                                                                                                                                                                                                                           int t = a[i][i] / a[j][i];
rep(k, i, n) a[i][k] = sub(a[i][k], mul(a[j][k], t)), swap(a[i][k], a[j][k]);
                                                                         // 无向图生成树个数: a[][] 任何一个 n-1 阶主子式的绝对值
// 有向图以 i 为根的生成树个数: a[][] 去掉第 i 行第 i 列的行列式的绝对值
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // ec(G) = tw(G) * pi((deg[v] - 1)!)
// ans = ec(G) * deg[w]; 如果求的不是本质不同的,就还需要这个
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 1, n+1) q.push(i), pos[i] = 0, mat[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    else if (rank[v][mat[v]] > rank[v][u]) {
from i to j has b[i][j] directed edges
                                                                                                                                                       int det(int n) { // det(a[1..n-1][1..n-1])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // 有向图要记得判断每个点的出度入度是否相等
// 无向图需要转换成有向图
                                                                                                                                                                                                                                 rep(j, i+1, n) while(a[j][i]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void match(int n, vi *g, vi *rank) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int &p = pos[u], v = g[u][p];
if (!mat[v]) mat[v] = u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int u = q.front(); q.pop();
                                                                                                                                                                                                                                                                                                                                                              if(a[i][i] == 0) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    1231341 1341231
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               1231341 1312341
                                                                                                                                                                                                                                                                                                                                                                                        ans = mul(ans, a[i][i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // tw(G): 以 w 为根的生成树个数 // ec(G) = tw(G) * pi((deg[v])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int mat1[N], mat[N], pos[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       稳定婚姻匹配
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              q.push(mat[v]);
                         // a[J[J] = d[J[J] - b[J[J]]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               while (!q.empty()) {
                                                                                                                                                                                                                                                                                                               ans = P - ans;
                                                                                                                                                                                                       rep(i, 1, n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 vi g1[N], g2[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                              return ans;
                                                                                                                                                                                   int ans=1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             queue<int> q;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // 本质相同:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               本质不同:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         6.36
```

7.3 CRT

rep(i, 0, k + 1) sum = add(sum, mul(C[k + 1][i], mul(B[i], qpow(n, k + 1 - i))));

return mul(sum, qpow(k + 1, MOD - 2));

int sum = 0;

```
const int N = 1e5+7;
11 a[N], mod[N];
```

7.1 BerlekampMassey

7 Math

rep(i, 1, n+1) mat1[mat[i]] = i;

mat[v] = u; }**else** q.push(u);

x = w[f][1] * a[j+k+i], y = a[j+k], a[j+k] = y+x, a[j+k+i] = y-x;

if (f) rep(i, 0, N) a[i].r /= N;

void work(){
 int d = __builtin_ctz(N);

rep(i, 0, N) {

rev[i] = (rev[i>>1] >> 1) | ((i&1) << (d-1)); w[1][i] = w[0][i] = vir(cos(2*pi*i/N), sin(2*pi*i/N)); w[1][i].i = -w[1][i].i;

void doit(vir *a, vir *b, int na, int nb) $\{ // [\theta,$

for (N = 1; N < na + nb - 1; N <<= 1);

rep(i, na, N) a[i] = vir(0, 0); rep(i, nb, N) b[i] = vir(0, 0); work(), fft(a, 0), fft(b, 0); rep(i, 0, N) a[i] = a[i] * b[i]; fft(a, 1);

//rep(i, 0, N) a[i].print();

7.6 FFTMOD

```
vir operator +(const vir &c) {return vir(r + c.r, i + c.i);} vir operator -(const vir &c) {return vir(r - c.r, i - c.i);} vir operator *(const vir &c) {return vir(r * c.r - i * c.i, r * c.i + i * c.r);}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       vir x, y;
rep(i, 0, N) if (i < rev[i]) swap(a[i], a[rev[i]]);
for (int i = 1; i < N; i <= 1)
for (int j = 0, t = N/(i<<1); j < N; j += i<<1)
for (int k = 0, 1 = 0; k < i; k++, 1 += t)
for (int k = 0, 1 = 0; k < i; st++, 1 += t)</pre>
                                                                                                                                    return Euler_qpow(a[1], work(1+1, r, phi(mod)), mod);
                                                                                                                                                                                                                                                                                                                                                                                                                                   vir(db \ r = 0.0, \ db \ i = 0.0) : r(r), \ i(i){}
                                                                                                                                                                                                                                                                                                                                                                                                                                                            void print() {printf("%f %f\n", r, i);}
                                                    11 work(int 1, int r, int mod) {
                                                                                                      if (1 == r) return a[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void fft(vir *a, int f){
                                                                                                                                                                                                                                                                                               const int M = 1 << 17 << 1;
                                                                             if (mod == 1) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int N, na, nb, rev[M];
return res + mod * ok;
                                                                                                                                                                                                                                                                                                                      const db pi = acos(-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     a[M], b[M], w[2][M];
                                                                                                                                                                                                                            FFT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              struct FFT{
                                                                                                                                                                                                                                                                                                                                                                               struct vir{
                                                                                                                                                                                                                                                                                                                                                                                                            db r, i;
                                                                                                                                                                                                                            7.5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         R = (R % M + M) % M; // 可能为 Ø 看是否需要是正整数
                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 2, n+1) {
    l1 g = __gcd(M, mod[i]);
    l1 inv = Inv(M / g, mod[i] / g);
    if ((a[i] - R) % g) return -1; // 无解
    R += inv * ((a[i] - R) / g) % (mod[i] / g) * M;
                                                    void exgcd(ll a, ll b, ll &x, ll &y){
   if (!b) { x = 1; y = 0; return;}
                                                                                                                                                                                                                                                                                                                          }
11 solve(int n, ll *a, ll *mod){
M = mod[1], R = a[1];
                                                                                                                                                                                                                                                                                                   return x < 0 > x + mod : x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                M = M / g * mod[i];
                                                                                                      exgcd(b, a % b, y, x);
                                                                                                                                                                                                                                               exgcd(a, mod, x, y);
                                                                                                                                                                 }
11 Inv(11 a, 11 mod){
                                                                                                                                                                                                               11 \times = 0, y = 0;
                                                                                                                                  y = a / b * x;
                                                                                                                                                                                                                                                                            :pow =% ×
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return R;
                           11 M, R;
  struct CRT{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      } crt;
```

7.4 EulerPower

```
// a[1] ^ a[1+1] ^ a[1+2] ... ^ a[r] % mod 注意结果要再模 mod
map<int, int> M;
                                                                                                         for(int i = 2; i * i <= n; i++) if (n % i == 0){ r = r / i * (i-1);
                                                                                                                                                                                                                                                                                                        111 res = 1; bool ok = (b > 0 && a >= mod);
while (b) {
                                                                                                                                                                                                                                                                                      11 Euler_qpow(11 a, 11 b, 11 mod) {
                                                                                                                                                      while (n \% i == 0) n /= i;
                                                                                                                                                                                                if (n > 1) r = r / n * (n-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ok |= (b > 1 \& a >= mod);
                                                                   if (M.count(n)) return M[n];
                                                                                                                                                                                                                                                                                                                                                                                              ok |= (res >= mod);
                                                                                                                                                                                                                                                                                                                                                                         res = res * a;
                                                                                          int r = n, nn = n;
                                                                                                                                                                                                                                                                                                                                                                                                                        res %= mod;
                                                                                                                                                                                                                                                                                                                                                     if (b & 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                               = a * a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           a %= mod;
                                              int phi(int n)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               b >>= 1;
                                                                                                                                                                                                                    M[nn] = r;
                                                                                                                                                                                                                                            return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 В
```

```
vir operator *(const vir &0) const{return vir(a*0.a-b*0.b,b*0.a+a*0.b);}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for(int i=0; i<=na, i++) (i&1 ? x[i>>1].b : x[i>>1].a) = a[i];
for(int i=0; i<=nb; i++) (i&1 ? y[i>>1].b : y[i>>1].a) = b[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (v) for(int i=0; i<k; i++) x[i] = vir(x[i].a/k,x[i].b/k);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       vir operator +(const vir &0) const{return vir(a+0.a,b+0.b);}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       vir operator —(const vir &o) const{return vir(a—o.a,b—o.b);
                                                                                                                                                                                                                                                                           ۳,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          vir operator *(const double &0) const{return vir(a*0,b*0);}
                                                                                                                                                                                                                                                                     a[i] = ((dd << (L^*2)) + ((db + dc) << L) + da) %
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                vir g = vir(cos(2*pi/i), (v ? -1 : 1) * sin(2*pi/i));
for(int j=(i>>1); j>=0; j-=2) w[j] = w[j>>1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for(int j=1; j<i>i>i>i) w[j] = w[j-1] * g;
for(int j=0; j<k; j+=i){
    vir *a = x+j, *b = a+(i>>1);
    for(int l=0; l<i>i>>1; l++){
                                                                                                                                                                   db = (11)(C[i].r / N + 0.5) % P,
dc = (11)(D[i].i / N + 0.5) % P,
dd = (11)(D[i].r / N + 0.5) % P;
D[j] = db * dd + db * dc * vir(0, 1);
                                                                                                                                 da = (1)(C[i].i / N + 0.5) % P,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        vir(double r=0.0, double i=0.0) {a=r, b=i;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         vir\ operator\ !()\ const\{return\ vir(a,-b);\}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void doit(int *a, int *b, int na, int nb)
for(K = 1; K <= na+nb>>1; K <<= 1);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(i, 0, K) \times [i] = y[i] = vir(0, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(i>j)Swap(x[i],x[j]);
for(int l=k>1; (j^=1)<l; l>=1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           } x[N|1], y[N|1], z[N|1], w[N|1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       vir o = b[1] * w[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 fft(x, K, 0); fft(y, K, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for(int i=0, j=0; i<k; i++){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void fft(vir x[],int k,int v){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  w[0] = vir(1, 0);
for(int i=2; i<=k; i<<=1){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         b[1] = a[1] - 0;
a[1] = a[1] + 0;
                                                                FFT(C, N), FFT(D, N);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      const double pi=acos(-1.0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    const int N = 1 \ll 21
                                                                                                     0, N) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 0, K){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         double a, b;
                                                                                                                                                                                                                                                                                                                                                                                                                                           FFT
                                                                                                       rep(i,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       struct vir{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int K;
                                                                                                                                                                                                                                                                                             inline vir operator *(const vir &c) {return vir(r * c.r - i * c.i, r * c.i + i * c.r)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(i, 0, N) w[i] = vir(cos(2 * i * PI / N), sin(2 * i * PI / N)); rep(i, 0, N) {
                                                                                                                                                                                                                                                              inline vir operator -(const \ vir \ \&c) \ \{return \ vir(r-c.r, i-c.i);\}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (N = 1; N < na + nb - 1; N <<= 1); rep(i, 0, na) a[i] = (a[i] % P + P) % P; rep(i, na, N) a[i] = 0; rep(i, 0, nb) b[i] = (b[i] % P + P) % P; rep(i, nb, N) b[i] = 0;
                                                                                                                                                                                                                         inline vir operator +(const vir &c) {return vir(r + c.r, i + c.i);}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for (int d = 0; (1 << d) < n; ++d) {
  int m = 1 << d, m2 = m * 2, rm = n >> (d + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    vir &p1 = p[i + j + m], &p2 = p[i + j];
vir t = w[rm * j] * p1;
                                                                                                                                                                                                                                                                                                                                                              inline vir operator !() const {return vir(r, -i);}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              db = (A[i] + !A[j]) * vir(0.5, 0),
dc = (B[i] - !B[j]) * vir(0, -0.5),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       dd = (B[i] + !B[j]) * vir(0.5, 0);
= da * dd + da * dc * vir(0, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for (int s = n; j = s >>= 1, ~j & s;);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            vir da = (A[i] - !A[j]) * vir(0, -0.5),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for (int i = 1, j = 0; i < n - 1; ++i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void doit(int *a, int *b, int na, int nb){
                                                                                                                                                                                             vir(db \ r = 0.0, \ db \ i = 0.0) \ : \ r(r), \ i(i) 
                                                                                                                                                                                                                                                                                                                                                                                               void print() {printf("%lf %lf\n", r, i);}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    A[i] = vir(a[i] >> L, a[i] & MASK);
B[i] = vir(b[i] >> L, b[i] & MASK);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for (int i = 0; i < n; i += m2) {
  for (int j = 0; j < m; ++j) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               p1 = p2 - t, p2 = p2 + t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (i < j) swap(p[i], p[j]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   vir w[M], A[M], B[M], C[M], D[M];
void FFT(vir p[], int n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  static const int M = 1 << 18 <<
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    L = 15; MASK = (1 << L) - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int j = (N - i) \% N;
                                                         const int M = 1 << 18 << 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void mul(int *a) {
    FFT(A, N), FFT(B, N);
                                                                                             int na, nb, a[M], b[M];
                         const db PI = acos(-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 0, N) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int N, L, MASK;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                   struct FFTMOD{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       mul(a);
                                                                                                                       struct vir{
                                                                                                                                                                db r, i;
```

2.8

*= M) ret += (x%M + y%M) % M*B;

for $(; \times || \dot{}) \times /= M$, $y \neq M$, B return ret;

inline friend Num operator — (const Num &a, const Num &b) {

return c;

rep(i, 0, K) c.a[i] = add(a.a[i], -b.a[i]);

return c;

int get(int x, int y) {

int ret = 0, B = 1;

void Multiply_B(11 A[], 11 B[], int n, 11 C[]) {
 rep(i, 0, n) rep(j, 0, n) (C[get(i, j)] += mul(A[i], B[j])) %= .

```
if (K & 1 ^ 1) ret -= add(a[K >> 1], -(L > 1)^*a[(K >> 1) + cnt]), ret %= _p;
                                                             0, K) (c.a[(i + j) % K] += mul(a.a[i], b.a[j])) %= _p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           :0 : d⁻
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int cnt = KR-K, L = K / cnt; ll ret = add(a[0], -(L > 1)*a[cnt]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    (n, -1); ll inv = Pow(n, _p - 2);
n) C[i] = mul(a[i].Value(), inv), C[i] < 0 ? C[i] += _
  inline friend Num operator * (const Num &a, const Num &b)
                                                                                                                                                                                                                                                                                                                                                                                    for (; k; k >>= 1, x = x^*x) if (k & 1) ret = ret*x;
                                                                                                                                                             호
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                tmp[j] = tmp[j] + (a[S + L*k + i] >> t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(i, 0, K) printf("a[%d] => %d\n", i, a[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void Multiply(11 A[], 11 B[], int n, 11 C[])
                                                                                                                                                           inline friend Num operator >> (const Num &a,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Num<K> tmp[M << 1], a[N], b[N]; int t;
void FWT(Num<K> a[], int S, int n, int op)
                                                                                                                                                                                                                                                                                                                      inline friend Num operator ^{\wedge} (Num \times, 11 k)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(j, 0, M) a[S + L^*j + i] = tmp[j]
                                                                                                                                                                                           Num c;
rep(i, 0, K) c.a[(i + k) % K] = a.a[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             t = op^*j^*k\%M, t < 0 ? t += M : 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 0, n) a[i] = A[i], b[i] = B[i];
FWT(a, 0, n, 1), FWT(b, 0, n, 1);
rep(i, 0, n) a[i] = a[i] * b[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(i, 0, M) FWT(a, S + L*i, n / M, rep(i, 0, L) {
    rep(j, 0, M) tmp[j] = 0;
    rep(j, 0, M) rep(k, 0, M) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (n == 1) return; int L = n / M;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             printf("\n\n\n\s\n", s.c_str());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             inline void print(string s = "") {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         template <int M, int N, int K>
                                                             rep(i, 0, K) rep(j,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  inline 11 Value() {
                                                                                                                                                                                                                                                                                                                                                         Num ret = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                       return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         o` o
                                                                                                  return c;
                                                                                                                                                                                                                                                           return c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      FWT(a,
rep(i,
                                  Num c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    struct FT {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   inline Num& operator = (int x) { mem(a, 0), a[0] = x; return *this; }
                                                                                                                                                                                                                                                                                                                                                                                                        for (int k = 0; 1 << k < len; ++k) rep(i, 0, len) if (\simi >> k \& 1)
                             vir tmp = (i&K>>1) ? vir(1, 0) - w[i^K>>1] : w[i] + vir(1, 0); z[i] = (x[i]^*y[i]^*4 - (x[i] - !^K[i])^*(y[i] - !^K[i])^*tmp)^*6.25;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (; k; k >>= 1, x = mul(x, x)) if (k & 1) ret = mul(ret, x);
                                                                                                                                                        rep(i, 0, na+nb+1) a[i] = i&1 ? z[i>>1].b + 0.1 : z[i>>1].a +
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                inline friend Num operator + (const Num &a, const Num &b) \{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                   x = (a[i] + a[j]) \% P, y = (a[i] - a[j] + P) \% P, // xor

if (o == -1) \times = (11) \times 1002 \% P, y = (11) \times 1002 \% P,

//x = (a[i] + a[j]) \% P, y = a[j]; // and
                                                                                                                                                                                                                                                                                                                                          const int P = 1e9 + 7, inv2 = P + 1 >> 1; // P is odd prime void FWT(int *a, int len, int o = 1) { // o=-1 UFWT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Num c;
rep(i, 0, K) c.a[i] = add(a.a[i], b.a[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 //if (o == -1) x = (a[ij - a[j] + P) \% P; //x = a[ij], y = (a[ij + a[j]) \% P; // or
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              //if (o == -1) y = (a[j] - a[i] + P) \% P;

a[i] = x, a[j] = y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         11 add(11 x, 11 y) { x += y; return x%_p; }
11 mul(11 x, 11 y) { return x*y%_p; }
11 Pow(11 x, 11 k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Num(int x = 0) { mem(a, 0), a[0] = x; } inline Num% operator = (const Num &t) {
                                                                                                                                                                                                                                                                                                                                                                                                                                   int j = i \land (1 << k), x, y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 0, K) a[i] = t.a[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              xor
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                const int _p = 998244353;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 k 拼動
int j = K-1 \& K-i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return *this;
                                                                                                                           fft(z, K, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            template <int K>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 FWT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            11 ret = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return ret;
                                                                                                                                                                                                                                                              \mathbf{FWT}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          struct Num {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          11 a[K];
```

7.9

```
inline int mul(int x, int y) { return (11)x^*y^3P; } inline int add(int x, int y) { return (x += y) >= P ? x - P : x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   inline friend Num operator ^{*} (const Num &a, const Num &b) \{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inline int operator [] (int x) const { return a[x]; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void fwt(V a[], int len, int o = 1) { // O=-1 UFWT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          c[i + j] = add(c[i + j], mul(a[i], b[j]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               inline int& operator [] (int x) { return a[x]; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        for (int j = 0; i + j < L; ++j) if (b[j])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              (0 == 1) ? a[j] += a[i] : a[j] -= a[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, L) a[i] = add(a[i], P - b[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            inline void operator -= (const Num &b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   inline void operator += (const Num &b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   void mul(V a[], V b[], int len, V c[])
fwt(a, len), fwt(b, len);
rep(i, 0, len) c[i] = a[i] * b[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(i, 0, L) a[i] = add(a[i], b[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for (int k = 0; 1 << k < len; ++k)
rep(i, 0, len) if (~i >> k & 1)
int j = i ^ (1 << k);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        inline void clear() { a.fill(0); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      const int P = 1e9 + 7, M = 18;
                                                                                                                                                                                                                                                                                                                                                                                                                 子集卷积
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Num<L> c; c.clear();
rep(i, 0, L) if (a[i])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              V aa[1 << M], bb[1 << M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                fwt(c, len, -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 array<int, L> a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     struct Calculator {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          template <class V>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             template <int L>
                                                                                                                                                                                                                                                                                                                                                                                                                      {
m FWT}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return c;
                         12 86475609
14 9196980
18 4138593
21 32705801
24 304035978
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          struct Num {
                                                                                                                                                                                                                                                                                                                                 14 467509451
    9 246325263
                                                                                                                                                                                                                                                                                                    8 372528824
                                                                                                                                                                                                                                      4 86583718
                                                                                                                                                                                                                                                                        7 14553391
                                                                                                                                                                                                             998244353
                                                                                                                                                                                                                                                                                                                                                                                                                      7.11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    11 tmp[K << 1], a[N], b[N], w[K]; int t;
void Init(11 w0) { w[0] = 1; rep(i, 1, K) w[i] = mul(w[i - 1], w0); }
void FWT(11 a[], int S, int n, int op) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void Multiply_B(11 A[], 11 B[], int n, 11 C[]) {
    rep(i, 0, n) rep(j, 0, n) (C[get(i, j)] += mul(A[i], B[j])) %= _p;
    rep(i, 0, n) C[i] < 0 ? C[i] += _p : 0;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        for (; \times || y; \times /= K, y /= K, B *= K) ret += (x%K + y%K) % K*B;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        \mathsf{FWT}(a,\ 0,\ n,\ -1);\ 11\ \mathsf{inv} = \mathsf{Pow}(n,\ -p-2); \mathsf{rep}(i,\ 0,\ n)\ \mathsf{C}[i] = \mathsf{mul}(\mathsf{a}[i],\ \mathsf{inv}),\ \mathsf{C}[i] < 0\ ?\ \mathsf{C}[i]\ += \_p\ :\ 0;
                                                                                                                                                                                                                                                                                                                                 for (; k; \dot{k} >>= 1, x = mul(x, x)) if (k & 1) ret = mul(ret, x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(j, 0, K) tmp[j] = 0;

rep(j, 0, K) rep(k, 0, K) {

t = op*j*k%K, t < 0 ? t += K : 0;

tmp[j] = add(tmp[j], mul(a[S + L*k + i], w[t]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   3 进制的,进制要整除模数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void Multiply(11 A[], 11 B[], int n, 11 C[])
rep(i, 0, n) a[i] = A[i], b[i] = B[i];
FWT(a, 0, n, 1), FWT(b, 0, n, 1);
rep(i, 0, n) a[i] = mul(a[i], b[i]);
                                                                                                                                                                                  const int _p = (int)1e9 + 9, w0 = 11538139811;
11 add(11 x, 11 y) { x += y; return x%_p; }
11 mul(11 x, 11 y) { return x*y%_p; }
11 Pow(11 x, 11 k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(i, 0, K) FWT(a, S + L*i, n / K, op);
rep(i, 0, L) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(j, 0, K) a[S + L^*j + i] = tmp[j]
    .;
0
..
a
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (n == 1) return; int L = n / K;
                                                                                                               xor 版本
      ij
+
  rep(i, 0, n) C[i] < 0 ? C[i]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       };
// ₩0 表示单位根模域表示,默认是
                                                                                                               k 拼塑
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int get(int x, int y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int ret = 0, B = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                           template <int N, int K>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return ret;
                                                                                                                    7.10 FWT
                                                                                                                                                                                                                                                                                                      11 \text{ ret} = 1;
                                                                                                                                                                                                                                                                                                                                                                      return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                6 115381399
7 95932470
                                                                                                                                                                                                                                                                                                                                                                                                                                                           struct FT {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            3 115381398
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              8 118835338
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                10000000001
```

rep(i, 0, len) a[i].clear(), a[i][_builtin_popcount(i)] = mask[i]; fwt(a, len), ret[0] = 0;

L = K + 1;

rep(j, 1, k + 1) { if (j == 1) rep(i, 0, len) b[i] = a[i];

else rep(i, 0, len) b[i] *= a[i];

int &t = ret[j] = 0; rep(i, 0, len) if (_builtin_parity((len - 1) $^{\wedge}$ i)) t = add(t, -b[i][k]);else t = add(t, b[i][k]); 40/93

const int N = 50;

Poly<int> PP;

cal T;

```
inline int mul(int x, int y) { return (11)x * y % P; } inline int add(int x, int y) { if ((x += y) >= P) \times -= P; return \times < 0 ? \times + P : x; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 inline void operator += (const vec &b) { rep(i, 0, L) a[i] = add(a[i], b[i]); }
inline void operator -= (const vec &b) { rep(i, 0, L) a[i] = add(a[i], -b[i]); }
inline vec operator *= (const vec &b) {
rep(i, 0, n+1) {
  fill_n(a1, n+1, 0); a1[0] = 1;
  rep(j, 0, n+1) if (j != i) a1[0] = mul(a1[0], x[i] - x[j]);
  a1[0] = mul(y[i], kpow(a1[0], P - 2));
  rep(j, 0, n+1) if (j != i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               inline int operator [] (int x) const { return a[x]; } inline void clear() { fill_n(a, L, 0); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void fwt(vec[a[], int len, int 0 = 1) { // 0=-1 UFWT}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           c[i + j] = add(c[i + j], mul(a[i], b[j]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void pow(int mask[], int len, int k, int ret[]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 inline int& operator [] (int x) { return a[x]; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  vec c; c.clear();
rep(i, 0, L) if (a[i])
for (int j = 0; i + j < L; ++j) if (b[j])</pre>
                                                                                                                                                                                                                                                                                         rep(j, 0, n+1) a[j] = add(a[j], a1[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       o == 1 ? a[j] += a[i] : a[j] -= a[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i, 0, len) if (\simi >> k & 1)
int j = i ^ (1 << k);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int k = 0; 1 << k < len; ++k)
                                                                                                                                                                                                                                                                                                                                                                                                                                   const int P = 1e9 + 7, M = 20; int L;
                                                                                                                                                                                b1[0] = -x[j]; b1[1] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         vec a[1 << M], b[1 << M];
                                                                                                                                                                                                                       calc(n, a1, b1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return *this = C;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           struct Cal {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int a[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 struct vec {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void Mul(int A[], int B[], int len, int C[]) {
   In(A, len, aa), In(B, len, bb), mul(aa, bb, len, aa), Out(aa, len, C);
                                                                                                                                                                                                                                                                                                                                                              rep(i, 0, len) a[i].clear(), a[i][__builtin_popcount(i)] = A[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void Pow(int A[], int len, int k, int C[]) {
   In(A, len, aa), pow(aa, len, k, bb), Out(bb, len, C);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(i, 0, len) A[i] = a[i][__builtin_popcount(i)];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   * M 为 pit 数,数组范围 [0,2~M—1], Num 范围 [0,M]
* 多组数据, L 可改造用以减少计算量
                                                                                                                                                                                rep(j, 0, k-1) c[i] = c[i] * a[i];
                                      void pow(V a[], int len, int k, V c[]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void ModP(int a[], int len) {
    rep(i, 0, len) a[i] = add(a[i], P);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       * Out 拆箱操作,将集合幂级数转化为普通数组
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      * In 装箱操作,将普通数组封装成集合幂级数
                                                                                                                                                                                                                                                                                                                          void In(int A[], int len, V a[]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                   void Out(V a[], int len, int A[])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 * 集合幂级数用于计算快速子集卷积
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Calculator<Num<M + 1>> T;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               * Pow 计算多重子集自卷积
                                                                          fwt(a, len);
rep(i, 0, len) {
                                                                                                                                                                                                                                                        fwt(c, len, -1);
                                                                                                                                         c[i] = a[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              * Mu1 计算子集卷积
```

染色多项式 FWT

```
T kpow(T a, T b) {T r=1; for(;b;b>=1,a=mul(a,a)) {if(b&1)r=mul(r,a);}return r;} void calc(int n, T *a, T *b) {
                                                                                                                                                                                                                                                                                                                                                              rep(i, 0, n+1) rep(j, 0, 2) c[i+j] = add(c[i+j], mul(a[i], b[j]));
memcpy(a, c, sizeof(a[0]) * (n+1));
                                                                                                                   T al[N], bl[N], c[N];
T add(T a, T b) {a = (a + b) % P; return a < 0 ? a + P : a;}
T mul(T a, T b) {a = 111 * a * b % P; return a < 0 ? a + P : a;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void solve(int n, T *x, T *y, T *a){ // a[\theta]^*x^{\lambda\theta} ... a[n]^*x^{\lambda n}
                                                                         static const int N = 30, P = 1e9 + 7;
                                                                                                                                                                                                                                                                                                                                 fill_n(c, n+1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     fill_n(a, n+1, 0);
template<class T>
                                   struct Poly{
```

```
int a[N], mask[1 << M], col[N], ret[N], n, m, u, v, X[N], Y[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                1}
                           mask[0] = 1; int L = 1 << n;
rep(i, 1, L) {
  int t = i & -i, k = __builtin_ctz(t);
                                                                    mask[i] = mask[i \land t] \& !(i \& a[k]);
                                                                                              \tilde{T}.pow(mask, L, n, col);
rep(i, 0, n+1) X[i] = i, Y[i] = col[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                -12, 13,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                4,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            { 0, 0, 0, 6, 192, 1620, 7680
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       1}
                                                                                                                          PP.solve(n, X, Y, ret);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              x (x - 1)^{\lambda} 2 (x - 2)^{\lambda} 2 = \{0,
              void solve(int a[], int n)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       32,
                                                                                                                                                                                                cin >> u >> v;
                                                                                                                                                                                                             a[u] |= pw(v);
a[v] |= pw(u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                      { 0, 0, 0, 12, 144,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Chromatic Poly
{0, -16, 48, -56, 3
*/
                                                                                                                                                     int main() {
    cin >> n >> m;
                                                                                                                                                                                 rep(i, 0, m) {
                                                                                                                                                                                                                                                     solve(a, n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Chromatic Poly
                                                                                                                                                                                                                                                                     return 0;
                                                                                                                                                                                                                                                                                                              Graph: link
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Graph: link
                                                                                                                                                                                                                                                                                                                                                                                                                                        Color Ways
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Color Ways
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      0010177808
0178884467
                                                                                                                                                                                                                                                                                                                          00000000
0004444
```

7.13 Fib

```
// sum(fib[1..n]) + 1=fib[n + 2]
// gcd(fib[n], fib[m]) = fib[gcd(n, m)]
```

7.14 Fraction

7.15 GaussDB

typedef Fra<ll> fll;

[0..var]

namespace Gauss{

```
rep(j, col, var+1) a[i][j] = add(a[i][j], \negmul(a[k][j], t));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(j, i+1, var) if (a[i][j]) t = add(t, -mul(a[i][j], x[j]));
                                                                                                                                                     if (p != k) rep(j, col, var+1) swap(a[p][j], a[k][j]);
if(!a[k][col]) {k--; continue;}
                                                             int Gauss(int equ, int var){
   for(k = col = 0; k < equ && col < var; ++k, ++col){
      p = k; rep(i, k, equ) if (a[i][col]) {p = i; break;}</pre>
                                                                                                                                                                                                              int inv = kpow(a[k][col], P - 2);
rep(i, col, var+1) a[k][i] = mul(a[k][i], inv);
                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, k, equ) if (a[i][var]) return –1;//无解
                                                                                                                                                                                                                                                                               rep(i, k+1, equ) if (a[i][col]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return var — k;//自由变元个数
                                                                                                                                                                                                                                                                                                             int t = a[i][col];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     per(i, 0, var) {
   int t = a[i][var];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            //对 2 取模的 01 方程组
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           GaussXor
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       //genx(var);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         x[i] = t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(k < var){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           7.17
                                                                                                                                                                                                                 for(k = col = 0; k < equ && col < var; ++k, ++col){
    p = k; rep(i, k+1, equ) if(fabs(a[i][col]) > fabs(a[p][col])) p = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  per(i, 0, var) {
   db t = a[i][var];
   rep(j, i+1, var) if (fabs(a[i][j]) > eps) t -= x[j] * a[i][j];
   x[i] = t / a[i][i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(i, k, equ) if (fabs(a[i][var]) > eps) return -1;//无解
                                                                                                                                                                                                                                                                               if (p != k) rep(j, col, var+1) swap(a[p][j], a[k][j]),
                                                                                                                                                                                                                                                                                                                                                                                                     db t = a[i][col] / a[k][col];
rep(j, col, var+1) a[i][j] -= a[k][j] * t;
                                                                                                                                                                                                                                                                                                             if(fabs(a[k][col]) < eps) {k--; continue;}
rep(i, k+1, equ){</pre>
rep(j, p+1, var) x[p] = a[i][j] * x[j];
                                                                                                                                                                                                                                                                                                                                                                      if (fabs(a[i][col]) < eps) continue;</pre>
                                                                                            rep(j, 0, pre) free[fnum++] = j;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return var — k;//自由变元个数
                                                                                                                                                                                       int Gauss(int equ, int var){
                                 x[p] /= a[i][p];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // genx(var);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      GaussInt
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(k < var){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      7.16
```

```
int free[N], frum; //一组合法自由变元(多解枚举自由变元可以使用)
//返回值为 –1 表示无解,为 Ø 是唯一解,否则返回自由变元个数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      p = k; rep(i, k, equ) if (a[i][col]) {p = i; break;} if (p := k) swap(a[k], a[p]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         For(k = 0, col = 0; k < equ && col < var; k++, col++){
static const int N = 2e3 + 10; //有 equ 个方程, var 个变元。增广矩阵行数为 equ 列数为,
                                                                                                                                                                                                                                                                                                                                                                                                                rep(j, p+1, var) x[p] ^= (a[i][j] && x[j]);
                                                                                                                                                                                                                                                                                                                                         rep(j, 0, var) if(a[i][j]) { p = j; break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             k--; free[fnum++] = col;//这个是自由变元
                                                                                                                                                                                                                                                                       rep(i, 0, fnum) x[free[i]] = (msk >> i) & 1;
per(i, 0, k) {
                                                                                                                                 int p, col, k; // k 为增广矩阵的秩
                                                            bitset<N> a[N]; //增广矩阵 modif
                                                                                                                                                                                                                                        void genx(int msk, int var) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int Gauss(int equ, int var){
                                                                                                                                                                                                                                                                                                                                                                                 x[p] = a[i][var];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (!a[k][col]){
                                                                                                    int x[N]; //解集
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            funm = 0;
                                                                                                                                                                                                                                        int kpow(int a, int b) {int r=1;for(;b;b>>=1,a=mul(a,a)) {if(b&1)r=mul(r,a);}return r
                                                                                                 int a[N][N], x[N]; //增广矩阵和解集
int free[N], fnum, k, col, p; // 一组合法自由变元
int add(int a, int b) {if ((a += b) >= P) a -= P; return a < 0? a + P: a;}
int mul(int a, int b) {return 111 * a * b % P;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(1, p, var+1) a[j][1] = add(a[j][1], -mul(a[i][1], t));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(j, p+1, pre) free[fnum++] = j, x[j] = (?); pre = p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(j, p+1, var) x[p] = add(x[p], \neg mul(a[i][j], x[j]));
                                                                                                                                                                                                                                                                                                                                                                           int pre = var; fnum = 0;
per(i, 0, k) {
    rep(j, 0, var) if (a[i][i]) { p = j; break; }
    rep(j, 0, i) if (a[j][p]) {
    int t = a[j][p];
}
                                                                    static const int N = ::N, P = 1e9 + 7;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(j, 0, pre) free[fnum++] = j;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           x[p] = a[i][var];
                                                                                                                                                                                                                                                                                                                                                    void genx(int var) {
                                       namespace GaussInt{
```

```
if (a[i]) x^=a[i], y^=tmp[i]; else { a[i]=x, tmp[i]=y; return 1; }
                                                                                                                         11 a[M];
LB() { mem(a,0); }
void Clear() { mem(a,0); }
void Copy(LB &A) { rep(i,0,M) a[i]=A.a[i]; }
// 向 this 中插入 x, 返回 y在后来插入元素中的投影
                                                                                                                                                                                                                                                                                                               for(int i=M-1; ~i && x; —i) if (x>>i&1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                for(int i=M-1; \sim i \& x; —i) if (x>>i\& 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (a[i]) \times^{\wedge}=a[i]; else return 0;
                                                                                                                                                                                                                                                            bool I(11 x, 11 &y) {
                    // 集合线性基求交与查询
                                                                                                                                                                                                                                                                                                                                                                                                                    bool Q(11 x) {
                                                                                                                                                                                                                                                                                                                                                                     return 0;
                                                    const int M=33
                                                                          11 tmp[M];
                                                                                                     struct LB{
                                                rep(i, 0, equ) if (i != k && a[i][col]) a[i] ^{-} a[k];
                                                                                                                                                                                                                                                                                                                                       rep(j, i+1, var) x[i] \wedge = (a[i][j] \&\& x[j]);
                                                                                                                             rep(i, k, equ) if (a[i][var]) return -1;
                                                                                                   rep(i, col, var) free[fnum++] = i;
                                                                                                                                                                                                        return var - k;//自由变元个数
                                                                                                                                                                                                                                                                                                             x[i] = a[i][var];
                                                                                                                                                                                 // genx(0, var);
                                                                                                                                                                                                                                                                                       per(i, 0, var){
continue
                                                                                                                                                       if(k < var) {
                                                                                                                                                                                                                                                            //唯一解,回代
                                                                                                                                                                                                                                                                                                                                                                                            return 0;
```

```
return (b/c)*n+(a/c)*n*(n-1)/2+(a%c?cal(c,(a*n+b)%c,a%c,(a%c*n+b%c)/c):0);
ll cal(ll a,ll b,ll c,ll n) { // sum_{i=0...n-1}floor((a^*i+b)/c)
                                                  if(n == 0) return 0;
```

7.18 LikeEuclid

7.19 LinearBasis

```
il Qry(int l, ll x=0) { per(i, 0, M) if (id[i]>=1) x=max(x, x^a[i]); return x; }
} B[N];
                                                                                                                                                                                                                                                                                                                                                                                                          void Copy(const LB &L) { rep(i,0,M) a[i]=L.a[i],id[i]=L.id[i]; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 else if (no>id[i]) swap(a[i],x), swap(id[i], no);
                                                                                                                                                                                        if (a[i]) x^=a[i]; else { a[i]=x; break; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Copy(L); for (int i=M-1; ~i && x; —i) if (x>>i&1) {
                                                                                                                                                           for(int i=M-1; ~i && x; —i) if (x>>i&1)
                                                                                                         void Clear() { memset(a,0,sizeof(a)); }
                                                                                                                                                                                                                                                                                                                                                                                 void Clear() { memset(a,0,sizeof(a)); }
                                                                                                                                                                                                                                                 };
// 可持久化线性基 ( 序列前缀最右线性基
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (!a[i]) a[i]=x,id[i]=no;
                                                                                                                                                                                                                                                                                                                                                                                                                                        void Ins(LB &L,ll \times, int no) {
                                                                                                                                                                                                                                                                                                                                                        11 a[M]; int id[M];
                                                                                                                                      void ins(11 x){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              x^=a[i];
// 普通集合线性基
                         const int M=63;
                                                                                                                                                                                                                                                                                                      const int M=32;
                                                                                 11 a[M];
                                                      struct LB{
                                                                                                                                                                                                                                                                                                                                   struct LB{
```

7.20 LinearRecursion

void build () { per(i,0,M) per(j,0,i) a[i]=min(a[i],a[i]^a[j]);

// 化为最简型,方便线性空间的 hash

;;

LB AA; 11 y,z; AA.Copy(A),C.Clear(); mem(tmp,0); per(i,0,M) if (B.a[i]) if (!AA.I(B.a[i],y)) C.I(y,z);

friend void Intersect(LB &A,LB &B,LB &C) {

return 1;

```
__builtin_clzll(n)) : 0; W; W >>= 1, x <<= 1) {
                                                                                                                                                                                                                                                                                                                        rep(i, 0, m) rep(j, 0, m) (u[i + b + j] += v[i] * v[j]) %= P, per(i, m, 2*m) rep(j, 0, m) (u[i - m + j] += c[j] * u[i]) %= P,
                             int linear_recurrence(ll n, int m, vi a, vi c) {
// a_{m} = \sum_{j=0}^{4} (-m1)a_{j} = 0 
                                                                                                                                                                                                                                                                                                                                                                                                                         copy(u.begin(), u.begin() + m, v.begin());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, m) (ans += v[i] * a[i]) %= P;
                                                                                                                                                          for(11 \times = 0, W = n ? 111<<(63 -
                                                                                                                                                                                                                      int b = !!(n & W); if(b) x++;
                                                                                              vector<ll> v(m, 0), u(m<1, 0);
                                                         if (n<m) return (a[n]+P)%P;</pre>
                                                                                                                                                                                                                                                            if(x < m) u[x] = 1;
                                                                                                                                                                                        fill(all(u), 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return (ans+P)%P
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        11 \text{ ans} = 0;
                                                                                                                                 V[0] = 1;
                                                                                                                                                                                                                                                                                               else {
```

MathFunction 7.21

```
| const int N = 1e6 + 7;
```

ull k = ((long double)a * b / mod + 0.1);

for (; b; b >>= 1,a = a * a % P) if (b & 1) c = c * a %P;

rep(i, 0, N) if (i < rev[i]) swap(a[i], a[rev[i]]); for (int i = 1; i < N; i <= 1) for (int j = 0, t = N / (i << 1); j < N; j += i << 1)

void FFT(int *a, int f){

return c;

if ((11)res < 0) res += mod;</pre>

return res;

ull res = a * b - k * mod;

inline ull add(ull a, ull b) {
 if ((a += b) >= mod) a -= mod;

```
for (int k = 0, l = 0, x, y; k < i; k++, l += t) x = (11) w[f][1] * a[j+k+i] % P, <math>y = a[j+k], a[j+k+i] = (y+x) % P, a[j+k+i]
                                                                              if (f) for (int i = 0, x = kpow(N, P-2); i < N; i++) a[i] = (11)a[i] * x % P;
                                                                                                                                                        int d = __builtin_ctz(N);
w[0][0] = w[1][0] = 1;
for (int i = 1, x = kpow(G, (P-1) / N), y = kpow(x, P-2); i < N; i++) {
    rev[i] = (rev[i>>1] >> 1) | ((i&1) << (d-1));
    w[0][i] = (11)x * w[0][i-1] % P, w[1][i] = (11) y * w[1][i-1] % P;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          * 首先列出所有可能的染色方案, 然后找出每个置换下保持不变的方案(不动点)数。
* 等价类数目: 所有置换的不动点数的平均值。
                                                                                                                                                                                                                                                                                                                                                  void doit(int *a, int *b, int na, int nb){ // [0, na)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (mod < int(2e9)) return a * b % mod;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                      work(), FFT(a,0), FFT(b,0);
rep(i, 0, N) a[i] = (11)a[i] * b[i] % |
FFT(a, 1);
                                                                                                                                                                                                                                                                                                                                                                               for (N = 1; N < na + nb - 1; N <= 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          //rep(i, 0, N) cout << a[i] << endl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    inline ull mul(ull a, ull b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      using ull = unsigned long long;
                                                         = (y-x+P) % P;
                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, na, N) a[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                               rep(i, nb, N) b[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      using pli = pair<ull, uint>;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 * Polya enumeration theorem
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               using uint128 = __uint128_t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            using uint = unsigned int;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     #define eb emplace_back
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            * 一个循环的颜色需相同
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   using 11 = 1ong long;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   * Burnside's lemma
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        Polya
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            namespace prime
                                                                                                                                  void work(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             \mathbf{Rho}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ull mod;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        7.23
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             7.24
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  } ntt;
  int n, M, f[N], g[N], h[N], bhi[N], u[N], p[N];
// f[n] 为 n 的最小质因子 ; g[n]=f[n]^k; phi[n] 为欧拉函数 ; u[n] 为莫比乌斯函数 ; h[n] 为一
                                                                                                                                                                                                                                                                                                                                                                       for (int j = 1, k; j <= M && p[j] <= f[i] && i * p[j] <= n; j++){
f[k = i * p[j]] = p[j];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     static const int G = 3, P = 1004535809; //P = C*2^{1}k + 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // phi[i*p[j]]=phi[i]*(p[j]<f[i]?phi[p[j]];p[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // u[i*p[j]]=u[i]*(p[j]<f[i]?u[p[j]]:0),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       /*phi[i*j]=phi[i]*phi[j] (gcd(i,j)=1)
                                                                                                                              u[1]=phi[1]=1,h[1]=(0); // 1 的时候特判
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              phi[k] = phi[i] * phi[p[j]];
u[k] = u[i] * u[p[j]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    h[k] = h[i / g[i]] * (0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            u[i*j]=u[ij*u[jj] (gcd(i,j)=1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      g[k] = g[i] * p[j];
phi[k] = phi[i] * p[j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  h[k] = h[i] * h[p[j]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int N, na, nb, w[2][M], rev[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 phi[ij^*j(j|i)]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   > /* 质数次幂特判 */
                                                                                                                                                                                                                                                                                                                                                                                                                         if (p[j] < f[i]) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              const int M = 1 << 17 << 1;
                                                                                                                                                                                                                                       f[i] = g[i] = i;
                                                                                                                                                                                                                                                                phi[i] = i - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         11 kpow(11 a, int b){
                                                                                                                                                                                                                                                                                                                                                } // 质数的时候特判
                                                                                                                                                                                                                                                                                                                                                                                                                                                        g[k] = p[j]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         u[k] = 0;
                                                                                                                                                                                                                                                                                                                   h[i] = (0);
                                                                                                                                                                                                                                                                                             u[i] = -1;
                                                                                                     void prime(int n) {
                                                                                                                                                      rep(i, 2, n+1) {
if (!f[i]) {
                                                                                                                                                                                                            ; i=[M++]d
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 }else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int a[M], b[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      11 c = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                LLZ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            struct NTT{
                                                     般积性函数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              7.22
```

```
MATH
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              45/93
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              7
                                                                                                                                                                                                                                    ull g = gcd(n, p);

if (g == 1) continue;

if (g == n) for (g = 1, y = sy; g == 1; ) y = add(mul(y, y), c), g = gcd(n)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (n > 1) ret.eb(n, 1);
if (sz(ret) - s >= 2) sort(ret.begin() + s, ret.end());
                                               for (int i = 0; i < 1; ++i) y = add(mul(y, y), c);
                                                                                                                                    for (int i = 0; i < min(s, 1 - k); ++i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   while (n \% p == 0) n /= p, e++;
                                                                                                                                                                                        p = mul(p, add(y, n - x));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          6++;
                                                                                            for (int k = 0; k < 1; k += s)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 while (n > lim && !is_prime(n)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (!is_prime(p)) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               uint e = __builtin_ctzll(n);
                                                                                                                                                                   y = add(mul(y, y), c)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      while (n \% p == 0) n /= p,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ull lim = sqr(primes.back());
For (ull l = 1; ; l <<= 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        for (ull c = 1; ; ++c) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    const db EPS = 1e-8, DINF = 1e15;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ull p = brent(n, c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           uint e = 1; n /= p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                      assert(n < (1ull << 63));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (sqr(p) > n) break;
                                                                                                                                                                                                                                                                                                           , add(y, n - x));
                                                                                                                                                                                                                                                                                                                                                                                                                               vector<pli>factors(ull n)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (e) ret.eb(p, e);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for (auto &&p: primes)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (n <= 1) return {};</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ret.eb(p, e);
                                                                                                                     ull sy = y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         uint s = sz(ret);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                vector<pli>ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ret.eb(2, e);
                                                                                                                                                                                                                                                                                                                                      return g;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (!(n & 1)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                uint e = 0;
                           ull \times = y;
                                                                    ull p = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Simplex
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  n >>= e;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 7.25
                                                                                                                                                                                                                                                                                                                                for (j = s - 1; j > 0; --j) { a = mul(a, a); if (a == n - 1) break; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                 bool is_prime(ull n) { // reference: http://miller-rabin.appspot.com
                                                                                            for (; b; a = mul(a, a), b >>= 1) if (b & 1) res = mul(res, a);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 325, 9375, 28178, 450775, 9780504, 1795265022}
```

{2, 2570940, 211991001, 3749873356u},
{2, 2570940, 880937, 610386380, 4130785767u},
{2, 325, 9375, 28178, 450775, 9780504, 179526

{2, 3}, {2, 299417}, {2, 7, 61}, {15, 176006322, 4221622697u},

static const uint base[][7] = {

assert(n < (ull(1) << 63));

bool composite(ull n, const uint* base, int m) {

int s = __builtin_ctzll(n - 1);
ull d = (n - 1) >> S; mod = n;
for (int i = 0, j; i < m; ++i) {</pre>

inline ull sqr(ull x) { return x * x; }

inline ull kpow(ull a, ull b) {

return a;

ull res = 1;return res; **if** (a == 1 | | a == n - 1) **continue**;

if (j == 0) return 1;

return 0;

ull a = kpow(base[i], d);

```
struct Simplex {
                                                                                                  ull brent(ull n, ull c) \{ // n \text{ must be composite and odd} \}
     0
for (uint j = i * i; j <= n; j += i) isp[j]
                                                                                                                                                                     ull y = 1; c \% = n; mod = n;
                                                                                                                                      const ull s = 256;
```

for (uint i = 2; i <= sq; ++i) if (isp[i]) {
 if (i != 2) primes.pb(i);</pre>

 $vector<box{bool}> isp(n + 1, 1);$

primes.clear();

uint sq = sqrt(n);

vector<uint> primes; void init(uint n)

else if $(n < 3770579582154547) \times = y = 5;$ **else if** $(n < 47636622961201) \times = y = 4;$

return !composite(n, base[x], y);

else if $(n < 4759123141) \times = 2, y = 3;$ **else if** $(n < 154639673381) \times = y = 3;$

else if $(n < 19471033) \times = 1$, y = 2;

if $(n < 1373653) \times = 0$, y = 2;

};
if (n <= 1) return 0;
if (!(n & 1)) return n == 2;
if (n <= 8) return 1;
int x = 6, y = 7;</pre>

c)

```
fbc,
                                                                                                                                                                                                                                                                                                                                                                                                                                            R, fb,
                                                                                                                                                                                                                                                                                                                                                                                                                                            return asr(a, ab, b, esp / 2, L, fa, fab, fb) + asr(b, bc, c, esp / 2,
                                                                                                                                                                                                                                                                                                                                                                                       db L = simpson(fa, fab, fb, a, b), R = simpson(fb, fbc, fc, b, c);

if (fabs(L + R - A) <= 15 * esp) return L + R + (L + R - A) / 15.0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          fc);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          fb,
                                                                                                                                                                                                                                                                                                                    db fb, db fc) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          fa,
                                                                                                                                                                                                                                            c)
{
                                                                                                                                                                                      const db eps = 1e-10; // 精度感觉一般要多设 1e-3 左右
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          fc, a,
                                                                                                                                                                                                                                            g
                                                                                                                                                                                                                                                                                                                db asr(db a, db b, db c, db esp, db A, db fa, db ab = (a + b) / 2, bc = (b + c) / 2; db fab = F(ab), fbc = F(bc);
                                                                                                                                                                                                                                        db a,
                                                                                                                                                                                                                                        inline db simpson(db fa, db fb, db fc, db a return (fa + 4 * fb + fc) * (c - a) / 6;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             db fa = F(a), fb = F(b), fc = F(c);
                                                                                                                                                                                                             inline db F(db \times) \{ F(x) = (?) \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             db asr(db a, db c, db eps)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      db b = (a + c) / 2;
                                                                                                  Simpson
                                                                                                                                                                  namespace Simpson {
return v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              }
// f(a, c)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         fc);
                                                                                                                                                                                                                                                                                                                                                                                                                                                   b[i] -= A[i][e] * b[1];
rep(j, 1, n + 1) A[i][i] -= (j!=e) * A[i][e] * A[1][j]; // 可以链式优化
A[i][e] = - A[i][e] / tmp;
```

inline int $sgn(db \times) \{ return (x > EPS) - (x < -EPS); \}$

void pivot(int 1, int e) {

 $db \ tmp = A[1][e];$

rep(i, 1, m + 1) B[i] = i + n;

 $n = _n$, $m = _m$, $v = _0$; rep(i, 1, n + 1) N[i] = i;

void init(int _n, int _m) {

* s.t.Ax <= b, x >= 0

* maxf(x)=cx

b[1] /= tmp, A[1][e] = 1 / tmp; rep(i, 1, n + 1) if (i != e) A[1][i] /= tmp; rep(i, 1, m + 1) if (i != 1 && sgn(A[i][e])) {

int n, m, B[M], N[M]; db v, ans[M], b[M], c[M], A[M][M]; // 全幺模矩阵可以改整数

static const int M = 550;

/* n — variables, m — equations

SternBrocotTree 7.27

rep(i, 1, m+1) if (sgn(b[i]) < 0 & (1 == -1 || (rand() & 1))) = i;

v += b[1] * c[e]; c[e] *= -A[1][e]; swap(B[1], N[e]);

bool ini(){ // 随机化初始解

int 1 = -1, e = -1;

if(1 == -1) break;

rep(i, 1, n + 1) c[i] -= (i!=e) * c[e] * A[l][i];

```
pii operator+(const pii &a, const pii &b) { return mp(a.fi + b.fi, a.se + b.se); }
pii operator*(const pii &a, U x) { return mp(a.fi * x, a.se * x); }
bool search(V v, U MAXB, pii &lo, pii &hi, int f) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 0.1 = 0, r = f > 0? (hi.se? (MAXB - lo.se) / hi.se : INF)
                                                                                                                                                                                                                                         typedef pair<T, T> V; // V = [double|long double|fraction]
                                                                                                                                                                                                                                                                                                                                                                                                       inline bool in(const V &a, const V &b, const V &c)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     (lo.se ? (MAXB - hi.se) / lo.se : INF);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        x = f > 0 ? 10 + hi * z : 10 * z + hi;

f * cmp(x, v) \Leftarrow 0 ? 1 = z : r = z;
                                                                                                                                                                                                                                                                                                                                                                                                                                        return 0 <= cmp(c, a) && cmp(c, b) < 0;
                                                                                                                                                                                                                                                                   inline int cmp(const V &a, const V &b) {
                                                                                                                                                                                                                                                                                                         T \times = a.fi * b.se - a.se * b.fi;
                                                                                                                                                                                                                                                                                                                                  return (x > 0) - (x < 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       U z = (1 + r) >> 1;
                                                                                                                                      typedef pair<U, U> pii;
                                                                    typedef long double db;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        while (1 + 1 < r) {
                                                                                                                                                                     const U INF = 1e9 + 7;
                                                                                                                                                                                                           typedef __int128 T;
                                                                                                     typedef int U;
                                        namespace SBT
                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(i, 1, m + 1) if (sgn(A[i][j]) > 0 && b[i] / A[i][j] < tmp) // 找基变量
r = i, tmp = b[i] / A[i][j];
rep(j, 1, n+1) if (sgn(A[1][j]) < 0 && (e == -1 \mid | (rand() \& 1))) = j;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            0 很多可以加上 break 因为转轴代价可能较小
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (delt < tmp * c[j]) l = r, e = j, delt = tmp * c[j];
                                                                                                                                                                                                                                                                                                                                                                                             rep(j, 1, n + 1) if (sgn(c[j]) > 0) { // 找非基变量
                                                                                                                                                                                                                                    b < 0 need ini()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(i, 1, m+1) if (B[i] \le n) ans[B[i]] = b[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (tmp == DINF) return DINF; // 无界
                                                                                                                                                                                                                               //if (!ini()) return —DINF; // 无解
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // 贪心取最大如果矩阵为全幺模或
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (e == -1) break; // 找到最优解
                                                                                                                                                                                                                                                              rep(i, 1, n+1) ans[i] = 0;
                              if(e == -1) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                              db tmp = DINF;
                                                                                                                                                                                                                                                                                                                                  int r, 1, e = -1;
                                                                                                                                                                                                                                                                                                                                                                 db delt = -DINF;
                                                                    pivot(1, e);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               pivot(1, e);
                                                                                                                                                                                                                                                                                               while (1) {
                                                                                                                                    return 1;
                                                                                                                                                                }
db run() {
```

```
return asr(a, b, c, eps, simpson(fa, fb,
```

```
T kpow(T a, T b) {T r=1;for(;b;b>>=1,a=mul(a,a)) {if(b&1)r=mul(r,a);}return r;} void calc(int n, T *a, T *b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 0, n+1) rep(j, 0, 2) c[i+j] = add(c[i+j], mul(a[i], b[j]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Tal[N], bl[N], c[N], a[N], pre[N], suf[N], ifac[N], fac[N]; Tadd(Ta, Tb) {a = (a + b) % P; return a < 0 ? a + P : a; T mul(Ta, Tb) {a = 111 * a * b % P; return a < 0 ? a + P : a;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for(int i = 1; i <= m && 1ll * p[j] * p[j] <= w[i]; i++){</pre>
                                                                                                                                                                                                                                                                       // S[x][y] 表示 [2, x] 中最小质因子大于等于 p[y] 的 F(i) 的和
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    tot = upper_bound(p + 1, p + cntp + 1, Sqr) - (p + 1);
rep(i, 1, cntp+1) sp[i] = sp[i-1] + f(p[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int k = t <= Sqr? id1[t] : id2[n / t];
g[i] -= f(p[j]) * (g[k] - sp[j - 1]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Ξ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         w[m] \le Sqr ? id1[w[m]] = m : id2[j] =
                                                                                                                                                            S(11 x, int y){
   if(x <= 1 || p[y] > x) return 0;
   int k = (x <= Sqr ? id1[x] : id2[n/x]);
                                                                                                                                                                                                                                            11 ret = -(g[k] - sp[y-1]); // 质数的答案
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // g[i] 表示 [2, w[i]] 中质数位置 f(i) 的和
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for(11 i = 1, j; i <= n; i = j + 1){
 j = n / (n / i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    11 solve(11 _n) {
    n = _n;if (n == 0) return 0;
    m = 0;Sqr = sqrt(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    static const int N = 101010;
static const int P = 998244353;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ilt = w[i] / p[j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            g[m] = calc(w[m]);
                           p[++cntp] = INT\_MAX;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   w[++m] = n / i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(j, 1, tot + 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             fill_n(c, n+1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return S(n,1) + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ploynomial
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          struct polynomial{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    template<class T>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       7.29
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      4 余 1 的质数个数
                                                                                                                                                            pii solve(V v, U MAXB) { // find ROUND_HALF_UP(a / b) = v, b <= MAXB V L = mp(v.fi * 10 - 5, v.se * 10); V R = mp(v.fi * 10 + 5, v.se * 10); V R = mp(v.fi * 10 + 5, v.se * 10);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              struct Min_25{
// F(i) 要拆成多个完全积性函数的和
// 或者 F(i) 的质数位置前缀和能通过埃氏筛法 dp 求出,如求模
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for(int j = 1; j <= cntp && i * p[j] <= n; j++){
  isp[i * p[j]] = 1;
  if(i % p[j] == 0)break;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (t2 - t3 \le t3 - t1) return hi;else return lo;
                                                  r = f * cmp(x, v) \le 0 ? r : 1;

f > 0 ? 1o = 1o + hi * r : hi = 1o * r + hi;
                                                                                                                                                                                                                                                                                                                           //V m = mp(lo.fi + hi.fi, lo.se + hi.se);
//if (in(L, R, m)) return mp(m.fi, m.se);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // 要求的积性函数 F(p ^ e)
11 F(int p, int e) { return e == 1 ? -1 : 0;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int Sqr, m, p[N], id1[N], id2[N], tot, cntp;
11 g[N], sp[N], h[N], n, w[N];
                             = f > 0 ? lo + hi * r : lo * r + hi;
                                                                                                                                                                                                                                                                                                                                                                                   hi, 1);
hi, -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // 假设都是质数的完全积性函数前缀和去掉11 calc(11 n) { return n - 1;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    //if (in(L, R, lo)) return lo;
//if (in(L, R, hi)) return hi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(i, 2, n+1) {
    if(!isp[i]) p[++cntp] = i;
                                                                                                                                                                                                                                                                                                                                                                                   ok |= search(v, MAXB, lo, ok |= search(v, MAXB, lo,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          db t1 = (db) lo.fi / lo.se;
db t2 = (db) hi.fi / hi.se;
db t3 = (db) v.fi / v.se;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             static const int N = 1e6 + 7;
                                                                                                                                                                                                                                              pii lo(0, 1), hi(1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              11 f(int p) { return 1;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               cntp = 0; isp[1] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return mp(-1, -1);
                                                                                                                                                                                                                                                                                                                                                                                                            ok |= search(v,
if (!ok) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void prime(int n){
                                                                                                                                                                                                                                                                         while (true) {
bool ok = 0;
                                                                                                          return r > 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // f(p) = p \wedge k
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            bool isp[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       min
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   7.28
```

```
11 qpolysum(11 R, 11 n, 11 *a, 11 m) { // a[0].. a[m] \\Sum_{[i=0}\^{n-1}\\ a[i]\^{n-1}\) if (R == 1) return Polysum(n, a, m);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 il t = mul(ifac[i], ifac[m+1-i]);
p3 = i & 1 ? add(p3, -mul(h[i][0], t));
p4 = i & 1 ? add(p4, -mul(h[i][1], t)); add(p4, mul(h[i][1], t));
                                                                                                                                                                                                                                                                                                                                                                                                                       (n-i) % P);
(n-d+i) % P);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     c = mul(kpow(p4, P - 2), -p3);
rep(i, 0, m+2) h[i][0] = add(h[i][0], h[i][1] * c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ans = add(mul(calcn(m, C, n), kpow(R, n)), -c);
                                                                                                                                                                                                                                                                                                                                  t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ans;
    ans = (d-i)&1 ? add(ans, -t) : add(ans,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ပ်
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              h[i][0] = mul(h[i-1][0] + a[i-1], r);

h[i][1] = mul(h[i-1][1], r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(i, 1, m+2) a[i] = add(a[i-1], a[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              p4 = 0,
                                                                                                                                                                                                                                                                    11 s2 = mul(ifac[i], ifac[d - i]);
                                                                                                                  rep(i, 0, d+1) p1[i+1] = mul(p1[i], rep(i, 0, d+1) p2[i+1] = mul(p2[i],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int j=0;j<cntp&&p[j]*i<N;j++){</pre>
                                                                                                                                                                                                                                                                                              ll t = mul(mul(s_1, s_2), a[i]);
                                                                                                                                                                                                                                       il s1 = mul(p1[i], p2[d-i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         11 r = kpow(R, P - 2), p3 = 0,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(i, 0 ,m+2) C[i] = h[i][0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              a[m+1] = calcn(m, a, m+1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            a[m+1] = calcn(m, a, m+1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return calcn(m+1, a, n—1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     h[0][0] = 0; h[0][1] = 1; rep(i, 1, m+2) {
                                                           if (n <= d) return a[n];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 2, N) {
    if (isp[i]) p[cntp++]=i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               fill_n(isp + 2, N - 2, 1);
                                                                                      p1[0] = p2[0] = 1;
                                                                                                                                                                                                             rep(i, 0, d+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 0, m+2) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        const int N = 1e6 + 6;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int low[N], cntp, p[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // low[] : optional
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void getprime() {
                                                                                                                                                                                                                                                                                                                                                                                              return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 prime
                                                                                                                                                                                  11 ans=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // time : O(n)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    bool isp[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               7.31
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 11 a[D], fac[D], ifac[D], pi[D], p2[D], h[D][2], C[D];
11 add(11 a, 11 b) {a = (a + b) % P; return a < 0 ? a + P : a;}
11 mul(11 a, 11 b) {a = 111 * a * b % P; return a < 0 ? a + P : a;}
11 kpow(11 a, 11 b) {11 r=1;for(;b;b>>=1,a=mul(a,a)) {if(b&1)r=mul(r,a);}return r;}
                                                                                                                rep(i, 0, n+1) {
fill_n(a1, n+1, 0); a1[0] = 1;
rep(j, 0, n+1) if (j != i) a1[0] = mul(a1[0], x[i] - x[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        \vec{T} \ s1 = y[i], \ s2 = 1; \\ rep(j, 0, n+1) \ \textbf{if} \ (j != i) \ s1 = mul(s1, \ k-x[j]); \\ rep(j, 0, n+1) \ \textbf{if} \ (j != i) \ s2 = mul(s2, x[i]-x[j]); 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    fac[0] = 1; rep(i, 1, M+5) fac[i] = mul(fac[i-1], i); ifac[M+4] = kpow(fac[M+4], P - 2);
                                                           void solve(int n, T *x, T *y){ // a[0]^*x^{\wedge 0} ... a[n]^*x^{\wedge n}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              fac[0] = 1; rep(i, 1, n+1) fac[i] = mul(fac[i-1], i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(i, 1, n+1) pre[i] = mul(pre[i-1], k-i); per(i, 1, n+1) suf[i] = mul(suf[i+1], k-i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ans = add(ans, mul(fg*s1, mul(s2, y[i]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                res = add(res, mul(s1, kpow(s2, P - 2)));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          per(i, 0, n) ifac[i] = mul(ifac[i+1], i+1);
pre[0] = suf[n+1] = 1;
                                                                                                                                                                                                                                                                                                                                                              rep(j, 0, n+1) a[j] = add(a[j], a1[j]);
                                                                                                                                                                                                         a1[0] = mul(y[i], kpow(a1[0], P - 2));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          static const int D = 101000, P = 998244353;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   T get(int n, int k, T *y) { // x is [1..n]
                                                                                                                                                                                                                                                                                                                                                                                                                                                  T get(int n, int k, T *x, T *y) \{ // f(k)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   T s2 = mul(ifac[i-1], ifac[n-i]);
memcpy(a, c, sizeof(a[0]) * (n+1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   T s1 = mul(pre[i-1], suf[i+1]);
                                                                                                                                                                                                                                       rep(j, 0, n+1) if (j = i) {
                                                                                                                                                                                                                                                                    b1[0] = -x[j]; b1[1] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ifac[n] = kpow(fac[n], P - 2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 T fg = (n-i)&1 ? -1 : 1;
                                                                                                                                                                                                                                                                                                       calc(n, a1, b1);
                                                                                      fill_n(a, n+1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(i, 0, n+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(i, 1, n+1){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void init(int M) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 polysum
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             struct polysum {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   T ans=0;
```

//low[p[j] * i] = p[j]

per(i, 0, M+4) ifac[i] = mul(ifac[i+1], i+1);

```
(a[2] & c.a[2]);
                                                                                                                                                                                                                                                                                             r.a[1] = (a[0] & c.a[1]) | (a[1] & c.a[0]) | (a[2] & c.a[2]);
r.a[2] = (a[0] & c.a[2]) | (a[2] & c.a[0]) | (a[1] & c.a[1]);
r.a[0] ^= r.a[1] ^ r.a[2];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  x = (x % 3 + 3) % 3;
if (x == 1) { swap(r.a[0], r.a[2]); swap(r.a[1], r.a[2]); }
if (x == 2) { swap(r.a[0], r.a[2]); swap(r.a[0], r.a[1]); }
                                                              r.a[0] = a[0] | c.a[0];
r.a[1] = (a[1] & c.a[1]) | (a[2] & c.a[2]);
r.a[2].set(); r.a[2] ^= r.a[0] ^ r.a[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                             inline vec3 operator — (const vec3 &c) const {
inline vec3 operator * (const vec3 &c) const
                                                                                                                                                                                                                                 inline vec3 operator + (const vec3 &c) const
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (x == 0) { r.ini(); }
if (x == 2) { swap(r.a[1], r.a[2]); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            inline vec3 operator * (int x) const {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      inline vec3 operator + (int x) const{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return (*this) + (c * -1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      x = (x \% 3 + 3) \% 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             vec3 r = *this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         vec3 r = *this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return r;
                                                                                                                                                                  return r;
                                                                                                                                                                                                                                                                                                                                                                                                 return r;
```

cntp = 2;p[0] = 2;p[1] = 3;for (int i = 5, k = 1; i <= N; (k & 1) ? i+=2 : i+=4 , k++){

int cntp,p[M];
void getprime(int N) {

bitset<N / 3 + 1> isp;

// int low[N],

const int N = 3e7 + 6, M = 2e6 + 6;

// 优化版欧拉筛法 bitset 需要

isp[p[j] * i] = 0; if (i % p[j] == 0) break; for (int j = 2; j < cntp && p[j] * i <= N; j++)
// low[p[j] * ij = p[j];
isp[p[j] * i / 3] = 1;</pre>

// low[i] = i;

p[cntp++]=i;

if (!isp[k]) {

 $if(i\%p[j] == \overline{0})$ break;

7.33 划分数

```
const int N = 1e6 + 5, P = 998244353;
int n, f[N], fv[N];
inline int add(int a, int b) { if((a += b) >= P) a -= P; return a < 0 ? a + P : a;}

void init(int n) {
    f[0] = f[1] = 1;
    int m = sqrt(n) + 1;
    rep(i, 1, m+1) fv[i] = i * (3 * i - 1) / 2;
    rep(i, 1, m+1) fv[i] = i * (3 * i - 1) / 2;
    rep(i, 2, n+1) {
        for(int j = 1; fv[j] <= i; j++) {
            f[i] = add(f[i], j & 1 ? f[i - fv[j]] - j]);
        f[i] = add(f[i], j & 1 ? f[i - fv[j] - j] : -f[i - fv[j] - j]);
    }
}</pre>
```

7.34 原根

```
11 Pow(11 x, 11 k, 11 p)
```

for(; i <= n; (j&1) ? i+=2 : i+=4 , j++) if(bit[j] == 0) p[cntp++]=i;</pre>

int i, j; cntp = 2; p[0] = 2; p[1] = 3; for(i = 5, j = 1; i * i <= n; (j & 1) ? i += 2 : i += 4 , j++) { if(bit[j] == 0) {

const int N = 3e8 + 6, M = 2e7 + 6;

bitset<N / 3 + 1> bit;

int cntp,p[M];

void getprime(int n){

// 优化埃氏筛法空间最小可以不存质数

for(int j = i * i; j <= n; j += i)
if(j % 2 != 0 && j % 3 != 0) bit[j / 3] = 1;</pre>

```
rep(i, 0, phi) if (\_gcd((ll)i, phi) == 1) ret.pb(kpow(g, i, p));
     d
 == 4) return phi = p + 1 >> 1,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          n,
m,
                                                                                                                       for (auto &t : P) t = phi / t;
for (g = 1; __gcd(g, p) != 1 || !check_g(g, p); ++g);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ⊢`
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int c[N], k[N], col[N], u[N], v[N], w[N], sum, ans,
                                                                        for (auto t : P) phi = phi / t^*(t-1)
                                                                                                                                                                                                                      inline vector<ll> getAllRoot(ll p) {
                                                                                                                                                                                                                                                 vector<ll> ret; ll g = getRoot(p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   vi g[N]; bool vis[N], exist[N];
                                                                                                                                                                                                                                                                                                                         sort(all(ret));        return ret;
if (p == 1 || p == 2 || p
                      if (!check(p)) return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             const int N = 85, INF = pw(30);
                                                                                                                                                                                                                                                                        if (g == -1) return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                      带权拟阵交
                                                                                                  factor(phi);
                                                                                                                                                                            return g;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             struct GM {
                                                                                                                                                                                                                                                                                                                                                                                                                        7.36
 11 ret = 1;   
for (; k; k >>= 1, x = x*x\%p) if (k & 1) ret = ret*x\%p;
                                                                                                                                                                     rep(i, 0, sz(c)) if (Pow(g, c[i], p) == 1) return 0;
                                                                                                                                                                                                                                                                                                                         for (11 k = 2; k^*k \le tmp; ++k) if (tmp % k == 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(i, 0, sz(c)) c[i] = (p-1) / c[i];
for (g=1); icheck_g(g, p); ++g);
                                                                                                                                                                                                                                                                                                                                                                     while (tmp \% k == 0) tmp /= k;
                                                                                                                                                  inline bool check_g(ll g, ll p)
                                                                                                                                                                                                                                                                                                                                                                                               }
if (tmp != 1) c.pb(tmp);
                                                                                                                                                                                                                                                 inline 11 getRoot(11 p)
                                                                                                                                                                                                                                                                                                  11 tmp = p - 1, g;
                                                                                                                                                                                                                                                                                                                                                  c.pb(k);
                                                                                                                                                                                                                                                                           c.clear();
                                                                                                struct Euler {
  vector<ll> c;
                                                                                                                                                                                               return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return g;
                                                     return ret;
```

Ή,

```
d[N], cost[N]; bool inq[N], has[N]; vi g[N]; queue<int>
                                                                                                                                                                                                                                     tot2;
tot,
                                                                                                                                                                                                                                                                                                                                                                                                                                                            for(auto x : vec) cnt[col[x]]++;
rep(i, 1, m+1) if(cnt[i] > c[i] - k[i]) return 0;
return 1;
                                                                                                                                                                     rep(i, 1, n+2) g[i].clear(), vis[i] = 0;
memset(exist, 1, sizeof(exist));
for(auto x : vec) exist[X] = 0;
                                                                                                     for(auto \ v : g[u]) if (!vis[v]) dfs(v);
                                                                                                                                                                                                                                                                          rep(i, 1, n+2) if(!vis[i]) return 0;
return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                      memset(cnt, 0, sizeof(cnt));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        template <class MT1, class MT2>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     inq[i] = pre[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int n, S, T, pre[N],
MI(int n) : n(n) {}
                                                                                                                                               bool test(vi &vec) {
                                                                                                                                                                                                                                                                                                                                                                                                                   bool test(vi &vec) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void clear() {
    rep(i, 1, n+3) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                g[i].clear();
                                                           void dfs(int u) {
                                                                                    vis[u] = 1
                                                                                                                                                                                                                                                                                                                                                                                          int cnt[125];
                                                                                                                                                                                                                                                           dfs(1);
                                                                                                                                                                                                                                                                                                                                                                         struct CM {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              struct MI {
```

<u>.</u>

```
inline bool check_g(ll g, ll p) {
    rep(i, 0, sz(P)) if (kpow(g, P[i], p) == 1) return 0;
    return 1;
                                                                                                   for (; k; k >>= 1, x = x^*x\%p) if (k & 1) ret = ret*x%p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           == 2) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (P[0] != 2 || P[0] == 2 \&\& A[0] > 1) return 0;
                                                                                                                                                                                                                                                                                                                                                                          for (11 k = 2; k^*k \le m; ++k) if (m\%k == 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        //if (m==1 || m==2 || m==4) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (sz(P) > 2 | | sz(P) == 1 \&\& P[0]
                                                                                                                                                                                                                                                                                                                                                                                                                     while (m%k == 0) m /= k, cnt++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (m > 1) P.pb(m), A.pb(1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (sz(P) == 1) return 1;
                                                                                                                                                                         struct Euler {
  vector<ll> P, A; ll phi, g;
                                                                                                                                                                                                                                                                                                                       inline void factor(ll m) {
                                                                                                                                                                                                                                                                                                                                                                                                                                              P.pb(k), A.pb(cnt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             inline 11 getRoot(11 p) {
                                                                                                                                                                                                                                                                                                                                                  P.clear(), A.clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                inline bool check(11 m)
                                                        11 kpow(11 x, 11 k, 11 p)
                                                                                                                                                                                                                                                                                                                                                                                             int cnt = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                factor(m);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return 1;
                                                                           ll ret = 1;
原根
                                                                                                                               return ret;
 7.35
```

7.37 拟阵交

template <class MT1, class MT2>

```
if (!inq[v]) q.push(v), inq[v] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int la = pre[T];
while (la != S) has[la] ^= 1, la = pre[la];
                                                                                                                                                                                                                                                                                                                                                                                vi tmp = getcur();
if (mt1.test(tmp)) g[S].pb(i); // X1
if (mt2.test(tmp)) g[i].pb(T); // X2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               vi tmp = getcur();
rep(j, 1, n+1) if (!has[j] && i != j) {
   tmp.pb(j);
   if (mt1.test(tmp)) g[i].pb(j);
   if (mt2.test(tmp)) g[j].pb(j);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           while(!q.empty()) {
   int u = q.front(); q.pop(); inq[u] = 0;
   for(auto v : g[u])
    if(d[v] < d[u] + cost[v]) {
        d[v] = d[u] + cost[v];
}</pre>
                                                                                                                                                                                                     memset(has, 0, sizeof(has));
S = n + 1, T = n + 2, cost[S] = cost[T] = 0;
while (1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (!pre[T]) return mp(getcur(), ans);
                                                                                    rep(i, 1, n+1) if(has[i]) ret.pb(i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      d[S] = 0; q.push(S); inq[S] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(i, 1, n+1) if (has[i]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          } else cost[i] = -w[i];
                                                                                                                                                                             ll ans = 0; MT1 mt1; MT2 mt2;
while(!q.empty()) q.pop();
                                                                                                                                                                                                                                                                                          rep(i, 1, n+1) {
    if(!has[i]) {
        cost[i] = w[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                tmp.pop_back();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             pre[v] = u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                      has[i] ^= 1;
                                                                                                                                                                                                                                                                                                                                                            has[i]^= 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            has[i] ^= 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           has[i] ^= 1;
                                                                                                                                                        pair<vi, 11> run() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           //hdu 6636 Milk Candy
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ans += d[T];
                      }
vi getcur() {
                                                                                                                return ret;
                                                                                                                                                                                                                                                                       clear();
                                                                     vi ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int main() {
    cin >> T;
```

.; ()

۵,

ж %

a % P) if (b & 1) r =

t = t * x % P; }

۳, sa %

z = z * Inv(w, P) % P, ans = bsgs(x, z, P);

return ans + (ans !=-1) * C;

//Pick Your Own Nim

```
else for(auto x : res) if (col[x] > n) cout \Leftrightarrow val[x] \iff endl;
                                                                                                                                                                                                                                                        rep(j, 0, k) cin \gg x, val[++tot] = x, col[tot] = tot2;
                                                                                                                 = ++tot2;
//In real cases, Linear Matroid Need Optimization to Pass
                                                                                                            rep(i, 0, n) cin \Rightarrow x, val[++tot] = x, col[tot]
                                                                                                                                                                                                                                                                                                                                                                                                                if (sz(res) < n + m) cout << -1 << end1;
                                                                                                                                                                                                                                                                                                                                             MI<LM, CM> matint(tot);
                                                                                                                                                                                                                                                                                                                                                                                vi res = matint.run();
                                                                                                                                                                                                                              cin >> k; tot2++;
                                                                                                                                                                                           rep(i, 0, m) {
                                                                                                                                                     cin >> m;
                                                                           cin >> n;
                                        int main() {
                                int n, pre[N], id[N]; bool vis[N], sink[N], has[N]; queue<int> q;
                                                                                                                                                                                                                                                                                                                                                                                                                                                         void push(int v, int p) { vis[v] = 1, pre[v] = p, q.push(v); }
                                                                                                                                                                                                                                                                                                                                          rep(i, 1, n+1) if (has[i]) ret.pb(i), id[i] = sz(ret) - 1;
```

rep(i, 1, n+1) vis[i] = sink[i] = pre[i] = 0;

MI(int n) : n(n) {}

struct MI {

void clear() {

while (!q.empty()) q.pop();

vi getcur() { vi ret;

离散对数 7.38

memset(has, 0, sizeof(has));

MT1 mt1; MT2 mt2;

vi run() {

return ret;

```
? (ex_gcd(b, a \% b, y, x), y = a / b * x) : (x = 1, y =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if (x % P == 0) return -1;
1l res = 2 % P, sa, t = 1, sq = sqrt(P); M.clear();
rep(i, 0, sq + 1) { if (M.count(t)) break; M[t] = i,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 0, t + 1) if (M.count(res))
return i * sq + M[res]; else res = res
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  z /= t, P /= t, w = w * x / t % P, C++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        t = P / sq, sa = Inv(kpow(x, sq, P), P);
                                                                                                                                                                                              void ex_gcd(int a, int b, int &x, int &y) {
                                                                                                                                                                                                                                                                                                        inline int Inv(int a, int P) {
   int x, y; ex_gcd(a, P, x, y);
   return x < 0 ? x + P : x;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                11 bsgs(11 x, 11 z, 11 P) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (z % t) return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (z == w) return c;
                                                                                         я
=
*
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         unordered_map<11, int> M;
                               11 kpow(11 a, 11 b, 11 P)
                                                            11 r = 1;
for (; b; b >>= 1,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                              struct BSGS {
                                                                                                              return r;
                                                                                                                                                                                                                         q
                                                                                                                                                                                                                  rep(i, 1, n+1) if (sink[i] && vis[i]) { has[i] ^{\wedge} 1; ok = 1; break;}
                                                                                                                                                                                                                                                                                                  vector<M1> vmt1(sz(cur)); vector<M12> vmt2(sz(cur));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int u = q.front(); q.pop();
if (sink[u]) { t = u; break;}
rep(v, 1, n+1) if (!vis[v] && has[u] != has[v]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(vmt2[id[v]].test(col[u])) push(v, u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(vmt1[id[u]].test(va1[v])) push(v, u);
                                                    for(auto \times : cur) mt1.add(val[x]), mt2.add(col[x]);
                                                                                                      if(mt1.test(val[i])) push(i, 0); // X1;
if(mt2.test(col[i])) sink[i] = 1; // X2;
                                                                                                                                                                                                                                                                                                                             rep(i, 0, sz(cur))
rep(j, 0, sz(cur)) if (i != j)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (t == -1) return cur;
while (t) has[t] ^= 1, t = pre[t];
                                                                                                                                                                                                                                                                                                                                                                                 vmt1[i].add(val[cur[j]]);
                                                                                                                                                                                                                                                                                                                                                                                                            vmt2[i].add(co1[cur[j]]);
                                                                               rep(i, 1, n+1) if (!has[i])
vi cur = getcur(); clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       while(!q.empty()) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(has[u])
                           MT1 mt1; MT2 mt2;
                                                                                                                                                                                                                                              if (ok) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               else {
                                                                                                                                                                                         bool ok = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int t = -1;
```

:pow =% ×

struct CRT {

```
if (p == 1 || p == 2 || p == 4) return phi = p + 1 >> 1, phi_phi = 1, p - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                            .,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for (g = 1; __gcd(g, p) != 1 || !check_g(g, p); ++g);
                                                                                                                                                        = (R % M + M) % M; // 可能为 Ø 看是否需要是正整数
                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, sz(P)) if (kpow(g, P[i], p) == 1) return
                                                                                                       R += inv^* ((a[i] - R) / g) \% (mod[i] / g) * M;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             inline void norm(11 &x, 11 p) { x = (x%p + p) % p; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             <u>.</u>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (sz(P) > 2 | | sz(P) == 1 \& P[0] == 2) return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (P[0] != 2 || P[0] == 2 && A[0] > 1) return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              <u></u>
                                                                                                                                                                                                                                                                                                                                                                          struct Euler {
   v11 P, A, _P, _A; 11 phi, g, phi_phi; BSGS T;
   inline bool check_g(11 g, 11 p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        factor(phi, P, A), phi_phi = get_phi(phi);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, sz(P)) phi = phi / P[i] * (P[i]
                        P.clear(), A.clear(); for (11 k = 2; k^*k <= m; ++k) if (m%k ==
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         inline void factor(ll m, vll &P, vll &A)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for (auto t:P) phi=phi/t*(t-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  //if (m==1 || m==2 || m==4) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // solve equation: ax=b(\%p), gcd(a,p)!=1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, 0, sz(P)) P[i] = phi / P[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              while (m%k == 0) m /= k, cnt++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for (auto &t:P) t=phi/t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if (m > 1) P.pb(m), A.pb(1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (!check(p)) return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (sz(P) == 1) return 1;
                                                                                                                             M = M / g * mod[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inline 11 get_phi(11 p) {
    11 phi = p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       inline 11 getRoot(11 p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     inline bool check(ll m) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      P.pb(k), A.pb(cnt);
                                                                                                                                                                                                                                                                                                                                                 typedef pair<11, 11> pll;
ep(i, 2, n + 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   phi = get_phi(p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          factor(m, P, A);
                                                                                                                                                                                                                                                                                                                         typedef vector<ll> vll
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int cnt = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return phi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return g;
                                                                                                                                                                                                                return R;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return 1;
                                                                                                                                                                                                                                                                 } crt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           11 res = z \% P, sa, t = 1, sq = sqrt(P); M.clear(); rep(i, 0, sq + 1) { if (M.count(t)) break; M[t] = i, t = t * x % P;
                                                                                                                                                                                                                                            void ex_gcd(11 a, 11 b, 11 &x, 11 &y) {
 b ? (ex_gcd(b, a % b, y, x), y = a / b * x) : (x = 1, y = 0);
                                                                                                                                                                    ۳,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           11 t = 1 % P, w = 1, ans, C = 0; Z %= P; rep(i, 0, 51) { if (t == z) return i; t = t * x % P; }
                                                                                                                                                                for (; b; b >>= 1, a = a * a % P) if (b & 1) r = r * a %
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return i * sq + M[res]; else res = res * sa % P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for (t = \_gcd(x, P); t != 1; t = \_gcd(x, P)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ex_bsgs(11 x, 11 z, 11 P) { //x^y==z(mod P) }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    = bsgs(x, z, P);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      z /= t, P /= t, w = w * x / t % P, C++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              t = P / Sq, Sa = Inv(kpow(x, Sq, P), P);
rep(i, 0, t + 1) if (M.count(res))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (b == 0) \{ x = 1; y = 0; return; \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       void exgcd(ll a, ll b, ll &x, ll &y)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  11 M, R; static const int N = 55;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return ans + (ans != -1) * c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ..
×
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  = z * Inv(w, P) % P, ans
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     11 bsgs(ll x, ll z, ll P) {
   if (x % P == 0) return -1;
                                                                                                                                                                                                                                                                                                                                                          11 x, y; ex_gcd(a, P, x, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (z \% t) return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (z == w) return c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return x < 0? x + mod
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           exgcd(b, a % b, y, x);
                                                                                                                                       11 r = 1; assert(b >= 0);
                                                                                                                                                                                                                                                                                                                             inline 11 Inv(11 a, 11 P) {
                                                                                                                                                                                                                                                                                                                                                                                  return x < 0 ? x + P : x;
                                                                                                               11 kpow(11 a, 11 b, 11 P) {
                                                 小
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 M = mod[1], R = a[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 exgcd(a, mod, x, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   }
11 Inv(11 a, 11 mod) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    11 \times = 0, y = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        y = a / b * x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             }
11 solve(11 n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           11 a[N], mod[N];
                                                 高次同余
                                                                                                                                                                                                                                                                                                                                                                                                                                                            map<11, int> M;
```

return -1;

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struct BSGS {

return r;

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inline void norm(11 &x, 11 p) { x = (x%p + p) % p; }

inline 11 get_phi(11 p)

for (auto t : P) phi = phi / $t^*(t-1)$

11 kpow(11 a, 11 b, 11 P) {
 11 r = 1; assert(b >= 0);

高次同余

7.40

```
t = t * x % P; }
                                                                                                  b > (ex_gcd(b, a \% b, y, x), y = a / b * x) : (x = 1, y = 0);
 ۳,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        r * a %
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               .;
o
                                                                                                                                                                                                                                                                                                  ۳,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, 0, sz(P)) if (kpow(g, P[i], p) == 1) return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return i * sq + M[res]; else res = res * sa %
 П
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for (11 k = 2; k^*k \le m; ++k) if (m%k == 0)
 a = a * a % P) if (b & 1) r
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  z = z * Inv(w, P) % P, ans = bsgs(x, z, P);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        z /= t, P /= t, w = w * x / t % P, C++
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                struct Euler {
  vll P, A; ll phi, g, phi_phi; BSGS T;
  inline bool check_g(ll g, ll p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               while (m%k == 0) m /= k, cnt++
                                                                       void ex_gcd(ll a, ll b, ll &x, ll &y)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return ans + (ans !=-1) * c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (m > 1) P.pb(m), A.pb(1);
                                                                                                                                                                              11 x, y; ex_gcd(a, P, x, y);
return x < 0 ? x + P : x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (z == w) return c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    inline void factor(ll m) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     P.pb(k), A.pb(cnt);
                                                                                                                                                    inline 11 Inv(11 a, 11 P) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  P.clear(), A.clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          typedef pair<11, 11> pll;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              typedef vector<ll> vll,
for (; b; b >>= 1,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int cnt = 0;
                                                                                                                                                                                                                                                         struct BSGS {
  map<11, int> M;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return 1;
                         return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              9
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       } // solve equation: x^a=b(\%p), p could not be a prime, but p must have a primitive
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Ш
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        11 g = t.se, x = t.fi, ans = kpow(g, x, p), d = kpow(g, p / g, p), ret
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              factor(p, _P, _A); int tot = sz(_P); ll ret = 1, ans; pll tmp[32];
rep(i, 0, tot) {
                                                                                                  return mp(kpow(a, phi_phi - 1, p)*b%p, g);//note that phi_phi
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          (cnt) t1 = get_pow(pp, cnt), t2 = get_pow(pp, cnt / a),
                                                                                                                                                                                                                                                                                                                                                            ll p = get_pow(pp, k); norm(b, p); ll t1, t2, t3; if (!a) return b == 1? mp(0, p) : mp(-1, 0ll); if (!b) return mp(!a, get_pow(pp, k-(k-1)/(a-1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           tmp[i + 1] = solve_high(a, b, _P[i], _A[i]),
                                                                                                                                                                                                                                                                                                                                                                                                                                     11 g = getRoot(p);
if (g == -1) return mp(-1, 0);
int cnt = 0; while (b%pp == 0) b /= pp, cnt++;
                                                                                                                                                                                                                                                             } // solve equation: x^a=b(\%pp^\lambda k), pp is a prime
                     norm(a, p); norm(b, p); ll g = gcd(a, p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (cnt%a) return mp(-1, 0); bool ok = 0;
if (cnt) t1 = get_pow(pp, cnt), t2 = get_p
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        crt.mod[i + 1] = get_pow(_P[i], _A[i])
                                                                                                                                                                                                                                                                                                            pll solve_high(ll a, ll b, ll pp, int k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // 注: 返回 pair( 最小非负解 , [0,p) 中解的个数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        pair<ll, ll> t = solve(a, _b, _p);
if (t.fi == -1) return mp(-1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  \dot{t}3 = \dot{t}1 / \dot{t}2, ok = 1, p /= \dot{t}1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             11 _b = T.ex_bsgs(g, b, p);
if (_b == -1) return mp(-1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                pll solve_high(ll a, ll b, ll p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       crt.a[i + 1] = tmp[i + 1].fi,
                                                                                                                                                                                                                                                                                                                                  assert(pp > 1), assert(k > 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (ok) ans *= t2, ret *= t3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          root, that is 8 cannot divide p
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (p == 1) return mp(0, 1);
                                                                                                                                                      get_pow(11 p, int k) {
11 ret = 1; assert(k >= 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (!ret) return mp(-1, 0);
                                                   if (b%g) return mp(-1, g);
pll solve(ll a, ll b, ll p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        assert(p > 0); norm(b, p);
                                                                                                                                                                                                       rep(i, 0, k) ret = ret*p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             11 _{p} = p / pp^{*}(pp - 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          *= tmp[i + 1].se;
                                                                         /= g, b /= g, p /= g;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ans = crt.solve(tot);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return mp(ans, ret);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return mp(ans, ret)
                                                                                                                                                                                                                                   return ret;
                                                                                                                              11}
```

```
Returns one plus the index of the least significant 1-bit of x, or if x is zero, returns
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Returns the number of leading 0—bits in x, starting at the most significant bit position
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int _builtin_ctz (unsigned int x) Returns the number of trailing \theta-bits in x, starting at the least significant bit
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Returns the parity of x, i.e. the number of 1—bits in x modulo 2.
                                                                                                                                                                                                                                                                                                     rep(i, 0, n) {
    for(int j = (1 << n) - 1; -j; -j) if(!(j >> i & 1)) {
        upd(s[j], s[j | (1 << i)]);
}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     position. If x is 0, the result is undefined
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               _builtin_ffsll (unsigned long long)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int __builtin_popcount (unsigned int x)
                                                                                                                     rep(i, 0, n) {
    rep(j, 0, 1 << n) if(j >> i & 1)
    upd(s[j], s[j ^ (1 << i)]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int __builtin_parity (unsigned int 	imes)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             . If x is 0, the result is undefined
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int __builtin_clz (unsigned int x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          Returns the number of 1-bits in x.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int __builtin_ffs (unsigned int x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int __builtin_ffsl (unsigned long)
    for(int i = x; i; (—i) & x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            b.set(); // all to 1
b.reset(); // all to 0
b.flip(); // all = 0 <->
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 b.test(p); // b[p] is 1
b.reset(p);// b[p] = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     b.set(p); // b[p] = 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          b.count(); // cnt of 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // all 0 ?
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // has 1 ?
                                                                                                                                                                                                                                                                       // 统计超集的答案
                                                                                       // 统计子集的答案
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Bitset
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         b.none();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           b.any();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Base
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               8.2
                                                                                                                                                                                                                                                                                                                               inline 11 getRoot(11 p) {
    if (p == 1 || p == 2 || p == 4) return phi = p + 1 >> 1, phi_phi = 1, p - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (t.fi == -1) return ret;
11 _g = t.se, x = t.fi, ans = kpow(g, x, p), d = kpow(g, _p / _g, p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return mp(kpow(a, phi_phi - 1, p)*b%p, g);//note that phi_phi
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (g = 1; \_gcd(g, p) != 1 || !check\_g(g, p); ++g);
                                                                                                                                                                                    == 2) return 0;
                                                                                                                                                                                                                                              .
0
                                                                                                                                                                                                                                         if (P[0] != 2 || P[0] == 2 && A[0] > 1) return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // solve equation: x^{\wedge}a=b(\%p), p must be a prime
rep(i, 0, sz(P)) phi=phi/P[i]*(P[i]-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              norm(a, p); norm(b, p); ll g = __gcd(a, p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(i, 1, _{-g}) ans = ans*d%p, ret.pb(ans);
                                                                                                                   //if (m==1 || m==2 || m==4) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // solve equation: ax=b(\%p), gcd(a,p)!=1 pll solve(ll a, ll b, ll p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                  factor(phi), phi_phi = get_phi(phi);
for (auto &t : P) t = phi / t;
                                                                                                                                                                               if (sz(P) > 2 || sz(P) == 1 \&\& P[0]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              vll solve_high(ll a, ll b, ll p) {
    vll ret; norm(b, p); assert(p > 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(i, 0, sz(P)) P[i]=phi/P[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  };
// 注 : 返回所有 [0,p) 中的非负整数解
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (b\%g) return mp(-1, g);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                11 g = getRoot(p);
if (g == -1) return ret;
11 _b = T.bsgs(g, b, p);
if (_b == -1) return ret;
                                                                                                                                                                                                           if (sz(P) == 1) return 1;
                                                                                                                                                                                                                                                                                                                                                                                           if (!check(p)) return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      pll t = solve(a, _b, _p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (!a == b) ret.pb(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        a /= g, b /= g, p /= g;
                                                                                       inline bool check(11 m)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (!b) return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      sort(all(ret));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      11_{p} = p - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ret.pb(ans);
                                  return phi;
                                                                                                                                                      factor(m);
                                                                                                                                                                                                                                                                            return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return g;
```

<-> 0 =

b.flip(p); // b[p]

// _builtin_ctz in bitst b._Find_first();

// Black tech

BitOperation

// 枚举子集

Others

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.
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ~FastIO() { if (wpos) fwrite(wbuf, 1, wpos, stdout), wpos = 0; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  inline void wstring(const char *s) { while (*s) wchar(*s++); }
                                                                                                                                                                                                                                               for (; '0' <= c && c <= '9'; c = xchar()) x = x * 10 + c
                                                                                                                                                                                                                                                                                                                                                                                                     for (; '0' <= c && c <= '9'; c = xchar()) x = x * 10 + c
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         else {
   if (wb == 32) len = 31 - __builtin_clz(n - 1) + wb;
   else len = 63 - __builtin_clzll(n - 1) + wb;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (wpos == S) fwrite(wbuf, 1, S, stdout), wpos = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         while (x \mid | \mid | \mid n) s[n++] = \mid 0 \mid + \times \% \ 10, \ \times / = 10;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  while (c <= 32) c = xchar();
for (; c > 32; c = xchar()) *s++ = c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               x = ((T2(1) << len) + n - 1) / n;
                                                                                                                                                                                                                          if (c == '-') s = -1, c = xchar();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                const static int wb = sizeof(T1) * 8;
                                                                                                 int c = xchar(), x = 0, s = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (x < 0) wchar('-'), x = -x;
                                                                                                                                                                                                                                                                                                                                                                               while (c <= 32) c = xchar();
if (pos == len) return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   inline void xstring(char *s) {
                                                                                                                        while (c <= 32) {
   if(!~c) return ed = 1;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (n == 1) \times = 1, len = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   while (n—) wchar(s[n]);
                                                                                                                                                                                                                                                                                                                                                        int c = xchar(), x = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     inline void wchar(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             template<class T1, class T2>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      inline void wint(int x)
                         return buf[pos++];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       wbuf[wpos++] = x;
                                                                                                                                                                                                                                                                                                                             inline int xuint() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int c = xchar();
                                                                                                                                                                               c = xchar();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        FastD(T1 n): m(n) {
                                                                      inline int xint()
                                                                                                                                                                                                                                                                              return × * s;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int len; T1 m, x;
FastD() = default;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       char s[24];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       8.5 FastMod
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int n = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                  return x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ,s = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     struct FastD {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         while(sz(ch) && pri(ch.back()) >= pri(c)) rpn.pb(ch.back()), ch.pop_back();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                   char c = s[i];
if(c == '(') { ch.pb(c);
} else if(c == ')') {
while(ch.back() != '(') rpn.pb(ch.back()), ch.pop_back();
                                            for (int i = b._Find_first(); i < sz(b); i = b._Find_next(i));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            static int len = \theta, pos = \theta;

if (pos == len) pos = \theta, len = fread(buf, 1, S, stdin);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            reverse(all(ch));    rpn.insert(rpn.end(), all(ch));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        sta[sz(sta) - 1] = calc(u, sta.back(), b);
} else { sta.pb(u); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                char b = sta.back(); sta.pop_back();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FastIO() : wpos(0), ed(0) { }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 static const int S = 1310720
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      else if(pri(c) > 0) {
                                                                                                       ExpressionParse
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   static char buf[S];
                                                                                                                                                                                                                                                                                                                                                                                                                      rpn.clear(); ch.clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          } else { rpn.pb(c); }
                                                                                                                                                                                                                                                                    if(ch == '(') return 0;
                                                                                                                                                                                          vector<char> rpn, ch, sta;
// 定义运算符优先级
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // read untill EOF (xint)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       inline int xchar() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, sz(rpn)) {
                                                                                                                                                                                                                                                                                                                                                                    char solve(string s) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                char u = rpn[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 0, sz(s)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ch.pop_back()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(pri(u) > 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // 后缀表达式计算
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ch.pb(c);
                         // travel all 1
                                                                                                                                                                                                                                           int pri(char ch) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 char wbuf[S];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return sta[0];
                                                                                                                                                               // 二元运算左结合
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    FastIO
                                                                                                                                                                                                                                                                                                                                                                                             // 中缀转后缀
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 sta.clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       struct FastIO {
                                                                                                                                                                                                                                                                                                                       return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int wpos;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         boo1 ed;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     8.4
                                                                                                       8.3
```

```
for(char* p=strtok(s," .,()");p;p=strtok(NULL," .,()")) a.pb(p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(i, 0, 30) if (d >= rom[i]) d -= rom[i], r += smb[i];
                                                                                                                                                             3000, 2000, 1000, 900, 800, 700, 600, 500, 400, 300, 200, 100,
||db rnd(db 1, db r) { RR dis(1, r); return dis(gen); }
                                                                                                                                                                                                                                                                                 string smb[30]={
    "MMM", "MM",
    "CM", "DCC", "DC", "D", "CD", "CCC", "CC", "C",
    "XC", "LXXX", "LXX", "LX", "L", "XL", "XXX", "XXX", "XX",
    "IX", "VIII", "VII", "VII", "VII", "III", "III", "II", "II
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void add(int &a) { sta[++top] = mp(&a, a); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              char s[111]; gets(s); vector<string> a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         clock_t st = clock(); CLOCKS_PER_SEC;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       pair<int*, int> sta[N * 5]; int top;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if diff sol.out dp.out; then
                                                               RomanNumerals
                                                                                                                                                                                            90, 80, 70, 60, 50, 40, 30, 20, 10,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 回溯时还原标记
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ./sol <gen.in >sol.out
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ./dp <gen.in >dp.out
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         string toRoman(11 d) {
                                                                                                                                 const int rom[30] = {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       printf "AC\n"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      printf "Wa\n"
                                                                                                                                                                                                                        9,8,7,6,5,4,3,2,1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ./gen > gen.in
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int ttop = top;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      duipai
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void dfs(int u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Time
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Strtok
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // sh duipai.sh
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     while true; do
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  exit 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          string r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        #!/bin/bash
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         8.10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      8.11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Ę
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     8.12
                                                               \infty\infty
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            8.9
friend T1 operator / (const T1 &n, const FastD &d) { return T2(n) * d.x >> d.len; } friend T1 operator % (const T1 &n, const FastD &d) { return n-n/d*d.m; }
                                                                                                                                                                                                                                                                                                                                                                      friend T operator / (const T &n, const ExactD &d) { return n * d.i; }
                                                                                                                                                                                                                                                                                                        return !e ? \times : mul_inv(n, e - 1, \times * (2 - \times * n));
                                                                                                                                                                                                                                                                            constexpr static T mul_inv(T n, int e = 6, T x = 1) {
                                                                                                                                                                                                                                                                                                                                                                                                    bool divide(const T &n) const { return n * i <= t; }</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 11 rnd(11 1, 11 r) { RR dis(1, r); return dis(gen); }
typedef uniform_real_distribution
                                                                                                                                                                                                                                                ExactD(const T &n): t(T(-1) / n), i(mul_inv(n)) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Map<String, Integer> mymap2 = new TreeMap<>();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Map<String, Integer> mymap = new HashMap<>();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     List<String> mylist2 = new LinkedList<>();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      List<String> mylist1 = new ArrayList⇔(),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            Queue<String> que = new LinkedList<>();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   List<String> mylist3 = new Vector<>();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        public static void main(String[] args) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Set<String> myset2 = new TreeSet<>(),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Vector<String> vec = new Vector<>();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Set<String> myset = new HashSet\Leftrightarrow();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Scanner cin=new Scanner(System.in);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        using FastDiv64 = FastD<uint64, uint128>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          Stack<String> sta = new Stack<>();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     BigInteger a=cin.nextBigInteger();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  BigInteger b=cin.nextBigInteger();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  typedef uniform_int_distribution<ll> RR;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              using FastDiv32 = FastD<uint32, uint64>;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                System.out.println(a.add(b));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ExactDiv32 = ExactDcuint32>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ExactDiv64 = ExactDcuint64>
                                                                                                                        template<class T> // 只能用于奇数
                                                                                                                                                                                                                    ExactD() = default;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           a=cin.nextInt();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      mt19937 gen(998244353)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          b=cin.nextInt();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               import java.util.*;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           import java.math.*,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         public class code
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Integer a,b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  import java.io.*,
                                                                                                                                                         struct ExactD {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Rand
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Java
```

8.7

using [using

8.6

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 \begin{array}{lll} & \text{for(int } i = 1, i < = n, ++i) & \text{rk}[sa[i]] & = i, \\ & \text{for(int } i = 0, i < n, h[rk[i++]] & = k) & \text{for}(k\& -k, j = sa[rk[i] - 1], s[i+k] == s[j+k], ++k), \\ \end{array} 
bool cmp(int *x,int a,int b,int d){ return x[a] == x[b] && x[a+d] == x[b+d]; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        \textbf{for}(\texttt{int} \ \texttt{i=1}, \texttt{i<=1im}, \texttt{++i}) \ \texttt{p[j][i]} = \min(\texttt{p[j-1][i]} \ , \ \texttt{p[j-1][i+(1<<j>1)]});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   log[0] = -1; for(int i=1; i <= n; ++i) log[i] = log[i-1] + (i==(i&(-i)));
                                                                                                                                                                                                                                                                           swap(x , y); p = 1; x[sa[0]] = 0; \\ rep(1,1,n) x[sa[i]] = cmp(y, sa[i], sa[i-1], j)?p-1:p++; \\
                                                                                                                                                                                    \begin{array}{ll} p = 0; rep(i,n-j,n) \ y[p++] = i; \\ rep(i,0,n) \ if(sa[i] >= j) \ y[p++] = sa[i] - j; \end{array}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for(int i=1;i<=n;++i) p[0][i] = Doubling::h[i];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int p[18][N] , rk[N] , in[N] , Log[N] , n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return min(p[t][a] , p[t][b-(1<<t)+1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void exkmp(char *s,int *z,char *t,int *p){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // rank[0~n-1]: 以 i 开头的后缀排名 rank[i]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              struct DA\{ // [\theta, n], in[n] = \theta, n \ load static const int N = 101010;
                                                                                         rep(i,0,n) \times [i] = s[i], y[i] = i;
                                                                                                                       sort(x , y , n , m);
for(int j=1, p=1; p<n; m=p, j<<=1){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                void cal_h(int *s,int n,int *rk){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       * S 串的每个后缀与 t 串的最长公共前缀
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              a = rk[a] , b = rk[b];
if(a > b) swap(a , b);++a;
                            void da(int *s,int n,int m){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Doubling: :da(in, n+1, 300);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Doubling::cal_h(in,n,rk);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for(int j=1;1<<j<=n;++j){
                                                                                                                                                                                                                                                 sort(x , y , n , m);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int lim = n+1-(1 << j)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // 某两个后缀的最长公共前缀
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int t = Log[b-a+1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int lens = strlen(s);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int lent = strlen(t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int lcp(int a,int b){
                                                               int *x=wa, *y=wb;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            a w
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       void Build(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            Exkmp
                                                                                                                                                                                                                                                                                                                                                                                                                                   int j, k=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             В
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            п
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             q
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        * t: a
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    * ns: 3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       * nt: 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            9.3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int ne[N][M] , fail[N] , fa[N] , rt , L;
void ini(){ fill_n(ne[fail[0] = N-1],M,0);L = 0;rt = newnode();}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       v.pb(ne[c][i]) , fail[ne[c][i]] = ne[fail[c]][i]
ne[c][i] = ne[fail[c]][i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(!ne[p][c]) ne[p][c] = newnode() , fa[L-1] = p;
p = ne[p][c];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // h[1~n]:S[sa[i-1]] 与 S[sa[i]] 的最长公共前缀长度为 h[i]
                                                                                                                       while(top > ttop) *sta[top].fi = sta[top].se, —top;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int newnode(){ fill_n(ne[L],M,0); return L++; }
void add(char *s){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int t[N] , wa[N] , wb[N] , sa[N] , h[N];
void sort(int *x,int *y,int n,int m){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // sa[0~n]: 排名第的后缀是以i sa[i] 开头
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             * addition: end[] end[c] |= end[fail[c]]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         per(i, 0, n) sa[-t[x[y[i]]]] = y[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         static const int N = 101010, M = 26;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int c = s[i] - 'a'; // modify
                                                                                                                                                                                                                                                                                                                                                                                                                     ^* [0,L) , N-1 is virtual , 0 is rt
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i,0,M) ne[c][i] ?
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i,1,m) t[i] += t[i-1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            static const int N = 101010;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for(int i=0;s[i];++i){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i,0,n) t[x[y[i]]]++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     DoublingArray
                                                                                                                                                                                                                                                                                                            ACAutomaton
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(i, 0, m) t[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int c = v[i];
add(var); modify var;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i,0,sz(v)){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         vi v;v.pb(rt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int p = rt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              namespace Doubling{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void Build(){
                                                                                                                                                                                                                                 String
                                                            // .. dfs
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        struct Trie{
                                                                                                                                                                                                                                                                                                                                                                                                                                               * init!!
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     9.2
```

```
int p = i >> 1, q = i - p, r = ((j + 1) >> 1) + pa[j] - 1; pa[i] = r < q ? 0 : min(r - q + 1 , pa[(j << 1) - i]); while(0 <= p - pa[i] && q + pa[i] < n && s[p - pa[i]] == s[q + pa[i]]) pa[i]++; if(q + pa[i] - 1 > r) j = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    * i: [0, n) pa[i<1]: odd string 整个回文长度为 2*pa[i<1]-1
* i: [0, n - 1) pa[i<1|1]: even string 整个回文长度为 2*pa[i<1]
                                                                                                                                                                                                                                                                                                                                            // 生成字符集为 m , 长度不超过 n 的所有 lyndon word , 字符集从 a 开始
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for (int j = x; j < n; ++j) s[j] = s[j - x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (strlen(s)==1 && s[0]=='a'+m-1) return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void Manacher(char *s,int n,int *pa){
                                                                                                                                                                                                                                                                                                                                                                  void lyndon_generate(int n, int m) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for(int i=1, j=0; i<(n<<1)-1;++i){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            \widehat{\check{}}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 * length of pa is two size of str
                                                                                                                                                                                                                                                                                                                                                                                       char z = 'a' + m - 1, s[1000];
s[0] = 'a' - 1;
for (int i = 1, x = 1; ; ++i) {
                        while (start + temp <= i){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for (x = n; s[x - 1] == z;
                                                              ret.push_back(start);
    int temp = mid - start;
                                                                                                                                                                                                                                                                                                                                                                                                                                                     S[x - 1] ++; S[x] = 0;
                                             start += temp;
                                                                                                            i = cur = start;
                                                                                                                               mid = start + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Manacher
                                                                                                                                                                                               return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            puts(s);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 * N>2*n
                                                                                                                                                                                                                                                                                0126
                                                                                                                                                                                                                                                            cbaabc
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 9.6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    aab
ab
abb
b
                                            while(j >= 0 && s[i] != t[j + 1]) j = nt[j];
if(s[i] == t[j + 1]) ++j;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // O(n) 分解为字典序非严格降的 1yndon word 分解唯
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int n = strlen(s) + 1; // zero used here int start = 0, mid = 1, cur = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void kmp(char *s,int *ns,char *t,int *nt){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(j + 1 == lent) j = nt[j];
                      for(int i=0, x=0, y=0; i<lens; ++i){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (++cur == mid) cur = start;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for(int i=0, j=-1;i<lens;++i){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        for (int i = 0; i < n; ++i){
  if (s[i] == s[cur]){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      else if (s[i] > s[cur]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      else if (s[i] < s[cur]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 vector<int> duval(char s[]){
                                                                                                                                                                                                                 exkmp(t+1,nt+1,t,nt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int lens = strlen(s);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int lent = strlen(t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            LyndonWord
                                                                                                                                                                                                                                                                                                                                                                                                                             s a
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   kmp(t+1,nt+1,t,nt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       void KMP(){
    scanf("%s%s", s, t);
                                                                                                                                                                                              scanf("%s%s", s, t);
                                                                                                                                                                                                                                        exkmp(s,ns,t,nt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ret.push_back(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          kmp(s,ns,t,nt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ns[i] = j;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             mid = i + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           vector<int> ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  cur = start;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    nt[0] = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                             S
                                                                                                                                                                                                                                                                                                        Kmp
                                                                                                                                                                        void Exkmp(){
                                                                                                                                                                                                                                                                                                                                                                                     a o
                                                                                                                                                                                                                                                                                                                                                                                                                             а
p[0]=0;
                                                                                                                                                                                                                                                                                                                                                                                                      nt:-1 -1
                                                                                                                                                                                                                                                                                                                                                                                                                                             ns: 0
*/
                                                                                                                                                                                                                                                                                                                                                                                    В
                                                                                                                                                                                                                                                                                                                                                                                                                             æ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          9.5
                                                                                                                                                                                                                                                                                                          9.4
```

$9.7 ext{PAM}$

```
0, cs) cnt[fail[i]][j] += cnt[i][j]; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int sa[N], rk[N], ht[N], s[N << 1], t[N << 1], p[N], cnt[N], cur[N];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 #define inducedSort(v) std::fill_n(sa, n, -1); std::fill_n(cnt, m, 0);
                                                                                                                                                                                                                                                                                           p) rep(j,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for (int i = 0; i < n; i++) cnt[s[i]]++;
last = ne[cur][c], cnt[last][cs]++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    #define pushS(x) sa[cur[s[x]]—] = x #define pushL(x) sa[cur[s[x]]++] = x
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 const static int N = 100000 + 10;
                                                                                                                                                                                                                                                                                           o`
                                                                                                                                                                                      for(all char) add(char);
                                  id[n] = last, no[last] = n;
                                                                                                                                                                                                                                                                                      inline void build() { per(i,
                                                                                                                                                             ++cs; add(-cs-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      * time complexity: O(n)
                                                                                                                        for(all string)
                                                                                           inline void ins()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      namespace SA {
                                                                                                                                                                                                                                                                                                                                                                                   SAIS
                                                                                                                                                                                                                                                                                                                                                                                   9.9
                                                                                                                                                                                                     return p++; } inlin() { newnode(p = 0), newnode(s[0] = -1), fail[last = n = 0] = 1; }
                                                                                                                             int s[N], len[N], ne[N][M], fail[N], cnt[N], dep[N], id[N], no[N], last, n, p;
inline int newnode(int l) { fill_n(ne[p], M, 0); cnt[p] = dep[p] = 0; len[p] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    inline void build() { per(i, 0, p) cnt[fail[i]] += cnt[i]; }
                                                                                                                                                                                                                                                                                                while(s[n - len[x] - 1] != s[n]) x = fail[x];
                                       // [0,p) , \theta(even) and 1(odd) is virtual , init!!
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      fail[now] = ne[getfail(fail[cur])][c];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int now = newnode(len[cur] + 2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ne[cur][c] = now;
dep[now] = dep[fail[now]] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    last = ne[cur][c], cnt[last]++;
id[n] = last, no[last] = n;
                                                                                                  static const int N = ::N, M = 26;
                                                                                                                                                                                                                                                                                                                                                                                                                                                      int cur = getfail(last);
                                                                                                                                                                                                                                                                     inline int getfail(int \times)
                                                                                                                                                                                                                                                                                                                                                                                           inline void add(int c) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(!ne[cur][c]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                s[++n] = c;
                                                                                                                                                                                                                                                                                                                                  return x;
                                                                       struct PAM
```

9.8 PAM $_$ multi

```
П
                                                           cs;
                                                                                                                                                                                                                                                          inline void init() { newnode(p = 0), newnode(s[0] = -1), fail[last = n = 0] = 1; cs
                                                  int s[N], len[N], ne[N][M], fail[N], cnt[N][K], dep[N], id[N], no[N], last, n, p,
                                                                                                                                                                                                                                                                                                                                            while(s[n - len[x] - 1] != s[n]) x = fail[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(c < 0) \{ s[++n] = c; last = 1; return; \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      fail[now] = ne[getfail(fail[cur])][c];
                          const int K = 11, N = ::N * K, M = 26;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int now = newnode(len[cur] + 2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                dep[now] = dep[fail[now]] + 1;
                                                                                                                                                                                                                                                                                                               inline int getfail(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int cur = getfail(last);
                                                                                                                                                                        dep[p] = 0; len[p] = 1;
                                                                                      inline int newnode(int 1)
                                                                                                                                                                                                                                                                                                                                                                                                                              inline void add(int c) {
                                                                                                                                         fill_n(cnt[p], K, 0);
                                                                                                            fill_n(ne[p], M, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ne[cur][c] = now;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(!ne[cur][c]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         s[++n] = c;
                                                                                                                                                                                                     return p++;
                                                                                                                                                                                                                                                                                                                                                                             return x;
struct PAM {
```

```
for (int i = n - 2; -i; i - i) t[i] = s[i] = s[i + 1]; t[i + 1] : s[i] > s[i + 1]; for (int i = 1; i < n; i + i) rk[i] = t[i - 1] && !t[i]? (p[n1] = i, n1 + i) : -1;
* Ensure that str[n] is the unique lexicographically smallest character in str.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for (int i = 0, i < n, i++) if (sa[i] > 0 && t[sa[i]-1]) pushL(sa[i]-1); \
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for (int i = n-1; -i; i-) if (sa[i] > 0 && !t[sa[i]-1]) pushS(sa[i]-1) void sais(int n, int m, int *s, int *p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (ch < 1 || p[x + 1] - p[x] != p[y + 1] - p[y]) ch++;
else for (int j = p[x], k = p[y]; j <= p[x + 1]; j++, k++)
if ((s[j] << 1 | t[j]) != (s[k] << 1 | t[k])) { ch++; break; }</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for (int i = 0, x, y; i < n; i++) if (\sim(x = rk[sa[i]]))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (ch + 1 < n1) sais(n1, ch + 1, s1, t + n, p + n1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int n1 = t[n-1] = 0, ch = rk[0] = -1, *s1 = s + n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          else for (int i = 0; i < n1; i++) sa[s1[i]] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (int i = 0; i < n; i++) rk[str[i]] = 1; for (int i = 0; i < m; i++) rk[i+1] := rk[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for (int i = 0; i < n1; i++) s1[i] = p[sa[i]];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for (int i = 1; i < m; i++) cnt[i] += cnt[i-1];
for (int i = 0; i < m; i++) cur[i] = cnt[i]-1;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int i = 0; i < m; i++) cur[i] = cnt[i]-1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for (int i = 1; i < m; i++) cur[i] = cnt[i-1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for (int i = n1-1; \sim i; i...) pushS(v[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int mapCharToInt(int n, const T *str) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int m = *max_element(str, str + n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           std::fill_n(rk, m + 1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 template<typename T>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  inducedSort(s1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           -uducedSort(p);
```

```
O(nlogn)
                                                                                                                                                                                                                 // trie 树点带字母,每个点到根的字符串排序,
// C 为字符集大小, 从 a 开始, M 为倍增深度
                                                     rep(i, 1, L + 1) cnt[i] += cnt[i - 1];
                                                                                rep(i, 1, L + 1) cur[cnt[1[i]]—] = i;
                                                                                                                                                                                                                                                                                                          const int N = 5e5, M = 21, C = 26;
                          rep(i, 1, L + 1) ++cnt[l[i]];
                                                                                                                                                                                                                                                                      // 调用 Init 之后, 取 sa[]
                                                                                                                                                                                                                                                                                                                                  int n, fa[N]; char s[N];
                                                                                                                                                SA trie
// BucketSort
                                                                                                                                                                                                                                                                                                                                                                  struct SA {
                                                                                                                                                                                                                                                                                      while (i + h < n \& i + h < n \& s[i + h] == s[j + h]) h++;
for (int i = 0; i < n; i++) s[i] = rk[str[i]] - 1;</pre>
                                                                                                                                                                    sais(n, m, s, t, p); for (int i = 0; i < n; i++) rK[sa[i]] = i; for (int i = 0, h = ht[0] = 0; i < n - 1; i++) {
                                                                                                             void suffixArray(int n, const T *str)
                                                                                                                                       int m = mapCharToInt(++n, str);
                                                                                                                                                                                                                                                                                                                 if (ht[rk[i]] = h) h—;
                                                                                                                                                                                                                                                       int j = sa[rk[i] - 1];
                                                                                  template<typename
                            return rk[m];
```

$9.10 \quad SAM$

```
if(ne[p][c] \& l[ne[p][c]] == l[p] + 1) { last = ne[p][c]; return; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       while(p && ne[p][c] == q) ne[p][c] = nq, p = par[p];
                                                                                                                                                                                                                                                                                                                                                                         while(p && !ne[p][c]) ne[p][c] = np, p = par[p];
                                                                                                                         int par[N], 1[N], ne[N][M], rt, last, L;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     l[nq] = l[p] + 1;
copy(ne[q], ne[q] + M, ne[nq]);
* [0,L] , 0 is virtual , 1 is rt , init!!
                                                                                              static const int N = ::N << 1, M = 26;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(1[q] == 1[p] + 1) par[np] =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                par[q] = par[np] = nq;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       fill(ne[rt], ne[rt] + M, 0);
                                                                                                                                                                                                                                                                                                  fill(ne[np], ne[np] + M, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     par[nq] = par[q];
                                                                                                                                                                                                                                                                                                                                                                                                                                                      int q = ne[p][c];
                                                                                                                                                                                                                                                                                                                                                                                                    if(!p) par[np] = rt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int nq = ++L;
                     * [1[par[s]] + 1, 1[s]]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rt = last = L = 1;
                                                                                                                                                                                                                                                                                                                           l[np] = l[p] + 1;
                                                                                                                                                void add(int c) {
                                                                                                                                                                                                                                                                         int np = ++L;
                                                                                                                                                                           int p = last;
                                                                                                                                                                                                                                                                                                                                                      last = np;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  1[0] = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void ini() {
                                                                     struct SAM {
                                                                                                                                                                                                  /* ex
```

```
(tmp[sa[i]] == tmp[sa[i-1]] \& tmp[pa[sa[i]][p]] == tmp[pa[sa[i-1]][p]])
int R[N], RF[N], tmp[N], pos[N], tax[N], tp[N], sa[N], siz, n, pa[N][M];
                                                                                                                                                                                                                                                                                                                                                                                           n = _n, pa[1][0] = 0; rep(i, 2, n + 1) pa[i][0] = fa[i];
rep(i, 2, n + 1) rep(j, 1, M) pa[i][j] = pa[pa[i][j - 1]][j - 1];
rep(i, 1, n + 1) R[i] = h(s[i]), tp[i] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Qsort(sa, R, tp, C); rep(i, 1, n + 1) pos[sa[i]] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Qsort(sa, R, tp, R[sa[n]]);
rep(i, 1, n + 1) tmp[i] = R[i]; R[sa[1]] = 1;
rep(i, 2, n + 1) R[sa[i]] =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           For (int W = 1, p = 0; W < n; W <<= 1, p++) {
                                                                                                                                                                                                                  ser(i, 1, n + 1) sa[tax[R[tp[i]]] - ] = tp[i];
                                    int h(int c) { return c - 'a' + 1; }
void Qsort(int *sa, int *R, int *tp, int siz)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(i, 1, n + 1) RF[i] = pos[pa[i][p]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        R[sa[i-1]] : R[sa[i-1]] + 1;
                                                                                                                                                                                 rep(i, 1, siz + 1) tax[i] += tax[i - 1];
                                                                                                                                                                                                                                                                                                                                                             void Init(int _n, int fa[], char s[]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 1, n + 1) pos[sa[i]] = i;
                                                                                                                                             rep(i, 1, n + 1) tax[R[tp[i]]]++;
                                                                                                         rep(i, 0, siz + 1) tax[i] = 0;
                                                                                                                                                                                                                                                                                                                           // fa[] 表示树上父节点编号, 根为 1
                                                                                                                                                                                                                                                                                    // s[] 表示字母点权,下标从 1 开始
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Qsort(tp, RF, sa, n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              StrHash
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                9.12
```

```
const int P = 169 + 7, N = 101010;
struct Str {
   int B[N], h[N], ba;
   Str(int ba) : ba(ba) { B[0] = 1; rep(i, 1, N) B[i] = mul(B[i - 1], ba); }
   int upd(int a, int b) {
      if(a += b) >= P) a -= P;
      return a < 0 ? a + P : a;
   }
   int mul(int a, int b) { return 111 * a * b % P; }
   void init(vi &s) {</pre>
```

```
f[x][y]=(f[x][y]+Dfs(nxt1[x][i],nxt2[y][i]))&mod;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // 求一个 A , B 的最长公共子序列 S , 使得 C 是 S 的子序列
                                                                                                                                                                                                                                                                                                                                                                                                                                                               LL Dfs(LL x,LL y){
   if(f[x][y]) return f[x][y];
   for(LL i=1;i<=a;++i) if(nxt1[x][i]&&nxt2[y][i]){</pre>
                                                                                                                                                                                                                                                                                                            for(LL i=1;i<=a;++i) if(nxt1[x][i]&&nxt2[y][i])</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(nxt1[x][i]+nxt2[y][i]>n+1) continue;
if(nxt1[x][i]+nxt2[y][i]<n+1) f[x][y]++;</pre>
                                                                                            for(LL i=n,i>=1;—i){
  for(LL j=1;j<=a;++j) nxt[i-1][j]=nxt[i][j];</pre>
                                                                                                                                                                                                                                                                                                                                      f[x][y]+=Dfs(nxt1[x][i],nxt2[y][i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(s[i+k]>s[j+k])i=max(i+k+1,j+1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           while(S[i+k]==S[j+k] && k<L)++k
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i,0,L) s[L+i]=s[i]; s[2*L]=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for(LL j=1;j<=a;++j) nxt[i][j]=i
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for(LL i=1;i<=a;++i) nxt[n][i]=n,</pre>
                                                                                                                                                                                                                                                                                if(f[x][y]) return f[x][y];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(k==L)return min(i,j);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   else j=max(j+k+1, i+1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int MINR(char s[],int L){
  * include empty string
                                                                                                                                                                                                                // 求两串的公共子序列个数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      nxt[i][c[i+1]]=i+1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       最小表示法
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             while(i<L && j<L){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return ++f[x][y];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for(LL i=0;i<n;++i){</pre>
                                                                                                                                                       nxt[i-1][s[i]]=i;
                                                                                                                                                                                                                                                                                                                                                                            return ++f[x][y];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   / 最大改成 <
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return min(i,j);
                                                                                                                                                                                                                                               LL Dfs(LL x, LL y){
                                                                                                                                                                                                                                                                                                                                                                                                                                   // 求回文子序列个数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // s[] 开两倍长度
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int i=0, j=1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // 下标从 0 开始
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int k=0;
                                                             // 构建
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            9.15
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        inline Str operator - (const Str &c) const \{ return Str(a-c.a\ ^*\ B[len-c.len],\ len
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             inline Int operator + (const Int &c) const { return Int(upd(a, c.a), upd(b, c.b)); } inline Int operator - (const Int &c) const { return Int(upd(a, -c.a), upd(b, -c.b));}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     inline Int operator * (const Int &c) const { return Int(mul(a, c.a), mul(b, c.b)); } inline bool operator == (const Int &c) const {return a == c.a \&\& b == c.b;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Str(int x) {a = Int(x, x); len = 1;} inline Str operator + (const Str &c) const { return Str(a * B[c.len] + c.a, len + c.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   inline bool operator == (const Str &c) const { return a == c.a && len == c.len;}
h[0] = s[0] + 1; rep(i, 1, sz(s)) h[i] = upd(mul(h[i - 1], ba), s[i] + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void init(vi &s, Str *ha) {
    rep(i, 0, sz(s)) ha[i] = i > 0 ? ha[i-1] + Str(s[i] + 1) : Str(s[0] + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     inline int mul(int a, int b) {return 111 * a * b % P; }
                                                                                                                      return upd(h[r], \negmul(h[l - 1], B[r - l + 1]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Str(Int a = _0, int len = 0) : a(a), len(len) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            Int(int a = 0, int b = 0) : a(a), b(b) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return 1 > 0? ha[r] - ha[1-1] : ha[r];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         B[0] = 1; B[1] = Int(233, 241);

rep(i, 2, n+1) B[i] = B[i-1] * B[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   0 = Int(), 1 = Int(1, 1), B[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Str sub(Str *ha, int 1, int r) {
                                                                                                                                                                                                                                                                                                                                                            inline int upd(int a, int b) {
                                                                                                                                                                                                                                                      StrHash 双哈希
                                                                                                                                                                                                                                                                                                                                                                                        if((a += b) >= P) a -= P;
                                                                                                                                                                                                                                                                                                                                                                                                                         return a < 0 ? a + P : a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (1 > r) return Str();
                                                             int sub(int 1, int r) {
                                                                                            if(!1) return h[r];
                                                                                                                                                                                                                                                                                                                                  const int P = 1e9 + 7;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   序列自动机
                                                                                                                                                                                      }ha1(233), ha2(241);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Int a; int len;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void init(int n){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // 减去一个前缀
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     } ha[N], hb[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int a, b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      struct Int{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          struct Str{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  len); \ \}
                                                                                                                                                                                                                                                      9.13
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       9.14
```

10.1 DsuOnTree

* a is char size * n is string lenth

* 0 is root

 Tree

10

```
10.3
                                                                                                                     for(auto t:g[c]) if(t!=fa) dfs(t,c,g),sz[c]+=sz[t],(sz[t]>=sz[s])&&(s=t);
                                                                                                                                                          solve(1,0,false,g); // 如果输入是单组数据, 改成 true 可以优化常数
                                                                                                                                                                                                                                                                                                                                             // 如果当前子树是轻儿子,删除这棵子树的信息
                                                         int sz[N] , wson[N] , par[N];
void dfs(int c,int fa,vi g[]){
   sz[c]=1;par[c]=fa;int &s=wson[c]=0;
                                        static const int N = ::N;
                                                                                                                                                                                                                                                                                // 将当前节点的信息加入
                     namespace QuerySubtree{
                                                                                                                                                                                                                                                                                                                                                                                                        void solve(vi g[]){
// id starts with 1
                                                                                                                                                                                                                                                                                                                             if(!iswson) {
                                                                                                                                                                                                                                                                                                                                                                                                                                dfs(1,0,g);
```

0.2 HeavyChain

```
int sz[N], wson[N], top[N], dep[N], id[N], _, par[N], who[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(s) \ top[s] = top[c], \ dfs2(s, \ c, \ g); for(auto \ t \ : g[c]) \ if(t \ != fa \& t \ != s) \ dfs2(t, \ c, \ g);
                                                                                                                                                                                                                                 for(auto t : \tilde{g}[\tilde{c}]) if(t != fa) {
                                                                                                                                                                                                                                                                                                                                                                                                        void dfs2(int c, int fa, vi g[]){
                                                                                                                                                                                                              int &s = wson[c] = top[c] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int fa = top[a], fb = top[b];
while(fa != fb){
                                                                                                  void dfs(int c, int fa, vi g[]){
                                                                                                                                                                                                                                                                                              sz[c] += sz[t];
if(sz[t] >= sz[s]) s = t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(!top[c]) iop[c] = c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void Query(int a, int b){
                                                  static const int N = ::N;
                                                                                                                                                        par[c] = fa;
dep[c] = dep[fa] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int s = wson[c];
                                                                                                                                                                                                                                                                  dfs(t, c, g);
// id starts with 1
                    struct HeavyChain{
                                                                                                                                                                                                                                                                                                                                                                                                                                 id[c] = ++_{-};
                                                                                                                                                                                                                                                                                                                                                                                                                                                            who[\_] = c;
                                                                                                                                 SZ[c] = 1;
```

```
if(dep[fa] < dep[fb]) swap(a, b), swap(fa, fb);
    // cal id[fa] .. id[a]
    a = par[fa]; fa = top[a];
    if(dep[a] < dep[b]) swap(a, b);
    // cal id[b] .. id[a]
    // b is lca
    soid Build(vi g[]){
        dfs(1, 0, g);
        -=0;
        dfs2(1, 0, g);
}
</pre>
```

D.3 LCARMQ

```
rep(j,0,lim) a[i][j] = rmin(a[i-1][j] , a[i-1][j+(1<<i>>1)]);
                                                                                                                                                                                                                                                                 for(auto t : g[c]) if(t!=fa) dep[t]=dep[c]+1,dfs(t,c,g),add(c);
                                                                                         int a[20][N] , lft[N] , dep[N] , lg[N] , L;
int rmin(int x,int y){return dep[x] < dep[y] ? x : y;}</pre>
\ensuremath{\text{//}} N is 2 size of tree , id of nodes start from
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return rmin(a[i][x] , a[i][y+1-(1<<i)]);</pre>
                                                                                                                                                                void add(int x){ a[0][L++] = x;}
void dfs(int c,int fa,const vi g[]){
                                                             static const int N = 101010 << 1;
                                                                                                                                                                                                                                                                                                                                                                L = 0; dfs(1,0,g); dep[0] = -1;

rep(i,2,L) lg[i]=lg[i>>1]+1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int \lim = L+1-(1 < i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      x = lft[x], y = lft[y];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(x > y) swap(x , y);

int i = lg[y-x+1];
                                                                                                                                                                                                                                                                                                                            void Build(const vi g[]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int lca(int x, int y){
                                                                                                                                                                                                                                lft[c]=L;add(c);
                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(i, 1, 20){
                                   struct LCARMQ{
```

10.4 LongChain

```
struct LongChain{
    static const int N = ::N;
    int wson[N] , top[N] , dep[N] , lg[N];
    int jump[N][20] , id[N] , who[N] , rwho[N] , _;
    void dfs(int c, int fa, vi g[]){
        dep[c]=1;int &s=wson[c]=top[c]=0;
        jump[c][0]=fa;rep(i,1,20) jump[c][i]=jump[jump[c][i-1]][i-1];
    for(auto t:g[c]) if(t!=fa)
        dfs(t,c,g),dep[c]=max(dep[t]+1,dep[c]), (dep[t]>=dep[s])&&(s=t);
```

if(nd.lca) upd(st[nd.lca], 1); while(r > nd.r) upd(r--, -1);
while(1 < nd.l) upd(l++, -1);</pre>

while(r < nd.r) upd(++r, 1);
while(1 > nd.l) upd(—1, 1);

For(auto &nd : nds) {

int l = 1, r = 0;

sort(all(nds));

// adde(u, v)

```
for(int i = 1; i < M && pre[u][i - 1]; ++i) pre[u][i] = pre[pre[u][i - 1]][i - 1];
                                struct Node {
   int l, r, id, lca;
   Node(int id, int l, int r, int lca = 0) : id(id), l(l), r(r), lca(lca) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int lca(int x, int y) {
   if(dep[x] > dep[y]) swap(x, y);
   per(i, 0, M) if(dep[pre[y][i]] >= dep[x]) y = pre[y][i];
   per(i, 0, M) if(pre[x][i] != pre[y][i]) x = pre[x][i], y = pre[y][i];
int dep[N], pre[N][M], st[N], ed[N], dfn[N << 1], B[N << 1], cnt[N];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for(auto v : g[u]) if(v != fa) dfs(v, u, g);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(f == u) \{ nds.pb(Node(id, st[u], st[v]));
                                                                                                                           bool operator < (const Node &c) const {
   if(B[1] != B[c.1]) return B[1] < B[c.1];
   return (r < c.r) ^ (B[1] & 1);</pre>
                                                                                                                                                                                                                                                                                                                      void dfs(int u, int fa, vi g[]) {
  dep[u] = dep[fa] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void adde(int u, int v, int id) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(st[u] > st[v]) swap(u, v);
int f = lca(u, v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       nds.pb(Node(id, 1, r, f));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int l = ed[u], r = st[v];
                                                                                                                                                                                                                                                                                                                                                                                                                                                    dfn[++cd] = u, st[u] = cd;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               dfn[++cd] = u, ed[u] = cd;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(1 > r) swap(1, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(x == y) return x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // p is index in tree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return pre[x][0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void add(int p) { }
                                                                                                                                                                                                                                                                                                                                                                                    pre[u][0] = fa;
                                                                                                                                                                                                                                                                                         vector<Node> nds;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // 注意统计以 c 为起点的链的答案,注意深度的限制(两棵子树都要注意)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for(auto t : g[c]) if(t != fa && t != wson[c]) {
                                                                                                                                                      if(s) top[s]=top[c],dfs2(s,c,jump[rc][0],g);
for(auto t:g[c]) if(t!=fa&&t!=s) dfs2(t,c,t,g);
                                                                                                                                                                                                                                                                                                                                                                                                             for(auto t : g[c]) if(t != fa) solve(t, c, g);
if(wson[c]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // upd c by wson[c], O(1) or O(\log(n))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    else return rwho[id[top[p0]]+j1—del];
                             void dfs2(int c,int fa,int rc,vi g[]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(del>=j1) return who[id[p0]-j1];
                                                                                                                                                                                                                                                                                                                                                                                       void solve(int c, int fa, vi g[]) {
                                                                                                                                                                                                                                                      void Build(vi g[]){
  dfs(1,0,g);_=0;dfs2(1,0,1,g);
  rep(i,2,N) lg[i]=lg[i>>1]+1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // brute force upd c by t
                                                                                             who[id[c]=++_]=c;rwho[_]=rc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int del=id[p0]—id[top[p0]]
                                                                  if(!top[c]) top[c]=c,rc=c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int kth_par(int x,int k){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int p0=jump[x][lg[k]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // kth par should exist
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(k==0) return ×;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int j0=1<<lg[k];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // c is leaf
                                                                                                                             int s=wson[c];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int j1=k-j0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  } else {
```

* 当 $p \neq a$ 时,我们也要一样统计 [ed[a], st[b]]/[st[b] , ed[a] 的点(从 ed[a] 开始为保 * 我们考虑这个新 dfs 序上 [st[a],st[b]] 的点,我们可以发现 * a—b 上的点被算了一遍,其他点都被算了 2 遍或 0 遍! 那么我们统计的时候注意一下就可以了。 time 排序 a-b 是一段父子链 带修改莫队: 块大小 M(2/3) 按照 1 所在块, r 所在块, * 我们假设要询问一条路径 a-b ,设 lca 为 p=lca(a,b) * 不妨设 st[a]<=st[b] (否则交换一下)。 **const int** N = ::N, SZ = Sqrt(N), M = 17; 当 p = a 时,这应该是一个比较简单的情形。 证 a 不会被排除掉) * 但是这回 Ica 不会被统计到,所以要另外算 int cd; // starts from 1 namespace MoonTree { // 不带修改莫队

(cnt[p] == 1) ? add(p) : sub(p);

 $cnt[p] \leftarrow c;$ p = dfn[p];

void sub(int p) { }
void upd(int p, int c) {

MoOnTree

rep(i, 0, N << 1) B[i] dfs(1, cd = 0, g);

void solve(vi g[]) {

```
fill_n(G + 1, n, vi());
                                          fill_n(par + 1, n, 0);
                                                                                                    点分治
           void init() {
                                                                                                      10.8
             if(nd.lca) upd(st[nd.lca], -1);
// save ans
                                                                                                                                           namespace Vtree{
                                                                                                                           // sort !
                                                                                        10.6
```

```
\label{eq:force_force} \textbf{for}(\texttt{auto} \ \texttt{i} : \texttt{g[c]}) \ \textbf{if}(\texttt{!vis[t]} \& \texttt{k!=fa}) \ \texttt{dfssz(t,c,Sz,rt)} \ , \ \texttt{sz[c]+=sz[t]};
                                                                                                                                                                                                                                                                                                                                         int rt=0;dfssz(c,0,0,rt);dfssz(c,0,sz[c],rt=0);
                                                                                                                                                                                                                                                                                                                                                                                                                                            * 注意计算以 rt 为起点的路径、只包含 rt 的路径
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for(auto t : g[rt]) if(!vis[t]) dfs(t);
                                                                                          bool vis[N]; int sz[N];
void dfssz(int c,int fa,int Sz,int &rt){
                                                                                                                                                                                                                                    if(!rt && sz[c]*2>Sz) rt=c
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    vis[rt] = true;
                                                                  const int N = ::N;
                               namespace Centriod {
// id starts from 1
                                                                                                                                                                                                                                                                                                    void dfs(int c){
                                                                                                                                                                    sz[c] = 1;
```

int u = 1[i], v = 1[i - 1];

// g[n].pb(v);

per(i, 0, _-1) {
 int u = tp[i], v = tp[i + 1];

// g[u].pb(v);

rep(i, 1, cntd + 1) {
// del

 $_{-}$ = cntd = 0; del[++cntd] = tp[_++] = v[0];

int tp[N], _, del[N], cntd, l[N], cntl;
void solve(vi&v,LCARMQ&R){

const int N = ::N << 1;

边分树 10.9

```
if(rt == -1 \mid | max(sz[g.to[rt]], Sz - sz[g.to[rt]]) > max(sz[v], Sz - sz[v]))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for(int i = g.hd[u]; \sim i; i = g.ne[i]) if(!vis[i] && g.to[i] != fa)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void init(int n) { fill_n(vis, n << 1, 0); }</pre>
                                                                                                                                          void dfssz(int u, int fa, int Sz, int &rt) {
                                                                                                     Gra g, T; int L, n, sz[N]; bool vis[N << 1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(sz[u] == n) { T.init(n); }
if(sz[u] == 1) return u;
dfssz(u, 0, sz[u], I = -1);
vis[I] = vis[I ^ 1] = true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int I = 0; dfssz(u, 0, 0,
                                                                                                                                                                                                                                                                                          dfssz(v, u, Sz, rt);
                         namespace ET {
  const int N = ::N << 1;</pre>
                                                                                                                                                                                                                                                     int v = g.to[i];
                                                                                                                                                                                                                                                                                                                               sz[n] += sz[v];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int dfs(int u)
                                                                                                                                                                                  sz[u] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                        rt = i;
// init
                                                                                                                                                                                                                                                                                                                                                                                                   \textbf{for}(\textbf{auto} \ \texttt{t} \ : \ g[\texttt{c}]) \ \textbf{if}(\texttt{!vis}[\texttt{t}] \& \texttt{k}! = \texttt{fa}) \ d\texttt{fssz}(\texttt{t},\texttt{c},\texttt{Sz},\texttt{rt}) \ , \ \texttt{sz}[\texttt{c}] + = \texttt{sz}[\texttt{t}];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int rt=0;dfssz(c,0,0,rt);dfssz(c,0,sz[c],rt=0);
                                                                                                                                                                                                                                                                                       bool vis[N]; int sz[N], par[N]; vi G[N];
void dfssz(int c, int fa, int Sz, int &rt){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for(auto v : g[rt]) if(!vis[v])
int t = dfs(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                          if(!rt && sz[c]*2>Sz) rt=c;
```

const int N = ::N;

sz[c] = 1;

namespace Centriod { // id starts from 1

10.7

G[rt].pb(t);

par[t] = rt;

return rt;

vis[rt] = true;

int dfs(int c){

```
tree[i-1] = Insert(tree[i], 0, mx, a[i], i == n+1?1 : tree[i]->sum, i);
                                                                                                                                                                                                                                                                    for(int i = 1; i <= n; i ++) scanf("%d", &a[i]), mx = max(mx, a[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for(int i = 1; i <= top; i ++) printf("%d ", st[i]);</pre>
                                                                                                                                                                                                                                                                                                                            tree[n+1]->1s = tree[n+1]->rs = tree[n+1];
                                                                                                                                                                                                                                                                                                                                                                                                        if(k > tree[0] \rightarrow sum) return puts("-1"), 0
                                                                                                                                                                                                                                                                                               tree[n+1] = new Segtree(0x0, 0x0, 0, 0);
return Find(p→rs, mid+1, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           0, mx);
                                                                                                                                                                                                                                                                                                                                                     for(int i = n+1; i >= 0; i -
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           now = Find(tree[now],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 st[++ top] = a[now];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(now == n+1)break
                                                                                                        // 求字典序第 k 小的子序列
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               printf("%d\n", top);
                                                                                                                                                                                                                  cin >> n >> k;
                                                                                                                                     Segtree *tree[M];
                                                                                                                                                            int st[M], top;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                while(true){
                                                                                                                                                                                                                                               int mx = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                       int now = 0
                                                                                                                                                                                         int main(){
                                                                                                                                 bool F = 0; int pre = u;
for(int i = 6.hd[u]; ~i; i = 6.ne[i]) if(6.to[i] != fa) {
                                                                             void rebuild(int u, int fa, const Gra &G) {
                                                                                                          if(u == 1) L = n = ::n, g.init(n << 1);
                                                                                                                                                                                                                                                                                                                                                     g.add(pre, G.to[i], G.val[i]);
                                                                                                                                                                                                                                                                      g.add(n, G.to[i], G.val[i]);
                                                                                                                                                                                                                                                                                                                                                                                                        } eİse {
    g.add(u, G.to[i], G.val[i]);
                                                                                                                                                                                                                                         g.add(pre, ++n, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rebuild(G.to[i], u, G);
                                                                                                                                                                                                              if(~G.ne[i]) {
T._add(_, dfs(ed));
                                                                                                                                                                                                                                                                                                   pre = n;
                                                                                                                                                                                                                                                                                                                            } else {
                             return _;
```

return 0;

ZProblems

K 小子序列

11.1

```
Segtree(Segtree *_, Segtree *_, long long __, long long __): ls(_), rs(_), sum(__), pos(__){} friend Segtree* Insert(Segtree *p, int l, int r, long long x, long long val, long
                                                                                                                                                                                                                                                                                                                                                                                                                                            return new Segtree(temp, p->rs, min(temp->sum + p->rs->sum, k+1), 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return new Segtree(p->ls, temp, min(temp->sum + p->ls->sum, k+1), 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Segtree *temp = Insert(p->rs, mid+1, r, x, val, pos);
                                                                                                                                                                                                                                                                                                                                                                                                       Segtree *temp = Insert(p->ls, l, mid, x, val, pos);
                                                                                                                                                                                                                                                                                                                                       if(1 == r)return new Segtree(0x0, 0x0, val, pos);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(k <= p->ls->sum) return Find(p->ls, l, mid);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       friend int Find(Segtree *p, int 1, int r){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(1 == r)return p->pos;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                     int mid = 1 + r >> 1;
                             int n, a[M]; long long k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   k -= p->1s->sum;
                                                                                                                                      long long sum, pos;
                                                            struct Segtree{
   Segtree *ls, *rs;
                                                                                                                                                                                                                                                                                                                                                                          if(x <= mid){</pre>
#define M 1001000
                                                                                                                                                                                                                                                                             long pos){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              else{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   else{
```

SchreierSims

```
66/93
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     bucketsInv[i].pb(inv(p));
lookupTable[i][p[i]] = sz(buckets[i]) - 1;
                                                                                                                                                                                                                                                                                                                                                   int fastFilter(const P&g, bool addToGroup = true) {
                                                                                                                                                                                              operator * (const P&a, const P&b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     buckets[i].push_back(p);
                                                                                                                                                                                                                                                                                                                                                                                                                           int res=lookupTable[i][p[i]];
                                                                                                                                                                                                                                 rep(i,0,sz(a)) r[i]=b[a[i]];
                                                                                                                                                                                                                                                                                                             vector<B> buckets , bucketsInv;
                                                                                                                                      rep(i,0,sz(p)) r[p[i]]=i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(addToGroup) {
                                                                                                                                                                                                                                                                                                                                 vector<vi> lookupTable;
                                                                                                                                                                                                                                                                                                                                                                      int n = sz(buckets);
                                                                              typedef vector<P> B;
                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(res == -1)
                                         namespace SchreierSims
                                                                                                                                                                                                                                                                                                                                                                                                          rep(i,0,n) {
                                                           typedef vi P;
                                                                                                 P inv(P p) {
                                                                                                                                                          return r;
                                                                                                                                                                                                                                                       return r;
                                                                                                                                                                                                                                                                                                                                                                                         P p = g;
                                                                                                                                                                                                                                                                                            int n , m;
                                                                                                                                                                                                                   P r=a;
                                                                                                                      P r=b;
11.2
```

```
inline data operator+(const data&x) { return data(sum + x.sum, min(minv, x.minv), max
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inline data operator+(const data&a, const tag&b) { return a.size ? data(a.sum*b.a + a.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  tag ctag[N], ttag[N];
inline bool isroot(int x, int t) {
   if (t) return !f[x] || !in[f[x]] || !in[x];
   return !f[x] || (son[f[x]][0] != x&&son[f[x]][1] != x) || in[f[x]] || in[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          data(int \ a, int \ b, int \ c, int \ d) \ \{ \ sum = a, minv = b, maxv = c, size = d; \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int f[N], son[N][4], a[N], tot, rt, rub, ru[N], val[N]; bool rev[N], in[N];
                                                                                                                                                                                                                                                                                                                                                                tag(inf x, int y) { a = x, b = y; } inline bool ex() { return a := 1 \mid \mid b; } inline tag operator+(const tag&x) { return tag(a*x.a, b*x.a + x.b); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           size*b.b, atag(a.minv, b), atag(a.maxv, b), a.size) : a; } //son: :\theta-1 if \thetaL\varphi, 2-3 : AAA \thetaAL\varphi
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   data() { sum = size = 0, minv = inf, maxv = -inf; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             inline int atag(int x, tag y) { return x*y.a + y.b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      data(int \times) \{ sum = minv = maxv = x, size = 1; \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    inline void tagtree(int x, tag p, bool t) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       swap(son[x][0], son[x][1]); rev[x]^{-1}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  (maxv, x.maxv), size + x.size); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               inline void tagchain(int x, tag p)
                                                                                                        Claris
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 data csum[N], tsum[N], asum[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  asum[x] = csum[x] + tsum[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int sum, minv, maxv, size;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           val[x] = atag(val[x], p);
                                                                                                                                                                                                                                                          struct tag {
  int a, b; //ax+b
  tag() { a = 1, b = 0; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     inline void rev1(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   csum[x] = csum[x] + p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ctag[x] = ctag[x] + p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      tsum[x] = tsum[x] + p;
                                                                                                                                                                                                                         const int inf = \sim 0U >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ttag[x] = ttag[x] + p;
                                                                                                     全功能
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (!x) return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (!x) return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (!x) return;
                                                                                                                                                                                        #define N 200010
                                                                                                     \operatorname{LL}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      struct data {
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```

if (!in[x] && ctag[x] ex())tagchain(son[x][0], ctag[x]), tagchain(son[x][1], ctag[x])

if (rev[x])rev1(son[x][0]), rev1(son[x][1]), rev[x] = 0;

if (!x)return;

, ctag[x] = tag();

if (!in[x] && t)tagchain(x, p); **else** asum[x] = csum[x] + tsum[x];

```
inline void pb(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         queue<pair<pii, pii> > toUpdate;
rep(i,0,n) rep(j,i,n) rep(k,0,sz(buckets[i])) rep(1,0,sz(buckets[i]))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int res=fastFilter(buckets[a.fi][a.se]*buckets[b.fi][b.se]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         pii a=toUpdate.front().fi , b=toUpdate.front().se;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(i<=res) toUpdate.push(mp(mp(i,j),np));</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(res<=i) toUpdate.push(mp(np,mp(i,j)));</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     pii np(res, sz(buckets[res])-1);
rep(i,0,n) rep(j,0,sz(buckets[i])) {
                                                                                                                                                                                                                                                                                                                                   return fastFilter(g , false) == -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         toUpdate.push(mp(mp(i,k),mp(j,l)));
                                                                                                                                                                                                                                                                                                                                                                               // 置换群的生成集合, 第二维是置换的长度
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          fill(all(lookupTable[i]),-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                          bucketsInv=buckets=vector<B>(n);
                                                                                                                                                                                                                 rep(i,0,n) res*=sz(buckets[i]);
                                            p = p * bucketsInv[i][res];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(i,0,m) fastFilter(gen[i]);
                                                                                                                                                                                                                                                                                                                                                                                                        void solve(const B&gen, int _n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  lookupTable[i].resize(n),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              lookupTable=vector<vi>(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            bucketsInv[i].pb(id);
lookupTable[i][i]=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(res==-1) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      buckets[i].pb(id);
                                                                                                                                                                                                                                                                                                             bool inGroup(const P&g)
                                                                                                                                                                                                                                                                                                                                                                                                                                    = _n , m = sz(gen);
                                                                                                                                                                                                                                                                                     // 判断置换是否在置换群中
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   while(sz(toUpdate))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i,0,n) id[i]=i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               toUpdate.pop();
return i;
                                                                                                                   }
// 计算置换群的阶
11 cal() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(i,0,n) {
                                                                                                                                                                                                                                           return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(i,0,n)
                                                                                           return -1;
                                                                                                                                                                                           11 res=1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        P id(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            3 4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    277
```

```
while (son[x][2] \& in[son[x][2]])x = child(x, 2);
                                                                                                                                                                                     inline void del(int x) { // 将 x 与其虚边上的父亲断开
                                                                                                                                                                                                                                                                                                                                                                                                                                                          setson(z, pos(y), child(y, pos(x) ^ 1));
                                                                                                                                                                                                                                                                                                                                                 int s = 1, i = y, z = f[y]; a[1] = i;
while (!isroot(i, 2))a[++s] = i = f[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        inline int fa(int x) { // x 通过虚边的父亲
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               while (son[x][0])x = son[x][0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int y = 0;
for (; x; y = x, x = fa(x)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    inline int lca(int x, int y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (!f[x])return 0;
if (!in[f[x]])return f[x];
                                                       setson(z, 2, son[x][2]);
setson(z, 3, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inline int access(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                       while (s)pb(a[s—]),
if (z) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      son[y][pos(x)] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            add(x, son[x][1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               inline int root(int x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       setson(x, 1, y);
                              int z = newnode();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       splay(z, 2);
                                                                                                                                                                                                                                                                     if (!f[x])return;
int y = f[x];
if (in[y]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ru[++rub] = y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return access(y);
                                                                                                        setson(x, 2, z);
                                                                                                                                                                                                                 if (!x)return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int t = f[x];
splay(t, 2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      splay(x);
                                                                                                                                   splay(z, 2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return f[t];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   splay(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               del(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            access(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     access(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   f[x] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     splay(x);
                                                                                                                                                                                                                                              splay(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   (x)dn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   splay(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (!isroot(y, t)) { if ((son[f[y]][t] == y) ^ (son[y][t] == x))rotate(x, t); else
  rotate(y, t); }
rotate(x, t);
                                                                                                                                                                                                                                                                                                                                                                                                                             for (int i = 0; i < 2; i++)if (son[x][i])csum[x] = csum[x] + csum[son[x][i]]; asum[x] = csum[x] + tsum[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      son[y][w] = son[x][w ^ 1];
if (son[x][w ^ 1])f[son[x][w ^ 1]] = y;
if (f[y])for (int z = f[y], i = 0; i < 4; i++)if (son[z][i] == y)son[z][i] = x;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 inline void setson(int x, int t, int y) { son[x][t] = y; f[y] = x; } inline int pos(int x) { for (int i = 0; i < 4; i++)if (son[f[x]][i] == x)return i;
                                                                                                                                                                                                               for (int i = 0; i < 2; i++)if (son[x][i])tsum[x] = tsum[x] + tsum[son[x][i]]; for (int i = 2; i < 4; i++)if (son[x][i])tsum[x] = tsum[x] + asum[son[x][i]]; if (in[x]) {
                          ttag[x], 0), tagtree(son[x][1], ttag[x], 0);
ttag[x], 1), tagtree(son[x][3], ttag[x], 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        inline int child(int x, int t) { pb(son[x][t]); return son[x][t]; }
inline void rotate(int x, int t) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 inline void add(int x, int y) { // 从 x 连出一条虚边到
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     f[x] = f[y]; f[y] = x; son[x][w \land 1] = y; up(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (int i = 2, i < 4, i++)if (!son[x][i]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int y = f[x], w = (son[y][t + 1] == x) + t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int s = 1, i = x, y; a[1] = i;
while (!isroot(i, t))a[++s] = i = f[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                son[x][2] = son[x][3] = 0; in[x] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        inline void splay(int x, int t = 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int x = rub ? ru[rub--] : ++tot;
                                                                                                                                                                                                                                                                                                                                                                                                         csum[x] = data(val[x])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 while (!isroot(x, t)) {
                        tagtree(son[x][0],
tagtree(son[x][2],
                                                                                                                                                                                                                                                                                                                      asum[x] = tsum[x];
                                                                                                                                                              inline void up(int x) {
                                                                                                                                                                                                                                                                                                  csum[x] = data();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      while (s)pb(a[s—]);
  if (ttag[x].ex()) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        setson(x, i, y);
                                                                              ttag[x] = tag();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               inline int newnode() {
                                                                                                                                                                                     tsum[x] = data();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (!y)return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return 4; }
                                                                                                                                                                                                                                                                                                                                                                              else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                (x)dn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ; (x)qd
```

```
read(x), read(y);
printf("%d\n", askchain(x, y).minv);
makeroot(rt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              read(x), read(y);
printf("%d\n", askchain(x, y).maxv);
makeroot(rt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                              printf("%d\n", asktree(x).minv);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             printf("%d\n", asktree(x).maxv);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            printf("%d\n", asktree(x).sum);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           changechain(x, y, tag(0, z));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (k == 6) { // 链加
read(x), read(y), read(z);
changechain(x, y, tag(1, z));
                                                                                                                  if (k == 9) { // x 的父亲变成 y
read(x), read(y);
                                                                                                                                                            if (lca(x, y) == x)continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (k == 2) { // 链赋值
    read(x), read(y), read(z);
                                                                                                                                                                                                                                                                                                    changetree(x, tag(0, y));
                                                                                                                                                                                                                                                                                                                                                                                  changetree(x, tag(1, y));
                                                                                                                                                                                                                                                                                                                                                                                                                         if (k == 3) { // 子树最小值
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (k == 4) { // 子树最大值
                                                                                                                                                                                                                                                            if (k == 0) { // 子树赋值
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (k == 7) { // 链最小值
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (k == 8) { // 链最大值
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (k == 11) { // 子树和
                                                                                                                                                                                                                                                                                                                                        if (k == 5) { // 子树加
read(x), read(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (k == 10) { // 链和
                                      if (k == 1) { // 换根
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 read(x), read(y);
                                                                                                                                                                                                                                                                                  read(x), read(y);
                                                                             makeroot(rt);
                                                                                                                                                                                                                         makeroot(rt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 makeroot(rt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    makeroot(rt);
                                                                                                                                                                                                   link(y, x);
                                                         read(rt)
                                                                                                                                                                                                                                                                                                                                                                                                                                                  read(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             read(x);
while (m—) {
                                                                                                                                                                             cut(x);
                     read(k);
```

```
for (int i = 2; i < 4; i++) if (son[x][i])tagtree(son[x][i], p, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for (int i = 2; i < 4; i++) if (son[x][i])t = t + asum[son[x][i]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for (i = 1; i < n; i++) read(ed[i][0]), read(ed[i][1]);
for (i = 1; i <= n; i++) read(val[i]), up(i);
for (i = 1; i < n; i++) link(ed[i][0], ed[i][1]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                   inline void changechain(int x, int y, tag p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           inline void changetree(int x, tag p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               inline data askchain(int x, int y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int n, m, x, y, z, k, i, ed[N][2];
                                                                                                                                            inline void link(int x, int y) {
                                     inline void makeroot(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             inline data asktree(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       splay(x);
val[x] = atag(val[x], p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         splay(x);
data t = data(val[x]);
                                                                                                                                                                                                                                                 inline void cut(int x)
                                                                                                                                                                                                                                                                                            splay(x);
f[son[x][0]] = 0;
son[x][0] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         read(n); read(m);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        tagchain(y, p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return csum[y];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      makeroot(rt);
                                                                                                                                                                  makeroot(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    makeroot(x);
                                                                                                                                                                                                                                                                                                                                                                                                                            makeroot(x);
                                                            access(x);
                                                                                                                                                                                      add(y, x);
                                                                                                                                                                                                                                                                         access(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                             access(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           access(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   access(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      access(x);
                                                                                                                                                                                                           access(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     splay(x);
                                                                                 splay(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           splay(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 read(rt);
return x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                   splay(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              tot = n;
                                                                                                      rev1(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    (x)dn
                                                                                                                                                                                                                                                                                                                                                              (x)dn
```

```
// return x, where ax = 1 \pmod{mod}
                                                                                                                                                    if (gcd(a, mod) != 1) return -1;
11 b = mod, s = 1, t = 0;
while (b) {
exgcd(b, a % b, g, y, x);
y == x * (a / b);
                                                                                                                           11 mod_inv(11 a, 11 mod) {
printf("%d\n", askchain(x, y).sum);
                            makeroot(rt);
                                                                                                    return 0;
```

std::swap(a -= q * b, b); std::swap(s -= q * t, t);

11 q = a / b;

$_{ m basic}$ 11.4

```
return mul\_mod(r2 + mod2 - r1, inv, mod2) * mod1 + r1;
                                                                                                                                                                                                                                                                                                                                                       bool linear_equation(ll a, ll b, ll c, ll &x, ll &y)
                                                                                                                                                                    ull crt2(ull r1, ull mod1, ull r2, ull mod2) {
                                                                                                                                                                                                                                                                                               //ax + by = c, x >= 0, x is minimum
                                                                                                                                                                                                                                                                                                                        //xx = x + t * b, yy = y - t * a
                                                                                                                                                                                                   ull inv = mod_inv(mod1, mod2);
                                                                                                              return s < 0 ? s + mod : s;
                                                                                                                                                                                                                                                                                                                                                                                                                    exgcd(a,b,g,x,y);
if (c % g) return false;
                                                                                                                                                                                                                                                                                                                                                                                      11 g;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             inline ll add_mod(ll x, ll y, ll mod) { return (x + y) % mod; } inline ll sub_mod(ll x, ll y, ll mod) { return (x - y + mod) % mod; } inline ull mul_add_mod(ull a, ull b, ull c, ull mod) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // mod should be not greater than 2^62 (about 4e18) // return a * b % mod when mod is less than 2^31
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           T gcd(T a, T b) { return !b ? a : gcd(b, a % b); }
// ax + by = gcd(a, b), |x| + |y| is minimum
void exgcd(11 a, 11 b, 11 &g, 11 &x, 11 &y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return mod128\_64\_small(uill(a) * b + c, mod);
                                                                                                                                                                                                                                                                                                                               : "=a"(q), "=d"(r)
: "0"(ull(a)), "1"(ull(a >> 64)), "rm"(b)
                                                                                                                                                                                                            inline ull mod128_64_small(uill a, ull b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 inline ull mul_mod(ull a, ull b, ull mod) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ull k = (ull)((long double)a * b / mod);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (mod < int(1e9)) return a * b % mod;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (n \& 1) res = mul\_mod(res, a, m);
                                                                                                                   using ull = unsigned long long;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 11 pow_mod(11 a, 11 n, 11 m) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (!b) x = 1, y = 0, g = a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if ((11)res < 0) res += mod;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               assert(0 <= a && a < mod);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         assert(0 <= b && b < mod);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ull res = a * b - k * mod;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for (a %= m; n; n >>= 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       a = mul_mod(a, a, m);
                                                                                                                                             using uill = \_uill\_t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               template<typename T>
                                                                                    using 11 = 1 ong 1 ong
                                                          #include <algorithm>
                            #include <cassert>
                                                                                                                                                                                                                                                                asm____
"divq\t%4"
"'~)
                                                                                                                                                                                // return a % b
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    11 res = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return res;
#pragma once
                                                                                                                                                                                                                                      ull q, r;
                                                                                                                                                                                                                                                                                                                                                                                                                              return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        else {
```

for (11 i = 2; i * i <= n; ++i) if (n % i == 0)if (n > 1) ret = ret / n * (n - 1); b /= g, a /= g, c /= g; x = (x % b * (c % b) % b + b) % b; y = (c - a * x) / b; typedef unsigned long long ull; while (n % i == 0) n /= i;ret = ret / i * (i - 1);// 求的欧拉函数值,简易版n factors_pe 11 euler_phi(11 n) { return true; 11 ret = n;return ret; 11.5

```
if (\_gcd(a, mod) != 1) return -1;
                                                                                                                                                                                                                    return s < 0 ? s + mod : s;
                                                                                    11 b = mod, s = 1, t = \theta;
                                         li mod_inv(ll a, ll mod) {
typedef __uint128_t dw;
typedef vector<ull> vl;
                                                                                                                                                swap(a -= q * b,
                                                                                                                                                                      swap(s -= q * t,
                                                                                                                             11 q = a / b;
                                                                                                       while (b) {
```

```
* f_p[][0/1/2/3/...] 分别代表质数个数 / 质数和 / 质数平方和 / 质数三次方和 /... 根据自己需要
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        add = (dw)pows[ex] * prod % pe * inv[i] % pe * add % pe * f_pe[i] % pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        * pow_sum() 函数中 (38-43 行 ) 填幂和函数(如果需要更高次的话可以在这里添加)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ull j = deg - 1 - i, ex = v - vs[i] - cfac_vs[i] - cfac_vs[j];
                                                                                                                                                                                                                                                                                                                                                                                                                                   iprod = (dw)iprod * ((x - i) / pows[vs[i]]) %
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return (dw)fact_range(u, v) * evaluate(u) % pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              * f() 函数中 (31-37 行 ) 填函数在质数幂次处的表达式
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ull add = (dw)cifac[j] * cifac[i] % pe;
                                                                                                                                                                                      for (; m % p == 0; m /= p, ++vs[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (ex & 1) ret = (dw)ret * fac % pe;
                                                                                                                                                                                                                                                                                                                                                                       for (int i = deg - 1; i >= 0; —i) {
                                                                                                                                                                                                                                                                                                                                                                                                       inv[i] = (dw)iprod * inv[i] % pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     be'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // ((up+v)!)_p \mod p^ne: O(min(p, e))
auto fact_p = [&](ull u, ull v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ull ret = 0;
for (ull i = 0; i < deg; ++i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ret = (dw)ret * fact_p(u, v) %
                                                                                                                                                                                                                                                                                                                                           ull iprod = mod_inv(prod, pe);
                                                                                                                       for (ull i = 0; i < deg; ++i)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (ex %= period; ex; ex >>= 1)
                            if (x < deg) return f_pe[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (j & 1) add = pe - add
                                                                                                                                                                                                                                                                                   prod = (dw)prod * m % pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ret = (ret + add) % pe;
auto evaluate = [\&](ull \times) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (ex >= e) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ull q = n / p, v = n % p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ac = (dw)fac * fac % pe;
                                                           vl vs(deg), inv(deg);
                                                                                      ull v = \vec{0}, prod = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ull u = q \% period;
                                                                                                                                                         ull m = x - i;
                                                                                                                                                                                                                                                  inv[i] = prod;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ull ret = 1, ex = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          * 202-205 行按要求填写
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ex += n, n = d;
                                                                                                                                                                                                                          v += vs[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                26
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     while (n > 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     min
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                11.6
                                                         // f_{-\{p,\,e\}} = \prod_{\{i=0\}}/\{x-1\}(1+\sum_{\{k=1\}}/\{e-1\}\frac_{\{stir1ingfirst_{\{p\}}\{k+1\}\}\{v\}\}}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          s1[0 + j] = (s1[0 + j - min_pe - 1] + (dw)s1[0 + j - min_pe] * i) % pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 f_pe[i] = (dw)f_pe[i-1] * fact_range(i-1, p-1) % pe * ifac % pe;
                            // n! / p^{(n!)}} mod p^{n}e, assume p^{n}e < 2^{n}63 - 1, pe < 10^{n}6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             pe);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ret = (ret + (dw)prod * s1[v * min_pe + k]) % pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                auto fact_range = [&] (ull u, ull v) {
  ull coef = (dw)u % pe * p % pe, prod = 1, ret = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // f_{-}\{p,e\}\{0..2e-2\}: O(e * min(p, e) + e log(p)\} ull fac = fact_range(0, p - 1), ifac = mod_inv(fac,
                                                                                                                                                                                                                                                                                                                                                                                                              e)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for (int i = deg - 2; i >= 0; ---i) {
    cifac[i] = (dw)cifac[i + 1] * cifac[i] % pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // find the value of f_{-}\{p, e\}(x): O(e \log x)
                                                                                                                                                                                                                                                                                                                                                                                                         // first kind stirling number: O(p * min(p, v1 s1(p * min_pe); s1[0] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // product of \{up + 1, \ldots, up + v\} mod p^{A}e
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 s1[o] = (dw)s1[o - min_pe] * i % pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // coprime factorials: 0(e + e log(p))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for (ull k = 0; k < min_pe; ++k) {</pre>
                                                                                                                                                                                                                                                                                                              ull period = pe / p * 2, deg = e * 2
                                                                                                                                                                                                                                                                               rep(i, 1, e+1) pows[i] = (pe *= p);
                                                                                                                                                                                                                                                                                                                                           if (p == 2 && e >= 3) period >>= 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for (; j % p == 0; j /= p, ++v);
cfac_vs[i] = cfac_vs[i - 1] + v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          cifac[deg - 1] = mod\_inv(prod, pe);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             prod = (dw)prod * coef % pe;
                                                                                                                                               stirlingfirst{p}{1} (ip)^\klapha ) ull fact_pe(ull n, ull p, ull e) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (ull i = 1; i < deg; ++i) {
                                                                                                                                                                                                                                               ull pe = 1, min_pe = min(p, e);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           vl cifac(deg, 1), cfac_vs(deg);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (ull i = 1; i < deg; ++i)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            prod = (dw)prod^* j \% pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 1, p) {
    int o = i * min_pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ull j = i, v = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            cifac[i-1] = j;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(j, 1, min_pe)
                                                                                                                                                                                                                       v1 pows(e + 1, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  vl f_pe(deg, 1);
                                                                                           +1}{k+1} \bmod p^e
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ull prod = 1;
```

```
inline int get_id(ll k){ ///give a number like 'n/i', return the id of it
                                                                                                                                    for(int j=1;j<=p_sz_2&&p[j]*i<=n_2;j++){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(type=-1)st.f_val = f(p[k],e);
                                                                                                                                                                                                                                                                                               if(k>n_2) return val_id_num-n/k+1;
                                                                                                                                                                                                                                                                                                                                                                                   int lowbit(int n){return n & (-n);}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    else st.f_val = poww(i,type);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for(11 i=p[k];i<n/n_3;i*=p[k]){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void update_bfs(int k,int type){
                                             p[++p_sz_2] = i;
if(i<=n_3) p_sz_3++;
                                                                                                                                                         isp[i*p[j]] = 0;
if(i%p[j]==0) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          while(!q.empty()) q.pop();
                                                                                        if(i<=n_6) p_sz_6++;
 for(int i=2;i<=n_2;i++){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 node hd = q.front();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           while(!q.empty()){
                                                                                                                                                                                                                                                                                                                                                                                                             void add(int \times, 11 d){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                               x+=lowbit(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            x==lowbit(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   st.k_max = k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            q.push(st);
                          if(isp[i]){
                                                                                                                                                                                                                                                                                                                                                                                                                                     while(x<maxn){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        st.val = i;
                                                                                                                                                                                                                                                                                                                       else return k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         dnene<node> d;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ans+=c[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                node st;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               11 sum(int x){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                            c[x]+=q
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int e = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int k_max;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 11 f_val;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             while(x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 struct node{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         11 ans=0;
                                                                                                                                                                                                                                                                                                                                                               11 c[maxn];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             11 val;
* 例: 如果该函数在质数处表达式为 f(p) = p^2+3*p+1 ,则表明需要质数个数 / 质数和 / 质数平方和, ||
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ll val_id[maxn]; ///give the id, return the id—th number like 'n/i', (val_id[1] = 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int val_id_num_3; ///how many numbers like 'n/i' below n/n_3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int val_id_num; ///how many numbers like 'n/i'
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(k==2) return n^*(n+1)^*(2^*n+1)/6;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ///return sum(i^{\Lambda}k), i from 1 to n.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                11 f_p[maxn][3];///F_prime(id(n/i))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int n_3; //(int)pow(n,1.0/3.0)
int n_6; //(int)pow(n,1.0/6.0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    val id[++val id num] = i;
                      即 f_p[][0],f_p[][1],f_p[][2]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(k==1) return n*(n+1)/2;
                                                                  const int maxn = 20000000+100
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           n_3 = (int)pow(n, 1.0/3.0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             n_6 = (int)pow(n, 1.0/6.0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         memset(isp,1,sizeof isp);
                                                                                                                                                                                                                                                                                                                                                                                                                                if(p==1||e==0) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return res*res+3*res+1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int n_2; //(int)sqrt(n)
                                                                                                                                                                                                                                                                                                                                                                                                      inline 11 f(11 p, int e){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              pow_sum(11 n, int k){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           11 res = poww(p,e);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int p_sz_2; ///pi(n_2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int p_sz_6; ///pi(n_6)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     n_2 = (int) sqrt(n);
                                                                                                                                                    while(b){
   if(b&1){
      res *= base;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int p_sz_3; ///pi(n_3)
                                                                                                                                                                                                                           //res %= mod;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for(11 i=1;i<=n;){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 i = n/(n/(i+1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(k==0) return n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(i==n) break;
                                                                                                                                                                                                                                                                                               //base %= mod;
                                                                                                                                                                                                                                                                                                                                                                                                                                                        ///return f(p^e)
                                                                                     11 poww(11 a,11 b){
                                                                                                                                                                                                                                                                   base *= base;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int p[200000+100];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     val_id_num = 0;
                                                                                                                               ll base = a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         bool isp[maxn];
                                                                                                          11 \text{ res} = 1;
                                                                                                                                                                                                                                                                                                                                                              return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  isp[1] = 0;
                                                                                                                                                                                                                                                                                                                    b>>=1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            void init(){
```

```
else f_p[j][tt] = f_p[j][tt] - (f_p[get_id(w)][tt]-sum(p[now-1]))*poww(p[now-1])
                                                                                                                             if(wcn/n_3) f_p[j][tt] = f_p[j][tt] - (sum(get_id(w)) - sum(p[now-1]))*poww(
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for(int pp=p_sz_3+1;p[pp]<=(int)(sqrt(val_id[now]))&&pp<=p_sz_2;pp++){
    F[now] += f(p[pp],2) + (f(p[pp],1))*(f_p[get_id(val_id[now]/p[pp])][0]-f_p[</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ///if f(p) = p \wedge 2 + 3p + 1, then write:f_p[i][0] = f_p[i][2] + 3 + f_p[i][1] + f_p[i][0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         f_p[j][tt] = (f_p[get_id(w)][tt] - f_p[p[now-1]][tt])*poww(p[now],tt);
                                                                                                                                                                                                                                                                                                                                                          for(int i=1;i<=val_id_num&&val_id[i]<n/n_3;i++) f_p[i][tt] = sum(i);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 F[now] += F[get_id(val_id[now]/_p)]*f(p[k],e);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for(int i=2;val_id[i]<n/n_3;i++) add(i, F[i] - F[i-1]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        f_p[i][0] = f_p[i][2] + 3*f_p[i][1] + f_p[i][0]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   F[now] = 1+(f_p[now][0]-f_p[q-1][0]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       F[now] = 1+(f_p[now][0]-f_p[q-1][0]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       11 F[2000000+100];

void get_f_3(11 n){ ///V(F_{pi(n^(1/3))+1},n)

11 q = p[p_sz_3+1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void get_f_6(11 n) \{ ///V(F_{ful}(n^{1/6}))+1\}, n)
For(int j=val\_id\_num; j>=1; j---){
                                                                                                                                                                                                                                                                                                                                                                                                                           For(int j=val_id_num;j>=1;j---){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for(int now=1;now<=val_id_num;now++){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          while(val_id[now]/_p){
   if(val_id[now]/_p>=n/n_3){
                                                                 if(val_id[j]<n/n_3) break;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(val_id[j]<n/n_3) break;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for(;val\_id[now]>=n/n_3;now—){
                         11 w = val_id[j]/p[now];
                                                                                                                                                                                                                                                                                                                                                                                                                                                       il\ w = val\_id[j]/p[now]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for(int i=1;i<=val_id_num;i++){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for(int k=p_sz_3; k>p_sz_6; k—){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      else if(val_id[now]<q*q){</pre>
                                                                                          if(w<p[now]) break;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(w<p[now]) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   get_id(p[pp])][0]);
                                                                                                                                                                                                                                                                                                                                                                                             for(;now<=p_sz_2;now++){
                                                                                                                                                                                                                                                                                                update_bfs(now,tt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int now = val id num;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(val_id[now]<q){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       memset(c,0,sizeof c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               11 _p = p[k];
                                                                                                                                                                p[now],tt)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        F[now] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int e = 1;
                                                                                                                                                                                                                               ],tt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  add(1, F[1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        else{
                                " << val_id[val_id_num] << "]" <<
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 f_p[j][k] = f_p[j][k] - val^*(f_p[get_id(w)][k]-f_p[p[now-1]][k]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               add(1, f\_p[1][tt]); \\ \textbf{for(int} i=2; val\_id[i] < n/n\_3; i++) \ add(i, f\_p[i][tt] - f\_p[i-1][tt]); \\
                                                                                                                                                                                                                                                                                                                                                                                           for(int i=hd.k_max+1;hd.val*p[i]<n/n_3&&i<=p_sz_2;i++){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(type==-1) nxt.f_val = hd.f_val*f(p[i],e);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        else nxt.f_val = hd.f_val*poww(res,type);
                                W = n/W_i //Cout << hd.val << "[" << W<" ,
                                                                                                                                                           add(val_id_num+1,-111*hd.f_val);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    f_p[i][j] = pow_sum(val\_id[i], j)-1;
                                                                                                                                                                                                                                                             add(get\_id(w), -111*hd.f\_val);
                                                                                                                                                                                                                                                                                              add(val_id_num+1,hd.f_val)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for(int j=val_id_num; j>=1; j--){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              For(int k = 0; k \leftarrow times; k + +)
                                                                                                                             add(get_id(w),hd.f_val);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          nxt.val = hd.val*res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for(int i=1;i<=val_id_num;i++){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for(int tt = 0;tt<=times;tt++){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      //for(now=1;now<=p_sz_2;now++){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(hd.val*res<n/n_3){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              11 w = val_id[j]/p[now];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for(int j=0;j<=times;j++){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for(now=1;p[now]<=n_6;now++){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for(;p[now]<=n_3;now++){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              nxt.k_max = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void get_f_p(ll n,int times){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(w<p[now]) break;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                            for(int e=1;;e++){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       q.push(nxt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               memset(c,0,sizeof c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int nnow = now, val = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    val *= p[now];
  11 w = n/hd.val;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                node nxt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         res *= p[i];
                                                                                                                                                                                                                                                                                                                                                                                                                           11 res = p[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        else break;
                                                                                                    if(type==-1){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       11 val=1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     now = now;
                                                                                                                                                                                                                                  else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int now;
```

```
if (ok) ans += use[1] * use[2] + use[2] * use[3] + use[3] * use[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (!ok) { ans += 111 * sz(tmp) * sz(tmp);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for (auto u : tmp) ans += sz(g[u]);
                                                                                                                                                                                                                                                                                                               if (vis[v] != inc(vis[u])) ok = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (\text{vis}[v] := \text{dec}(\text{vis}[u])) ok = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 1, 4) use[i] = 0;

for (auto u : tmp) use[vis[u]]++;

rep(i, 1, 4) ok &= use[i] > 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ok = 1; tmp.clear(); vis[i] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 1, n+1) if (!vis[i])
                                                                                                                                                                                                                                                                                                                                                                                                                                            vis[v] = dec(vis[u]);
                                                                                                                                                                                                                                    vis[v] = inc(vis[u]);
                                                                                                                                                                                                                                                                                                                                                                                     for (auto v : gg[u]) {
                                                                                                                                                          tmp.pb(u);
for (auto v : g[u]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     cout << ans << endl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int t = 0;
                                                   if (x == 0) x = 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(i, 1, m+1) {
cin >> u >> v;
                                                                                                                                                                                                          if (!vis[v])
                                                                                                                                                                                                                                                                                                                                                                                                                  if (!vis[v])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          gg[v].pb(u);
                                                                                                                           void dfs(int u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              g[u].pb(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     cin >> n >> m;
                                                                                                                                                                                                                                                            dfs(v);
 int dec(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      dfs(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             dfs(i);
                                                                                                                                                                                                                                                                                         }else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  }else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return 0;
                                                                               return x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int main(){//n = 10000000000; //1e10:455052511,0.83s/0.58s 1e12:37607912018 9.224s/5.105s
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int kpow(int a, int b) {int r=1;for(;b;b>>=1,a=mul(a,a)) {if(b&1)r=mul(r,a);}return r;} bool ok; int vis[N], n, m, u, v; ll use[N], ans; vi g[N], gg[N], tmp;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      C 三种颜色染色,满足对所有边 u→ν 有 v 的颜色是 u 的下一种颜色
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                get_f_6(n);
get_f(n);
for(int i=1;i<=val_id_num;i++) cout << val_id[i] << " : " << F[i] << endl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             const int P = 1e9 + 7, N = 1e5 + 8;
int add(int a, int b) {if((a += b) >= P) a -= P; return a < 0 ? a + P : a;}
int mul(int a, int b) {return 111 * a * b % P;}</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        * 1. 如果能染色且没用够三种颜色,不能增加边
* 2. 如果能染色且用了三种颜色,把点按颜色分为三类,三类点中相邻两类都有边
* 3. 如果不能染色,所有点之间都有边
                                                                                                                                                                                                                                                            for(int i=1;i<=val_id_num&&val_id[i]<n/n_3;i++) F[i] = sum(i);</pre>
F[now] += sum(get_id(val_id[now]/_p))*f(p[k],e);
                                                                                                                                                                              //cout << "*****" << p[k] << "*****" << n/n_3 << endl;
                                                                                                                                                                                                          update_bfs(k,-1);//bfs_to update [lpf(i)==P{k-1}]f(i)
                                                                                                                                                                                                                                                                                                                                                                                         int e = 1;
11 _p = p[k];
while(val_id[now]/_p){
    F[now] += F[get_id(val_id[now]/_p)]*f(p[k],e);
                                                                                                                                                                                                                                                                                                                                                                 for(int now = val\_id\_num;now>=1;now—){
                                                                                                                                                                                                                                                                                                             void get_f(11 n){
   for(int k=p_sz_6;k>=1;k—){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           三元闭包边计数
                                                   _p *= p[k];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          * 染色: 能用 A · B ·
* 对每一个弱连通子图:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              p^* = p[k];
                                                                                                                                                          if(k==1) break;
                                                                           e++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            6++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              get_f_p(n, 2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              * 三元闭包边计数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          get_f_3(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              cin >> n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          init();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               11.7
```

主元法网格图随机游走

11.8

#include<bits/stdc++.h>

if (x == 4) x = 1;

return x;

int inc(int x) {

using namespace std;

```
rep(i, 0, n+2) rep(j, 0, n+2) hole[i][j] = !(i>=1 && i<=n && j>=1 && j<=n); rep(i, 1, m+1) cin >> x[i] >> y[i], hole[x[i]][y[i]] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ans[i] = mul(eqs[i]^* ans, kpow(P - eqs[i][i], P - 2));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         eqs[i] = eqs[i] * kpow(eqs[i][i], P - 2);
rep(j, i+1, m) eqs[j] = eqs[j] - eqs[i] * eqs[j][i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     0};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(j, i, m) if (eqs[j][i]) {id = j; break;}
if (id != i) swap(eqs[i], eqs[id]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        o`
                            per(i, 0, sz(a)) r[i] = mul(r[i], x);
                                                                                                                                                                       per(i, 0, sz(a)) r[i] = mul(r[i], x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              vec ans; ans.clear(n); ans.a.back() = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     const int dx[] = \{0, 0, -1, 1\}, dy[] = \{1,
                                                                                                                                          vec r = *this; x = kpow(x, P - 2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return 4-(x==1)-(x==n)-(y==1)-(y==n);
                                                                                                                                                                                                                                                                                                               r.a.back() = add(r.a.back(), -x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int n = sz(eqs[0].a), m = sz(eqs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for (int i = 0; i+1 < n; ++i){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (int i = n-2; i >= 0; --i)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             vec gauss(vector<vec> &eqs){
                                                                                                                vec operator / (int \times) {
                                                                                                                                                                                                                                                            vec operator - (int \times) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ios::sync_with_stdio(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            inline int D(int x,int y)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            vector<vec> tmp = eqs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                assert(m && m >= n—1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int id[N][N], stx, sty;
vec expr[N][N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int A[N][N], B[N][N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               cin >> n >> m;
vec r = *this;
                                                                                                                                                                                                                                                                                  vec r = *this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int id = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            cin >> T;
rep(cas, 0, T){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      bool hole[N][N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              vector<vec> eqs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int x[N], y[N];
                                                           return r;
                                                                                                                                                                                                     return r;
                                                                                                                                                                                                                                                                                                                                                  return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            cin.tie(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int main(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int T;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int kpow(int a, int b) {int r=1;for(;b;b>>=1,a=mul(a,a)) {if(b&1)r=mul(r,a);}return r;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int add(int a, int b) \{if((a += b) >= P) \ a -= P; return a < 0 ? a + P : a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               //ll rnd(ll l, ll r) { RR dis(l, r); return dis(gen); }
const int P = 1e9 + 7;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     per(i, 0, sz(a)) res = add(res, mul(a[i], c[i]));
                                                                                                                                        #define rep(i, a, b) for(int i=(a); i<(b); i++) #define per(i, a, b) for(int i=(b)-1; i>=(a); i--)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int mul(int a, int b) {return 111 * a * b % P;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          per(i, 0, sz(a)) r[i] = add(r[i], -c[i]);
                                                                                                                                                                                                                  per(i, 0, sz(a)) r[i] = add(r[i], c[i]);
                                                                                                                                                                                                                                                 #define dd(a) cout << #a << " = " << a << "
                                                                                                                                                                                                                                                                                                                                                                                                #define FI(x) freopen(#x".in","r",stdin)
#define FO(x) freopen(#x".out","w",stdout)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    //typedef uniform_int_distribution<ll> RR;
                                                                                                                                                                                                                                                                                  #define all(a) (a).begin(), (a).end() #define pw(x) (111<<(x))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     typedef unsigned long long ull;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int& operator[] (int idx) {
    return a[idx];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 a.clear(); a.resize(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    vec operator + (vec &c) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int operator * (vec &c) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     vec operator - (vec c) {
                                                                                                                                                                                               #define sz(a) (int)a.size()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             vec operator * (int \times) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               typedef pair<int, int> pii;
                                                                                                                                                                                                                                                                                                                                       #define lb(x) (x) & -(x) #define end1 "\n"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              //mt19937 gen(998244353);
                                                                                                             #define eb emplace_back
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              typedef vector<int> vi
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        typedef long long 11;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void clear(int n){
                                                                                 #define pb push_back
                                                         #define mp make_pair
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        vec r = *this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  vec r = *this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int res = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                         typedef double db;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      const int N = 211;
                            #define se second
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return res;
#define fi first
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             struct vec{
```

```
B[i][j] = 0;
rep(k, 0, 4) {
  int nx = i + dx[k], ny = j + dy[k];
  if (!hole[nx][ny]) B[i][j] = add(B[i][j], mul(A[nx][ny] + B[nx][ny], kpow(D(
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 1, m+1) {
    if (!A[x[i]][y[i]]) cout << "GG";else cout << mul(B[x[i]][y[i]], kpow(A[x[i]][y
                                                                                                                                                                                      rep(k, 0, 3) {
   int nx = i + dx[k], ny = j + dy[k];
   if (!hole[nx][ny]) eq = eq - expr[nx][ny] / D(nx, ny) - mul(A[nx][ny],
if (!hole[nx][ny]) eq = eq - \exp[nx][ny] / D(nx, ny) - mul(A[nx][ny],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(i, 1, n+1) rep(j, 1, n+1) if (!hole[i][j]) B[i][j] = expr[i][j] * ans; rep(i, 1, n+1) rep(j, 1, n+1) if (hole[i][j]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(i, 1, N) \ f[i] = i \ * (i-1) / 2, \ g[i] = i \ * (i-1) \ * (i-2) / 6; while (cin >> n){
                                                                                                                                                                                                                                                                                                                                                                                                                                         assert((int)eqs.size()==N); // 数组表示到每个点所有的路径长度期
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               bitset<N> a[N]; int n; string s; ll ans, b[9], f[N], g[N], d[N]; ll c[9] = \{24, 48, 2, 12, 6, 12, 36, 12, 24\};
                                                                                                                                                                                                                                                                                                                                               eq = eq * D(i+1,j); eq = eq - A[i+1][j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(j, 0, n) if (s[j] == '1') a[i].set(j);
                                                                                                                                                         vec &eq=expr[i+1][j]; eq=expr[i][j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // ans = 非六元简单环计数
// 六元环 = ( 只用走六步的所有方案 – ans) /
                             \mathsf{kpow}(\mathsf{D}(\mathsf{nx},\;\mathsf{ny}),\;\mathsf{P}-2));
                                                                                                                                                                                                                                                                                  \mathsf{kpow}(\mathsf{D}(\mathsf{nx},\;\mathsf{ny}),\;\mathsf{P}-2));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(i, 0, n) rep(j, i+1, n) {
   int x = (a[i] & a[j]).count();
   if (a[i][j]) b[0] += x;
   b[1]+=f[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           望B Bu = sigma((Bv + Av) / Dv) ans = gauss(eqs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 0, n) a[i].reset();
rep(i, 0, n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     [ij], P - 2);
cout << " \n"[i == m];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 nx, ny), P - 2)));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      d[i] = a[i].count();
                                                                                            eds.eb(eq);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 const int N = 1e3 + 7;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         六元环计数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // time : 0(n^3 / 64)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       cin >> s;
                                                                                                                              }else{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int main(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 11.9
                                                                                                                                                                                      rep(i, 1, n+1) rep(j, 1, n+1) if (!hole[i][j] && id[i][j] != -1){ // 初始化主元主元
为所有非洞且上方为洞的变量
expr[i][j].clear(N+1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (!hole[nx][ny]) A[i][j] = add(A[i][j], mul(A[nx][ny], kpow(D(nx,ny), P -
                                                            rep(i, 1, n+1) rep(j, 1, n+1) id[i][j] = -1;
rep(j, 1, n+1) if (!hole[1][j]) id[1][j] = N++;
rep(i, 2, n+1) rep(j, 1, n+1) if (hole[i-1][j] && !hole[i][j]) id[i][j] = N++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 1, n+1) rep(j, 1, n+1) if (!hole[i][j]) A[i][j] = expr[i][j] * ans; rep(i, 1, n+1) rep(j, 1, n+1) if (hole[i][j]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 1, n+1) rep(j, 1, n+1) if (!hole[i][j] && id[i][j] != -1){
   expr[i][j].clear(N+1);
   expr[i][j][id[i][j]] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (!hole[nx][ny]) eq = eq - \exp[nx][ny] / D(nx, ny);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (!hole[nx][ny]) eq = eq - expr[nx][ny] / D(nx, ny);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                assert((int)eqs.size()==N); // 数组表示经过每个点的期望次
                                                                                                                                                                                                                                                                                                                                        rep(i, 1, n+1) rep(j, 1, n+1) if (!hole[i][j]){
if (hole[i+1][j]){ // 下方是洞那么会产生一个方程
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(i, 1, n+1) rep(j, 1, n+1) if (!hole[i][j]){
if (hole[i+1][j]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          vec &eq = expr[i+1][j]; eq = expr[i][j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        }else{ // 下方不是洞那么下方变量可以用主元表示
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(k, 0, 3) { int nx = i + dx[k], ny = j + dy[k];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(k, 0, 3) { int nx = i + dx[k], ny = j + dy[k];
                                                                                                                                                                                                                                                                                                                                                                                                                                         _= 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (i == stx && j == sty) eq[N] -= 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(k, 0, 4) {
    int nx = i + dx[k], ny = j + dy[k];
                                                                                                                                                                                                                                                                                                                                                                                                                                    if (i == stx \&\& j == sty) eq[N]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               \cancel{a}(A - Au = sigma(Av / Dv) + (u == st)
vec ans = gauss(eqs);
                                                                                                                                                                                                                                                                              expr[i][j][id[i][j]] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                          vec eq = expr[i][j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     vec eq = expr[i][j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   eq = eq * D(i+1, j);
cin >> stx >> sty;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                eds.eb(eq);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    A[i][j] = 0;
                                                                                                                                                           eqs.clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            eds.clear();
                                  int N = 0;
```

rep(i, 1, n+1) cin \gg a[i], V.pb(a[i]); rep(i, 1, m+1) {

cin >> s >> q[i].a >> q[i].b; if(s[0]=='Q') cin >> q[i].k;

string s;

q[i].op = (s[0]=-|Q'|);

else V.pb(q[i].b);

V.clear(); seg.init(); fw.init();

///read

cin >> n >> m;

while(T---) {

```
for(; x<=n; x+=1b(x)) seg.upd(rt[x+n], rt[x+n], p, c, 0, sz(V)-1);</pre>
rep(i, 0, sz(add)) add[i] = rs[add[i]];
rep(i, 0, sz(sub)) sub[i] = rs[sub[i]];
                                                           return qry(L, R, k—lc, mid+1, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return seg.qry(1, r, k, 0, sz(V)—1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for(; x; x^=lb(x)) sub.pb(rt[n+x]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for(; x; x^{-1}b(x)) add.pb(rt[n+x]);
                                                                                                                                                                                                                    #define lb(x) ((x)&(-x))
void init() { fill_n(rt+1+n, n, 0); }
                                                                                                                                                                                                                                                                                                                                                                                                                                     add.pb(rt[r]);sub.pb(rt[l-1]);
                                                                                                                                                                                                                                                                                 void upd(int x, int p, int c) {
                                                                                                                                                                                                                                                                                                                                                                            int qry(int 1, int r, int k) {
                                                                                                                                                                                                                                                                                                                                                                                                         add.clear();sub.clear();
                                                                                                                                                                                       struct Fenwick {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int \times = r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    x = 1-1;
                                                                                                                                                                                                                                                                                                                                                                       b[0]/=3; b[1]/=2; b[4]-=3*b[0]; b[7]-=2*b[6]; b[8]-=2*b[6]; ans=0; rep(i, 0, 9) ans += b[i] * c[i], b[i] = 0;
                                                                                                                                                                                                                                                                          rep(j, 0, n) if (a[i][j]) res += (a[i] & a[j]).count();
res /= 2; b[8] += res * (res - 1) / 2;
if (a[i][j]) b[2]++;
if (a[i][j]) b[4] += (d[i]-1)*(d[j]-1);
if (a[i][j]) b[6] += f[x];
b[7] += f[x] * (d[i] + d[j] - 4);
                                                                                                                                                                                                                                                                                                                                                                                                                                        cout << ans << endl;
                                                                                                                                                                                b[3] += f[d[i]];
                                                                                                                                                                                                                      b[5] += g[d[i]];
                                                                                                                                                        rep(i, 0, n) {
                                                                                                                                                                                                                                                ll res = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return 0;
```

対核 k 大 11.10

```
int T; cin >> T;
                    int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            11.11
                                                                                                      inline int rk(int x) \{ return lower_bound(all(V), x) - V.begin(); \}
                                                                                                                                                                                                                                                                                              int cntn, cnt[N], ls[N], rs[N];
void init() { fill_n(rt+1, n, cntn = 0); }
void upd(int pre, int &now, int p, int c, int l, int r) {
                                                                                                                                                                                                                                                                     static const int N = 2500005; //(::N + 32 * ::M) * 16;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(p<=mid) upd(ls[pre], ls[now], p, c, l, mid);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          else upd(rs[pre], rs[now], p, c, mid+1, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 0, sz(add)) add[i] = ls[add[i]];
rep(i, 0, sz(sub)) sub[i] = ls[sub[i]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int qry(int L, int R, int k, int l, int r) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for(auto i : add) lc += cnt[ls[i]];
for(auto i : sub) lc -= cnt[ls[i]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return qry(L, R, k, l, mid);
                         const int N = 50505, M = 10101;
                                                                                                                                                                                                                                                                                                                                                                                                         cnt[now] = cnt[pre] + c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(1 == r) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(1 == r) return ;
                                                int n, m, a[N], rt[N<<1];</pre>
ls[now] = ls[pre];
rs[now] = rs[pre];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int mid = 1+r>>1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int mid = 1+r>>1;
                                                                                                                                                                                                                                                                                                                                                                                  now = ++cntn;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(1c>=k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int lc = 0;
                                                                               vi V, add, sub;
                                                                                                                                                                                        int a, b, k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        } else {
                                                                                                                                                                                                                                      struct Seg {
                                                                                                                                                            bool op;
                                                                                                                                   struct Q {
```

动态树上路径 k 大

return 0;

if(q[i].op) { cout << V[fw.qry(q[i].a, q[i].b, q[i].k)] << endl; } else {

fw.upd(p, rk(a[p]), -1); fw.upd(p, rk(a[p] = c), 1);

int p = q[i].a, c = q[i].b;

rep(i, 1, n+1) seg.upd(rt[i-1], rt[i], rk(a[i]), 1, 0, sz(V)-1); rep(i, 1, m+1) {

V.erase(unique(all(V)), V.end());

sort(all(V));

///solve

```
int n, m, L, dfn, val[N], rt[N], cnt[M], ls[M], rs[M], st[N], ed[N], fw[N], pair<int, pii> Q[N]; vi V, res[2], g[N]; LCARMQ R;
int F(int x) { return lower_bound(all(V), x) - V.begin() + 1; }
                                                                                                                                                              bəs //
```

```
<< endl;
b), d = par[c];
                                                           cout << V[qry(k, 1, sz(V)) - 1]
                    upd(a, 0); upd(b, 0);
upd(c, 1); upd(d, 1);
int c = R.lca(a)
```

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```
for(int i = 1; i * i < 'r; i++) cnt1 += sqrt(r - i * i);
for(int i = 1; i * i < r; i += 2) cnt2 += (sqrt(r - i * i) + 1) / 2;</pre>
                                                bool vis[N];
int w1[N * 2], w2[N * 2], id1[N * 2], id2[N * 2], t1;// 注意 longlong
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ans += 1ll * (n / l) * (w2[id(r)] - w2[id(l-1)]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ans += 1ll * (n / l) * (w1[id(r)] - w1[id(l-1)]);
                                                                                                                                                                                                                                                                                                                                                                                                                           int id(int \times) { return \times <= Sqr ? id1[x] : id2[n / x];}
                                                                                                                                                                                                     for(int j = 1; j <= tot && p[j] * i < N; j++){
  int u = p[j] * i;</pre>
                                                                                                                                                                                                                                                                                           if(i % p[j] == 0) { mu[u] = 0; break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   r <= Sqr ? id1[r] = t1 : id2[n / r] = t1;
                                                                                                                                                    rep(i, 2, N) {
    if (!vis[i]) p[++tot] = i,mu[i]=-1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for(int 1 = 1, r; 1 <= n; 1 = r + 1){
    r = n / (n / 1);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for(int 1 = 1, r; 1 \le n; 1 = r + 1){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for(int 1 = 1, r; 1 <= n; 1 = r + 1){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               w1[++t1] = cnt1, w2[t1] = cnt2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for(int k = 1; k * k <= n; k++){</pre>
                      int mu[N], p[N], tot = 0, Sqr, n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (mu[k] == 0) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int cnt1 = 0, cnt2 = 0;
                                                                                                                                                                                                                                                                                                                     mu[u] = -mu[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            n = _{-n};
Sqr = sqrt(n); t1 = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               r = n / (n / 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               r = n / (n / 1);
                                                                                                                                                                                                                                                              vis[u] = 1;
const int N = 34000;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             solve(int _n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             11 ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  11 ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ll ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return ans;
                                                                                                                                  mu[1] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return ans
                                                                                                                                                                                                                                                                                                                                                                                                                                                    11 h1(int n){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             il h2(int n){
                                                                                                     void init(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  SZ
```

```
11.12
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void upd(int p, int o, int c) \{ for( ; p <= n; p += lb(p)) upd(fw[p], fw[p], c, o, 1, p) \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  upd(rt[u], rt[fa], F(val[u]), 1, 1, sz(V));
rep(i, 0, sz(g[u])) if(g[u][i] != fa) dfs(g[u][i], u);
void upd(int &now, int pre, int p, int c, int l, int r)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int p = st[u]; for( ; p; p ^{\land} = 1b(p)) res[o].pb(fw[p]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(o, 0, 2) \ res[o].clear(); \\ \textbf{int} \ a = Q[i].se.fi, \ b = Q[i].se.se, \ k = Q[i].fi; \\ \end{cases}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(i, 0, sz(res[0])) res[0][i] = ls[res[0][i]];
rep(i, 0, sz(res[1])) res[1][i] = ls[res[1][i]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(i, 0, sz(res[0]))    res[0][i] = rs[res[0][i]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(i, 0, sz(res[1]))    res[1][i] = rs[res[1][i]];
                                                                                                                                                                                                 if(p \le mid) \ upd(ls[now], ls[pre], p, c, l, mid);
                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 0, sz(res[0])) cntr += cnt[rs[res[0][i]]];
rep(i, 0, sz(res[1])) cntr -= cnt[rs[res[1][i]]];
if(cntr >= k) {
                                                                                                                                                                                                                                   else upd(rs[now], rs[pre], p, c, mid + 1, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int p = Q[i].se.fi, c = Q[i].se.se;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        upd(st[p], 1, F(val[p]));
upd(ed[p] + 1, -1, F(val[p]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   upd(st[p], -1, F(val[p]));
upd(ed[p] + 1, 1, F(val[p]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return qry(k - cntr, 1, mid);
                                                                                                                                                                                                                                                                                           int qry(int k, int l, int r) {
  if(l == r) return l;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return qry(k, mid + 1, r);
                                                     cnt[now] = cnt[pre] + c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       void upd(int u, int o) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void dfs(int u, int fa)
                                                                                                                                                                                                                                                                                                                                                   int mid = 1 + r >> 1;
                                                                                                                                                                          int mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     dfs(1, 0);
rep(i, 1, m + 1) {
if(!Q[i].fi) {
                                                                                                                                           if(1 == r) return ;
                                                                                   ls[now] = ls[pre];
                                                                                                                  rs[now] = rs[pre];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         res[o].pb(rt[u]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  val[p] = c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              st[u] = ++dfn;
                                                                                                                                                                                                                                                                                                                                                                                int cntr = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // build 主席树
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void solve() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    par[u] = fa;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ed[u] = dfn;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     R.Build(g);
                               now = ++L;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // fenwick
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               (v)); }
```

```
if (A[sa[i]] != A[sa[i-1]] || B[sa[i]] != B[sa[i-1]])rk[sa[i]] ++;
                                                                                                                                                                                                                             if (r >= 1 && S1.1 % S1.d == S2.1 % S1.d)return Seq(1, r, S1.d);
                                                                                                                                                                                                                                                                                                                                                                                                                            vector<vi> pos[maxlog];
int name[N][maxlog], cntA[N],cntB[N],tsa[N],A[N],B[N], sa[N],rk[N];
void init(char *ch, int n){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for (int i=n;i>=1;i—)sa[cntA[A[tsa[i]]]—] = tsa[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              (int i=n; i>=1; i--)tsa[cntB[B[i]]--] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for (int i=0;i<=n;i++)cntA[i] = cntB[i] = 0;
                                                                                                                                                                       if (S1.d == S2.d){
   int 1 = max(S1.1,S2.1), r = min(S1.r,S2.r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int i=1;i<=n;i++)cntB[i] += cntB[i-1];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             (int i=1;i<=n;i++)cntA[i] += cntA[i-1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (ch[sa[i]] != ch[sa[i-1]])rk[sa[i]] ++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for (int i=n; i>=1; i—)sa[cntA[ch[i]]—] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (int step = 1,l=1;l <= n;l<<=1,step ++){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          pos[step].resize(rk[sa[n]] + 1,vi (0));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for (int i=1;i<N;i++)cntA[i] += cntA[i-1]</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          cntB[B[i]=(i+l<=n)?rk[i+l]:0]++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for (int i=1;i<=n;i++)cntA[ch[i]]++;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    pos[0].resize(rk[sa[n]] + 1,vi(0));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rk[sa[i]] = rk[sa[i-1]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   \} // get sequence [2^step, 2^(step+1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          pos[step][rk[i]].pb(i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    cntA[A[i] = rk[i]] ++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for (int i = 1;i <=n;i++){
                                                        if (S2.has(x)) pos.pb(x);
                                                                                                                                                                                                                                                                                                                                                                      struct Dictionary_of_Basic_Factories{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  name[i][step] = rk[i]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rk[sa[i]] = rk[sa[i-1]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      (int i=1;i<=n;i++){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (int i=2;i<=n;i++){</pre>
                              for (int \times : S1.to_list())
                                                                                                                                                                                                                                                           else return Seq(0,0,0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       pos[0][rk[i]].pb(i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          For (int i=2;i<=n;i++){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for (int i=1;i<=n;i++).
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           name[i][0] = rk[i]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ch[0] = ch[n+1] = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rk[sa[1]] = 1;
                                                                                                            return Seq(pos);
                                                                                                                                                                                                                                                                                        }else assert(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rk[sa[1]] = 1;
vi pos(0);
                                                                                                                                                                                                                                                                                                                                                                                                  /** 1—base **/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        for
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  bool has(int x){ return d and x \ge 1 and x \le r and x \% d == 1 \% d; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                };
Seq operator -(int x, Seq S){return Seq(X - S.r,X - S.1, S.d);}
Seq operator -(Seq S, int x){return Seq(S.1 - X, S.r - X, S.d);}
Seq operator &(Seq S1, Seq S2){
   int cnt1 = S1.count(), cnt2 = S2.count();
   int cnt1 = S1.count(), cnt2 = S2.count();
}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Seq(int l = 0, int r = 0, int d = 0) : l(1), r(r), d(d) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (cnt1 == 0 || cnt2 == 0) return Seq(0,0,0);
if (cnt1 > cnt2) swap(S1,S2), swap(cnt1,cnt2);
if (cnt1 < 3){</pre>
                            if (k \& 1) ans -= h2(n/k/k) * mu[k];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for (int i=1;i<=r;i+=d)list.pb(i);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       const int N = 2e5 + 100, maxlog = 20)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               }else if (pos.size() == 1){
    ans += h1(n/k/k) * mu[k];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  d = pos[1] - pos[0];
                                                                                                                                                                                                                                                                                                                  cout << solve(nn) << endl;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                      区间 border 查询
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return (r-1) / d + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (d == 0)return list;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            1 = pos.front();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int count(){
   if (d == 0)return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             1 = pos.front(),
r = pos.front(),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      r = pos.back();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    1 = r = d = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (pos.empty()){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Seq(const vi & pos){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       /** 1 + K*d <=r **/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           to_list(){
  vi list(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return list;
                                                                                                                                                                                                                                                           rep(cas, 0, T) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        d = 1;
                                                                                    return ans /
                                                                                                                                                                                                                                                                                        cin >> nn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  }else{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int 1, r, d;
                                                                                                                                                                  int main() {
                                                                                                                                                                                                                         cin >> T;
                                                                                                                                                                                                                                                                                                                                                                      return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             struct Seq{
                                                                                                                                           int T, nn;
                                                                                                                                                                                                     init();
                                                                                                                                                                                                                                                                                                                                                                                                                                                        11.13
```

```
ZPROBLEMS
                                                                                                                                                                                                                                                                                       else return max(query(x << 1, 1, t, fl, t), query(x << 1 | 1, t + 1, r, t + 1,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void updata(int x, int y) { for (int i = x; i < N; i += i\&-i)d[i] += y; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // r 为结尾的回文串的长度一定可以分成 10gn 段等差数列
                                                                                                                                                                                                                                                          else if (f1 > t) return query(x << 1 | 1, t + 1, r, f1, fr);
                                                  char s[N]; int m, n, 1, r; ll ans = 0, ret[N]; vector<pii> Q[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ď
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int res = 0; for (int i = x; i; i -= i\&-i) res += d[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              _`
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int next[N][26], fail[N], len[N], s[N], id[N], last, int in[N], out[N], d[N], up[N], dfn = 0; vector<int> 6[N]; //dfs \vec{\beta}
                                                                                                                                                                                                                            if (fr <= t) return query(x << 1, 1, t, fl, fr);</pre>
                                                                                                                                                                                                                                                                                                                                                                                void updata(int x, int 1, int r, int pos, int y)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       while (s[n - len[x] - 1] != s[n]) x = fail[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          fail[now] = next[get_fail(fail[cur])][c];
                                                                               struct SegTree {
  int a[N << 2];
  int query(int x, int 1, int r, int fl, int fr)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (pos <= t) updata(x << 1, 1, t, pos, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           inline int newnode(int l) {
for (int i = 0; i < 26; ++i) next[p][i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  else updata(x << 1 | 1, t + 1, r, pos, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             a[x] = max(a[x << 1], a[x << 1 | 1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     last = n = 0; s[n] = -1; fail[0] = 1;
                                                                                                                                                                      if (1 == f1 && r == fr) return a[x];
int t = (1 + r) >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int now = newnode(len[cur] + 2);
                                                                                                                                                                                                                                                                                                                                                                                                           if (1 == r) { a[x] = y; return; }
int t = (1 + r) >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     p = 0; newnode(0); newnode(-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              inline void add(int c, int cc)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inline int get_fail(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int cur = get_fail(last);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (!next[cur][c]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            inline void init() {
                      const int N = 600005;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int sum(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 len[p] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           s[++u] = c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return p++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         c -= 'a';
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return x;
namespace Space {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        struct BIT {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              struct PAM {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int d[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             }Seg;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for (int step = 0;(1<<step) < r - 1 + 1;step++) ret.pb(get_border(1,r,step));
                                                                                                                                                                                                          int last = upper_bound(list.begin(),list.end(),r) - list.begin() - 1;
```

int idx = lower_bound(list.begin(),list.end(),l) - list.begin();

get_seq(vi & list, int l, int r){

vi pos(0);

while (idx < list.size() &% pos.size() < 3 &% list[idx] <= r)

if (pos.size() < 3)return Seq(pos);</pre>

pos.pb(list[idx]);idx ++;

int L = pos.front(), d = pos[1] - pos[0], R = list[last];

return Seq(L, R, d);

Seq seq1 = $get_seq(pos[step][namel], r - giant + 1, r - baby + 1),$

seq1 = (r + 1) - seq1; seqr = seqr - (1 - baby);

return seql & seqr;

* Attention: can contain empty sequence (0,0,0) * if [2^1,2^(1+1)) border does not exist.*/

vector<Seq> get_border_series(int l,int r){

vector<Seq> ret(0);

return ret;

for (**int** $k = \max \log - 1$; $k \ge 0$; k = 0

Seq seq = get_border(1, r, k); if ((1<<k) >= len)continue

if (seq.r)return seq.r;

return 0;

int get_biggest_border(int l, int r){

int len = r - 1 + 1;

/** return O(logn) border series of S[1,r].

int name1 = name[1][step], namer = name[r - baby + 1][step]; $seqr = get_seq(pos[step][namer], 1, 1 + giant - baby);$

int baby = 1 << step, giant = min(len-1, (baby * 2-1));

Seq get_border(int 1,int r,int step){

int len = r - 1 + 1;

区间本质不同回文子串计数

scanf("%d%d", &1,&r); printf("%d\n", dbf.get_biggest_border(1,r));

return 0;

scanf("%d%d", &n, &q); scanf("%s",s + 1); dbf.init(s, n);

while (q—){

char s[N]; int n,q;

}dbf;

int main(){

11.14

```
i64 solve_fast(i64 N) {
    auto inside = [N] (i64 x, i64 y) { return x * x + y * y <= N; };
    auto cut = [] (i64 x, i64 y, int dx1, int dy1) { return dx1 * x >= dy1 * y; };
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ret += i64(dx1) * (y - 1) + ((i64(dx1 + 1) * (dy1 + 1)) >> 1) - dy1;
                                                                                                                                                                                                                                                                                                                                                                                                                              i64 \text{ y} = i64(sqrtl(max<i64>(0, N - (v + 1) * (v + 1)))) + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   auto stac = stack< pair<int, int> >({{0, 1}, {1, 1}});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (cut(x + dx12, y - dy12, dx1, dy1)) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (inside(x + dx12, y - dy12)) {
   stac.emplace(dx1 = dx12, dy1 = dy12);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       while (1) {
   int dx12 = dx1 + dx2, dy12 = dy1 + dy2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (inside(x + dx1, y - dy1)) break;
                                                                                                                                                                                                                                                                                                                                                                           const i64 v = sqrtl(N / 2), w = sqrtl(N);
                                                                                                                                                                                       n<=1e18
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       while (inside(x + dx1, y - dy1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       tie(dx1, dy1) = stac.top()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      dx2 = dx12, dy2 = dy12;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  tie(dx1, dy1) = stac.top();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int dx2 = dx1, dy2 = dy1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (stac.empty()) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   dx2 = dx1, dy2 = dy1;
                                                                                                                                                                                     // x^2+y^2<=n 整点个数包括负数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             while (!stac.empty()) {
                                                                                                                          圆内整点计数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        stac.pop();
                                                                                                                                                                                                                    using i64 = int64_t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int dx1, dy1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \times += dx1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              y = dy1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                stac.pop();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        i64 \text{ ret} = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               while (1) {
                                                                                                                                                                                                                                                                                                                                                                                                        164 \times = v;
                                                                                                                                11.15
* 77 22
```

ret = ret * 4 + 4 * 164(w) + 1;

return ret;

int main() {

ret = ret * 2 + i64(v) * v;

```
for (int j = id[i]; j; j = fail[up[j]]) {
   int l = max(1, Seg.query(1, 1, dfn, in[j], out[j]) - len[j] + 2);
   int r = i - len[up[j]] + 2;
                                                                                                                                                                void build() { for (int i=0; i< p; i++)if (i:=1) G[fail[i]].pb(i); } void dfs(int x=1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for (int i = 1; i <= m; i++) scanf("%d%d", &1, &r), Q[r].pb(mp(1, i));
                    d[now] = len[now] - len[fail[now]];
up[now] = (d[fail[now]] == d[now] ? up[fail[now]] : now);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Seg.updata(1, 1, dfn, in[id[i]], i);
for (auto j : Q[i]) ret[j.se] = BT.sum(j.fi);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 1, m + 1) printf("%lld\n", Space::ret[i]);
return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for (int i = 1; i <= n; i++) A.add(s[i], i);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                    BT.updata(1, 1); BT.updata(r, -1);
                                                                                                                                                                                                                                                                                                                                      for (int i = 1; i <= n; i++) {
                                                                                                                                                                                                                                        for (auto i : G[x]) dfs(i);
next[cur][c] = now;
                                                                                          last = next[cur][c];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void work(int n, int m) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       , O(nlogn^2) , 下标从 1 开始
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            scanf("%s", s + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           scanf("%d%d", &n, &m);
                                                                                                                                                                                                                  in[x] = ++dfn;
                                                                                                                      id[cc] = last;
                                                                                                                                                                                                                                                          out[x] = dfn;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Space::work(n, m);
                                                                                                                                                                                                                                                                                                          void solve() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 A.build();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          A.solve();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int n, m, 1, r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      A.init();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            A.dfs();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               /*注: 离线算法
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       12 5
abcddcbaabcd
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int main() {
```

```
rep(i, 0, len - 1) f[i] = cp(a[i] >> 16, a[i] \& 65535), g[i] = <math>cp(b[i] >> 16, b[i] \& 65535)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               \begin{array}{l} t = -f[i\ ?\ lim-i\ :\ 0], \ f0 = (f[i]-t)\ ^*\ cp(0,\ -0.5), \ f1 = (f[i]+t)\ ^*\ 0.5; \\ t = -g[i\ ?\ lim-i\ :\ 0], \ g0 = (g[i]-t)\ ^*\ cp(0,\ -0.5), \ g1 = (g[i]+t)\ ^*\ 0.5; \\ p[i] = f1\ ^*\ g1, \ q[i] = f1\ ^*\ g0 + f0\ ^*\ g1 + f0\ ^*\ g0\ ^*\ cp(0,\ 1); \\ \end{array} 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           b[i] = mul(h[i + n], res), res = mul(res, mul(g[i], p2 + 1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(i, 0, n) f[i] = mul(a[i], mul(ifac[i], ifac[n - i])); for (R int i = n - 1; i >= 0; i -= 2) f[i] = P - f[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               fd(i, n + n, 1) isum[i - 1] = mul(isum[i], g[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 1, n + n) g[i] = mul(isum[i], sum[i - 1]);
                                                                       if (!ty) rep(i, 0, lim - 1) A[i] = A[i] * iv[d];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 1, n + n) sum[i] = mul(sum[i - 1], g[i]);

isum[n + n] = ksm(sum[n + n], P - 2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for (R int i = 0; i <= n; p2 = add(p2, 1), ++i)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      static int f[N], g[N], h[N], sum[N], isum[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                fd(i, n, 1) isum[i - 1] = mul(isum[i], g[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 1, n) g[i] = mul(isum[i], sum[i-1]);
                                                                                                                                                                                                                                                                                                                                            rep(i, len, lim - 1) f[i] = g[i] = cp(0, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 1, n) sum[i] = mul(sum[i - 1], g[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(i, 0, n) g[i] = (011 + P + p1 + i) % P;
sum[0] = g[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           * res * i % P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void calc(int *a, int *b, int n, int k) {
                                                                                                                                                 void MTT(int *a, int *b, int len, int
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, n + n) g[i] = add(i, t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(i, n + n + 1, len - 1) g[i] =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int res = 1, p1 = k - n, p2 = k;
                                                                                                                                                                                       static cp f[N], g[N], p[N], q[N]
lim = len, d = lg[lim];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(i, n + 1, len - 1) f[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      while (len <= n + n) len <<= 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         isum[n] = ksm(sum[n], P - 2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ((11)(q[i].y + 0.5))) % P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(i, p1, p2) res = 111
                                                                                                                                                                                                                                                                                                                                                                               FFT(f, 1), FFT(g, 1);
rep(i, 0, lim - 1) {
cp t, f0, f1, g0, g1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        FFT(p, 0), FFT(q, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int t = dec(k, n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 MTT(f, g, len, h);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    res = add(res, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         g[0] = isum[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   g[0] = isum[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 snm[0] = g[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int len = 1;
                                                                                                                                                                                                                                                                                                           65535);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         inline cp operator+(const cp &b) const { return cp(x+b.x, y+b.y); } inline cp operator-(const cp &b) const { return cp(x-b.x, y-b.y); } inline cp operator*(const cp &b) const { return cp(x-b.x, y-b.y); } inline cp operator*(const cp &b) const { return cp(x*b.x-y*b.y, x*b.y, x*b.y+y*b.y)}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep[i, 2, 131072] inv[i] = mul(P - P / i, inv[P % i]), ifac[i] = mul(ifac[i - 1], inv
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for (R int mid = 1; mid < lim; mid <<= 1) for (R int j = 0; j < lim; j += (mid << 1))</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                   inline int add(R int x, R int y) { return 011 + x + y >= P ? 011 + x + y - P : x + y; } inline int dec(R int x, R int y) { return x-y<0? x-y+P : x-y; } inline int mul(R int x, R int y) { return 111 * x * y - 111 * x * y / P * P; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               #define fd(i, a, b) for (R int i = (a), I = (b)-1; i > I; —i) #define go(u) for (int i = head[u], v = e[i].v; i; i = e[i].n, v = e[i].v)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       A[j + k + mid] = A[j + k] - (t = w[ty][mid + k] * A[j + k + mid]);

A[j + k] = A[j + k] + t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             inline cp operator*(const double &b) const { return cp(x * b, y * b); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for (; y; y >>= 1, x = mul(x, x)) (y & 1) ? res = mul(res, x) : 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (R int i = 1, d = 0; i < 131072; i <<= 1, ++d) rep(k, 0, i - :
w[1][i + k] = cp(cos(Pi * k * iv[d]), sin(Pi * k * iv[d]));
w[0][i + k] = cp(cos(Pi * k * iv[d]), -sin(Pi * k * iv[d]));</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  inline cp(R \text{ double } xx = 0, R \text{ double } yy = 0) : x(xx), y(yy) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(i, 0, lim - 1) if (i < r[d][i]) swap(A[i], A[r[d][i]]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    inline cp operator~() const { return cp(x, -y); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int r[21][N], ifac[N], lg[N], inv[N]; double iv[21];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   = ifac[0] = ifac[1] = 1;
                                printf("%llu\n", solve_fast(n));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    const double Pi = acos(-1.0)
                                                                                                                                                                                                                                                                                                                                                                                              const int N = (1 << 17) + 5;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int ksm(R int x, R int y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(k, 0, mid - 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void FFT(cp *A, int ty) {
                                                                                                                                                                                     大阶乘取模
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(d, 1, 17) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   inv[0] = inv[1]
                                                                                                                                                                                                                                                                              #define R register
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   R int res = 1;
int n; cin>>n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           double \times, y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           iv[0] = 1;
                                                                             return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void Pre() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           struct cp {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int lim, d;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          w[2][N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ......
                                                                                                                                                                                          11.16
```

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int n,n_x, lab[M], match[M], slack[M], st[M], pa[M], flower_from[M][N+1], S[M], vis[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for(int \ u=1; u<=n; ++u) \ if(g[u][x].w>0&&st[u]!=x&&S[st[u]]==0) \ update\_slack(u,x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(x>n) for(size_t i=0;i<flower[x].size();++i) set_st(flower[x][i],b);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inline int get_pr(int b,int xr){
    int pr=find(flower[b].begin(),flower[b].end(),xr)—flower[b].begin();
    if(pr%2==1){ // 检查他在前一层图是奇点还是偶点
                                                                                                                                                                                                                                                                                                                                                    rotate(flower[u].begin(),flower[u].begin()+pr,flower[u].end());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             else for(size_t i=0;i<flower[x].size();i++)q_push(flower[x][i]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for(int i=0;i<pr: ++i)set_match(flower[u][i], flower[u][i^1]);</pre>
                                                                                                                                                                                                                                         E g[M][M]; vi flower[M]; queue<int> q;
inline int e_delta(const E &e){ // does not work inside blossoms
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        reverse(flower[b].begin()+1,flower[b].end());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int xr=flower_from[u][e.u],pr=get_pr(u,xr);
                                                                                                                                                                                                                                                                                              return lab[e.u]+lab[e.v]—g[e.u][e.v].w*2;
                                                                                                                                                              E(int u, int v, int w):u(u), v(v), w(w){}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return (int)flower[b].size()—pr;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   inline void set_match(int u,int v){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     inline void augment(int u,int v){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 inline void set_st(int x,int b){
                                                                                                                                                                                                                                                                                                                                                                                                                              inline void set_slack(int x){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for(;;){
  int xnv=st[match[u]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(x \le n) q.push(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            match[u]=g[u][v].v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              set_match(xr,v)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      set_match(u,v);
#define INF INT_MAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void q_push(int x){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                }else return pr;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            E e=g[u][v];
                                                         #define M N*2+1
                                                                                                                                                                                                                                                                                                                                                                                                                                                               slack[x]=0;
                              #define N 600
                                                                                                           int u, v, w;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(u>n){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  st[x]=b;
                                                                                  struct E{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      P);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 1, p) a[p] = mul(a[p], (111 * b1 * p + i) %
                                                                                                                                                                                                                                                                                                                                                                             int res = ksm(GetFac(P - 1 - n), P - 2);
                                                                                                                                                                                                                                                                                                                                                  rep(i, 0, p) a[i] = mul(a[i], b[i]);
                                                                                                                                                                                                                calc(a, b, p, p + 1);
rep(i, 0, p) a[p + i + 1] = b[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int res = 1;
rep(i, 0, bl - 1) res = mul(res, a[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(i, s * s + 1, n) res = mul(res, i);
                                                                                                                                                                                                                                                                                              calc(a, b, p << 1, mul(p, qwq));
                                                                            for (int p = b1; p; p >>= 1) ++S;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            scanf("%d%d", &n, &P), Pre();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int s = sqrt(n), res = solve(s);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return n & 1? res : P - res;
                                                                                                                                                            for (int p = 0; s >= 0; —s) {
                            static int a[N], b[N], c[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           printf("%d\n", Fac(n))
                                                                                                                                    int qwq = ksm(b1, P - 2);
                                                                                                                                                                                                                                                                      a[p \ll 1 \mid 1] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (n >= P) return 0;
if (n > P - 1 - n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return GetFac(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int GetFac(int n) {
    int solve(int bl) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          scanf("%d", &T);
                                                                                                         a[0] = 1, -s;
                                                                                                                                                                                                                                                                                                                             p <<= 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int Fac(int n) {
                                                                                                                                                                                           if (p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     while (T—)
                                                         int s = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int T;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int n;
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set_match(xnv,st[pa[xnv]]);

if(!xnv)return;

u=st[pa[xnv]],v=xnv;

inline int get_lca(int u, int v){

```
\textbf{for(int} \ x=1; x<=n\_x; ++x) \ \textbf{if}(st[x]==x\&slack[x]\&st[slack[x]]!=x\&e\_delta(g[slack[x]]) = x\&e\_delta(g[slack[x]]) 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for(int b=n+1; b<=n_x; ++b) if(st[b]==b&&S[b]==1&&lab[b]==0) expand_blossom(b);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for(int x=1;x<=n_x;++x) if(st[x]==x&\&!match[x]) pa[x]=0,S[x]=0,q_push(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for(int b=n+1;b<=n_x;++b)    if(st[b]==b&&S[b]==1)    d=min(d,lab[b]/2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       else if(S[x]==0)d=min(d,e_delta(g[slack[x]][x])/2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(S[x]==-1)d=min(d,e_delta(g[slack[x]][x])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for(int x=1;x\leq n_x;++x) if(st[x]==x&&slack[x])
                                                                                                                                                                                                                                                                                             if(!lca)return augment(u,v), augment(v,u), true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(on_found_E(g[slack[x]][x]))return true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(on_found_E(g[u][v]))return true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for(int b=n+1;b<=n_x;++b) if(st[b]==b){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            inline pair<long long, int> weight_blossom(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      else_if(S[st[b]]==1)lab[b]-=d*2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            } else update_slack(u,st[v])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   |else if(S[st[u]]==1)lab[u]+=d;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     memset(slack+1,0,sizeof(int)*n_x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(S[st[b]]==0)lab[b]+=d*2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           memset(match+1,0,sizeof(int)*n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(e_delta(g[u][v])==0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(lab[u]<=d)return 0;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       memset(S+1, -1, sizeof(int)*n_x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int u=q.front();q.pop();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(S[st[u]]==1)continue
                                                                                                                                                                                                                                                                                                                                                       else add_blossom(u,lca,v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(q.empty())return false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for(int u=1;u<=n;++u){
                                                         slack[v]=slack[nu]=0;
                                                                                                                                                                                                                                       int lca=get_lca(u,v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    long long tot_weight=0;
int nu=st[match[v]]
                                                                                                                        S[nu]=0, d_push(nu);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(S[st[u]]==0){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             inline bool matching(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         while(q.size()){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          q=queue<int>();
                                                                                                                                                                         }else if(S[v]==0){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int n matches=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    d=dnene<int>();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ]][x])==0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int d=INF;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for(int x=u,y;x!=lca;x=st[pa[y]]) flower[b].pb(x), flower[b].pb(y=st[match[x]]),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        for(int x=v,y;x!=lca;x=st[pa[y]]) flower[b].pb(x), flower[b].pb(y=st[match[x]]),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for(int x=1;x<=n_x;++x) if(g[b][x].w==0||e_delta(g[xs][x])<e_delta(g[b][x]]))
g[b][x]=g[xs][x], g[x][b]=g[x][xs];
for(int x=1;x<=n;++x) if(flower_from[xs][x]) flower_from[b][x]=xs;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for(size_t i=0;i<flower[b] size();++i) set_st(flower[b][i],flower[b][i]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int xr=flower_from[b][g[b][pa[b]].u],pr=get_pr(b,xr);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   reverse(flower[b].begin()+1,flower[b].end());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for(int x=1; x<=n_x; ++x)g[b][x].w=g[x][b].w=0,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        inline void expand_blossom(int b){ // S/b} == 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 inline void add_blossom(int u, int lca, int v){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        for(size_t i=pr+1;i<flower[b].size();++i){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int xs=flower[b][i], xns=flower[b][i+1],
                                                                                                                                                                                                                          vis[u]=t; // 这种方法可以不用清空 v 数组
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for(int x=1;x<=n;++x)flower_from[b][x]=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      For(size_t i=0;i<flower[b].size();++i){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  inline bool on_found_E(const E &e){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         slack[xs]=0, set_slack(xns);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   S[xs]=-1,set_slack(xs);
                                                                                                                                                                    if(vis[u]==t)return u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int u=st[e.u], v=st[e.v];
                                                         for(++t;u||v;swap(u,v)){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 while(b<=n_x&&st[b])++b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int xs=flower[b][i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 pa[xs]=g[xns][xs].u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int xs=flower[b][i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 For(int i=0;i<pr;i+=2){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              S[xr]=1, pa[xr]=pa[b];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              match[b]=match[lca];
                                                                                                                        if(u==0)continue;
                                                                                                                                                                                                                                                                                                                                                       if(u)u=st[pa[u]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               S[xs]=1, S[xns]=0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    pa[v]=e.u,S[v]=1;
                                                                                                                                                                                                                                                                                    u=st[match[u]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    flower[b].clear()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  flower[b].pb(lca)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         lab[b]=0,S[b]=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               (sux)ysnd_p
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(b>n_x)++n_x;
    static int t=0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        set_slack(b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(S[v]=-1){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 set_st(b,b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int b=n+1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           d_push(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  d_push(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  st[b]=0;
```

using pli = pair<ull, uint>;

namespace prime {

强连通子图计数

11.18

```
for (int x = (i - 1) \& i; x > 0; x = (x - 1) \& i) {
   if (x & u) g[i] = sub(g[i], mul(f[x], g[i ^ x]));
                                                                                                                                                                                                                                                                                          for (int x = i; x > 0; x = (x - 1) & i) { f[i] = sub(f[i], mul(g[x], p[cal(i ^ x, i)]));
                                                                                      2);
                                                                           rep(i, 1, m+1) p[i] = mul(p[i-1], rep(i, 1, S+1) 
                         rep(i, 1, S+1) cnt[i] = get(i);
p[0] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               using ull = unsigned long long;
                                                                                                                                                                                                                                                                                                                                                                                     g[i] = add(g[i], f[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 using uint128 = __uint128_t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        using uint = unsigned int;
                                                                                                                                                                                                                                                              f[i] = p[cal(i, i)];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           快速 Rho
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            using 11 = 1ong 1ong;
                                                                                                                                               u = i \& (-i);
                                                                                                                                                                                                                                                                                                                                                                                                                                           cout << f[S];
  S = pw(n)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  11.19
                                                                                                                                                                                                                                 for(int u=1;u<=n;++u) if(match[u]&&match[u]<u) tot_weight+=g[u][match[u]].w;</pre>
                                                                                                                                                                                                                                                                                                                         inline void init_weight_graph(){
  for(int u=1;u<=n;++u) for(int v=1;v<=n;++v) g[u][v]=E(u,v,0);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      printf("%lld\n",weight_blossom().first);
for(int u=1;u<=n;++u)printf("%d ",match[u]);puts("");</pre>
for(int u=0;u<=n;++u)st[u]=u,flower[u].clear();</pre>
                                                        for(int u=1;u<=n;++u) for(int v=1;v<=n;++v){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int u, v, w; scanf("%d%d%d", &u, &v, &w);
                                                                                                                                                                            for(int u=1;u<=n;++u)lab[u]=w_max;
                                                                                                                                                                                                                                                                 return mp(tot_weight,n_matches);
                                                                                    flower_from[u][v]=(u==v?u:0);
                                                                                                                 w_max=max(w_max,g[u][v].w);
                                                                                                                                                                                                            while(matching())++n_matches;
                                                                                                                                                                                                                                                                                                                                                                                                                                           int m; scanf("%d%d", &n, &m);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  g[u][v] .w=w. [u][v] .w=w;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for(int i=0;i<m;++i){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           init_weight_graph();
                               int w_max=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                  int main(){
```

```
Mod operator += (const Mod& rhs) { if ((x += rhs.x) >= mod) \dot{x} -= mod; return *this
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Mod operator -= (const Mod& rhs) { if (sT(x -= rhs.x) < 0) \times += mod; return *this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        Mod operator *= (const Mod& rhs) { x = reduce(dT(x) * rhs.x); return *this; }
                                                                                                                                             T \gcd(T \ a, \ T \ b) \ \{ \ while \ (b) \ \{ \ T \ t = a \ \% \ b; \ a = b; \ b = t; \ \} \ return \ a; \ \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Mod operator + (const Mod &rhs) const { return Mod(*this) += rhs; }
Mod onerator - (const Mod &rhs) const { return Mod(*this) -= rhs; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Mod operator — (const Mod &rhs) const { return Mod(*this) == rhs; Mod operator * (const Mod &rhs) const { return Mod(*this) *= rhs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     bool operator == (const Mod& rhs) const { return x == rhs.x; \} bool operator != (const Mod& rhs) const { return x := rhs.x; \}
                                                                       inline uint ctz(ull x) { return __builtin_ctzll(x); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Mod operator - () const \{ return Mod() - *this; \}
                                   inline uint isqrt(ull x) { return sqrtl(x); }
inline ull sqr(ull x) { return x * x; }
                                                                                                                                                                                                                                                                                          static T mod, inv, r2;
static const int wb = sizeof(T) * 8;
                                                                                                                                                                                                                     template <class T, class dT, class sT>
                                                                                                                                                                                                                                                                                                                                                                                                                                 Mod(T_x): x(init(x))  {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      Mod pow(ull e) const {
                                                                                                                                                                                                                                                                                                                                                                                                {} (0)x :()pow
                                                                                                           template <class
                                                                                                                                                                                                                                                           struct Mod {
                                                                     然后把枚举出度为零的点集容斥改为枚举缩点后出度为零的点集容斥
                                                                                                                                    int n, cnt[N], S, g[N], f[N], u, v, a[N], m, p[300];
int get(int x) {
                                                                     // 首先要会 n 点 m 边 DAG 计数,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              a[pw(u-1)] |= pw(v-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  res += cnt[a[t] & y];
                                 // n 点 m 边强连通子图计数
                                                                                                         const int N = 1 << 15;
                                                                                                                                                                                                                                                                                                                                x = (x - 1) \& x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int cal(int x, int y)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 1, m+1) {
cin >> u >> v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              t = x \& (-x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int res = 0, t;
while (x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       cin >> n >> m;
                                                                                                                                                                                                                       int res = 0;
                                                                                                                                                                                                                                                      while (x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return res;
                                                                                                                                                                                                                                                                                                                                                                                                      return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         \times \wedge= t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int main() {
```

a,

Mod r(1); for (Mod a = *this; e; e >>= 1, a *= a) if (e & 1) r *=

return r;

```
\widehat{\times}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (g == 1) continue;
if (g == n) for (g = 1, y = sy; g == 1; ) <math>y = y * y + mc, g = gcd(n, (y == n))
                                                            if (n < (1u << 31)) return !composite uint, Mod32>(n, bases[x], y);
                                                                                                                                                                                                                         ExactDiv(ull n) : n(n), i(Mod64::mul_inv(n)), t(ull(-1) / n) {}
friend ull operator / (ull n, ExactDiv d) { return n * d.i; };
bool divide(ull n) { return n / *this <= t; }</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 .;
o
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        For (int i = 0; i < (int)min(s, l - k); ++i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (n < (1u << 31)) return brent<uint, Mod32>(n, c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (uint i = 2; i \le sqrt_n; ++i) if (is_prime[i])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for (uint j = i * i; j <= n; j += i) is_prime[j]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for (int i = 0; i < (int)1; ++i) y = y * y + mc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          template <class T, class mod>
T brent(T n, T c) { // n must be composite and odd.
const ull s = 256;
                                                                                             return !composite<ull, Mod64>(n, bases[x], y);
                              else if (n < 3770579582154547) \times = y = 5;
else if (n < 47636622961201) \times = y = 4;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for (int k = 0; k < (int)1; k += s)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (i != 2) primes.pb(ExactDiv(i));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                const mod one = mod(1), mc = mod(c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           vector<bool> is_prime(n + 1, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for (ull 1 = 1; ; 1 <<= 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return brent<ull, Mod64>(n,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           assert(n < (1ull << 63));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              y = y * y + mc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              T g = gcd(n, p.x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            vector<pli>factors(ull n)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ull brent(ull n, ull c) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (n <= 1) return {};</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                               uint sqrt_n = sqrt(n);
                                                                                                                                                                                                                                                                                                                                                                                             vector<ExactDiv> primes;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               auto sy = y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             mod::set_mod(n);
                                                                                                                                                                                                                                                                                                                                                                                                                              void init(uint n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               vector<pli>ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                "wod b = one:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            primes.clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return g;
                                                                                                                                                            struct ExactDiv {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   auto x = y;
                                                                                                                                                                                                ExactDiv() {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 mod y = one;
                                                                                                                                                                                                                                                                                                                                   ull n, i, t;
                                                                                           static void set_mod(T m) { mod = m, inv = mul_inv(mod), r2 = -dT(mod) % mod;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            bool is_prime(ull n) { // reference: http://miller-rabin.appspot.com
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for (j = s - 1; j > 0; --j) { if ((a *= a) == fone) break;
                                                                                                                                                          T y = T(x >> wb) - T((dT(T(x) * inv) * mod) >> wb)
                                                                                                                                                                                                                                                            static T mul_inv(T n, int e = 6, T x = 1) {
    return !e ? x : mul_inv(n, e - 1, x * (2 - x * n));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          [2, 2570940, 211991001, 3749873356u],[2, 2570940, 880937, 610386380, 4130785767u],[2, 325, 9375, 28178, 450775, 9780504, 1795265022]
                                                                 static T init(T w) { return reduce(dT(w) * r2); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                bool composite(T n, const uint* bases, int m)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (a == one || a == fone) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         else if (n < 4759123141) \times = 2, y = 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          else if (n < 154639673381) \times = y = 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           else if (n < 19471033) \times = 1, y = 2;
  get() const { return reduce(x); ]
                                                                                                                                                                                             return ST(y) < 0 ? y + mod : y;
                              static T modulus() { return mod; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for (int i = 0, j; i < m; ++i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                 using Mod64 = Mod<ull, uint128, ll>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           static const uint bases[][7] = {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           mod a = mod(bases[i]).pow(d);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         {2, 3},
{2, 299417},
{2, 7, 61},
{15, 176006322, 4221622697u},
                                                                                                                                                                                                                                                                                                                                                                                                                                                               using Mod32 = Mod<uint, ull, int>;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int s = \_builtin\_ctzll(n - 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (n < 1373653) \times = 0, y = 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           template <> uint Mod32::mod = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               template <> uint Mod32::inv = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            template <> ull Mod64::inv = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          };
if (n <= 1) return 0;
if (!(n & 1)) return n == 2;
if (n <= 8) return 1;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                template \Rightarrow ull Mod64::mod = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  template \Rightarrow uint Mod32::r2 = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          template <> ull Mod64::r2 = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               template <class T, class mod>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          assert(n < (ull(1) << 63))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           mod one(1), fone(n-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (j == 0) return 1;
                                                                                                                                static T reduce(dT \times) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             T d = (n - 1) >> s;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                mod :: set_mod(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int x = 6, y = 7;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return 0;
```

```
for (int s = 0, u = sum; s <= k - r; ++s, u = mul(u, 1)) add(cur, mul(u, cof
                                                                                                                                                                                                                                                                                                                                                                                       int v = mul(c[s][i], u);
rep(r, 0, k-s+1) add(cof[r + 0 * i][s - i], mul(v, tmp[r][s]));
                         rep(j, 1, i+1) C[i][j] = (C[i-1][j] + C[i-1][j-1]) % P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(s, 0, k-r) add(cof[s][r + 1 - i], mul(u, tmp[r][s]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          b / c); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int cur = 0, x = reduce(a, c), y = (reduce(b, c) + P) % P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(r, 0, k-s+1) add(tmp[r][s - i], mul(u, cof[r][s]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for (int i = 1, u = n; i <= r + 1; ++i, u = mul(u, n))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              add(sum, mul(u, mul(C[r + 1][i], B[r + 1 - i]));
                                                                                                                                                                                                                                                                                                 rep(i, 0, k) memcpy(tmp[i]+1, cof[i]+1, 4 * (k-i)); for (int i = 1, u = x; i <= k; ++i, u = mul(u, x))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (k1 == 0) { res = 1; rep(i, 0, k2) res = mul(res, rep(i, 0, k) memset(cof[i]+1, 0, 4 * (k - i));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int u = mul(C[r+1][i], mul(B[i], inv[r+1]));
                                                                                                                                               rep(j, 0, i) add(sum, mul(C[i + 1][j], B[j]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i, 0, k) memset(cof[i]+1, 0, 4*(k-i));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int run(int n, int a, int b, int c, int k1, int k2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, k) memset(tmp[i], 0, 4 * (k-i));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(s, 1, k+1) rep(i, 1, s+1) {
   int u = mul(C[s][i], i & 1 ? 1 : P - 1);
                                                                                                                                                                           B[i] = (1 + mul(P - sum, inv[i + 1])) \% P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            sum = mul(sum, inv[r + 1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int 1 = ((11)a * n + b) / c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(r, 0, k) rep(i, 0, r+1)
                                                                                                                                                                                                                                                                     inline void calc(int x, bool o) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          = -b - 1; sign = P - sign;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         add(res, mul(sign, cur));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         calc(x, 1); calc(y, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              k = k1 + k2;

int res = 0, sign = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            = 1; swap(a, c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    cof[r][0] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(r, 0, k+1) {
                                                                                                                                                                                                                                                                                                                                                                rep(s, i, k+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int sum = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (!a) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               cof[k1][k2] = 1;
                                                                                                                   int sum = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        [r][s]);
C[i][0] = 1;
                                                                                     rep(i, 0, K+1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                while (1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return res
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         //\sum_{X} = 0} ^ {n} × ^ {k_1} {\left \lfloor \frac{2x}{2x} + b}{c} \rlight \rfloor} ^ {k_2}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  inv[1] = 1; rep(i, 2, K+2) inv[i] = mul(P - P / i, inv[P % i]); rep(i, 0, K+2) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            }
if (n > 1) ret.emplace_back(n, 1);
if (ret.size() - s >= 2) sort(ret.begin() + s, ret.end());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    inline void add(int &a, int b) { if ((a += b) >= P) a -= P;
inline int mul(int a, int b) { return 111 * a * b % P; }
int reduce(int &a, int b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int inv[K + 2], C[K + 2][K + 2], B[K + 1]; // \check{U}_{\text{DDDD}}^{2}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   static const int K = 10, P = 998244353; // e1+e2 <= K
  2;
  ||
||
||
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int cof[K + 1][K + 1], tmp[K + 1][K + 1], k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (p.divide(n)) {
    uint e = 1; n = n / p;
    while (p.divide(n)) n = n / p, e++;
ull v2 = sqrtl(n), v3 = cbrtl(n), v = v2,
                       if (v2 * v2 == n || v3 * v3 * v3 == n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   uint e = 1; n /= p;
while (n % p == 0) n /= p, e += 1;
                                                     if (v2 * v2 != n) v = v3, b = 3;
                                                                                                                   for (auto &&e: ret) e.se *= b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (!is_prime(p)) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 while (n > lim && !is_prime(n))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if ((a \%= b) < 0) a += b, —res;
                                                                                                                                                                                                                                                                                                                                                             ull lim = sqr(primes.back().n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ret.emplace_back(p.n, e);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ret.emplace_back(p, e);
                                                                                                                                                                                                                                                                                                                                                                                                                            if (sqr(p.n) > n) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for (ull c = 1; ; ++c) {
                                                                                                                                                                                                                                                                          ret.emplace_back(2, e);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ull p = brent(n, c);
                                                                                                                                                                                                                                                                                                                                                                                            for (auto &&p: primes)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   扩展类欧几里得
                                                                                     ret = factors(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      uint s = ret.size();
                                                                                                                                                                                                                                          uint e = ctz(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int res = a / b;
                                                                                                                                                                                  }
if (!(n & 1)) {
                                                                                                                                                    return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  break;
                                                                                                                                                                                                                                                                                                        n >>= e;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void init() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         namespace _lo {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        11.20
```

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for(int \_ = mi == 1? j + 1: j - 2; ; mi == 1? ++\_: —_) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              hm[0].upd(x | (1 << t[j-1]) | (2 << t[j]), y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       hm[o].upd(x, y); \\ hm[o].upd(x \wedge (k << t[j-1]) \wedge (k << t[j]), y); \\
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  else if(p == 2 && q == 1 || p == q && p >= 3) {
                                                                                                                                                                                                for(int i = hd[p]; \sim i; i = ne[i]) if(u == s[i]) {
                                                                                                                                                                                                                                                                                                                                                                                                 s[L] = u; f[L] = v; ne[L] = hd[p]; hd[p] = L++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int x = hm[o \wedge 1].s[k], y = hm[o \wedge 1].f[k] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(x >> t[m + 1] || y <= 0) continue;
int p = x >> t[j - 1] & 7, q = x >> t[j] & 7;
int tx = x ^ (p << t[j - 1]) ^ (q << t[j]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         hm[o].upd(nx^{\wedge} ((3^{\wedge} p ^{\wedge} q) << t[\_]), y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(hm[0].s[k] >> t[m]) hm[0].f[k] = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int mi = min(p, q), now = 1, nx = tx;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int o = \vec{0}; hm[o].init(); hm[o].upd(\theta, \theta);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              \label{eq:hm[o] upd(x | (kk << t[j-1]), y);} $$ $$ hm[o].upd(x | (kk << t[j]), y); $$
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(!p \&\& !q) hm[o].upd(x, y-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   else if(p == 1 && q == 2) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          else if(min(p, q) <= 2) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(c == (mi \land 3)) \longrightarrow now
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int c = x >> t[\_] & 7;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(k, 0, hm[o \land 1].L) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          } else if(a[i][j] == 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  else hm[o].s[k] <<= 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(c == mi) ++now;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        hm[o].upd(x, y - 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(j, 1, m + 1) {
 o ^= 1; hm[o].init();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   else if(!p || !q) {
                                                                                            void upd(int u, int v) {
                                                                                                                                                                                                                                                  f[i] = min(f[i], v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int kk = a[i][j] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int k = max(p, q);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 1, n + 1) { rep(k, 0, hm[o].L) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        hm[o].upd(tx, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(a[i][j] == 1) {
                                                                                                                                                  int p = u \& INF;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(!p && !q)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(!now)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(!p && !q)
                                                                                                                                                                                                                                                                                                            return ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int solve() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    } else {
   L = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     }hm[2];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      世
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                res.g=add(res.g,add(111*(x<<1)*res.h%P,add(111*(y<<1)*res.f%P,add(111*ss(n)*pow(
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          S5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  * 给定 9 * 9 的棋盘,格子四联通,有两类格子, 1 不能走 0 可以走。要求从 S1 走到 11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      res.g=dec(dec(dll*n*M%P*(M+1)%P,res.f),mul(h,2)),mul(f,2));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     inline int s(R int x){return 111*x*(x+1)%P*inv2%P;}
inline int ss(R int x){return 111*x*(x+1)%P*((x<<1)+1)%P*inv6%P;}</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              x)%P, add(111*n*(n+1)%P*x%P*y%P, 111*(n+1)*pow(y)%P))));
                                      // g = \sl / 2 | \lambda \frac{ai+b}{c} \cdot \frac{ai+b}{c} \frac{ai+b}
                                                                                                                                                                                                                                                                                             inline int add(R int x,R int y){return x+y>=P?x+y-P:x+y;}
inline int dec(R int x,R int y){return x-y<0?x-y+P:x-y;}
inline int mul(R int x,R int y){return 111*x*y-111*x*y/P*P;}</pre>
res.h=add(res.h,add(111*ss(n)*x%P,111*s(n)*\sqrt{8}P));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   res.f=add(res.f,add(111*s(n)*x%P,111*(n+1)*y%P));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        res.h=111*inv2*dec(dec(111*M*n%P*(n+1)%P,g),f)%P,
                                                                                                                                                                                                                                                      const int P=998244353, inv2=499122177, inv6=166374059;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for(;y;y>>=1,x=mul(x,x))if(y&1)res=mul(res,x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      static const int INF = pw(18) - 1, N = 8e5;
                                                                                                                                                                                                                                                                                                                                                                                                                                               inline int pow(R int x){return ill*x*x%P;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int hd[INF + 1], ne[N], s[N], L, f[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void get(int a,int b,int c,int n){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           res.g=111*pow(y)*(n+1)%P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int h=res.h, g=res.g, f=res.f;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         到 72, 且路径不相交, 求最短路径*/
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            res.f=dec(111*n*M%P,res.f);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             两通路
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    memset(hd, -1, sizeof(hd))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         res.f=111*y*(n+1)%P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int n, m, a[22][22], t[22];
struct HM {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        struct node{int f, g, h;}res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 res.h=111*y*s(n)%P
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int ksm(R int x,R int y){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      get(a%c,b%c,c,n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int M=(111*a*n+b)/c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           get(c, c-b-1, a, M-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         插头 db
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int x=a/c, y=b/c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(a>=c||b>=c){
                                                                                                                                                                                                        #define R register
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            R int res=1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void init() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    11.21
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\label{eq:hm[o].upd(x, y);} $$ hm[o].upd(x \wedge ((p \mid q) << t[j-1]) \wedge ((p \mid q) << t[j]), y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for(int _ = p == 1 ? j + 1 : j - 2; ; p == 1 ? ++_ : --_) int c = x >> t[_] & 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       \label{eq:hm[o].upd(x | (1 << t[j - 1]) | (2 << t[j]), y);} \textbf{if}(s[i][j] == '*') \ \mbox{hm[o].upd(x, y);}
                         s[L] = u; f[L] = v; ne[L] = hd[p]; hd[p] = L++;
                                                                                                                                                                                                                                                                                                                                      rep(i, 1, n + 1) rep(j, 1, m + 1) ok[i][j] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int p = x >> t[j - 1] & 3, q = x >> t[j] & 3;
int tx = x ^ (p << t[j - 1]) ^ (q << t[j]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(j, 0, hm[o].L) hm[o].s[j] \ll t[1]; rep(j, 1, m + 1) {
                                                                                                                                                                                                                                                                                                                                                                                                             int o = 0; hm[o].init(); hm[o].upd(0, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        hm[o].upd(nx \land (3 << t[\_]), y);
                                                                                                                             per(i, 1, n + 1) per(j, 1, m + 1) {
                                                                                                                                                                                                                                                                                                          rep(i, 1, n + 1) cin >> (s[i] + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(ok[i][j] \& itx) ans += y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           } else if(p == 2 && q == 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            else if(p == 1 && q == 2) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(!p && !q) hm[o].upd(x, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        c == p ? ++now : --now;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int x = hm[0 ^ 1].s[k];
if(x >> t[m + 1]) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(k, 0, hm[o \land 1].L) {
                                                                                                                                                   ok[i][j] = 1;
if(s[i][j] == '0') return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         else if(p == q) {
int now = 0, nx = tx;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 o ^= 1; hm[o].init();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           } else if(!p || !q) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            11 y = hm[o \land 1].f[k];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(!c) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       hm[o].upd(tx, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(now == -1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(s[i][j] == 'X')
                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 1, n+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(!p && !q) {
                                                                                                                                                                                                                                                                                      cin >> n >> m;
                                                                                                                                                                                                                                                                                                                                                                                       11 ans = 0;
                                                                                                                                                                                                                                                          11 solve() {
                                                                                                   void gao() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      } else {
                                                                                                                                                                                                                                                                                                                                                                gao();
                                                                           }hm[2];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  * 给定 12 * 12 的棋盘,格子四联通,有三类格子, X 不能走 O 必走 * 可走可不走。画一条回路,求方
                                                                                                                                                       -2;; ma == 1? ++_{-}: --_{-})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 0, hm[o].L) if(!hm[o].s[i]) ans = hm[o].f[i] - 2;
                                                                                                                                                                                                                                                                                  hm[o].upd(nx \wedge ((3 \wedge ma \wedge kk) << t[\_]), y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int p = u & INF; for(int i = hd[p]; \simi; i = ne[i]) if(u == s[i]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 1, n+1) rep(j, 1, m+1) cin >> a[i][j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    static const int INF = pw(18) - 1, N = 8e5;
int hd[INF + 1], ne[N], s[N], L; ll f[N];
                                                                                                                                                     for(int _{-} = ma == 1 ? j + 1 : j
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int n, m, edx, edy, t[22], ok[22][22];
                                                                                                                                                                                                                                  if(c == (ma \land 3)) \longrightarrow now;
                                                                                                                                                                               int c = x >> t[_] & 7;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int main() {
  rep(i, 0, 22) t[i] = i + i + i;
  while(cin >> n >> m) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 memset(hd, -1, sizeof(hd));
                                                                                                                                                                                                        if(c == ma) ++now;
                                                                                                                               int now = 1, nx = tx;
                                                                         hm[o].upd(tx, y);
} else if(ma <= 2) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   cout << solve() << endl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               回路
                     int ma = max(p, q);
else if(!p || !q) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void upd(int u, 11 v) {
                                                                                                                                                                                                                                                            if(!now) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(!n && !m) break;
                                               if(ma == kk) {
                                                                                                                                                                                                                                                                                                                break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             插头 db
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        f[i] += v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void init() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  char s[22][22];
struct HM {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 11.22
```

```
hm[o] . upd(x \land ((p | q) << t[j-1]) \land ((p | q) << t[j]), y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                - 2; ; p == 1 ? ++_ : --_) {
                                                                                                                        int o = 0; hm[o].init(); hm[o].upd(sta[s] << t[1], 1);</pre>
                                                                                                                                                                                                                                                                      int p = x >> t[j - 1] & 3, q = x >> t[j] & 3;
int tx = x \wedge p << t[j - 1] \wedge q << t[j];
                                                                                                                                                                                                                                                                                                                    int x = hm[o \land 1].s[k], y = hm[o \land 1].f[k];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(_, 0, hm[o].L) if(!(hm[o].s[_] >> t[n])) {
    int i = id[hm[o].s[_]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                A.a[i][s] = add(A.a[i][s], hm[o].f[\_]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 0, pw(n << 1)) if(check(i)) {
   id[i] = sz(sta);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         hm[o].upd(nx \land (3 << t[\_]), y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int solve() {
   if((n & 1) && !(m & 1)) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for(int _ = p == 1 ? j + 1 : j
int c = x >> t[_] & 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       } else if(p == 2 && q == 1)
                                                                                                                                                                                                                                                if(x >> t[n + 1]) continue;
                                                                                                                                              rep(j, 1, n + 1) {
    o ^= 1; hm[o].init();
    rep(k, 0, hm[o ^ 1].L) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            c == p ? ++now : --now;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 0, n) {
    int c = x >> t[i] & 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                } else if(p == q) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int now = 0, nx = tx;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(now < 0) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(c == 3) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(c == 1) ++now;
if(c == 2) --now;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(!c) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(now == -1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  hm[o].upd(tx, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       bool check(int \times) {
                                                                                                                                                                                                                                                                                                                                                                                                hm[o].upd(x, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return now == 0;
                                                                                             void gao(int s) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int now = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 sta.clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    oreak;
b >>= 1;
                                                   return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, 0, k) rep(j, 0, k) rep(t, 0, k) r.a[i][j] += a[i][t] * c.a[t][j];
rep(i, 0, k) rep(j, 0, k) r.a[i][j] %= P;
                                                                                                                                            rep(i, 1, T + 1) cout << "Case " << i << ": " << solve() << endl;
                                                                                                                                                                                                                                                                                                                            * 给定 7 * 169 的棋盘,格子四联通,每个格子必走。求左上走到左下的方案数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   Mat() { rep(i, 0, k) rep(j, 0, k) a[i][i] = 0; }
void reset() { rep(i, 0, k) rep(j, 0, k) a[i][i] = 0; }
void set() { rep(i, 0, k) a[i][i] = 1; }
inline Mat operator * (const Mat &c) const {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            inline int mul(int a, int b) { return 111 * a * b % P; }
                                                                                                                                                                                                                                                                                                                                                                           const int P = 7777777, N = 150;
int n, m, id[20202], t[22], k, dp[2][N]; vi sta;
inline int add(int a, int b) {
                                                                                                                                                                                                                                              矩阵加速通路
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      s[L] = u, f[L] = v; hd[u] = L++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              inline void upd(int u, int v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 0, L) hd[s[i]] = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          static const int N = pw(16);
                                                                    int main() {
    rep(i, 0, 22) t[i] = i + i;
    int T; cin >> T;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int hd[N], s[N], L, f[N];
inline void init() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                        if((a += b) >= P) a -= P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       f[i] = add(f[i], v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(b & 1) r = r * a;
a = a * a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Mat kpow(Mat a, int b)
                                                                                                                                                                                                                                              插头 db
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int i = hd[u];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Mat r; r.set();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(~hd[u])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return r;
                        return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              11 a[N][N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     while(b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          struct Mat {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       struct HM {
                                                                                                                                                                         return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 L = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        Mat r;
                                                                                                                                                                                                                                                11.23
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 }hm[2];
```

```
- 2; ; k == 1 ? ++_ : --_) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for(int _ = k == 1 ? j + 1 : j - 2; ; k == 1 ? ++_ int c = x >> t[_] & 3;
int x = hm[o \land 1].s[k], y = hm[o \land 1].f[k] + a[i][j];
                                                                                                                                                                                                                   hm[o].upd(x | (1 << t[j - 1]) | (2 << t[j]), y);
hm[o].upd(x | (3 << t[j - 1]), y);
hm[o].upd(x | (3 << t[j]), y);
hm[o].upd(x, y = a[i][j]);
                                                                                                                                                                                                                                                                                                                                                                                                               hm[o].upd(x \wedge (k << t[j-1]) \wedge (k << t[j]), \; y);
                                                    int p = x >> t[j - 1] & 3, q = x >> t[j] & 3;
int tx = x ^ (p << t[j - 1]) ^ (q << t[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           hm[o].upd(nx^ ((3 ^ p ^ q) << t[_]), y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            hm[o].upd(nx \wedge (k << t[\_]), y),
                                                                                                                                     if(!p \&\& !q) hm[o].upd(x, y - a[i][j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               else if(min(p, q) <= 2) {
  int k = min(p, q), now = 1, nx = tx;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for(int \_ = k == 1 ? j + 1 : j
int c = x >> t[\_] & 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(!tx) ans = max(ans, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(c == (k \land 3)) --now;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 } else if(p == 1 && q == 2) {
} else if(p == 2 && q == 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(!tx) ans = max(ans, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(c == (k \land 3)) —now;
                           if(x >> t[m + 1]) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int now = 1, nx = tx;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(c == k) ++now;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(c == k) ++now;
                                                                                                                                                                                                                                                                                                                               else if(!p || !q) { int k = max(p, q);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      hm[o].upd(tx, y);
                                                                                                                                                                                                                                                                                                                                                                                        hm[o].upd(x, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(!now) {
                                                                                                           if(a[i][j] == 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                           if(k == 3) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         break
                                                                                                                                                                                            if(!p && !q) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(!now) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           break;
                                                                                                                                                                  } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           * 给定 7 * 7 的棋盘,格子四联通,格子有收益或不能走。求通路的最大收益。
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int p = u & INF; for(int i = hd[p]; \simi; i = ne[i]) if(u == s[i]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        s[L] = u; f[L] = v; ne[L] = hd[p]; hd[p] = L++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     static const int INF = pw(18) - 1, N = 8e5; int hd[INF + 1], ne[N], s[N], L, f[N];
                                                                                                                                                                                                                   int main() {
    rep(i, 0, 22) t[i] = i + i;
    memset(hm[0].hd, -1, sizeof(hm[0].hd));
    memset(hm[1].hd, -1, sizeof(hm[0].hd));
                                                                                                                                                                                                                                                                                                                                                                                                               else cout << "Impossible" << endl;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 1, n + 1) rep(j, 1, m + 1) { cin >> a[i][j];
                                                                                                                                     int i = id[1 \land 2 << t[n-1]];
                                                                                                                                                                                                                                                                                                                                                                                          if(ans) cout << ans << endl;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       memset(hd, -1, sizeof(hd)),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ans = max(ans, a[i][j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int n, m, t[22], a[22][22];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       void upd(int u, int v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      f[i] = max(f[i], v);
                                                      k = sz(sta); A.reset();
rep(j, 0, k) gao(j);
A = kpow(A, m);
                                                                                                                                                                                                                                                                                                                                 while(cin >> n >> m) {
                                                                                                                                                                                                                                                                                                                                                            int ans = solve();
```

插头 db

11.24

return 0;

void init() {

Struct HM {

return A.a[i][0];

sta.pb(i);

int main() {
 rep(i, 0, 22) t[i] = i + i;

return ans;

rep(j, 0, hm[o].L) hm[o].s[j] <<= t[1]; rep(j, 1, m + 1) {

rep(k, 0, hm[o \wedge 1].L) {

o \wedge = 1; hm[o].init();

int o = 0; hm[o].init(); hm[o].upd(0, 0);

rep(i, 1, n + 1) {

int ans = $-INT_MAX$;

int solve() {

}hm[2];

return ;

cin >> n >> m;

Ξ

```
for (auto v : f[0][3]) if (sz(v.fi) == 2) ans = add(ans, v.se);
for (int 1 = 1; 1 < m - 2; 1 \leftarrow 2) { // 6 \neq \mathbb{Z}
                                                                                                                   .;
0
                                                                                                             rep(i, 0, sz(tmp)) if (tmp[i]+1 > k) if (!p) continue;
                                                                                                                                                             ۳,
                                                                   rep(j, 1+2, m) tmp.pb(a[j]);
                                                                                                                                                               ||
                                          rep(j, 0, 1) tmp.pb(a[j]);
                                                                                                                                                             (f[o][t][tmp] += v.se)
                                                                                        p = 1;
                                                                                                                                                                                                                                                                                                                             cout << ans << endl
                                                                                                                                                                                                                                                                             ans = 0;
                                                                                                                                                                                                                                                                                                                                                                      return 0;
```

的排列数量

4

相邻差值小于等于

11.25

while(T--) cout << solve() << endl;</pre>

return 0;

int T; cin >> T;

// 求相邻差值小于等于 k(k<=4) 的排列数量 // 一种枚举排列的方法

垃双联通子图计数

```
11.26
                                                                                                int n, k, a[N], b[N], ok, p, ans, c[200], ans2, S, m; bool o; map<vi, int> f[2][4];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(j, 0, 1) tmp.pb(a[j]); tmp.pb(0); tmp.pb(0);
rep(j, 1, m) tmp.pb(a[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (1 == 0) (f[0][t | 1][tmp] += v.se) %= P,
if (1 == m) (f[0][t | 2][tmp] += v.se) %= P,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 0, sz(tmp)) if (tmp[i]+1 > k) p = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    .
0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(i, 0, sz(tmp)) if (tmp[i]+1 > k) p =
                                                                                                                                                                                                                                                                                                                                                                                                                                            m = sz(v.fi); vi a = v.fi;
rep(1, 0, m) {
   if (1 == 0 && (t & 1)) continue;
   if (1 == m - 1 && (t & 2)) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(1, 0, m) { // 放左或右
if (1 == 0 && (t & 1)) continue;
if (1 == m - 1 && (t & 2)) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for (int 1 = 0; 1 <= m; 1 += 2) { //
if (1 == 0 && (t & 1)) continue;
if (1 == m && (t & 2)) continue;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    vi tmp = a; tmp[1] = 0; p = 1;
                                                                                                                                                                                                                                                                    rep(i, 0, 2) rep(j, 0, 4) f[i][i].clear();
f[0][vi()] = 1; o = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 (f[o][t][tmp] += v.se) \% = P;
                                                                                                                                                                                                                                                                                                                                                                  rep(t, 0, 4) f[0][t].clear();
rep(t, 0, 4) {
   for (auto v : f[!0][t]) {
#pragma GCC optimize("Ofast")
#pragma GCC target("sse2")
#pragma GCC optimize("unroll-loops")
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (!p) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (!p) continue;
                                                                                                                                                                                              cout << 1 << endl;
                                                                                                                                               while (cin >> n >> k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 a[1]++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                vi tmp;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              p = 1;
                                                                                                                                                                                                                                                                                                                         rep(i, 1, n+1) {
                                                                                                                                                                       if (n == 1) {
                                                                                                                                                                                                                            continue;
                                                                           const int N = 10;
                                                                                                                                                                                                                                                                                                                                                 0 ^= 1;
                                                                                                                            int main()
```

```
for (int msk = (i - 1) & i; msk >= 0; msk = (msk - 1) & i) {
   if (msk & lb(i)) dc[i] = add(dc[i], mul(c[msk], pw2[e[i ^ msk][i ^ msk] / 2]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for (int msk = i; msk >= 0; msk = (msk - 1) & i) {
   if (msk & lb(i)) way[i][j] = add(way[i][j], mul(mul(way[i ^ msk][j], c[msk]),
                                                        int n, S, e[N][N], way[N][N], a[100], t, x, y, dc[N], c[N], c2[N], c1[N], pw2[500], T,
                                                                                                                                                                                                                                                                        S = pw(n) - 1;
rep(i, 0, S+1) rep(j, 0, S+1) {
    e[i][j] = 0;
rep(k, 0, n) if (pw(k) & i) e[i][j] += __builtin_popcount(a[k] & j);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(j, 1, S+1) way[0][j] = 1;
rep(i, 1, S+1) rep(j, 1, S+1) {
if ((j & i) || lb(j) > lb(i)) continue;
way[i][j] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               c[i] = sub(pw2[e[i][i] / 2], dc[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (msk == 0) break
                                   const int N = 1 << 10;
                                                                                                                                                                                                             // c2 边双联通子图个数
// 求边双联通子图个数
                                                                                                                                                                                                                                                                                                                                                                                                                              rep(i, 1, S+1) {
                                                                                                                                                   // dc 不联通子图个数
// c1 单联通子图个数
                                                                                                                                                                                                                                                                                                                                                                                                                                                              dc[i] = 0;
                                                                                                                  // c 联通子图个数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void solve2() {
                                                                                                                                                                                                                                         void solve1() {
```

if (msk == 0) break;

[msk][j]));

```
} rep(i, 1, S+1) {
    cr(1] = 0;
    for (int msk = (i - 1) & i; msk >= 0; msk = (msk - 1) & i) {
        if (msk & lb(i)) c1[i] = add(c1[i], mul(way[i ^ msk][msk], c2[msk]));
        if (msk == 0) break;
        }
} c2[i] = sub(c[i], c1[i]);
}

int main() {
    cin >> T;
    pw2[0] = 1;
    rep(i, 1, 300) pw2[i] = pw2[i-1] * 2 % P;
    rep(i, 0, n) a[i] = (pw(n) - 1) ^ pw(i);
    rep(i, 0, m) {
        cin > n >> w;
        rep(i, 0, m) {
        cin > b > w;
        rep(i, 0, m) {
        cin > b > w;
        rep(i, 0, m) {
        cin > b > w;
        rep(i, 0, m) {
        cin > b > w;
        rep(i, 0, m) {
        coin > cin > b > w;
        rep(i, 0, m) {
        coin > cin > b > w;
        rep(i, 0, m) {
        coin > cin > w;
        rep(i, 0, m) {
        rep(i, 0, m) {
        coin > cin > w;
        rep(i, 0, m) {
        rep(i, 0, m) {
```