Template

GummyBear

October 10, 2019

Щ	**	3.22 覆盖大于 k 次的矩形面积	
П	A 1.1 vimrc	4 Game 4.1 Nim 积	
N	DP 2.1 DigDP	5 Geo 12 5.1 1、基础点、向量 12 5.2 2、线段、直线、曲线 13	
ಣ	DataStructure 1	3、中旬	
	3.1 2DST	5.4 4、三角形	
-		က် မ	
		7, 3D	
	3.5 Fenwick	5.8 HalfPlane_n2	
	3.7 KDT		
,	3.9 LCT_diameter	5.12 MinAreaTri	
	0 Rope	<u>四四边形形数</u>	
	3.11 S1	5.14 半囲图转对偶图	
-	Splay		
		o Graph 6.1 2-sat	
	6 perTreap	BCC	
	3.17	6.3 CircleCount	
ž	ə.rs 幼浴 up_tct	DLX	
-	3.20 常见转化 10	DMST	
	3.91 线段树併化建图	6.7 Dinic	

Fuzhou University			目录	2/72
38 39 39 41 41 41 42	2 4 4 4 5	1 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	48 48 49 49 49 50 50	50 50 50 50 50 50 50 50 50 50 50 50 50 5
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		∞		6
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			30 30 31 31 32 32 33 33 34 35 36 37 37 37 37 37 37 37 37 37 37 37 37 37	3.3
			30 30 31 31 31 31 31 31 31 31 31 31 31 31 31	32 33 34 34 35 36 36 36 37 37 37 37 37 37 38 37 38 38 37 38 38 38 38 38 38 38 38 38 38 38 38 38
			30 30 31 31 31 31 31 31 31 31 31 31 31 31 31	32 32 33 34 34 34 35 36 36 36 37 37 37 37 37 37 38 37 38 38 37 38 38 38 38 38 38 38 38 38 38 38 38 38
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	latch	rTree Vagner_O(nmlog(m))	小	tor 版本
	latch	rTree Vagner_O(nmlog(m))	1人掌最短路 1向星 7在树 2短路矩阵中第 k 小 3.皮树计数与欧拉回路方案数 3.定婚姻匹配 erlekampMassey	rPower wOD Last L k 进制_xor 版本 rion ssDB ssInt ssXor Euclid arBasis arRecursion hFunction
Dominator Tree	MaxMatch Max_clique_BK Max_clique_fastest	SCC SteinerTree StoerWagner_O(n3) StoerWagner_O(nmlog(m)) StoerWagner_N(mmlog(m)) StoerWagner_N(mmlog	1人掌最短路 1向星 7在树 2短路矩阵中第 k 小 3.皮树计数与欧拉回路方案数 3.定婚姻匹配 erlekampMassey	CRT EulerPower FFT FrT FFT FFT FFT FY FWT k 进制 xor 版本 FWT k 进制 xor 版本 Fru
	MaxMatch Max_clique_BK Max_clique_fastest	SCC SteinerTree StoerWagner_O(n3) StoerWagner_O(nmlog(m)) StoerWagner_N(mmlog(m)) StoerWagner_N(mmlog	仙人掌最短路 前向星 带花树 最短路矩阵中第 k 小 生成树计数与欧拉回路方案数 稳定婚姻匹配 .h BerlekampMassey	rPower wOD Last L k 进制_xor 版本 rion ssDB ssInt ssXor Euclid arBasis arRecursion hFunction

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.vimrc

```
void init() { memset(f, -1, sizeof(f)); }
                                                       while(x) dig[pos++] = \times \% 10, \times /= 10;
                                                                                       return dfs(pos -1, ..., 1);
                                                                                                                                                                                                    init();
// 可调用 solve(x) 多次
11 solve(11 x) {
                             int pos = 0;
                                                                                                                                                                       void solve()
                                                                                                                                          nmap<F9> : :w <CR> :!g++ % -0 %< -02 -g -std=c++11 -wall <CR>
                             sts=2 sw=2
                                                                                                             nmap<F8> : !time ./%< < %<.in <CR>
                                                                                                                                                                       nmap<F10> : :w <CR> :make %< <CR>
                             set nu ai ci si mouse=a ts=2
                                                       nmap<F2> : vs %<.in <CR>
                                                                                    nmap<F3> : !gedit % <CR>
```

if (!lim) f[] = res;

return res;

DataStructure 3

#include<bits/stdc++.h>

1.2 head

using namespace std;

#define mp make_pair

#define se second #define fi first

```
rep(i,\ 1,\ dep1+1)\ rep(j,\ p[i],\ n+1)\ rep(k,\ 0,\ dep2+1)\ rep(1,\ p[k],\ m+1)\ st[i][k][j][1]=max(st[i-1][k][j]-p[i-1][l],\ st[i-1][k][j][l]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int l1 = Log[x2-x1+1], l2 = Log[y2-y1+1];
int res1 = max(st[l1][l2][x1+p[l1]-1][y1+p[l2]-1], st[l1][l2][x2][y2]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int res2 = max(st[l1][l2][x1+p[l1]-1][y2], st[l1][l2][x2][y1+p[l2]-1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(i, 1, n + 1) rep(j, 1, dep2 + 1) rep(k, p[j], m + 1) st[0][j][i][k] = max(st[0][j-1][i][k], st[0][j-1][i][k - p[j-1]]);
                                                                                                                                                                                                                                                                                      for(dep1 = 0; (1 << dep1) < n; dep1++);
                                                                                                                                                                                                                                                                                                                            For(dep2 = 0; (1 << dep2) < m; dep2++);
                                                                                                                                                                                                                                                                                                                                                                                                               st[0][0][i][j] = a[i][j]; // modify
                                                                                                                                                                                                      rep(i, 0, M) p[i] = 1 << i;
rep(i, 2, N) Log[i] = Log[i >> 1] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int qry(int x1, int y1, int x2, int y2){
                                                                                                                                                               void build(int n, int m, short a[][N]){
                                                                                                                                                                                                                                                                                                                                                                      rep(i, 1, n+1) rep(j, 1, m+1)
                                                                               int Log[N], p[M], dep1, dep2;
short st[M][M][N][N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            //attention to range of k
                                      const int N = 1010, M = 11;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return max(res1, res2);
namespace ST_2D{
```

2DSegTree3.2

```
void upd(int L,int R,int c,int l=0,int r=m,int rt=1) {
// 区域覆盖、标记永久化、标记单调
                                                                                                                                                        ma[rt]=max(ma[rt], c);
                                                                                                  int ma[N<<2], la[N<<2];</pre>
                                const int N=1010;
                                                                             struct seg {
                                                         int n, m, d;
```

if (...) res += dfs(pos - 1, ..., lim & (i == up));

if (!lim && ~f[...]) return f[...];

int up = lim ? dig[pos] : 9;

11 res = 0;

rep(i, 0, up + 1)

dfs(int pos, ..., bool lim) {

11 f[];

DigDP

DP

if (pos == -1) return ?;

2DST

```
#define rep(i, a, b) for(int i=(a); i<(b); i++) #define per(i, a, b) for(int i=(b)-1; i>=(a); i--)
                                                                                                               #define de(a) cout << #a << " = " << a << endl
                                                                                                                                          #define dd(a) cout << #a << " = " << a << " "
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // cout << setiosflags(ios::fixed);
                                                                                                                                                                                                                                                                                                                                                                                                                                                  std::ios::sync_with_stdio(false);
                                                                                                                                                                          #define all(a) a.begin(), a.end()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // cout << setprecision(3)
                                                                                    #define sz(a) (int)a.size()
                                                                                                                                                                                                                                                                                                typedef pair<int, int> pii;
                                                                                                                                                                                                        #define pw(x) (111<<(x))
                                                                                                                                                                                                                                                                                                                            typedef vector<int> vi;
                                                                                                                                                                                                                                                                typedef long long ll;
#define pb push_back
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         std::cin.tie(0);
                                                                                                                                                                                                                                     #define endl "\n"
                                                                                                                                                                                                                                                                                                                                                         typedef double db;
                                                                                                                                                                                                                                                                                                                                                                                                                  int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return 0;
```

```
rep(i, 1, r+1){
   if (p1 > mid) {tmp[i] = a[p2]; p2++;}
   else if (p2 > r) {tmp[i] = a[p1]; p1++;}
   else if (a[p1] y <= a[p2].y) {tmp[i] = a[p1]; p1++;}</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i, l, pos) fen.add(fen.a1, a[i].z, -a[i].num);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i, 1, n+1) cin >> a[i].x >> a[i].y >> a[i].z;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, 1, n+1) {
if (i > 1 && a[i] == a[i-1]) { a[nn].num++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         while (pos <= mid && a[pos].y <= a[i].y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            fen.add(fen.a1, a[pos].z, a[pos].num);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 1, nn+1) ans[a[i].ans] += a[i].num;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               a[i].ans += fen.sum(fen.a1, a[i].z);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 0, n) cout << ans[i] << endl
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      else {tmp[i] = a[p2]; p2++;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(i, 1, r+1) a[i] = tmp[i];
                                                                                                                                                                                                                                                                                                                                                                                                           CDQ(1, mid); CDQ(mid+1, r);
                                                                                                                                a[1].ans = a[1].num - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           CartesianTree
                                                                                                                                                                                                                                                                                                                                   int mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       sort(a+1, a+n+1, cmp)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 a[++nn] = a[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(i, mid+1, r+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         a[nn].num = 1;
     void CDQ(int 1, int r){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             p1 = 1; p2 = mid+1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int main(){
    cin >> n >> k;
                                                                       if (1 == r) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ;++sod
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       fen.ini(N);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CDQ(1, nn);
                                                                                                                                                                                                                  return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   pos = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                nn = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           3.4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(x2>=mid+1) ans=max(ans, qry(x1, x2, y1, y2, mid+1, r, rt<<1|1));</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void upd(int x1, int x2, int y1, int y2, int c, int l=0, int r=n, int rt=1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(x1<=mid) ans=max(ans, qry(x1, x2, y1, y2, 1, mid, rt<<1));</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    qry(int x1, int x2, int y1, int y2, int 1=0, int r=n, int rt=1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(x1<=1&&r<=x2) return ans=max(ans, ma[rt].qry(y1, y2));</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(R>=mid+1) ans=max(ans, qry(L, R, mid+1, r, rt<<1|1));</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(x2>=mid+1) upd(x1, x2, y1, y2, c, mid+1, r, rt<<1|1);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(x1<=1&&r<=x2) return la[rt].upd(y1, y2, c), void();</pre>
if(L<=l&&r<=R) return la[rt]=max(la[rt], c), void();</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(x1<=mid) upd(x1, x2, y1, y2, c, l, mid, rt<<1);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(L<=mid) ans=max(ans, qry(L, R, l, mid, rt<<1));</pre>
                                                                                                                           if(L<=mid) upd(L, R, c, l, mid, rt<<1);
if(R>=mid+1) upd(L, R, c, mid+1, r, rt<<1|1);</pre>
                                                                                                                                                                                                                                                                                                                                        int qry(int L,int R,int l=0,int r=m,int rt=1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(L<=l&&r<=R) return ans=max(ans, ma[rt]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         bool operator == (const node & b) const{ return x == b.x & x = b.x & x =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ans=max(ans, la[rt].qry(y1, y2));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int p1, p2, pos, n, k, nn, ans[N];
struct node{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ma[rt].upd(y1, y2, c);
```

ans=max(ans, la[rt]);

int ans=0;

int mid=1+r>>1;

int mid=l+r>>1;

return ans;

struct Seg {
 seg ma[N<<2], la[N<<2];</pre>

int mid=1+r>>1;

int mid=1+r>>1;

int ans=0;

int

return ans;

```
// desc : bud a cartesion tree from a[0] .. a[n-1]
                                                                                                                            // !!!! : return rt, a[n] will be rewrite
                                                                                                                                                                                                                                                       fill_n(ls, n, -1), fill_n(rs, n, -1); rep(i, 0, n) {
                                                                                                                                                                                         int cartesionTree(int a[], int n)
                                                                                                                                                                                                                         a[n] = INT\_MAX; vi v(1, n);
                                                                                                                                                          int ls[N], rs[N];
                                                                                               // time : 0(N)
                                                                                                                                                                                            //if (a.y != b.y) return a.y < b.y;
bool cmp(node a, node b){
   if (a.x != b.x) return a.x < b.x;
   if (a.y != b.y) return a.y < b.y;</pre>
```

bool cmp2(node a, node b){

return a.z < b.z;

} a[N], tmp[N];

//return a.z < b.z;

return a.y < b.y;

 $int \times$, y, z, num, ans;

const int N = 200005;

CDO

3.3);

```
KDT
                                                                                // init
                                     3.7
while (a[v.back()] < a[i]) ls[i] = v.back(), v.pop\_back();
                   v.pb(rs[v.back()] = i);
                                                        return v[1];
```

3.5 Fenwick

```
T sum(T *a, int p) { T r=0; for(; p>=1; p-=p & -p) r+=a[p]; return r; } T pre(int p) { return !p ? 0 : sum(a1, p) * p - sum(a2, p);} T qry(int l,int r) {return pre(r)-pre(l-1); }
                                                                                                                                                                                                                                                                                               void ini(int _n){ fill_n(a1+1, n=_n, 0);fill_n(a2+1, n=_n, 0); }
                                                                                                                                                                                                                                                                                                                                       void add(T *a, int p, T d) { for(; p<=n; p+=p & -p) a[p]+=d; }
                                                                                                                                                                                                                                                                                                                                                                                                                 add(a1, 1, d), add(a1, r + 1, -d);

add(a2, 1, d * (1 - 1)), add(a2, r + 1, -d * r);
                                                                                                                                                                                                                                                                                                                                                                            void add(int l,int r,T d) {
                                                                             // support : segment add, sum
                                                                                                                                                                                                                             static const int N = 2e5+7;
                                                                                                               // !!!! : use before init()!
                                                                                                                                                                                                                                                               int n;T a1[N], a2[N];
// index : [1, n]
                                                                                                                                                     template<class T>
                                  // time : nlogn
                                                                                                                                                                                          struct Fenwick{
```

3.6 IntervalMaximumChangeTimes

```
o`
                                                                                                                                                                                                                                                                                                                           1s)
                                                                                                                                                                                                                          down(l, r, mid, rt); if(ma[ls | o] < v) return o ? qry(L, R, v, o, 0, l, mid, ls) : qry(L, R, v, o,
                                                                                                                                                                                                                                                                                                                      R, v, o, 0, 1, mid,
ll &v, int o, bool spe, int l, int r, int rt)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ma[rt] = max(ma[1s], ma[rs]);
rep(o, 0, 2) { 11 v = 0; cnt[rt][0] = qry(1, r, v, o, 1, 1, r, rt); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(o == 0 && L <= mid) ans += qry(L, R, v, o, 0, 1, mid, 1s);
if(R > mid) ans += qry(L, R, v, o, 0, mid + 1, r, rs);
if(o == 1 && L <= mid) ans += qry(L, R, v, o, 0, 1, mid, 1s);</pre>
                                                                                                                                                                                                                                                                                                                         == 0 ? qry(L,
                                                                                                                                                                                                                                                                                                                    int ans = cnt[rt][0] - cnt[ls | 0][0] + (o
  qry(L, R, v, o, 0, mid + 1, r, rs));
                                                                                                                                                          if(1 == r) return v = ma[rt], 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int mid = 1 + r >> 1, ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void up(int 1, int r, int rt) {
                                                                                                                                                                                                                                                                                                                                                                                       return v = ma[rt], ans;
inline int qry(int L, int R,
                                                                                           if(ma[rt] < v) return 0;</pre>
                                                                                                                                                                                            int mid = 1 + r >> 1;
                                                                                                                            if(L <= 1 && r <= R) {
                                                                                                                                                                                                                                                                                           mid + 1, r, rs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        down(1, r, mid, rt);
                             if(L > R) return ⊕;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return ans;
                                                              if(!spe) {
```

T dis(P p, int k) {

```
struct P\{T \times [D]; bool operator < (const P &c) const { return <math>\times [W] < c.\times [W]; } \}p[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(!k) {k=newnode(),nd[k].val=p,nd[k].son[0]=nd[k].son[1]=0,up(k);return;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  nd[k].sz = 1; rep(i, 0, 2) nd[k].sz += nd[nd[k].son[i]].sz;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         0 = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ins(p, nd[k].son[nd[k].val.x[w] < p.x[w]], (w + 1) % D);
                                                                                                                                                                                                                                                                            struct Node{ T mi[D], ma[D]; int son[2], sz; P val; }nd[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(i, 0, 2) if(al * nd[k].sz < nd[nd[k].son[i]].sz)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(o) \{ int cnt = 0; pia(k,cnt), k = build(1,cnt,w);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      nd[k].mi[i] = min(nd[k].mi[i], nd[s].mi[i]);
nd[k].ma[i] = max(nd[k].ma[i], nd[s].ma[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   w=w, nth_element(p+l, p+mid, p+r+1), nd[k].val=p[mid];
                                                                                                                                                                                                                                                                                                                                                 void init() { rt = L = top = 0; }
int newnode() { return top ? sta[top—] : ++L; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        nd[k].son[0] = build(l,mid-1, (w + 1) % D);

nd[k].son[1] = build(mid+1, r, (w + 1) % D);
                                                                                                                                                                                                                                                                                                                                                                                                                                                     // 抄上面这部分就好了,下面部分是视具体题目定的
// 最近点(曼哈顿距离)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(nd[k].son[0]) pia(nd[k].son[0],cnt);
p[++cnt]=nd[k].val, sta[++top]=k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(nd[k].son[1]) pia(nd[k].son[1],cnt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int mid = 1 + r >> 1, k = newnode();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(o, 0, 2) if(nd[k].son[o]) {
    int s = nd[k].son[o];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int build(int l,int r,int w) {
                                                                       const int N = 1e6 + 7, D = 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void ins(P p, int &k, int w)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void check(int &k,int w) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            void pia(int k, int &cnt) {
                                                                                                                                                                                                                int rt, L, top, W, sta[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(1 > r) return 0;
typedef int T; // modify
                                                                                                         const T INF = 1e9 + 7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              up(k), check(k, w);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               up(k); return k;
                                                                                                                                           const db al = 0.75;
                                                                                                                                                                                                                                                                                                                                                                                                                   void up(int k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         bool 0 = 0;
                                       namespace KDT {
```

```
void down(int x) { if(nd[x].rev) gao(nd[x].son[0]), gao(nd[x].son[1]), nd[x].rev =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void access(int x) { for(int y = 0; x; y = x, x = nd[x].fa) splay(x), nd[x].son[1]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int 1 = id(x), r = (1 ^ 1), s = nd[x].son[r];
if(nrt(y)) nd[z].son[id(y)] = x; nd[x].son[r] = y; nd[y].son[1] = s;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void makeroot(int x) { access(x); splay(x); gao(x); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(nrt(y)) (id(x) \land id(y)) ? rot(x) : rot(y);
                                                                                                                                                                                                                                                                                                                                                                                              nd[x].rev \land = 1, swap(nd[x].son[0], nd[x].son[1]);
                                                                                                                   return nd[fa].son[0] == x || nd[fa].son[1] == x;
                                                                                                                                                                                                                                                                      nd[x].sum = nd[ls].sum + nd[rs].sum + nd[x].val;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(s) nd[s].fa = y; nd[y].fa = x; nd[x].fa = z;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      access(x); splay(x);
while(nd[x].son[0]) down(x), x = nd[x].son[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int id(int u) { return nd[nd[u].fa].son[1] == u;
                                                                                                                                                                                                                                          int ls = nd[x].son[0], rs = nd[x].son[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int \hat{y} = nd[x].fa, z = nd[y].fa;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           For(int i = x; ; i = nd[i].fa)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 while(top) down(sta[top—]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(!nrt(i)) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int y = nd[x] fa;
                            // if(no root) return 1
Node nd[N];        int        sta[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               sta[++top] = i;
                                                                                    int fa = nd[x].fa;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int findroot(int x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void splay(int x) {
                                                                                                                                                                                                                if(!x) return ;
                                                                                                                                                                                                                                                                                                                                                                    if(!x) return ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    while(nrt(x))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        (x)dn (x);
                                                             bool nrt(int \times) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int top = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void rot(int \times) {
                                                                                                                                                                                                                                                                                                                                 void gao(int x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rot(x);
                                                                                                                                                                                void up(int x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                = y, up(x); 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    splay(x);
return x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      /加拉
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // 找根
                            rep(i, 0, D) ans += max(0, p.x[i] - nd[k].ma[i]) + max(0, nd[k].mi[i] - p.x[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(d, 0, D) ans += max(sqr(nd[u].mi[d] - p.x[d]), sqr(nd[u].ma[d] - p.x[d]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                11 dis = 0; rep(d, 0, D) dis += sqr(nd[u].val.x[d] - p.x[d]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(i, 0, 2) if(nd[u].son[i]) qry(nd[u].son[i], ans);
                                                                                                                                                                                  T ans = 0; rep(i, 0, D) ans += abs(a.x[i] - b.x[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(all_in) { ans = max(ans, ma); return; }
                                                                                                                                                                                                                                                                                                                               int ls = nd[k].son[0], rs = nd[k].son[1];
T dl = ls ? dis(p, ls) : INF;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int ls = nd[u].son[0], rs = nd[u].son[1]
                                                                                                                                                                                                                                                                                                                                                                                                                             if(d1 > dr) swap(d1, dr), swap(ls, rs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(dl > dr) swap(dl, dr), swap(ls, rs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  sqr(int \times) \{ return 111 * \times * \times; \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(dr > -ans.top()) qry(p, rs);
                                                                                                                                                                                                                                                                                                     ans=min(ans,dis(p,nd[k].val));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(u_in) ans = max(ans, u_val)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(dl > -ans.top()) qry(p, ls)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        while(!ans.empty()) ans.pop();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(no_in || ma < ans) return ;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       11 d1 = 1s? Dis(p, Is) : -1;
11 dr = rs? Dis(p, rs) : -1;
                                                                                                                                                                                                                                                                                                                                                                                              T dr = rs ? dis(p, rs) : INF;
                                                                                                                                                                                                                                                                         void qry(P p, int k, T &ans) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ans.push(—dis), ans.pop();
                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(dl<ans) qry(p,ls,ans)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(dr<ans) qry(p, rs, ans)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void qry(int u, int &ans) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 0, k) ans.push(1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // 矩形区域的最大值(伪代码)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // 距离点 u 第 k 远
priority_queue<ll> ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void qry(P p, int u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // 0(n ^ (2 - 1 / D))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Dis(P p, int u) {
                                                                                                                                                 dis(P a, P b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            11 ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return ans;
                                                                                           return ans;
                                                                                                                                                                                                                return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void init() {
                                                             // modify
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ~11
```

if(findroot(y) != x) nd[x].fa = y;

void link(int x, int y) {

makeroot(x)

} // 惠达

son[2]; **bool** rev; };

sum, fa,

struct Node { int val,

struct LCT

LCT

3. 8 static const int N = ::N;

```
if(findroot(y) != x) makeroot(y), nd[x].fa = y, add(y, x), up(y);
                          int &rs = nd[x].son[1];
                                                                                                                                                                                               void link(int x, int y) {
                                                       if(y) del(x, y);
if(rs) add(x, rs);
                                                                                                                  rs = y, up(x);
splay(x);
                                                                                                                                                                                                                                makeroot(x);
                                                           П
                                                         if(findroot(y) == x \& nd[y].fa == x \& ind[y].son[0]) nd[y].fa = nd[x].son[1]
                                                                                                                                                                       void path(int x, int y) { makeroot(x); access(y); splay(y);
                                                                                                                                                                                                                              void upd(int x, int c) { splay(x); nd[x].val = c; up(x);
void cut(int x, int y)
                                                                                                                                        // nd[y]: 路径信息
                              makeroot(x)
                                                                                        0, up(x);
                                                                                                                                                                                                    // 单点修改
```

LCT diameter 3.9

```
(u'0] //
                                                                                         3.10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           3.11
}lct;
                                                                                                                                                                                                                                                                                                                                                                                void del(int x, int y) { Era(nd[x].chain, nd[y].lmx), Era(nd[x].path, nd[y].mxs); }
void add(int x, int y) { nd[x].chain.insert(nd[y].lmx), nd[x].path.insert(nd[y].mxs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Ma(nd[p].mxs, nd[ls].rmx + R); // 经过 p 父边的答案
Ma(nd[p].mxs, nd[rs].lmx + L); // 经过 u 向下实边的答案
Ma(nd[p].mxs, cha + sec(nd[p].chain) + (p > n)); // 虚子树中到根路径最长的两条拼起来
                                                                                                                                                                         struct Node { int fa, son[2], lmx, rmx, mxs, sum; bool rev; multiset<int> chain, path;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 nd[p].rmx = max(nd[rs].rmx, nd[rs].sum + L); // 从链底出发的最远距离
nd[p].mxs = max(nd[ls].mxs, nd[rs].mxs); // mxs[p] 表示当前范围的直径
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int L = max(cha, nd[1s].rmx) + (p > n); // 从 p 沿父亲走的最远距离 int R = max(cha, nd[rs].lmx) + (p > n); // 从 p 沿实儿子走的最远距离 nd[p].lmx = max(nd[1s].lmx, nd[1s].sum + R); // 从链项出发的最远距离
                                                                                      int sec(multiset < int> st) { return sz(st) > 1 ? *(++st.rbegin()) : 0; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    nd[p].sum = nd[1s].sum + nd[rs].sum + (p > n); // 当前链的长度 int cha = fir(nd[p].chain); // 从 <math>p 沿虚儿子走的最远距离
                                                   int fir(multiset<int> st) { return sz(st) ? *(st.rbegin()) : 0; ]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             nd[i].fa = nd[i].son[0] = nd[i].son[1] = nd[i].rev = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    nd[i].lmx = nd[i].rmx = nd[i].mxs = nd[i].sum = 0;
                                                                                                                                void Era(multiset<int> &s, int x) { s.erase(s.find(x)); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int p = x, ls = nd[x].son[0], rs = nd[x].son[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Ma(nd[p].mxs, fir(nd[p].path)); // 虚子树的直径
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             nd[i].chain.clear(), nd[i].path.clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // 以下考虑的都是链 p 与链 p 的所有虚子树
                                                                                                                                                                                                                                                                                                static const int N = 30303;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(i, 1, n + m + 1) {
                                                                                                                                                                                                                                                                                                                                                Node nd[N]; int sta[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(!x) return ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void gao(int \times) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(!x) return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void up(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       void init() {
                                                                                                                                                                                                                                                      struct LCT {
```

Rope

int getAns() { access(1); splay(1); return nd[1].mxs;

```
// 复制 cur 处开始的 1en 个字符到字符数组
                                                                                                                                                                                              // 提取从 cur 处开始的 1en 个字符 // 可持久化, 0(1), 直接拷贝根节点
                                                                                                                  // 删除 cur 处的字符,换成字符数组
                                                                                                // 删除 cur 开始的 1en 个字符
                                                                          // 在 cur 处插入字符数组
                                                                                                                                                        // 取第 cur 个字符
                                                                                                                                                                          // 取第 cur 个字符
                                                         // 在末尾插入字符
                                                                                                                                                                                                                                                                                                                                                             æ
                                                                                                                                                                                                                                                                                                                                                             ^
                                                                                                                                                                                                                                                                                                                                                        区间 a \rightarrow b, b \rightarrow c, c \rightarrow d ... z
                                                                                                                                                                                                                                                                                                                                * 1. 拆成多个子串, 重新安排它们的位置 * 三) 区间 a \rightarrow b, b \rightarrow c, c \rightarrow d...
                                                                                                                                      rp.copy(cur, len, 字符数组 );
                                                                                                                                                                                                                                                                             * 1. 维护一正一反两个 rope
* 2. 翻转等价于交换两个子串
                                                                                                                                                                                                                                                                          维护一正一反两个 rope
                                                                                                                rp.replace(cur, 字符数组 );
                     using namespace __gnu_cxx;
                                                                          rp.insert(cur, 字符数组 );
rp.erase(cur, len);
                                                                                                                                                                                                                                                                                                                                                                            维护 26 个 rope
                                                                                                                                                                                              rp.substr(cur, len);
#include <ext/rope>
                                                                                                                                                                                                                                                                                                                   区间循环位移
                                                           rp.push_back(ch);
                                                                                                                                                                                                                                                           一)翻转操作
                                         ropecchar> rp;
                                                                                                                                                                                                                     rp[i] = rp[i]
                                                                                                                                                           rp.at(cur);
                                                                                                                                                                             rp[cur];
```

\mathbf{S}

```
a[i][j] = max(a[i-1][j], a[i-1][j+(1 << i >> 1)]);
                                                                                        void build(int *v, int n){
    rep(i, 2, n + 1) lg[i] = lg[i >> 1] + 1;
    rep(i, 0, n) a[0][i] = v[i];
    rep(i, 1, lg[n] + 1) rep(j, 0, n - (1 << i) + 1) {</pre>
                             static const int N = 101010;
                                                                                                                                                                                                                                                                                                                                                                                       int i = \lg[r - 1 + 1]
                                                                                                                                                                                                                                                                                                                                                  if(1 > r) swap(1, r);
                                                                                                                                                                                                                                                                                                                  int qry(int 1, int r){
                                                             int a[20][N], lg[N];
struct ST{
```

for(**int** y = 0; x; y = x, x = nd[x].fa) {

void access(int x)

swap(nd[x].son[0], nd[x].son[1]); swap(nd[x].lmx, nd[x].rmx);

 $nd[x].rev ^{-1}$

```
if(nd[u].rev) gao(nd[u].son[0]), gao(nd[u].son[1]), nd[u].rev = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int y = nd[x].fa, z = nd[y].fa;
int l = id(x), r = (1 ^ 1), s = nd[x].son[r];
if(z) nd[z].son[id(y)] = x; nd[x].son[r] = y; nd[y].son[1] = s;
if(s) nd[s].fa = y; nd[y].fa = x; nd[x].fa = z;
                                                                                                                                                                                                                                                                                                               nd[u].rev \land = 1, swap(nd[u].son[0], nd[u].son[1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int y = nd[x].fa, z = nd[y].fa;
if(z != g) (id(x) ^ id(y)) ? rot(x) : rot(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int id(int u) { return nd[nd[u].fa].son[1] == u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        nd[u].sz = nd[ls].sz + nd[rs].sz + nd[u].cnt;
                                                                                                            nd[L].son[0] = nd[L].son[1] = nd[L].rev = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int ls = nd[u].son[0], rs = nd[u].son[1];
    6
    = 0, int 0 =
                                                                                                                                                                                                                           void init(int n) { rt = L = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void splay(int x, int g = 0) {
                                                                                                                                          nd[L].cnt = nd[L].sz = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    while(nd[x].fa != g) {
    int newnode(int c, int fa
                                                        nd[fa].son[o] = L;
                              nd[++L].fa = fa;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(!u) return ;
                                                                                nd[L].val = c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             fhqTreap
                                                                                                                                                                                                                                                           void gao(int u) {
                                                                                                                                                                                                                                                                                                                                                                 void down(int u)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(!g) rt = x;
                                                                                                                                                                                                                                                                                     if(!u) return
                                                                                                                                                                                                                                                                                                                                                                                                                                                      void up(int u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        nb(y), up(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // id starts from 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void rot(int x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rot(x);
                                                                                                                                                                           return L;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             3.14
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(L \le 1 \&\& r \le R \&\& c \le mi[rt][1]) return gao(rt, c), void();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(mi[rt][0] == mi[ls | i][0]) cnt[rt] += cnt[ls | i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void down(int rt) { gao(1s, mi[rt][0]); gao(rs, mi[rt][0]);
void upd(int L, int R, int c, int l, int r, int rt) {
   if(L > R) return ;
                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 0, 2) mi[rt][i] = min(mi[ls][i], mi[rs][i]);
cnt[rt] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   else mi[rt][1] = min(mi[rt][1], mi[ls | i][0]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int mid = 1 + r >> 1;
build(1, mid, 1s); build(mid + 1, r, rs); up(rt);
return max(a[i][1], a[i][r + 1 - (1 << i)]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 sum[rt] += 111 * cnt[rt] * (c - mi[rt][0]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(R > mid) upd(L, R, C, mid + 1, r, rs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            sum[rt] = mi[rt][0] = a[1]; //modify
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(L <= mid) upd(L, R, c, 1, mid, 1s);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        mi[rt][1] = inf; cnt[rt] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void build(int l, int r, int rt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int mid = 1 + r >> 1; down(rt);
                                                                                                                                                                                                                                                                                                    11 sum[N]; int mi[N][2], cnt[N];
                                                                                                                                                                                                                                                                                                                                                           sum[rt] = sum[ls] + sum[rs];
                                                                                                                                                                                                                                                                      static const int N = ::N << 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(c <= mi[rt][0]) return</pre>
                                                                                                                       SegIntervalMax
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void gao(int rt, int c) {
                                                                                                                                                                                                                区间水和
                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, 0, 2) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  mi[rt][0] = c;
                                                                                                                                                                                                                                                                                                                                 void up(int rt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(1 == r)  {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return ;
                                                                                                                                                                                                                // 区间取 max,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         up(rt);
                                                                                                                                                                                                                                            struct Seg {
                                                                                                                                                                                          // 0(nlogn)
                                                                                                                     3.12
```

```
void init() { rt = L = 0; srand(time(0)); }
11 Rand() { return ((rand() * 111 << 16) ^ rand()); }</pre>
                           struct Node { int val, cnt, sz, ls, rs; ll r; bool rev;};
                                                                                                                                                                                                                                                                                                 nd[L].1s = nd[L].rs = nd[L].rev = 0;
                                                                                                                                                                                                                                                                    nd[L].cnt = nd[L].sz = 1;
                                                                            static const int N = ::N;
                                                                                                              int rt, L; Node nd[N];
                                                                                                                                                                                                                    nd[++L].r = Rand();
                                                                                                                                                                                         int newnode(int c)
// 不要修改 Ø 节点的值
                                                                                                                                                                                                                                               nd[L].val = c;
                                                      struct fhqTreap {
                                                                                                                                                                                                                struct Node { int val, fa, son[2], cnt, sz; bool rev; };
                                                                                                                                                                                           // if go to vertex p, must splay(p)
                                                                                                                                                                                                                                                                      static const int N = ::N;
                                                                                                                                                                                                                                                                                                 int rt, L; Node nd[N];
                                                                                                                                                                  // id starts from 1
                                                                        \operatorname{Splay}
                                                                                                                                                                                                                                             struct Splay {
                                                                      3.13
                }sed;
```

```
if(min(nd[rt].getf(v[1]), nd[rt].getf(v[r])) >= max(k.getf(v[1]), k.getf(v[r])))
                                                                                                                                                                                                                                                                                                                                              if(max(mi[rt].getf(v[l]), mi[rt].getf(v[r])) \le min(k.getf(v[l]), k.getf(v[r]))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int rt[::N], L; Node nd[N];
void init() { fill_n(rt, L + 1, 0); L = 0; srand(time(0)); }
11 Rand() { return ((rand() * 111 << 32) ^ (rand() * 111 << 16) ^ rand()); }</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ll ans = max(abs(nd[rt].getf(v[p])), abs(mi[rt].getf(v[p])));
if(k.getf(v[mid]) > nd[rt].getf(v[mid])) swap(k, nd[rt]);
                                                                                                                                                                                                                                                                               if(k.getf(v[mid]) < mi[rt].getf(v[mid])) swap(k, mi[rt]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              struct Node { int val, cnt, sz, ls, rs; ll r, sum; bool rev; };
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void upd(int L, int R, Node c, int l, int r, int rt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(p \le mid) ans = max(ans, qry(p, 1, mid, 1s));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             else ans = max(ans, qry(p, mid + 1, r, rs));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int mid = 1 + r >> 1;
if(L <= mid) upd(L, R, c, 1, mid, 1s);
if(R > mid) upd(L, R, c, mid + 1, r, rs);
                                                                                                                                                                                                                                                                                                                                                                                                            if(mi[rt].k <= k.k) _min(k, l, mid, ls);</pre>
                                                                                                                        if(nd[rt].k > k.k) _upd(k, l, mid, ls);
else _upd(k, mid + 1, r, rs);
                                                                                                                                                                                                                   void _min(Node k, int l, int r, int rt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  nd[L].1s = nd[L].rs = nd[L].rev = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 qry(int p, int l, int r, int rt)
                                                                                                                                                                                                                                                                                                                                                                                                                                         else _min(k, mid + 1, r, rs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      nd[L].val = nd[L].sum = c;

nd[L].cnt = nd[L].sz = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(L <= 1 && r <= R) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   _upd(c, l, r, rt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(1 == r) return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                _min(c, 1, r, rt);
                                                                                                                                                                                                                                                  int mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               static const int N = 3e7;
                                 if(1 == r) return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(L > R) return ;
                                                                                                                                                                                                                                                                                                                 if(1 == r) return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           nd[++L].r = Rand();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int newnode(int c)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // 不要修改 の 节点的值
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         perTreap
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // id starts from 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return ans;
                                                                                                                                                                                                                                                                                                                                                                                    return ;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     struct fhqTreap {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return L;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // init
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ~=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    3.16
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           }sed;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(nd[x].r < nd[y].r)  { down(x), nd[x].rs = merge(nd[x].rs, y), up(x); return \times if(nd[x].rs
                                                                                                                                                                                                                                                                                                                                              void down(int x) { if(nd[x].rev) gao(nd[x].ls), gao(nd[x].rs), nd[x].rev = 0; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   else { down(y), nd[y].ls = merge(x, nd[y].ls), up(y); return y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(sz < k) \ \dot{x} = \dot{u}, \ splitk(nd[u].rs, \ k - sz - 1, \ nd[u].rs, \ y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(nd[u].val \le c) \times = u, splitc(nd[u].rs, c, nd[u].rs, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  else y = u, splitk(nd[u].ls, k, x, nd[u].ls);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    else y = u, splitc(nd[u].ls, c, x, nd[u].ls),
                                                                                                                                                         nd[x].sz = nd[1s].sz + nd[rs].sz + nd[x].cnt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Node nd[N], mi[N]; // nd: max val; mi: min val;
                                                                                                                                                                                                                                                                                  nd[x].rev ^= 1, swap(nd[x].ls, nd[x].rs);
                                                                                                                                                                                                                                                                                                                                                                                                          void splitc(int u, int c, int &x, int &y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void splitk(int u, int k, int &x, int &y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void _upd(Node k, int 1, int r, int rt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            11 k, b;
Node() : k(0), b(0) {}
Node(11 k, 11 b) : k(k), b(b) {}
11 getf(int x) const { return k * x + b;
                                                                                                                          int ls = nd[x].ls, rs = nd[x].rs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      struct Seg {
   static const int N = ::N << 2;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int sz = nd[nd[u].ls].sz;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int merge(int x, int y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // u -> (1 - k) (k+1 - L)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         } else return x + y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // !!!: nd[].cnt == 1
                                                                                                                                                                                                                                                                                                                                                                                  (3 <) (3 =>) <- n //
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     } else \times = y = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   } else \times = \vee = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               lcSegTree
                                                                                                if(!x) return ;
                                                                                                                                                                                                                        void gao(int \times) {
                                                                                                                                                                                                                                                     if(!x) return
                                                              void up(int \times) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(x && y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           down(u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         down(u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      (n)dn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      (n)dn
    return L;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             struct Node {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               3.15
```

```
for(int u = tp; u; f = u, u = wson[u]) {
for(int i = hd[u]; i; i = ne[i]) if(to[i] != f && to[i] != wson[u]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 1, n + 1) isr[i] = (son[fa[i]][0] != i && son[fa[i]][1] != i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 1, r + 1) tot += sz[sta[i]] - sz[wson[sta[i]]]; rep(i, 1, r + 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for(int u = tp; u; u = wson[u]) sta[++top] = u;
                                                                                                                                                                                                                                                                                                                                                                                                       if(son[x][0])    sum[x] = sum[son[x][0]] * sum[x];
if(son[x][1])    sum[x] = sum[x] * sum[son[x][1]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     fa[son[x][0]] = fa[son[x][1]] = x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       now += sz[sta[i]] — sz[wson[sta[i]]],
                            (sz[v] > sz[wson[u]]) && (wson[u] = v);
                                                                                                                                                                                                                                                                                                                    int fa[N], son[N][2], rt, sta[N], top,
inline void up(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       son[x][0] = sbuild(1, i - 1);
son[x][1] = sbuild(i + 1, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         inline int sbuild(int l, int r) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 fa[build(to[i], u)] = u;
                                                                                                                                                                                                                                                // upd h[x], a[x] = y, val[x]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if((now << 1) >= tot) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                inline int upd(int x, int y)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int build(int tp, int f) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(isr[x] \&\& fa[x])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return sbuild(1, top);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // get new f[x]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int tot = 0, now = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // get old f[x]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int \times = sta[i]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(1 > r) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // upd val[u]
                                                                                                                                                                                                                                                                                                                                                                            sum[x] = val[x];
sz[n] \leftarrow sz[n];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return x;
                                                                                    int s = wson[u];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ;(x)dn
                                                                                                                   // h[u] = f[u]
                                                                                                                                                                        [n]y pdn //
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              while(x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    top = 0;
                                                                                                                                              if(s)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        else { y = newcopy(y), down(y), nd[y].ls = merge(x, nd[y].ls), up(y); return y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(nd[x].r < nd[y].r)  { x = newcopy(x), down(x), nd[x].rs = merge(nd[x].rs, y),
                                                                                                                                                                                                                                                                                                                                               void down(int x) { if(nd[x].rev) gao(nd[x].ls), gao(nd[x].rs), nd[x].rev = 0; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       inline void ae(int u, int v) { to[++_] = v, ne[_] = hd[u], hd[u] = _; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(sz < k) \times = u, splitk(nd[u].rs, k - sz - 1, nd[u].rs, y); else y = u, splitk(nd[u].ls, k, x, nd[u].ls);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(nd[u].val \le c) \times = u, splitc(nd[u].rs, c, nd[u].rs, y);
                                                                                                                                              nd[x].sum = nd[ls].sum + nd[rs].sum + nd[x].val;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        else y = u, splitc(nd[u].ls, c, x, nd[u].ls);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for(int i = hd[u]; i; i = ne[i]) if(to[i] != fa) {
                                                                                                               nd[x].sz = nd[ls].sz + nd[rs].sz + nd[x].cnt;
int newcopy(int x) { nd[++L] = nd[x]; return L;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int n, m, a[N], sz[N], wson[N], f[N][2], h[N][2];
int to[N << 1], ne[N << 1], hd[N], _;</pre>
                                                                                                                                                                                                                                                                                        nd[x].rev \land = 1, swap(nd[x].ls, nd[x].rs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void splitk(int u, int k, int &x, int &y) {
                                                                                                                                                                                                                                                                                                                                                                                                       void splitc(int u, int c, int &x, int &y)
                                                                                  int ls = nd[x].ls, rs = nd[x].rs;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // sometimes do not need to newcopy
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int sz = nd[nd[u].ls].sz
                                                                                                                                                                                                                                                                                                                                                                                                                                                                u = newcopy(u), down(u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         u = newcopy(u), down(u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int merge(int x, int y) {
   if(x && y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // u \rightarrow (1 - k) (k+1 - L)
// !!!: nd[].cnt == 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  up(x); return x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    } else return x + y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void dfs(int u, int fa) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               动态 dp_bst
                                                                                                                                                                                                                                                                                                                                                                            } else x = y = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        else  x = y = 0 ;
                                                         if(!x) return ;
                                                                                                                                                                                                                                                                 x = newcopy(x);
                                                                                                                                                                                                     void gao(int &x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int v = to[i];
                                                                                                                                                                                                                                  if(!x) return
                               void up(int \times) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     dfs(v, u);
// upd f[u]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ;(n)dn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              :(n)dn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   sz[u] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 3.17
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inline void e() { rep(i, 0, 3) rep(j, 0, 3) a[i][j] = (i != j) * (-inf); }
                                                  rep(k, 1, 3) r.a[i][j] = max(r.a[i][j], a[i][k] + c.a[k][j]);
                                                                                                                                                                                                                                                                                                                                                                                                     int mid = 1 + r >> 1; build(mid + 1, r, rs); build(1, mid, ls);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   (id[u] <= mid) ? upd(u, 1, mid, 1s) : upd(u, mid + 1, r, rs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inline void qry(int L, int R, int l, int r, int rt, Mat &ans) {
   if(rt == 1) ans.e();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             struct HeavyChain{
    // if(s) top[s] = top[c], dfs2(s, c, g), leaf[c] = leaf[s];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(L <= 1 && r <= R) return ans = ans * m[rt], void();
int mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Mat tmp; seg.gry(id[x], id[leaf[x]], 1, n, 1, tmp);
11 f0 = max(tmp.a[0][0], tmp.a[0][1], tmp.a[0][2]);
11 f1 = max(tmp.a[1][0], tmp.a[1][1], tmp.a[1][2]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              inline void upd(int u, int 1, int r, int rt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(L <= mid) qry(L, R, l, mid, ls, ans);
if(R > mid) qry(L, R, mid + 1, r, rs, ans);
                                                                                                                                                                                                                         inline void build(int 1, int r, int rt) {
Mat r; rep(i, 0, 3) rep(j, 0, 3) {
    r.a[i][j] = a[i][0] + c.a[0][j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int u = top[v], fa = par[u];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         F[p][1] += c - a[p], a[p] = c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           inline pair<ll, ll> qry(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         seg.upd(v, 1, n, 1);
pair<ll, 11> _f = qry(u);
                                                                                                                                                                                                                                                                                                                                                                                                                              m[rt] = m[ls] * m[rs];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        m[rt] = m[ls] * m[rs];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                           int u = who[1];
// calc F, f
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // else leaf[c] = c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void upd(int p, int c)
                                                                                                                                                                                                                                                                                                                              // set m[rt]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // set m[rt]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return mp(f0, f1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // upd F[fa]
                                                                                                                                                                                                                                                    if(1 = r) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(1 == r) {
                                                                                                                                                                                                                                                                                                                                                          return ;
                                                                                                                                                                         struct Seg {
   Mat m[N << 2];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return ;
                                                                             } return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(fa) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     while(v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int v = p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int sz[N], wson[N], top[N], dep[N], id[N], _, par[N], who[N], leaf[N];
11 f[N][2], F[N][2];
struct Mat {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 inline int upd(int x, int y) {
    access(x); splay(x); nd[x].val.a[1][0] += y - a[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return max(nd[x].sum.a[0][0], nd[x].sum.a[1][0]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(1s) nd[x].sum = nd[1s].sum * nd[x].sum;
if(rs) nd[x].sum = nd[x].sum * nd[rs].sum;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            inline Mat operator * (const Mat &c) const {
                                                                                                                                                                                                                                                                                                                                                                                                                    int n, m, a[N], f[N][2];
namespace DP {
    struct Node { int fa, son[2]; Mat val, sum; };
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for(int y = 0; x; y = x, x = nd[x].fa) {
 // u = fa[x], get h[u], val[u]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          nd[x].son[1] = y; up(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              inline void access(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              splay(x);
if(nd[x].son[1]) {
    // upd val[x]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              nd[x].sum = nd[x].val;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          动态 dp_树链剖分
                                                                                                                             }
// get dp[1] by sum[rt]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     inline void up(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // upd val[x]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     up(x); a[x] = y;
                                                                                                                                                                                                                                                                                                                                                         对态 dp_lct
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int n, a[N]; vi g[N]; namespace DP \{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(y) {
                                                                                                  x = fa[x];
                                                    (x)dn
                         } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 11 a[3][3];
                                                                                                                                                                                                                                                                             bst.build(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                struct LCT .
                                                                                                                                                                                                                         void init() {
                                                                                                                                                                                                                                                        dfs(1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             }lct;
                                                                                                                                                                                                                                                                                                                                                            3.18
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              3.19
                                                                                                                                                                                                    }bst;
```

```
len[0][rt] = (1 == r) ? 0 : len[0][ls] + len[0][rs];
len[1][rt] = (1 == r) ? 0 : len[1][ls] + len[1][rs];
                                                                                                                                                                                                                                                                                         len[1][rt] = (1 == r) ? 0 : len[0][ls] + len[0][rs];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void upd(int L, int R, int C, int l, int r, int rt)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(L <= mid) upd(L, R, c, l, mid, ls);
if(R > mid) upd(L, R, c, mid + 1, r, rs);
                                                                                                             void up(int rt, int 1, int r) {
   if(la[rt] >= 2) {
       len[0][rt] = r - 1 + 1;
       len[1][rt] = r - 1 + 1;
   } else if(la[rt] >= 1) {
|// 这份代码没 down 函数, 感觉有问题
                                                            static const int N = ::N << 2;
                                                                                                                                                                                                                                                                len[0][rt] = r - 1 + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(L <= 1 && r <= R) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int mid = 1 + r >> 1;
                                                                                    int la[N], len[2][N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           up(rt, 1, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            la[rt] += c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     up(rt, 1, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return ;
                                                                                                                                                                                                                                                                                                                          else
                               struct Seg {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             }sed;
                                                                                                                                                                                                                                                                                                                                                                                               * 单点修改,区间查询 -> 单点修改,前缀查询 -> 后缀修改,单点查询
* 树剖路径问题:重链区间修改,轻边暴力维护。轻边深度小的点一定在重链上,深度大的一定是 top
```

线段树优化建图

3.21

 $f[u][0] = _f.fi, f[u][1] = _f.se, v = fa;$

seg.build(1, n, 1);

hc.Build(g);

void work() {

常见转化

3.20

高维偏序 3.23

```
const int N = :: N, M = sqrt(N) + 5, K = 7;
                                                                                                                                                                                                                                                                         // 如果有 02 比较快, 不然可能比较慢要手写 bitset
                                                                                                                                                                                                                                                                                                                                                                                                      vectorpii> V[K];
struct node { int d[K]; } a[N];
void init(int _n, int _k) {
                                                                                                                                                                                                                                                                                                                                                     int n, k, B, pos[K][N];
bitset<N> s[K][M];
                                                                                                                                                                                                                                                                                                     namespace PX{
                                                                                                                                                                                                                                                                                                                                   void link(int l, int r, int rt, int L, int R, int w, int o)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void link(int l1, int r1, int l2, int r2, int w, int n) {
                                                                                                                                                                         int *t = id[rt], *fa = id[rt / 2], mid = 1 + r >> 1;
t[0] = ++tim, t[1] = ++tim, liu(t[0], t[1], 0);
if (rt / 2) liu(fa[0], t[0], 0), liu(t[1], fa[1], 0);
if (1 == r) { p[1] = t[0]; return; }
build(1, mid, ls); build(mid+1, r, rs);
                                                                   void liu(int u, int v, int w) { g[u].pb(mp(v, w)); }
void build(int l, int r, int rt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            }
if (L <= mid) link(l, mid, ls, L, R, w, o);
if (R > mid) link(mid+1, r, rs, L, R, w, o);
                                                                                                                                                                                                                                                                                                                                                        int *t = id[rt], mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            }
// [11, r1] -> [12, r2] weight = w
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              w, 0);
                                                                                                                                                                                                                                                                                                                                                                                                              if (o) liu(t[o], tim, w);
                       static const int N = :: N << 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                        else liu(tim, t[o], w);
                                                                                                                                                                                                                                                                                                                                                                                  if (L <= 1 && R >= r) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            link(1, n, 1, 11, r1,
link(1, n, 1, 12, r2,
                                             int id[N][2], p[N], tim;
struct SegGraph {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ++tim;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       }
}
```

 $a[i].d[j] = lower_bound(all(V[j]), mp(a[i].d[j], i)) - V[j].begin();$

pos[j][a[i].d[j]] = i;

if (i = id * B - 1) s[j][id++] = tmp;

tmp.set(pos[j][i]);

rep(i, 0, n)

bitset<N> tmp; int id = 1

rep(j, 0, k) {

B = sqrt(n);

rep(i, 1, n+1) rep(j, 0, k) cin >> a[i].d[j]; rep(i, 1, n+1) rep(j, 0, k) V[j].pb(mp(a[i].d[j], i)); rep(j, 0, k) sort(all(V[j])); rep(i, 1, n+1) rep(j, 0, k) {

n = _n; k = _k;

覆盖大于 k 次的矩形面积 3.22

// 这里是覆盖次数大于 1 次的

```
friend inline bool operator <= (const SurNum &a, const SurNum &b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                (const SurNum &a, const SurNum &b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             friend inline bool operator == (const SurNum &a, const SurNum &b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         friend inline bool operator != (const SurNum &a, const SurNum &b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    friend inline bool operator < (const SurNum &a, const SurNum &b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     &b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     const SurNum
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      grow(a, b); return SurNum(a.x + b.x, a.k, 0).Simplify();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if (a.op == 1 || b.op == 1) return SurNum(0, 0, 1);
if (a.op == -1 || b.op == -1) return SurNum(0, 0, -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            friend inline SurNum operator —= (SurNum &a, SurNum b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          friend inline SurNum operator + (SurNum a, SurNum b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     SurNum b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      — (SurNum a, SurNum
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           friend inline SurNum operator >> (SurNum a, 11 k)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             friend inline SurNum operator — (const SurNum &a)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                friend inline bool operator > (const SurNum &a,
                                                                                                                                                                                                                                                                                   friend inline int compare(SurNum a, SurNum b)
                                                                                                                                                         SurNum &b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     += (SurNum &a,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return SurNum(—a.x, a.k, —a.op);
                                                                                                                                                       friend inline void grow(SurNum &a,
int k = max(a.k, b.k);
                                                                                                                                                                                                                                                                                                                                                                                                          int opa = sgn(a), opb = sgn(b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   friend inline bool operator >=
                                                                                                                                                                                                                                                                                                                if (a.op < b.op) return -1;
if (a.op > b.op) return 1;
if (a.op != 0) return 0;
                                                     \times *= 111 < kk - k, k = kk
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return compare(a, b) == -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             friend inline SurNum operator
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   friend inline SurNum operator
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return compare(a, b) <= 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return compare(a, b) == 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return compare(a, b) == 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return compare(a, b) i = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return compare(a, b) >= 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                          if (opa < opb) return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (opa > opb) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return sgn(a.x - b.x);
                             if (kk < k) return 0;
                                                                                                                                                                                                                        a.Grow(k), b.Grow(k);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return a = a + b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return a = a - b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return a + (-b)
Simplify();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            grow(a, b);
                                                                                               return 1;
                                                                                     rep(j, 0, k) {
   int ed = lower_bound(all(V[j]), mp(V[j][a.d[j]].fi, n+1)) - V[j].begin() - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (x < y) return Mul(y, x);
if (x < 2) return x && y; int a = 0;
while (x < (1 << (1 << a >) | | x >= (1 << (1 << (a + 1))) a++;
int m = 1 << (1 << a), p = x / m, q = x/m, s = y / m, t = y/m;
int c1 = Mul(p, s), c2 = Mul(p, t) ^ Mul(q, s), c3 = Mul(q, t);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (x < 2) return x && y; int a = 0; while (x < (1 << (1 << a)) || x >= (1 << (1 << (1 + 1))) a++; int m = 1 << (1 << a), p = x / m, s = y / m, t = y%m;
                                                                                                                                                    bitset<N> tmp; int id = ed / B, st = id? (id-1) * B : 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   friend inline int sgn(const SurNum \&a) \{ return <math>sgn(a.x); \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       SurNum(11 x, 11 k, 11 op = 0) :x(x), k(k), op(op) { }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return (m^*(c1^{\wedge}c2)) \wedge c3^{\wedge}nimPow(m / 2, c1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int d1 = nimPow(p, s), d2 = nimPow(p, t);
return (m*(d1^d2)) ^{\wedge} nimPow(m / 2, d1);
                                                                                                                                                                                                                      rep(i, st, ed+1) tmp[pos[j][i]] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  0 ? 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       SurNum(const SurNum &a) { *this = a; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    while (x \% 2 == 0 \&\& k > 0) \times /= 2,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (id) tmp = s[j][id - 1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        SurNum() { x = k = op = 0; }
                                                          bitset<N> ans; ans.set();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              inline bool Grow(int kk) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    namespace Nim {
  int nimPow(int x, int y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int sgn(11 \times) { return !x?
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            inline SurNum Simplify()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int Mul(int x, int y) {
                                                                                                                                                                                                                                                                                                                return ans.count();
                          int qry(node a) {
                                                                                                                                                                                                                                                 ans &= tmp;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             11 x, k; int op;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return *this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    SurNum
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    * 注: 高维硬币游戏
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Nim 积
                                                                                                                                                                                                                                                                                                                                                                                                                                                           Game
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                struct SurNum {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    4.2
```

基础点、 _ D

```
db \; Xm = p[m].x, \; lim = min(solve(1, \; m, \; p), \; solve(m + 1, \; r, \; p)); \\ inplace\_merge(p.begin() + 1, \; p.begin() + m + 1, \; p.begin() + r + 1, \; [&](P \; a, \; P \; b) \}
                                                                                                                                                                                         P rot90() { return P(-y, x); } P rot(db a) { return P(cos(a) * x - sin(a) * y, cos(a) * y + sin(a) * x); }
                             int quad() const { return sign(y) > 0 || (sign(y) == 0 && sign(x) >= 0); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(i, 1, r + 1) if(fabs(p[i].x - Xm) <= lim) V.pb(p[i]);
rep(i, 0, sz(V)) rep(j, i + 1, sz(V)) {
   if(fabs(V[i].y - V[i].y) >= lim) break;
   T dis = (V[i] - V[i]).len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  o = outC(p[i], p[j], p[k]), r = abs(o-p[k]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                sort(all(A), [\&](P a, P b)\{return a.x < b.x;\});
                                                                                                                                                                                                                         向
bool cmp(const pii &a, const pii &b) { // 级角排序
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      o = (p[i] + p[j]) / 2 , r = abs(o-p[j]);
rep(k,0,j) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(sgn(abs(0-p[k])-r) <= 0) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(sgn(abs(o-p[j])-r) \leftarrow 0) continue;
                                                                                                                                                                                                                                                                             int o = a > pii(0, 0), t = b > pii(0, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(sgn(abs(o-p[i])-r) \le 0) continue,
                                                                                                                                                                                                                                                                                                                                                                                                                                                 namespace NearestPoints \{ // sz(A) <= 1e5 \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              db solve(int l, int r, vector<P> &p) {
                                                                                                                           P norm() { return *this / len(); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return solve(0, sz(A) - 1, A);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(1 == r) return 1e100;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      lim = min(lim, dis);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               random_shuffle(p , p + n);
                                                                                                                                                                                                                                                                                                                if(0) = t return 0 < t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return a.y < b.y;});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             db solve(vector<P> A) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int m = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                return det(a, b) > 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          P \circ = p[0]; db r = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          o = p[i], r = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              C Mincir(P *p,int n){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             vector<P> V;
                                                                                                                                                                                                                                                                                                                                                                                                              // 【点集中最近点对】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(j,0,i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return lim;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return C(0, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              // 【最小圆覆盖】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i,1,n) {
struct P {
```

```
向量
```

```
while (op = getDir(S, a, b)) S = ((op == 1) ? S.goRight() : S.goLeft());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (x,x) = 0 & x + = 0 y = x, y + +; else y = x + q > 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 SurNum y; if (x.x \le 0 \& x.k == 0) y = x, y.x—; else y = p + x >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               SurTri(SurNum p, SurNum x, SurNum q) :p(p), x(x), q(q) {} SurTri(const SurTri &a) { *this = a; }
                                                     friend inline SurNum getMid(SurNum a, SurNum b) {
                                                                                                                                                                                                    if (op == 1) { printf("+inf\n"); return; }
                                                                                                                                                                                                                                    if (op ==-1) { printf("-inf \setminus n"); return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               struct SurCalculator {
  int getDir(SurTri S, SurNum a, SurNum b)
  if (a < S.x && S.x < b) return 0;</pre>
                                                                                                                                                                                                                                                                                                                                                                                      scanf("%lld%lld%lld", &a1, &a2, &a3);
return SurNum(a1, a2, a3).Simplify();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (a <= S.x && b <= S.x) return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (a >= S.x && b >= S.x) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               SurNum getValue(SurNum a, SurNum b) {
                                                                                                                                                                                                                                                                printf("%lld/%lld\n", x, 1 << k);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          p.print(), x.print(), q.print();
return a.k += k, a.Simplify();
                                                                                                                                                                                                                                                                                                                            inline static SurNum read() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              printf("\n\nSurTri:\n\n");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    SurTri S(-_inf, _0, _inf);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            SurNum p, x, q;
SurTri() { p = x = q = \_0; }
                                                                                                                                               inline void print() const {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return SurTri(x, y, q);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return SurTri(p, y, x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                } _0(0, 0, 0), _inf(0, 0, 1);
                                                                                                                                                                             printf("SurNum:\n");
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        printf("\nend\n\n")
                                                                                   return a + b >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             SurTri goRight() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            SurTri goLeft() {
                                                                                                                                                                                                                                                                                                                                                               11 a1, a2, a3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return S.x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void print() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     assert(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         struct SurTri {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         SurNum y;
```

 $\label{eq:control_do} \mbox{do } (++(\mbox{det}(\mbox{A[(1+1) \% n]}-\mbox{A[i]}) >= 0 \ \mbox{9 j : i)}) \ \% = n,$

res = max(res, (A[i] - A[j]).len()); while(i != 1 || j != r);

rep(i, 1, n) (A[i] < A[1]) && (1 = i), (A[r] < A[i]) && (r = i)

db res = (A[1]-A[r]).len();

int i = 1, j = r;

int 1 = 0, r = 0;

for(int i = 0; i < n; ds.pb(ps[i++]))int n = sz(ps); if(n <= 1) return ps;</pre>

sort(all(ps)); vector<P> qs;

3

 $\label{eq:miles} \textit{while}(sz(qs) > t \&\& sign(det(qs[sz(qs) - 2], qs.back(), ps[i])) <= 0) qs.pop_back();$

for(int i = n - 2, t = sz(qs); i >= 0; $qs.pb(ps[i-])) {$

db diameter(vector<P> A) if(n <= 1) return 0;

// 【凸包最远点对】

int n = sz(A);

```
return min(min(disToSeg(b, a.s), disToSeg(b, a.t)), min(disToSeg(a, b.s), disToSeg(a,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                p, 1.b) * sign(dot(1.b, p, 1.a)) == 1 ? disToL(1, p) : min((p
                                                                                           db c1 = det(a.t - a.s, b.s - a.s), c2 = det(a.t - a.s, b.t - a.s);
db c3 = det(b.t - b.s, a.s - b.s), c4 = det(b.t - b.s, a.t - b.s);
                                                                                                                                                                                                                                                                                                                                             bool isLS(P a1, P a2, P b1, P b2) { // 判断直线线段是否相交 (端点也算) db c1 = det(a2 - a1, b1 - a1), c2 = det(a2 - a1, b2 - a1);
                                                                                                                                                          return sign(c1) * sign(c2) <= 0 && sign(c3) * sign(c4) <= 0 &&
return sign(c1) ^* sign(c2) < 0 && sign(c3) ^* sign(c4) <
                                                                                                                                                                                     sign(max(a.s.x, a.t.x) - min(b.s.x, b.t.x)) >= 0 &&
                                                                                                                                                                                                                      sign(max(b.s.x, b.t.x) - min(a.s.x, a.t.x)) >= 0 &&
                                                                                                                                                                                                                                                   sign(max(a.s.y, a.t.y) - min(b.s.y, b.t.y)) >= 0 &&
                                                                                                                                                                                                                                                                                   sign(max(b.s.y, b.t.y) - min(a.s.y, a.t.y)) >= 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       p, 1.b) / (1.b - 1.a).len());
                                                                                                                                                                                                                                                                                                                                                                                                              return sign(c1) * sign(c2) <= 0;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        vector<P> convexHull(vector<P> ps)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             1.a).len(\hat{j}, (p - 1.b).len(\hat{j});
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(isSS(a, b)) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          r disToL(L 1, P p) {
return fabs(det(1.a,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return sign(dot(1.a,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              db disToS(L l, P p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          db disToL(L 1, P p)
                                                            bool isSS(L a, L b){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           db disSS(L a, L b)\{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                凸包
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // 【点到线距离】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // 【线到线距离】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // 【求凸包】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         b.t)));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ર્જ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     5.3
                                                                                                                                                                                                                                                                                                                                                                                                              if(sign(a[i] * a[i] - a[j] * a[j] - a[k] * a[k] - a[j] * a[k]) >= 0) return p[i];
                                                                                                                                                                                                                                                                                                             rep(i, 0, 3) a[i] = (p[(i + 2) % 3] - p[(i + 1) % 3]).len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              auto Rand = [&] () { return rand() % 10000 / 5000 * pi; }; P ans(0, 0); rep(i, 0, n) ans = ans + p[i]; ans = ans / n; db len = 0; rep(i, 0, n) len += (ans - p[i]).len(); db t = 100000; // modify
                                                            sqrt((a \land 2 + b \land 2 + c \land 2 + 4 * sqrt(3) * area) / 2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          P np(ans.x + t * sin(ang), ans.y + t * cos(ang));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    db k = 0; rep(i, 0, n) \dot{k} += (np - p[i]).len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(det(p[0], p[1], p[2]) < 0) swap(p[1], 
P q1 = (p[2] - p[0]).rot(pi / 3) + p[0]; 
P q2 = (p[0] - p[1]).rot(pi / 3) + p[1];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(sign(len - k) > 0) ans = np, len = k;
                                                                                                                                                                                                                                                                                                                                          rep(i, 0, 3) {
int j = (i + 1) % 3, k = (i + 2) % 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return isLL(L(q1, p[1]), L(q2, p[2]));
                                                                                                                                                                                                                  if(n = 2) return (p[0] + p[1]) / 2;

if(n = 3) {
                                                                                           如果有重点,大于 2 的直接用模拟退火法
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           曲线
                                                                                                                                                          int n = sz(p); assert(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           直线、
                                                                                                                                                                                       if(n == 1) return p[0];
                                                                                           // 如果有重点, 大于 2 的፤
P fermat(vector<P> p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               db ang = Rand();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           线段、
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      t^* = 0.999
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return ans;
                                                                                                                                                                                                                                                                                     db a[3];
         }
// 【费马点】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              5.2
```

```
db c1 = det(a.t - a.s, b.s - a.s), c2 = det(a.t - a.s, b.t - a.s);
db c3 = det(b.t - b.s, a.s - b.s), c4 = det(b.t - b.s, a.t - b.s);
                                                                                                                                                                                                                                                                                                                                                                                      – a0 * c1) / d;
                                                                                                                                                                                                                                                                                                                            db c1)
                                                                                                                                                  }
P isLL(L 1, db a, db b, db c) { // ax + by + c
                                                                                     db s2 = -\det(12.b - 12.a, 11.b - 12.a);
return (11.a * s2 + 11.b * s1) / (s1 + s2);
                                                        db s1 = det(12.b - 12.a, 11.a - 12.a);
                                                                                                                                                                                                                                                                                                                            db b1,
                                                                                                                                                                                                                                 db v = -(a * 1.b.x + b * 1.b.y + c);
                                                                                                                                                                                                                                                            return (l̀.a * v + l.b * u) / (u + v);
                                                                                                                                                                                                                                                                                                                                                                                return P(b0 * c1 - b1 * c0, a1 * c0
                                                                                                                                                                                                      db u = a * 1.a.x + b * 1.a.y + c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     bool isSSr(const L &a, const L &b){
                                                                                                                                                                                                                                                                                                                       P isLL(db a0, db b0, db c0, db a1,
                                                                                                                                                                                                                                                                                                                                                    db d = a0 * b1 - a1 * b0
                        P isLL(L 11, L 12) {
                                                                                                                                                                                                                                                                                                                                                                                                                                          // 【线相交判定】
// 【直线交点】
```

```
 \begin{split} \mathbf{if}(\mathrm{sgn}((\mathsf{r[i][j+1]} - \mathsf{r[i][j]}) * (\mathsf{r[t][g+1]} - \mathsf{r[t][g]})) < 0 \mid | \ i < t) \\ \mathrm{res}[\mathsf{sz++}] &= \mathsf{pdi}(\mathsf{getLoc}(\mathsf{r[i][j]}) , \ \mathsf{r[i][j+1]} , \ \mathsf{r[t][g]}) , \ 1); \\ \mathrm{res}[\mathsf{sz++}] &= \mathsf{pdi}(\mathsf{getLoc}(\mathsf{r[i][j]}) , \ \mathsf{r[i][j+1]} , \ \mathsf{r[t][g+1]}) , \ -1); \\ \end{split}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rt += ((r[i][j+1] - r[i][j]) * a + r[i][j]) / ((r[i][j+1]-r[i][j]) * b
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            else if(du < 0 && dv >= 0) res[sz++] = pdi(s1 / (s1 + s2) , -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 db s1 = (r[i][j] - r[t][g]) / (r[t][g+1] - r[t][g]);
db s2 = (r[t][g+1] - r[t][g]) / (r[i][j+1] - r[t][g]);
if(du >= 0 && dv < 0) res[sz++] = pdi(s1 / (s1 + s2) , 1);
                                                                                                                                int du = sgn((r[i][j+1] - r[i][j]) / (r[t][g] - r[i][j]));
int dv = sgn((r[i][j+1] - r[i][j]) / (r[t][g+1] - r[i][j]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(cnt == 0 && sgn(res[t].fi - res[t+1].fi)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(b < 0) continue; if(b > 1) b = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(a < 0) a = 0; if(a > 1) break;
db b = res[t+1].fi;
                                                 if(t == i) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             db \ a = res[t].fi;
                                                                                            rep(g,0,r[t].dn) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        sort(res , res + sz);
                                                                                                                                                                                                                                if(!du && !dv)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            cnt += res[t].se;
                                                                                                                                                                                                                                                                                                                                                                                                                             }} else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int cnt = 0; —sz;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      r[i][j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(t,0,sz) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return rt / 2;}
rep(t,0,n) {
                                                                                                                                                                                                                                                                                                                                                                                                                      return (b.y - a.y) * 111 * (c.x - b.x) \le (c.y - b.y) * 111 * (b.x - a.x);
```

if(p.x < h.begin()->se.x || p.x > h.rbegin()->se.x) return

// 插入点,询问点在不在凸包内部(包括边界)

// O(nlogn)

return res // 【动态凸包】 bool ao(Pa, Pb, Pc) { // 包括边界: 小等于

map<int, P> h1, h2;

namespace DCH {

 $if(p.x == 1 \rightarrow se.x) return p.y <= 1 \rightarrow se.y,$

auto 1 = h.lower_bound(p.x);

bool in(map<int, P> &h, P p) {

if(!sz(h)) return 0;

void ins(map<int, P> &h, P p) {

if(in(h, p)) return

h[p.x] = p;

auto pos = h.find(p.x);

return ao(l->se, p, r->se);

auto r = 1-...

三角形 4

5.4

if(ao(11—>se, 1—>se, p)) h.erase(1); **else break**;

auto rr = r; rr++; if(rr == h.end()) break;

auto r = pos; r++; if(r == h.end()) **break**

while(1) {

while(1) {
 auto 1 = pos; if(1 == h.begin()) break; —1;
 auto 11 = 1; if(11 == h.begin()) break; —11;
 auto 11 = 1; if(11 == h.begin()) in the interval in the interval in the interval in the interval inter

```
return A - P(b.y * dC - c.y * dB, c.x * dB - b.x * dC) / d;
                                                                                                                db dB = b.len2(), dC = c.len2(), d = 2 * det(b, c);
                                                                                                                                                                                                                                                                                                                                                                      fz = fz + (p[0] + p[i] + p[i + 1]) * t / 3;
                                                                                                                                                                                                                                                                                                           db t = det(p[0], p[i], p[i + 1]);
                                                   P outC(P A, P B, P C) { // 外心
                                                                                                                                                                                                            baryC(P p[], int n) { // 重心 P fz(0, 0); db fm = 0;
                                                                                  P b = B - A, C = C - A;
                                                                                                                                                                                                                                                                           rep(i, 1, n-1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    多边形
                                                                                                                                                                                                                                                                                                                                                                                                                                          return fz / fm;
                                                                                                                                                                                                                                                                                                                                             fm += t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Š
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         \vec{v}
                                                                                            void ins(int x, int y) { ins(h1, P(x, y)); ins(h2, P(x, -y)); } bool in(int x, int y) { return in(h1, P(x, y)) && in(h2, P(x, -y)); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(sgn(b.x - a.x)) return (p.x - a.x) / (b.x - a.x);
if(ao(p, r->se, rr->se)) h.erase(r); else break;
```

P operator [] (const int&n) {return d[n];}

typedef pair<db,int> pdi;

int n;pdi res[1000005];

db getLoc(P a,P b,P p){

P d[10]; int dn; // d[dn] = d[0]

namespace ConvecIntersection{ //

/ 【凸包交】

const int N = 1005

struct Rec {

```
db polyInter(vector<P> &p, vector<P> &q) {
                                                                                                              if(n < 3 || m < 3) return 0;
                                                                                       int n = sz(p), m = sz(q)
                         // 【平面图欧拉定理】 V + F
                                          // 【简单多边形求面积交】
                                                                                                         res[sz++] = pdi(0,0);res[sz++] = pdi(1,0);
                                                            rep(i,0,n) rep(j,0,r[i].dn){
                                                                                    int sz=0;
                    work() {
                                        db rt=0;
.
용
~
```

return (p.y - a.y) / (b.y - a.y);

II H

rep(j,0,n) if(j!=i&&!(c[i]==c[j])&&overlap(c[j],c[i])) cnt++;

rep(j,0,i) **if**(c[i]==c[j]) cnt++;

vector<E> evt;

int cnt=1;

vector<P> pts=insCC(c[i],c[j]);

if(sz(pts)) {

 $rep(j,0,n) if(j!=i){$

```
bool b1 = sign(s.len2() - r * r) == 1 , b2 = sign(t.len2() - r * r) == 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     (0 =>
                                                                                                                                                                                                                                                                  P p = 1.a - ((1.b - 1.a) * (x / y)), det = (1.b - 1.a) * (sqrt(d) / y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(sign(dot(s - p1, t - p1)) \le 0 \& sign(dot(s - p2, t - p2))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return r * r * (rad(s, p1) + rad(p2, t)) + det(p1, p2);
else return r * r * rad(s, t);
} else if(b1) return r * r * rad(s, p1) + det(p1, t);
else if(b2) return r * r * rad(p2, t) + det(s, p2);
                                                                                                                                                db y = (1.b - 1.a).len2();
db d = x * x - y * ((1.a - a.0).len2() - a.r * a.r);
                                                                                                                                                                                                                                                                                                p1 = p - det, p2 = p + det; // dir : I.a \rightarrow I.b
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          bool f = isCL(C(P(0, 0), r), L(s, t), p1, p2);
if(!f) return r * r * rad(s, t);
                                                                                                                                                                                                                                                                                                                                                                                                                     db areaCT(db r,P s,P t) { // 需要除 2
                                                                                       bool isCL(0 a, L 1, P &p1, P &p2) {
                                                                                                                  db \times = dot(1.a - a.o, 1.b - 1.a);
                                                                                                                                                                                                       if(sign(d) < 0) return 0;
                                                                                                                                                                                                                                                                                                                                                                                       // 【圆与三角形交面积】
                                                                                                                                                                                                                                     d = max(d, 0.);
                                                         // 【直线和圆求交】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(b1 && b2)
return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                     P p1, p2;
                                                                                                                                                                                                                                                                                                                                return 1;
                                                                                                                                                                                                                                                                                                f2 = 1;
                                                                                                                                                                                  1,
                                                                                                                                                                                                                                                                                                                                                                                                                     convexCut(ps, L(q2, q[0]));
db res = f1 == f2 ? area(ps) : —area(ps);
                                                                                                                                                                              if(det(p[0], p1, p2) < 0) swap(p1, p2), f1
                                                                                                                                                                                                                                                                                                if(det(q[0], q1, q2) < 0) swap(q1, q2),
                                                                                                                                                                                                                                                                                                                            vector<P> ps({p[0], p1, p2});
// if(area(p) < 0) reverse(all(p));
// if(area(q) < 0) reverse(all(q));
                                                                                                                                                                                                                                                                                                                                                       convexCut(ps, L(q[0], q1));
                                                                                                                                                                                                         rep(j, 1, m - 1) {
P q1 = q[j], q2 = q[j + 1];
bool f2 = 0;
                                                                                                                                                                                                                                                                                                                                                                                       convexCut(ps, L(q1, q2));
                                                                                                             P p1 = p[i], p\hat{z} = p[i + 1];

bool f1 = 0;
                                                                                       rep(i, 1, n-1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ans += res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return fabs(ans);
                                                             db ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          國
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            6
```

5.6

```
res.pb(c1.0 + (c2.0 - c1.0) * c1.r / (c1.r + c2.r));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           res.pb(c1.0 + (c2.0 - c1.0) * c1.r / (c1.r - c2.r));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    P det = ((p_0 - c.0) * (-c.r * sqrt(d) / x)).rot90();
                                                                                                                                                                                                                          if(sign(dis - fabs(A.r - B.r)) == 1) return 2; if(sign(dis - fabs(A.r - B.r)) == 0) return 1;
                                                                                                                                                                                                                                                                                                                                                                                      bool tanCP(0 c, P p0, P &p1, P &p2) {
    db x = (p0 - c.o).len2(), d = x - c.r * c.r;
    if(d < eps) return 0;</pre>
                                                                                                                                                                                                                                                  if(sign(dis - fabs(A.r - B.r)) == 0) return
                                                                                                                                                         if(sign(dis - (A.r + B.r)) == 1) return 4;
                                                                                                                                                                                         if(sign(dis - (A.r + B.r)) == 0) return 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              vector<P> tanCC(const C &c1, const C &c2) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(sign(dis - fabs(c1.r - c2.r) == 0)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(sign(dis - (c1.r + c2.r)) == 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    P p = (p0 - c.0) * (c.r * c.r / x),
                                                           // 相离4: 外切3: 相交2: 内切1: 内含0:
                                                                                              int relcc(c A, c B) { // 两圆关系
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            db dis = (c1.0 - c2.0).len();
                                                                                                                              db \ dis = (A.0 - B.0).len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       p1 = c.o + p + det;

p2 = c.o + p - det;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   vector<P> res;
                             // 注意相等关系
                                                                                                                                                                                                                                                                                                                                                      // 【点圆切点】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // 【圆圆切点】
// 【两圆关系】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return 1;
                                                                                                                                                                                                                                                                                               return 0;
```

P p;T ang;int delta; E(){} E(P p,T ang,int delta):p(p),ang(ang),delta(delta){} bool operator < (const E&b) const {return ang<b.ang;}</pre>

namespace CircleIntersection{ // ?

/ [國次]

struct E{

ans += areaCT(c.r, u - c.0, v - c.0);

return fabs(ans) / 2;

P u = p[i], v = p[(i + 1) % n];

rep(i, 0, n) {

db areaCPoly(C c, vector<P> p) {

int n = sz(p);

db ans = 0;

}
// 【圆与多边形交面积】 return det(s, t);

bool overlap(C a, C b) {return sgn(a.r-b.r-abs(a.o-b.o))>=0;}

memset(ans , 0 , sizeof(T) * (n+1)); rep(i,0,n) {

void solve(C *c, int n, T *ans)

```
0 0 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Mat rotate(P3 s, db a) { // 绕 s 为轴旋转 a 度, 右手方向 db l = s.len(), x = s.x / l, y = s.y / l, z = s.z / l, si = sin(a), co = cos(a);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      db p[4][4] = {
    co + (1 - co) * x * x, (1 - co) * x * y - si * z, (1 - co) * x * z + si * y, (1 - co) * y * x + si * z, co + (1 - co) * y * y, (1 - co) * y * z + si * z, co + (1 - co) * y * y, (1 - co) * y * z - si * x, (1 - co) * z * x - si * y, (1 - co) * z * y + si * x, co + (1 - co) * z * z, z, 0, 0, 0, 0, 1};
                                                                                                                                                                                                                                                                                                          db p[4][4] = {
    a, 0, 0, 0,
    0, 0, 0,
    0, 0, 0,
    0, 0, 1};
Mat r; rep(i, 0, 4) rep(j, 0, 4) r.a[i][j] = p[i][j]; return r;
                                                                                                                                                                                                                            Mat r; rep(i, 0, 4) rep(j, 0, 4) r.a[i][j] = p[i][j]; return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     4) r.a[i][j] = p[i][j]; return r;
                                                     Mat translate(db tx, db ty, db tz) { // 平移, 以下矩阵均为左乘
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void convexCut(vector<P> &p, db a, db b, db c) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(d1 * d2 < 0) q.pb(isLL(L(p1, p2), 1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i, 0, sz(p)) {
    P p1 = p[i], p2 = p[(i + 1) % sz(p)];
    int d1 = sign(a * p1.x + b * p1.y + c);
    int d2 = sign(a * p2.x + b * p2.y + c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            vector<P> q;
rep(i, 0, sz(p)) {
   P p1 = p[i], p2 = p[(i + 1) % sz(p)];
int d1 = sign(det(1.a, 1.b, p1));
int d2 = sign(det(1.a, 1.b, p2));
if(d1 >= 0) q.pb(p1);
                                                                                                                                                                                                                                                                                    Mat scale(db a, db b, db c) { // 缩放
db p[4][4] = {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void convexCut(vector<P> &p, L 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          o`
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Mat r; rep(i, 0, 4) rep(j,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         HalfPlane
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // 1: a->b 逆时针方向
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // ax + by + c >= 0
                                                                               db p[4][4] = {
1, 0, 0, tx,
0, 1, 0, ty,
0, 0, 1, tz,
0, 0, 0, 1};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    vector<P> q;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     b = d
return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           \infty
                                                                                                                                                                                                                                                                                                                                                                                                                                                         ans[cnt] += ang * c[i].r * c[i].r / 2 — sin(ang) * c[i].r * c[i].r / 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 0, 4) rep(j, 0, 4) rep(k, 0, 4) r.a[i][j] += a[i][k] * c.a[k][j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void set() { rep(i, 0, 4) rep(j, 0, 4) a[i][j] = 0;
void e() { rep(i, 0, 4) a[i][i] = 1; }
                          rep(j,0,2) a[j]=(pts[j]-c[i].o).arg();
                                                                                                                                                                                                                                                                                                                                                                        ans[cnt] += evt[j].p / evt[j+1].p / 2;
                                                                                                                                                                                                                                                                                                                                                                                                  db ang = evt[j + 1].ang - evt[j].ang;
if(ang < 0) ang += pi * 2;</pre>
                                                                                                                                                                                              if(!sz(evt)) ans[cnt] += pi*c[i].r*c[i].r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 db t = 1; P3 ans(0, 0, 0);
rep(i, 0, n) ans = ans + p[i]; ans = ans / n;
                                                     evt.pb(E(pts[0],a[0],1));
evt.pb(E(pts[1],a[1],-1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        db tmp = (p[i] - ans).len();
if(ret < tmp) ret = tmp, j =</pre>
                                                                                                              cnt += a[0] > a[1];
                                                                                                                                                                                                                                                                                                                                             cnt+=evt[j].delta;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ans = ans + (p[j] - ans) * t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Mat operator ^* (const Mat &c) ^{\cdot}
                                                                                                                                                                                                                                                                                    evt.pb(evt.front());
                                                                                                                                                                                                                                                                                                              rep(j, 0, sz(evt)-1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          P3 MinSphere(vector<P3> p) \{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int j = -1; db ret = -1;
                                                                                                                                                                                                                                                         sort(all(evt));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int n = sz(p); assert(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Mat r; r.set();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           while(t > eps) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(i, 0, n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // 【三维向量变换】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                7, 3D
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // 【最小球覆盖】
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             t^* = 0.999
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   db a[4][4];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           struct Mat {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                5.7
```

5.9 HalfPlane_nlogn

if(d1 * d2 < 0) q.pb(isLL(L(p1, p2), a, b, c));

if(d1 >= 0) q.pb(p1);

Mat kpow(Mat a, int b) {
 Mat r; r.set(); r.e();

while(b) {
 if(b & 1) r = r

a = a * a;

b >>= 1;

MaxAreaPoly 5.10

int quad() const { return sign(y) > 0 || (sign(y) == 0 && sign(x) >= 0);

0

(a != 0 || b !=

L(dba, dbb, dbc) { // ax + by + c >= 0,

struct L {

struct P {

if(sign(a)==0) {

```
for (int 1 : vals) area += 1d(1) * sqrt(1d(D) * 1d(D) - 1d(1) * 1d(1)) / 4; 1d hiArea = 1d(hi) * sqrt(1d(D) * 1d(D) - 1d(hi) * 1d(hi) / 4;
                                                                                                                                                                                                                                                                                                                                                                                       for (int 1 : vals) tot += 2 * asin(ld(1) / ld(D));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  while (tooSmall(ma)) numExpand++, ma += (ma - mi);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ld hiAng = 2 * asin(id(hi) / 1d(D));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             else return ang + hiAng >= 2 * PI;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            bool isReflex = (getAngle(hi) < PI);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (isReflex) return ang < hiAng;</pre>
                                                                                                                                                                                                                                                                                                                             auto getAngle = [\&](Id D) \rightarrow Id\{
                                                                                                                                                                            if (cur > hi) swap(cur, hi);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                1d md = mi + (ma - mi) / 2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(tim, 0, 50 + numExpand) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (tooSmall(md)) mi = md;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (isReflex) area —= hiArea;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          auto tooSmall = [\&](ld D)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Id mi = hi, ma = hi + 1;
                                                                                                                                                                                                                                                                                                 if (sum <= hi) return 0;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ld ang = getAngle(D);
                           assert(sz(S) > 0);

int sum = 0, hi = S[0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ld D = mi, area = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      else area += hiArea;
                                                                                                                rep(i, 1, sz(S)) {
    int cur = S[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int numExpand = 0;
ld solve_poly(vi &S)
                                                                                                                                                                                                                                          vals.pb(cur);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            else ma = md;
                                                                                                                                                                                                          sum += cur;
                                                                                                                                                                                                                                                                                                                                                           ld tot = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                     return tot;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return area;
                                                                                         vi vals;
```

bool includer(const P &p) const { return sign(det(b - a, p - a)) > 0; } bool include(const P &p) const { return sign(det(b - a, p - a)) >= 0; }

P det = (b - a).rot90().norm() * len;

// 向内(右手方向)推

L push(db len) {

return L(a + det, b + det)

this->a=P(0,0);**this**->b=P(sign(b), sign(b)*(-a/b));

int x=sign(c)*sign(det(P(-c/a,0), P(0,-c/b))); if(x==1) this->a=P(-c/a,0), this->b=P(0,-c/b);

if(sign(c)!=0) {

this \rightarrow a=P(-c/a, 0); **this** \rightarrow b=P(-c/a, -sign(a)); **this**->a=P(0, -c/b);**this**->b=P(sign(b), -c/b);

} **else if**(sign(b)==0)

else this->a=P(0,-c/b), this->b=P(-c/a,0);

MaxAreaTri5.11

bool check(L u, L v, L w) { return w.include(isLL(u, v)); }

deque<L> halfPlane(vector<L> 1) {

if(sameDir(10, 11)) **return** 11.includer(10.a); **return** (10.b - 10.a) < (11.b - 11.a);

bool operator < (const L &10, const L &11) {

return sign(det(a, b)) == 0 & sign(dot(a, b)) == 1;

P a = 10.a - 10.b, b = 11.a - 11.b;

bool sameDir(L 10, L 11) {

if(a.quad() != b.quad()) return a.quad() < b.quad();</pre>

return sign(det(a, b)) > 0;

const P &b)

bool operator < (const P &a,

P &c)

P &b,

```
while(cur <= (tmp = area(p[i], p[j], p[(k + 1) % n]))) (++k) %= n, cur = tmp; if(cur <= (tmp = area(p[i], p[(j + 1) % n], p[k]))) (++j) %= n, cur = tmp;
                                                                                                                                                                         T res = area(a, b, c), cur = res,
                                                                            void maxAreaTri(P *p, int n, P &a, int i = 0, j = 1, k = 2; a = p[i], b = p[j], c = p[k];
                                                                                                                                                                                                                                                                                                                                        else break;
                                                                                                                                                                                                                                           while(1) {
                                                 // o(n ^{\wedge} 2)
                                                                                          while(sz(q) > 2 && !check(q[sz(q) - 2], q.back(), q[0])) q.pop_back();
while(sz(q) > 2 && !check(q[1], q[0], q.back())) q.pop_front();
                                                          if(i && sameDir(l[i], l[i - 1])) continue;
sort(all(l)); dequec
                                  rep(i, 0, sz(1)) {
                                                                                                                                                               q.pb(1[i])
                                                                                                                                                                                                                                                                                         return q;
```

if(cur > res) a = p[i], b = p[j], c = p[k], res = cur;

cur = area(p[i], p[j], p[k]);

while(i);

MinAreaTri

5.12

if(i == j) (++j) %= n; if(j == k) (++k) %= n;

(++i) %= n;

if(o != t) return o < t;

bool gao(P a) { **return** a.y > 0 || (a.y == 0 && a.x >= 0); } **bool** cmp(P a, P b) {

int n; P p[N], q[N]; 11 s[N];
namespace CNT {

const int N = 1010;

凹四边形计数

5.13

bool o = gao(a), t = gao(b);

if(0 != t) return 0 > t;

return det(a, b) > 0;

5.14 平面图转对偶图

```
P a = ps[i.fi] - ps[V], b = ps[j.fi] - ps[V];
int o = P(0, 0) < a, t = P(0, 0) < b;
                       static const int N = 101010, M = 101010,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   bool cmp(const pii &i, const pii &j) {
                                                                                                                                                                                                                                                                                                  void init() {
    rep(i, 0, sz(ps)) g[i].clear();
                                                                                                                                                                                                                                                                                                                                                     fill_n(vis, cnte, false);
ps.clear(); cnte = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 g[u].pb(mp(v, cnte));
E[cnte++] = mp(u, v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  g[v].pb(mp(u, cnte));
                                                                                                                                                                                                                                                                                                                                                                                                                                                      void adde(int u, int v)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           \mathsf{E}[\mathsf{cnte++}] = \mathsf{mp}(\mathsf{v}, \mathsf{u});
                                                                                               // cnte id starts from
                                                // ps id starts from 0
                                                                                                                                                                                                                                                                                                                                                                                                           areas.clear();
                                                                                                                                                                             // u -> (v, cnte)
                                                                                                                                                                                                    vector<pii> g[N];
                                                                                                                                                                                                                                                       vector<db> areas;
                                                                                                                        int cnte, ne[M];
                                                                          vector<P> ps;
                                                                                                                                                  bool vis[M];
struct Planar {
                                                                                                                                                                                                                            pii E[M]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int V;
```

mi = min(mi, area(p[pu - 1], p[pu], p[pv + 1], p[v]));**bool** cmp(const P &x, const P &y) { return det(x, y) < 0; } else if(1[m].x == $\vec{0}$ && 1[m].y < $\vec{0}$) 1[m].y *= -1; ma = max(ma, area(p[1], p[pu], p[n], p[v])); rep(i, 1, n + 1) p[i].ind = i, pos[i] = i; m = 0; rep(i, 1, n + 1) rep(j, i + 1, n + 1) { l[++m] = p[i] - p[j]; if(1[m].x < 0) 1[m].x *= -1, 1[m].y *= -1;int pu = pos[u], pv = pos[v]; if(pu > pv) swap(u, v), swap(pu, pv); if(pu == 1 || pv == n) continue; cout << mi << " " << ma << endl; mi = inf, ma = 0; rep(i, 1, m + 1) { int u = l[i].u, v = l[i].v; **struct** P { **int** x, y, ind, u, v; }; sort(1 + 1, 1 + 1 + m, cmp);l[m].u = i, l[m].v = j;swap(p[pu], p[pv]); swap(pos[u], pos[v]); sort(p + 1, p + 1 + n);**const** 11 inf = 4e18; namespace MinAreaTri { const int N = 2020; int n, m, pos[N]; P p[N], 1[N * N]; // 无重点、三点共线 void solve() { $// 0(n^{2}\log_{2} 2n)$

- 1; }

```
while(\det(\hat{t}, ps[(p+1) \% n] - ps[p]) > 0) (++p) %= n; while(\det(\hat{t}, ps[(1+1) \% n] - ps[1]) < 0) (++1) %= n;
                                                                                                                                                                                                                                                                                                                                                    while(dot(t, ps[(r + 1) % n] - ps[r]) > 0) (++r) %= n;
                                                                                                                                                                                                                                                                                                                                                                                 11 et = abs(det(ps[p], ps[i], ps[(i + 1) % n]));
11 ot = abs(dot(t, ps[1] - ps[r]));
ans = min(ans, (db)et * ot / t.len2());
                             return min(solve(p, n, q, m), solve(q, m, p, n));
T work(P p[], int n, P q[], int m) {
                                                                                                                                                                            int p = 1, l = 1, r;
rep(i, 0, n) {
P t = ps[i] - ps[(i + 1) % n];
                                                                                                                                                 int n = sz(ps); T ans = 1e18;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ·// 【凸包最小周长外接矩形】
                                                                                   // 【凸包最小面积外接矩形】
                                                                                                                     solve(vector<P> ps) {
                                                                                                                                                                                                                                                                                                                             r = (p + 1) \% n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Graph
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ဗ
                                                                                                                                                                                                                                                                                           void solve(const vector<P> &_ps, const vector<pii> init(); ps = _ps;
  for(auto e : es) adde(e.fi, e.se);
                                                                                                                                            res += det(ps[E[e].se], ps[E[e].fi]); vis[e] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(j, 0, sz(g[i])) {
ne[g[i][j].se] = g[i][(j + 1) % sz(g[i])].se;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(i, 0, cnte) if(!vis[i]) go(i);
                                                                                                                                                                                                                                                                                                                                                                               rep(i, 0, sz(ps)) {
    V = i; sort(all(g[i]), cmp);
                                                                                                                                                                                                                                     if(res > 0) areas.pb(res / 2);
  return det(a, b) > 0;
                                                                                                                   while(!vis[e]) {
                                                                                                                                                                              e = ne[e \land 1]
                                                      void go(int e) {
```

```
void add_set(int a, int va) { a = a << 1 | va; g[a ^ 1].pb(a); } // va 必选
void add_then(int a, int va, int b, int vb) { // va 和 vb 不能同时取
addedge(a, va, b, vb ^ 1);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            void add_xor(int a, int va, int b, int vb) { // va 和 vb 同时取或同时不取
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void add_or (int a, int va, int b, int vb) { // va 和 vb 不能同时不取
                                                                                                                                                                                                                                                                                                                                                     void addedge(int a, int va, int b, int vb) { // va 选了 vb 必选
                                                                                                                                                                                                                                                    void init(int _n) { per(i, 0, (n = _n << 1)) g[i].clear(); }
int new_node() { rep(i, 0, 2) g[n++].clear(); return n / 2 -</pre>
                                                                                                                                                                   int dfn[N], low[N], id[N], st[N], _st,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int a = vu[i].fi, va = vu[i].se;
                                                                                                                                                                                                                                                                                                                                                                                 a = a \ll 1 \mid va; b = b \ll 1 \mid vb;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void add_at_most_one(vector<pii> vu)
                                                                                                                                                                                                                                                                                                                                                                                                                g[a].pb(b); g[b ^ 1].pb(a ^ 1);
                                                                                                                                       static const int N = ::N << 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 addedge(a, va \land 1, b, vb);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // 需要 sz(vu) 个额外的 dp 变量
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int dpi = new_node();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             addedge(a, va, b, vb); addedge(b, vb, a, va);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, 0, sz(vu)) {
                                                                                                                                                                                                                                                                                                                        /// optionals begin
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int pre = -1;
                                                                                                                                                                                                                            int mark[N], n;
                                 2-sat
                                                                                                        struct TwoSat
                                                                                                                                                                                                    vi g[N];
                                 6.1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(sign(tmp)) ans = min(ans, disToSeg(L(p[o], p[(o + 1) % n]), q[t]));
else ans = min(ans, disSS(L(p[o], p[(o + 1) % n]), L(q[t], q[(t + 1) % m])));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     P a = p[(0 + 1) % n] – p[0]; db tmp; while((tmp = det(a, q[(t + 1) % m] – q[t])) < 0) (++t) %= m;
                                                                                                                                                                                                                                                                                                                        while(det(t, ps[(p + 1) % n] - ps[p]) > 0) (++p) %= n;
                                                                                                                                                                                                                                                                                                                                                                                 ans = max(ans, (ps[(i + 1) %n] - ps[p]).len());
                                                                                                                                                                                                                                                                                                                                                ans = max(ans, (ps[i] - ps[p]).len());
                                                                                                                                                                                                if(n <= 1) return 0;
if(n == 2) return (ps[1] - ps[0]).len();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 1, n) if(p[i].y > p[o].y) o = i;
rep(i, 1, m) if(q[i].y < q[t].y) t = i;
rep(i, 0, n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // [凸包间的最小距离』
|T solve(P p[], int n, P q[], int m) {
| int o = 0, t = 0; T ans = inf;
| int o = 0, t = 0; T ans = inf;
                                                                                                                                                                                                                                                                                          P t = ps[i] - ps[(i + 1) % n];
                                                                                                                                  T diameter(vector<P> ps)
                                                                                                                                                              n = sz(ps); T ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         【凸包间的最大距离】点
【凸包间的最小距离】
                                                                                                     //【凸包直径】点 一 点
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                }
//【凸包宽度】点 - 边
                                                                       // 凸包都是顺时针给出
旋转卡壳
                                                                                                                                                                                                                                                             rep(i, 0, n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       (++0) %= n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                 return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return ans;
```

```
11 f[N][5], du[N], D[N], cnt4[N], cnt3[N], cnt1[N], t, ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i, 0, n) for(auto j:g[i]) if(id[i]!=id[j.fi])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for (auto v : g[u]) if (v != fa) dfs(v, d+1, u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void dfs(int u, int d, int fa) {
   if (d == 2) { d2.pb(u); w[u].pb(fa); return; }
   if (d == 1) d1.pb(u), vis[u] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                               if(low[t]>dfn[c]) key.pb(e.se);
} else if(dfn[t] != dfn[c] - 1 || cc++)
                                                                                                                                                                                                                               int dfn[N] , low[N] , id[N] , st[N] , _st , _;
void dfs(int c,int dep,vector<pii> g[]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        do{id[st[---st]]=_;}while(st[_st]!=c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 low[c] = min(low[c], dfn[t]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      四元环数量
                                                                                                                                                                                                                                                                                                                                                                                                                             low[c]=min(low[c],low[t]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i,0,n) if(!dfn[i]) dfs(i,1,g);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int solve(int n, vector<pii> g[]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      bcc[id[i]].pb(id[j.fi]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // cnt3,4 中为包含 i 号点的三 ,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 static const int N = 1e5 + 7;
                                                                                                           // key contains the id of edges
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            fill_n(bcc, n, key=vi());
                                                                                                                                                                                                                                                                                                                                                                                                        dfs(t, dep+1, g);
                                                                                                                                                                                                                                                                                   int cc=0;st[_st++]=c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       fill_n(low, n, _st=0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(low[c]==dfn[c]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               fill_n(dfn,n,_=0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      priority_queue<pii> q;
vi w[N], gg[N], d2, d1;
                                                                                                                                                                                                                                                                                                      dfn[c]=low[c]=dep;
                                                                                                                                                                                                                                                                                                                                 for(auto e:g[c]){
                                                                                                                                                                                const int N = 202020;
                                                                                                                                                                                                                                                                                                                                                                          if(!dfn[t]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int n, m, u, v, x, y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               CircleCount
                                                                                                                                                                                                                                                                                                                                                          int t=e.fi;
                                                                                                                                                                                                          vi key, bcc[N];
                                                                                                                                    // _ starts from 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 set<int> g[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return _;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           struct circle4 {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              bool vis[N];
                                                                                                                                                            namespace BCC{
                                                  BCC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               6.3
                                                     6.2
}ts;
```

```
if(!dfn[t]) dfs(t, g), low[c] = min(low[c], low[t]);
else if(!id[t]) low[c] = min(low[c], dfn[t]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(j, 0, tot) col[ans[j]] = col[ans[j] \wedge 1] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for (int i = 0; i < n; i += 2) if (!col[i])
                                                                                                                                                                                                                                                                                                                                                                                                                       do{id[st[--st]]=_;}while(st[_st] != c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for (auto \ v : g[u]) if (dfs(v)) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (id[i] == id[i + 1]) return 0;
mark[i >> 1] = (id[i] > id[i + 1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(i, 0, n) if(!dfn[i]) dfs(i, g);
                                                                          addedge(pre, 1, a, va ^{\wedge} 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (int i = 0; i < n; i += 2) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (!dfs(i ^ 1)) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    bool solve2() { // 构造字典序最小解
                                                   addedge(pre, 1, dpi, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     col[u] = 1; col[u \land 1] = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (col[u] == -1) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (col[u] == 1) return 1;
addedge(a, va, dpi, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               bool solve() { // 构造任意解
                                                                                                                                                                                                                                           dfn[c] = low[c] = ++cc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               fill_n(low, n, _st=0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void find(){
  fill_n(dfn, n, cc=0);
                                                                                                                                                                                                                          void dfs(int c, vi g[]){
                                                                                                                                                                                                                                                                                                                                                                   if(low[c] == dfn[c]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int col[N], ans[N], tot;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 0, n) —id[i],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       fill_n(id, n, _=0);
                                                                                                                                                                                                                                                                                           for(auto t : g[c])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (!dfs(i)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ans[tot++] = u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      bool dfs(int u) {
                                                                                                                                                                                                                                                                          st[\_st++] = c;
                                                                                                                                                                                                // optionals end
                                                                                                                         pre = dpi;
                        if (i)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        find();
```

```
// can handle isolate point and not connected graph and muti edge // can handle self circle ?
                                                                                                                                                                                                                                                                                                                                                                                                           while(st[--st]!=t) dcc[st[_st]].pb(_);
dcc[c].pb(_);dcc[t].pb(_++);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   }
int solve(int n, const vi g[]){// n is size of points
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, 0, n) if(sz(dcc[i]) == 0) dcc[i].pb(_++);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        } else if(dfn[t] != dfn[c] - 1 || cc++)
low[c] = min(low[c] , dfn[t]);
                                                                                                                                                                                                                                                                                                                                                                                if(++out==2) key.pb(c);
                                                                                                                                                                                                                                                                                                                           low[c]=min(low[c],low[t]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(i,0,n) if(!dfn[i]) dfs(i,1,g);
                                                                                                                                 int dfn[N] , low[N] , st[N] , _st , _
void dfs(int c,int dep,const vi g[]){
                                                                                                                                                                                        int cc=0,out=1<dep;st[_st++]=c;</pre>
                                                                                                                                                                                                                                                                                                                                                      if(low[t]>=dfn[c]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       fill_n(dcc, n, key=vi());
                                                                                                                                                                                                                                                                                                  dfs(t, dep+1, g);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              fill_n(low, n,_st=0);
                                                                                                                                                                                                                   dfn[c]=low[c]=dep;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   fill_n(dfn, n, _=0);
                                                                             const int N = 202020;
                                                                                                                                                                                                                                                for(auto t:g[c])
                                                                                                                                                                                                                                                                     if(!dfn[t]){
                                                                                                          vi key, dcc[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return _;
                                                      namespace DCC{
```

rep(i, 1, 5) rep(j, 1, n+1) for (auto v : gg[j]) f[j][i] += f[v][i-1];
while (!q.empty()) {
 x = q.top().se; y = q.top().fi; q.pop();
 if (du[x] != y) continue;

rep(j, 1, 5) f[i][j] = 0; f[i][0] = 1;

rep(i, 1, n+1) q.push(mp(du[i], i)); rep(i, 1, n+1) {

D[i] = du[i] = sz(gg[i]); cnt3[i] = cnt4[i] = 0;

void solve(int n, vi gg[]) {

rep(i, 1, n+1) {

for (auto v : gg[i]) g[i].insert(v);

for(auto u : d1) vis[u] = 0; d1.clear(); d2.clear();

for (auto u : g[x]) {
 q.push(mp(—du[u], u));

g[u].erase(x);

cnt3[x] += t / 2; t = 0;

//以第一次产生重复位置分类计数

if (vis[u]) cnt3[v]++, t++;

For (auto $\vee : w[u]$) {

dfs(x, 0, -1);for (auto u : d2) { 11 s = sz(w[u]); cnt4[v] += s - 1;

cnt4[x] += s * (s - 1) / 2; cnt4[u] += s * (s - 1) / 2;

w[u].clear();

```
#define FOR(i, ne, t) for(int i = ne[t]; i != t; i = ne[i])
static const int N = 2e4 + 8, D = 4, len = 16;
int n, m, tim, ansd, row[N], col[N], s[N], ans[N], l[N], u[N], d[N];
                                                                                                                                                                                                                                                                           rep(i, 0, m+1) l[i] = i-1, r[i] = i+1, u[i] = d[i] = i; l[0] = m, r[m] = 0, tim = m+1; rep(i, 0, m+1) s[i] = 0;
                                                                                                                                                                                  pair<pii, int> pos[N]; string ss[100];
void init(int _m) {
                                                                                                                                                                                                                                                                                                                                                                                                         void add(int R, const vi &tmp){
                                                                                                                                                                                                                                                                                                                                                                                                                                      int first = tim;
rep(i, 0, sz(tmp)) {
  int c = tmp[i];
                                                                                                                                                                                                                                                    .
| = m
                                                   struct DLX{
                                                                                                                                                                                                                                     ans == 2 * cnt3[i] * D[i]; for (auto v : gg[i]) ans == (D[v] - 1) * D[v]; //第一次重复为第 2 步
                                                                                                                                   for (auto v : gg[i]) ans3 -= D[v] - 1; ans -= ans3; // 边数为 3 的链数 for (auto v : gg[i]) ans -= 2 * cnt3[v]; ans += 4 * cnt3[i];
                                                                                                       ans -= cnt4[i] * 2; 11 ans3 = f[i][3] - D[i] * D[i] - 2 * cnt3[i];
rep(i, 1, n+1) { // 计算边数为 4 的链数
ans = f[i][4];
                                                                                                                                                                                                                                                                                                      ans -= D[i] * f[i][2];
                                                                       //第一次重复为第 4 步
                                                                                                                                                                                                     //第一次重复为第3步
                                                                                                                                                                                                                                                                                                                                      cntl[i] = ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                    } c4;
```

DCC 6.4

```
// dcc i \rightarrow j , i(points) , j(bcc\_block)
// cactus: n multi by 2
                                                                                                _st is top of stack
                                                                                                                              _ is number of dcc
                        // key is cuts
                                                                          // st is stack
```

l[tim] = tim-1, r[tim] = tim+1, u[tim] = u[c], d[tim] = c;

u[c] = tim; d[u[tim]] = tim;row[tim] = R, col[tim] = c;

tim++, s[c]++;

if (sz(tmp)) 1[first] = tim-1, r[tim-1] = first;

```
 \textbf{void} \  \  \, \text{addedge(int u, int v, int d) } \{e[m] = edge(\{u,v,d,u,v\}); \ e[m].reset();e[m].b[m] 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int u = e[i].u, v = e[i].v;
if(e[i].d < in[v] && u := v) in[v] = e[i].d, pre[v] = u, index[v] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int t = index[i]; while(vis[v] != i && id[v] == -1 && v!=root) vis[v] = i, v = pre[v];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(e[i].u != e[i].v) {e[i].d -= in[v];e[i].b ^= e[index[v]].b;}
                                                                                                               static const int N = ::N , M = N * N , inf = 2e9; edge e[M];int n, m, vis[N], pre[N], id[N], index[N], Pre[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for(int u=pre[v];u != v;u = pre[u]) id[u] = cnt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                e[i].u = id[e[i].u]; e[i].v = id[e[i].v];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, n) if(id[i] == -1) id[i] = cnt++; rep(i, 0, m) {
                                                     struct edge {int u, v, d, U, V;bitset<1005> b;};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(v != root && id[v] == -1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         memset(vis, -1, sizeof(*vis)*n);
                                                                                                                                                                                                                                     void ini(int n) {this->n = n, m = 0;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       memset(id, -1, sizeof(*id)*n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ans += in[i]; int v = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(in[i] == inf) return
                         // can handle multi edge, self ring
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(i == root) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 fang ^{\wedge}= e[index[i]].b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int cnt = 0;in[root] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                               rep(i, 0, n) in[i] = inf;

rep(i, 0, m){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          n = cnt; root = id[root];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      id[v] = cnt++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(cnt == 0) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int v=e[i].v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(i, 0, n){
                                                                                                                                                                           bitset<1005> fang;
                                                                                                                                                                                                                                                                                                                           int run(int root){
// id starts from 0
                                                                                                                                                                                                                                                                                                                                                              int ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                          while(1){
                                                                                                                                                                                                            int in[N];
                                                                                     struct DMST{
                                                                                                                                                                                                                                                                                                      1;m++;}
```

} return ans;

Dinic

6.7

} dmst;

$\overline{\mathrm{DMST}}$ 6.6

```
FOR(i, d, c) FOR(i, r, i) u[d[i]] = u[i], d[u[i]] = d[i], --s[col[i]];
                                                                                                                          FOR(i, u, c) FOR(j, l, i) u[d[j]] = j, d[u[j]] = j, ++s[col[j]], l[r[c]] = c; r[l[c]] = c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 1, len+1) {
   if (i > 1) cin >> ss[i];
   rep(j, 1, len+1) {
    if (ss[i][j-1] == '-') rep(k, 1, len+1) ins(i, j, k);
   else ins(i, j, ss[i][j-1] - 'A' + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      n++; pos[n] = mp(mp(x, y), c);

int p = ((x - 1) / D * D + (y - 1) / D) * 1en + c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  tmp[0] = ((x-1)*len + y);
tmp[1] = (len*len*1 + (x-1)*len + c);
tmp[2] = (len*len*2 + (y-1)*len + c);
tmp[3] = (len*len*3 + p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(i, 1, len+1) cout << ss[i] << endl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              SS[x][y - 1] = c + 'A' - 1;
                                                                                                                                                                                                                                                              int c = r[0];
FOR(i, r, 0) if (s[c] > s[i]) c =
                                                                                                                                                                                                                                  if (!r[0]) return ansd = dep, 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                              FOR(j, l, i) restore(col[j]);
                    l[r[c]] = l[c]; r[l[c]] = r[c];
                                                                                                                                                                                                                                                                                                                                                                                          FOR(j, r, i) remove(col[j]);
if (dance(dep+1)) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                while (cin >> ss[1]) {
    n = 0; init(len * len * 4);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            void ins(int x, int y, int c) {
                                                                                                  inline void restore(int c) {
inline void remove(int c) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 1, ansd) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  bool ok = dance(1);
                                                                                                                                                                                                                                                                                                                                      FOR(i, d, c) {
ans[dep] = row[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  restore(c); return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  cout << endl;
                                                                                                                                                                                                        bool dance(int dep) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          tmp.resize(4);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if (ok) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                add(n, tmp);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void work() {
                                                                                                                                                                                                                                                                                                                    remove(c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                vi tmp;
```

```
per(j, 0, sz(buf[p])) {
   int v = buf[p][j]; find(v);
   if (sem[v] == sem[mins[v]]) dom[v] = sem[v]; else buf2[v] = mins[v];
                                                                                                                                                                if (~mins[v] && dfn[sem[mins[v]]] < dfn[sem[mins[u]]]) mins[u] = mins[v];</pre>
for (auto v : g[u]) if (vis[v] != stamp) fa[v] = u, dfs(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ord.clear(); ++stamp; dfs(s); for (auto u : ord) fs[u] = u, mins[u] = buf2[u] = -1;
                                                                                                                                                                                                                                                                                                                                                                               for(auto v : revg[u]) if (vis[v] == stamp) {
   if (dfn[v] > dfn[u]) find(v), v = sem[mins[v]];
   if (dfn[v] < dfn[sem[u]]) sem[u] = v;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 对偶图最小生成构, 等于平面图所有边边权和减去平面图最大生成树
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         buf[sem[u]].pb(u); mins[u] = u; fs[u] = p;
                                                                                                                                                                                                                                                                                                                           per(i, 1, sz(ord)) {
   int u = ord[i], p = fa[u]; sem[u] = p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for( ; p[u] < sz(g[u]); ++p[u])
auto v = g[u][p[u]];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                vi ans; bool vis[N]; int p[N];
                                                                            if (u == fs[u]) return u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              vis[abs(v.se)] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(!vis[abs(v.se)]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             EulerianPath
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              dom[ord[0]] = ord[0];
                                                                                                                                  fs[u] = find(fs[u]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ans.pb(-v.se);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               buf[p].clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   DualMST
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           dfs(v.fi);
                                                                                                                                                                                                                                                 void mark(int s) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void dfs(int u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           vector<pii> g[N];
                                                                                                          int v = fs[u];
                                                                                                                                                                                             return fs[u];
                                                      int find(int u)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               6.10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   6.9
                                                                                                                                                     int s , t , n , h[N] , cur[N] , lv[N] , q[N] , e , ne[M] , to[M];
T cap[M] , flow;
void liu(int u,int v,T w){ to[e] = v;ne[e] = h[u];cap[e] = w;h[u] = e++;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 T flow = dfs(to[k], min(mx, cap[k]));
ret += flow;cap[k] -= flow, cap[k^1] += flow;mx -= flow;
                                                                                                                                                                                                                                void link(int u,int v,T w){ liu(u , v , w);liu(v , u , 0);}
void ini(int _n = N) { fill(h , h + (n=_n) , -1);e = 0;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for(int &k = cur[c]; -k; k = ne[k]){
   if(lv[to[k]] == lv[c] + 1 && cap[k] > 0){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          lv[q[R++] = to[k]] = lv[c] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                    for(int k = h[c]; ~k ; k = ne[k])
if(cap[k] > 0 && !~lv[to[k]])
                                                                                                                            const static int N = 10101, M = N * 10;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(!mx) return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              flow += dfs(s, ~0U>>1);
                                                                                                                                                                                                                                                                                                                                            fill(lv , lv + n , -1);
lv[q[R++] = s] = 0;
while(L < R && !~lv[t]){
int c = q[L++];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       copy(h, h + n, cur);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(c == t) return mx;
                                                                                                                                                                                                                                                                                                                   int L = 0, R = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       T run(int _s, int _t){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    S = _S , t = _t;
flow = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  T dfs(int c,T mx){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return ~lv[t];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        while(bfs()){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return flow;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          [v[c] = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return ret;
                                                 donple need eps
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          T ret = 0;
                                                                          template<class T>
                                                                                                                                                                                                                                                                                          bool bfs(){
                    // [0,n] init!!
                                                                                                     struct Dinic{
```

.11 FindCircle

vis[u] = stamp; dfn[u] = sz(ord); ord.pb(u);

void dfs(int u) {

vi revg[N], g[N], buf[N], ord;
int stamp, vis[N], dfn[N], fa[N];
int fs[N], mins[N], dom[N], sem[N], buf2[N];

DominatorTree

6.8

const int N = 1e5 + 7;

```
if (dep[u] < dep[v]) swap(u, v);
per(i, 0, M) if (dep[f[u][i]] >= dep[v]) res = min(res, h[u][i]), u = f[u][i];
per(i, 0, M) if (f[u][i] != f[v][i]) res = min(res, min(h[u][i], h[v][i])), u = f[u][i], v = f[v][i];
                                                                                                                                                                                                                                                                                                                                                                                                                                        Lindstrom Gessel Viennot Lemma
                                                                                                                                                                                                                                                                          if (u != v) res = min(res, min(h[u][0], h[v][0]));
                                                        void build() { solve(1, n); dfs(1, 0); } int get(int u, int v) { //  注意 Long long
                                                                                                                        int res = pw(30);
                                                                                                                                                                                                                                                                                                           return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                        6.13
                                                                                                                                                                                                                                                                                                                                        }
} tr;
                                                                                                                                                                                                                                                                                                                                                                                                                                 if (sz(cir[k]) > 1 && ne[cir[k][0]] != cir[k][1]) reverse(all(cir[k]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (!dfn[v]) {fa[v] = u; d[v] = d[u] + w; dfs(v, g[u][i].se);}
                                                                                                                                                                                                                                                                                                                                   int p = u; cir[k].pb(p); id[p] = k;
if (p != v) {do { p = fa[p]; cir[k].pb(p); id[p] = k;
                                                                                                                                                                                                             if (g[u][i].se == pre) continue;
int v = g[u][i].fi.fi, w = g[u][i].fi.se;
if (dfn[v] && dfn[v] <= dfn[u]) {</pre>
                                                                                                                     void dfs(int u, int pre) { // pre 为边编号
  곳
int tim, dfn[N], fa[N], d[N],
                                                      int ne[N]; // 有向图的出度
int id[N]; // 点属于的环编号
                                                                                                                                                                                                                                                                                                                                                                                                   while (p != v);}
                                                                                                                                                    dfn[u] = ++tim;
rep(i, 0, sz(g[u])) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  continue;
                              vi cir[N];
```

.12 Gomory-HuTree

```
void ini(int_n) { n = _n; G.ini(n + 5); rep(i, 1, n+1) id[i] = i, g[i].clear(); }
void link(int u, int v, int w) { G.link(u, v, w); G.link(v, u, w);}
                                                                                                                                                                                                                                                                          int s = id[1], t = id[1+1];
for(int i = 0; i < G.e; i + = 2) G.cap[i] += G.cap[i+1], G.cap[i+1] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              h[v.fi][i] = min(h[v.fi][i-1], h[f[v.fi][i-1]][i-1]);
                                                       static const int N = 1e5 + 100, M = 17; // (1 << M) > n
                                                                                       int id[N], tmp[N], n, f[N][M], h[N][M], dep[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (G.lv[id[i]] != -1) id[cl++] = id[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(i, 1, M) {
f[v.fi][i] = f[f[v.fi][i-1]][i-1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for (auto v : g[u]) if (v.fi != fa) {
  f[v.fi][0] = u; h[v.fi][0] = v.se;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 0, cr) id[cl + i] = tmp[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   else tmp[cr++] = id[i]
                                                                                                                                                                                                                void solve(int l, int r) {
  if (1 == r) return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void dfs(int u, int fa) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        dep[u] = dep[fa] + 1;
                                                                                                                                                                                                                                                                                                                                           int w = G.run(s, t);
                                                                                                                                                                                                                                                                                                                                                                                                                                       int cl = 1, cr = 0; rep(i, 1, r+1) {
                                                                                                                                                                                                                                                                                                                                                                           g[s].pb(mp(t, w));
                                                                                                                                                                                                                                                                                                                                                                                                          g[t].pb(mp(s, w));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             solve(1, c1 - 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  dfs(v.fi, u);
                                                                                                                      vector<pii> g[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               solve(cl, r);
Dinic<int> G;
                             struct GHT
```

6.14 ManhattanDistance

```
(x, y) \rightarrow (x + y, x - y) Manhattan distance \rightarrow Chebyshev distance (x, y) \rightarrow (x + y) \rightarrow (x + y) \rightarrow (x + y) Chebyshev distance \rightarrow Manhattan distance
```

6.15 ManhattanDistanceMST

```
per(i, 1, n+1) link[link[i]] = i; rep(i, 1, n+1) if (!link[i]) vis[i] = use[i] = 1, Q.push(i);
                                                                                                                                                                                                                                                                                                                                                                        rep(i, 1, n+1) if (link[i] && !use[link[i]]) use[i] = 2;
                                                                                                                                                                       if (!vis[v]) vis[v] = 1, 0.push(v);
                                                                                                                                                                                                                                                                                                   if (!vis[v]) vis[v] = 1, Q.push(v);
                                            while (!Q.empty()) {
  int u = Q.front(); Q.pop();
  if (use[u] == 1) {
                                                                                                                         for (auto v : g[u]) {
    use[v] = 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           BK
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       typedef unsigned long long T;
                                                                                                                                                                                                                                               int v = link[u];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Max clique
                                                                                                                                                                                                                                                                          use[v] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // g[i][i] should be
// g[i] is i's edge
// index [0..N)
                                                                                                                                                                                                                           }else {
                                                                                                                                                                                                                                                                                                                                                                                                       return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // 0(n ^ 3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           6.17
                                                int F(int x) { return lower_bound(all(V), x) - V.begin() + 1; }
void _solve(vector<pair<pre>cpii, int> > v) {
                                                                                                                     rep(i, 0, sz(v)) v[i].fi.se -= v[i].fi.fi, V.pb(v[i].fi.se);
                                                                                                                                                                                                                                                                                                                          int s = u.fi.fi * 2 + u.fi.se;
if(t.se != inf) E.pb(mp(t.fi - s, mp(t.se, u.se)));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 0, sz(v)) swap(v[i].fi.fi, v[i].fi.se);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                _solve(v);
rep(i, 0, sz(v)) swap(v[i].fi.fi, v[i].fi.se);
                                                                                                                                                                                                                                                                                                                                                                                                                                                     void solve(vector<pair<pre>rpairroid v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 0, sz(v)) v[i].fi.fi *= -1;
                                                                                                                                                                       V.erase(unique(all(V)), V.end());
                                                                                                                                                                                                                                                                                                                                                                          upd(F(u.fi.se), mp(s, u.se));
                                                                                                                                                                                                                                                                                                   pii t = qry(F(u.fi.se));
                                                                                                                                                                                                                                                    init();
for(auto u : v) {
                                                                                                                                                                                                                           reverse(all(v));
                                                                                                                                                    sort(all(V));
                                                                                                                                                                                                    sort(all(v))
 return ans;
                                                                                                V.clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              _solve(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              _solve(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             solve(v);
```

int link[N], vis[N], use[N], in[N];
queue<int> Q;

const int N = 1050;

namespace MaxMatch

6.16 MaxMatch

int dfs(int u, vi g[]) {
 for(auto v : g[u]) {
 if(!vis[v]) {

vis[v] = 1;

18 Max clique fastest

```
typedef bool BB[N];
                                                                                                                                                                                                                                                                                                                                 struct Maxclique {
                                                                                                                                                                                                                                                                                     const int N = 130
                                                                                                                                                                                                                                 6.18
if(!link[v] || dfs(link[v], g)) { return link[v] = u, 1; }
                                                                                                           int solve(int n, int m, vi g[]) {
                                                                                                                                                                         rep(i, 1, n+1) {
fill_n(vis, m+1, 0);
                                                                                                                                                                                                                                                                                                         void MVC(int n, vi g[]) {
  fill_n(vis, n+1, 0);
                                                                                                                                                                                                                  ret += dfs(i, g);
                                                                                                                               fill_n(link, m+1,
                                                                                                                                                     int ret = 0;
                                                                                                                                                                                                                                                                 return ret;
                                                                 return 0;
```

MinCostMaxFlow 6.19

```
void ini(int _n = N){ fill(h , h + (n=_n) , -1);e = 0;}
void liu(int u,int v,U c,V w){ to[e] = v;ne[e] = h[u];cap[e] = c;cost[e] = w;h[u] =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for(p = t;p != s;p = to[k^1]) p1 = min(p1, cap[k = pre[p]]);
for(p = t;p != s;p = to[k^1]) cap[k = pre[p]] -= p1, cap[k^1] += p1;
                                                                                                                                                                                                                                                                          void link(int u,int v,U c,V w){ liu(u,v,c,w);liu(v,u,0,-w);
                                                                                                                                                                                                                                                                                                                                                                                                                                                           int c = Q.front(); Q.pop(); ing[c] = 0;
for(int k = h[c]; -k; k = ne[k]) if (cap[k] > 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(!ing[v]) Q.push(v), ing[v] = 1;
                                                                                                                          s, t, n;
                                                                                                                   int h[N], ing[N], pre[N], to[M], ne[M], e,
U cap[M]; V dis[N], cost[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(dis[c] + cost[k] < dis[v])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   dis[v] = dis[c] + cost[k]
                                                                                       static const int N = 6000, M = 201010;
                                                                                                                                                                                                                                                                                                                                                                                                  Q.push(s), ing[s] = 1, dis[s] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       _t){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        U pl = inf; int p, k;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return mp(flow, mincost);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  mincost += pl * dis[t];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      pre[v] = k;
                                                                                                                                                                                                                                                                                                                                                                    fill(dis, dis+n, inf);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int v = to[k];
// [0,n) , init!! , inf modify
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     pair<U, V> run(int _s,int
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return dis[t] != inf;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 s = \_s, t = \_t;
flow = mincost = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                   while(!Q.empty()){
                         template<class U, class V>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                flow += pl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              while(spfa()){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    U flow; V mincost;
                                                                                                                                                                                                                                                                                                                                          queue<int> 0;
                                                                                                                                                                                                                                                                                                           bool spfa(){
                                                               struct MCMF{
                                                                                                                                                                                                                                                  6++;}
```

```
int dfn[N], low[N], id[N], st[N],_st,_,cc;
                                                              void dfs(int c, vi g[]){
                                                                                     dfn[c]=low[c]=++cc
                    const int N = 100050
                                                                                                                                  for(auto t:g[c])
                                                                                                           st[_st++]=c,
namespace SCC{
```

```
// _ starts from 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    SCC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      bool cuti(int pi , cc &va) { rep(i, 0, sz(va)) if (e[pi][va[i]]) return true; return
                                                                                                                                                                                                                                                                                                                                                                                                                                        static bool desc_deg(const ve &a, const ve &b) { return a.d > b.d; } void ini_col(ves &v) { per(i, 0, sz(v)) v[i].d = min(i, v[0].d) + 1; } void set_deg(ves &v) { rep(i, 0, sz(v)){v[i].d = 0; rep(j, 0, sz(v)) v[i].d += e[v[i, 0, sz(v)]]}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void cut2(ves &va, ves &vb) { rep(i, 0, sz(va) - 1) if (e[va.back().i][va[i].i]) vb.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(k, min_k, maxno + 1) rep(i, 0, sz(C[k])) R[j].i = C[k][i], R[j++].d = k;
                                                                                                                                                                                                                                                       Maxclique(BB *conn, int sz, const db tt = 0.025): pk(0), lv(1), Tlimit(tt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   void mcqdyn(int *mxc, int &sz) { // mcqdyn(int maxclique, int &siz)
                                                                                                                                                  //cc : ColorClass
                                    {}}; //ve : Vertex {}}; //sc : StepCount
                                                                                                                //ves: Vertices
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int j = 0, maxno = 1, min_k = max(sz(QMAX) - sz(Q) + 1, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void deg_sort(ves &R) { set_deg(R); sort(all(R), desc_deg); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (k > maxno) C[(maxno = k) + 1].clear(); C[k].pb(pi);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ini_col(V); rep(i, 0, sz(V) + 1) S[i].a = S[i].b = 0; exp_dyn(V); per(i, 0, sz(QMAX)) mxc[i] = QMAX[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (sz(Rp)) {
   if ((db) S[lv].a / ++pk < Tlimit) deg_sort(Rp);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (sz(Q) + R.back().d <= sz(QMAX)) return;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for (; sz(R); Q.pop_back(), R.pop_back()) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        } else if (sz(Q) > sz(QMAX)) QMAX = Q;
                                                                n: a(0),b(0)
                                 struct ve {int i, d; ve(int i): i(i), d(0) struct sc {int a, b; sc( ): a(0), b(0)
                                                                                                                                                                                                                                                                                           rep(i, 0, sz) \ V.pb(ve(i)); e = conn;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       set_deg(V); sort(all(V), desc_deg);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void exp_dyn(ves &R) { // expand_dyn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             S[1v].a += S[1v - 1].a - S[1v].b;

S[1v].b = S[1v - 1].a;
                                                                                                                                            typedef vector<int> cc; cc 0, QMAX;
const BB *e; int pk, lv; db Tlimit;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (k < min_k) R[j++].i = pi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               co_sort(Rp); S[lv++].a++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       while (cut1(pi, C[k])) k++;
                                                                                                          typedef vector<ve> ves; ves V;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(i, 1, 3) C[i].clear();
rep(i, 0, sz(R)) {
    int pi = R[i].i, k = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (j > 0) R[j - 1].d = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         exp_dyn(Rp); --1v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ves Rp; cut2(R, Rp);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     0.pb(R.back().i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void co_sort(ves &R) {
                                                                                                                                                                                                                                                                                                                                C.resize(sz + 1);
                                                                                                                                                                                                                                                                                                                                                                       S.resize(sz + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      SZ = SZ(QMAX);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          pb(va[i].i); }
                                                                                                                                                                                                                        vector<sc> S;
                                                                                                                                                                                   vector<c> C
```

t1), node(i, j, t2));

int &z = dp[msk][i][j];

```
pre[pw(k++)][i][j] = mp(node(0, 0, 0), node(0, 0, 0));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(j, 1, m+1) {
if (st[i][j] && !(st[i][j] & msk)) continue;
                                                                                                                                                                   memset(dp, 0x3f, sizeof(dp));
rep(i, 1, n+1) rep(j, 1, m+1) {
    cin >> a[i][i];
                                                                                                                                                int SteinerTree(int n, int m) {
                                                                                                                                                                                                                                               if (!a[i][j]) {
   st[i][j] = pw(k);
   dp[pw(k)][i][j] = 0;
node t1 = t.fi, t2 = t.se;
                          use[now.x][now.y] = 1;
                                                                                               if (t2.msk) dfs(t2);
                                                                                                                                                                                                                                                                                                                                                                                                                      rep(msk, 1, S+1) {
                                               if (!t1.x) return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(i, 1, n+1)
                                                                                                                                                                                                                                                                                                                                                                                              S = pw(k) - 1;
                                                                        dfs(t1);
                                                                                                                                                                                                                                                                                                                                              fill_n(ng,_,vi());
rep(i,0,n) for(auto j:g[i]) if(id[i]!=id[j]) ng[id[i]].pb(id[j]);
if(!dfn[t]) dfs(t,g),low[c]=min(low[c],low[t]);
                      else if(!id[t]) low[c] =min(low[c],dfn[t]);
                                                                                               do{id[st[---st]]=_;}while(st[_st]!=c);
                                                                                                                                                                                                                                                                                               rep(i,0,n) if(!dfn[i]) dfs(i,g);
                                                                                                                                                                                                int solve(int n, vi g[]){
                                                                                                                                                                                                                                               fill_n(low,n,_st=0);
                                                   if(low[c]==dfn[c]){
                                                                                                                                                                                                                                                                                                                       rep(i,0,n) \longrightarrow id[i];
                                                                                                                                                                                                                      fill_n(dfn,n,cc=0);
                                                                                                                                                                                                                                                                      fill_n(id, n, _=0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               SteinerTree
                                                                                                                                                                                                                                                                                                                                                                                                 return _;
                                                                                                                                                                         vi ng[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               6.21
```

Stoer Wagner_

O(n3)

```
void add_edge(int u, int v, int w) { g[u][v] += w; g[v][u] += w; }
                    static const int N = 305, INF = 0x3f3f3f3f;
                                                                                                                                                                                 rep(i, 1, n+1) fill_n(g[i] + 1, n, \Theta);
                                                                                                                                                                                                                                                                                                                g[v][i] += g[u][i];
                                                                                                                                n = _n;
fill_n(use + 1, n, 0);
                                                                                                                                                                                                                                                                 void merge(int u, int v)
                                                                                                                                                                                                                                                                                                                                            g[i][v] += g[i][u];
                                                int n, g[N][N], val[N];
                                                                         bool vis[N], use[N];
                                                                                                 void init(int _n) {
                                                                                                                                                                                                                                                                                             rep(i, 1, n+1)
struct StoerWagner{
```

```
for (int t = msk & (msk - 1); t > 0; t = (t - 1) & msk)
int t1 = t | st[i][i], t2 = msk ^ t | st[i][i];
int w = dp[t1][i][i] + dp[t2][i][i] - a[i][i];
if (z > w) z = w, pre[msk][i][i] = mp(node(i, j, t1),
                                                                                                                                                                                                                   if (z < inf) q.push(mp(i, j)), vis[msk][i][j] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, 1, n+1) rep(j, 1, m+1) if (ans > dp[S][i][j]])
ans = dp[S][i][j], now = node(i, j, S);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return ans == inf ? —1 : ans;
                                                                                                                                                                                                                                                                                                    spfa(msk);
                                                                                                                                                                                                                                                                                                                                                                               ans = inf;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     dfs(now);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  z = w, pre[t][nx][ny] = mp(node(x, y, msk), node(x, y, 0));
if (t == msk && !vis[msk][nx][ny]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, 4) {
   int nx = x + dx[i], ny = y + dy[i], t = msk | st[nx][ny];
   if (nx > n || nx < 1 || ny > m || ny < 1) continue;
   if (nx > n || nx < 1 || ny > m || ny < 1) continue;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                node(int \times = 0, int y = 0, int msk = 0):x(x), y(y), msk(msk){}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int &z = dp[t][nx][ny], w = dp[msk][x][y] + a[nx][ny];
      // 要视图的情况使用 spfa, dijstra, 多源 bfs
const int N = 11, M = 10, inf = 0x3f3f3f;
int n, m, k, a[N][N], st[N][N], dp[1 << M][N][N], S, ans;
bool use[N][N], vis[1 << M][N][N];
int dx[] = {1, -1, 0, 0};
int dy[] = {0, 0, 1, -1};
queue<pli>queue<pli>queue<pli>queue<pli>queuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeuequeue
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   pair<node, node> t = pre[now.msk][now.x][now.y];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       vis[msk][nx][ny] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    pair<node, node> pre[1 << M][N][N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    d.push(mp(nx, ny));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             pii u = q.front(); q.pop();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int x = u.fi, y = u.se;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           vis[msk][x][y] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     while (!q.empty()) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (z > w) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void dfs(node now) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void spfa(int msk)
                                                                                                                                                                                                                                                                                                                                                            int x, y, msk;
                                                                                                                                                                                                                                                                                                              struct node {
```

```
void ini(int _n = N){ fill(h , h + (n=_n) , -1);e = 0;}
void liu(int u,int v,U c,V w){ to[e] = v;ne[e] = h[u];cap[e] = c;cost[e] = w;h[u] =
                                                                                                                                                                                                                      while (!q.empty() && (vis[q.top().se] || val[q.top().se] != q.top().fi)) q.pop
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void link(int u,int v,U c,V w){ liu(u,v,c,w);liu(v,u,0,-w);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int h[N] , ing[N] , v[N] , to[M] , ne[M] , e , s , t , n;
U cap[M];V dis[N] , cost[M];
                                                                                                                                      if (!vis[v]) q.push(mp(val[v] += data[p], v));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(!ing[v]) Q.push(v), ing[v] = true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int c = Q.front();Q.pop();ing[c] = false;
for(int k=h[c];~k;k=ne[k]){
                                                                            for (int p = head[u]; \sim p; p = ne[p]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   res = min(res, MinimumCutPhase(i, s, t));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(dis[c] + cost[k^1] < dis[v]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         dis[v] = dis[c] + cost[k^{1}]
                                                     for (int u = s; ~u; u = link[u]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(cap[k^{1}] \le 0) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      static const int N = 1010 , M = 40404;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for (int i = n, s, t; i > 1; -i)
                                                                                                          int v = findset(to[p]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ing[t] = true, dis[t] = 0;
                                                                                                                                                                                                                                                                            if (q.empty()) return 0;
                                                                                                                                                                                                                                                                                                          t = q.top().se; q.pop();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // [0,n) , init!! , inf modify
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int v = to[k]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (res == 0) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         fill(dis,dis+n,inf);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        while(!Q.empty()){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               template<class U, class V>
                           vis[s = t] = 1;
while (---cnt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             queue<int> 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            merge(s, t);
                                                                                                                                                                                                                                                                                                                                                                                                                                           int res = INF;
                                                                                                                                                                                                                                                                                                                                                          return val[t];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Q.push(t);
                                                                                                                                                                                                                                                                                                                                                                                                              int solve() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ZKW
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void spfa()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               struct ZKW{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 e++;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           .
}
}
}
                                                                                                                                                                                                                                                                     rep(i, 1, i+1) if (!vis[i] && !use[i] && val[i] >= ma) ma = val[i], t = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int findset(int u) { return u == fa[u] ? u : fa[u] = findset(fa[u]); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int head[N], val[N], e, n, to[M], ne[M], data[M], fa[N], link[N];
                                                                                                                                                                                                                      static const int N = 3005, M = 1000005 * 2, INF = 0x3f3f3f3f;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         to[e] = v; data[e] = w; ne[e] = head[u]; head[u] = e++; to[e] = u; data[e] = w; ne[e] = head[v]; head[v] = e++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     res = min(res, MinimumCutPhase(i, s, t));
                                                     int MinimumCutPhase(int cnt, int &s, int &t) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int MinimumCutPhase(int cnt, int &s, int &t) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          {
m StoerWagner\_O(nmlog(m))}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for (int i = n, s, t; i > 1; --i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void add_edge(int u, int v, int w) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      while (\simlink[p]) p = link[p];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(i, 1, n+1) fa[i] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     fill_n(head + 1, n, -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 fill_n(link + 1, n, -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void merge(int u, int v) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (res == 0) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        fill_n(vis + 1, n, 0);
priority_queuecpii> q;
                                                                              fill_n(val + 1, n, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               fill_n(val + 1, n, 0);
                                                                                                          fill_n(vis + 1, n, 0);
                                                                                                                                                                                                                                                                                                          if (!ma) return 0;
                                                                                                                                                                                           vis[s = t] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void init(int _n) {
                                                                                                                                                           while (---cnt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        merge(s, t);
                                                                                                                                                                                                                                                    int ma = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                  int solve() {
  int res = INF;
                                                                                                                                                                                                                                                                                                                                                             return val[t];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       struct StoerWagner{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        link[p] = v;
use[u] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  fa[v] = u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        bool vis[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          .;
0
11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          6.23
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    } SW;
```

```
inline void ins(int &rt, db val, int id){ rt = merge(rt, newnode(val, id)); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (!vis[v] && fabs(dis[v] - dis[u] - rg.w[i]) <= eps) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(ht[ls[now]] < ht[rs[now]]) swap(ls[now],rs[now]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   val[p] = val[ori], id[p] = id[ori], ht[p] = ht[ori];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  inline int newnode(db _val, int _id, int _dis = 0){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int ls[M*B], rs[M*B], ht[M*B], id[M*B], tot;
                                                                                                                for (int i = rg.h[u]; i; i = rg.ne[i]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        val[p] = _val, id[p]=_id, ht[p] = _dis;
                                                                                                                                                                                                                                                                                                                                                                                                                                        for (int i = rg.h[u]; i; i = rg.ne[i]) {
  int v = rg.to[i];
                                                                                   if (vis[u]) continue; vis[u] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ls[p] = ls[ori], rs[p] = rs[ori];
                                                                                                                                                                       if (dis[v] > dis[u] + rg.w[i]
                                                                                                                                                                                                    dis[\bar{v}] = dis[\bar{u}] + rg.w[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(val[a] > val[b]) swap(a, b);
                                                            int u = pq.top().se; pq.pop();
                                                                                                                                                                                                                                 pq.push(mp(—dis[v], v));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       inline int merge(int a, int b){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int now = _copy(a);
rs[now] = merge(rs[now], b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ht[now] = ht[rs[now]] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                fa[v] = u; tree[i] = 1;
pq.push(mp(dis[T] = 0, T));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(!a || !b) return a|b;
                                                                                                                                                                                                                                                                                                                                                                                                               st[++top] = u; vis[u] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           inline int _copy(int ori){
                                                                                                                                            int v = rg.to[i]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ls[p] = rs[p] = 0;
                               while(!pq.empty()){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int p = ++tot;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int p = ++tot;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void build_heap(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return now;
                                                                                                                                                                                                                                                                                                                                                                                void dfs(int u){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              dfs(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  db val[M*B];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            namespace LT{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int rt[N];
                                                                                                                                              if(!v[t] \&\& cap[k] > 0) Min = min(Min , dis[t] + cost[k] - dis[c]);
                                                                                                                                                                                                                                                                                                                                                     if(c == t) return flow += mx , mincost += mx * dis[s] , mx;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(!v[t] \& cap[k] > 0 \& dis[c] - cost[k] == dis[t])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   U \text{ tmp} = dfs(t, min(cap[k], mx - ret));
                                                                                     rep(c,0,n)        if(v[c])        for(int k=h[c];~k;k=ne[k]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                cap[k] = tmp , cap[k^1] + tmp;
                                                                                                                                                                                                                                 rep(i,0,n) if(v[i]) dis[i] += Min;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        do do memset(v,0,sizeof(v[0])*n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(ret == mx) return ret,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return make_pair(flow , mincost)
                                                                                                                                                                                                         if(Min == inf) return false)
                                                                                                                                                                                                                                                                                                                                                                                                               for(int k=h[c];~k;k=ne[k]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       pair<U,V> run(int _s,int _t){
                                                                                                                                                                                                                                                                                                                                                                                  v[c] = true; U ret = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       while(dfs(s,inf));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ret += tmp;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 flow = mincost = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                               int t = to[k];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                while(modlable());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    s = _{-}s , t = _{-}t;
                                                                                                                                                                                                                                                                                                                       U dfs(int c,U mx){
                                                                                                                   int t=to[k];
  U flow;V mincost;
                                                                                                                                                                                                                                                                   return true;
                             bool modlable(){
                                                            V Min = inf
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return ret;
```

```
ne[++e] = h[u], h[u] = e, to[e] = v, w[e] = val;
                    // time : O(klogk + mlogn) space : O(nlogn)
                                                                                                                                                                                                      inline void add(int u, int v, db val){
                                                                             priority_queue<pair<db, int> > pq;
                                        const int N = 5050, M = 200005, B =
                                                             const db eps = 1e-9, inf = 1e16;
// S -> 7 可重复经过点的第 K 短路
                                                                                                                                                                                                                                                                                                          rep(i, 1, n+1) dis[i] = inf;
                                                                                                                                                             int h[N], ne[M], to[M],
                                                                                                                                                                                                                                                                   } g, rg;
void Dij(){
                                                                                                                                                                                      db w[M];
```

k短路

6.25

spfa();

for (int i = g.h[u]; i ; i = g.ne[i]) {

```
inline void init(int n) { L = 0; rep(i, 1, n + 1) hd[i] = -1; } inline void _add(int u, int v, 11 w) { to[L] = v; val[L] = w; ne[L] = hd[u]; hd[u] =
                                                                             inline void add(int u, int v, ll w) { _add(u, v, w); _add(v, u, w);
                                                                                                                                                                                                                                                                                                                                                                    int u, v, n, match[N], q[N], L, R, pred[N], b[N], s, t, newb;
bool inq[N], inb[N], inp[N];
                                                                                                                                                                                                                                                                                                                                                                                                                         void init(int _n) { n = _n; rep(i, 0, n) g[i].clear();
void link(int u, int v) { g[u].pb(v); g[v].pb(u); }
void push(int u) { q[R++] = u; inq[u] = 1; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(b[u] != newb) pred[u] = v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    inb[b[u]] = inb[b[v]] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (inp[v = b[v]]) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int pop() { return q[L++]; }
                                                                                                                                                                                                                                                                                                                  static const int N = 5005;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                v = pred[match[v]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 0, n) inp[i]=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                u = pred[match[u]]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void ResetTrace(int u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              while(b[u] != newb) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        inp[u = b[u]] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (u == s) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int LCA(int u,int v)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        v = match[u];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  u = pred[v];
                                                                                                                                                              带花树
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 while(1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   while(1) {
                                                                                                                                                                                                                                                        // id : 0 .. n-1
                                                                                                                                                                                                                                                                                      struct blossom {
                                                                                                                                                                                                                                 // time : 0(n/3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return v;
                                                                                                                                                                                                                                                                                                                                      vi g[N];
                                                         6.28
                         if (!tree[i] && dis[v] < inf) LT::ins(rt[u], dis[v] - dis[u] + g.w[i], v);
                                                                                                                                                                                                                                                                                                                                                                                                                                             if (rt[o]) pq.push(mp(w + LT::val[rt[o]], rt[o]));
if (ls) pq.push(mp(w + LT::val[ls] - LT::val[u], ls));
if (rs) pq.push(mp(w + LT::val[rs] - LT::val[u], rs));
                                                                                                                                                                                                                                                                              if (rt[S]) pq.push(mp(dis[S] + LT::val[rt[S]], rt[S]));
                                                                                                                                                                                                                                                    priority_queue<pdi, vector<pdi>, greater<pdi> > pq;
                                                                                                                                                                                                                                                                                                                                                                                           E = w; if (E >= 0) ++ans; else return ans;
                                                                                                                                                                                                                                                                                                                                                               db w = t.fi; int u = t.se, o = LT::id[u];
                                                                                                                                                                                                                                                                                                                                                                                                                     int ls = LT::ls[u], rs = LT::rs[u];
                                                                                                                                                                                                                                                                                                          while(!pq.empty()) {
   pdi t = pq.top(); pq.pop();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(i, 1, n+1) vis[i] = 0;
                                                                                                                                                                                              inline int calc_K(){
  int ans = 1; E -= dis[S];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                cout << calc_K() << endl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ios::sync_with_stdio(0);
cin.tie(0);
                                                                                                                                         typedef pair<db, int> pdi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       cin >> u >> w;
int v = g.to[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rg.add(v, u, w);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     cin >> n >> m >> E;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 g.add(u, v, w);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 1, m+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               S = 1; T = n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    build_heap();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int main(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            dfs(T);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Dij();
```

仙人掌最短路 6.26

*建出圆方树,选任意圆点作为根,环的根指的是环上深度最小的点。 *圆圆边边权不变,圆方边边权是圆点到它所在环的根的最短距离。 *如果询问两点的 1ca 是圆点, ans = dep[a] + dep[b] - dep[lca] *如果是方点, ans = dep[a] + dep[b] - dep[A] - dep[B] + dis(A,

B)

if(b[u] i= newb) pred[u] = v;if(b[v] != newb) pred[v] = u;

b[i] = newb; if (!inq[i]) push(i);

bool Find(int u) {
 bool found = 0;

void Blossom(int u, int v) { rep(i, 0, n) inb[i] = 0;

newb = LCA(u, v);

ResetTrace(u); ResetTrace(v);

前向星 6.27

static const int N = ::N << 1;
int L, hd[::N], ne[N], to[N]; 11 val[N];</pre> struct Gra {

```
pq.push(data(u.w-g[u.last][u.id].fi+g[u.last][u.id+1].fi,\ u.st,\ u.last,
                                                                                                                                                                                                                                if (sz(g[v])) pq.push(data(u.w + g[v][0].fi, u.st, v, 0));
                                                                                                                                                                                               k—; if (k == 0) return u.w;
                                                                                                                                 if (!vis.count(mp(u.st, v))) {
                                                                                                                                                                                                                                                                                                    if (u.id + 1 < sz(g[u.last]))
                                                                data \ u = pq.top(); pq.pop();
                                                                                                                                                                     vis.insert(mp(u.st, v));
                                                                                             int v = g[u.last][u.id].se
                                 while (!pq.empty()) {
                                                                                                                                                                                                                                                                                                                                                                         ;((1 + pi);
                                                                                                                                                                                                                                if (b[u] != b[v] && match[u] != v)
if(v == s || (match[v] >= 0 && pred[match[v]] >= 0))
b[i] = i, inq[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                      if (match[v] \geq 0) push(match[v]);
```

else if(pred[v] == -1) {

pred[v]=u;

Blossom(u, v);

per(i, 0, sz(g[u])) {
 int v = g[u][i];

int u = pop();

while(L < R) {

(s)ysnd

rep(i, 0, n) pred[i] = -1, s = u, t = -1, L = R = 0;

else return t = v, 1;

生成树计数与欧拉回路方案数 6.30

```
rep(k, i, n) a[i][k] = sub(a[i][k], mul(a[j][k], t)), swap(a[i][k], a[j][k]);
                                                                                                                                                                                      // 无向图生成树个数: a[][] 任何一个 n-1 阶主子式的绝对值
// 有向图以 i 为根的生成树个数: a[][] 去掉第 i 行第 i 列的行列式的绝对值
                                                                                                              // from i to j has b[i][j] directed edges
// a[][] = d[][] - b[][]
                                                                                                                                                                                                                                                                   int det(int n) { // det(a[1..n-1][1..n-1])
                                                                                                                                                                                                                                                                                                                  rep(i, 1, n) {
    rep(j, i+1, n) while(a[j][i]) {
                                                                                                                                                                                                                                                                                                                                                                      int t = a[i][i] / a[j][i]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(a[i][i] == 0) return 0;
                                                              i==j d[i][j]=in\_deg(i)
                                                                                                                                                                                                                                                                                                                                                                                                                         ans = P - ans;
                                     i!=j d[i][j]=0
                                                                                                                                                                                                                                                                                             int ans=1;
                                                                              // b[][]:
                                                                                                                                                                                                                                                                                                                                                      rep(i, 0, n) if (match[i] == -1) if (Find(i)) AugmentPath();
rep(i, 0, n) if (match[i] != -1) res++;
return res / 2;
                                                                                                                                                                                                                                                                                                                                // random_shuffle maybe faster
                                                                                                                                                   match[v] = u, match[u] = v;
                                                                                                                         v = pred[u], w = match[v];
                                                                                                                                                                                                                                                                                                     rep(i, 0, n) match[i] = -1;
                                           void AugmentPath() {
                                                                          int u = t, v, w;
while(u >= 0) {
return found;
                                                                                                                                                                                                                                                                               int res = 0;
                                                                                                                                                                                                                                                       int solve() {
                                                                                                                                                                               .×
□
                                                                                                                                                                                                                                                                                                                                                                                                                                                          }
};
```

最短路矩阵中第 k 小 6.29

```
data(11 W, int S, int L, int I) { w = W; st = S; last = L; id = I; }
                                                                                                                                                                                                                                     复杂度最坏应该是 O( min(nmlogn, k^2logk) ) 正常应该是 O(klogk + nlogn)
                                                                                                                                                           bool operator < (const data &c) const { return w > c.w; }
                                                                                                                                                                                                                                                                                                                                              rep(i, 1, n+1) {
if (sz(g[i])) pq.push(data(g[i][0].fi, i, i, 0));
                                               int n, m, k, u, v, w;
struct data { // 距离起点当前点当前扩展过的边编号
                    vector<pii>yell]; // ( 边权 , 终点 ) 需要排序
                                                                                                                                                                                                                                                                  solve(int n, vector<pii> g[], int k)
                                                                                                                                                                                                            连通图的话 k <= n * (n - 1)
                                                                                                                                                                                                                                                                                           priority_queue<data> pq;
                                                                                                                                                                                                                                                                                                                                                                                                        vis.insert(mp(i, i));
                                                                                                     ll w; int st, last, id;
const int N = 2e5 + 7;
                                                                                                                                                                                                                                                                                                                            set<pii>vis;
                                                                                                                                                                                     \
\
\
\
                                                                                                                                                                                                                                       \ \
```

稳定婚姻匹配

// ec(G) = tw(G) * pi((deg[V] - 1)!)// ans = ec(G) * deg[w]; 如果求的不是本质不同的,就还需要这个

本质相同: / 本质不同:

有向图要记得判断每个点的出度入度是否相等

// tw(G): 以 w 为根的生成树个数

// 无向图需要转换成有向图

ans = mul(ans, a[i][i]);

return ans;

```
int mat1[N], mat[N], pos[N];
                   vi g1[N], g2[N];
                                      queue<int> q;
```

if (M.count(n)) return M[n];

int r = n, nn = n;

rep(i, 0, N) C[i][0] = 1;

int C[N][N], B[N];

void ini() {

```
rep(i, 0, k+1) sum = add(sum, mul(C[k+1][i], mul(B[i], qpow(n, k+1-i))));
N) rep(j, 1, i + 1) C[i][j] = add(C[i-1][j-1], C[i-1][j]);
                      B[0] = 1;
rep(i, 1, N) {
    B[i] = 0;
rep(j, 0, i) B[i] = add(B[i], MOD - mul(C[i + 1][i], B[i]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // a[1] ^ a[1+1] ^ a[1+2] ... ^ a[r] % mod 注意结果要再模 mod
map<int, int> M;
int phi(int n) {
                                                                                                                       B[i] = mul(B[i], qpow(C[i+1][i], MOD - 2)) % MOD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                = (R % M + M) % M; // 可能为 Ø 看是否需要是正整数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 R += inv^* ((a[i] - R) / g) % (mod[i] / g) * M;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ll g = __gcd(M, mod[i]);
ll inv = Inv(M / g, mod[i] / g);
if ((a[i] - R) % g) return -1; // 无解
                                                                                                                                                                                                                                                                      return mul(sum, qpow(k + 1, MOD - 2));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            void exgcd(ll a, ll b, ll &x, ll &y){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (!b) \{ x = 1; y = 0; return; \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       }(pow*
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return x < 0? x + mod : x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ll solve(int n, ll *a, ll
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      M = M / g * mod[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            exgcd(b, a % b, y, x);
y -= a / b * x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          M = mod[1], R = a[1];
                                                                                                                                                                                                int cal(int n, int k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     exgcd(a, mod, x, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     11 Inv(11 a, 11 mod){ 11 \times 0, y = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 2, n+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        7.4 EulerPower
                                                                                                                                                                                                                                                                                                                                                                                                                                     const int N = 1e5+7;
                                                                                                                                                                                                                         int sum = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                              11 a[N], mod[N];
 rep(i, 0,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             :pow =% ×
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return R;
                                                                                                                                                                                                                                                                                                                                                                             CRT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               struct CRT{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      11 M, R;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     } crt;
                                                                                                                                                                                                                                                                                                                                                                           7.3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, sz(B)) C[i + m] = add(C[i + m], mul(c, B[i]));
if(2 * L <= n) L = n + 1 - L, B = T, b = d, m = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // s_{m} = \sum_{j=0}^{(m-1)}s_{j}^{(j)}*c_{j} 系数直接适配线性递推 vi BM(vi s) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 0, L+1) (d += 111 * C[i] * s[n-i]) %= P;
                                             rep(i, 1, n+1) q.push(i), pos[i] = 0, mat[i] = 0; while (!q.empty()) {
                                                                                                                                                                      else if (rank[v][mat[v]] > rank[v][u]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  vi T = C;
11 c = P - d * kpow(b, P - 2) % P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 while(sz(C) < sz(B) + m) C.pb(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // desc : 0^{\Lambda}k + 1^{\Lambda}k + 2^{\Lambda}k + ... + (n-1)^{\Lambda}k
                    void match(int n, vi *g, vi *rank) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return vi(C.begin(), C.end() - 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i, 0, sz(C)) C[i] = P - C[i];
                                                                                                                                                                                                                                                                                                                        rep(i, 1, n+1) mat1[mat[i]] = i;
                                                                                                                         int &p = pos[u], v = g[u][p];
                                                                                                int u = q.front(); q.pop();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         7.1 BerlekampMassey
                                                                                                                                               if (!mat[v]) mat[v] = u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      vi C(1, 1), B(1, 1);

int L = 0, m = 1, b = 1;

rep(n, 0, sz(s)) {
                                                                                                                                                                                                q.push(mat[v]);
                                                                                                                                                                                                                                                }else q.push(u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       const int N = 1000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(d == 0) ++m;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // time_cal : k + log
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               namespace Bernoulli {
                                                                                                                                                                                                                           mat[v] = u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // time_ini : O(n^2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   reverse(all(C));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Bernoulli
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             else ++m;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     11 d = 0;
                                                                                                                                                                                                                                                                                                                                                                                                             Math
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      O(1en^{\lambda}2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                7.2
```

```
inline vir operator +(const vir &c) {return vir(r+c.r,\ i+c.i);} inline vir operator -(const vir &c) {return vir(r-c.r,\ i-c.i);} inline vir operator *(const vir &c) {return vir(r*c.r-i*c.i, r*c.i+i*c.r)
                      na)
                                                                                                                                                void doit(vir *a, vir *b, int na, int nb)\{ // [\theta,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      i(i){}
                                                                                                                                                                   for (N = 1; N < na + nb - 1; N <= 1); rep(i, na, N) a[i] = vir(0, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     vir(db \ r = 0.0, \ db \ i = 0.0) : r(r),
                                                                                                                                                                                                            rep(i, nb, N) b[i] = vir(0, 0);
work(), fft(a, 0), fft(b, 0);
rep(i, 0, N) a[i] = a[i] * b[i];
fft(a, 1);
                                                                                                                                                                                                                                                                                                  //rep(i, 0, N) a[i].print();
   _builtin_ctz(N);
                                                                                                                                                                                                                                                                                                                                                                                                                                                    const int M = 1 << 18 << 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                const db PI = acos(-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int na, nb, a[M], b[M];
                                                                                                                                                                                                                                                                                                                                                                                   FFTMOD
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    db r, i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 struct vir{
                                                                                                                                                                                                                                                                                                                                         } fft;
                                                                                                                                                                                                                                                                                                                                                                                 9.2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return Euler_qpow(a[1], work(1+1, r, phi(mod)), mod);
    }(0 ==
                                                                                                                                                                     for(int i = 2; i * i <= n; i++) if (n % i</pre>
                                           while (n \% i == 0) n /= i;
                                                                    }
if (n > 1) r = r / n * (n-1);
                                                                                                                                                                                                                                                                                                                                                              ok |= (b > 1 \& a > = mod);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         11 work(int 1, int r, int mod)
                                                                                                                                                                                                                                                                           ok |= (res >= mod);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (1 == r) return a[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if (mod == 1) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                               return res + mod * ok;
                        r = r / i * (i-1);
                                                                                                                                                                                                                                                        res = res * a;
                                                                                                                                                                                                                                                                                                  res %= mod;
                                                                                                                                                                                                                                  if (b & 1) {
                                                                                                                                                                                                                                                                                                                                       = a * a;
                                                                                                                                                                                                                                                                                                                                                                                    ; pow =%
                                                                                                                                                                                                            while (b) {
                                                                                                                                                                                                                                                                                                                                                                                                         b >>= 1;
                                                                                                          M[nn] = r;
                                                                                                                                 return r;
                                                                                                                                                                                                                                                                                                                                            ø
```

```
for (int d = 0; (1 << d) < n; ++d) {
   int m = 1 << d, m2 = m * 2, rm = n >> (d + 1);
                                   inline vir operator !() const {return vir(r, -i);}
                                                                                                                                                                                                                                                                                                                    for (int s = n; j = s >>= 1, -j \& s;);
                                                                                                                                                                                                                                                                                for (int i = 1, j = 0; i < n - 1; ++i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void doit(int *a, int *b, int na, int nb){ for (N = 1; N < na + nb - 1; N <<= 1);
                                                                  void print() {printf("%lf %lf\n", r, i);}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int j = 0; j < m; ++j) {
    vir &p1 = p[i + j + m], &p2</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for (int i = 0; i < n; i += m2) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      p1 = p2 - t, p2 = p2 + t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  vir t = w[rm * j] * p1;
                                                                                                                                                                                                                                                                                                                                                   if (i < j) swap(p[i], p[j]);
                                                                                                                                                             static const int M = 1 \ll 18 \ll 1;
                                                                                                                                                                                     struct FFTMOD{
                                                                                                                                                                                                                                                                                                                                                vir operator *(const vir &c) {return vir(r \cdot c.r - i \cdot c.i, r \cdot c.i + i \cdot c.r);}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (int k = 0, 1 = 0; k < i; k++, 1 += t)
x = w[f][1] * a[j+k+i], y = a[j+k], a[j+k] = y+x, a[j+k+i] = y-x;</pre>
                                                                                                                                                                                                                                                                                                                    vir operator -(const vir \&c) \{return vir(r-c.r, i-c.i);\}
                                                                                                                                                                                                                                                   void print() {printf("%f %f\n", r, i);}
vir operator +(const vir &c) {return vir(r + c.r, i + c.i);}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   vir x, y;
rep(i, 0, N) if (i < rev[i]) swap(a[i], a[rev[i]]);
for (int i = 1; i < N; i <= 1)
for (int j = 0, t = N/(i<1); j < N; j += i<1)</pre>
                                                                                                                                                                                                                           vir(db \ r = 0.0, \ db \ i = 0.0) \ : \ r(r), \ i(i){}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (f) rep(i, 0, N) a[i].r /= N;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void fft(vir *a, int f){
                                                                     const int M = 1 << 17 << 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int N, na, nb, rev[M];
                                                                                                 const db pi = acos(-1);
                                                                                                                                                                                                                                                                                                                                                                                  } a[M], b[M], w[2][M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void work(){
ГHН
                                                                                                                                                             struct vir{
                                                                                                                                                                                                                                                                                                                                                                                                                                                struct FFT{
                                                                                                                                                                                          db r, i;
7.5
```

= p[i + j];

for (; k; k >>= 1, x = mul(x, x)) **if** (k & 1) ret = mul(ret, x);

11 ret = 1;return ret;

MATH

7

```
fft(z, K, 1);
rep(i, 0, na+nb+1) a[i] = i&1 ? z[i>>1].b + 0.1 : z[i>>1].a + 0.1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     vir tmp = (i&K>>1) ? vir(1, 0) - w[i^{\Lambda}K>>1] : w[i] + vir(1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                z[i] = (x[i]^*y[i]^*4 - (x[i] - ix[i])^*(y[i] - iy[i])^*tmp)^*0.25;
                                                                                                                                                                                                                                                                                                                                                                                                             for(int i=0; i<=na; i++) (i&1 ? x[i>>1].b : x[i>>1].a) = a[i];
for(int i=0; i<=nb; i++) (i&1 ? y[i>>1].b : y[i>>1].a) = b[i];
                                                                                                                                                                                                                                                                            if (v) for(int i=0; i<k; i++) x[i] = vir(x[i].a/k,x[i].b/k);</pre>
      Ġ.
  For(int j=1; j<i>>1; j+=2) w[j] = w[j-1]*
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               const int _p = 998244353;
11 add(11 x, 11 y) { x += y; return x%_p; }
11 mul(11 x, 11 y) { return x*y%_p; }
11 Pow(11 x, 11 k) {
                                                                                                                                                                                                                                                                                                                                 void doit(int *a, int *b, int na, int nb)
                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, K) \times [i] = y[i] = vir(0, 0);
                                                                                                                                                                                                                                                                                                                                                             for(K = 1; K <= na+nb>>1; K <<= 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 版朴
                           for(int j=0; j<k; j+=i){
  vir *a = x+j, *b = a+(i>>1);
  for(int l=0; l<i>>1; l++){
                                                                                                           vir o = b[1] * w[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          \mathbf{xor}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       fft(x, K, 0); fft(y, K, 0);
                                                                                                                                       b[1] = a[1] - 0;
a[1] = a[1] + 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               k 莊野
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int j = K-1 \& K-i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(i, 0, K){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   FWT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   2.8
                                                                              rep(i, 0, N) w[i] = vir(cos(2 * i * PI / N), sin(2 * i * PI / N));
    N) a[i] = 0;
N) b[i] = 0;
  a[i]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      dd = (11)(D[1].r / N + 0.5) % P;
= ((dd << (L * 2)) + ((db + dc) << L) + da) % P;
rep(i, 0, na) a[i] = (a[i] % P + P) % P; rep(i, na, rep(i, 0, nb) b[i] = (b[i] % P + P) % P; rep(i, nb, L = 15; MASK = (1 <<L) - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                db = (A[i] + iA[j]) * vir(0.5, 0),
dc = (B[i] - iB[j]) * vir(0, -0.5),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       dd = (B[i] + iB[j]) * vir(0.5, 0);
                                                                                                                                                                                                                                                                                                                                                                                        vir da = (A[i] - !A[j]) * vir(0, -0.5),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     da = (ll)(C[i].i / N + 0.5) % P,
db = (ll)(C[i].r / N + 0.5) % P,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            dc = (11)(D[i].i / N + 0.5) \% P,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                = da * dd + da * dc * vir(0, 1);
= db * dd + db * dc * vir(0, 1);
                                                                                                                                 A[i] = vir(a[i] >> L, a[i] & MASK);
B[i] = vir(b[i] >> L, b[i] & MASK);
                                                                                                                                                                                                                                                                                                                                                             int j = (N - i) \% N;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FFT(C, N), FFT(D, N);
                                                                                                                                                                                                                                                                          void mul(int *a) {
    FFT(A, N), FFT(B, N);
                                                                                                                                                                                                                                                                                                                                   rep(i, 0, N) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(i, 0, N) {
ll da = (l
                                                                                                              rep(i, 0, N)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    C[j]
P[j]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     a[i]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         FFT
                                                                                                                                                                                                                       mul(a);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       7.7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    } fft;
```

```
vir operator +(const vir &0) const{return vir(a+o.a,b+o.b);} vir operator -(const vir &0) const{return vir(a-o.a,b-o.b);} vir operator *(const vir &0) const{return vir(a*o.a-b*o.b,b*o.a+a*o.b);}
                                                                                                                                                                                                                                                                                     vir operator *(const double &0) const{return vir(a*0,b*0);}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      vir g = vir(cos(2*pi/i), (v ? -1 : 1) * sin(2*pi/i));
for(int j=(1>>1); j>=0; j-=2) w[j] = w[j>>1];
                                                                                                                                         vir(double r=0.0, double i=0.0) {a=r, b=i,}
                                                                                                                                                                                                                                                                                                                             vir operator !() const{return vir(a, -b);}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for(int l=k>>1; (j^=1)<1; l>>=1);
                                                                                                                                                                                                                                                                                                                                                                     } ×[N|1], y[N|1], z[N|1], w[N|1];
                                                                                                                                                                                                                                                                                                                                                                                                                                       void fft(vir x[],int k,int v){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for(int i=0, j=0; i<k; i++){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              w[0] = vir(1, 0);
for(int i=2; i<=k; i<<=1){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(i>j)swap(x[i], x[j]);
                            const double pi=acos(-1.0);
const int N = 1 << 21;
                                                                                                         double a,b;
                                                                       struct vir{
```

inline Num& operator = (int x) { mem(a, 0), a[0] = x; return *this; } inline friend Num operator + (const Num &a, const Num &b) {

Num(int x = 0) { mem(a, 0), a[0] = x; inline Num& operator = (const Num &t)

return *this;

Num(**int** x = 0) { mem(a, 0), a[0] rep(i, 0, K) a[i] = t.a[i];

template <int struct Num {

11 a[K];

rep(i, 0, K) c.a[i] = add(a.a[i], b.a[i]);

return c;

Num c;

inline friend Num operator - (const Num &a, const Num &b) $\{$

rep(i, 0, K) c.a[i] = add(a.a[i], -b.a[i]);

Num c;

, d

```
11 tmp[K << 1], a[N], b[N], w[K]; int t;
void Init(11 w0) { w[0] = 1; rep(i, 1, K) w[i] = mul(w[i - 1], w0); }
void FWT(11 a[], int S, int n, int op) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          *= K) ret += (x%K + y%K) % K*B;
void Multiply_B(11 A[], 11 B[], int n, 11 C[]) {
    rep(i, 0, n) rep(j, 0, n) (C[get(i, j)] += mul(A[i], B[j])) %= .
    rep(i, 0, n) C[i] < 0 ? C[i] += _p : 0;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 0, n) rep(j, 0, n) (C[get(i, j)] += mul(A[i], B[j])) \% - rep(i, 0, n) <math>C[i] < 0 ? C[i] += \_p : 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     .
0
                                                                                                                                                                                                                                                                                                                                                                                                                                                      for (; k; k >>= 1, x = mul(x, x)) if (k & 1) ret = mul(ret, x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                FWT(a, \ 0, \ n, \ -1); \ l1 \ inv = Pow(n, \ -p - 2); rep(i, \ 0, \ n) \ C[i] = mul(a[i], \ inv), \ C[i] < 0 \ ? \ C[i] += -p
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         tmp[j] = add(tmp[j], mul(a[S + L*k + i], w[t]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // wo 表示单位根模域表示,默认是 3 进制的,进制要整除模数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void Multiply_B(ll A[], ll B[], int n, ll C[]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void Multiply(11 A[], 11 B[], int n, 11 C[])
                                                                                                                                                                                                                                                                       const int _p = (int)1e9 + 9, w0 = 11538139811;
11 add(11 x, 11 y) { x += y; return x%_p; }
11 mul(11 x, 11 y) { return x*y%_p; }
11 Pow(11 x, 11 k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 0, \dot{K}) FwT(a, S + L*i, n / \dot{K}, op);
rep(i, 0, L) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(j, 0, K) a[S + L^*j + i] = tmp[j]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(j, 0, K) tmp[j] = 0;
rep(j, 0, K) rep(k, 0, K) {
t = op*j*k%k, t < 0 ? t += K : 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 0, n) a[i] = A[i], b[i] = B[i];
FWT(a, 0, n, 1), FWT(b, 0, n, 1);
rep(i, 0, n) a[i] = mul(a[i], b[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (n == 1) return; int L = n / K;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (; x || y; x /= K, y /= K, B return ret;
                                                                                                                                                                                                           xor 版本
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int get(int x, int y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int ret = 0, B = 1;
                                                                                                                                                                                                        k 讲题
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 template <int N, int K>
                                                                                                                                                                                                              \mathbf{FWT}
                                                                                                                                                                                                                                                                                                                                                                                                                         11 ret = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           struct FT {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               3 115381398
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              6 115381399
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    4 430477711
                                                                                                                                                                                                              7.9
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int cnt = K_8-K, L = K / cnt; 11 ret = add(a[0], -(L > 1)*a[cnt]); if (K & 1 ^ 1) ret -= add(a[K >> 1], -(L > 1)*a[(K >> 1) + cnt]), ret %= _p;
                                                                                                                                          rep(i, 0, K) rep(j, 0, K) (c.a[(i + j) % K] += mul(a.a[i], b.a[j])) % - p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          .;
o
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for (; \times || y; \times /= M, y /= M, B *= M) ret += (\times3M + y3M) % M*B;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, 0, n) a[i] = A[i], b[i] = B[i];
FWT(a, 0, n, 1), FWT(b, 0, n, 1);
rep(i, 0, n) a[i] = a[i] * b[i];
FWT(a, 0, n, -1); ll inv = Pow(n, _p - 2);
rep(i, 0, n) C[i] = mul(a[i].Value(), inv), C[i] < 0 ? C[i]
                                                                         inline friend Num operator ^{st} (const Num &a, const Num &b) \{
                                                                                                                                                                                                                                                                                                                                                                                                                                                      Num ret = 1; for (; k; k >>= 1, x = x^*x) if (k & 1) ret = ret*x;
                                                                                                                                                                                                                                                inline friend Num operator >> (const Num &a, int k) \{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          tmp[j] = tmp[j] + (a[S + L*k + i] >> t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               printf("\n\n\n%S\n", s.c_str());
rep(i, 0, K) printf("a[%d] => %d\n", i, a[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void Multiply(ll A[], ll B[], int n, ll C[]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void FWT(Num<K> a[], int S, int n, int op) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 0, M) FWT(a, S + L*i, n / M, op);

rep(i, 0, L) {

   rep(j, 0, M) tmp[j] = 0;

   rep(j, 0, M) rep(k, 0, M) {

   t = op*j*k%M, t < 0 ? t += M : 0;
                                                                                                                                                                                                                                                                                                                                                                                                                 inline friend Num operator ^{\wedge} (Num \times, 11 k)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(j, 0, M) a[S + L^*j + i] = tmp[j]
                                                                                                                                                                                                                                                                                                              rep(i, 0, K) c.a[(i + k) % K] = a.a[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Num<K> tmp[M << 1], a[N], b[N]; int t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (n == 1) return; int L = n / M;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inline void print(string s = "") {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      template <int M, int N, int K>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int get(int x, int y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int ret = 0, B = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      inline 11 Value() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return ret;
                                                                                                                                                                              return c;
                                                                                                                                                                                                                                                                                                                                                   return c;
                                                                                                                                                                                                                                                                                    Num c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   struct FT {
```

p = k; rep(i, k+1, equ) if(fabs(a[i][col]) > fabs(a[p][col])) p = i;

for(k = col = 0; k < equ & col < var; ++k, ++col){

int Gauss(int equ, int var){

rep(j, 0, pre) free[fnum++] = j;

if (p != k) rep(j, col, var+1) swap(a[p][j], a[k][j]);

 $if(fabs(a[k][col]) < eps) {k--; continue;}$

rep(i, k+1, equ){
 if (fabs(a[i][col]) < eps) continue;
 db t = a[i][col] / a[k][col];
 rep(j, col, var+1) a[i][j] -= a[k][j] * t;</pre>

```
per(i, 0, k) { rep(j, 0, var) if (fabs(a[i][j]) > eps) { p = j; break;
                                                                                                                                                                                                                                                                   rep(j, p+1, pre) free[fnum++] = j, x[j] = (?); pre = p;
                                                                                                                                                                                                                         rep(1, \bar{p}, \bar{var+1}) \bar{a}[j][1] = a[i][1] * t;
                                      一组合法自由变元
                                                                                                                                                                                                                                                                                                           rep(j, p+1, var) x[p] = a[i][j] * x[j]
                                                                                                                                                                                   rep(j, 0, i) if (fabs(a[j][p]) > eps) {
                 db a[N][N], x[N]; //增广矩阵和解集
                                      int free[N], fnum, k, col, p; //
const db eps = 1e-14;
                                                                                                                                                                                                        db t = a[j][p] / a[i][p]
                                                                                                                        int pre = var; fnum = 0;
static const int N = 505
                                                                                                                                                                                                                                                                                          x[p] = a[i][var];
                                                                                                                                                                                                                                                                                                                              x[p] /= a[i][p]
                                                                                                 void genx(int var) {
                                                                                                                                                                                                                                                                     14 467509451
*/
                 8 118835338
9 246325263
                                                                                                                                             304035978
                                                        12 86475609
14 9196980
18 4138593
21 32705801
24 304035978
                                                           86475609
                                                                                                                                                                                                                                                 8 372528824
                                                                                                                                                                                                         4 86583718
                                                                                                                                                                                                                         7 14553391
95932470
                                                                                                                                                                                      998244353
```

Fraction

```
// gcd(fib[n], fib[m]) = fib[gcd(n, m)]
// sum(fib[1..n]) + 1=fib[n + 2]
```

Fib

7.10

7.11

```
* c.b); }
* c.b); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                bool operator == (const Fra &c) const { return a == c.a && b == c.b; } bool operator != (const Fra &c) const { return !(*this == c); } void print() { cout << a << "/" << b; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Fra operator + (const Fra &c) const { return Fra(a * c.b + b * c.a, b Fra operator - (const Fra &c) const { return Fra(a * c.b - b * c.a, b Fra operator * (const Fra &c) const { return Fra(a * c.a, b * c.a); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Fra operator * (const Fra &c) const { return Fra(a * c.a, b Fra operator / (const Fra &c) const { return Fra(a * c.b, b
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Fra operator * (const T &c) const { return Fra(a * c, b); } Fra operator / (const T &c) const { return Fra(a, b * c); }
                                                                                                                                                                           stringstream ss(s); char c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                            if(b < 0) a = -a, b = -b;
                                                                                                                                                                                                                                                                                                                                                                                                                         = _a / d, b = _b / d;
                                                                                                                                                                                                                                                                                                              Fra(T c) : a(c), b(1) {}
Fra(T _a, T _b) {
                                                                                                                                                                                                                                                                                                                                                                                     T d = gcd(a, b);
                                                                                                    Fra(): a(0), b(1) {}
                                                                                                                                                                                                                                             *this = Fra(a, b);
                                                                                                                                                                                                                  ss >> a >> c >> b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     typedef Fra<ll> fll;
                                                                                                                                     Fra(string s) {
template<class T>
                                struct Fra{
                                                                      та, b;
```

per(i, 0, var) {
 db t = a[i][var];
 rep(j, i+1, var) if (fabs(a[i][j]) > eps) t -= x[j] * a[i][j];

x[i] = t / a[i][i];

return 0;

return var — k;//自由变元个数

// genx(var);

if(k < var){

GaussDB 7.12

namespace GaussDB{

```
int free[N], fnum, k, col, p; // 一组合法自由变元
int add(int a, int b) {if ((a += b) >= P) a -= P; return a < 0 ? a + P : a;}
int mul(int a, int b) {return 111 * a * b % P;}
                                                                                                                        static const int N = ::N, P = 1e9 + 7;
                                                                                                                                                  int a[N][N], x[N]; //增广矩阵和解集
GaussInt
                                                                                         namespace GaussInt{
7.13
```

```
return (b/c)^*n+(a/c)^*n^*(n-1)/2+(a\%c?cal(c,(a^*n+b)\%c,a\%c,(a\%c^*n+b\%c)/c):0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               11 cal(11 a, 11 b, 11 c, 11 n) { // sum_{i=0...n-1}floor((a*i+b)/c)
if(n == 0) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 0, equ) if (i != k && a[i][col]) a[i] ^= a[k];
                                                                                                                                                                                                                                                                                                                                                     for(k = 0, col = 0; k < equ \&\& col < var; k++, col++){
 p = k; rep(i, k, equ) if (a[i][col]) {p = i; break;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      per(i, 0, var){
    x[i] = a[i][var];
    rep(j, i+1, var) x[i] ^= (a[i][i] && x[i]);
                           rep(i, 0, fnum) x[free[i]] = (msk >> i) & 1;
per(i, 0, k) {
    rep(j, 0, var) if(a[i][j]) { p = j; break;
    x[p] = a[i][var];
                                                                                                                                                             rep(j, p+1, var) x[p] \wedge = (a[i][j] \&\& x[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                k—; free[fnum++] = col;//这个是自由变元
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, k, equ) if (a[i][var]) return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, col, var) free[fnum++] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                     if (p != k) swap(a[k], a[p]);
if (!a[k][col]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return var — k;//自由变元个数
                                                                                                                                                                                                                                                                                             int Gauss(int equ, int var){
  void genx(int msk, var) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // genx(0, var);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    7.16 LinearBasis
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        LikeEuclid
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(k < var) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        //唯一解, 回代
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        7.15
int kpow(int a, int b) {int r=1;for(;b;b>>=1,a=mul(a,a)) {if(b&1)r=mul(r,a);}return r ||
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int t = a[i][col];
rep(j, col, var+1) a[i][j] = add(a[i][j], -mul(a[k][j], t));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(j, i+1, var) if (a[i][j]) t = add(t, -mul(a[i][j], x[j]));
                                                                                                                                                                                                                                                                                        rep(1, p, var+1) a[j][1] = add(a[j][1], -mul(a[i][1], t));
                                                                                                                                                                                                                                                                                                                                                     rep(j, p+1, pre) free[fnum++] = j, x[j] = (?); pre = p; x[p] = a[i][var];
                                                                                                                                                                                                                                                                                                                                                                                                                     rep(j, p+1, var) x[p] = add(x[p], \neg mul(a[i][j], x[j]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int Gauss(int equ, int var){
   for(k = col = 0; k < equ && col < var; ++k, ++col){
      p = k; rep(i, k, equ) if (a[i][col]) {p = i; break;}
   if (p != k) rep(j, col, var+1) swap(a[p][j], a[k][j]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int inv = kpow(a[k][col], P - 2);
rep(i, col, var+1) a[k][i] = mul(a[k][i], inv);
rep(i, k+1, equ) if (a[i][col]) {
                                                                                                                      int pre = var; fnum = 0;
per(i, 0, k) {
    rep(j, 0, var) if (a[i][j]) { p = j; break;
    rep(j, 0, i) if (a[j][p]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, k, equ) if (a[i][var]) return –1;//无解
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(!a[k][col]) {k--; continue;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(j, 0, pre) free[fnum++] = j;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return var — k;//自由变元个数
                                                                                                                                                                                                                                                        int t = a[j][p];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int t = a[i][var];
                                                                                               void genx(int var) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              per(i, 0, var) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            //genx(var);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         GaussXor
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            x[i] = t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(k < var).
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         7.14
```

```
if (a[i]) x^=a[i]; else { a[i]=x; break; }
                                                                                                                                                                 for(int i=M-1; \sim i \& x; \longrightarrow i) if (x>>i\& 1)
                                                                                                           void Clear() { memset(a, 0, sizeof(a)); }
                                                                                                                                     void ins(11 \times){
// 普通集合线性基
                              const int M=63;
                                                                                  11 a[M];
                                                          struct LB{
                                                                                                   //有 equ 个方程, var 个变元。增广矩阵行数为 equ 列数为, [0..var]
bitset<n> a[N]; //增广矩阵 modif
                                                                                                                                                                                                                         int free[N], fnum; //一组合法自由变元(多解枚举自由变元可以使用)
//返回值为 –1 表示无解,为 Θ 是唯一解,否则返回自由变元个数
                                                                                                                                                                                         int p, col, k; // k 为增广矩阵的秩
                                                                               static const int N = 2e3 + 10;
                         //对 2 取模的 01 方程组
                                                                                                                                                             int x[N]; //解集
                                                          namespace Gauss{
```

```
// f[n] 为 n 的最小质因子 ; g[n]=f[n]^k; phi[n] 为欧拉函数 ; u[n] 为莫比乌斯函数 ; h[n] 为一般积性函数
                                                                                  per(i, m, 2*m) rep(j, 0, m) (u[i - m + j] += c[j] * u[i]) %= P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for (int j = 1, k; j <= M && p[j] <= f[i] && i * p[j] <= n; j++){
  f[k = i * p[j]] = p[j];
  if (p[j] < f[i]) {</pre>
                                                          rep(i, 0, m) rep(j, 0, m) (u[i + b + j] += v[i] * v[j]) \% = P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // phi[i*p[j]]=phi[i]*(p[j]<f[i]?phi[p[j]]:p[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // u[i*p[j]]=u[i]*(p[j]<f[i]?u[p[j]]:0);
                                                                                                                                              copy(u.begin(), u.begin() + m, v.begin());
                                                                                                                                                                                                                                                                                                                                                                                                                                                 int n, M, f[N], g[N], h[N], phi[N], u[N], p[N];
                                                                                                                                                                                                                                     ۳,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    u[1]=phi[1]=1,h[1]=(0); // 1 的时候特判
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       phi[k] = phi[i] * phi[p[j]];
                                                                                                                                                                                                                                   rep(i, 0, m) (ans += v[i] * a[i]) %=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         h[k] = h[i / g[i]] * (0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   phi[k] = phi[i] * p[j];
u[k] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    u[k] = u[i] * u[p[j]];

h[k] = h[i] * h[p[j]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      g[k] = g[i] * p[j];
                                                                                                                                                                                                                                                                                                                                                     MathFunction
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      } /* 质数次幂特判
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        f[i] = g[i] = i;
    if(x < m) u[x] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     phi[i] = i - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // 质数的时候特判
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              g[k] = p[j]
                                                                                                                                                                                                                                                                                                                                                                                                                      const int N = 1e6 + 7;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           h[i] = (0);
                                                                                                                                                                                                                                                              return (ans+P)%P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              void prime(int n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     u[i] = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (!f[i]) {
   p[++M]=i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 2, n+1)
                                                                                                                                                                                                      11 ans = 0;
                                                                                                                                                                                                                                                                                                                                                       7.18
                                                                                                                                                                                                                                                                                                                                                                                                        11 Qry(int 1,11 x=0) { per(i,0,M) if (id[i]>=1) x=max(x,x^a[i]); return x; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for(int i=M-1; ~i && x; --i) if (x>>i&1)
if (a[i]) x^=a[i],y^=tmp[i]; else { a[i]=x,tmp[i]=y; return 1; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void build () { per(i,0,M) per(j,0,i) a[i]=min(a[i],a[i]^a[j]); }
                                                                                                                                              \label{eq:const} \textbf{void} \; \texttt{Copy}(\textbf{const} \; \texttt{LB} \; \&\texttt{L}) \; \{ \; \texttt{rep}(\texttt{i}, \texttt{0}, \texttt{M}) \; \texttt{a[i]=L.a[i]}, \texttt{id[i]=L.id[i]}; \; \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          per(i,0,M) if (B.a[i]) if (!AA.I(B.a[i],y)) C.I(y,Z);
                                                                                                                                                                                                                                                                                           else if (no>id[i]) swap(a[i],x),swap(id[i],no);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  friend void Intersect(LB &A,LB &B,LB &C) {
LB AA; 11 y,z; AA.Copy(A),C.Clear(); mem(tmp,0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             11 a[M];
LB() { mem(a,0); }
void Clear() { mem(a,0); }
void Copy(LB &A) { rep(i,0,M) a[i]=A.a[i]; }
// 向 this 中插入 x , 返回 y 在后来插入元素中的投影
                                                                                                                                                                                                                                 for (int i=M-1; ~i && x; —i) if (x>>i&1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for(int i=M−1; ~i && x; —i) if (x>>i&1)
                                                                                                                 void Clear() { memset(a, 0, sizeof(a)); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (a[i]) x^=a[i]; else return 0;
// 可持久化线性基 ( 序列前缀最右线性基
                                                                                                                                                                                                                                                              if (!a[i]) a[i]=x,id[i]=no;
                                                                                                                                                                              void Ins(LB &L,ll \times, int no) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           }
// 化为最简型,方便线性空间的
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              bool I(11 x,11 &y) {
                                                                                    11 a[M]; int id[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // 集合线性基求交与查询
                                                                                                                                                                                                                                                                                                                          x^=a[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   bool Q(11 ×) {
                                 const int M=32;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               const int M=33;
                                                                                                                                                                                                             Copy(L);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            11 tmp[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    struct LB{
                                                              struct LB{
                                                                                                                                                                                                                                                                                                                                                                                                                                     } B[N];
```

LLZ

```
/*phi[i*j]=phi[i]*phi[j] (gcd(i,j)=1)
                          v[i^*j] = v[ij^*j'(j|i)]
v[i^*j] = v[ij^*v[jj]'(gcd(i,j)=1)
                                                                                                                                                                                                                     7.19
                                                                                                                                                                                            __builtin_clzll(n)) : 0; W; W >>= 1, X <<= 1) {
                                                         // a_{m} = \sum_{j=0}^{4} -m1 a_{j} = 0 
                                                                                    int linear_recurrence(ll n, int m, vi a, vi c) {
                                                                                                                                                                                              for(11 x = 0, W = n? 111<<(63 -
                                                                                                                                                                                                                                                int b = !!(n & W); if(b) x++;
                                                                                                                                          vector<ll> v(m, 0), u(m < 1, 0);
LinearRecursion
                                                                                                             if (n<m) return (a[n]+P)%P;</pre>
                                                                                                                                                                                                                     fill(all(u), 0);
                                                                                                                                                                 V[0] = 1;
7.17
```

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bool operator != (const Mod& rhs) const { return \times != rhs.\times; } Mod operator += (const Mod& rhs) { if ((\times += rhs.\times) >= mod) \times -= mod; return *this
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ; } Mod operator -= (const Mod& rhs) { if (sT(x -= rhs.x) < 0) x += mod; return *this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 static void set_mod(T m) { mod = m, inv = mul_inv(mod), r2 = -dT(mod) % mod; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Mod operator *= (const Mod& rhs) { x = reduce(dT(x) * rhs.x); return *this;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ъ,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Mod r(1); for (Mod a = *this; e; e >>= 1, a *= a) if (e \& 1) r *=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Mod operator + (const Mod &rhs) const { return Mod(*this) += rhs; }
Mod operator - (const Mod &rhs) const { return Mod(*this) -= rhs; }
Mod operator * (const Mod &rhs) const { return Mod(*this) *= rhs; }
                                                                                                                                                                                                                                                                                                         T \gcd(T \ a, T \ b) \ \{ \ while \ (b) \ \{ \ T \ t = a \ % \ b; \ a = b; \ b = t; \ \} \ return \ a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            Mod(\overrightarrow{T}_x): \overrightarrow{x}(init(\underline{x})) {}
bool operator == (const Mod& rhs) const { return x == rhs.x; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rtic T reduce(dT x) {
T y = T(x >> wb) - T((dT(T(x) * inv) * mod) >> wb);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return !e ? x : mul_inv(n, e - 1, x * (2 - x * n));
                                                                                                                                                                                      inline uint isgrt(ull x) { return sqrtl(x); }
inline uint ctz(ull x) { return __builtin_ctzll(x); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           Mod operator - () const { return Mod() - *this; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              static T init(T w) { return reduce(dT(w) * r2); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             static T mul_inv(T n, int e = 6, T x = 1) {
                                                                                                                                                      inline ull sqr(ull \times) { return \times * \times; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  static const int wb = sizeof(T) * 8;
                                                                                                                                                                                                                                                                                                                                                                                  template <class T, class dT, class ST>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    T get() const { return reduce(x); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return ST(y) < 0 ? y + mod : y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       static T modulus() { return mod; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         using Mod64 = Mod<ull, uint128, ll>;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          using Mod32 = Mod<uint, ull, int>;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   template \Rightarrow uint Mod32::mod = 0,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         template \Rightarrow uint Mod32::inv = 0,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                template \Leftrightarrow ull Mod64::mod = \Theta;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      template \Rightarrow ull Mod64::inv = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            template \Rightarrow ull Mod64::r2 = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         template <class T, class mod>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            :emplate <> uint Mod32::r2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Mod pow(ull e) const {
                                                                               using pli = pair<ull, uint>;
                                                                                                                                                                                                                                                                                                                                                                                                                                                      static T mod, inv, r2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    static T reduce(dT x)
                                         using uint = unsigned int;
                                                                                                                                                                                                                                                                        template <class T>
using 11 = 1ong long;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              40d(): x(0) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return r;
                                                                                                                     namespace prime {
                                                                                                                                                                                                                                                                                                                                                                                                                           struct Mod {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int i = 1; i < N; i <<= 1)
  for (int j = 0, t = N / (i << 1); j < N; j += i << 1)
  for (int k = 0, 1 = 0, x, y; k < i; k++, 1 += t)
  x = (11) w[f][1] * a[j+k+i] % P, y = a[j+k], a[j+k] = (y+x) % P, a[j+k+i]</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (f) for (int i = 0, x = kpow(N, P-2); i < N; i++) a[i] = (11)a[i] * x % P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for (int i = 1, x = kpow(G, (P-1) / N), y = kpow(x, P-2); i < N; i++) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rev[i] = (rev[i>>1] >> 1) | ((i&1) << (d-1));   
w[0][i] = (11)× * w[0][i-1] % P, w[1][i] = (11) y * w[1][i-1] % P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  * 首先列出所有可能的染色方案,然后找出每个置换下保持不变的方案(不动点)数。* 等价类数目:所有置换的不动点数的平均值。
                                                                                                                                                                                                                                                                                                11 c = 1;
for (; b; b >>= 1,a = a * a % P) if (b & 1) c = c * a %P;
                                                                                                                                                                             static const int G = 3, P = 1004535809; //P = C*2^{1}k + 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 0, N) if (i < rev[i]) swap(a[i], a[rev[i]]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              na)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void doit(int *a, int *b, int na, int nb){ // [0,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           work(), FFT(a,0), FFT(b,0);
rep(i, 0, N) a[i] = (11)a[i] * b[i] % P;
FFT(a, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for (N = 1; N < na + nb - 1; N <<= 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              //rep(i, 0, N) cout << a[i] << endl;
                                                                                                                                                                                                                int N, na, nb, w[2][M], rev[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int d = __builtin_ctz(N);
w[0][0] = w[1][0] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        using uint128 = __uint128_t;
using ull = unsigned long long;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     = (y-x+P) % P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(i, na, N) a[i] = 0;
rep(i, nb, N) b[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Polya enumeration theorem
                                                                                                                                                                                                                                                                                                                                                                                                                                                   void FFT(int *a, int f){
                             const int M = 1 << 17 << 1;
                                                                                                                                                                                                                                                       11 kpow(11 a, int b){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               * 一个循环的颜色需相同
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Burnside's lemma
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Polya
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            void work(){
                                                                   int a[M], b[M];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Rho
                                                                                                                                             struct NTT{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             7.20
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           } ntt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             7.21
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\widehat{\times}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if (g == 1) continue;
if (g == n) for (g = 1, y = sy; g == 1; ) y = y * y + mc, g = gcd(n, (y == n)) for <math>(g == 1, y = sy; g == 1; y = y = x + mc, g = gcd(n, y == x + mc, g = x + mc, g = gcd(n, y == x + mc, g = x + mc, g = gcd(n, y == x + mc, g = x + mc, g = x + mc, g = gcd(n, y == x + mc, g = x + m
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               auto sy = y;
for (int i = 0; i < (int)min(s, 1 - k); ++i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (n < (1u << 31)) return brent<uint, Mod32>(n, c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for (int i = 0; i < (int)1; ++i) y = y * y + mc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                = 2;
                                                                   T brent(T n, T c) \{ // n \text{ must be composite and odd.} \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          Q
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ull v2 = sqrtl(n), v3 = cbrtl(n), v = v2,
if (v2 * v2 == n || v3 * v3 * v3 == n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            while (p.divide(n)) n = n / p, e^{++};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for (int k = 0; k < (int)1; k += s)
                                                                                                                                                                                                                                                                               const mod one = mod(1), mc = mod(c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               while (n > lim && !is_prime(n)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (v2 * v2 != n) v = v3, b =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ull lim = sqr(primes.back().n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return brent<ull, Mod64>(n, c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for (auto &&e: ret) e.se *=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ret.emplace_back(p.n, e);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              uint e = 1; n = n / p;
                                                                                                                                                                                                                                                                                                                                   mod y = one;

for (ull l = 1; ; l \ll 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (sqr(p.n) > n) break;
template <class T, class mod>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          assert(n < (1ull << 63));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            y = y * y + mc;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       T g = gcd(n, p.x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for (auto &&p: primes) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 vector<pli>rectors(ull n)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ull brent(ull n, ull c) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ret.emplace_back(2,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (n <= 1) return {};</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (p.divide(n)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                x - \lambda = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           uint s = ret.size();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ret = factors(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    uint e = ctz(n)
                                                                                                                                            const ull s = 256;
                                                                                                                                                                                                                mod::set_mod(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            vector<pli>ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (!(n & 1)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       mod p = one;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return g;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          auto x = y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      n >>= e;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ×:
```

```
if (n < (1u << 31)) return !composite<uint, Mod32>(n, bases[x], y);
                                                                                                                                                                                                                                                                                                                                                                                                                                  bool is_prime(ull n) { // reference: http://miller-rabin.appspot.com
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ExactDiv(ull n) : n(n), i(Mod64::mul\_inv(n)), t(ull(-1) / n) {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   friend ull operator / (ull n, ExactDiv d) { return n * d.i; };
bool divide(ull n) { return n / *this <= t; }</pre>
                                                                                                                                                                                                                                                                  for (j = s - 1; j > 0; --j) { if ((a *= a) == fone) break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       .;
o
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            {2, 2570940, 211991001, 3749873356u},
{2, 2570940, 880937, 610386380, 4130785767u},
{2, 325, 9375, 28178, 450775, 9780504, 1795265022}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (uint i = 2; i <= sqrt_n; ++i) if (is_prime[i])
if (i != 2) primes.pb(ExactDiv(i));</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for (uint j = i * i; j <= n; j += i) is_prime[j]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return !composite<ull, Mod64>(n, bases[x], y);
bool composite(T n, const uint* bases, int m)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    else if (n < 3770579582154547) \times = y = 5;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 else if (n < 47636622961201) \times = y = 4;
                                                                                                                                                                                                                                 if (a == one || a == fone) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    else if (n < 4759123141) \times = 2, y = 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  else if (n < 154639673381) \times = y = 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                else if (n < 19471033) \times = 1, y = 2;
                                                                                                                                 mod one(1), fone(n - 1); for (int i = 0, j; i < m; ++i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               static const uint bases[][7] = {
                                                                                                                                                                                              mod a = mod(bases[i]) pow(d);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                {2, 3},
{2, 299417},
{2, 7, 61},
{15, 176006322, 4221622697u},
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                vector<bool> is_prime(n + 1, 1);
                                                                    int s = \_builtin\_ctzll(n - 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (n < 1373653) \times = 0, y = 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (!(n & 1)) return n == 2;
if (n <= 8) return 1;
int x = 6, y = 7;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 assert(n < (ull(1) << 63));
                                                                                                                                                                                                                                                                                                 if (j == 0) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               uint sqrt_n = sqrt(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    };
if (n <= 1) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     vector<ExactDiv> primes;
                                                                                                T d = (n - 1) >> S;
                                        mod :: set_mod(n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   void init(uint n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    primes.clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   struct ExactDiv {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ExactDiv() {}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ull n, i, t;
                                                                                                                                                                                                                                                                                                                                                                     return 0;
```

```
rep(i, 1, m + 1) if (sgn(A[i][j]) > 0 && b[i] / A[i][j] < tmp) // 找基变量
                                                                                                                                                                                                                                                                                                                      0 很多可以加上 break 因为转轴代价可能较小
                                                                                                                                                                                                                                                                     if (delt < tmp * c[j]) l = r, e = j, delt = tmp * c[j];</pre>
                                                                                                                                         rep(j, 1, n + 1) if (sgn(c[j]) > 0) { // 找非基变量
                      //if (!ini()) return —DINF; // 无解 b < 0 need ini()
                                                                                                                                                                                                                                              if (tmp == DINF) return DINF; // 无界
                                                                                                                                                                                                                       r = i, tmp = b[i] / A[i][j];
                                                                                                                                                                                                                                                                                                                      // 贪心取最大如果矩阵为全幺模或
                                                                                                                                                                                                                                                                                                                                                                J
if (e == -1) break; // 找到最优解
                                               rep(i, 1, n+1) ans[i] = 0;
                                                                                               int r, 1, e = -1;
                                                                                                                                                                     db tmp = DINF;
                                                                                                                         db delt = -DINF;
                                                                                                                                                                                                                                                                                                 break;
                                                                      while (1) {
 db run() {
                                                                                                                                                                                                }
if (n > 1) ret.emplace_back(n, 1);
if (ret.size() - s >= 2) sort(ret.begin() + s, ret.end());
                                                                        uint e = 1; n /= p;
while (n % p == 0) n /= p, e += 1;
                                         if (!is_prime(p)) continue;
                                                                                                                         ret.emplace_back(p, e);
For (ull c = 1; ; ++c) {
                        ull p = brent(n, c);
                                                                                                                                                                                                                                                                                                                                                                        Simplex
                                                                                                                                                    break;
                                                                                                                                                                                                                                                                                                                                                                        7.22
```

7.23

} } sb;

db v, ans[M], b[M], c[M], A[M][M]; // 全幺模矩阵可以改整数

/* n - variables, m - equations

* s.t.Ax <= b, x >= 0

* maxf(x)=cx

const db EPS = 1e-8, DINF = 1e15;

static const int M = 550

struct Simplex {

int n, m, B[M], N[M];

```
SternBrocotTree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   typedef pair<U, U> pii;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  typedef long double db;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             const U INF = 1e9 + 7;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        typedef int U;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         namespace SBT {
                                                                                                                                                                                                                                                                                                                                                       // f(a, c)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(j, 1, n+1) if (sgn(A[1][j]) < 0 && (e == -1 \mid | (rand() \& 1))) = j;
                                                                                                                                                                                                                                                                                                                rep(j, 1, n + 1) A[i][j] -= (j!=e) * A[i][e] * A[1][j]; // 可以链式优化
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 1, m+1) if (sgn(b[i]) < 0 \& (1 == -1 || (rand() \& 1))) = i;
                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 1, n + 1) c[i] -= (i!=e) * c[e] * A[l][i];
v += b[l] * c[e]; c[e] *= -A[l][e]; swap(B[l], N[e]);
                                                                                                                                inline int sgn(db x) \{ return (x > EPS) - (x < -EPS); \}
                                                                                                                                                                                                         b[1] /= tmp, A[1][e] = 1 / tmp;
rep(i, 1, n + 1) if (i != e) A[1][i] /= tmp;
rep(i, 1, m + 1) if (i != 1 && sgn(A[i][e])) {
                      A[i][e] = - A[i][e] / tmp;
                                                                                                                                                                                                                                                                                      b[i] -= A[i][e] * b[1];
void init(int _n, int _m) {
                                                                                                                                                          void pivot(int 1, int e) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(e == -1) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             bool ini(){ // 随机化初始解
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 while(1){
int 1 = -1, e = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(1 == -1) break;
                                                                                                                                                                                    db tmp = A[1][e];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    pivot(l, e);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return 1;
```

Simpson

rep(i, 1, m+1) if (B[i] <= n) ans[B[i]] = b[i]; return v;

pivot(1, e);

```
fbc,
                                                                                                                                                                                                                                                                                                                                      R, fb,
                                                                                                                                                                                                                                                                                                                                 return asr(a, ab, b, esp / 2, L, fa, fab, fb) + asr(b, bc, c, esp / 2,
                                                                                                                                                                                                                                                                    db L = simpson(fa, fab, fb, a, b), R = simpson(fb, fbc, fc, b, c);

if (fabs(L + R - A) <= 15 * esp) return L + R + (L + R - A) / 15.0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      fc);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    fc, a, c), fa, fb,
                                                                                                                                                                                  db fb, db fc) {
                                                                                      db a, db c) {
                            const db eps = 1e-10; // 精度感觉一般要多设 1e-3 左右
                                                                                                                                                                             db asr(db a, db b, db c, db esp, db A, db fa, db ab = (a + b) / 2, bc = (b + c) / 2; db fab = F(ab), fbc = F(bc);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    fb,
                                                        inline db F(db x) { F(x) = (?) }
inline db simpson(db fa, db fb, db fc, db a,
return (fa + 4 * fb + fc) * (c - a) / 6;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  simpson(fa,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   db fa = F(a), fb = F(b), fc = F(c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                      db asr(db a, db c, db eps) {
    db b = (a + c) / 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return asr(a, b, c, eps,
namespace Simpson {
```

```
for(int i = 1; i <= m && 111 * p[j] * p[j] <= w[i]; i++){ 11 t = w[i] / p[j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     for(int i = y; i <= tot && 111 * p[i] * p[i] <= x; i++){
    11 t1 = p[i], t2 = 111 * p[i] * p[i];
    for(int e = 1; t2 <= x; e++, t1 = t2, t2 *= p[i]) {
    if (F(p[i], e)) ret += S(x / t1, i + 1) * F(p[i], e);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       tot = upper_bound(p + 1, p + cntp + 1, Sqr) - (p + 1);
                                                                                                                                                                                                                                                                                                                            rep(i, 2, n+1) {
   if(!isp[i]) p[++cntp] = i;
   for(int j = 1; j <= cntp && i * p[j] <= n; j++){
        isp[i * p[j]] = 1;
        isp[i * p[j]] = 1;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, 1, cntp+1) sp[i] = sp[i - 1] + f(p[i]);
p[++cntp] = INT_MAX;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int k = t <= Sqr ? id1[t] : id2[n / t];
g[i] -= f(p[j]) * (g[k] - sp[j - 1]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                Ξ
                                                                                      // 要求的积性函数 F(p \land e)
11 F(int p, int e) { return e == 1? -1: 0;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            w[m] \le Sqr ? id1[w[m]] = m : id2[j] =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ret += F(p[i], e + 1);// 合数的答案
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         11 ret = -(g[k] - sp[y-ī]);// 质数的答案
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int k = (x \le Sqr ? id1[x] : id2[n/x]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   For (11 \ i = 1, \ j; \ i <= n; \ i = j + 1)
                                                                                                                                                                            // 假设都是质数的完全积性函数前缀和去掉
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(x \le 1 \mid | p[y] > x) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(i % p[j] == 0)break;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               11 solve(11 _n) {
    n = _n;if (n == 0) return 0;
    m = 0;Sqr = sqrt(n);
                                                                                                                                                                                                          ll calc(ll n) { return n - 1;}
                       11 f(int p) { return 1;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              g[m] = calc(w[m]);
                                                                                                                                                                                                                                                                                                    cntp = 0; isp[1] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               j = n / (n / i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(j, 1, tot + 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  w[++m] = n / i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return S(n,1) + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   S(11 x, int y){
                                                                                                                                                                                                                                                                        void prime(int n){
// f(p) = p \wedge k
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        Π
                                                                                                                                                                                                                                                                        pii operator+(const pii &a, const pii &b) { return mp(a.fi + b.fi, a.se + b.se); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            pii solve(V v, U MAXB) { // find ROUND_HALF_UP(a / b) = v, b <= MAXB
                                                                                                                                                                                                                                                                                                  pii operator*(const pii &a, U \times) { return mp(a.fi * \times, a.se * \times); } bool search(V \vee, U MAXB, pii &lo, pii &hi, int f) {
                                                                                                                                                                                                                                                                                                                                                                                             U 1 = 0, r = f > 0? (hi.se? (MAXB - 10.se) / hi.se : INF)
                           typedef pair<T, T> V; // V = [double|long double|fraction]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               } db t1 = (db) lo.fi / lo.se; db t2 = (db) hi.fi / hi.se; db t3 = (db) v.fi / v.se; if (t2 - t3 <= t3 - t1) return hi;else return lo;
                                                                                                                                                                              inline bool in(const V &a, const V &b, const V &c)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               f > 0 ? 10 = 10 + hi * r : hi = 10 * r + hi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          //V m = mp(lo.fi + hi.fi, lo.se + hi.se);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      //if (in(L, R, m)) return mp(m.fi, m.se);
                                                                                                                                                                                                                                                                                                                                                                                                                           (lo.se ? (MAXB - hi.se) / lo.se : INF);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Uz = (1 + r) >> 1;
 x = f > 0 ? 10 + hi * z : 10 * z + hi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int Sqr, m, p[N], id1[N], id2[N], tot, cntp;
11 g[N], sp[N], h[N], n, w[N];
bool isp[N];
                                                                                                                                                                                                       return 0 <= cmp(c, a) && cmp(c, b) < 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             f * cmp(x, v) \le 0 ? 1 = z : r = z;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       = f > 0 ? lo + hi * r : lo * r + hi;
                                                          inline int cmp(const V &a, const V &b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           hi, 1);
hi, —1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   V L = mp(v.fi * 10 - 5, v.se * 10);
V R = mp(v.fi * 10 + 5, v.se * 10);
                                                                                      T \times = a.fi * b.se - a.se * b.fi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   r = f * cmp(x, v) \le 0 ? r : 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    //if (in(L, R, lo)) return lo;
//if (in(L, R, hi)) return hi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ok |= search(v, MAXB, lo, ok |= search(v, MAXB, lo,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        // F(1) 要拆成多个完全积性函数的和
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               static const int N = 1e6 + 7;
                                                                                                                    return (x > 0) - (x < 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    pii lo(0, 1), hi(1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                       while (1 + 1 < r) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return mp(-1, -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ok |= search(v,
if (!ok) break;
  typedef __int128 T;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                bool ok = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                while (true) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return r > 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    25
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      min
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        struct Min_25{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  7.25
```

t);

t);

t)) : add(p3, mul(h[i][0],
t)) : add(p4, mul(h[i][1],

ans;

ပ်

ploynomial 7.26

```
11 kpow(11 a, 11 b) {11 r=1;for(;b;b>>=1,a=mul(a,a)) {if(b&1)r=mul(r,a);}return r;}
void init(int M) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  qpolysum(ll R, ll n, ll *a, ll m) { // a[0].. a[m] \setminus sum_{i=0} \setminus \{n-1\} \ a[i] \times ni
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Polysum(11 n, 11 *a, 11 m) { // a[0].. a[m] \sum_{i=0}^{i=0}^{n}{n-1} a[i]
                                                                                                                                    11 a[D], fac[D], ifac[D], p1[D], p2[D], h[D][2], C[D];
11 add(11 a, 11 b) {a = (a + b) % P; return a < 0 ? a + P : a;}
11 mul(11 a, 11 b) {a = 111 * a * b % P; return a < 0 ? a + P : a;}</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 fac[0] = 1; rep(i, 1, M+5) fac[i] = mul(fac[i-1], i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(i, 0, m+2) h[i][0] = add(h[i][0], h[i][1] * c);
rep(i, 0 ,m+2) C[i] = h[i][0];
ans = add(mul(calcn(m, C, n), kpow(R, n)), —c);
                                                                                                                                                                                                                                                                                                                                                                               per(i, 0, M+4) ifac[i] = mul(ifac[i+1], i+1);
                                                                                                                                                                                                                                                                                                                                                                                                                                           ll calcn(int d, ll *a, ll n) { // a[0].. a[d]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ans = (d-i)&1? add(ans, -t) : add(ans,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      h[i][0] = mul(h[i-1][0] + a[i-1], r);
h[i][1] = mul(h[i-1][1], r);
                                                                                                             static const int D = 101000, P = 998244353;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(i, 1, m+2) a[i] = add(a[i-1], a[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          p4 = 0,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           11 t = mul(ifac[i], ifac[m+1-i]);
p3 = i & 1 ? add(p3, -mul(h[i][0],
p4 = i & 1 ? add(p4, -mul(h[i][1],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ll s2 = mul(ifac[i], ifac[d-i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (R == 1) return Polysum(n, a, m);
                                                                                                                                                                                                                                                                                                                                             ifac[M+4] = kpow(fac[M+4], P - 2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ll t = mul(mul(s1, s2), a[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ll s1 = mul(p1[i], p2[d-i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          <u>۰</u>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             c = mul(kpow(p4, P - 2), -p3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  lī r = kpow(R, P - 2), p3 = h[0][0] = 0; h[0][1] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                a[m+1] = calcn(m, a, m+1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        a[m+1] = calcn(m, a, m+1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return calcn(m+1, a, n—1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (n <= d) return a[n];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    p1[0] = p2[0] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 0, d+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(i, 0, m+2) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 1, m+2)
     polysum
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return ans;
                                                                              struct polysum 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          11 ans=0;
7.27
                                                                                                                                                                                                                                                                            T kpow(T a, T b) {T r=1; for(;b;b>>=1,a=mul(a,a)) {if(b&1)r=mul(r,a);}return r;}
                                                                                                                                                                                                                                                                                                                                                                          rep(i, 0, n+1) rep(j, 0, 2) c[i+j] = add(c[i+j], mul(a[i], b[j]));
memcpy(a, c, sizeof(a[0]) * (n+1));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(j, 0, n+1) if (j != i) a1[0] = mul(a1[0], x[i] - x[j]);
                                                                                                                                                                         Tal[N], bl[N], c[N], a[N], pre[N], suf[N], ifac[N], fac[N]; Tadd(Ta, Tb) {a = (a + b) % P; return a < 0 ? a + P : a; T mul(Ta, Tb) {a = 111 * a * b % P; return a < 0 ? a + P : a;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(j, 0, n+1) if (j != i) s1 = mul(s1, k - x[j]);
rep(j, 0, n+1) if (j != i) s2 = mul(s2, x[i] - x[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void solve(int n, T *x, T *y){ // a[0]^*x^{\wedge 0} ... a[n]^*x^{\wedge n}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   fac[0] = 1;rep(i, 1, n+1) fac[i] = mul(fac[i-1], i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, 1, n+1) pre[i] = mul(pre[i-1], k - i);
per(i, 1, n+1) suf[i] = mul(suf[i+1], k - i);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ans = add(ans, mul(fg*s1, mul(s2, y[i])));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    res = add(res, mul(s1, kpow(s2, P - 2)));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       per(i, 0, n) ifac[i] = mul(ifac[i+1], i+1);
pre[0] = suf[n+1] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(j, 0, n+1) a[j] = add(a[j], a1[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      a1[0] = mul(y[i], kpow(a1[0], P - 2));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         get(int n, int k, T *y) { // x is [1..n]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              get(int n, int k, T *x, T *y) \{ // f(k) \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 T s2 = mul(ifac[i-1], ifac[n-i]);
T fg = (n-i)&1 ? -1 : 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     T s1 = mul(pre[i-1], suf[i+1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(i, 0, n+1) {
fill_n(a1, n+1, 0); a1[0] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(j, 0, n+1) if (j i= i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          b1[0] = -x[j]; b1[1] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ifac[n] = kpow(fac[n], P - 2);
                                                                                                        static const int N = 101010;
static const int P = 998244353;
                                                                                                                                                                                                                                                                                                              void calc(int n, T *a, T *b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   T s1 = y[i], s2 = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               calc(n, a1, b1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 fill_n(a, n+1, 0);
                                                                                                                                                                                                                                                                                                                                                fill_n(c, n+1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(i, 0, n+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 1, n+1){
                                                                              struct polynomial{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                T res = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return ans
                                         template<class
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    T ans=0;
```

7

```
for( ; i <= n; (j&1) ? i+=2 : i+=4 , j++) if(bit[j] == 0) p[cntp++]=i;
                            prime
                          7.28
```

7.30

cntp = 2;p[0] = 2;p[1] = 3; for (int i = 5, k = 1; i <= N; (k & 1) ? i+=2 : i+=4 , k++){

void getprime(int N) {

bitset<N / 3 + 1> isp;

// int low[N],

int cntp,p[M];

const int N = 3e7 + 6, M = 2e6 + 6;

// 优化版欧拉筛法 bitset 需要 02

for (int j = 2; j < cntp && p[j] * i <= N; j++) {
 // low[p[j] * ij = p[j];
 isp[p[j] * i / 3] = 1;
 if (i % p[j] == 0) break;</pre>

// low[i] = i;

p[cntp++]=i;

if (!isp[k]) {

const int N = 3e8 + 6, M = 2e7 + 6;

bitset<N / 3 + 1> bit;

int cntp,p[M];

void getprime(int n){

// 优化埃氏筛法空间最小可以不存质数

```
for (; k; k >>= 1, x = x*x%) if (k & 1) ret = ret*x%p;
                                                                                                                                       rep(i, 0, sz(c)) if (Pow(g, c[i], p) == 1) return 0; return 1;
                                                                                                                                                                                                                                    ll tmp = p - 1, g; for (ll k = 2; k*k <= tmp; ++k) if (tmp % k == 0) {
                                                                                                                                                                                                                                                                                                         while (tmp % k == 0) tmp /=
                                                                                                                           inline bool check_g(ll g, ll p)
                                                                                                                                                                                              inline 11 getRoot(11 p) {
11 Pow(11 x, 11 k, 11 p)
                                                                                                                                                                                                                                                                        c.pb(k);
                                                                                                                                                                                                                  c.clear();
                                                                                                          vector<ll> c;
                                                                                                                                                                                                                                                                                                                                                                              return g;
                                                                                        struct Euler {
                   11 ret = 1;
                                                       return ret;
```

7.31

```
11 kpow(11 x, 11 k, 11 p) {
                                                                                                                                                                               11 ret = 1;
inf i, j;
cntp = 2; p[0] = 2; p[1] = 3;
for(i = 5, j = 1; i * i <= n; (j & 1) ? i += 2 : i += 4 , j++) {
  if(bit[j] == 0) {
                                                                                                                                                    if(j \% 2 != 0 && j \% 3 != 0) bit[j / 3] = 1;
                                                                                                                             for(int j = i * i; j <= n ; j += i)
```

```
int m = sqrt(n) + 1;
rep(i, 1, m+1) fv[i] = i * (3 * i - 1) / 2;
rep(i, 2, n+1) {
    for(int j = 1; fv[j] <= i; j++) {
        f[i] = add(f[i], j & 1 ? f[i - fv[j]] : -f[i - fv[j]]);
    if (fv[j] + j <= i) f[i] = add(f[i], j & 1 ? f[i - fv[j]].</pre>
                                                                                                                                                               inline int add(int a, int b) { if((a += b) >= P) a = P; return a < 0 ? a + P : a;)
                                                                                        const int N = 1e6 + 5, P = 998244353;
                                                                                                                         int n, f[N], fv[N];
                                                                                                                                                                                                                               f[0] = f[1] = 1;
                                                                                                                                                                                            void init(int n) {
划分数
```

void getprime() {
 fill_n(isp + 2, N - 2, 1);
 rep(i, 2, N) {
 if (isp[i]) p[cntp++]=i;
 for (int j=0;j<cntp&&p[j]*i<N;j++){</pre>

const int N = 1e6 + 6;

// low[] : optional

// time : 0(n)

int low[N], cntp, p[N];

bool isp[N];

if (i % p[j] == 0) break;

 $\frac{1}{2} \frac{1}{2} \frac{1}$

```
if (x % P == 0) return -1;
11 res = 2 % P, sa, t = 1, sq = sqrt(P); M.clear();
rep(i, 0, sq + 1) { if (M.count(t)) break; M[t] = i, t = t * x %
                                                                                                                                                                                                                                                                                                                                                                                                    ď,
                                                                                                                                                                                                                                                                                                                                 sa %
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           P);
                                                                                                                                                                                                                                                                                                                               return i * sq + M[res]; else res = res
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    z /= t, P /= t, w = w * x / t % P, C++;
                                                                                                                                                                                                                                                                            t = P / sq, sa = Inv(kpow(x, sq, P), P);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           z = z * Inv(w, P) % P, ans = bsgs(x, z,
                                                                                                                                                                                                                                                                                                     rep(i, 0, t + 1) if (M.count(res))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return ans + (ans ! = -1) * c;
inline int Inv(int a, int P) {
   int x, y; ex_gcd(a, P, x, y);
   return x < 0 ? x + P : x;</pre>
                                                                                                                                                                          11 bsgs(11 x, 11 z, 11 P) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (z \% \tilde{t}) return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (z == w) return c;
                                                                                                                                                    unordered_map<11, int> M;
                                                                                                                                                                                                                                                                                                                                                          return -1;
                                                                                                                             struct BSGS {
```

inline bool check_g(ll g, ll p) {
 rep(i, 0, sz(P)) if (kpow(g, P[i], p) == 1) return 0;

vector<ll>P, A; ll phi, g;

return ret;
}
struct Euler {

} (0 ==

P.clear(), A.clear(); for (11 k = 2; $k^*k <= m$; ++k) if (m%k

inline void factor(ll m) {

return 1;

while (m%k == 0) m /= k, cnt++;

int cnt = 0;

P.pb(k), A.pb(cnt);

if (m > 1) P.pb(m), A.pb(1);

for (; k; k >>= 1, x = x^*x %p) **if** (k & 1) ret = ret*x%p;

7.33 高次同余__合数

11 kpow(11 a, 11 b, 11 P) {

```
if (sz(p) == 1) return 1;
if (p[0] != 2 || P[0] == 2 && A[0] > 1) return 0;
return 1;
}
inline || getRoot(|| p) {
   if (p == 1 || p == 2 || p == 4) return phi = p + 1 >> 1, p - 1;
        if (!check(p)) return -1;
        phi = p;
        for (auto t: P) phi = phi / t*(t - 1);
        factor(phi);
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
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        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &t : P) phi = phi / t;
        for (auto &
```

if $(sz(P) > 2 \mid | sz(P) == 1 \& P[0] == 2)$ return 0;

//if (m==1 || m==2 || m==4) return 1;

factor(m);

inline bool check(11 m)

7.32 离散对数

return i * sq + M[res]; else res = res * sa %

return -1;

t = P / sq, sa = Inv(kpow(x, sq, P), P);

rep(i, 0, t + 1) if (M.count(res))

<u>(</u>

 $b ? (ex_gcd(b, a % b, y, x), y = a / b * x) : (x = 1, y = a / b * x)$

void ex_gcd(ll a, ll b, ll &x, ll &y) {

return r;

11 x, y; ex_gcd(a, P, x, y); return x < 0 ? x + P : x;

map<ll, int> M;

struct BSGS {

inline 11 Inv(11 a, 11 P) {

۳,

11 r = 1; assert(b >= 0); for (; b; b >>= 1, a = a * a % P) if (b & 1) r = r * a %

```
Η,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (p == 1 || p == 2 || p == 4) return phi = p + 1 >> 1, phi_phi = 1, p -
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return mp(kpow(a, phi_phi - 1, p)*b%p, g);//note that phi_phi
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if (cnt%a) return mp(-1, 0); bool ok = 0;
if (cnt) t1 = get_pow(pp, cnt), t2 = get_pow(pp, cnt / a),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          pll solve high(ll a, 11 b, 11 pp, int k) {
    assert(pp > 1), assert(k > 0);
    ll p = get_pow(pp, k); norm(b, p); ll t1, t2, t3;
    if (!a) return b == 1 ? mp(0, p) : mp(-1, 0ll);
    if (!b) return mp(!a, get_pow(pp, k - (k - 1) / a - 1));
    ll g = getRoot(p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         for (g = 1; __gcd(g, p) != 1 || !check_g(g, p); ++g);
return g;
                                                                                                                                                                                                                                                                                                                                       factor(m, P, A);
if (sz(P) > 2 || sz(P) == 1 && P[0] == 2) return 0;
if (sz(P) == 1) return 1;
if (P[0] != 2 || P[0] == 2 && A[0] > 1) return 0;
                                                            inline void norm(11 &x, 11 p) { x = (x%p + p) % p; }
                                                                                                                                                                                         -1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (g == -1) return mp(-1, 0);
int cnt = 0; while (b%pp == 0) b /= pp, cnt++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // solve equation: x^a=b(xpp^k), pp is a prime
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   );
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        factor(phi, P, A), phi_phi = get_phi(phi);
// for (auto &t:P) t=phi/t;
                                                                                                                                                     // for (auto t:P) phi=phi/t*(t-1);
rep(i, 0, sz(P)) phi = phi / P[i] * (P[i]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            pll solve(ll a, ll b, ll p) {
    norm(a, p); norm(b, p); ll g = __gcd(a,
                                                                                                                                                                                                                                                                                                               //if (m==1 || m==2 || m==4) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // solve equation: ax=b(%p), gcd(a,p)!=1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 0, sz(P)) P[i] = phi / P[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    pair<ll, ll> t = solve(a, _b, _p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         \dot{t}3 = \dot{t}1 / \dot{t}2, ok = 1, p /= t1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (\_b == -1) return mp(-1, 0);
if (m > 1) P.pb(m), A.pb(1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                11 _b = T.ex_bsgs(g, b, p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     il ret = 1; assert(k \geq 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if (b%g) return mp(-1, g);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            if (!check(p)) return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 0, k) ret = ret*p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            11 _p = p / pp^*(pp - 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          a /= g, b /= g, p /= g;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         }
11 get_pow(ll p, int k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                inline 11 getRoot(11 p) {
                                                                                                                                                                                                                                                                               inline bool check(ll m) {
                                                                                    inline 11 get_phi(11 p)
11 phi = p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              phi = get_phi(p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return ret;
                                                                                                                                                                                                                      return phi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return 1;
```

```
rep(i, 0, 51) { if (t == z) return i; t = t * x % P; } for (t = __gcd(x, P); t != 1; t = __gcd(x, P)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               struct Euler {
   v11 P, A, _P, _A; 11 phi, g, phi_phi; BSGS T;
   inline bool check_g(11 g, 11 p) {
      rep(i, 0, sz(P)) if (kpow(g, P[i], p) == 1) return 0;
   return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     R = (R % M + M) % M; // 可能为 Ø 看是否需要是正整数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if ((a[i] - R) % g) return -1; // 无解
R += inv * ((a[i] - R) / g) % (mod[i] / g) * M;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             } (0 ==
ex_bsgs(11 x, 11 z, 11 P) { //x^y==z(mod P) }
                                                                                                                                                                                                              = z * Inv(w, P) % P, ans = bsgs(x, z, P);
                                                                                                                             z /= t, P /= t, w = w * x / t % P, C++;
                          11 t = 1 % P, w = 1, ans, c = 0; z %= P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         inline void factor(ll m, vll &P, vll &A) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for (11 k = 2; k^*k \le m; ++k) if (m%k
                                                                                                                                                                                                                                                                                                                                                                                                                        if (b == 0) { x = 1; y = 0; return; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 2, n + 1) {
    ll g = __gcd(M, mod[i]);
    ll inv = Inv(M / g, mod[i] / g);
                                                                                                                                                                                                                                                                                                                                                                                              void exgcd(ll a, ll b, ll &x, ll &y)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              while (m%k == 0) m /= k, cnt++;
                                                                                                                                                                                                                                      return ans + (ans !=-1) *
                                                                                                                                                                                                                                                                                                                                           11 M, R; static const int N =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return x < 0 > x + mod : x;
                                                                                                       if (z \% t) return -1;
                                                                                                                                                         if (z == w) return c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           M = M / g * mod[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                              exgcd(b, a % b, y, x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          P.pb(k), A.pb(cnt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       solve(11 n) {
M = mod[1], R = a[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     P.clear(), A.clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         }
ll Inv(ll a, ll mod) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    exgcd(a, mod, x, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           typedef pair<ll, ll> pll;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     11 \times = 0, y = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              typedef vector<ll> vll,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                            y = a / b * x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int cnt = 0;
                                                                                                                                                                                                                                                                                                                                                                       11 a[N], mod[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                :pow =% ×
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return R;
                                                                                                                                                                                                                                                                                                                       struct CRT {
    Ξ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              } crt;
```

7

```
if (p == 1 || p == 2 || p == 4) return phi = p + 1 >> 1, phi_phi = 1, p - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return mp(kpow(a, phi_phi - 1, p)*b%p, g);//note that phi_phi
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // rep(i, \theta, sz(P)) P[i]=phi/P[i];
for (g = 1; __gcd(g, p) != 1 || !check_g(g, p); ++g);
                                                                                                                                                                                                                                                                                                                                               rep(i, 0, sz(P)) if (kpow(g, P[i], p) == 1) return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           inline void norm(11 &x, 11 p) { x = (x + p) % p; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (sz(P) > 2 \mid | sz(P) == 1 \& P[0] == 2) return
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               .
0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (P[0] != 2 || P[0] == 2 && A[0] > 1) return
                                                                                                                                                                                                                                                                                                                                                                                                                                                            P.clear(), A.clear(); for (11 k = 2; k^*k \le m; ++k) if (m%k == 0)
                                                       z = z * Inv(w, P) % P, ans = bsgs(x, z, P);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(i, 0, sz(P)) phi=phi/P[i]*(P[i]-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   __gcd(a, p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for (auto t : P) phi = phi / t^*(t-1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              //if (m==1 || m==2 || m==4) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // solve equation: ax=b(\%p), gcd(a,p)!=1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  factor(phi), phi_phi = get_phi(phi);
                                                                                                                                                                                                                                                           while (m%k == 0) m /= k, cnt++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 norm(a, p); norm(b, p); 11 g =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for (auto &t : P) t = phi / t;
                                                                                   return ans + (ans !=-1) * c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (m > 1) P.pb(m), A.pb(1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (b\%g) return mp(-1, g);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (!check(p)) return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (sz(P) == 1) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  pll solve(ll a, ll b, ll p)
    if (z == w) return c;
                                                                                                                                                                                                                                                                                                                                                                                                                             inline void factor(ll m) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      a /= g, b /= g, p /= g;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        inline 11 get_phi(11 p) {
    11 phi = p;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             inline bool check(ll m) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               inline 11 getRoot(11 p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            P.pb(k), A.pb(cnt);
                                                                                                                                                                                                                               typedef pair<ll, 11> pll;
                                                                                                                                                                                                      typedef vector<ll> vll
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int cnt = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return phi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             factor(m);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return 1;
                                                                                                                                                                                                                                                                                                                                                                              return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return g;
                                   6
                                                                                                                     } // solve equation: x^a=b(\%), p could not be a prime, but p must have a primitive
if (t.fi == -1) return mp(-1, 0);
11 _g = t.se, x = t.fi, ans = kpow(g, x, p), d = kpow(g, _p / _g, p), ret = _
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          t = t * \times % P;
                                                                                                                                                                                                                                                                                        factor(p, _P, _A); int tot = sz(_P); ll ret = 1, ans; pll tmp[32];
rep(i, 0, tot) {
  tmp[i + 1] = solve_high(a, b, _P[i], _A[i]),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     b ? (ex_gcd(b, a \% b, y, x), y = a / b * x) : (x = 1, y = 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ۳,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        11 t = 1 % P, w = 1, ans, c = 0; z %= P;
rep(i, 0, 51) { if (t == z) return i; t = t * x % P; }
for (t = \_gcd(x, P); t != 1; t = \_gcd(x, P)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 0, sq + 1) \{ if (M.count(t)) break; M[t] = i,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ll res = z % P, sa, t = 1, sq = sqrt(P); M.clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return i * sq + M[res]; else res = res * sa % P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for (; b; b >>= 1, a = a * a % P) if (b & 1) r = r *
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ex_bsgs(11 x, 11 z, 11 P) { //x^y==z (mod P) }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           z /= t, P /= t, w = w * x / t % P, C++;
                                                                                                                                                                                                                                                                                                                                                                                                    crt.mod[i + 1] = get_pow(_P[i], _A[i]),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   t = P / sq, sa = Inv(kpow(x, sq, P), P);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // 注: 返回 pair( 最小非负解 , [0,p) 中解的个数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(i, 0, t + 1) if (M.count(res))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        void ex_gcd(ll a, ll b, ll &x, ll &y) {
                                                                                                                                                                                                  pll solve_high(ll a, ll b, ll p) {
                                                                                                                                                                                                                                                                                                                                                                          crt.a[i + 1] = tmp[i + 1].fi,
                                                       if (ok) ans *= t2, ret *= t3;
                                                                                                                                                                          root, that is 8 cannot divide p
                                                                                                                                                                                                                                                           if (p == 1) return mp(0, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (!ret) return mp(-1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                11 bsgs(11 x, 11 z, 11 P) {
   if (x % P == 0) return -1;
                                                                                                                                                                                                                               assert(p > 0); norm(b, p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         11 x, y; ex_gcd(a, P, x, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (z \% t) return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                   ret *= tmp[i + 1].se;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return x < 0 ? x + P : x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        inline 11 Inv(11 a, 11 P) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             11 kpow(11 a, 11 b, 11 P) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          11 r = 1; assert(b >= 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ans = crt.solve(tot);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             质数
                                                                                          return mp(ans, ret);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return mp(ans, ret)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             高次同余
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          map<ll, int> M;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           struct BSGS {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               7.34
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \. I
```

```
Returns the number of trailing 0—bits in x, starting at the least significant bit
                                                                                                                                                                      Returns the parity of x, i.e. the number of 1—bits in x modulo 2.
                       position. If x is 0, the result is undefined.
                                                                      (unsigned int \times)
                                                                                                                                               _builtin_parity (unsigned int \times)
                                                                                              Returns the number of 1—bits in x.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                b.flip(); // all = 0 <->
                                                                                                                                                                                                                                                                                                                                                                                                                                         b.reset(); // all to 0
                                                                                                                                                                                                                                                                                                                                                                  b.count(); // cnt of 1
                                                                                                                                                                                                                                                                                                                                                                                                                // all to 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  b.set(p); // b[p] = 1
                                                                                                                                                                                                                                                                                                                                        // all 0?
                                                                                                                                                                                                                                Bitset
                                                                                                                                                                                                                                                                                                                                           b.none();
                                                                                                                                                                                                                                                                                                                                                                                                                    b.set();
                                                                                                                                                                                                                                                                                                                 b.any();
                                                                                                                                                                                                                                                                                           // Base
                                                                                                                                                                                                                                8.5
                                                                                                                                                                                                                                                                                                                          g = t.se, x = t.fi, ans = kpow(g, x, p), d = kpow(g, p);
                        // solve equation: x^na=b(\%p), p must be a prime
                                                                                                                                                                                                                                                                                                                                                                            rep(i, 1, _g) ans = ans*d%p, ret.pb(ans);
sort(all(ret));
                                            v11 solve high(11 a, 11 b, 11 p) {
  v11 ret; norm(b, p); assert(p > 0);
if (!a == b) ret.pb(0);
if (!b) return ret;
11 g = getRoot(p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              };
// 注 : 返回所有 [0,p) 中的非负整数解
                                                                                                                                                                                                                                                                                                 if (t.fi == -1) return ret;
                                                                                                                                                                   if (g ==-1) return ret;
11 _b = T.bsqs(g, b, p);
if (_b == -1) return ret;
11 _p = p - 1;
                                                                                                                                                                                                                                               11 _p = p - 1;
pl1 t = solve(a, _b, _p);
                                                                                                                                                                                                                                                                                                                                                   ret.pb(ans);
                                                                                                                                                                                                                                                                                                                                                                                                                              return ret;
```

8 Others

8.1 BitOperation

```
Returns one plus the index of the least significant 1-bit of x, or if x is zero, returns
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             Returns the number of leading 0—bits in x, starting at the most significant bit position
                                                                                                                                                                                                                                                                                                                                                rep(i, 0, n) { for(int j = (1 << n) - 1; -j; --j) if(!(j >> i & 1)) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int __builtin_ffsll (unsigned long long)
                                                                                                                                                    rep(i, 0, n) {
    rep(j, 0, 1 << n) if(j >> i & 1) {
        upd(s[j], s[j ^ (1 << i)]);
    }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 . If x is 0, the result is undefined.
                                                                                                                                                                                                                                                                                                                                                                                                             upd(s[j], s[j | (1 << i)]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int __builtin_clz (unsigned int x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int __builtin_ffs (unsigned int \times)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        _builtin_ffsl (unsigned long)
                          for(int i = x; i; (—i) & x) {
                                                                                                                       // 统计子集的答案
                                                                                                                                                                                                                                                                                                                // 统计超集的答案
// 枚举子集
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          zero.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int
```

int __builtin_ctz (unsigned int x)

8.3 ExpressionParse

for (int i = b._Find_first(); i < sz(b); i = b._Find_next(i));</pre>

b.flip(p); // b[p] = 0 <->

b.test(p); // b[p] is 1 b.reset(p);// b[p] = 0 // _builtin_ctz in bitst b._Find_first();

// Black tech

// travel all 1

```
~FastIO() { if (wpos) fwrite(wbuf, 1, wpos, stdout), wpos = 0; }
                                                                                                                                                                                                             inline void wstring(const char *s) { while (*s) wchar(*s++); }
                                                                                                                                    while (x \mid | \mid !n) s[n++] = '0' + x \% 10, x /= 10;
                                                                  if (x < 0) wchar('-'), x = -x;
                                                                                                                                                               while (n—) wchar(s[n]);
                                            inline void wint(int x) {
                                                                                                                                                                                                                                                                                                                                                                 template<class T1, class T2>
x = [++sodm] = x
                                                                                           char s[24];
                                                                                                                                                                                                                                                                                                          FastMod
                                                                                                                  int n = 0;
                                                                                                                                                                                                                                                                                                          ∞
.∵
                                            reverse(all(ch)); rpn.insert(rpn.end(), all(ch));
                                                                                                                                                                                                      sta[sz(sta) - 1] = calc(u, sta.back(), b);
} else { sta.pb(u); }
                                                                                                                                                                                  char b = sta.back(); sta.pop_back();
} else { rpn.pb(c); }
                                                                                                           if(pri(u) > 0)
                                                                  // 后缀表达式计算
                                                                                                                                                                                                                                                                               return sta[0];
                                                                                                                                                                                                                                                                                                                                                 FastIO
                                                                                            sta.clear();
                                                                                                                                                                                                                                                                                                                                                     8.4
```

```
friend T1 operator / (const T1 &n, const FastD &d) { return T2(n) * d.x >> d.len; } friend T1 operator % (const T1 &n, const FastD &d) { return n-n/d*d.m; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  friend T operator / (const T &n, const ExactD &d) { return n * d.i; }
                                                                                                                                                                      else {
   if (wb == 32) len = 31 - _builtin_clz(n - 1) + wb;
   else len = 63 - _builtin_clzll(n - 1) + wb;
   x = ((T2(1) << len) + n - 1) / n;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ExactD(const T &n): t(T(-1) / n), i(mul_inv(n)) {}
constexpr static T mul_inv(T n, int e = 6, T x = 1) {
    return !e ? x : mul_inv(n, e - 1, x * (2 - x * n));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 bool divide(const T &n) const { return n * i <= t; }</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          using FastDiv32 = FastDcuint32, uint64>;
using FastDiv64 = FastDcuint64, uint128>;
                       const static int wb = sizeof(T1) * 8;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     using ExactDiv32 = ExactD<uint32>;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 using ExactDiv64 = ExactD<uint64>;
                                                                                                                                               if (n == 1) \times = 1, len = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   template<class T> // 只能用于奇数
                                                                                                                FastD(T1 n): m(n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ExactD() = default;
                                                                                      FastD() = default;
                                                          int len; T1 m, x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          import java.util.*;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           import java.math.*;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              import java.io.*;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    struct ExactD {
struct FastD {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Java
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     8.6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for (; '0' <= c && c <= '9'; c = xchar()) x = x * 10 + c - '0';
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for (; '0' <= c && c <= '9'; c = xchar()) x = x * 10 + c
                                                                                                                                                                                                                                                                                                                        if (pos == len) pos = \theta, len = fread(buf, 1, S, stdin);
if (pos == len) return -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inline void wchar(int x) {
   if (wpos == S) fwrite(wbuf, 1, S, stdout), wpos = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  while (c <= 32) c = xchar();
for (; c > 32; c = xchar()) *s++ = c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (c == '-') s = -1, c = xchar();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int c = xchar(), x = 0, s = 1; while (c <= 32) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             while (c \le 32) c = xchar();
                                                                                                                                                                                                                                                                                         static int len = 0, pos = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     inline void xstring(char *s) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(!\sim c) return ed = 1;
                                                                                                                                                                                              FastIO() : wpos(0), ed(0) { }
inline int xchar() {
    static char buf[S];
                                                                             static const int S = 1310720
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int c = xchar(), x = 0;
                                                                                                                                                                                                                                                                                                                                                                                return buf[pos++];
              // read untill EOF (xint)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   c = xchar();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       inline int xuint() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int c = xchar();
                                                                                                                                                                                                                                                                                                                                                                                                                                         inline int xint() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        return × * s;
                                                                                                                                     char wbuf[S];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return x;
                                              struct FastIO {
                                                                                                            int wpos;
                                                                                                                                                                    boo1 ed;
```

```
clock_t st = clock(); CLOCKS_PER_SEC;
                                                                                                                                                                                                                                                                        if diff sol.out dp.out; then
                                                                                                                                                                                                                         ./sol <gen.in >sol.out
                                                                                                                                                                                                                                                 ./dp <gen.in >dp.out
                                                                                                                                                                                                                                                                                                printf "AC\n"
                                                                                                                                                                                                                                                                                                                                              printf "Wa\n"
                                                                                                                                                                                                      ./gen > gen.in
                                                                                                duipai
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         String
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // sh duipai.sh
                                                                                                                                                                              while true; do
                                                                                                                                                                                                                                                                                                                                                                          exit 0
                                                                                                                                                    #!/bin/bash
                                                                                                                                                                                                                                                                                                                          else
                                                                                                  8.11
8.10
                                                                                                                                                                                                                                                                                                                                                                                                  Ę
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             0
                                                                                                                                                                                                                                                                                                                                                                                                                                             Map<String, Integer> mymap2 = new TreeMap<>()
                                                                                                                                                                                                                                                                                                                                                                                                                       Map<String, Integer> mymap = new HashMap<>();
                                                                                                                                                                                                                                               List<String> mylist2 = new LinkedList<>();
                                                                                                                                                                                                                         List<String> mylist1 = new ArrayList⇔()
                                                                                                                                                                                                                                                                                                                      Queue<String> que = new LinkedList⇔();
                                                                                                                                                                                                                                                                         List<String> mylist3 = new Vector⇔();
                             public static void main(String[] args) {
                                                                                                                                                                                                                                                                                                                                                                                           Set<String> myset2 = new TreeSet<>();
                                                                                                                                                                                                                                                                                                                                                                        Set<String> myset = new HashSet\Leftrightarrow();
                                                                                                                                                                                                                                                                                                  Vector<String> vec = new Vector<>();
                                                       Scanner cin=new Scanner(System.in);
                                                                            BigInteger a=cin.nextBigInteger();
                                                                                                                                                                                                                                                                                                                                              Stack<String> sta = new Stack<>();
                                                                                                    BigInteger b=cin.nextBigInteger();
                                                                                                                            System.out.println(a.add(b));
                                                                                                                                                                           a=cin.nextInt();
                                                                                                                                                                                                 b=cin.nextInt();
     public class code {
                                                                                                                                                      Integer a,b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            Rand
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          8.7
```

9.1 ACAutomaton

```
/* [0,L), N-1 is virtual, 0 is rt
* init!!
    * addition: end[] end[G] |= end[fail[G]]
    */
| struct Trie{
```

static const int N = 101010 , M = 26;

int newnode(){ fill_n(ne[L],M,0); return L++; }
void add(char *s){

 $\begin{array}{ll} \inf \ c = s[i] - \ ^a'; // \ \textit{modify} \\ \text{if}(!ne[p][c]) \ ne[p][c] = newnode() \ , \ fa[L-1] = p; \end{array}$

b = ne[p][c]

for(int i=0;s[i];++i){

int p = rt;

8.8 RomanNumerals

typedef uniform_int_distribution<11> RR;
11 rnd(11 1, 11 r) { RR dis(1, r); return dis(gen); }
typedef uniform_real_distribution<4b> RR;
db rnd(db 1, db r) { RR dis(1, r); return dis(gen); }

mt19937 gen(998244353)

```
const int rom[30] = {
    3000, 2000, 1000, 900, 800, 700, 600, 500, 400, 300, 200, 100,
    90, 80, 70, 60, 50, 40, 30, 20, 10,
    9, 8, 7, 6, 5, 4, 3, 2, 1
};
string smb[30] = {
    "wMMM", "MM", "M",
    "CG", "DCC", "DCC", "DCC", "CCC", "CC", "CC",
    "XC", "LXXX", "LXX", "LX", "L", "XL", "XXX", "XX", "X",
    "IX", "VIII", "VII", "VI", "V", "IN", "III", "II", "I",
};
string toRoman(11 d) {
    string r;
    rep(i, 0, 30) if (d >= rom[i]) d -= rom[i], r += smb[i];
    return r;
}
```

8.9 Strtok

v.pb(ne[c][i]) , fail[ne[c][i]] = ne[fail[c]][i] :
ne[c][i] = ne[fail[c]][i];

rep(i,0,M) ne[c][i] ?

int c = v[i];

vi v;v.pb(rt);
rep(i,0,sz(v)){

void Build(){

```
char s[111]; gets(s); vector<string> a;
for(char* p=strtok(s," .,()");p;p=strtok(NULL," .,()")) a.pb(p);
```

9.2 DoublingArray

Exkmp

9.3

```
Mile(i + z[i] < lens && z[i] < lent && s[i + z[i]] == t[z[i]]) ++z[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               while(j >= 0 && s[i] != t[j + 1]) j = nt[j];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // O(n) 分解为字典序非严格降的 1yndon word 分解唯一
                                                                                                                                                                                                                                                                                                                                                                                        if(y \le i + z[i]) \times = i, y = i + z[i];
                                                                                                                                                                                                                                                                                                                                     z[i] = i \le y ? min(y-i, p[i-x]) : 0;
                                                                                                                                                                                             void exkmp(char *s,int *z,char *t,int *p){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void kmp(char *s,int *ns,char *t,int *nt){
                                                                                                                                                                                                                                                                                                       for(int i=0, x=0, y=0;i<lens; ++i){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(j + 1 == lent) j = nt[j]
                             * S 串的每个后缀与 t 串的最长公共前缀
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for(int i=0, j=-1;i<lens; ++i){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if(s[i] == t[j + 1]) ++j;
                                                                                                                  а
                                                                                                                                                                                                                        int lens = strlen(s);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              exkmp(t+1,nt+1,t,nt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int lens = strlen(s),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int lent = strlen(t)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         LyndonWord
                                                                                                                                                                                                                                                  int lent = strlen(t)
                                                                                                                  9
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ъ 2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                scanf("%s%s", s, t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            kmp(t+1,nt+1,t,nt)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               scanf("%s%s", s, t);
                                                                                                                  a w
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         exkmp(s,ns,t,nt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               q 7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    <mp(s,ns,t,nt);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ns[i] = j;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            nt[0] = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 C
__1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          Kmp
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void Exkmp(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               a s
                                                                                                                                                                                                                                                                                b[0]=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void KMP(){
                                                       * t: a
                                                                                * nt: 0
                                                                                                                                          * ns: 3
                                                                                                                * S: a
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         9.5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          В
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   nt:-1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               В
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            9.4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           S:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          \begin{array}{lll} & \text{for(int } i = 1; i < = n; ++1) & \text{rk}[sa[i]] & = i; \\ & \text{for(int } i = 0; i < n; i < n; i ++1] & = k) & \text{for}(k\&\& --k, j = sa[rk[i] --1]; s[i +k] = s[j +k]; ++k); \\ \end{array} 
                                                                                                                                                                                                                                                                                                     bool cmp(int *x,int a,int b,int d){ return x[a] == x[b] \& x[a+d] == x[b+d]; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for(int i=1;i<=lim;++i) p[j][i] = min(p[j-1][i] , p[j-1][i+(1<<j>>1)]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       Doubling::cal_h(in,n,rk); 
 Log[0] = -1; for(int i=1;i<=n;++i) Log[i] = Log[i-1] + (i==(i&(-i)));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(i,1,n) \times [sa[i]] = cmp(y,sa[i],sa[i-1],j)?p-1:p++;
                                                                              // h[1~n]:S[sa[i-1]] 与 S[sa[i]] 的最长公共前缀长度为 h[i]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      \begin{array}{ll} p = 0; rep(i,n-j,n) \ y[p++] = i; \\ rep(i,0,n) \ if(sa[i] >= j) \ y[p++] = sa[i] - j; \end{array}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for(int i=1;i<=n;++i) p[0][i] = Doubling::h[i]</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int p[18][N] , rk[N] , in[N] , Log[N] , n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return min(p[t][a] , p[t][b-(1<<t)+1]);</pre>
                                                                                                          int t[N] , wa[N] , wb[N] , sa[N] , h[N];
                                                // sa[0-n]: 排名第的后缀是以i sa[i] 开头
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // rank[0~n—1]: 以 i 开头的后缀排名 rank[i]
                                                                                                                                                                                                                                                  per(i,0,n) sa[-t[x[y[i]]]] = y[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 struct DA{ // [0,n], in[n] = 0, n load static const int N = 101010;
                                                                                                                                     void sort(int *x, int *y, int n, int m){
    rep(i, 0, m) t[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                      rep(i,0,n) \times [i] = s[i], y[i] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                sort(x , y , n , m);
swap(x , y); p = 1; x[sa[0]] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                   sort(x , y , n , m);
for(int j=1, p=1; p<n; m=p, j<<=1){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void cal_h(int *s,int n,int *rk){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 a = rk[a], b = rk[b];
if(a > b) swap(a, b);++a;
                                                                                                                                                                                                                    rep(i,1,m) t[i] += t[i-1];
                                                                                                                                                                                                                                                                                                                              void da(int *s,int n,int m){
                             static const int N = 101010;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Doubling::da(in,n+1,300);
                                                                                                                                                                                           rep(i,0,n) t[x[y[i]]]++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for(int j=1;1<<j<=n;++j)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int \lim = n+1-(1 < j)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         // 某两个后缀的最长公共前缀
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int t = Log[b-a+1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int lcp(int a, int b){
                                                                                                                                                                                                                                                                                                                                                            int *x=wa, *y=wb;
namespace Doubling{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void Build(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int ], k=0;
```

```
int p = i >> 1, q = i - p, r = ((j + 1) >> 1) + pa[j] - 1; pa[i] = r < q ? 0 : min(r - q + 1 , pa[(j << 1) - i]); while(0 <= p - pa[i] && q + pa[i] < n && s[p - pa[i]] == s[q + pa[i]]) pa[i]++; if(q + pa[i] - 1 > r) j = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                    int ne[N][M] , fail[N] , len[N] , S[N] , last , n , p, cnt[N], las[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   void build() { for(int i = p - 1; \sim i; --i) cnt[fail[i]] += cnt[i]; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  while(S[n - len[x] - 1] != S[n]) x = fail[x];
                                                                                                                                                                                                                                                                                                                                                           // [0,p) , 0(even) and 1(odd) is virtual , init!!
struct Palindromic_Tree {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  fail[now] = ne[get_fail(fail[cur])][c];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(!ne[cur][c]){
  int now = newnode(len[cur] + 2);
                                             void Manacher(char *s,int n,int *pa){
                                                                                                                                                                                                                                                                                                                                                                                                             static const int N = ::N, M = 26;
                                                                                             for(int i=1, j=0; i<(n<1)-1;++i){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             p = 0; newnode(0); newnode(-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     fill(ne[p] , ne[p] + M , \odot);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int cur = get_fail(last);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   S[n = last = 0] = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               ne[cur][c] = now;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         jast = ne[cur][c];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int get_fail(int x){
                                                                                                                                                                                                                                                                                                                                                                                                                                                            int newnode(int 1){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         void add(int c){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     cnt[last]++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            fail[0] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        len[p] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     las[p] = n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     S[++n] = c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            cnt[p] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return p++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void ini(){
                                                                                                                                                                                                                                                                                                  PAM
* N>2*n
                                                                                                                                                                                                                                                                                                 9.7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                }pam;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             // 生成字符集为 m , 长度不超过 n 的所有 lyndon word , 字符集从 a 开始
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for (int j = x; j < n; ++j) s[j] = s[j - x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (strlen(s)==1 && s[0]=='a'+m-1) return;
                                             int n = strlen(s) + 1; // zero used here int start = 0, mid = 1, cur = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void lyndon_generate(int n, int m) {
    char z = 'a' + m - 1, s[1000];
                                                                                                                   for (int i = 0; i < n; ++i){
  if (s[i] == s[cur]){
   if (++cur == mid) cur = start;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (x = n; s[x - 1] == z; --x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 S[0] = 'a' - 1;
for (int i = 1, x = 1; ; ++i) {
                                                                                                                                                                                                                                                                                                                    while (start + temp <= i){
                                                                                                                                                                                                                                                                  else if (s[i] < s[cur]){
                                                                                                                                                                                            } else if (s[i] > s[cur]){
                                                                                                                                                                                                                                                                                             int temp = mid - start;
                                                                                                                                                                                                                                                                                                                                                                     ret.push_back(start);
vector<int> duval(char s[]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     S[x - 1]++; S[x] = 0;
                                                                                                                                                                                                                                                                                                                                                start += temp;
                                                                                                                                                                                                                                                                                                                                                                                                                      = cur = start;
                                                                                                                                                                                                                                                                                                                                                                                                                                               mid = start + 1;
                                                                                             ret.push_back(0);
                                                                                                                                                                                                                      mid = i + 1;
                          vector<int> ret;
                                                                                                                                                                                                                                               cur = start;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return ret;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               puts(s);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      0126
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                cbaabc
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ab
abb
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   3 2
a
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      aab
```

9.8 SAIS

```
|/*
* Ensure that str[n] is the unique lexicographically smallest character in str.
| * time complexity: O(n)
```

* i:[0, n) pa[i<<1]: odd string 整个回文长度为 2^* pa[i<<1]-1 * i:[0, n-1) pa[i<<1|1]: even string 整个回文长度为 2^* pa[i<<1]

* length of pa is two size of str

Manacher

9.6

```
if(ne[p][c] \& l[ne[p][c]] == l[p] + 1) \{ last = ne[p][c]; return ; \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int R[N], RF[N], tmp[N], pos[N], tax[N], tp[N], sa[N], siz, n, pa[N][M];
int h(int c) { return c - 'a' + 1; }
void Qsort(int *sa, int *R, int *tp, int siz) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        par[q] = par[np] = nq;
while(p && ne[p][c] == q) ne[p][c] = nq, p = par[p];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            while(p && !ne[p][c]) ne[p][c] = np, p = par[p];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        O(nlogn)
                                                                                                                                                                                                 int par[N], 1[N], ne[N][M], rt, last, L;
void add(int c) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  copy(ne[q], ne[q] + M, ne[nq]);
                          * [0,L] , 0 is virtual , 1 is rt , init!!
* [1[par[s]] + 1, 1[s]]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(1[q] == 1[p] + 1) par[np] = q;
                                                                                                                                                               static const int N = ::N << 1, M = 26;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // trie 树点带字母,每个点到根的字符串排序,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // C 为字符集大小, 从 a 开始, M 为倍增深度
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 1, L + 1) cnt[i] += cnt[i - 1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           fill(ne[rt], ne[rt] + M, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                        fill(ne[np], ne[np] + M, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  const int N = 5e5, M = 21, C = 26;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       1[nq] = 1[p] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(i, 1, L + 1) ++cnt[l[i]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            par[nq] = par[q]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(!p) par[np] = rt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int q = ne[p][c];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int nq = ++L;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // 调用 Init 之后, 取 sa[]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int n, fa[N]; char s[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rt = last = L = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             l[np] = l[p] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          SA trie
                                                                                                                                                                                                                                                                                                                                                                                                           int np = ++L;
                                                                                                                                                                                                                                                                        int p = last;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    1[0] = -1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 last = np;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void ini() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // BucketSort
                                                                                                                                struct SAM {
                                                                                                                                                                                                                                                                                                        /* ex
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           struct SA {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            9.10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int n1 = t[n-1] = 0, ch = rk[0] = -1, *s1 = s+n; for (int i = n-2; -i; i--) t[i] = s[i] = s[i+1]? t[i+1] : s[i] > s[i+1]; for (int i=1; i < n; i++) rk[i] = t[i-1] && !t[i] ? (p[n1] = i, n1++) : -1;
                                                                                                                                                                                               for (int i = 0; i < n; i++) cnt[s[i]]++;
for (int i = 1; i < m; i++) cnt[i] += cnt[i-1];
for (int i = 0; i < m; i++) cur[i] = cnt[i]-1;
for (int i = n1-1; -i; i—) pushS(v[i]);
for (int i = 1; i < m; i++) cur[i] = cnt[i-1];
for (int i = 0; i < n; i++) if (sa[i] > 0 && t[sa[i]-1]) pushL(sa[i]-1);
for (int i = 0; i < m; i++) cur[i] = cnt[i]-1;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                        for (int i = n-1; -i; i-) if (sa[i] > 0 && !t[sa[i]-1]) pushS(sa[i]-1) void sais(int n, int m, int *t, int *p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (ch < 1 || p[x + 1] - p[x] != p[y + 1] - p[y]) ch++;
else for (int j = p[x], k = p[y]; j <= p[x + 1]; j++, k++)
if ((s[j] << 1 | t[j]) != (s[k] << 1 | t[k])) { ch++; break; }</pre>
                                                              int sa[N], rk[N], ht[N], s[N << 1], t[N << 1], p[N], cnt[N], cur[N]; #define pushS(x) sa[cur[s[x]]—] = x
                                                                                                                                                                     <u>(</u>)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             while (i + h < n && j + h < n && s[i + h] == s[j + h]) h++;
                                                                                                                                                                  #define inducedSort(v) std::fill_n(sa, n, -1); std::fill_n(cnt, m,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (int i = \vec{0}, x, y; i < n; i++) if (\sim(x = rk[sa[i]])) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (ch + 1 < n1) sais(n1, ch + 1, s1, t + n, p + n1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for (int i = 0; i < n; i++) rk[str[i]] = 1;
for (int i = 0; i < m; i++) rk[i + 1] += rk[i];
for (int i = 0; i < n; i++) s[i] = rk[str[i]] - 1;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      else for (int i = 0; i < n1; i++) sa[s1[i]] = i;
for (int i = 0; i < n1; i++) s1[i] = p[sa[i]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       sais(n, m, s, t, p);

for (int i = 0; i < n; i++) rk[sa[i]] = i;

for (int i = 0, h = ht[0] = 0; i < n - 1; i++) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int mapCharToInt(int n, const T *str) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void suffixArray(int n, const T *str) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int m = *max_element(str, str + n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int m = mapCharToInt(++n, str);
                                                                                                                                #define pushL(x) sa[cur[s[x]]++] = x
                               const static int N = 1000000 + 10;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  std::fill_n(rk, m + 1, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if (ht[rk[i]] = h) h—;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int j = sa[rk[i] - 1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          s1[y = x] = ch;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 template<typename T>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      template<typename T>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               inducedSort(s1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           inducedSort(p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return rk[m];
namespace SA {
```

SAM9.9

rep(i, 0, siz + 1) tax[i] = 0; rep(i, 1, n + 1) tax[R[tp[i]]]++;

```
Fuzhou University
                                                                         inline Int operator * (const Int &c) const { return Int(mul(a, c.a), mul(b, c.b)); }
          inline Int operator - (const Int \&C) const { return Int(upd(a, -C.a), upd(b, -C.b));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inline Str operator + (const Str &c) const { return Str(a * B[c.len] + c.a, len +
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               inline Str operator - (const Str \&c) const \{ return Str(a-c.a * B[len-c.len],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      inline bool operator == (const Str &c) const { return a == c.a && len == c.len;}
                                                                                                             inline bool operator == (const Int &c) const {return a == c.a && b == c.b;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void init(vi &s, Str *ha) { rep(i, 0, sz(s)) ha[i] = i > 0 ? ha[i-1] + Str(s[i] + 1) : Str(s[0] + 1);
                                                                                                                                                                                                                                                                                                                                                                                                   Str(Int a = _0, int len = 0) : a(a), len(len) {}
                                                                                                                                                                                                                                                        rep(i, 2, n+1) B[i] = B[i-1] * B[1];
                                                                                                                                                                                                                                                                                                                                                                                                                                    Str(int \times) \{a = Int(x, \times); len = 1;\}
                                                                                                                                                                                                                    B[0] = _1; B[1] = Int(233, 241);
                                                                                                                                                   _0 = Int(), _1 = Int(1, 1), B[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Str sub(Str *ha, int 1, int r)
                                                                                                                                                                                                                                                                                                                                                                Int a; int len;
                                                                                                                                                                                      void init(int n){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // 减去一个前缀
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ha[N], hb[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        - c.len); }
                                                                                                                                                                                                                                                                                                                         struct Str{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                len); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     Qsort(sa, R, tp, R[sa[n]]);
rep(i, 1, n + 1) tmp[i] = R[i]; R[sa[1]] = 1;
rep(i, 2, n + 1) R[sa[i]] =
   (tmp[sa[i]] == tmp[sa[i - 1]] && tmp[pa[sa[i]][p]] == tmp[pa[sa[i - 1]][p]])
                                                                                                                                                                                    void Init(int _n, int fa[], char s[]) {
    n = _n, pa[1][0] = 0; rep(i, 2, n + 1) pa[i][0] = fa[i];
    rep(i, 2, n + 1) rep(j, 1, M) pa[i][j] = pa[pa[i][j - 1]][j - 1];
    rep(i, 1, n + 1) R[i] = h(s[i]), tp[i] = i;
    Qsort(sa, R, tp, C); rep(i, 1, n + 1) pos[sa[i]] = i;
                                                                                                                                                                                                                                                                                                                                                                  for (int w = 1, p = 0; w < n; w <<= 1, p++) {
    rep(i, 1, n + 1) RF[i] = pos[pa[i][p]];</pre>
          rep(i, 1, siz + 1) tax[i] += tax[i - 1];
per(i, 1, n + 1) sa[tax[R[tp[i]]]—] = tp[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         R[sa[i-1]]: R[sa[i-1]] + 1; rep(i, 1, n + 1) pos[sa[i]] = i;
                                                                                                             // s[] 表示字母点权,下标从 1 开始
// fa[] 表示树上父节点编号,根为 1
                                                                                                                                                                                                                                                                                                                                                                                                                                       Qsort(tp, RF, sa, n);
```

最小表示法 9.13

return 1 > 0? ha[r] - ha[1-1] : ha[r];

if (1 > r) return Str();

StrHash

9.11

```
inline void init_h(char st[], int n, 11 _base = 163, 11 _P = 1e9 + 7, char c = 'a') {
                                                                                                                        base = _base, P = _P, h[0] = st[0] - c;
rep(i, 1, n) h[i] = (h[i - 1] * base + st[i] - c) % P;
if (_B[0] == 1) return; _B[0] = 1;
                                                                                                                                                                                                                                                                                                                             inline 11 H(int 1, int r) {
   if (!1) return h[r] < 0 ? h[r] + P : h[r];
   11 ans = (h[r] - h[1 - 1] * _B[r - 1 + 1]) % P;
                                                                                                                                                                                                                                                 rep(i, 1, N) _B[i] = _B[i - 1] * base %P,
                                                                                                                                                                                                                                                                                                                                                                                                                                                            return ans < 0 ? ans + P : ans;
struct STR {
    11 _B[N], h[N], base, P;
```

StrHash 双哈希 9.12

```
Int(int \ a = 0, int \ b = 0) : a(a), \ b(b) \ \{\}
inline Int operator + (const Int &c) const { return Int(upd(a, c.a), upd(b, c.b)); }
                                                                                                                                                                           inline int mul(int a, int b) {return 111 * a * b % P; }
                                inline int upd(int a, int b) {
                                                                 if((a += b) >= P) a -= P;
                                                                                                    return a < 0 ? a + P : a;
const int P = 1e9 + 7;
                                                                                                                                                                                                                                                  int a, b;
                                                                                                                                                                                                              struct Int{
```

```
if(s[i+k]>s[j+k])i=max(i+k+1,j+1);
                                                                                                                                              while(s[i+k]==s[j+k] && k<L)++k;
                                         int MINR(char s[],int L){
    rep(i,0,L) s[L+i]=s[i]; s[2*L]=0;
                                                                                                                                                                     if(k==L)return min(i,j);
                                                                                                                                                                                                                                     else j=max(j+k+1,i+1)
                                                                                                    while(i<L && j<L){</pre>
                                                                                                                                                                                         // 最大改成 ~
                                                                                                                                                                                                                                                                           return min(i,j);
                     // s[] 开两倍长度
                                                                                     int i=0, j=1;
// 下标从 Ø 开始
                                                                                                                              int k=0;
```

Tree

DsuOnTree 10.1

```
static const int N = ::N;
                      namespace QuerySubtree{
// id starts with 1
```

```
int a[20][N] , lft[N] , dep[N] , lg[N] , L; int rmin(int x,int y){return dep[x] < dep[y] ? x : y;}
                                                                                                                                                                                                                                                                                                                                                                                                       \ensuremath{\text{//}} N is 2 size of tree , id of nodes start from
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void dfs(int c,int fa,const vi g[]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                               static const int N = 101010 << 1;
  if(dep[a] < dep[b]) swap(a, b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void add(int \times){ a[0][L++] = \times;}
                               // Cal id[b] .. id[a]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           lft[c]=L;add(c);
                                                                                                              void Build(vi g[]){
                                                                                                                                                                                                                                                                                                                              LCARMO
                                                                                                                                                                                                         dfs2(1, 0, g);
                                                                                                                                                  dfs(1, 0, g);
                                                               // b is lca
                                                                                                                                                                                                                                                                                                                                                                                                                                      struct LCARMQ{
                                                                                                                                                                                                                                                                                                                                   10.3
                                                                                                                                                                                                                                                                      }hc;
                                                                                     for(auto t:g[c]) if(t!=fa) dfs(t,c,g),sz[c]+=sz[t],(sz[t]>=sz[s])&&(s=t);
                                                                                                                                              void solve(int c, int fa, bool iswson, vi g[]){
    for(auto t : g[c]) if(t != wson[c] && t != fa) solve(t , c , false , g);
    if(wson[c]) solve(wson[c] , c , true , g);
    for(auto t : g[c]) if(t != wson[c] && t != fa) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            solve(1,0,false,g); // 如果输入是单组数据,改成 true 可以优化常数
                                                                                                                                                                                                                                                                                                                                                                                                              // 如果当前子树是轻儿子,删除这棵子树的信息
int sz[N] , wson[N] , par[N];
void dfs(int c,int fa,vi g[]){
   sz[c]=1;par[c]=fa;int &s=wson[c]=0;
                                                                                                                                                                                                                                                               // 将该子树的信息加入
                                                                                                                                                                                                                                                                                                                          // 将当前节点的信息加入
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void solve(vi g[]){
                                                                                                                                                                                                                                                                                                                                                                                       if(!iswson) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               dfs(1,0,g);
                                                                                                                                                                                                                                                                                                                                                       // 查询
```

HeavyChain

10.2

```
int sz[N], wson[N], top[N], dep[N], id[N], _, par[N], who[N];
void dfs(int c, int fa, vi g[]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(s) \ top[s] = top[c], \ dfs2(s, c, g); for(auto \ t : g[c]) \ if(t \ != fa \ \&k \ t \ != s) \ dfs2(t, c, g);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 while(fa != fb){
   if(dep[fa] < dep[fb]) swap(a, b), swap(fa, fb);</pre>
                                                                                                                                                                                                                                  for(auto t : g[c]) if(t != fa)
                                                                                                                                                         par[c] = fa;
dep[c] = dep[fa] + 1;
int &s = wson[c] = top[c] = 0;
                                                                                                                                                                                                                                                                                                                                                                                               void dfs2(int c, int fa, vi g[]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int fa = top[a], fb = top[b];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                a = par[fa]; fa = top[a];
                                                                                                                                                                                                                                                                                                                  if(sz[t] >= sz[s]) s =
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      // Cal id[fa] .. id[a]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if(!top[c]) top[c] = c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void Query(int a, int b){
                                                   static const int N = ::N;
                                                                                                                                                                                                                                                                                         sz[c] \leftarrow sz[t];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int s = wson[c];
                                                                                                                                                                                                                                                               dfs(t, c, g);
// id starts with 1
                                                                                                                                                                                                                                                                                                                                                                                                                            id[c] = ++_{-};
                            struct HeavyChain{
                                                                                                                                                                                                                                                                                                                                                                                                                                                     who[\_] = c;
                                                                                                                              SZ[C] = 1;
```

10.4 LongChain

```
struct LongChain{
    static const int N = ::N;
    int wson[N] , top[N] , dep[N] , lg[N];
    int jump[N][20] , id[N] , who[N] , rwho[N] , .;
    void dfs(int c,int fa,vi g[]){
        dep[c]=1;int &s=wson[c]=top[c]=0;
        jump[c][0]=fa;rep(i,1,20) jump[c][i]=jump[jump[c][i-1]][i-1];
        for(auto t:g[c]) if(t!=fa)
        dfs(t,c,g),dep[c]=max(dep[t]+1,dep[c]),(dep[t]>=dep[s])&&(s=t);
    }
    void dfs2(int c,int fa,int rc,vi g[]){
        if(!top[c]) top[c]=c,rc=c;
        who[id[c]=++_]=c;rwho[_]=rc;
    }
}
```

```
per(1, 0, M) if(dep[pre[y][i]] >= dep[x]) y = pre[y][i];
per(i, 0, M) if(pre[x][i] != pre[y][i]) x = pre[x][i], y = pre[y][i];
                                                                                                                                                                                                                                                                                                                  if(f == u) \{ nds.pb(Node(id, st[u], st[v]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i, 0, N << 1) B[i] = i / SZ;

dfs(1, cd = 0, g);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               (cnt[p] == 1)? add(p) : sub(p);
                                                  int lca(int x, int y) {
   if(dep[x] > dep[y]) swap(x, y);
                                                                                                                                                                                                                                     void adde(int u, int v, int id) {
                                                                                                                                                                                                                                                                                                                                                                                                                     nds.pb(Node(id, 1, r, f));
                                                                                                                                                                                                                                                               if(st[u] > st[v]) swap(u, v);
int f = lca(u, v);
                                                                                                                                                                                                                                                                                                                                                                   int \tilde{l} = ed[u], r = st[v];
dfn[++cd] = u, ed[u] = cd;
                                                                                                                                                                                                                                                                                                                                                                                               if(1 > r) swap(1, r);
                                                                                                                                                            if(x == y) return x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void upd(int p, int c)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // p is index in tree
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void solve(vi g[]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int l = 1, r = 0;
                                                                                                                                                                                      return pre[x][0];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void add(int p) { }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         sort(all(nds));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                // adde(u, v)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       void sub(int p)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              p = dfn[p];
cnt[p] += c;
                                                                                                                                                                                                                                                                                                                                            } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // 注意统计以 c 为起点的链的答案,注意深度的限制(两棵子树都要注意)
                                                    for(auto t:g[c]) if(t!=fa&&t!=s) dfs2(t,c,t,g);
                                                                                                                                                                                                                                                                                                                                                                                               for(auto t : g[c]) if(t != fa && t != wson[c])
                                                                                                                                                                                                                                 for(auto t : g[c]) if(t != fa) solve(t, c, g);
if(wson[c]) {
                      if(s) top[s]=top[c],dfs2(s,c,jump[rc][0],g);
                                                                                                                                                                                                                                                                                         // upd c by wson[c], O(1) or O(log(n))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                else return rwho[id[top[p0]]+j1—del];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(del>=j1) return who[id[p0]-j1];
                                                                                                                                                                                                            void solve(int c, int fa, vi g[]) {
                                                                                                                           dfs(1,0,g);_=0;dfs2(1,0,1,g);
rep(i,2,N) lg[i]=lg[i>>1]+1;
                                                                                                                                                                                                                                                                                                                                                                                                                       // brute force upd c by t
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int del=id[p0]-id[top[p0]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int p0=jump[x][lg[k]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int kth_par(int x,int k){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               // kth_par should exist
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if(k==0) return x;
                                                                                                   void Build(vi g[]){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int j0=1<<lg[k];</pre>
                                                                                                                                                                                                                                                                                                                                          // c is leaf
  int s=wson[c];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int j1=k-j0;
                                                                                                                                                                                                                                                                                                                      } else {
```

\mathbf{Path} MoOnTree10.5

```
10.6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for(int i = 1; i < M && pre[u][i - 1]; ++i) pre[u][i] = pre[pre[u][i - 1]][i - 1];</pre>
                                                                                                                                                                                                                    int 1, r, id, lca;
Node(int id, int 1, int r, int lca = 0) : id(id), l(l), r(r), lca(lca) {}
                                                                                                                                                        int dep[N], pre[N][M], st[N], ed[N], dfn[N << 1], B[N << 1], cnt[N];</pre>
                           time 排序
                        // 带修改莫队: 块大小 N^(2/3) 按照 1 所在块, r 所在块,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for(auto v : g[u]) if(v != fa) dfs(v, u, g);
                                                                                                                                                                                                                                                                                                                       if(B[1] := B[c.1]) return B[1] < B[c.1];
                                                                                                                                                                                                                                                                                       bool operator < (const Node &c) const
                                                                                    const int N = ::\mathring{N}, SZ = Sqrt(N), M = 17; int cd; // starts from 1
                                                                                                                                                                                                                                                                                                                                                        return (r < c.r) \wedge (B[1] \& 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     void dfs(int u, int fa, vi g[]) {
  dep[u] = dep[fa] + 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    dfn[++cd] = u, st[u] = cd;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   pre[u][0] = fa;
                                                              namespace MoonTree {
                                                                                                                                                                                                                                                                                                                                                                                                                                                         vector<Node> nds;
                                                                                                                                                                                      struct Node {
// 不带修改莫队
```

VTree

if(nd.lca) upd(st[nd.lca], -1); **if**(nd.lca) upd(st[nd.lca], 1); while(r > nd.r) upd(r--, -1);
while(1 < nd.l) upd(l++, -1);</pre>

// save ans

while(r < nd.r) upd(++r, 1);
while(l > nd.l) upd(—1, 1);

for(auto &nd : nds) {

```
_ = cntd = 0; del[++cntd] = tp[_++] = v[0];
                                                                           int tp[N], _, del[N], cntd, l[N], cntl;
void solve(vi&v,LCARMQ&R){
                                                                                                                                                         rep(i, 1, sz(v)){
int lca = R.lca(tp[_-1] , v[i]);
                                                    const int N = ::N << 1;
                     namespace Vtree{
// sort !
```

g.add(pre, G.to[i], G.val[i]);

g.add(u, G.to[i], G.val[i]);

} else {

 $\textbf{for}(\textbf{auto} \ t \ : \ g[c]) \ \textbf{if}(\texttt{!vis[t]\&k!=fa}) \ dfssz(t,c,Sz,rt) \ , \ sz[c]+=sz[t];$

void dfssz(int c, int fa, int Sz, int &rt){

sz[c] = 1;

10.8

```
dfssz(v, u, Sz, rt);
sz[u] += sz[v];
if(rt == -1 || max(sz[g.to[rt]], Sz - sz[g.to[rt]]) > max(sz[v], Sz - sz[v]))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     \begin{array}{l} \hbox{int } \_ = (I >> 1) + 1 + n, \ \ st = g.fr[I >> 1 << 1], \ \ ed = g.to[I >> 1 << 1]; \\ T.\_add(\_, \ dfs(st));  \end{array} 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for(int i = g.hd[u]; \sim i; i = g.ne[i]) if(!vis[i] && g.to[i] != fa) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for(int i = G.hd[u]; \sim i; i = G.he[i]) if(G.to[i]! = fa) {
                                                                                    int rt=0;dfssz(c,0,0,rt);dfssz(c,0,sz[c],rt=0);
                                                                                                                                                                   * 注意计算以 rt 为起点的路径、只包含 rt 的路径
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  void init(int n) { fill_n(vis, n << 1, 0); }</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Gra g, T; int L, n, sz[N]; bool vis[N << 1];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                void dfssz(int u, int fa, int Sz, int &rt) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void rebuild(int u, int fa, const Gra &G) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(u == 1) L = n = ::n, g.init(n << 1);
                                                                                                                                                                                                                                                          for(auto t : g[rt]) if(!vis[t]) dfs(t),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            g.add(n, G.to[i], G.val[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int I = 0; dfssz(u, 0, 0, I)
if(sz[u] == n) { T.init(n);
if(sz[u] == 1) return u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    g.add(pre, ++n, 0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             dfssz(u, 0, sz[u], I = -1);
if(!rt && sz[c]*2>Sz) rt=c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     vis[I] = vis[I^{-1}] = true
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   bool F = 0; int pre = u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(~G.ne[i]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                namespace ET {
  const int N = ::N << 1;</pre>
                                                                                                                                                                                                 * 注意 v != vis[rt]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int v = g.to[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            T._add(_, dfs(ed));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             pre = n;
                                                                                                              vis[rt] = true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         } else {
                                                    void dfs(int c){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int dfs(int u)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rt = i;
                                                                                                                                                                                                                                                                                                                                                                    边分核
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 sz[u] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return _;
                                                                                                                                                                                                                                                                                                                                                                                                                                      // init
                                                                                                                                                                                                                                                                                                                                                                      10.9
cntl = 0; while(_ > 0 && R.dep[lca] < R.dep[tp[_-1]]) l[++cntl] = tp[--_];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             \textbf{for}(\textbf{auto} \ \texttt{t} \ : \ \texttt{g[c]}) \ \textbf{if}(\texttt{!vis[t]\&kt!=fa}) \ \texttt{dfssz}(\texttt{t,c,Sz,rt}) \ , \ \texttt{sz[c]+=sz[t]};
                          if(_ == 0 || lca != tp[_-1]) del[++cntd] = tp[_++] = lca;
l[++cnt1] = tp[_-1]; del[++cntd] = tp[_++] = v[i];
rep(i, 2, cntl + 1) {
   int u = l[i], v = l[i - 1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         int rt=0;dfssz(c,0,0,rt);dfssz(c,0,sz[c],rt=0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      bool vis[N]; int sz[N], par[N]; vi G[N];
void dfssz(int c,int fa,int Sz,int &rt){
  sz[c] = 1;
                                                                                                                                                                                                                         per(i, 0, _ - 1) {
   int u = tp[i], v = tp[i + 1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for(auto v : g[rt]) if(!vis[v])
int t = dfs(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(!rt && sz[c]*2>Sz) rt=c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            fill_n(G + 1, n, vi());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      fill_n(par + 1, n, 0);
                                                                                                                                                                                                                                                                                                                                          rep(i, 1, cntd + 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               bool vis[N]; int sz[N];
                                                                                                                                         // g[u].pb(v);
                                                                                                                                                                                                                                                                                  // g[u].pb(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      G[rt].pb(t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              const int N = ::N;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     par[t] = rt;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        vis[rt] = true
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       const int N = ::N;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    namespace Centriod {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      namespace Centriod {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       // id starts from 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 // id starts from 1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int dfs(int c){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         点分治
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  点分树
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               void init() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return rt;
                                                                                                                                                                                                                                                                                                                                                                         // de1
```

10.7

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if (!isroot(y, t)) { if ((son[f[y]][t] == y) ^ (son[y][t] == x))rotate(x, t); else
rotate(y, t); }
                                                                                                                                                              if (rev[x])rev1(son[x][0]), rev1(son[x][1]), rev[x] = 0;
if (!in[x] && ctag[x].ex())tagchain(son[x][0], ctag[x]), tagchain(son[x][1], ctag[x])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for (int i = 0; i < 2; i++)if (son[x][i])csum[x] = csum[x] + csum[son[x][i]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      son[y][w] = son[x][w ^ 1];
if (son[x][w ^ 1])f[son[x][w ^ 1]] = y;
if (f[y])for (int z = f[y], i = 0; i < 4; i++)if (son[z][i] == y)son[z][i] = x;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for (int i = 0; i < 2; i++)if (son[x][i])tsum[x] = tsum[x] + tsum[son[x][i]]; for (int i = 2; i < 4; i++)if (son[x][i])tsum[x] = tsum[x] + asum[son[x][i]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                inline void setson(int x, int t, int y) { son[x][t] = y; f[y] = x; }
                                 if (!in[x] && t)tagchain(x, p); else asum[x] = csum[x] + tsum[x];
                                                                                                                                                                                                                                                                                                   ttag[x], 0), tagtree(son[x][1], ttag[x], ttag[x], tagtree(son[x][3], ttag[x],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       inline int child(int x, int t) { pb(son[x][t]); return son[x][t];
inline void rotate(int x, int t) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       f[x] = f[y]; f[y] = x; son[x][w \land 1] = y; up(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int y = f[x], w = (son[y][t + 1] == x) +
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       while (!isroot(i, t))a[++s] = i = f[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            inline void splay(int \times, int t = 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          son[x][2] = son[x][3] = 0; in[x]
return x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int x = rub ? ru[rub - ] : ++tot;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      asum[x] = csum[x] + tsum[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int s = 1, i = x, y; a[1] = i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        csum[x] = data(val[x]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            while (!isroot(x, t)) {
                                                                                                                                                                                                                                                                                              agtree(son[x][0],
ttag[x] = ttag[x] + p;
                                                                                                                                                                                                                                                                                                                                  agtree(son[x][2],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          asum[x] = tsum[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     inline void up(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (in[x]) {
    csum[x] = data();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           while (s)pb(a[s-]);
                                                                                                                                                                                                                                                               if (ttag[x].ex()) {
                                                                                                                                                                                                                                                                                                                                                                      :tag[x] = tag();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               inline int newnode() {
                                                                                              inline void pb(int x)
                                                                                                                                                                                                                                      , ctag[x] = tag();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      tsum[x] = data();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rotate(x, t);
                                                                                                                                     if (!x)return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               (x)dn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     max
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               inline data operator+(const data&a, const tag&b) { return a.size ? data(a.sum*b.a + a.
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                inline data operator+(const data&x) { return data(sum + x.sum, min(minv, x.minv),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                inline bool isroot(int x, int t) {
  if (t) return !f[x] || !in[f[x]] || !in[x];
  return !f[x] || (son[f[x]][0] != x&&son[f[x]][1] != x) || in[f[x]] || in[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            data(int \ a, int \ b, int \ c, int \ d)  { sum = a, minv = b, maxv = c, size = d;  }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              inline tag operator+(const tag&x) { return tag(a^*x.a, b^*x.a + x.b); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int f[N], son[N][4], a[N], tot, rt, rub, ru[N]; bool rev[N], in[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                size*b.b, atag(a.minv, b), atag(a.maxv, b), a.size) : a; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            data() { sum = size = 0, minv = inf, maxv = -inf; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             inline int atag(int x, tag y) { return x*y.a + y.b; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           data(int \times) \{ sum = minv = maxv = x, size = 1; \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      tag(int x, int y) { a = x, b = y; } inline bool ex() { return a != 1 || b; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      tag p, bool t) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   swap(son[x][0], son[x][1]); rev[x]^{-1};
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 //son::0-1 重链儿子, 2-3:AAA 树儿子
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 (maxv, x.maxv), size + x.size); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   inline void tagchain(int x, tag p)
                                                                                                                                                                                                                                                                                                                             Claris
                                                               rebuild(G.to[i], u, G);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                data csum[N], tsum[N], asum[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     csum[x] = csum[x] + p;

asum[x] = csum[x] + tsum[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int sum, minv, maxv, size;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     val[x] = atag(val[x], p)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            tag() \{ a = 1, b = 0; \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      inline void tagtree(int x,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                inline void rev1(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                              const int inf = \sim 0U >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      ctag[x] = ctag[x] + p;
                                                                                                                                                                                                                                              ZProblems
                                                                                                                                                                                                                                                                                                                             全功能
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    tag ctag[N], ttag[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        int a, b; //ax+b
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if (!x) return;
  F = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (!x) return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (!x) return;
                                                                                                                                                                                                                                                                                                                                                                                                       #define N 200010
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 struct data {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          struct tag {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int val[N];
                                                                                                                                                                                                                                                                                                                                  11.1
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tsum[x] = tsum[x] + p;

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for (int i = 2; i < 4; i++) if (son[x][i])tagtree(son[x][i], p, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for (int i = 2; i < 4; i++) if (son[x][i])t = t + asum[son[x][i]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     inline void changechain(int x, int y, tag p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        inline void changetree(int x, tag p) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      inline data askchain(int x, int y) {
                                                                                                                                      splay(x);
while (son[x][0])x = son[x][0];
                                                                                                                                                                                                                                                                                                                inline void link(int x, int y) {
                  inline int lca(int x, int y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 inline data asktree(int \times) {
                                                                                                                                                                                                                 inline void makeroot(int x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              splay(x);

val[x] = atag(val[x], p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     splay(x);
data t = data(val[x]);
                                                                                                                                                                                                                                                                                                                                                                                                               inline void cut(int x)
                                                                                              inline int root(int x)
                                                          return access(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                        splay(x);
f[son[x][0]] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  tagchain(y, p);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return csum[y];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            son[x][0] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       makeroot(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           makeroot(x);
                                                                                                                                                                                                                                                                                                                                      makeroot(x);
                                                                                                                                                                                                                                        access(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      access(x);
                                          access(x);
                                                                                                                       access(x);
                                                                                                                                                                                                                                                                                                                                                         add(y, x);
                                                                                                                                                                                                                                                                                                                                                                                                                                     access(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               access(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               access(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              access(x);
                                                                                                                                                                                                                                                                                                                                                                            access(x);
                                                                                                                                                                           return x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           splay(x);
                                                                                                                                                                                                                                                        splay(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              splay(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               splay(y);
                                                                                                                                                                                                                                                                            rev1(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               (x)dn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          (x)dn
inline int pos(int x) { for (int i = 0; i < 4; i++)if (son[f[x]][i] == x)return i;
                                     inline void add(int x, int y) { // 从 x 连出一条虚边到
                                                                                                                                                                           while (son[x][2] \& in[son[x][2]])x = child(x, 2);
                                                                                                                                                                                                                                                                                                              inline void del(int x) { // 将 x 与其虚边上的父亲断开
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               setson(z, pos(y), child(y, pos(x) ^{\wedge} 1)); splay(z, 2);
                                                                                              for (int i = 2; i < 4; i++)if (!son[x][i])</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                 int s = 1, i = y, z = f[y]; a[1] = i;
while (!isroot(i, 2))a[++s] = i = f[i];
while (s)pb(a[s--]);
if (z) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               inline int fa(int x) { // x 通过虚边的父亲
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for (; x; y = x, x = fa(x))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (!f[x])return 0;
if (!in[f[x]])return f[x];
                                                                                                                                                                                                            setson(z, 2, son[x][2]);
setson(z, 3, y);
setson(x, 2, z);
splay(z, 2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       inline int access(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               son[y][pos(x)] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      del(y);
add(x, son[x][1]);
                                                                                                               setson(x, i, y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          setson(x, 1, y);
                                                                                                                                                                                                int z = newnode();
                                                                                                                                                                                                                                                                                                                                                       splay(x);
if (!f[x])return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ru[++rub] = y;
                                                                                                                                                                                                                                                                                                                                                                                           int y = f[x];
if (in[y]) {
                                                                                                                                                                                                                                                                                                                                   if (!x)return;
                                                       if (!y)return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int t = f[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             splay(t, 2);
return f[t];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               splay(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       splay(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int y = 0;
                                                                                                                                         return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               (x)dn
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          f[x] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      splay(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return y;
                      return 4; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              else {
                                                                            (x)qd
```

```
makeroot(rt);

}
if (k == 8) { // 链最大值
    read(x), read(y);
    printf("%d\n", askchain(x, y).maxv);

makeroot(rt);
}
if (k == 10) { // 链和
    read(x), read(y);
    printf("%d\n", askchain(x, y).sum);
    makeroot(rt);
}

return 0;
```

11.2 basic

```
inline uint64 mul_add_mod(uint64 a, uint64 b, uint64 c, uint64 mod) {
   return mod128_64_small(uint128(a) * b + c, mod);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      inline uint64 mul_mod(uint64 a, uint64 b, uint64 mod) {
                                                                                                                                                                                                                                                                                        inline uint64 mod128_64_small(uint128 a, uint64 b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   inline int64 sub_mod(int64 x, int64 y, int64 mod) { return (x-y+mod)\ \% mod;
                                                                                                                                                                                                                                                                                                                                                                                                                      : "=a"(q), "=d"(r)
: "0"(uint64(a)), "1"(uint64(a >> 64)), "rm"(b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     // mod should be not greater than 2^62 (about 4e18)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      inline int64 add_mod(int64 x, int64 y, int64 mod)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (mod < int(1e9)) return a * b % mod;
uint64 k = (uint64)((long double)a * b / mod);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // return a ^{st} b \% mod when mod is less than 2^31
                                                                                                                         using uint64 = unsigned long long;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if ((int64)res < 0) res += mod
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     uint64 res = a * b - k * mod;
                                                                                                                                                                                          using uint128 = __uint128_t;
using float80 = long double;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          assert(0 \le a \&\& a < mod); assert(0 \le b \&\& b < mod);
                                                                                                                                                       using int128 = \_int128\_t;
                                                       #include <algorithm>
using int64 = long long;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return (x + y) \% mod;
                              #include <cassert>
                                                                                                                                                                                                                                                            // return a % b
                                                                                                                                                                                                                                                                                                                                                              _asm_ (
"divq\t%4"
                                                                                                                                                                                                                                                                                                                           uint64 q, r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return res;
#pradma once
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             return r;
```

```
For (i = 1, i < n, i++) read(ed[i][0]), read(ed[i][1]);
                                                                                   for (i = 1; i <= n; i++) read(val[i]), up(i);
for (i = 1; i < n; i++) link(ed[i][0], ed[i][1]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            printf("%d\n", askchain(x, y).minv);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        printf("%d\n", asktree(x).minv);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            printf("%d\n", asktree(x).maxv);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                printf("%d\n", asktree(x).sum);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   changechain(x, y, tag(0, z));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         changechain(x, y, tag(1, z));
makeroot(rt);
                                                                                                                                                                                                                                                                                              if (lca(x, y) == x)continue;
                                                                                                                                                                                                                                              }
if (k == 9) { // x 的父亲变成 y
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   read(x), read(y), read(z);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       read(x), read(y), read(z);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       changetree(x, tag(1, y));
int n, m, x, y, z, k, i, ed[N][2];
int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                   changetree(x, tag(0, y));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       }
if (k == 3) { // 子树最小值
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            }
if (k == 4) { // 子树最大值
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        }
if (k == 7) { // 链最小值
read(x), read(y);
                                                                                                                                                                                                                                                                                                                                                                 }
if (k == 0) { // 子树赋值
                                                                                                                                                                                                                                                                                                                                                                                                                                    }
if (k == 5) { // 子树加
read(x), read(y);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              }
if (k == 11) { // 子树和
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 (k == 2) { // 链赋值
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      (k == 6) { // 链加
                                                                                                                                                                         read(k);
if (k == 1) { // 換根
                                                                                                                                                                                                                                                                              read(x), read(y);
                                                                                                                                                                                                                                                                                                                                                                                                    read(x), read(y);
                                                                                                                                                                                                                           makeroot(rt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     makeroot(rt);
                                                                                                                                                                                                                                                                                                                                                   makeroot(rt);
                                                                                                                                                                                                                                                                                                                                link(y, x);
                                     read(n); read(m);
                                                                                                                                                                                                           read(rt);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 read(x);
                                                                                                                                                         while (m--) {
                                                                                                                                                                                                                                                                                                                cut(x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          read(x)
                                                                                                                                       makeroot(rt);
                                                                                                                         read(rt);
                                                     tot = n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ~:
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ~ ;;
```

ull fac = fact_range(0, p - 1), ifac = mod_inv(fac, pe);

vl f_pe(deg, 1);

 $// f_{-}\{p,e\}(0..2e-2)$: $O(e^{*} min(p,e) + e log(p))$

for (ull k = 0; k < min_pe; ++k) {
 ret = (ret + (dw)prod * s1[v * min_pe + k]) % pe;</pre>

prod = (dw)prod * coef % pe;

return ret;

;;

. (0 ||

```
//f_{-\{p,e\}} = \prod_{\{i=0\}^{\ell}\{x-1\}(1 + \sum_{k=1}^{\ell=1}^{\ell=1}) \footnote{\{stirlingfirst\{p\}\{k+1\}\}\{n\}\}} = (1+1)^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell}f_{-1}^{\ell
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        S1[0 + j] = (S1[0 + j - min_pe - 1] + (dw)S1[0 + j - min_pe] * i) % pe,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // product of \{up + 1, \ldots, up + v\} mod p^{Ae}
auto fact_range = [&] (ull u, ull v) {
  ull coef = (dw)u % pe * p % pe, prod = 1, ret
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  // first kind stirling number: O(p^* \min(p, e))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 1, e+1) pows[i] = (pe *= p);
ull period = pe / p * 2, deg = e * 2 - 1;
if (p == 2 && e >= 3) period >>= 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    s1[o] = (dw)s1[o - min_pe] * i % pe,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (\_gcd(a, mod) != 1) return -1; 11 b = mod, s = 1, t = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ull fact_pe(ull n, ull p, ull e) {
    vl pows(e + 1, 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 ull pe = 1, min_pe = min(p, e);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                vl s1(p * min_pe); s1[0] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                {\sf typedef\ unsigned\ long\ long\ ull;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return s < 0 ? s + mod : s;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      stirlingfirst\{p\}\{1\}\} (ip)^{\wedge}k)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ll mod_inv(ll a, ll mod) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           swap(a -= q * b, b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          swap(s = q * t, t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(i, 1, p) {
    int o = i * min_pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(j, 1, min_pe)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      typedef __uint128_t dw;
typedef vector<ull> vl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     11 q = a / b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         +1}{k+1} \bmod p^e
                                                                                                                                                                                                                                                                                                   factors
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              while (b) {
return ret;
```

```
bool linear_equation(int64 a, int64 b, int64 c, int64 &x, int64 &y)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                uint64 crt2(uint64 r1, uint64 mod1, uint64 r2, uint64 mod2) {
                                                                                                                                                                                                                                                                                                                           \lambda' ax + by = gcd(a, b), |x| + |y| is minimum void exgcd(int64 a, int64 b, int64 &g, int64 &x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       inv, mod2) * mod1 + r1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for (int64 i = 2; i * i <= n; ++i) if (n % i == 0) {
int64 pow_mod(int64 a, int64 m, int64 m)
                                                                              if (n \& 1) res = mul\_mod(res, a, m);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         \frac{1}{1} if (n > 1) ret = ret / n * (n - 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (c % g) return false;
b /= g, a /= g, c /= g;
x = (x % b * (c % b) % b + b) % b;
y = (c - a * x) / b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int64 mod_inv(int64 a, int64 mod) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // return x, where ax = 1 \pmod{mod}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           uint64 inv = mod\_inv(mod1, mod2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            //ax + by = c,x >= 0, x is minimum //xx = x + t * b, yy = y - t * a
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (gcd(a, mod) != 1) return -1;
int64 b = mod, s = 1, t = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     return mul_mod(r2 + mod2 - r1,
                                                                                                                                                                                                                                                                          return !b ? a : gcd(b, a % b);
                                                                                                                                                                                                                                                                                                                                                                                       if (!b) x = 1, y = 0, g = a;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           while (n \% i == 0) n /= i;
                                                                                                                                                                                                                                                                                                                                                                                                                                          exgcd(b, a % b, g, y, x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           std::swap(a -= q * b, b);
std::swap(s -= q * t, t);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return s < 0 ? s + mod : s;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ret = ret / i * (i - 1);
                                                     or (a %= m; n; n >>= 1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int64 euler_phi(int64 n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     std::swap(a -= q * b,
                                                                                                          a = mul_mod(a, a, m);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   // 求的欧拉函数值,简易版n
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        y = x * (a / b);
                                                                                                                                                                                                                         template<typename T>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int64 q = a / b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         exgcd(a, b, g, x, y);
                                                                                                                                                                                                                                                 T gcd(T a, T b) {
                             int64 res = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int64 ret = n;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  return true;
                                                                                                                                                                    return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      while (b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int64 g;
```

```
if (ex & 1) ret = (dw)ret * fac % pe;
                                                        for (ex %= period; ex; ex >>= 1) {
                                                                                                                   fac = (dw)fac * fac % pe;
p = n, n = q;
```

```
const int P = 1e9 + 7, N = 1e5 + 8;
int add(int a, int b) {if((a += b) >= P) a -= P; return a < 0 ? a + P : a;}
int mul(int a, int b) {return 111 * a * b % P;}
int kpow(int a, int b) {int r=1;for(;b;b>>=1,a=mul(a,a)) {if(b&1)r=mul(r,a);}return r;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (vis[v] != inc(vis[u])) ok = \theta;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (vis[v] != dec(vis[u])) ok = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       vis[v] = dec(vis[u]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                vis[v] = inc(vis[u]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ios::sync_with_stdio(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for (auto v : gg[u]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                for (auto v : g[u]) {
                                                                                                          int vis[N], n, m, u, v;
                                                                                                                                                                                                                 if (x == 4) x = 1;
                                                                                                                                                                                                                                                                                                                          if (x == 0) x = 3;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                rep(i, 1, m+1) {
cin >> u >> v;
                                                                                                                                                    vi g[N], gg[N], tmp;
int inc(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                          if (!vis[v])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (!vis[v])
                                                                                                                                                                                                                                                                                                                                                                                        void dfs(int u) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      g[u].pb(v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        cin >> n >> m;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            dfs(v);
                                                                                                                                                                                                                                                                                  int dec(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      dfs(v);
                                                                                                                              11 use[N], ans;
                                                                                                                                                                                                                                                                                                                                                                                                                 tmp.pb(u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      cin.tie(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int main() {
                                                                                                                                                                                                                                          return x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          }else
                                                                                                                                                                                                                                                                                                                                                   return x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    }e1se
                                                                                      bool ok;
```

```
三元闭包边计数
                                                                                                                                                 return ret;
                                                                                                                                                                                                                                   11.4
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   add = (dw)pows[ex] * prod % pe * inv[i] % pe * add % pe * f_pe[i] % pe;
ret = (ret + add) % pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 for (ull i = 0; i < deg; ++i) {
  ull j = deg - 1 - i, ex = v - vs[i] - cfac_vs[i] - cfac_vs[j];
  if (ex >= e) continue;
  ull add = (dw)cifac[j] * cifac[i] % pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  iprod = (dw)iprod * ((x - i) / pows[vs[i]]) % pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          co fact_p = [&](ull u, ull v) {
    return (dw)fact_range(u, v) * evaluate(u) % pe;
                                                                                                                                                                                                                                                                                                                                               cifac[i] = (dw)cifac[i + 1] * cifac[i] % pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                 // find the value of f_{-}\{p,\ e\}(x): O(e \log x) auto evaluate = [\&](ull\ x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for (; m % p == 0; m /= p, ++vs[i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for (int i = deg - 1; i >= 0; —i) { inv[i] = (dw)iprod * inv[i] % pe;
// coprime factorials: O(e + e \log(p))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ret = (dw)ret * fact_p(u, v) % pe;
                                                                                                                                                                                                                                                                                                                for (int i = deg - 2; i \ge 0; —i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           // ((up+v)!)_p \mod p^{\wedge}e: O(min(p, e))
                                                                                                                                        for (; j % p == 0; j /= p, ++v);
cfac_vs[i] = cfac_vs[i - 1] + v;
                                                                                                                                                                                                                                                                                      cifac[deg - 1] = mod\_inv(prod, pe)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ull v = 0, prod = 1;
for (ull i = 0; i < deg; ++i) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            ull iprod = mod_inv(prod, pe);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (j & 1) add = pe - add;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       auto fact_p = [&](ull u, ull v)
                                                                                   for (ull i = 1; i < deg; ++i) {</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (x < deg) return f_pe[x];
vl vs(deg), inv(deg);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         prod = (dw)prod * m % pe;
                          vl cifac(deg, 1), cfac_vs(deg);
                                                                                                                                                                                                                              prod = (dw)prod * j % pe;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ull q = n / p, v = n % p;
ull u = q % period;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ull m = x - i;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        ull ret = 1, ex = 0;
                                                                                                                ull j = i, v = 0;
                                                                                                                                                                                                  cifac[i-1] = j;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               inv[i] = prod;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    v += vs[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ull ret = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   while (n > 0) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         return ret;
                                                       ull prod = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ;;
```

```
\dot{b}[0]/=3; b[1]/=2; b[4]-=3*b[0]; b[7]-=2*b[6]; b[8]-=2*b[6]; ans=0; rep(i, 0, 9) ans += b[i] * c[i], b[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                         inline int rk(int \times) { return lower_bound(all(V), \times) - V.begin(); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   static const int N = 2500005; //(::N + 32 * ::M) * 16;
                                                                                                                                                                                                                                                                                            const_int N = 50505, M = 10101;
                                                                            cout << ans << endl;
                                                                                                                                                                                                                                                                                                                       int n, m, a[N], rt[N<<1];</pre>
                                                                                                                                                                                                                                                                  // zoj 2112 动态区间 k 大
                                                                                                                                                                                                       必参 k 大
                                                                                                                                                                                                                                                                                                                                                                                                                                                      int a, b, k;
                                                                                                                                                                                                                                                                                                                                               vi V, add, sub;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                }q[M];
|struct Seg {
                                                                                                                                 return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                          bool 'op;
                                                                                                                                                                                                                                                                                                                                                                                                     struct Q {
                                                                                                                                                                                                            11.6
                                                                                                                                                                                                                                                              if (ok) ans += use[1] * use[2] + use[2] * use[3] + use[3] * use[1];
                                                                                                                             if (!ok) { ans += 111 * sz(tmp) * sz(tmp);
                                                                                                                                                                                                                                                                                                                                           for (auto u : tmp) ans += sz(g[u]);
                                                                                                                                                                             rep(i, 1, 4) use[i] = 0;
for (auto u : tmp) use[vis[u]]++;
                                                                                                                                                                                                                                  rep(i, 1, 4) ok \&=use[i] > 0;
                                                                          ok = 1; tmp.clear(); vis[i] = 1;
                                                rep(i, 1, n+1) if (!vis[i]) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                    cout << ans << endl;
                                                                                                                                                                                                                                                                                                                 int t = 0;
gg[v].pb(u);
                                                                                                                                                             }else {
                                                                                                       dfs(i)
```

六元环计数

```
rep(i, 1, N) \ f[i] = i \ * (i-1) / 2, \ g[i] = i \ * (i-1) \ * (i-2) / 6; while (cin >> n){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(j, 0, n) if (a[i][j]) res += (a[i] & a[j]).count();
res /= 2; b[8] += res * (res - 1) / 2;
= 只用走六步的所有方案(-ans)/6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if (a[i][j]) b[2]++;
if (a[i][j]) b[4] += (d[i]-1)*(d[j]-1);
if (a[i][j]) b[6] += f[x];
                                                                                                                                                                                                                                                                                                                               rep(j, 0, n) if (s[j] == '1') a[i].set(j);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            b[7] += f[x] * (d[i] + d[j] - 4);
                                                                                                                                                                                                                                                                                                                                                                                                                                                         int \times = (a[i] \& a[j]).count();
                                                                                                  int n; string s;
11 ans, b[9], f[N], g[N], d[N];
11 c[9] = {24, 48, 2, 12, 6, 12, 36, 12, 24};
int main(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (a[i][j]) b[0] += x;
                                                                                                                                                                                                                                                    rep(i, 0, n) a[i].reset();
rep(i, 0, n) {
                                                                                                                                                                                                                                                                                                                                                          d[i] = a[i].count();
// ans = 非六元简单环计数六元环
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(i, 0, n) {
b[3] += f[d[i]];
b[5] += g[d[i]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          b[1]+=f[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                rep(j, i+1, n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          11 res = 0;
                                                  const int N = 1e3 + 7;
                           // time : O(n^3 / 64)
                                                                                                                                                                                                                                                                                                                                                                                                           rep(i, 0, n)
                                                                                                                                                                                                                                                                                                        cin >> s;
                                                                           bitset<N> a[N];
```

```
for(; x<=n; x+=lb(x)) seg.upd(rt[x+n], rt[x+n], p, c, 0, sz(V)-1);
int cntn, cnt[N], ls[N], rs[N];
void init() { fill_n(rt+1, n, cntn = 0); }
void upd(int pre, int &now, int p, int c, int l, int r) {
                                                                                                                                                                                                                                                                  if(p<=mid) upd(ls[pre], ls[now], p, c, l, mid);</pre>
                                                                                                                                                                                                                                                                                                else upd(rs[pre], rs[now], p, c, mid+1, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(i, 0, sz(add)) add[i] = rs[add[i]];
                                                                                                                                                                                                                                                                                                                                                    int qry(int L, int R, int k, int l, int r) {
   if(l == r) return l;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 0, sz(sub)) sub[i] = rs[sub[i]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     rep(i, 0, sz(add)) add[i] = ls[add[i]];
rep(i, 0, sz(sub)) sub[i] = ls[sub[i]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   return qry(L, R, k-lc, mid+1, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for(auto i : add) lc += cnt[ls[i]];
for(auto i : sub) lc -= cnt[ls[i]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                #define lb(x) ((x)&(-x))
void init() { fill_n(rt+1+n, n, 0); }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                return qry(L, R, k, l, mid);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            void upd(int x, int p, int c) {
                                                                                                                    cnt[now] = cnt[pre] + c;
                                                                                                                                                                                                           if(1 == r) return;
                                                                                                                                                    ls[now] = ls[pre];
                                                                                                                                                                                rs[now] = rs[pre];
                                                                                                                                                                                                                                                                                                                                                                                                                     int mid = 1+r>>1;
                                                                                                                                                                                                                                           int mid = 1+r>>1;
                                                                                             now = ++cntn;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(lc>=k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                       int lc = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       struct Fenwick {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            } else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              }seg;
```

SZ

```
void upd(int p, int o, int c) \{ for( ; p <= n; p += lb(p)) upd(fw[p], fw[p], c, o, 1, p \text{ or } p \text{ o
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      rep(i, 0, sz(g[u])) if(g[u][i]!= fa) dfs(g[u][i], u);
ed[u] = dfn;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int p = st[u]; for( ; p; p ^{\wedge}= 1b(p)) res[o].pb(fw[p]);
                                                                                                                                                                                                                                                                                                                                                rep(i, 0, sz(res[0])) res[0][i] = rs[res[0][i]];
rep(i, 0, sz(res[1])) res[1][i] = rs[res[1][i]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              rep(i, 0, sz(res[0])) res[0][i] = ls[res[0][i]];
rep(i, 0, sz(res[1])) res[1][i] = ls[res[1][i]];
                                                                                                                                                                   rep(i, 0, sz(res[0])) cntr += cnt[rs[res[0][i]]];
                                                                                                                                                                                                                             rep(i, 0, sz(res[1])) cntr -= cnt[rs[res[1][i]]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     upd[rt[u], rt[fa], F(val[u]), 1, 1, sz(V));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int_p = Q[i].se.fi, c = Q[i].se.se;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           upd(st[p], -1, F(val[p]));
upd(ed[p] + 1, 1, F(val[p]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return qry(k - cntr, 1, mid);
                                                                                                                                                                                                                                                                                                                                                                                                                                                               return qry(k, mid + 1, r);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void dfs(int u, int fa) {
                                                         int mid = 1 + r >> 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void upd(int u, int o)
if(1 == r) return 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             dfs(1, 0);
rep(i, 1, m + 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           res[o].pb(rt[u]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(!Q[i].fi) {
                                                                                                                                                                                                                                                                                       if(cntr >= k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        st[u] = ++dfn;
                                                                                                                       int cntr = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            // build 主席树
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             par[u] = fa;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          void solve() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    R.Build(g);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             else {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    // fenwick
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(q[i].op) { cout << V[fw.qry(q[i].a, q[i].b, q[i].k)] << endl;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 1, n+1) seg.upd(rt[i–1], rt[i], rk(a[i]), 1, 0, sz(V)–1);
rep(i, 1, m+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    rep(i, 1, n+1) cin >> a[i], V.pb(a[i]); rep(i, 1, m+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                               return seg.qry(1, r, k, 0, sz(V)-1)
                                                                                                                                                                                                                                                                                  for(; x; x^=lb(x)) add.pb(rt[n+x]);
                                                                                                                                                                                                                                                                                                                                                                                                     for(; x; x^=lb(x)) sub.pb(rt[n+x]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         V.erase(unique(all(V)), V.end());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             int p = q[i].a, c = q[i].b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        fw.upd(p, rk(a[p] = c), 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     V.clear(); seg.init(); fw.init();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        cin >> s >> q[i].a >> q[i].b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 q[i].op = (s[\tilde{0}]=='Q');

if(s[\tilde{0}]=='Q') cin >> q[i].k;
                                                                                                                                                                   add.pb(rt[r]);sub.pb(rt[l-1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       fw.upd(p, rk(a[p]), -1);
                                                         int qry(int 1, int r, int k) {
                                                                                                                   add.clear();sub.clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         else V.pb(q[i].b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    cin >> n >> m;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int T; cin >> T;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             sort(all(V));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              string s;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    } else {
                                                                                                                                                                                                                                 int x = r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      while(T--) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ///solve
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       ///read
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int main() {
```

11.8 勾股数计数

int a = Q[i].se.fi, b = Q[i].se.se, k = Q[i].fi;

rep(o, 0, 2) res[o].clear();

else {

int n, m, L, dfn, val[N], rt[N], cnt[M], ls[M], rs[M], st[N], ed[N], fw[N], par[N];
pair<int, pii>Q[N]; vi V, res[2], g[N]; LCARMQ R;
int F(int x) { return lower_bound(all(V), x) - V.begin() + 1; }

动态树上路径 k 大

void upd(int &now, int pre, int p, int c, int l, int r) {

cnt[now] = cnt[pre] + c;

now = ++L;

sed

ls[now] = ls[pre];
rs[now] = rs[pre];
if(1 == r) return;
int mid = 1 + r >> 1;

upd(st[p], 1, F(val[p])); upd(ed[p] + 1, -1, F(val[p]));

val[p] = c;

int c = R.lca(a, b), d = par[c]

upd(a, 0); upd(b, 0); upd(c, 1); upd(d, 1); << end]

cout << V[qry(k, 1, sz(V)) - 1]

```
int mu[N], p[N], tot = 0, Sqr, n; bool vis[N];
                                const int N = 34000;
if(p <= mid) upd(ls[now], ls[pre], p, c, 1, mid);
else upd(rs[now], rs[pre], p, c, mid + 1, r);</pre>
                                                                                                   int qry(int k, int l, int r) {
```

//为结尾的回文串的长度一定可以分成段等差数列rlogn

//序dfs

```
cout << solve(nn) << endl;</pre>
cin >> T;
rep(cas, 0, T) {
                                    cin >> nn;
                                                                                     return 0;
```

区间本质不同回文子串计数

```
int sum(int \times) { int res = 0; for (int i = x; i; i -= i&-i)res += d[i]; return res
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (fr <= t)return query(x << 1, 1, t, fl, fr); else
if (fl > t) return query(x << 1 | 1, t + 1, r, fl, fr); else
return max(query(x << 1, 1, t, fl, t), query(x << 1 | 1, t + 1, r + 1, r
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      void updata(int x, int y) { for (int i = x; i < N; i += i\&-i)d[i] += y;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if (pos <= t) updata(x << 1, 1, t, pos, y); else
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int next[N][26], fail[N], len[N], s[N], id[N], last,
int in[N], out[N], d[N], up[N], dfn = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              s[n] = -1;//开头放一个字符集中没有的字符,减少特判
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int query(int x, int 1, int r, int f1, int fr) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       void updata(int x, int 1, int r, int pos, int y)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for (int i = 0; i < 26; ++i) next[p][i] = 0; len[p] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      updata(x << 1 \mid 1, t + 1, r, pos, y); a[x] = max(a[x << 1], a[x << 1 \mid 1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           if (1 == f1 \& r == fr) return a[x];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   if (1 == r) \{ a[x] = y; return; \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inline int newnode(int 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          newnode(0); newnode(-1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int t = (1 + r) > 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int t = (1 + r) > 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   char s[N]; int m, n, 1, r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inline void init() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           const int N = 600005
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      vector<int>G[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   11 ans = 0, ret[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               vector<pii> Q[N];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       struct SegTree {
  int a[N << 2];</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return p++;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  last = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       namespace Space {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              struct BIT {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  struct PAM {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              ;0 = d
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      n = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int d[N];
                                                                                                                                                                                                                                                                                                                                                                                                                       11.9
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for(int i = 1; i * i < r; i++) cnt1 += sqrt(r - i * i);
for(int i = 1; i * i < r; i += 2) cnt2 += (sqrt(r - i * i) + 1) / 2;</pre>
int w1[N * 2], w2[N * 2], id1[N * 2], id2[N * 2], t1;// 注意 longlong
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ans += 111 * (n / 1) * (w2[id(r)] - w2[id(1-1)]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ans += 1ll * (n / l) * (w1[id(r)] - w1[id(l-1)]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int id(int x) { return x <= Sqr ? id1[x] : id2[n / x];}</pre>
                                                                                                                                                                                                                                                               for(int j = 1; j <= tot && p[j] * i < N; j++){
  int u = p[j] * i;</pre>
                                                                                                                                                                                                                                                                                                                                                                       vis[u] = 1;
if(i % p[j] == 0) { mu[u] = 0; break; }
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  r \le Sqr ? id1[r] = t1 : id2[n / r] = t1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if (k & 1) ans -= h2(n/k/k) * mu[k];
                                                                                                   mu[1] = 1;
rep(i, 2, N) {
   if (!vis[i]) p[++tot] = i,mu[i]=-1;
   if (!vis[i]) p[++tot] = i,mu[i]=-1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for(int 1 = 1, r; 1 \le n; 1 = r + 1){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for(int 1 = 1, r; 1 \le n; 1 = r + 1){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              w1[++t1] = cnt1, w2[t1] = cnt2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for(int l = 1, r; l < = n; l = r + 1){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for(int k = 1; k * k <= n; k++){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (mu[k] == 0) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          ans += h1(n/k/k) * mu[k];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int cnt1 = 0, cnt2 = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                       mu[u] = -mu[i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  ios::sync_with_stdio(0);
cin.tie(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Sqr = Sqrt(n); t1 = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      r = n / (n / 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   r = n / (n / 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               r = n / (n / 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return ans / 2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      solve(int _n) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               11 ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               11 ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return ans;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          11 ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       11 h2(int n){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       11 h1(int n){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int main() {
                                                   void init(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int T, nn;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              init();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      FI(a);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              Ħ
```

```
, O(nlogn^2), 下标从 1 开始
/*注: 离线算法
                12 5
abcddcbaabcd
                                     1 8
4 8
1 12
                                4
                                                            04804
```

while (s[n - len[x] - 1]! = s[n]) x = fail[x];

inline int get_fail(int x) {

fail[0] = 1;

inline void add(int c, int cc)

return x;

int cur = get_fail(last); if (!next[cur][c]) {

s[++n] = c;c -= 'a';

带花树最大权匹配

```
inline void update_slack(int u,int x){
    if(!slack[x]||e_delta(g[u][x])<e_delta(g[slack[x]][x]))slack[x]=u;</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             if(x<=n)q.push(x);
else for(size_t i=0;i<flower[x].size();i++)q_push(flower[x][i]);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                queue<int> q;
inline int e_delta(const edge &e){ // does not work inside blossoms
return lab[e.u]+lab[e.v]-g[e.u][e.v].w*2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if(g[u][x].w>0&&st[u]!=x&&S[st[u]]==0)update_slack(u,x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              int match[MAXN*2+1], slack[MAXN*2+1], st[MAXN*2+1], pa[MAXN*2+1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int flower_from[MAXN*2+1][MAXN+1],S[MAXN*2+1],vis[MAXN*2+1];
vector<int> flower[MAXN*2+1];
                                                                                                                                                                                                                                                                          // from vfleaking
// 求的是在权最大情况下的匹配权值大优先应该要是正数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 edge(){} edge(int u, int v, int w):u(u),v(v),w(w){}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               inline void set_st(int x,int b){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               inline void set_slack(int x){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                edge g[MAXN*2+1][MAXN*2+1];
int lab[MAXN*2+1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           slack[x]=0;
for(int u=1;u<=n;++u)
                                                                                                                                                                                                                                                                                                                                   // id : 1 .. n
// time : 应该也是 O(n^3)
                                                                                                                                                                                                                                                                                                                                                                                               #define INF INT MAX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             void q_push(int x){
                                                                                                                                                                                                                                                                                                                                                                                                                            #define MAXN 600
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 int u,∨,w;
                                                                                                                                                                                                                                                                                                                                                                                                                                                            struct edge{
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int n,n_x;
                                                                                                                                                                                                          11.10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for (int j = id[i]; j; j = fail[up[j]]) {
   int l = max(1, Seg.query(1, 1, dfn, in[j], out[j]) - len[j] + 2);
   int r = i - len[up[j]] + 2;
                                                                                                                                                                                                                                                                 void build() { for (int i = 0; i < p; i++)if (i != 1) G[fail[i]].pb(i); }</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for (int i = 1; i <= m; i++) scanf("%d%d", &1, &r), Q[r].pb(mp(1, i));
                                                           next[cur][c] = now;
d[now] = len[now] - len[fail[now]];
up[now] = (d[fail[now]] == d[now] ? up[fail[now]] : now);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         Seg.updata(1, 1, dfn, in[id[i]], i);
for (auto j : Q[i]) ret[j.se] = BT.sum(j.fi);
                             fail[now] = next[get_fail(fail[cur])][c];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i, 1, m + 1) printf("%lld\n", Space::ret[i]);
return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for (int i = 1; i <= n; i++) A.add(s[i], i);</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                BT.updata(1, 1); BT.updata(r, -1);
int now = newnode(len[cur] + 2);
                                                                                                                                                                                                                                                                                                                                                                                                                                            void solve() {
  for (int i = 1; i <= n; i++) {</pre>
                                                                                                                                                                                                                                                                                                                                                            for (auto i : G[x]) dfs(i);
                                                                                                                                                                             last = next[cur][c];
                                                                                                                                                                                                                                                                                               void dfs(int \dot{x} = 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           void work(int n, int m)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       scanf("%s", s + 1);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 scanf("%d%d", &n, &m);
                                                                                                                                                                                                                                                                                                                            in[x] = ++dfn;
                                                                                                                                                                                                             id[cc] = last;
                                                                                                                                                                                                                                                                                                                                                                                        out[x] = dfn;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 Space::work(n, m);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           A.build();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    A.solve();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int n, m, 1, r;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       A.init();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             A.dfs();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int main() {
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if(g[b][x].w=0|e_delta(g[xs][x])<e_delta(g[b][x]))
                                                                                                                                                                                                                                                                                                                                                                                                                              int xr=flower_from[b][g[b][pa[b]].u], pr=get_pr(b,xr);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(st[x]==x&&!match[x])pa[x]=0,S[x]=0,q_push(x);
                                                                                                                                                                                                               if(flower_from[xs][x])flower_from[b][x]=xs,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(!lca)return augment(u,v),augment(v,u),true;
                                                                                                                                                    [sx][x]6=[q][x]6x][x][sx]6=[x][q]6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int xs=flower[b][i], xns=flower[b][i+1];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for(size_t i=pr+1;i<flower[b].size();++i){
  int xs=flower[b][i];</pre>
for(int x=1;x<=n;++x)flower_from[b][x]=0</pre>
                         for(size_t i=0;i<flower[b].size();++i){</pre>
                                                                                                                                                                                                                                                                                                                                  inline void expand_blossom(int b){ // S[b]
                                                                                                                                                                                                                                                                                                                                                                 for(size_t i=0;i<flower[b].size();++i)</pre>
                                                                                                                                                                                                                                                                                                                                                                                               set_st(flower[b][i],flower[b][i]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         inline bool on_found_edge(const edge &e){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     memset(slack+1,0,sizeof(int)*n_x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int u=q.front();q.pop();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(S[st[u]]==1)continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     slack[xs]=0, set_slack(xns);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         memset(S+1, -1, sizeof(int)*n_x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    else add_blossom(u,lca,v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      for(int v=1;v<=n;++v)</pre>
                                                                                  for(int x=1;x<=n_x;++x)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        S[xs]=-1, set\_slack(xs);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               if(q.empty())return false
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int lca=get_lca(u,v);
                                                                                                                                                                                for(int x=1;x<=n;++x)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                slack[v]=slack[nu]=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int nu=st[match[v]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int u=st[e.u], v=st[e.v];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          pa[xs]=g[xns][xs].u;
                                                             int xs=flower[b][i];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                for(int x=1;x<=n_x;++x)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 S[nu]=0, q_push(nu);
                                                                                                                                                                                                                                                                                                                                                                                                                                                               for(int i=0;i<pr;i+=2)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   pa[v]=e.u, S[v]=1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              S[xr]=1, pa[xr]=pa[b];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      S[xs]=1, S[xns]=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             while(q.size()){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inline bool matching(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             }else if(S[v]==0){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    d_push(xns);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        q=queue<int>()
                                                                                                                                                                                                                                                                          set_slack(b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         if(S[v]=-1){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 return false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                st[b]=0;
```

```
flower[b].push_back(x),flower[b].push_back(y=st[match[x]]),q_push(y);
reverse(flower[b].begin()+1,flower[b].end());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               flower[b].push_back(x),flower[b].push_back(y=st[match[x]]),q_push(y);
                                                                                                                     int pr=find(flower[b].begin(),flower[b].end(),xr)—flower[b].begin();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rotate(flower[u].begin(),flower[u].begin()+pr,flower[u].end());
                                                                                                                                                                                                                                                                                                                                                                                                                                                                   for(int i=0;i<pr:/++i)set_match(flower[u][i],flower[u][i^1]);</pre>
                                                                                                                                                                                     reverse(flower[b].begin()+1,flower[b].end());
                                                                                                                                                                                                                                                                                                                                                                                                                                  int xr=flower_from[u][e.u],pr=get_pr(u,xr);
if(x>n)for(size_t i=0;i<flower[x].size();++i)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for(int x=1;x<=n_x;++x)g[b][x].w=g[x][b].w=0;
                                                                                                                                                 if(pr%2==1){ // 检查他在前一层图是奇点还是偶点
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              vis[u]=t; // 这种方法可以不用清空 v 数组
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      inline void add_blossom(int u,int lca,int v){
                                                                                                                                                                                                                    return (int)flower[b].size()—pr;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for(int x=u,y;x!=lca;x=st[pa[y]])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    for(int x=v,y;x!=lca;x=st[pa[y]])
                                                                                                                                                                                                                                                                                                          inline void set_match(int u,int v){
                               set_st(flower[x][i],b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  set_match(xnv,st[pa[xnv]]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         inline void augment(int u,int v){
                                                                                        inline int get_pr(int b,int xr){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       inline int get_lca(int u,int v){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(vis[u]==t)return u;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        flower[b].push_back(lca);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int xnv=st[match[u]]
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      For(++t;u||v;swap(u,v)){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               u=st[pa[xnv]],v=xnv;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  while(b<=n_x&&st[b])++b;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(u)u=st[pa[u]];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(u==0)continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    set_match(xr,v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               match[b]=match[lca];
                                                                                                                                                                                                                                                                                                                                         match[u]=g[u][v].v;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               u=st[match[u]];
                                                                                                                                                                                                                                                                                                                                                                                                       edge e=g[n][v];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         set_match(u,v);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(!xnv)return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              flower[b].clear();
                                                                                                                                                                                                                                                   }else return pr;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                lab[b]=0,S[b]=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           static int t=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 if(b>n_x)++n_x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                set_st(b,b);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int b=n+1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          return 0;
                                                                                                                                                                                                                                                                                                                                                                             if(u>n){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for(;;){
```

```
for(int u=1;u<=n;++u)printf("%d ",match[u]);puts("");</pre>
                                                                                                                                                                                                                                                                                      printf("%lld\n", weight_blossom().first);
                                                                                                                                                                                                              scanf("%d%d%d", &u, &v, &w);
                    g[u][v]=edge(u,v,0);
                                                                                                                                                                                                                                        g[u][v].w=w.[u][n]g
for(int v=1;v<=n;++v)
                                                                                                                                                                   for(int i=0;i<m;++i){
                                                                                                                   scanf("%d%d", &n, &m);
                                                                                                                                           init_weight_graph();
                                                                                                                                                                                       int u, v, w;
                                                                                                                                                                                                                                                                                                                                        return 0;
                                                                      int main(){
                                                                                              int m
```

if(g[u][v].w>0&&st[u]!=st[v]){

强连通子图计数

```
int kpow(int a, int b) {int r=1; for(;b;b>>=1, a=mul(a,a)) {if(b&1)r=mul(r,a);}return r;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   int add(int a, int b) {if((a += b) >= P) a -= P; return a;}
int sub(int a, int b) {if((a -= b) < 0) a += P; return a;}
int mul(int a, int b) {return 111 * a * b % P;}</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int n, cnt[N], S, g[N], f[N], u, v, a[N], m, p[300];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               #define rep(i, a, b) for(int i=(a); i<(b); i++)
#define per(i, a, b) for(int i=(b)-1; i>=(a); i--)
#define sz(a) (int)a.size()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     #define dd(a) cout << #a << " = " << a << " "
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             #define de(a) cout << #a << " = " << a
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             #define all(a) a.begin(), a.end()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           typedef unsigned long long ull;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      typedef pair<int, int> pii;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           #define pw(x) (111<<(x)) #define endl "\n"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          #include<br/>cbits/stdc++.h>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         typedef vector<int> vi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      const int P = 1e9 + 7;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  const int N = 1 << 15;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              x = (x - 1) \& x;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           typedef long long 11;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        using namespace std;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 #define mp make_pair
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    #define pb push_back
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          // ooóooooonum±1%
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      typedef double db;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      #define se second
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      #define fi first
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           int get(int x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int res = 0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              while (x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   11.11
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if(st[x] == x \& \& slack[x] \& \& st[slack[x]]! = x \& \& e\_delta(g[slack[x]][x]) == 0)
                                                                                                                                                                                                                                                                                                                                                    else if(S[x]==0)d=min(d,e_delta(g[slack[x]][x])/2);
                             if(on_found_edge(g[u][v]))return true;
}else update_slack(u,st[v]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if(st[b]==b&&S[b]==1&&lab[b]==0)expand_blossom(b);
                                                                                                                                                                                                                                                                                                                    if(S[x]==-1)d=min(d,e_delta(g[slack[x]][x]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if(on_found_edge(g[slack[x]][x]))return true;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for(int u=0;u<=n;++u)st[u]=u,flower[u].clear();</pre>
                                                                                                                                                                                                                         if(st[b]==b&&S[b]==1)d=min(d,lab[b]/2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              else if(S[st[b]]==1)lab[b]—=d*2;
if(e_delta(g[u][v])==0){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   inline pair<long long,int> weight_blossom(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                }else if(S[st[u]]==1)lab[u]+=d;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return make_pair(tot_weight,n_matches);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(S[st[b]]==0)lab[b]+=d*2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             flower_from[u][v]=(u==v?u:0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         tot_weight+=g[u][match[u]].w;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             w_max=max(w_max,g[u][v].w);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                if(lab[u]<=d)return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for(int u=1;u<=n;++u)lab[u]=w_max;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   memset(match+1,0,sizeof(int)*n);
                                                                                                                                                                                                                                                                                       if(st[x]==x&&slack[x]){
                                                                                                                                                                                           for(int b=n+1; b<=n_x; ++b)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for(int b=n+1;b<=n_x;++b)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        for(int b=n+1; b<=n_x; ++b)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        while(matching())++n_matches;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if(match[u]&&match[u]<u)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  inline void init_weight_graph(){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          for(int x=1;x<=n_x;++x)</pre>
                                                                                                                                                                                                                                                            for(int x=1;x<=n_x;++x)
                                                                                                                                                                                                                                                                                                                                                                                                                  for(int u=1;u<=n;++u){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             for(int v=1;v<=n;++v){</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(S[st[u]]==0){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    long long tot_weight=0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     lab[u]-=d;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              if(st[b]==b){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  for(int u=1;u<=n;++u)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for(int u=1;u<=n;++u)</pre>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for(int u=1;u<=n;++u)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            q=queue<int>();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int n matches=0
                                                                                                                                                              int d=INF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      return false;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int w max=0;
```

```
for (int s = 0, u = sum; s <= k - r; ++s, u = mul(u, 1)) add(cur, mul(u, cof
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(r, 0, k-s+1) add(cof[r + 0 * i][s - i], mul(v, tmp[r][s]));
                                                                                                                                                                                                        rep(j, 1, i+1) C[i][j] = (C[i-1][j] + C[i-1][j-1]) % P;
                                                                               rep(s, 0, k-r) add(cof[s][r + 1 - i], mul(u, tmp[r][s]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        if (k1 == 0) { res = 1; rep(i, 0, k2) res = mul(res, b / c); } rep(i, 0, k) memset(cof[i]+1, 0, 4 * (k - i));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             rep(s, 1, k+1) rep(i, 1, s+1) {
   int u = mul(C[s][i], i & 1 ? 1 : P - 1);
   rep(r, 0, k-s+1) add(tmp[r][s - i], mul(u, cof[r][s]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int cur = 0, x = reduce(a, c), y = (reduce(b, c) + P) % P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              for (int i = 1, u = n; i <= r + 1; ++i, u = mul(u, n))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       add(sum, mul(u, mul(C[r + 1][i], B[r + 1 - i])));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 0, k) memcpy(tmp[i]+1, cof[i]+1, 4 * (k - i));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for (int i = 1, u = x; i <= k; ++i, u = mul(u, x))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     int u = mul(C[r+1][i], mul(B[i], inv[r+1]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 rep(i, 0, k) memset(cof[i]+1, 0, 4 * (k-i));
rep(r, 0, k) rep(i, 0, r+1) {
                                                                                                                                                                                                                                                                                                                       rep(j, 0, i) add(sum, mul(C[i + 1][j], B[j]));
B[i] = (1 + mul(P - sum, inv[i + 1])) % P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      int run(int n, int a, int b, int c, int K1, int K2) K = K1 + K2;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             \mathsf{rep}(i, 0, k) \; \mathsf{memset}(\mathsf{tmp[i]}, 0, 4 * (k-i));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       sum = mul(sum, inv[r + 1]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       int 1 = ((11)a * n + b) / c;
                                                                                                                                                                                                                                                                                                                                                                                                                                       inline void calc(int x, bool o) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                int v = mul(C[s][i], u);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 add(res, mul(sign, cur));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       calc(x, 1); calc(y, 0);
  < 0) a += b,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int res = 0, sign = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  n = 1; swap(a, c);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           cof[r][0] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   rep(r, 0, k+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(s, i, k+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  int sum = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (!a) break;
                                                                                                                                                                                                                                                                 rep(i, 0, K+1) {
int sum = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 cof[k1][k2] = 1;
if ((a %= b)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              while (1) {
                               return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            //\Sum_{X = 0} ^ {n} x ^ {k_1} {\left \lfloor \frac{ax + b}{c} \cdot \right \rfloor} ^ {k_2}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   static const int K = 10, P = 998244353; // e1+e2 <= K
int inv[K + 2], C[K + 2][K + 2], B[K + 1]; // Ŭuuuu 20
int cof[K + 1][K + 1], tmp[K + 1][K + 1], k;
inline void add(int &a, int b) { if ((a += b) >= P) a == P; }
inline int mul(int a, int b) { return 111 * a * b % P; }
int reduce(int &a, int b) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       for (int x = (i - 1) \& i; x > 0; x = (x - 1) \& i) { if (x & u) g[i] = sub(g[i], mul(f[x], g[i \ x]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           for (int x = i; x > 0; x = (x - 1) \& i) {
f[i] = sub(f[i], mul(g[x], p[cal(i ^ x, i)]));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i, 1, m+1) p[i] = mul(p[i-1], 2); rep(i, 1, S+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    //cout << setiosflags(ios::fixed);
//cout << setprecision(2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                         std::ios::sync_with_stdio(false);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 1, S+1) cnt[i] = get(i);
                                                                                                                                                                                                                                                                                                                                                                                                                                              freopen("a.in","r",stdin);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             扩展类欧几里得
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    g[i] = add(g[i], f[i])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      a[pw(u-1)] | = pw(v-1);
                                                                                                                                                                                                                                     res += cnt[a[t] & y];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              f[i] = p[cal(i, i)];
                                                                                                                    int cal(int x, int y) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           rep(i, 1, m+1) {
 cin >> u >> v;
                                                                                                                                                                                                            t = x & (-x);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         std::cin.tie(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 u = i \& (-i);
                                                                                                                                               int res = 0, t;
while (x) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  cin >> n >> m;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               S = pw(n) - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           cout << f[S];
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 namespace _lo {
                             return res;
                                                                                                                                                                                                                                                                                                                              return res;
                                                                                                                                                                                                                                                                     \times \wedge = t;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        p[0] = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                  int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               11.12
```

```
int add(int a, int b) {if((a += b) >= P) a -= P; return a;}
int sub(int a, int b) {if((a -= b) < 0) a += P; return a;}
int mul(int a, int b) {return 111 * a * b % P;}
int kpow(int a, int b) {int r=1;for(;b;b>>=1, a=mul(a,a)) {if(b&1)r=mul(r,a);}return r;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Ξ,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  Ś
                                                                                                                                                                                                                                                                       #define per(i, a, b) for(int i=(b)-1; i>=(a); i\longrightarrow
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       rep(i, 0, 2) rep(j, 0, 4) f[i][j].clear(); f[0][0][vi()] = 1; o = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int n, k, a[N], b[N], ok, p, ans, c[200], ans2,
                                                                                                                                                                                                                                             #define rep(i, a, b) for(int i=(a); i<(b); i++)
                                                                                                                                                                                                                                                                                                                                             #define de(a) cout << #a << " = " << a << end1
#define dd(a) cout << #a << " = " << a << " "
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               rep(t, 0, 4) f[o][t].clear();
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            //cout << setiosflags(ios::fixed);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            std::ios::sync_with_stdio(false);
#pragma GCC optimize("unroll—loops")
                                                                                                                                                                                                                                                                                                                                                                                                                  #define all(a) a.begin(), a.end()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               typedef unsigned long long ull;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 //cout << setprecision(2);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    freopen("a.in","r",stdin);
                                                                                                                                                                                                                                                                                                               #define sz(a) (int)a.size()
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  typedef pair<int, int> pii;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       cout << 1 << endl;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  #define lb(x) ((x) & -(x)) #define endl "\n"
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 while (cin >> n >> k) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  typedef vector<char> vi;
                                                                                                                                                                                                                                                                                                                                                                                                                                                     #define pw(x) (111<<(x))
                                     #include<br/>cbits/stdc++.h>
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  const int P = 1e9 + 7;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         rep(i, 1, n+1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          typedef long long 11;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  map<vi, int> f[2][4];
                                                                                                                                                                          #define mp make_pair
                                                                                                                                                                                                             #define pb push_back
                                                                       using namespace std;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            std::cin.tie(0);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    if (n == 1) {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       typedef double db;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         continue;
                                                                                                                                          #define se second
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  const int N = 10;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         0 ^= 1;
                                                                                                          #define fi first
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    bool o;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       res.g=add(res.g,add(111*(x<<1)*res.h%P,add(111*(y<<1)*res.f%P,add(111*ss(n)*pow(
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       res.g=dec(dec(dec(111*n*MMP*(M+1)MP,res.f),mul(h,2)),mul(f,2));\\
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          inline int ss(R int x) \{ return 111^*x^*(x+1) \%^*((x<<1)+1) \%^*inv6\%P; \}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       \times)%P, add(111*n*(n+1)%P*x%P*y%P,111*(n+1)*pow(y)%P))));
                                                                                                                                                                                                                                       // g= \sum \limits_{==} \{i=0\}^{\Lambda} \{i\eta_{}\{1\}\{1\}\{100r \ frac\{ai+b\}\{c\} \ rfloor\}^{\Lambda Z} \} // h= \sum \limits_{==} \{i=0\}^{\Lambda} \{h\}i \ lfloor \ frac\{ai+b\}\{c\} \ rfloor \}
                                                                                                                                                                                                                                                                                                                                                                                                                                               inline int dec(R int x, R int y) {return x-y<0?x-y+P:x-y;} inline int mul(R int x, R int y) {return 111*x*y-111*x*y/P*P;}
                                                                                                                                                                                                       // f = \sum_{i=0}^{n} |i=0|^{i=0} 
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       res.h=add(res.h,add(111*ss(n)*x%P,111*s(n)*y%P));
                                                                                                                                                                                                                                                                                                                                                                                                                  inline int add(R int x,R int y){return x+y>=P?x+y-P:x+y;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         res.f=add(res.f,add(111*s(n)*x%P,111*(n+1)*\sqrt{8}P));
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    res.h=111*inv2*dec(dec(111*M*n%P*(n+1)%P,g),f)%P;
                                                                                                                                                                                                                                                                                                                                                                               const int P=998244353,inv2=499122177,inv6=166374059;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     inline int pow(R int x){return 111*x*x%P;}
inline int s(R int x){return 111*x*(x+1)%P*inv2%P;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               for(;y;y>>=1,x=mul(x,x))if(y&1)res=mul(res,x);
     - sign;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    void get(int a, int b, int c, int n){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            res.g=111*pow(y)*(n+1)%P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int h=res.h, g=res.g, f=res.f;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       res.f=dec(111*n*M%P,res.f);
  sign = P
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            res.f=111*V*(n+1)%P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       struct node{int f, g, h; }res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            res.h=111*y*s(n)%P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            int ksm(R int x,R int y){
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          get(a%c,b%c,c,n);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               int M=(111*a*n+b)/c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       get(c, c-b-1, a, M-1);
  b = -b - 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          int x=a/c, y=b/c;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  if(a>=c||b>=c){}
                                                                                                                                                                                                                                                                                                                                                  #define R register
                                                                       return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    R int res=1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return res;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    return;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               eturn;
```

11.13 相邻差值小于等于 4 的排列数量

```
// k(k<=4)ooooooob/
// oooooooobkooke ...
#pragma GCC optimize("Ofast")
#pragma GCC target("sse2")
```

if (1 == m - 1 & & (t & 2)) continue;

if (1 == 0 && (t & 1)) continue;

m = sz(v.fi); vi = v.fi; rep(1, 0, m) {

for (auto v : f[!o][t]) {

rep(t, 0, 4) {

```
for (int msk = (i - 1) & i; msk >= 0; msk = (msk - 1) & i) {
   if (msk & lb(i)) dc[i] = add(dc[i], mul(c[msk], pw2[e[i ^ msk][i ^ msk] / 2]));
                                                                                                                                                                                                                                                                                                                                             int add(int a, int b) {if((a += b) >= P) a -= P; return a;}
int sub(int a, int b) {if((a -= b) < 0) a += P; return a;}
int mul(int a, int b) {return 111 * a * b % P;}
int kpow(int a, int b) {int r=1;for(;b;b>>=1,a=mul(a,a)) {if(b&1)r=mul(r,a);}return r;}
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  rep(j, 1, S+1) way[0][j] = 1;
rep(i, 1, S+1) rep(j, 1, S+1) {
   if ((j & i) || lb(j) > lb(i)) continue;
   way[i][j] = 0;
   for (int msk = i; msk >= 0; msk = (msk - 1) & i) {
        for (int msk = i; msk >= 0; msk = add(way[i][j], mul(mul(way[i ^ msk][j], c[msk]),
        if (msk & lb(i)) way[i][j] = add(way[i][j]j, mul(mul(way[i ^ msk][j], c[msk]),
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ⊢`
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    int n, S, e[N][N], way[N][N], a[100], t, x, y, dc[N], c[N], c2[N], c1[N], pw2[500],
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        S = pw(n) - 1;
rep(i, 0, S+1) rep(j, 0, S+1) {
    e[i][i] = 0;
    rep(k, 0, n) if (pw(k) & i) e[i][j] += __builtin_popcount(a[k] & j);
                            << a << end1
                                                   =
=
V
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          c[i] = sub(pw2[e[i][i] / 2], dc[i]);
                                                 #define dd(a) cout << #a << " = " << a
                        #define de(a) cout << #a << " = "
                                                                              #define all(a) a.begin(), a.end()
                                                                                                                                                                                                                                          typedef unsigned long long ull;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     if (msk == 0) break;
#define sz(a) (int)a.size()
                                                                                                                                                                                                                                                                 typedef pair<int, int> pii;
                                                                                                                                 #define lb(x) ((x) & -(x)) #define endl "\n"
                                                                                                      #define pw(x) (111<<(x))
                                                                                                                                                                                                                                                                                            typedef vector<int> vi;
                                                                                                                                                                                                                                                                                                                  const int P = 1e9 + 7;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                const int N = 1 << 10;
                                                                                                                                                                                                             typedef long long 11;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(i, 1, S+1) {
                                                                                                                                                                                       typedef double db;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        dc[i] = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   void solve1() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 void solve2() {
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             //dc _____2»j
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          //c1 ======µ¥j
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     //c ____j,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     ' n '
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            for (auto v : f[o][3]) if (sz(v.fi) == 2) ans = add(ans, v.se);
                                                                                                                                                                                                           rep(j, 0, 1) tmp.pb(a[j]); tmp.pb(0); tmp.pb(0);
rep(j, l, m) tmp.pb(a[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(i, 0, sz(tmp)) if (tmp[i]+1 > k) p = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            rep(i, 0, sz(tmp)) if (tmp[i]+1 > k) p = 0;
                                                                                                                                                                                                                                                                                                                      rep(i, 0, sz(tmp)) if (tmp[i]+1 > k) p =
                                                                          if (1 == 0 && (t & 1)) continue;
if (1 == m - 1 && (t & 2)) continue;
vi tmp = a; tmp[1] = 0; p = 1;
                                                                                                                                                                                                                                                                                                                                           if (1 == 0 && (t & 1)) continue;
if (1 == m && (t & 2)) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        rep(j, 1+2, m) tmp.pb(a[j]);
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               [f[o][t][tmp] += v.se) \% = P;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          rep(j, 0, 1) tmp.pb(a[j]);
                                                   rep(1, 0, m) { // oooooo•
                                                                                                                                                                                       if (!p) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      if (!p) continue;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       if (!p) continue
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    垃双联通子图计数
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       cout << ans << endl;
                                                                                                                                                                                                                                                                                                                                                                                                   vi tmp;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   p = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     vi tmp;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     p = 1;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ans = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            return 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        11.14
```

```
#define rep(i, a, b) for(int i=(a); i<(b); i++) #define per(i, a, b) for(int i=(b)-1; i>=(a); i--)
#include<bits/stdc++.h>
                                                                                                                                      #define pb push_back
                                                                                                            #define mp make_pair
                              using namespace std;
                                                      #define fi first
#define se second
```

υ

if (msk == 0) break;

[msk][j]);

```
Pp(1, 1, S+1) {
    cl[1] = 0;
    cl[1] = 0;
    for (int msk = (i - 1) & i; msk >= 0; msk = (msk - 1) & i) {
        if (msk & lb(i)) cl[i] = add(cl[i], mul(way[i ^ msk] [msk], c2[msk]));
        if (msk == 0) break;
    }
    c2[i] = sub(c[i], cl[i]);
}

int main() {
    freqpen("a.in", "r", stdin);
    std::ios::sync_with_stdio(false);
    std::ios::sync_with_stdio(false);
    //cout << setiosflags(ios::fixed);
    cin >> T;
    pw2[i] = 1;
    rep(i, 1, 300) pw2[i] = pw2[i-1] * 2 % P;
    rep(i, 0, n) a[i] = (pw(n) - 1) ^ pw(i);
    rep(i, 0, n) a[i] = (pw(n) - 1) ^ pw(i);
    rep(i, 0, n) a[i] = pw(u);
    a[u] ^ = pw(u);
    solvez();
    solvez();
    solvez();
    return 0;
}
```