VE281 — Data Structures

and Algorithms

Programming Assignment 2

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— UM-SJTU-JI (Fall 2021)

Notes

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• Submission: on JOJ (joj.sjtu.edu.cn)

1 Introduction

In this project, you are asked to implement a STL-like hash table data structure.

In the Standard Template Library, hash table is implemented as std::unordered_map[1], which is introduced in the C++11 standard. It is an associative container that contains key-value pairs with unique keys. Search, insertion, and removal of elements have average constant-time complexity. It is named "unordered" because there already exists an ordered data structure of key-value pairs based on RB-tree, std::map.

Internally, the elements are not sorted in any particular order, but organized into buckets. Which bucket an element is placed into depends entirely on the hash of its key. This allows fast access to individual elements, since once the hash is computed, it refers to the exact bucket the element is placed into.

The C++ standard does not mandates whether unordered_map use separate chaining or open addressing for collision resolution. Actually, different compilers use different policies: g++ uses separate chaining and LLVM/Clang uses open addressing. In this project, you're going to use separate chaining with std::forward_list[2], which is easier to implement and maintain.

You will also have a basic knowledge on iterators in C++: what are iterators and how they work. You can further try to use range-based for loops[3] (a feature introduced in C++11) to make use of iterators.

2 Programming Assignment

2.1 The HashTable Template

2.1.1 Overview

In the project starter code, we define a template class for you:

```
template<
typename Key, typename Value,
typename Hash = std::hash<Key>,
typename KeyEqual = std::equal_to<Key>
class HashTable;
```

Here Key and Value are the types of the key-value pair stored in the hash table. Hash is the type of a function object, whose instance returns the hash value of a key. The standard library defines a class template std::hash<T>, which can be used as the default. Similarly, KeyEqual is another type of a function object, whose instance returns whether two

Key objects are equal. It is used to determine which key-value pair should be returned when there is a hash collision, and it also help ensure the keys are unique in the hash table.

If you want to define your own hash function and key-equal function, you can refer to the following definitions:

2.1.2 Number of Buckets

Basically, you will use the "Hashing by Modulo" scheme. Suppose n is the number of buckets in the hash table, you should put a key into the i-th bucket where $i = hash(key) \mod n$. As we've discussed in the lecture, you should choose the hash table size n as a large prime number in ideal.

The number of buckets in your hash table should be dynamic (like a std::vector, but not exactly the same). A vector in C++ doubles its size when it is full (in most implementations), but this strategy may not be applied to a hash table because you should choose a prime number as the new size. Here we define the following strategy to choose a new hash table size before a rehash.

- First we define a list of prime numbers, each doubles its predecessor approximately. The list is taken from the g++ source code, and is provided with you as the file hash_prime.hpp.
- When a hash table is considered full (its load factor exceeds a preset maximum value), use the next prime as the new number of buckets and perform a rehash.

Furthermore, the maximum load factor value can also be changed in runtime; you can set a minimum number of buckets manually (i.e., to prevent rehashes if you've already know the data size) despite the load factor is small. **One important thing is that whenever the number of buckets is changed, you need to do a rehash.** You will fulfill all these requirements in the function findMinimumBucketSize. Please read its description carefully before implementing it. Though not mandatory, you are encouraged to use binary search to find the nearest prime. You can use the standard function std::lower_bound to perform the binary search so that you don't need to implement it by yourself.

2.1.3 Internal Data Structures

We've already defined the internal data structures for you in this project. The HashNode is a key-value pair. The HashNodeList is a single directional linked list in each bucket, here we use std::forward_list to implement it. The HashTableData is a std::vector of these lists, representing the buckets in the hash table.

```
class HashTable {
public:
typedef std::pair<const Key, Value> HashNode;
typedef std::forward_list<HashNode> HashNodeList;
```

```
typedef std::vector<HashNodeList> HashTableData;
protected:
HashTableData buckets;
size_t tableSize;
double maxLoadFactor;
Hash hash;
KeyEqual keyEqual;
}
```

tableSize means the number of key-value pairs in the hash table. You can also add your own private / protected variables (or attributes) after these if necessary, but mostly the defined ones are enough. Here we use the protected keyword so that your HashTable class can be further inherited and overwritten for testing.

2.1.4 Iterators

We're introducing iterators in this section. First of all, why you need to use iterators in this project? Supposing you want to find a key-value pair in the hash table, and then you may erase it from the hash table if it satisfies certain conditions. There are three implementations to achieved this:

- (1) Use the *find* method to find a key-value pair, use the *erase* method to erase it.
- (2) Use the *find* method to find a pointer to a key-value pair, use the *erase* method which accepts a pointer to erase it.
- (3) Use the *find* method to find an iterator to a key-value pair, use the *erase* method which accepts an iterator to erase it.

In the first implementation, two lookups of the key is performed.

In the second implementation, only one lookup of the key is performed. However, the user can access the internal data structure of the hash table with the pointer, which is dangerous and violates the rule of packaging in Object-Oriented Programming.

In the third implementation, only one lookup of the key is performed as well, and the iterator only provides a restricted access to the key-value pair, so it's a better solution.

In this project, we've already provided you with a completed iterator. You are going to use the iterator in the implementation of other methods in the hash table.

```
class lterator {
private:
    typedef typename HashTableData::iterator VectorIterator;

typedef typename HashNodeList::iterator ListIterator;

const HashTable &hashTable;

VectorIterator bucketIt;

ListIterator listItBefore;

bool endFlag = false;

}
```

Here bucketIt means which bucket the iterator is in, listItBefore means the iterator pointer that points "before" the key-value pair in the linked list.

We'll give a simple explanation of the "before" iterator. If you want to erase a node in a linked list, you need to link the previous node and the next node. However, the list is single directional, so that you can't get the previous node in $\mathcal{O}(1)$ time unless you've saved it. If you always use a "before" iterator, the deletion of node will be possible, and you can access the current node by "next" of the "before" iterator. This is a built-in functionality of the std::forward_list[2] class. The class also provides a before_begin method, which is different from other STL containers. You can check the documentation for more information.

Since the list is single directional (in order to save memory), the iterator only supports single directional iteration. The operator ++ is already overloaded for you. The iterator doesn't have a const version, you can implement it if you're interested in iterators, but it's not mandatory. You can see the detail implementation of the iterator in the starter code.

We also defines a variable

```
typename <u>HashTableData</u>::iterator firstBucketIt;
```

in the hash table. It provides an $\mathcal{O}(1)$ access to the first key-value pair in the hash table. You need to update its value whenever an insert, erase or rehash operation is applied to the hash table.

What's more, the hash table supports basic iteration and range-for loops[3] with the help of iterators and two methods: begin and end. More specifically, with the C++98 standard you can iterate the hash table by:

```
for (auto it = hashTable.begin(); it != hashTable.end(); ++it) {
    std::cout << it->first << " " << it->second << std::endl;
}</pre>
```

With C++11, you can use the following as an alternative:

```
for (auto &item : hashTable) {
    std::cout << item.first << " " << item.second << std::endl;
}</pre>
```

With C++17, you can even do it in a more graceful way (similar to python and some other modern languages):

```
for (auto &[key, value] : hashTable) {
    std::cout << key << " " << value << std::endl;
}</pre>
```

The order of the output of the above code is arbitrary and is dependent on implementation. We'll not test the internal order of the key-value pairs in your hash table (returned by iteration), since they're meant to be "unordered".

2.2 Comparison of Hash Table and Linked List

We also recommend you to study the performances of hash table and linked list. Basically, you will compare these classes:

- HashTable
- std::unordered_map
- std::list or std::forward_list (their performances should be similar)

You can design your own comparison metric. For example, you can insert n key-value pairs into all these classes, then run k find, update, insert or erase operations. In a linked list, you can use linear search, it should be very simple to implement these operations with std::list or std::forward_list.

No report is required, but you are recommended to study their differences for your better understanding in terms of hash table.

2.2.1 Hints

- The performance of programs on Windows is usually not stable, so you should do the experiments on a Unix based system.
- You may want to write another program to do this study.
- You can use the C++11 pseudo-random number generation library to generate more randomized numbers (instead of using std::rand).
- You can use the C++11 chrono library to get more accurate runtime of functions than std::clock.
- (Optional) You can use GNU Perf (only available on Linux) to find the bottleneck of your implementation.
- Although the major factor that affects the runtime is the size of the input array, however, the runtime for an algorithm may also weakly depend on the detailed input array. Thus, for each size, you should generate a number of arrays of that size and obtain the mean runtime on all these arrays. Also, for fair comparison, the same set of arrays should be applied to all the data structures.
- You should try at least 5 representative sizes.

3 Implementation Requirements and Restrictions

3.1 Requirements

- You must make sure that your code compiles successfully on a Linux operating system with g++ and the options
 -std=c++1z -Wconversion -Wall -Werror -Wextra -pedantic.
- You should not change the definitions of the functions and variables, as well as the public or protected keywords for them in hashtable.hpp.
- You can define helper functions and new variables, don't forget to mark them as private or protected.
- You should only hand in one file hashtable.hpp.
- You can use any header file defined in the C++17 standard. You can use cppreference as a reference.

You only need to implement the methods (functions) marked with "TODO" in the file hashtable.hpp. Here is a list of the methods (functions):

- Copy Constructor and Assignment Constructor
- findMinimumBucketSize
- find
- insert
- erase
- operator[]
- rehash

Please refer to the descriptions of these functions in the starter code.

3.2 Memory Leak

Hint: You're not going to use any dynamic memory allocation functions (new, malloc, etc.) directly in this project, thus it's not possible to have memory leak in your program. This section is only for your reference.

You may not leak memory in any way. To help you see if you are leaking memory, you may wish to call valgrind, which can tell whether you have any memory leaks. (You need to install valgrind first if your system does not have this program.) The command to check memory leak is:

```
valgrind --leak-check=full <COMMAND>
```

You should replace <COMMAND> with the actual command you use to issue the program under testing. For example, if you want to check whether running program

```
./main < input.txt

causes memory leak, then <COMMAND> should be "./main < input.txt". Thus, the command will be

valgrind --leak-check=full ./main < input.txt
```

4 Grading

Your program will be graded along five criteria:

4.1 Functional Correctness

Functional Correctness is determined by running a variety of test cases against your program, checking your solution using our automatic testing program.

4.2 Implementation Constraints

We will grade Implementation Constraints to see if you have met all of the implementation requirements and restrictions. In this project, we will also check whether your program has memory leak. For those programs that behave correctly but have memory leaks, we will deduct some points.

4.3 General Style

General Style refers to the ease with which TAs can read and understand your program, and the cleanliness and elegance of your code. Part of your grade will also be determined by the performance of your algorithm.

4.4 Performance

We will test your program with some large test cases. If your program is not able to finish within a reasonable amount of time, or it uses too much memory, you will lose the performance score for those test cases.

5 Acknowledgement

The programming assignment is co-authored by Yihao Liu, an alumni of JI and the chief architect of JOJ.

References

- [1] std::unordered map cppreference: https://en.cppreference.com/w/cpp/container/unordered_map
- [2] std::forward list cppreference : https://en.cppreference.com/w/cpp/container/forward_list
- [3] Range-based for loop cppreference: https://en.cppreference.com/w/cpp/language/range-for

Appendix

```
hash prime.hpp
 1 // adopted from
     → /usr/include/c++/10.2.0/ext/pb_ds/detail/resize_policy/hash_prime_size_policy_imp.hpp
    #include <utility>
    namespace HashPrime {
        enum {
            num_distinct_sizes_32_bit = 30,
            num_distinct_sizes_64_bit = 62,
            num_distinct_sizes = sizeof(std::size_t) != 8 ?
                                  num_distinct_sizes_32_bit : num_distinct_sizes_64_bit,
10
        };
11
12
13
        // Originally taken from the SGI implementation; acknowledged in the docs.
        // Further modified (for 64 bits) from tr1's hashtable.
14
        static constexpr std::size_t g_a_sizes[num_distinct_sizes] = {
                                            5ul,
                /* 1
                                            11ul,
                          */
17
                /* 2
                                            23ul,
                          */
                /* 3
                                            47ul,
                          */
                /* 4
                          */
                                            97ul,
20
                /* 5
                                            199ul,
                /* 6
                                            409ul,
                          */
                /* 7
                                            823ul,
23
                /* 8
                                            1741ul,
                /* 9
                                            3469ul,
                          */
                /* 10
                                            6949ul,
26
                /* 11
                          */
                                            14033ul,
27
                /* 12
                                            28411ul,
                          */
                /* 13
                                            57557ul,
                                            116731ul,
                /* 14
                          */
                /* 15
                                            236897ul,
                          */
31
                /* 16
                                            480881ul,
                /* 17
                                            976369ul,
                          */
33
                /* 18
                                            1982627ul,
                          */
                /* 19
                          */
                                            4026031ul,
                /* 20
                          */
                                            8175383ul,
                                            16601593ul,
                /* 21
                          */
37
                /* 22
                                            33712729ul,
                          */
                /* 23
                          */
                                            68460391ul,
                                            139022417ul,
                /* 24
                          */
                /* 25
                          */
                                            282312799ul,
                                            573292817ul,
                /* 26
                          */
                /* 27
                                            1164186217ul,
```

```
/* 28
                                          2364114217ul,
               /* 29
                         */
                                          4294967291ul,
45
                         */ (std::size_t) 8589934583ull,
               /* 30
                         */ (std::size_t) 17179869143ull,
               /* 31
               /* 32
                         */ (std::size_t) 34359738337ull,
                         */ (std::size_t) 68719476731ull,
               /* 33
               /* 34
                         */ (std::size_t) 137438953447ull,
               /* 35
                         */ (std::size_t) 274877906899ull,
51
                         */ (std::size_t) 549755813881ull,
               /* 36
               /* 37
                         */ (std::size_t) 1099511627689ull,
53
               /* 38
                         */ (std::size_t) 2199023255531ull,
54
                         */ (std::size_t) 4398046511093ull,
               /* 39
               /* 40
                         */ (std::size_t) 8796093022151ull,
               /* 41
                         */ (std::size_t) 17592186044399ull,
57
                         */ (std::size_t) 35184372088777ull,
               /* 42
58
                         */ (std::size_t) 70368744177643ull,
               /* 43
               /* 44
                         */ (std::size t) 140737488355213ull,
60
                         */ (std::size_t) 281474976710597ull,
               /* 45
61
                         */ (std::size_t) 562949953421231ull,
               /* 46
               /* 47
                         */ (std::size_t) 1125899906842597ull,
63
               /* 48
                         */ (std::size_t) 2251799813685119ull,
64
                         */ (std::size_t) 4503599627370449ull,
               /* 49
               /* 50
                         */ (std::size_t) 9007199254740881ull,
               /* 51
                         */ (std::size_t) 18014398509481951ull,
67
               /* 52
                         */ (std::size_t) 36028797018963913ull,
                         */ (std::size_t) 72057594037927931ull,
               /* 53
                         */ (std::size_t) 144115188075855859ull,
               /* 54
70
               /* 55
                         */ (std::size_t) 288230376151711717ull,
                         */ (std::size_t) 576460752303423433ull,
               /* 56
                         */ (std::size_t) 1152921504606846883ull,
               /* 57
73
               /* 58
                         */ (std::size_t) 2305843009213693951ull,
               /* 59
                         */ (std::size_t) 4611686018427387847ull,
               /* 60
                         */ (std::size_t) 9223372036854775783ull,
76
               /* 61
                         */ (std::size_t) 18446744073709551557ull,
       };
79
  }
80
```

hashtable.hpp

```
#include "hash prime.hpp"
   #include <exception>
   #include <functional>
  #include <vector>
  #include <forward_list>
8 /**
   * The Hashtable class
    \star The time complexity of functions are based on n and k
    * n is the size of the hashtable
    * k is the length of Key
    * @tparam Key
                          key type
    * @tparam Value
                          data type
14
                          function object, return the hash value of a key
    * @tparam Hash
    * @tparam KeyEqual function object, return whether two keys are the same
    */
17
   template<
           typename Key, typename Value,
           typename Hash = std::hash<Key>,
20
           typename KeyEqual = std::equal_to<Key>
21
22
   class HashTable {
23
   public:
24
       typedef std::pair<const Key, Value> HashNode;
25
       typedef std::forward_list<HashNode> HashNodeList;
       typedef std::vector<HashNodeList> HashTableData;
27
28
       /**
        * A single directional iterator for the hashtable
        * ! DO NOT NEED TO MODIFY THIS !
31
        */
32
       class Iterator {
33
       private:
34
           typedef typename HashTableData::iterator VectorIterator;
           typedef typename HashNodeList::iterator ListIterator;
37
           const HashTable *hashTable;
38
           VectorIterator bucketIt; // an iterator of the buckets
           ListIterator listItBefore; // a before iterator of the list, here we use
            → "before" for quick erase and insert
           bool endFlag = false;  // whether it is an end iterator
           /**
43
            * Increment the iterator
            * Time complexity: Amortized O(1)
```

```
void increment() {
47
               if (bucketIt == hashTable->buckets.end()) {
                   endFlag = true;
                   return;
               }
               auto newListItBefore = listItBefore;
               ++newListItBefore;
               if (newListItBefore != bucketIt->end()) {
                   if (++newListItBefore != bucketIt->end()) {
                       // use the next element in the current forward_list
                       ++listItBefore;
                       return;
                   }
               }
               while (++bucketIt != hashTable->buckets.end()) {
                   if (!bucketIt->empty()) {
62
                       // use the first element in a new forward_list
63
                       listItBefore = bucketIt->before_begin();
                       return;
65
                   }
               }
               endFlag = true;
           }
69
           explicit Iterator(HashTable *hashTable) : hashTable(hashTable) {
               bucketIt = hashTable->buckets.begin();
               listItBefore = bucketIt->before_begin();
               endFlag = bucketIt == hashTable->buckets.end();
           }
           Iterator(HashTable *hashTable, VectorIterator vectorIt, ListIterator
            hashTable(hashTable), bucketIt(vectorIt), listItBefore(listItBefore) {
               endFlag = bucketIt == hashTable->buckets.end();
           }
80
81
       public:
82
           friend class HashTable;
83
84
           Iterator() = delete;
           Iterator(const Iterator &) = default;
           Iterator &operator=(const Iterator &) = default;
90
           Iterator & operator++() {
```

```
increment();
                 return *this;
93
             }
             Iterator operator++(int) {
                 Iterator temp = *this;
                 increment();
                 return temp;
             }
101
             bool operator==(const Iterator &that) const {
102
                 if (endFlag && that.endFlag) return true;
103
                 if (bucketIt != that.bucketIt) return false;
104
                 return listItBefore == that.listItBefore;
105
             }
106
107
             bool operator!=(const Iterator &that) const {
108
                 if (endFlag && that.endFlag) return false;
109
                 if (bucketIt != that.bucketIt) return true;
                 return listItBefore != that.listItBefore;
111
             }
112
             HashNode *operator->() {
114
                 auto listIt = listItBefore;
115
                 ++listIt;
                 return &(*listIt);
117
             }
118
119
             HashNode &operator*() {
120
                 auto listIt = listItBefore;
121
                 ++listIt;
122
                 return *listIt;
124
        };
125
    protected:
                                                                                      // DO NOT USE
127
     → private HERE!
         static constexpr double DEFAULT_LOAD_FACTOR = 0.5;
                                                                                      // default
128
         → maximum load factor is 0.5
         static constexpr size_t DEFAULT_BUCKET_SIZE = HashPrime::g_a_sizes[0]; // default
129
         → number of buckets is 5
130
        HashTableData buckets;
                                                                                      // buckets,
131

→ of singly linked lists

         typename HashTableData::iterator firstBucketIt;
                                                                                     // help get
         \hookrightarrow begin iterator in O(1) time
133
```

```
size_t tableSize;
                                                                                      // number of
134
         \rightarrow elements
         double maxLoadFactor;
                                                                                      // maximum
         → load factor
         Hash hash;
                                                                                      // hash
136

→ function instance

         KeyEqual keyEqual;
                                                                                      // key equal
137

→ function instance

138
139
         * Time Complexity: O(k)
140
          * @param key
141
          * @param bucketSize
142
          * @return the hash value of key with a new bucket size
143
         */
144
         inline size_t hashKey(const Key &key, size_t bucketSize) const {
             return hash(key) % bucketSize;
146
         }
147
         /**
149
         * Time Complexity: O(k)
150
          * @param key
          * @return the hash value of key with current bucket size
152
         */
153
         inline size_t hashKey(const Key &key) const {
             return hash(key) % buckets.size();
155
         }
156
157
         /**
158
          * Find the minimum bucket size for the hashtable
159
          * The minimum bucket size must satisfy all of the following requirements:
160
          \star - It is not less than (i.e. greater or equal to) the parameter bucketSize
          * - It is greater than floor(tableSize / maxLoadFactor)
162
          * - It is a (prime) number defined in HashPrime (hash_prime.hpp)
163
          * - It is minimum if satisfying all other requirements
          * Time Complexity: O(1)
165
          * @throw std::range_error if no such bucket size can be found
166
          * @param bucketSize lower bound of the new number of buckets
167
          */
168
         size_t findMinimumBucketSize(size_t bucketSize) const {
169
            // TODO: implement this function
170
171
172
         // TODO: define your helper functions here if necessary
173
175
    public:
176
```

```
HashTable() :
177
                 buckets(DEFAULT_BUCKET_SIZE), tableSize(0),
178

→ maxLoadFactor(DEFAULT_LOAD_FACTOR),
                 hash(Hash()), keyEqual(KeyEqual()) {
179
             firstBucketIt = buckets.end();
180
         }
182
         explicit HashTable(size_t bucketSize) :
183
                 tableSize(0), maxLoadFactor(DEFAULT_LOAD_FACTOR),
                 hash(Hash()), keyEqual(KeyEqual()) {
185
             bucketSize = findMinimumBucketSize(bucketSize);
186
             buckets.resize(bucketSize);
187
             firstBucketIt = buckets.end();
188
        }
189
190
         HashTable(const HashTable &that) {
191
             // TODO: implement this function
192
193
         }
         HashTable &operator=(const HashTable &that) {
195
             // TODO: implement this function
196
         };
198
         ~HashTable() = default;
199
         Iterator begin() {
201
             if (firstBucketIt != buckets.end()) {
202
                 return Iterator(this, firstBucketIt, firstBucketIt->before_begin());
203
204
             }
             return end();
205
         }
206
         Iterator end() {
208
             return Iterator(this, buckets.end(), buckets.begin()->before_begin());
209
         }
211
212
         * Find whether the key exists in the hashtable
213
          * Time Complexity: Amortized O(k)
214
          * @param key
215
          * @return whether the key exists in the hashtable
216
217
         bool contains(const Key &key) {
218
             return find(key) != end();
219
         }
220
221
222
```

```
* Find the value in hashtable by key
223
         * If the key exists, iterator points to the corresponding value, and it.endFlag =
224
        false
         * Otherwise, iterator points to the place that the key were to be inserted, and
225
        it.endFlag = true
         * Time Complexity: Amortized O(k)
226
         * @param key
227
         * @return the iterator of the value
228
         */
229
        Iterator find(const Key &key) {
230
            // TODO: implement this function
231
232
        }
233
        /**
234
         * Insert value into the hashtable according to an iterator returned by find
235
         \star the function can be only be called if no other write actions are done to the
        hashtable after the find
         * If the key already exists, overwrite its value
237
         * firstBucketIt should be updated
         * If load factor exceeds maximum value, rehash the hashtable
239
         * Time Complexity: O(k)
240
         * @param it an iterator returned by find
         * @param key
242
         * @param value
243
         * @return whether insertion took place (return false if the key already exists)
245
        bool insert(const Iterator &it, const Key &key, const Value &value) {
246
            // TODO: implement this function
247
        }
249
250
         * Insert <key, value> into the hashtable
          * If the key already exists, overwrite its value
252
         * firstBucketIt should be updated
253
         * If load factor exceeds maximum value, rehash the hashtable
          * Time Complexity: Amortized O(k)
255
         * @param key
256
         * @param value
257
         * @return whether insertion took place (return false if the key already exists)
258
259
        bool insert(const Key &key, const Value &value) {
260
            // TODO: implement this function
261
        }
262
263
        /**
         * Erase the key if it exists in the hashtable, otherwise, do nothing
265
         * DO NOT rehash in this function
```

```
* firstBucketIt should be updated
267
         * Time Complexity: Amortized O(k)
268
         * @param key
269
         * @return whether the key exists
270
         */
271
        bool erase(const Key &key) {
            // TODO: implement this function
273
        }
274
275
276
         * Erase the key at the input iterator
277
         * If the input iterator is the end iterator, do nothing and return the input
278
        iterator directly
         * firstBucketIt should be updated
279
         * Time Complexity: O(1)
280
         * @param it
281
         * @return the iterator after the input iterator before the erase
282
         */
283
        Iterator erase(const Iterator &it) {
            // TODO: implement this function
285
        }
286
        /**
288
         * Get the reference of value by key in the hashtable
289
         * If the key doesn't exist, create it first (use default constructor of Value)
         * firstBucketIt should be updated
291
          * If load factor exceeds maximum value, rehash the hashtable
292
         * Time Complexity: Amortized O(k)
293
         * @param key
         * @return reference of value
295
         */
296
        Value &operator[](const Key &key) {
             // TODO: implement this function
298
        }
299
        /**
301
         * Rehash the hashtable according to the (hinted) number of buckets
302
         * The bucket size after rehash need not be same as the parameter bucketSize
303
          * Instead, findMinimumBucketSize is called to get the correct number
304
         * firstBucketIt should be updated
305
         * Do nothing if the bucketSize doesn't change
306
          * Time Complexity: O(nk)
307
         * @param bucketSize lower bound of the new number of buckets
308
309
        void rehash(size_t bucketSize) {
310
             bucketSize = findMinimumBucketSize(bucketSize);
311
             if (bucketSize == buckets.size()) return;
312
```

```
// TODO: implement this function
313
        }
314
316
         * @return the number of elements in the hashtable
317
         */
         size_t size() const { return tableSize; }
319
320
        /**
321
322
         * @return the number of buckets in the hashtable
323
         size_t bucketSize() const { return buckets.size(); }
324
325
        /**
326
         * @return the current load factor of the hashtable
327
328
         double loadFactor() const { return (double) tableSize / (double) buckets.size(); }
329
330
         * @return the maximum load factor of the hashtable
332
333
         double getMaxLoadFactor() const { return maxLoadFactor; }
335
        /**
336
         * Set the max load factor
337
          * @throw std::range_error if the load factor is too small
338
          * @param loadFactor
339
340
         void setMaxLoadFactor(double loadFactor) {
341
             if (loadFactor <= 1e-9) {</pre>
342
                 throw std::range_error("invalid load factor!");
343
             }
             maxLoadFactor = loadFactor;
345
             rehash(buckets.size());
346
        }
348
   };
349
```