

Special Topics in the Industrial Applications of Machine Learning

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Chapter 4: Basic ML Algorithms

Machine Learning is a field of study that gives computers the capability to learn from data and improve performance without being explicitly programmed.

By the end of this chapter, students should be able to:

- Understand the main categories of ML algorithms.
- Learn the principles behind training and optimization of models.
- Implement and evaluate basic and commonly used ML algorithms.
- Compare models on industrial datasets using appropriate evaluation metrics.
- Recognize the strengths, limitations, and suitable applications of each algorithm in industrial contexts.

Chapter 4: Basic ML Algorithms

- Section 1: ML Algorithms & Training Basics Overview of ML types and core training concepts.
- Section 2: Regression Models
 Predicting continuous outputs from industrial process data.
- Section 3: Classification Models
 Assigning discrete labels for fault detection and decision tasks.
- Section 4: Unsupervised Learning
 Discovering hidden patterns and structure without labeled data.

Introduction to ML Algorithms

An ML algorithm is a procedure that learns patterns from data to make predictions or decisions.

General workflow:



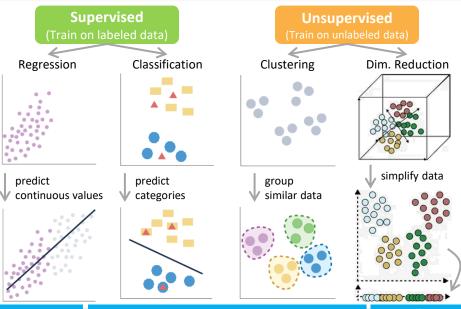
Algorithms differ in:

- The kind of data they need (labeled or unlabeled)
- How they express the relation between inputs and outputs
- How they learn and adjust their parameters

Examples of industrial applications:

- Forecasting energy demand (Regression)
 - Detecting faults in machines (Classification)
 - Clustering consumers by load profiles (Clustering)
 - Reducing sensor data for monitoring (Dimensionality Reduction)

Categories of ML Algorithm



What Does "Training" Mean?

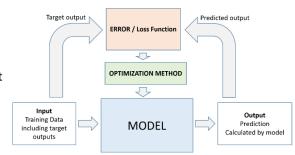
Training in machine learning means adjusting model parameters to minimize a **loss function**.

The model prediction is $\hat{y} = f_{\theta}(x)$, and we aim to solve:

$$\theta^* = \arg mean_\theta \ \mathcal{L}(y, \hat{y})$$

where

- θ: model parameters (e.g., weights, bias)
- f(x): input features
- \hat{y} : model's predicted output
- L: loss function measuring prediction error



Optimization algorithms (like Gradient Descent) update parameters step-by-step toward lower loss.

Key Terminology

Meaning (Concise Definition)

One parameter update step

Term

Batch Size

teration

Industrial ML

Model	A mathematical function (e.g., $\hat{y}=f_{\theta}(x)$) that maps inputs to outputs; its parameters θ are learned from data
Feature (Input)	Measurable variable(s) describing each sample (e.g., temperature, voltage)
Target / Label (Output)	True value or category we want the model to predict
Sample / Example	One data point: a pair (x_i,y_i)
Training	Adjusting model parameters to minimize error on training data
Validation	Testing model performance on unseen data to tune hyperparameters
Prediction / Inference	Using the trained model to estimate outputs for new inputs
Learning Rate	Controls how big each parameter update step is during training
Epoch	One complete pass through the entire training dataset

Number of samples processed before updating the model parameters

Common Loss Functions

Category	Loss Function	Formula	Typical Use / Behavior
ssion	Mean Squared Error (MSE)	$L = \frac{1}{N} \sum_{i=1}^{N} (y_i - \hat{y}_i)^2$	Linear regression; penalizes large errors strongly
Regression	Mean Absolute Error (MAE)	$L = \frac{1}{N} \sum_{i=1}^{N} y_i - \hat{y}_i $	Robust to outliers; linear penalty
Classification	Binary Cross- Entropy (Log Loss)	$\sum_{i=1}^{N} [y_i \log \hat{y}_i + (1 - y_i) \log(1 - \hat{y}_i)]$	Binary classification; compares probabilities
Classi	Categorical Cross- Entropy	$L = \frac{1}{N} \sum_{i=1}^{N} \sum_{c} y_{i,c} \log \hat{y}_{i,c}$	Multi-class (softmax) classification
arization	$L_{total} = L_{data} + \lambda L_{reg}$	Ridge (L2): $L_{reg} = \sum_i w_i^2$	Penalizes large weights; reduces variance
Regulari	L_{data} : Any loss L_{reg} : Penalty Term	Lasso (L1): $L_{reg} = \sum_i w_i $	Promotes sparsity; implicit feature selection

The Gradient Descent Algorithm

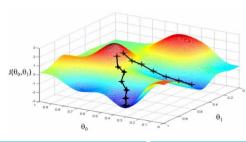
Gradient Descent (GD) is an iterative algorithm that minimizes a loss function $L(\theta)$ by updating parameters **opposite to the gradient**.

Parameter vector $\theta = [w_1, w_2, \dots, w_n, b]$ is updated as:

$$\theta \leftarrow \theta - \eta \nabla_{\theta} L(\theta)$$

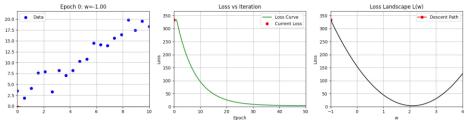
- η : the learning rate
- $\nabla_{\theta} L(\theta) = \left[\frac{\partial L}{\partial w_1}, \frac{\partial L}{\partial w_2}, \cdots, \frac{\partial L}{\partial w_n}, \frac{\partial L}{\partial b}\right]$: gradient of the loss
- 1D model: Single parameter moves downhill along the loss parabola.
- $w := w \alpha * \frac{\partial L}{\partial w}$ $(\alpha = learning rate)$ $gradient(\frac{\delta L}{\partial w})$

2D model: Parameters descend the 3D loss bowl toward the minimum.

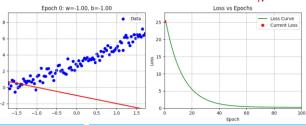


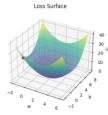
Example: GD on Linear Regression

1D Linear Regression (Only w): $L(w) = \frac{1}{N} \sum_{i=1}^{N} (y_i - wx_i)^2$



2D Linear Regression (w and b): $L(w) = \frac{1}{N} \sum_{i=1}^{N} (y_i - (wx_i + b))^2$





Underfitting and Overfitting

Underfitting

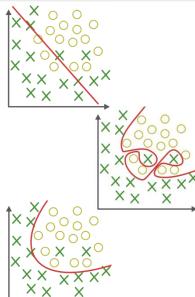
- Model is too simple → misses real patterns
- Poor on both training & test data
- Example: Forecasting demand using only daily averages, ignoring seasons

Overfitting

- Model is too complex → memorizes data, not patterns
- Excellent on training but poor on new data
- Example: Forecasting demand by following every random fluctuation, failing next year

Appropriate Fitting

- Model captures key patterns without memorizing noise
- Generalizes well to new conditions (new equipment, customers, or weather)



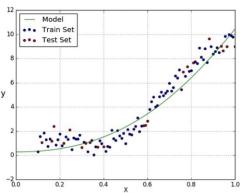
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Introduction to Regression Models

What is regression?

- Regression models estimate a continuous output variable y from one or more inputs x₁, x₂, ··· , x_n.
- Goal: Learn a function f(X) that best approximates the relationship between inputs and outputs.
- Used widely in **industrial systems** for prediction, control, and monitoring.



Examples:

- Predict energy consumption from temperature, humidity, and time.
- Estimate machine wear from vibration, current, and operation time.
- Forecast process output quality from sensor readings.

Main idea: Find parameters that minimize prediction error (e.g., MSE, MAE).

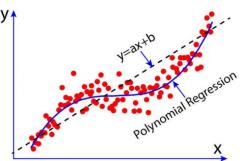
Linear & Polynomial Regression

Linear regression models the relationship between the input features x_1, x_2, \cdots, x_n and a target variable y as a **linear combination** of inputs:

$$\hat{y} = w_0 + w_1 x_1 + w_2 x_2 + \dots + w_n x_n$$

Polynomial regression extends linear regression by including crossterms and powers of the inputs:

$$\hat{y} = w_0 + w_1 x_1 + w_2 x_2 + w_3 x_1^2 + w_4 x_2^2 + w_5 x_1 x_2 \cdots$$



Polynomial regression is often implemented by first expanding input features and then applying ordinary linear regression to the transformed features.

Regularized forms are derived by adding the penalty terms (e.g., L1 and L2) to the MSE loss.

Tree-Based Regression

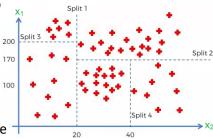
Basic Idea: Partition the data space into regions with similar target values, and predict y as the average in the region R_m containing the input:

$$\hat{y} = \bar{y}_m = \frac{1}{|R_m|} \sum_{i \in R_m} y_i$$

Data Splitting: Splits are chosen to minimize the Residual Sum of Squares (RSS):

$$RSS = \sum_{j=1}^{J} \sum_{i \in R_j} \left(y_i - \hat{y}_{R_j} \right)$$

Tree Construction: At each node, the algorithm selects the feature and threshold that minimize error, recursively splitting data until stopping criteria (e.g., max depth or min samples per leaf) are met.





Ensemble Tree Models

Random Forest (Bagging)

- Trains many trees on bootstrap samples (data with replacement).
- Each split considers a random subset of features.
- Prediction = average of all tree outputs.
- Reduces variance and overfitting.

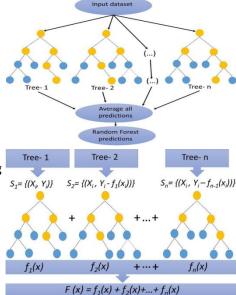
Gradient Boosting

 Builds trees sequentially, each predicting the residuals of the previous model.

$$\hat{y}^{(m)}(x) = \hat{y}^{(m-1)}(x) + \gamma_m h_m(x)$$

where $\hat{y}^{(m)}(x)$ is the new tree and γ_m is the learning rate.

- Gradually corrects errors, improving accuracy.
- Requires tuning to prevent overfitting.



K-Nearest Neighbors (KNN) Regression

Idea:

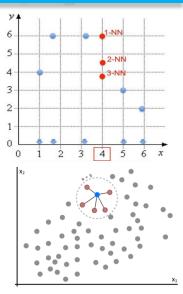
 Predict the output for a new input by averaging the targets of its k nearest neighbors.

$$\hat{y}(x) = \frac{1}{k} \sum_{i \in \mathcal{N}_k(x)} y$$

 $\mathcal{N}_k(x)$ is the set of the k closest samples to x.

Key Points:

- Non-parametric: No model is trained; predictions are based directly on data.
- **Distance metric:** Usually Euclidean; defines the neighborhood.
- Effect of k:
 - Small $k \rightarrow$ flexible but sensitive to noise.
 - Large k → smoother but may underfit.
- Works best in low-dimensional spaces.



Note: Regression can also be performed using Neural Networks — introduced in the next chapter.

Evaluation & Diagnostics

Common metrics:

• MAE =
$$\frac{1}{n} \sum_{i=1}^{n} |y_i - \hat{y}_i|$$

· robust to outliers

•
$$MAPE = \frac{1}{n} \sum_{i=1}^{n} \frac{|y_i - \hat{y}_i|}{y_i}$$

unstable near zero

•
$$RMSE = \sqrt{\frac{1}{n}\sum_{i=1}^{n}(y_i - \hat{y}_i)^2}$$

· penalizes large errors



• Coefficient of Determination:
$$R^2 = 1 - \frac{\sum_i (y_i - \hat{y}_i)^2}{\sum_i (y_i - \bar{y}_i)^2}$$

· fraction of variance explained

Diagnostics & Industrial Notes:

- Check predicted vs. actual (identity line), residual and learning curves
- Select metrics reflecting operational or business costs
- Use k-fold CV; rolling/blocked CV for temporal data

Regression - Summary



Linear Regression

- Fast, interpretable baseline; assumes linearity.
- Struggles with nonlinearity and multicollinearity.



Polynomial Regression

- Extends linear models to nonlinear patterns.
- Risk of overfitting with high-degree terms.



Decision Tree Regression

- Captures nonlinearities and interactions.
- Easy to visualize, but prone to overfitting.



Random Forest (Bagging)

- Reduces variance via averaging multiple trees.
- Robust, less interpretable.



Gradient Boosting

- Sequentially corrects prior errors; very accurate.
- Needs careful tuning (learning rate, number of trees).



KNN Regression

- Simple, non-parametric; adapts to local data.
- Sensitive to noise and scaling; slow on large data.

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Introduction to Classification

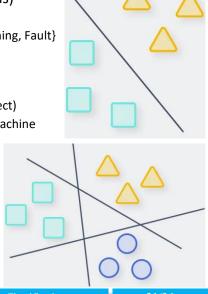
- **Goal:** Predict **discrete categories** (labels) instead of continuous values.
 - Example: Machine status → {Normal, Warning, Fault}
 - Example: Product quality → {Pass, Fail}

Types of Classification:

- Binary: Two classes (e.g., defect vs. no defect)
- Multi-class: More than two classes (e.g., machine states, fault location)

Core Concepts:

- Decision boundaries separate classes in feature space.
- Loss functions differ from regression (e.g., Cross-Entropy for classification).
- Evaluation metrics: accuracy, precision, recall, F1-score (detailed later).



Logistic Regression

• Extends Linear Regression to **binary classification**, by predicting the probability of Class 1 (vs. Class 0) via the sigmoid function:

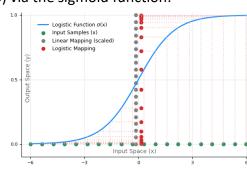
$$\hat{y} = \sigma(\mathbf{w}^T \mathbf{x} + b) = \frac{1}{1 + e^{(\mathbf{w}^T \mathbf{x} + b)}}$$

• Decision rule:

$$\hat{y} \ge 0.5 \Rightarrow Class1$$
, $\hat{y} < 0.5 \Rightarrow Class0$

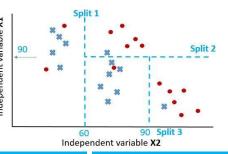
- Use Binary Cross-Entropy Loss.
- Key Points (Industrial Note):
 - \bullet Highly interpretable useful when understanding feature impact matters.
 - Works well for linearly separable data or as a baseline classifier.
- For multi-class problems use softmax to predict probabilities:

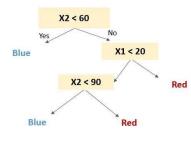
$$\hat{y}_k = \frac{e^{z_k}}{\sum_{i=1}^{K} e^{z_i}}$$
 Decision: class with **highest probability**



Tree-Based Classifiers

- Basic idea: Split feature space; assign majority class in each leaf.
- Key points:
 - Handles nonlinear boundaries.
 - · Works with mixed feature types.
 - Interpretable visualize splits and leaf classes.
 - Useful for baseline classifiers or when interpretability is required.
 - Ensemble Tree Models (Random Forest, Gradient Boosting) improve accuracy and reduce overfitting.





K-Nearest Neighbors (KNN) Classifiers

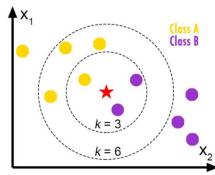
- Classifies a sample by the majority label among its k nearest neighbors in feature space.
- Simple and intuitive; effective for small or low-dimensional datasets but **computationally heavy** for large ones.
- Sensitive to data scaling and the choice of k.

Distance measures:

- Euclidean: $d(p,q) = \sqrt{\sum_i (p_i q_i)^2}$
- Manhattan: $d(p,q) = \sqrt{\sum_i |p_i q_i|}$
- Other metrics (e.g., cosine, Minkowski) can be used depending on data characteristics.

Choosing K:

- Small $K \rightarrow$ captures local detail but noisy
- large K → smoother decision boundary, less sensitive to outliers



Naïve Bayes Classifier

Based on Bayes' theorem:

$$P(C_k|x) \propto P(x|C_k)P(C_k)$$

ullet predict the class \mathcal{C}_k with the highest posterior probability

- Probabilities are estimated as:
 - Feature independence (Naïve): $P(x|C_k) = \prod_i P(x_i|C_k)$
 - $P(C_k)$: frequency of each class in the training data
 - $P(x_i|\mathcal{C}_k)$: estimated from data distribution of feature x_i under class \mathcal{C}_k
- Industrial example (fault detection):

Feature	Value	P(x _i Normal)	P(x _i Faulty)
Temperature > 60 °C	Yes	0.2	0.8
Vibration > 1.0 m/s ²	Yes	0.1	0.7
Prior P(C ₁), P(C ₂)	-	0.6	0.4

Common variants:

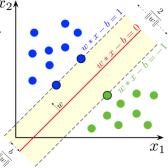
- Gaussian NB continuous features (e.g., temperature, vibration, voltage levels)
- Multinomial NB discrete/count features (e.g., number of sensor triggers)
- Bernoulli NB binary features (e.g., alarm on/off, switch status)

Support Vector Machines (SVM)

- Concept: Find the hyperplane that maximizes the margin between two classes.
- Decision function: $f(x) = w^T x + b$
- Optimization problem:

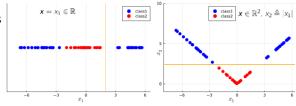
$$\min_{\mathbf{w},b} \frac{1}{2} \|\mathbf{w}\|^2 \quad s.t. \quad y_i(\mathbf{w}^T \mathbf{x}_i + b) \ge 1$$

 Only support vectors (points on the margins) affect the solution



• Extensions:

- Soft-Margin SVM: Permits some misclassification for noisy data
- Kernel SVM: Maps inputs to higher dimensions for non-linear separation



• SVR (Support Vector Regression): An SVM variant for regression tasks

Evaluation Metrics



Actual Positive Negative False Positive (FP) True Positive (TP) 15 False Negative (FN) True Negative (TN)

Confusion Matrix

 $Precision = \frac{TP}{TP + FP} = 0.833 \quad \left| Accuracy = \frac{TP + TN}{TP + TN + FP + FN} = 0.800 \right|$

$$TN + FP$$
 $FP = 0.100$

Specificity = $\frac{TN}{TN + FP}$ = 0.813 | Recall (Sens., TPR) = $\frac{TP}{TP + FN}$ = 0.789

$$FPR = \frac{FP}{FP + TN} = 0.188$$

$$F1 = \frac{2 * Precision*Recall}{Precision*Recall} = 0.810$$

- Accuracy: Overall correct predictions
- Precision: True positives among predicted positives
- Recall (Sensitivity): True positives among actual positives
- •F1-Score: Balance of Precision & Recall

ROC/AUC

Predicted

ROC: Plot of TPR vs. FPR for different thresholds.

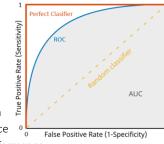
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AUC: Area under ROC

Multi-Class Evaluation

Compute metrics for each class separately (treat one as "positive," others as "negative"), and then average:

- Macro: Equal weight to all classes good for balanced data
- Weighted: Weighted by class frequency handles imbalance
- Micro: Aggregates TP, FP, FN globally reflects overall performance



Classification - Summary



Logistic Regression

- Fast, interpretable baseline for linear separations
- Struggles with nonlinear boundaries



Decision Tree Classifier

- Captures nonlinearities and interactions
- Easy to visualize, but prone to overfitting



KNN (k-Nearest Neighbors)

- Simple, non-parametric; adapts to data shape
- Sensitive to scaling and k choice



Naive Bayes

- · Probabilistic; fast and effective for text or event data
- Assumes feature independence



Support Vector Machine (SVM)

- · Maximizes margin; strong for high-dimensional data
- Kernel trick handles nonlinear cases; slower on large sets



Evaluation Metrics

- · Accuracy, Precision, Recall, F1, ROC-AUC
- Macro/Micro averaging for multi-class tasks
- ▶ **Note:** NNs also perform classification covered in *Deep Learning* chapter.

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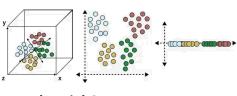
Introduction to Unsupervised Learning

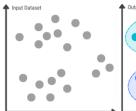
Definition:

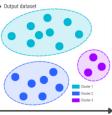
Learning from **unlabeled data** to **discover hidden structures or patterns** without predefined outputs.

Main Approaches:

- **Clustering:** Groups similar samples (e.g., *k*-Means).
- Dim. Reduction: Compresses data while preserving important information (e.g., PCA).







Industrial Context:

Industrial systems often produce large volumes of **unlabeled sensor data**. Unsupervised methods support:

- Identifying operating modes of machines.
- Anomaly detection in production systems.
- Data compression for real-time monitoring.

K-Means: Concept

• Idea:

k-Means partitions data into k groups so that samples within each group are **similar**, and groups are **distinct** from one another.

· Key Intuition:

Each cluster is represented by its center (centroid) — data points are assigned to the nearest centroid, and centroids shift to the mean of their assigned points.

• Algorithm Steps:

- 1. Choose number of clusters (k).
- 2. Initialize k centroids (randomly or with k-Means++).
- 3. Assign each sample to the nearest centroid.
- 4. Update centroids as the mean of assigned samples.
- 5. Repeat steps 3–4 until assignments stop changing.

• Distance Measure (default):

$$d(x,\mu_i) = ||x - \mu_i||^2$$

This quantifies the closeness of data point to cluster center

K-Means: Visualization & Practical Notes

k-means clustering (
$$k = 4$$
, #data = 300)

music: "fast talkin" by K. MacLeod incompetech.com

Other distance measures:

- o Manhattan (L1): $|x \mu_i|$
- o Cosine distance: $1 \frac{x \cdot \mu_i}{\|x\| \|\mu_i\|}$

• Stopping Criteria:

- Cluster assignments stop changing
- Centroid shifts below a small threshold
- Maximum iteration limit reached

- Choosing Number of Clusters (k):
 - o **Elbow Method:** Plot total variance vs. *k*; look for "bend".
- Initialization Strategy:
 - k-Means++ improves stability and convergence speed.
 - \circ Run algorithm multiple times with different seeds \rightarrow choose lowest loss.

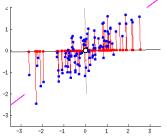
PCA: Intuition and Goal

Objective:

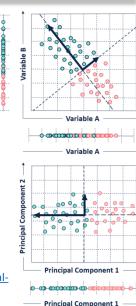
Reduce high-dimensional data to a few principal components capturing main patterns and variations.

Key Ideas:

- Industrial data often have correlated variables (e.g., temperatures, currents).
- PCA finds uncorrelated axes capturing maximum variance, ordered by importance.
- Projecting onto top components enables simpler visualization and analysis.



Explore interactive GIFs at: https://setosa.io/ev/principalcomponent-analysis/



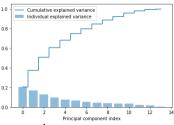
PCA: Procedure & Key Notes

Procedure:

- Center/standardize data.
- 2. Compute covariance: $\Sigma = \frac{1}{n-1}X^TX$
- 3. Eigen-decomposition: $\Sigma v_i = v_i \lambda_i \rightarrow v_i = PC \ direction, \lambda_i = variance$
- 4. Sort PCs by λ_i , select top k.
- 5. Project data: $Z = XV_k$.

Notes & Practical Tips:

- PCs = linear combinations of original features.
- For nonlinear patterns, use kernel PCA or t-SNE.
- PCs are orthogonal (uncorrelated).
- PCA rotates axes to align with directions of maximum variance.
- Keep only top PCs to reduce dimensionality and filter noise.
- Industrial Monitoring:
 - · Sudden jumps in PC scores indicate faults.
 - Slow drift may indicate sensor aging or process changes.
 - Applications: sensor monitoring, fault detection, visualization, predictive maintenance.



Ensemble Methods

Idea:

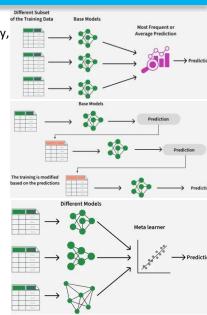
Combine multiple models to improve accuracy, stability, and generalization.

• Techniques:

- Bagging: parallel models on bootstrap samples → aggregate predictions.
 Good for high-variance learners (trees).
- Boosting: sequential models correct previous errors.
 Best with simple, fast learners.
- Stacking: combine diverse models via a meta-learner.
 Leverages complementary strengths.

Industrial Benefits:

- Outperforms single models on highdimensional data.
- Robust to noise and overfitting.
- Strong baseline before deep learning.



Summary & Next Steps

Summary:

- **Supervised vs. Unsupervised:** understand task type and data labels.
- Regression & Classification: key models, loss functions, and evaluation metrics.
- Unsupervised Learning: K-Means for clustering; PCA for dimensionality reduction and process monitoring.
- Ensemble Methods: bagging, boosting, stacking improve accuracy, robustness, and generalization.
- Neural Networks: versatile models for supervised and unsupervised tasks; foundation for deep learning.

Next Steps:

Deep Learning Models: handling complex and unstructured industrial data

