



MINISTÉRIO DA CIÊNCIA E TECNOLOGIA
INSTITUTO NACIONAL DE PESQUISAS ESPACIAIS

Assimilação de Dados por Redes Neurais Artificiais

Haroldo F. de Campos Velho – INPE

Helaine C. M. Furtado - UFOPA

Juliana A. Anochi – INPE

Roberto P. Souto – LNCC

Vinicius A. Albuquerque - UFRJ

Mini-curso: Assimilação de Dados por Redes Neurais

■ O que é "assimilação de dados"?

- O porque da necessidade e breve histórico

■ Métodos de assimilação de dados

- *Nudging* e Métodos Variacionais
- Filtro de Kalman e filtro de Kalman por conjunto

■ Redes neurais: breve descrição

- Redes neurais: MLP, FBR, Deep Learning
- Redes neurais para assimilação de dados
- Modelo de circulação oceânica 2D

■ Aplicações

- Modelos de baixa ordem: Lorenz-63, *shallow water* 1D e 2D
- Processamento paralelo para assimilação com redes neurais
- Modelos atmosféricos 3D: WRF (regional), SPEED e FSU (globais)

Mini-curso: Assimilação de Dados por Redes Neurais

■ O que é "assimilação de dados"?

- O porque da necessidade e breve histórico

■ Métodos de assimilação de dados

- *Nudging* e Métodos Variacionais
- Filtro de Kalman e filtro de Kalman por conjunto

■ Redes neurais: breve descrição

- Redes neurais: MLP, FBR, Deep Learning
- Redes neurais para assimilação de dados
- Modelo de circulação oceânica 2D

■ Aplicações

- Modelos de baixa ordem: Lorenz-63, *shallow water* 1D e 2D
- Processamento paralelo para assimilação com redes neurais
- Modelos atmosféricos 3D: WRF (regional), SPEED e FSU (globais)

Assimilação de dados por redes neurais

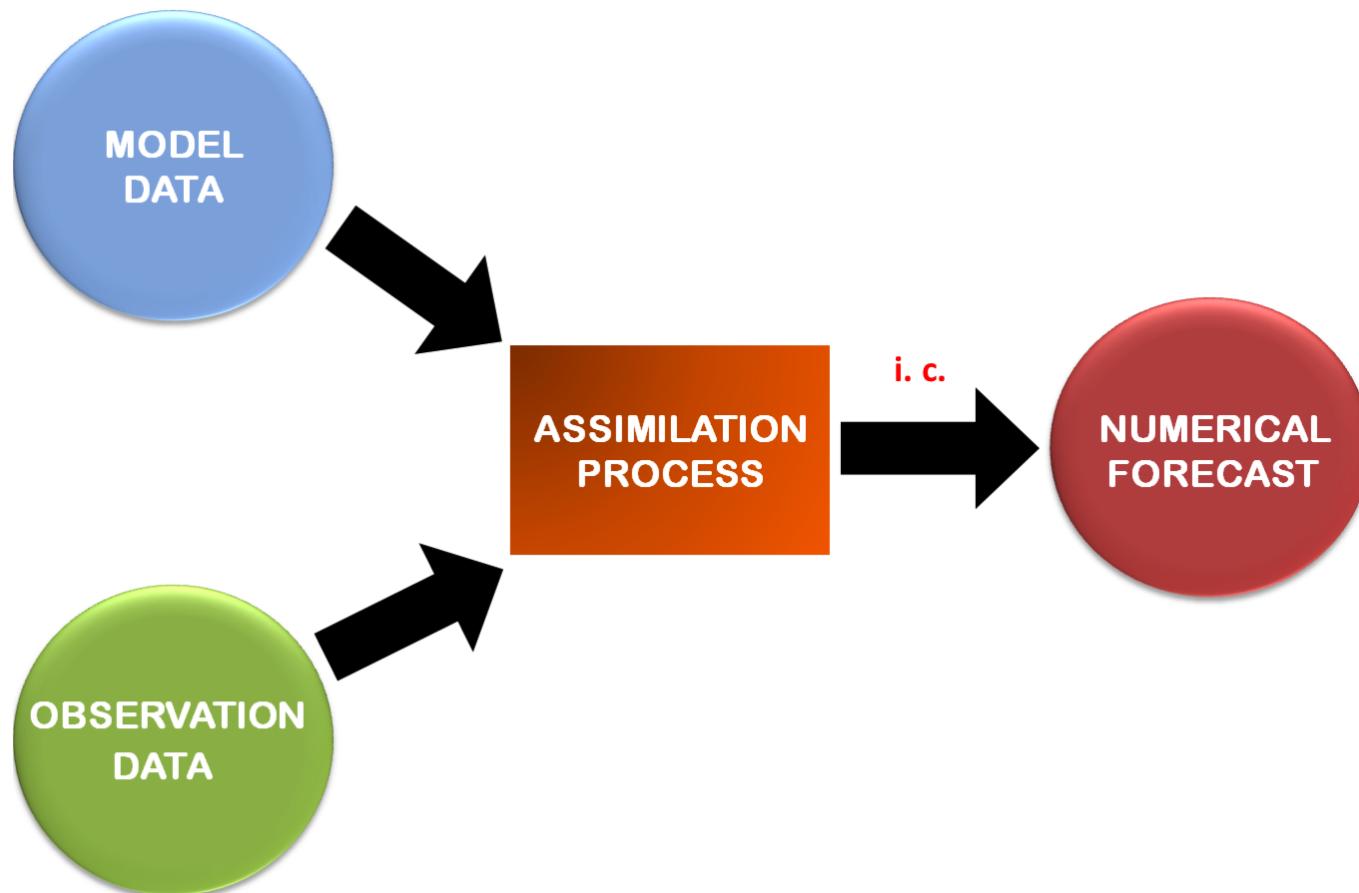
■ Instrutores:

- Haroldo F. de Campos Velho – INPE
- Helaine C. M. Furtado - UFOPA
- Juliana A. Anochi – INPE
- Roberto P. Souto – LNCC
- Gerônimo Lemos – INPE
- Marcelo Paiva – INPE

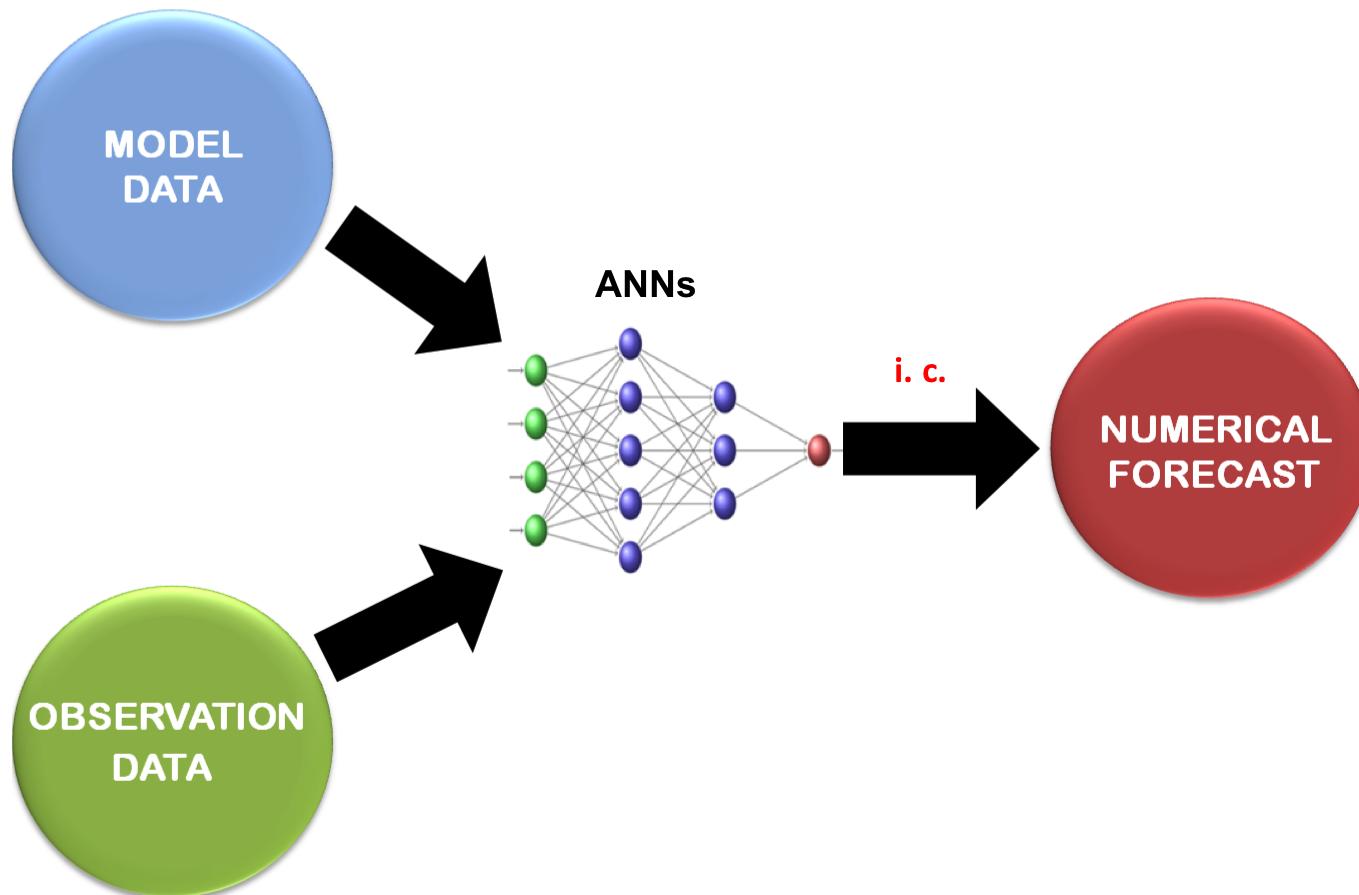
Data assimilation – concept



Data assimilation – concept



Data assimilation – concept



Data assimilation (DA) – methods

- Newtonian relaxation (nudging)
- Statistical (“optimal”) interpolation
- Kalman filter
- Variational method: 3D and 4D
- New methods for data assimilation:
 - Ensemble Kalman filter
 - Hybrid method: variational + EnKF
 - Particle filter
 - **Artificial neural networks**

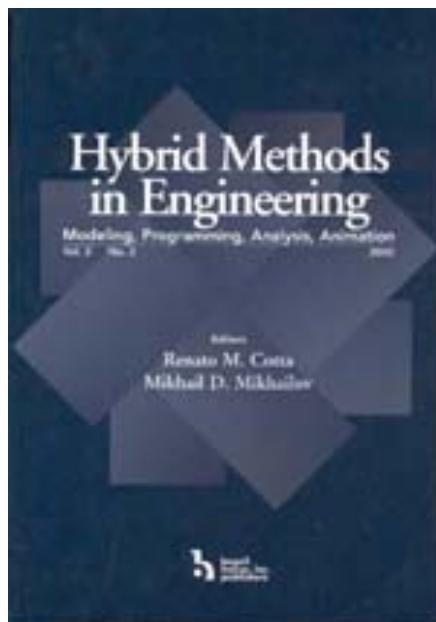
Data assimilation – first application

Data Assimilation Using an Adaptative Kalman Filter and Laplace Transform

A.G. Nowosad^a (DCM)

A. Rios Neto^b

H.F. de Campos Velho^a (LAC)



^a Instituto Nacional de Pesquisas Espaciais (INPE)
Caixa Postal 515
12201-970 – São José dos Campos (SP), BRAZIL,
E-mail: alex@met.inpe.br - haroldo@lac.inpe.br

^b Instituto de Pesquisa e Desenvolvimento (IP&D)
Universidade do Vale do Paraíba (UNIVAP)
Av. Shishima Hifumi, 2.911 - Urbanova
12245-720 - São José dos Campos (SP), BRAZIL
E-mail: atair@univap.br

Hybrid Methods in Engineering: (2000) 2(3): 291-310

Data assimilation – NN emulating KF

- NN emulating Kalman filter: Lorenz's system

Revista Brasileira de Meteorologia, v.20, n.3, 411-420, 2005

**REDES NEURAIS RECORRENTES TREINADAS COM CORRELAÇÃO CRUZADA
APLICADAS A ASSIMILAÇÃO DE DADOS EM DINÂMICA NÃO-LINEAR**

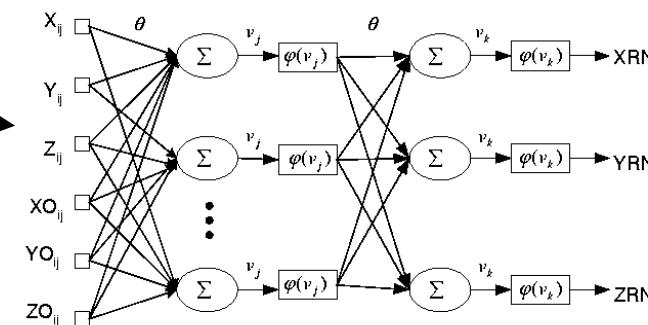
FABRÍCIO PEREIRA HÄRTER e HAROLDO FRAGA DE CAMPOS VELHO



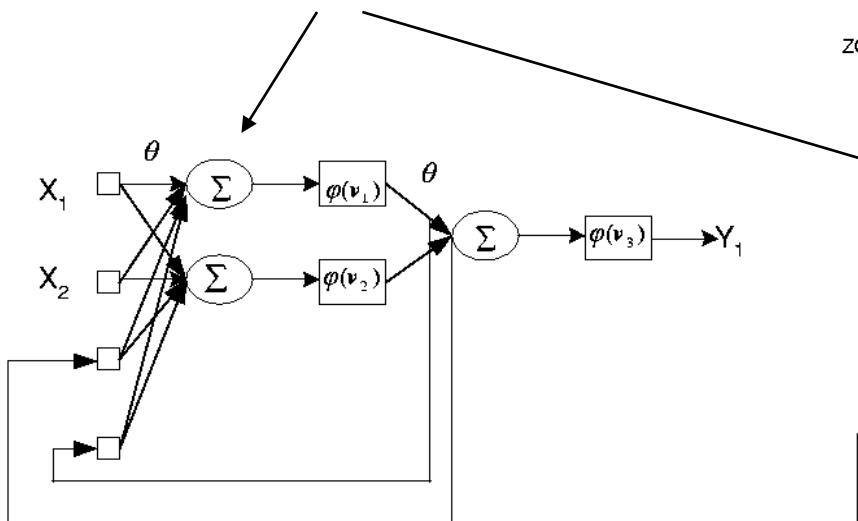
Data assimilation – NN emulating KF

■ NN emulating Kalman filter: Lorenz's system

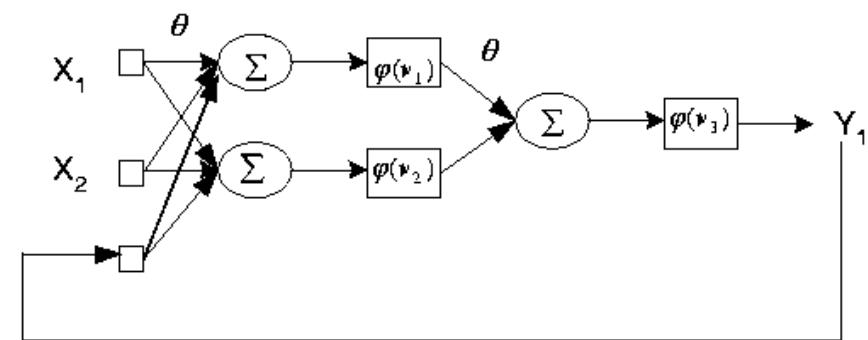
Standard NN



Recurrent NNs:



Elman-NN



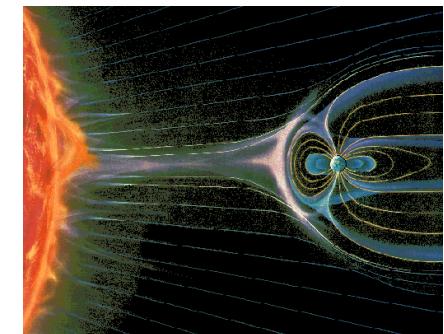
Jordan-NN



Data assimilation – NN emulating KF

- NN emulating Kalman filter: Space Weather

Interaction: Sun-Earth

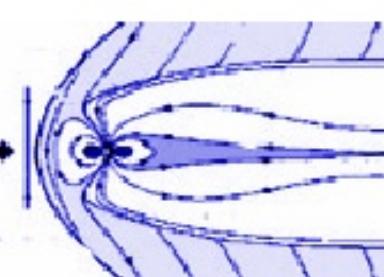
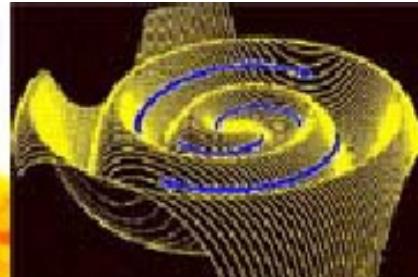
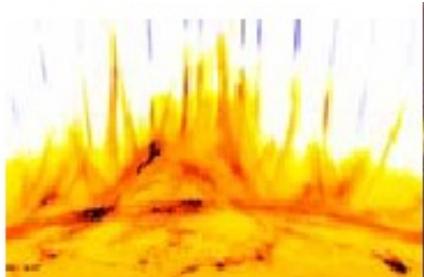


Solar
Activity

Propagation

Impact on
magnetosphere

ionosphere



Data assimilation – NN emulating KF

■ NN emulating Kalman filter: Space Weather

Journal of Atmospheric and Solar-Terrestrial Physics 70 (2008) 1243–1250



Review article

Neural networks in auroral data assimilation

Fabrício P. Härter^{a,b,c,*}, Haroldo F. de Campos Velho^{a,b,c},
Erico L. Rempel^{a,b,c}, Abraham C.-L. Chian^{a,b,c}

^a University of Waterloo (UofW), Waterloo, ON, Canada N2L 3G1

^b National Institute for Space Research (INPE), São José dos Campos, SP, 12227-010, Brazil

^c Instituto Tecnológico de Aeronáutica, Praça Marechal Eduardo Gomes, 50, CEP 12228-900, São José dos Campos, Brazil

ARTICLE INFO

Article history:

Received 14 November 2006

Received in revised form

14 February 2008

Accepted 23 March 2008

Available online 18 April 2008

Keywords:

Auroral radio emissions

Nonlinear dynamics

Chaos

Data assimilation

Kalman filter

Neural networks

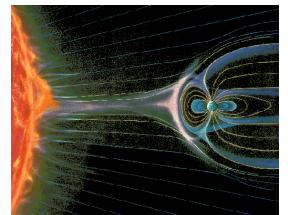
ABSTRACT

Data assimilation is an essential step for improving space weather forecasting by means of a weighted combination between observational data and data from a mathematical model. In the present work data assimilation methods based on Kalman filter (KF) and artificial neural networks are applied to a three-wave model of auroral radio emissions. A novel data assimilation method is presented, whereby a multilayer perceptron neural network is trained to emulate a KF for data assimilation by using cross-validation. The results obtained render support for the use of neural networks as an assimilation technique for space weather prediction.

© 2008 Elsevier Ltd. All rights reserved.

Data assimilation – NN emulating KF

- NN emulating Kalman filter: Space Weather



Equations: three-waves coupled

Interaction: Sun-Earth

$$dA_L/d\tau = \nu_L A_L + A_W A_A$$

$$dA_W/d\tau = \nu_W A_W - A_L A_A^*$$

$$dA_A/d\tau = (i\delta + \nu_A)A_A - A_L A_W^*$$

$$\nu_L = 1$$

$$\nu_L = \nu_L = -\nu$$

$$\delta = 2$$

$$\tau \equiv \kappa(z - vt)$$

Data assimilation – NN emulating KF

■ NN emulating Kalman filter: Shallow Water 1D



Available online at www.sciencedirect.com



Applied Mathematical Modelling 32 (2008) 2621–2633

APPLIED
MATHEMATICAL
MODELLING

www.elsevier.com/locate/apm

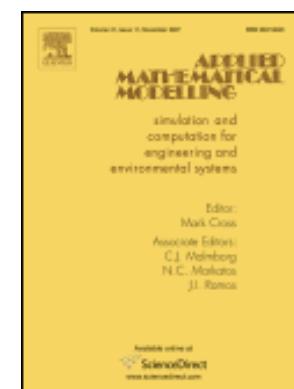
New approach to applying neural network in nonlinear
dynamic model

Fabrício P. Härter *, Haroldo Fraga de Campos Velho

Instituto Nacional de Pesquisas Espaciais, Laboratório Associado de Computação e Matemática Aplicada, São José dos Campos, SP, Brazil

Received 2 January 2007; received in revised form 31 July 2007; accepted 17 September 2007

Available online 30 October 2007



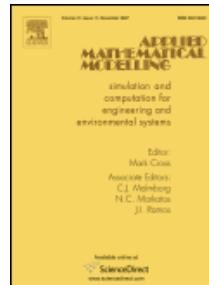
Data assimilation – NN emulating KF

- NN emulating Kalman filter: Shallow Water 1D

$$\frac{\partial \zeta}{\partial t} + R_o \frac{\partial(u\zeta)}{\partial x} + \delta + R_\beta v = 0$$

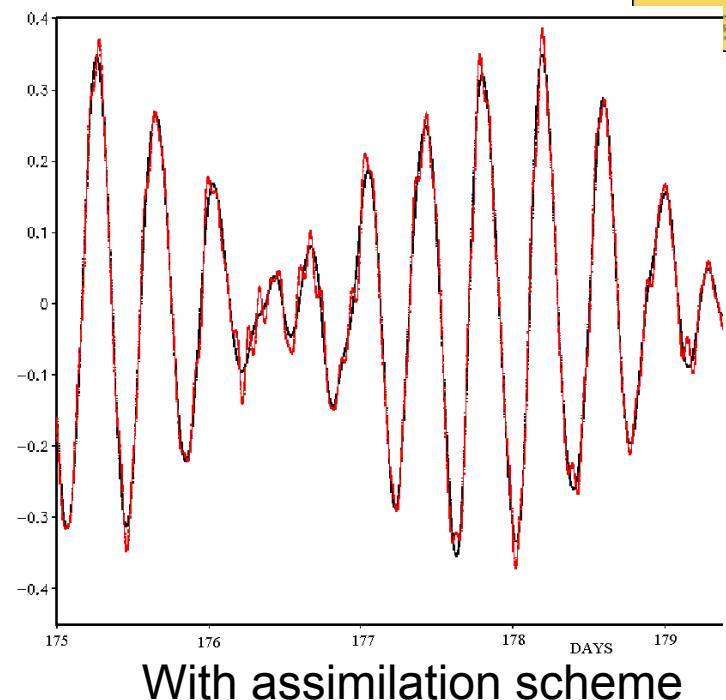
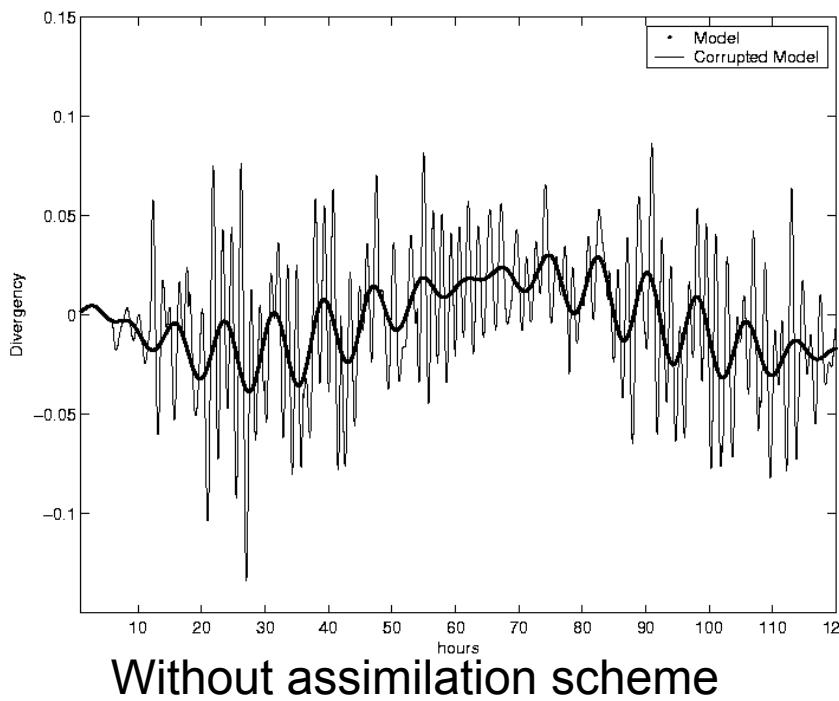
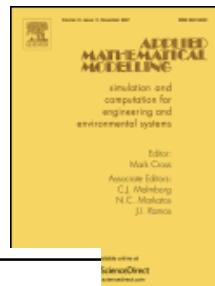
$$\frac{\partial \delta}{\partial t} + R_o \frac{\partial(u\delta)}{\partial x} - \zeta + R_\beta u + \frac{\partial^2 \phi}{\partial x^2} = 0$$

$$\frac{\partial \phi}{\partial t} + R_o \frac{\partial(u\phi)}{\partial x} - R_o u_0 v + R_F \delta = 0$$



Data assimilation – NN emulating KF

■ NN emulating Kalman filter: Shallow Water 1D



New feature: assimilation by ANN at each grid point, reducing the complexity of the algorithm.
Example – 3 variables + 3 observations + 3 forecasts = 3 assimilated data for each grid point.

Data assimilation – NN emulating KF

- NN emulating Kalman filter: Linear wave 1D



Springer Nature is making Coronavirus research free. [View research](#) | [View latest news](#) | [Sign up for updates](#)



[Pure and Applied Geophysics](#)

pp 1–21 | [Cite as](#)

Two Geoscience Applications by Optimal Neural Network Architecture

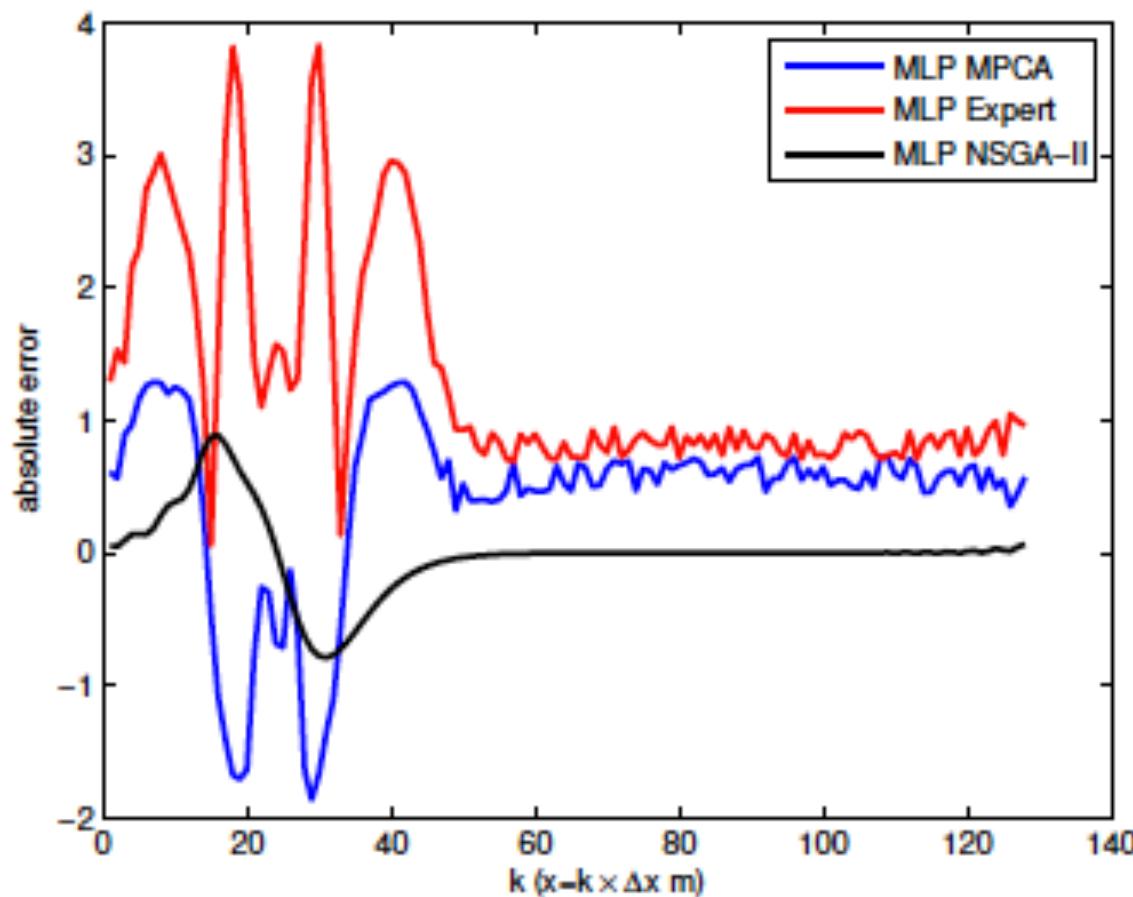
Authors

Authors and affiliations

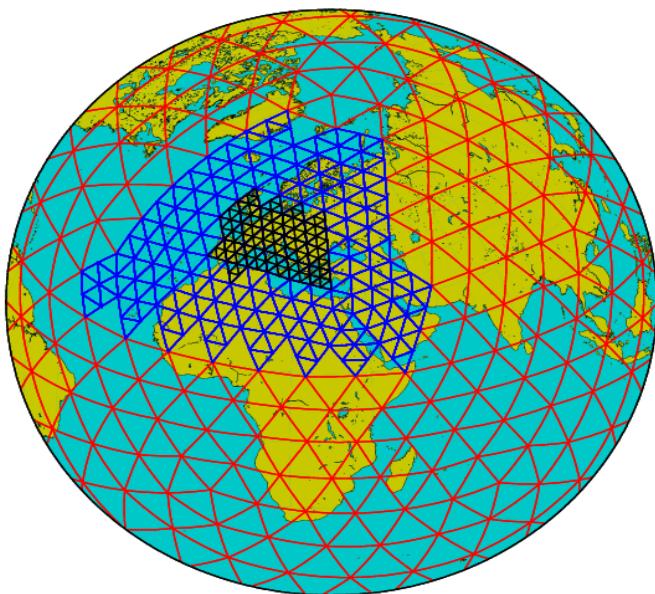
Juliana Aparecida Anochi , Reynier Hernández Torres, Haroldo Fraga de Campos Velho

Data assimilation – NN emulating KF

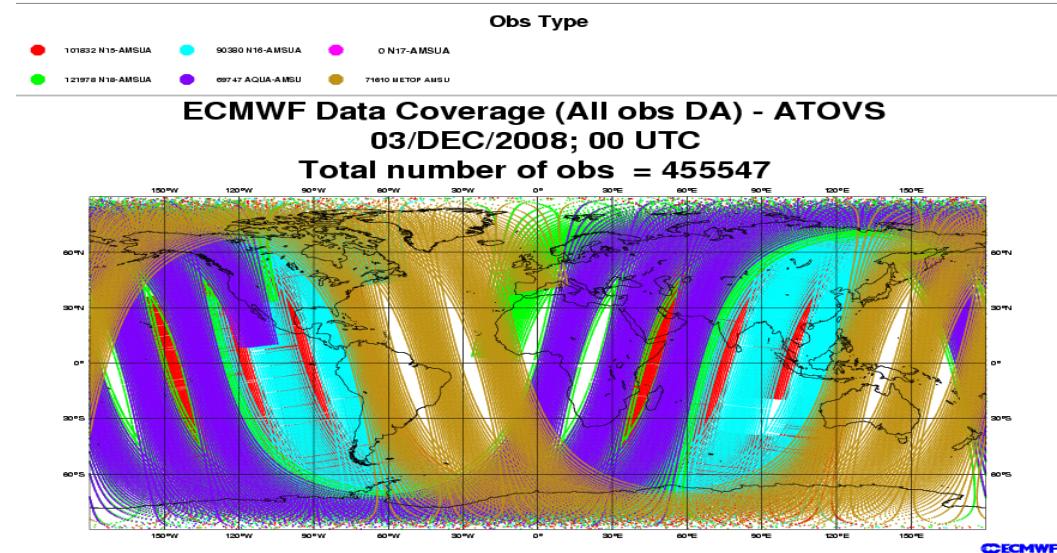
- NN emulating Kalman filter: Linear wave 1D



Why? Exponential growth for the available data



Numerical models with very high resolution



Number of observations are increasing:
different satellites with thousands of
bands, sensor cost decreasing.

DA: neural networks – our methodology

- We are using supervised neural networks
- We use NN for emulating another technique
- Why to emulate another technique?
For saving processing time – at least!
- Database: a set of predictions, observations, analysis
- Domain decomposition
 - Each subdomain with different NN
 - Assimilation for each model grid point
 - Automatic configuration for all neural networks

Finding an OPTIMAL neural network

- Design of supervised neural network:
Optimization problem – cost function:

$$E_{trein} = \frac{1}{N} \sum_{k=1}^N (d_k - s_k)^2$$
$$E_{gen} = \frac{1}{(M-N+1)} \sum_{k=N+1}^M (d_k - s_k)^2$$
$$F_{obj} = \text{penalty} * \frac{\rho_1 * E_{trein} + \rho_2 * E_{gen}}{\rho_1 + \rho_2}$$
$$\text{penalty} = \underbrace{\left(c_1 * \left(e^{\# \text{neuron}} \right)^2 \right)}_{\text{complexity factor-1}} \times \underbrace{\left(c_2 * (\# \text{epoch}) \right)}_{\text{complexity factor-2}} + 1$$

MPCA: Multi-Particle Collision Algorithm

Available for download:

www.epacis.net/jcis/PDF_JCIS/JCIS11-art.01.pdf



Journal of Computational Interdisciplinary Sciences (2008) 1(1): 3-10

© 2008 Pan-American Association of Computational Interdisciplinary Sciences

ISSN 1983-8409

<http://epacis.org>

A new multi-particle collision algorithm for optimization in a high performance environment

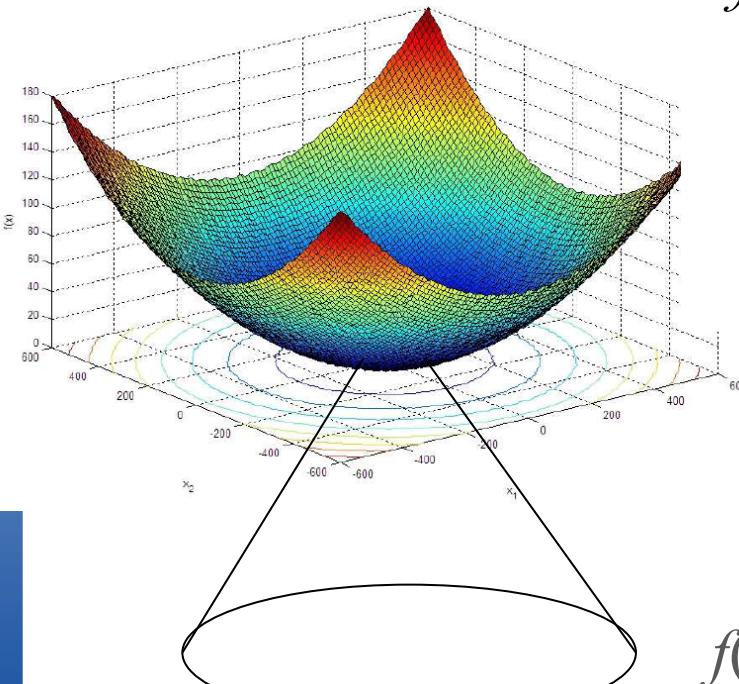
Eduardo Fávero Pacheco da Luz, José Carlos Becceneri and Haroldo Fraga de Campos Velho

Manuscript received on July 31, 2008 / accepted on October 5, 2008



PCA vs MPCA (2)

Griewank function



$$f(x_1, \dots, x_n) = 1 + \sum_{j=1}^n \frac{x_j^2}{4000} - \prod_{i=1}^n \cos\left(\frac{x_i}{\sqrt{i}}\right)$$

$$\|(x_1, \dots, x_n)\|_2^2 \leq 600$$

$$\min : (0, \dots, 0), \quad f(0, \dots, 0) = 0$$

PCA

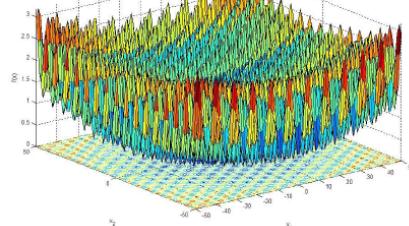
$$(-3.14, 4.43)$$

$$f(x_1, x_2) = 7.4 \times 10^{-3}$$

MPCA

$$(-1.8 \times 10^{-8}, -3.3 \times 10^{-8})$$

$$f(x_1, x_2) = 3.3 \times 10^{-16}$$



Finding an OPTIMAL neural network

- Supervised neural network: Multi-Layer Perceptron (MLP)

MPCA solution

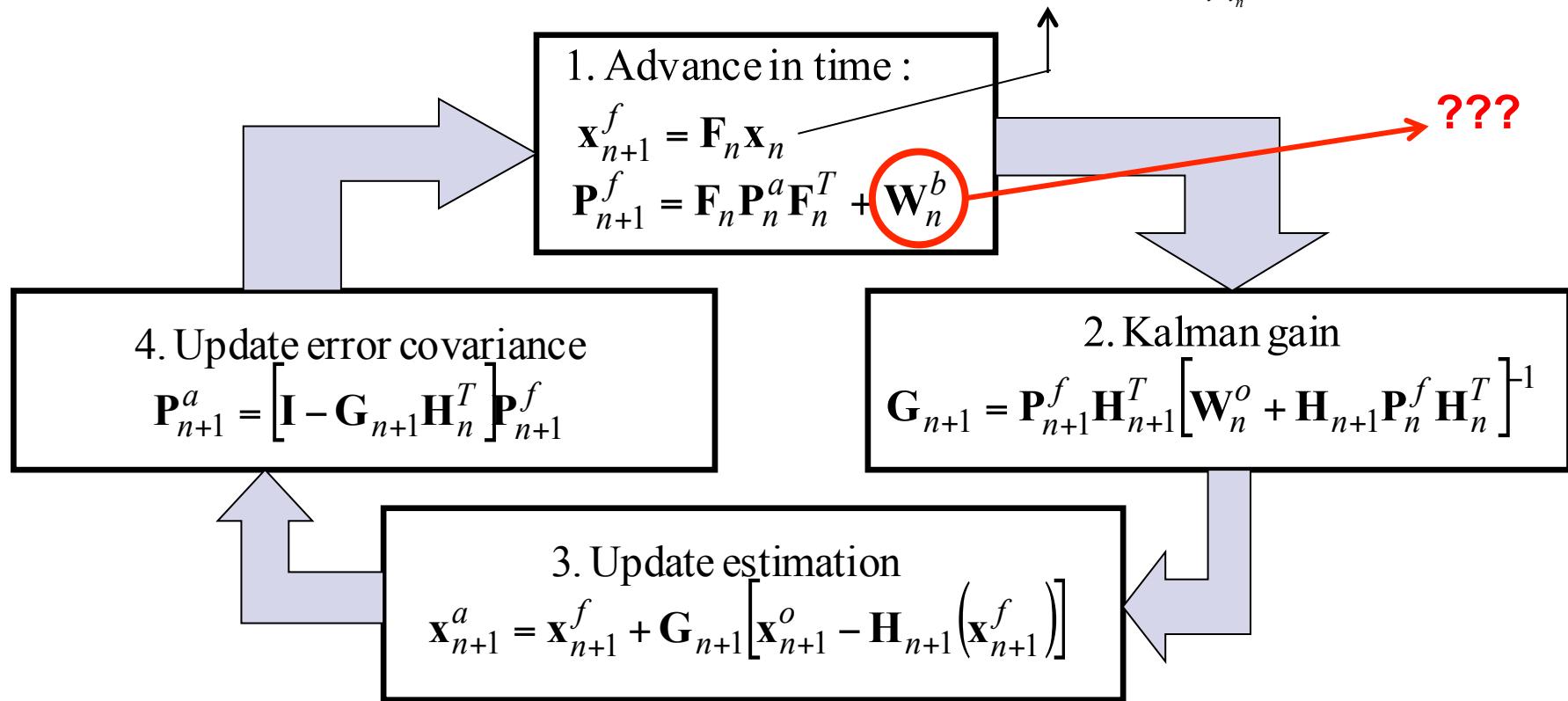


# hidden layers	# neurons layer-1	# neurons layer-2	# neurons layer-3	Activation function	Momentum ratio	Learning ratio
Parameters			Value			
Number of hidden layers				1 2 3		
Number of neurons for each layer				1 ... 32		
Learning ratio				0 ... 1		
Momentum				0 ... 0.9		
Activation function				Tanh Log Gauss		

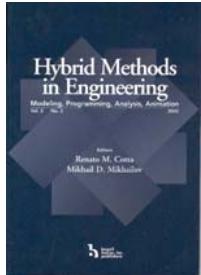
Data assimilation – first application

■ Kalman filter

$$\mathbf{x}_{n+1} = F[\mathbf{x}_n, t_n] \approx \mathbf{F}_n + \frac{\partial F}{\partial \mathbf{x}} \Big|_{t=t_n} \mathbf{x}_n + O(\Delta t^2) \approx \mathbf{E}_n \mathbf{x}_n$$



Bayesian filters



- **Kalman filter**
- Estimating the error modeling co-variance matrix
 - Estimating \mathbf{W}^b by parameterization
 - Estimating \mathbf{W}^b by Fokker-Planck equation
 - Estimating \mathbf{W}^b by ensemble strategy

$$\mathbf{W}^b \approx \frac{1}{N_k - m} \sum_{k=1}^{N_k} \left(\mathbf{x}_k^f - \bar{\mathbf{x}}^f \right) \left(\mathbf{x}_k^f - \bar{\mathbf{x}}^f \right)^T \quad \left\{ \begin{array}{l} \bar{\mathbf{x}} : \text{ensemble average} \\ N_k : \text{number of members} \\ m = 1 \text{ or } 2 \end{array} \right.$$

Bayesian filters

- **Ensemble Kalman filter**
- Estimating the error modeling co-variance matrix
 - Estimating \mathbf{W}^b by parameterization
 - Estimating \mathbf{W}^b by Fokker-Planck equation
 - Estimating \mathbf{W}^b by ensemble strategy

$$\mathbf{W}^b \approx \frac{1}{N_k - m} \sum_{k=1}^{N_k} \left(\mathbf{x}_k^f - \bar{\mathbf{x}}^f \right) \left(\mathbf{x}_k^f - \bar{\mathbf{x}}^f \right)^T \quad \left\{ \begin{array}{l} \bar{\mathbf{x}} : \text{ensemble average} \\ N_k : \text{number of members} \\ m = 1 \text{ or } 2 \end{array} \right.$$

SPEED model

Forward model (x^f):

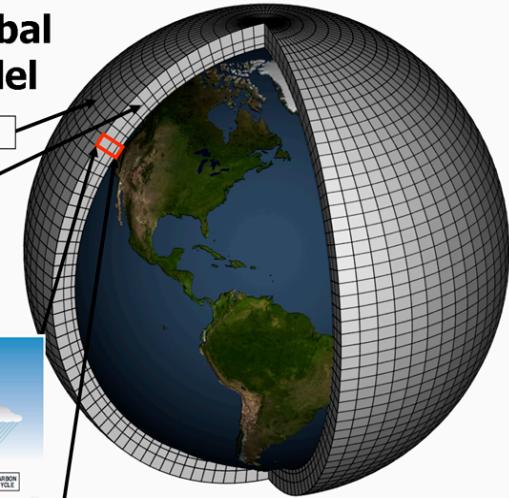
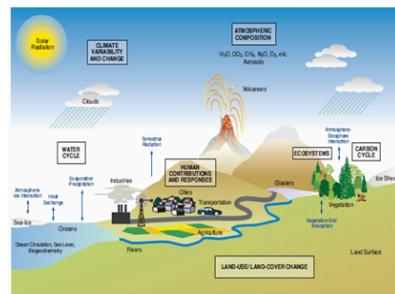
SPEED model

- Atmospheric general circulation model
- 3D spectral model
- simplified parameterization

Schematic for Global Atmospheric Model

Horizontal Grid (Latitude-Longitude)

Vertical Grid (Height or Pressure)



Vertical coordinates: $\sigma = p_s/p$.

Horizontal coordinates: (lat , long) on a Gaussian grid

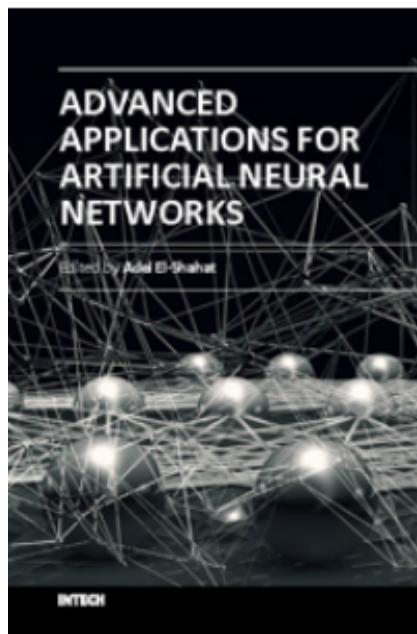
The spectral model: T30 horizontal resolution and 7 vertical levels

Observations: 12035 (00 and 12 UTC) = 415 x 4 x 7 + 415

Observations: 2075 (00 and 12 UTC) = 415 x 5 (only surface)

SPEED model

Chapter 14



Data Assimilation by Artificial Neural Networks for an Atmospheric General Circulation Model

Rosangela Saher Cintra and
Haroldo F. de Campos Velho

Additional information is available at the end of the chapter

<http://dx.doi.org/10.5772/intechopen.70791>

SPEED: atm. general circulation model

Spectral 3D model, with simplified parameterization

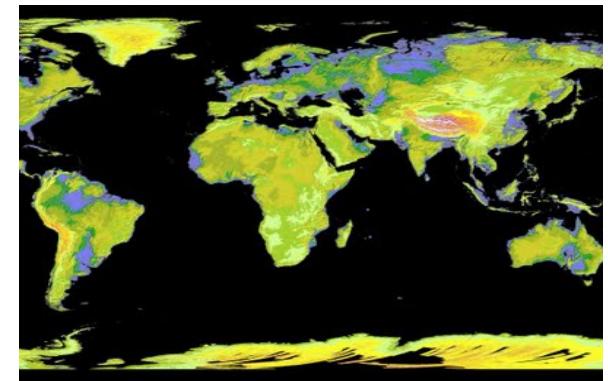
$$\frac{\partial \zeta}{\partial t} = -\nabla \cdot (\zeta + f)\mathbf{U} - \mathbf{k} \cdot \nabla \times \left(RT' \nabla lp + \dot{\sigma} \frac{\partial \mathbf{U}}{\partial \sigma} + \mathbf{F} \right)$$

$$\frac{\partial D}{\partial t} = \mathbf{k} \cdot \nabla \times (\zeta + f)\mathbf{U} - \nabla \cdot \left(RT' \nabla lp + \dot{\sigma} \frac{\partial \mathbf{U}}{\partial \sigma} + \mathbf{F} \right) - \nabla^2 (\Phi' + RT_0 lp + \frac{1}{2} \mathbf{U} \cdot \mathbf{U})$$

$$\frac{\partial T}{\partial t} = -\nabla \cdot \mathbf{U} T' + T' D + \dot{\sigma} \gamma - \frac{RT}{c_p} \left(D + \frac{\partial \dot{\sigma}}{\partial \sigma} \right) \quad \text{{with: } } \phi = gh ; \text{ and: } \sigma = p/p_0$$

$$\frac{\partial q}{\partial t} = -D - \frac{\partial \dot{\sigma}}{\partial \sigma} - \mathbf{U} \cdot \nabla lp \quad \text{{with: } } q = \log(p_0)$$

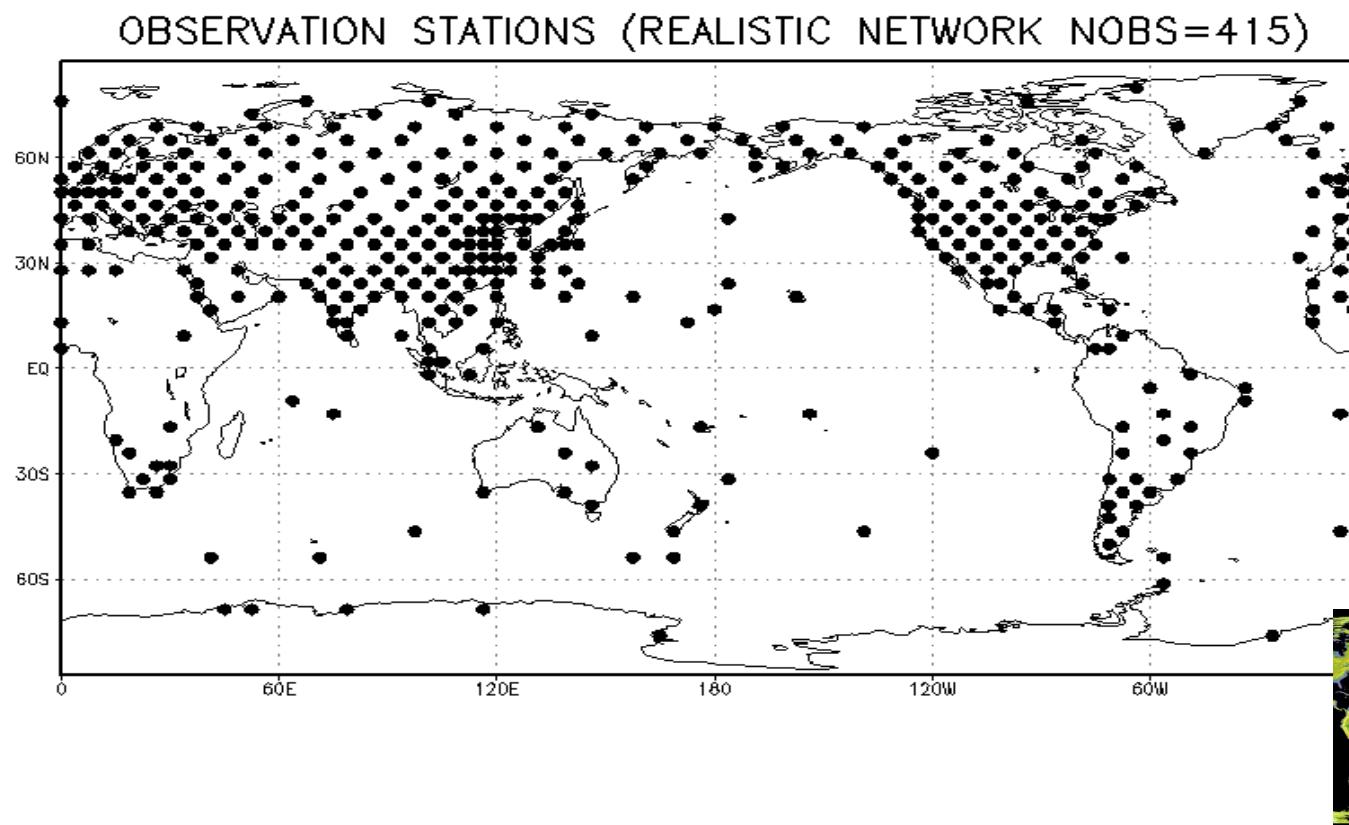
- (a) ζ : vorticity
- (b) D : divergence
- (c) T : temperature
- (d) q : moisture



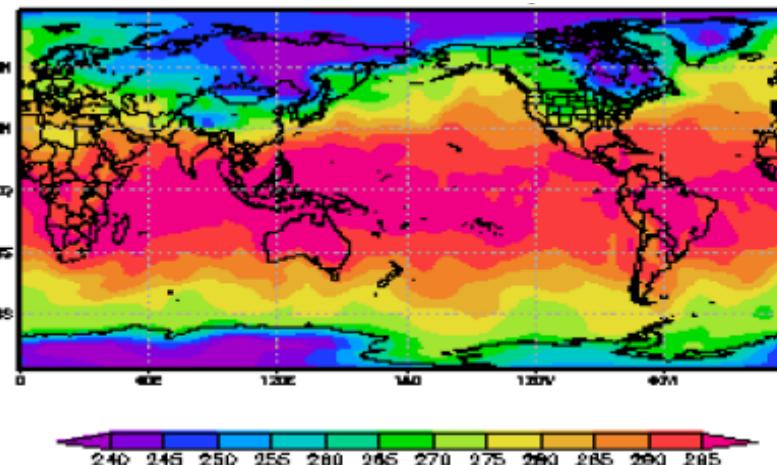
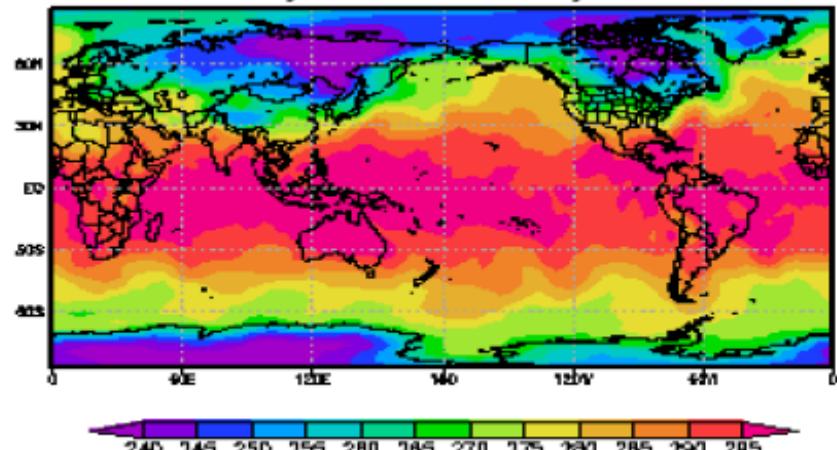
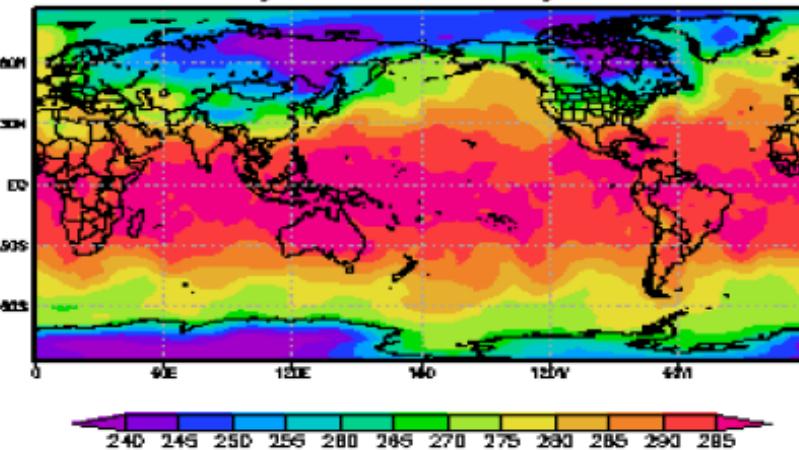
SPEED: atmospheric general circulation model

Spectral 3D model, with simplified parameterization

Observation grid: NN emulating LEnTKF



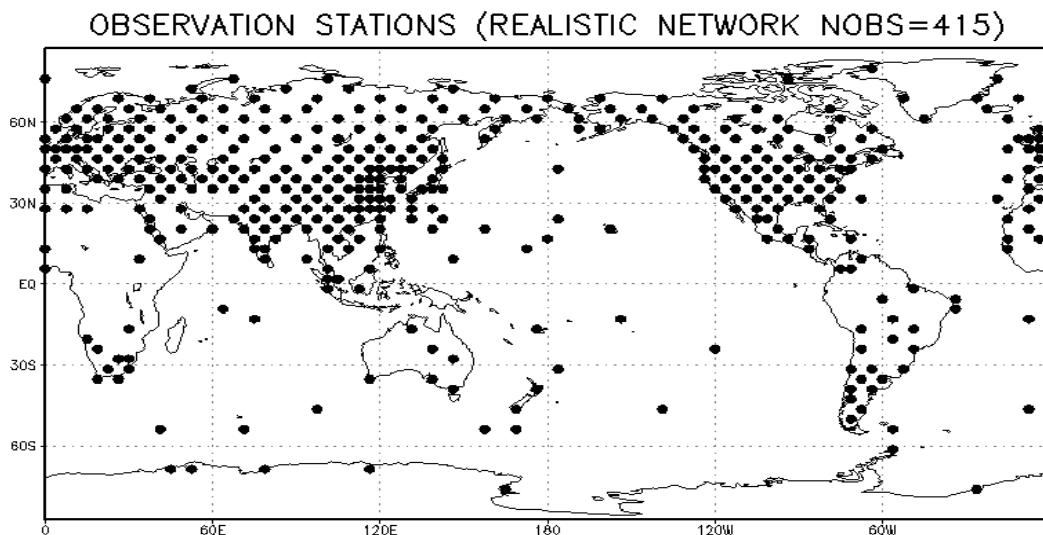
Temperature: assimilation experiment



LETKF neural network
True

Results from Rosangela Cintra PhD thesis (2011)

Experiment: LETKF and neural network



Execution time	
LETKF method	ANN method
04:20:39	00:02:53
hours : minutes : seconds	

General atmospheric Circulation Modelo 3D (spectral model):

SPEEDY (Simplified Parameterizations primitivE Equation DYnamics)

Gaussian grid: 96 x 48 (horizontal) x 7 levels (vertical) = T30L7

Total grid points: 32.256 Total de variáveis: 133.632

Observations: (00, 06, 12, 18 UTC) – radiosondes “OMM stations”

Observations: 12035 (00 e 12 UTC) = $415 \times 4 \times 7 + 415$

Observations: 2075 (00 e 12 UTC) = 415×5 (only surface)

Results from the Rosangela Cintra's PhD thesis (2011)

Global model for NWP

- FSU-COAPS global model: equations

$$\begin{aligned}
 \frac{\partial \zeta}{\partial t} &= -\nabla \cdot (\zeta + f) \vec{v}_H - \vec{k} \cdot \nabla \times \left(RT \nabla q + \dot{\sigma} \frac{\partial \vec{c}_H}{\partial \sigma} - \vec{f} \right) \\
 \frac{\partial D}{\partial t} &= \vec{k} \cdot \nabla \times (\zeta + f) \vec{v}_H - \nabla \cdot \left(RT \nabla q + \dot{\sigma} \frac{\partial \vec{c}_H}{\partial \sigma} - \vec{f} \right) - \nabla^2 \left(\phi + \frac{\vec{v}_H \cdot \vec{v}_h}{2} \right) \\
 \frac{\partial T}{\partial t} &= -\nabla \cdot (T \vec{v}_H) + TD + \dot{\sigma} \gamma - \frac{RT}{c_p} \left(D + \frac{\partial \dot{\sigma}}{\partial \sigma} + H_T \right) \\
 \frac{\partial q}{\partial t} &= -\vec{v}_H \cdot \nabla q - D - \frac{\partial \dot{\sigma}}{\partial \sigma} \quad \{ \text{with: } q = \log(p_0) \} \\
 \sigma \frac{\partial \phi}{\partial \sigma} &= -RT \quad \{ \text{with: } \phi = gh ; \text{ and: } \sigma = p/p_0 \} \\
 \frac{\partial r}{\partial t} &= -\nabla \cdot (r \vec{v}_H) + rD - \dot{\sigma} \frac{\partial r}{\partial \sigma} + M \quad \{ \text{with: } r \text{ moisture and: } M \text{ source/sink} \}
 \end{aligned}$$

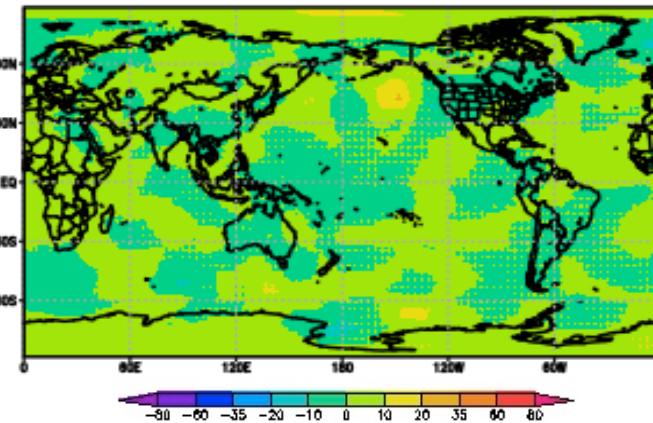
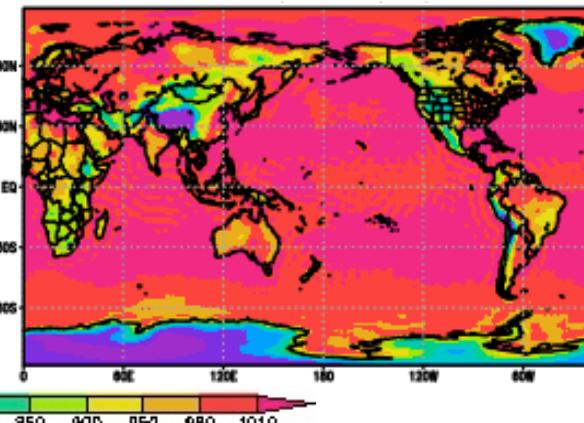
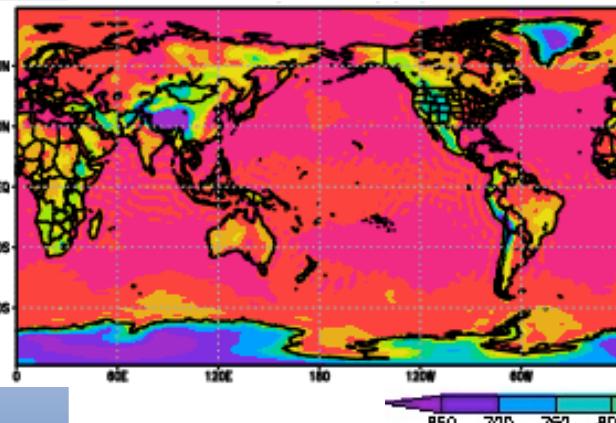
Data assimilation: LETKF x ANN (FSU model)

- LETKF with 40 members
- Model resolution T63L27: 63 spherical harmonic components for horizontal resolution (~ 1.875), and 27 unevenly spaced vertical levels.
- Number of grid points: 96 x 192 x 27
- MLP-NNs: **96** (4 horiz x 6 vert x 4 variables)
- Cray XE6 CPTEC: 24 nodes - 2 Opteron 12-cores

Data assimilation: LETKF x ANN (FSU model)

Surface Pressure(Kg/Kg) generalization

04/Jan/2005 – 12 UTC



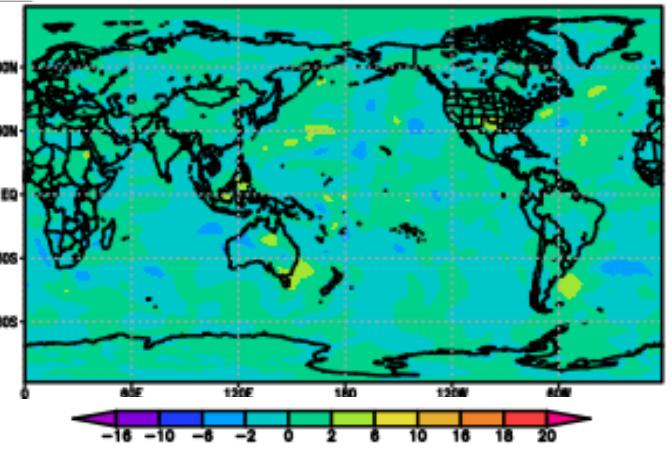
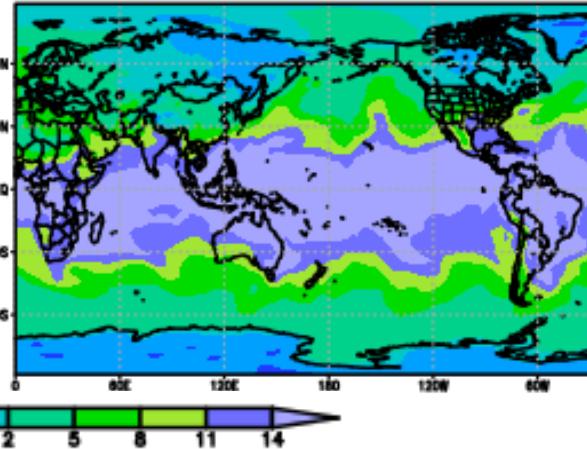
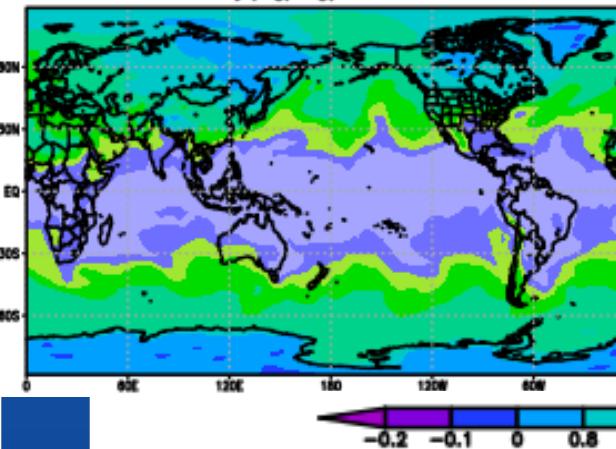
LETKF analysis

NN_MLP analysis

Differences analysis

Specific Humidity (Kg/Kg) generalization

04/Jan/2005 – 12 UTC



LETKF analysis

NN_MLP analysis

Differences analysis

Data assimilation: LETKF x ANN (FSU model)

Execution of 124 cycles	MLP-DA (hour:min:sec)	LETKF (hour:min:sec)	
Analysis time	00:02:29	11:01:20	← 266 times faster
Ensemble time	00:00:00	15:50:40	
Parallel model time	00:27:20	00:00:00	
Total Time	00:29:49	26:52:00	← 55 times faster

The LETKF analysis runs on 40 nodes at Cray XT/16 (1280 nodes, each node with 2 Opteron 12 cores, total of 30720 cores) (<http://www.cptec.inpe.br/supercomputador>)).

MLP-DA computed analyses for the FSUGSM model:

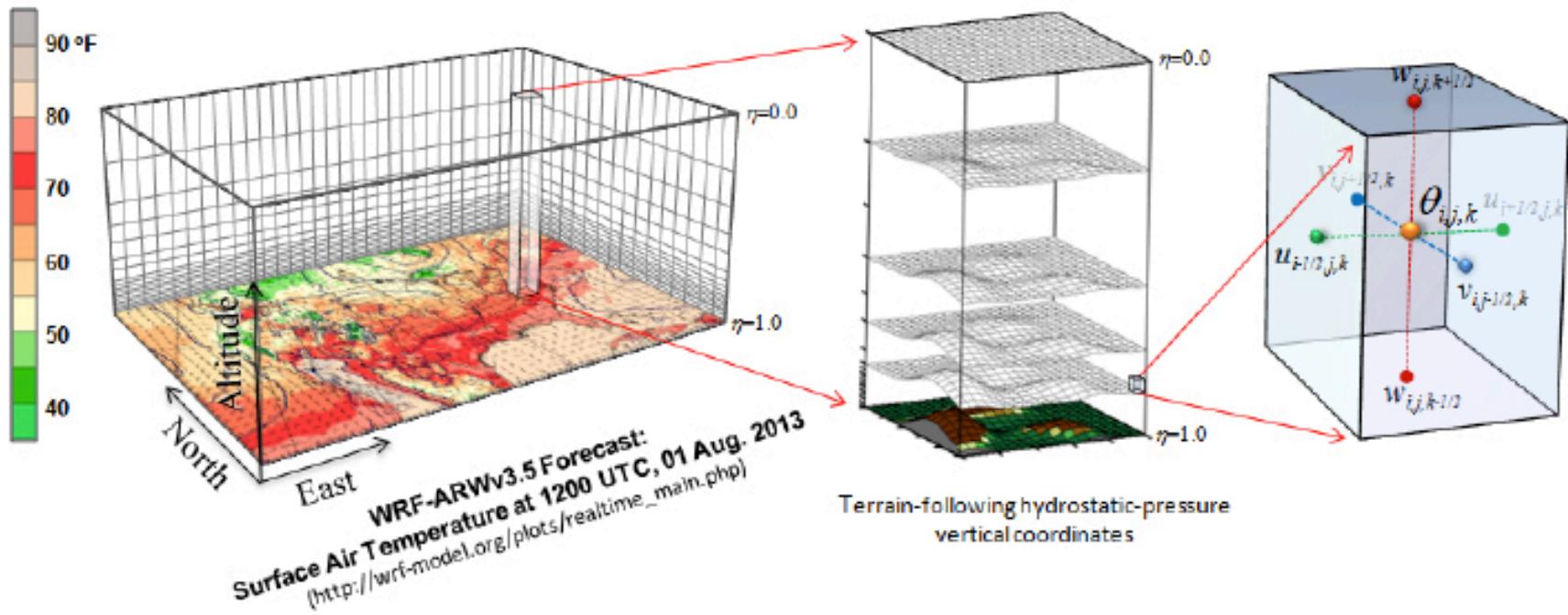
- **Analyses with similar LETKF quality**
- **Analysis with better computer performance.**

WRF: data assimilation by NN

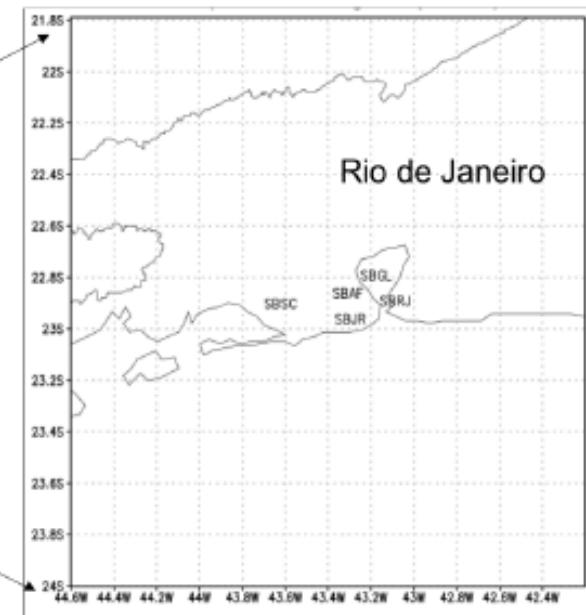
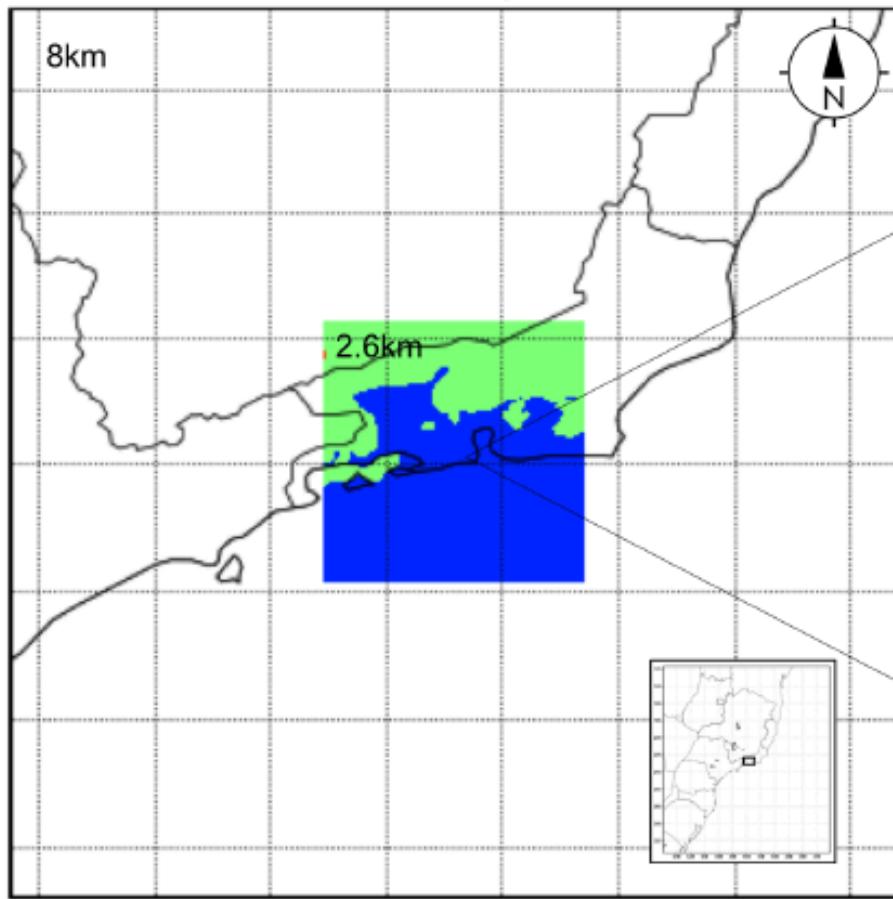
■ Cooperation:

- CODPT-INPE (BR)
- Universities (BR): UFPel + IFI-Bagé + UFOPA + UFRJ
- LNCC (BR)

WRF 3D Grid Cell Representation

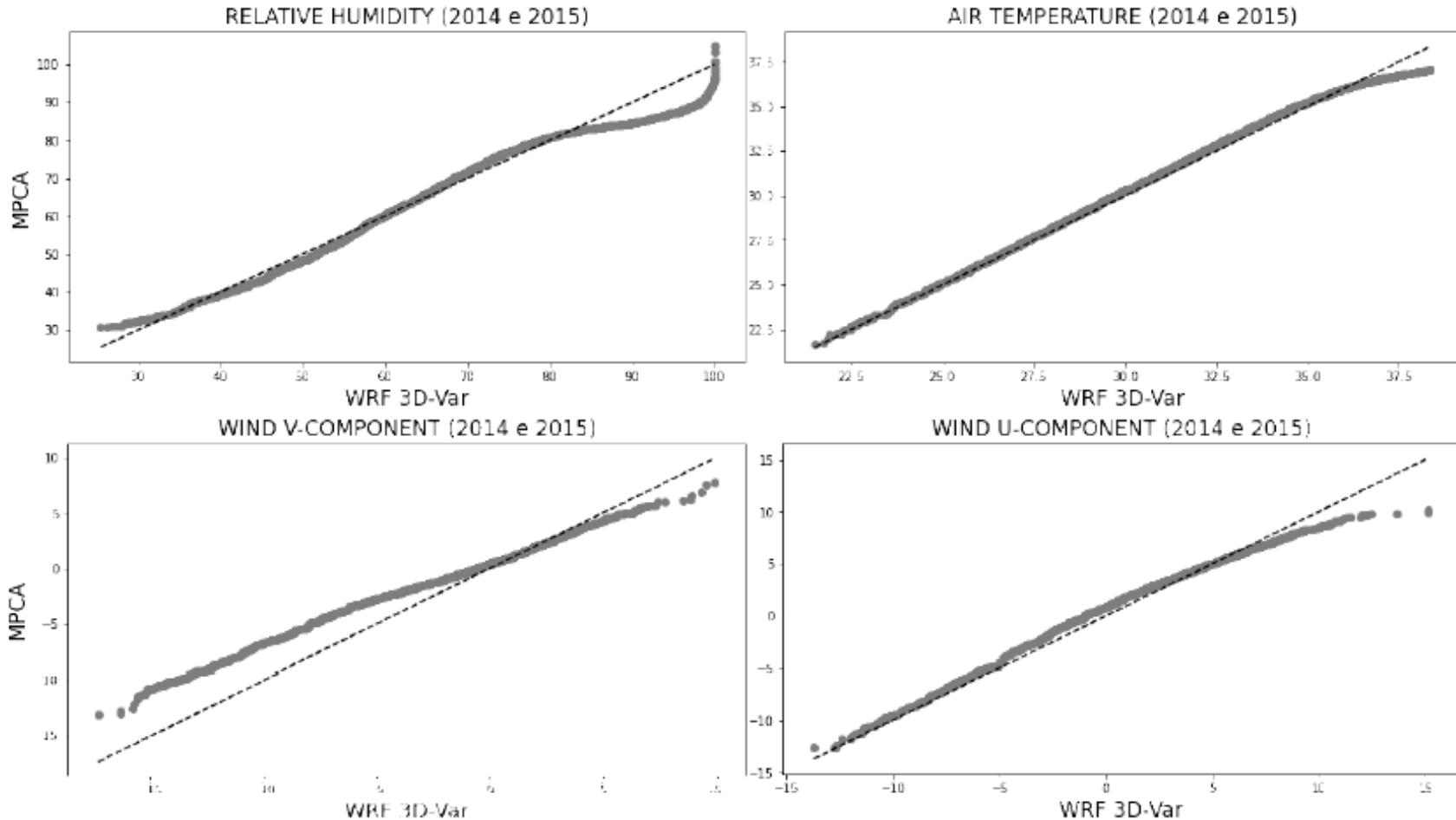


WRF-NCAR model



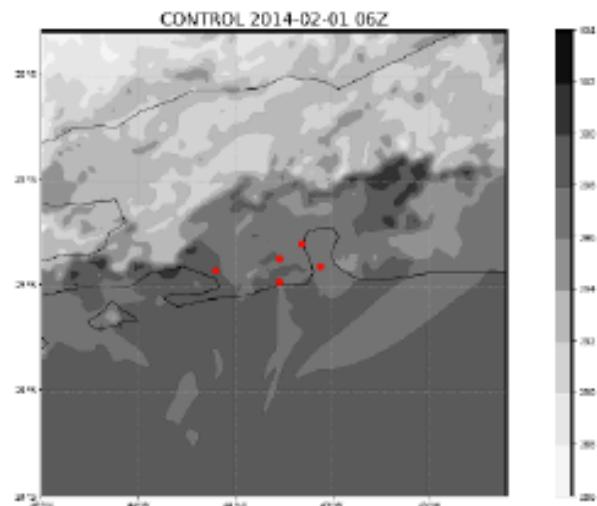
SBSC, SBAF, SBGL, SBRJ,
SBJR are airports within the
study area

WRF-NCAR model

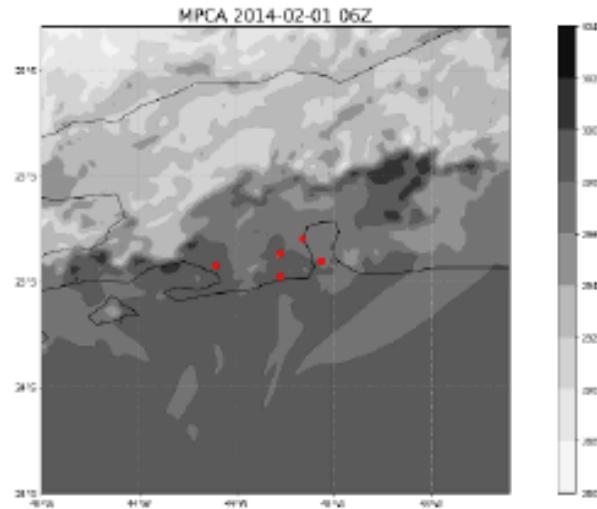


WRF-NCAR model

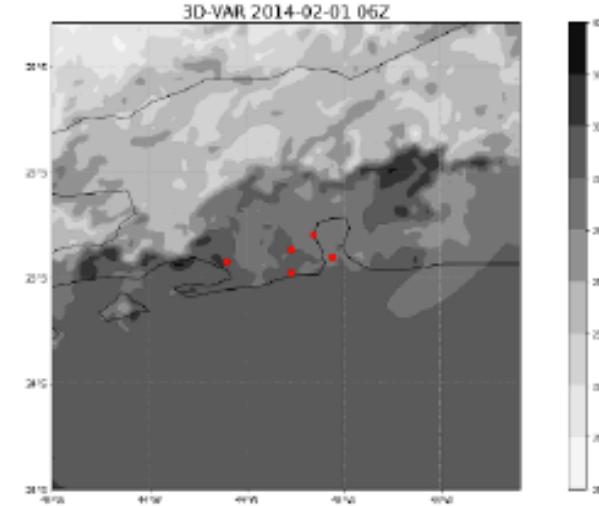
Control



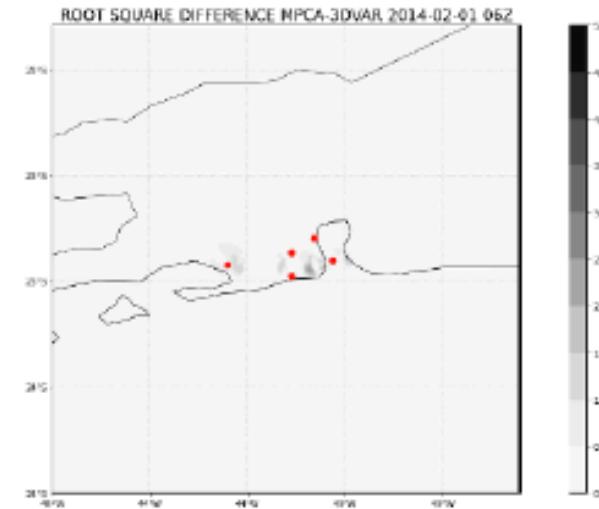
MPCA



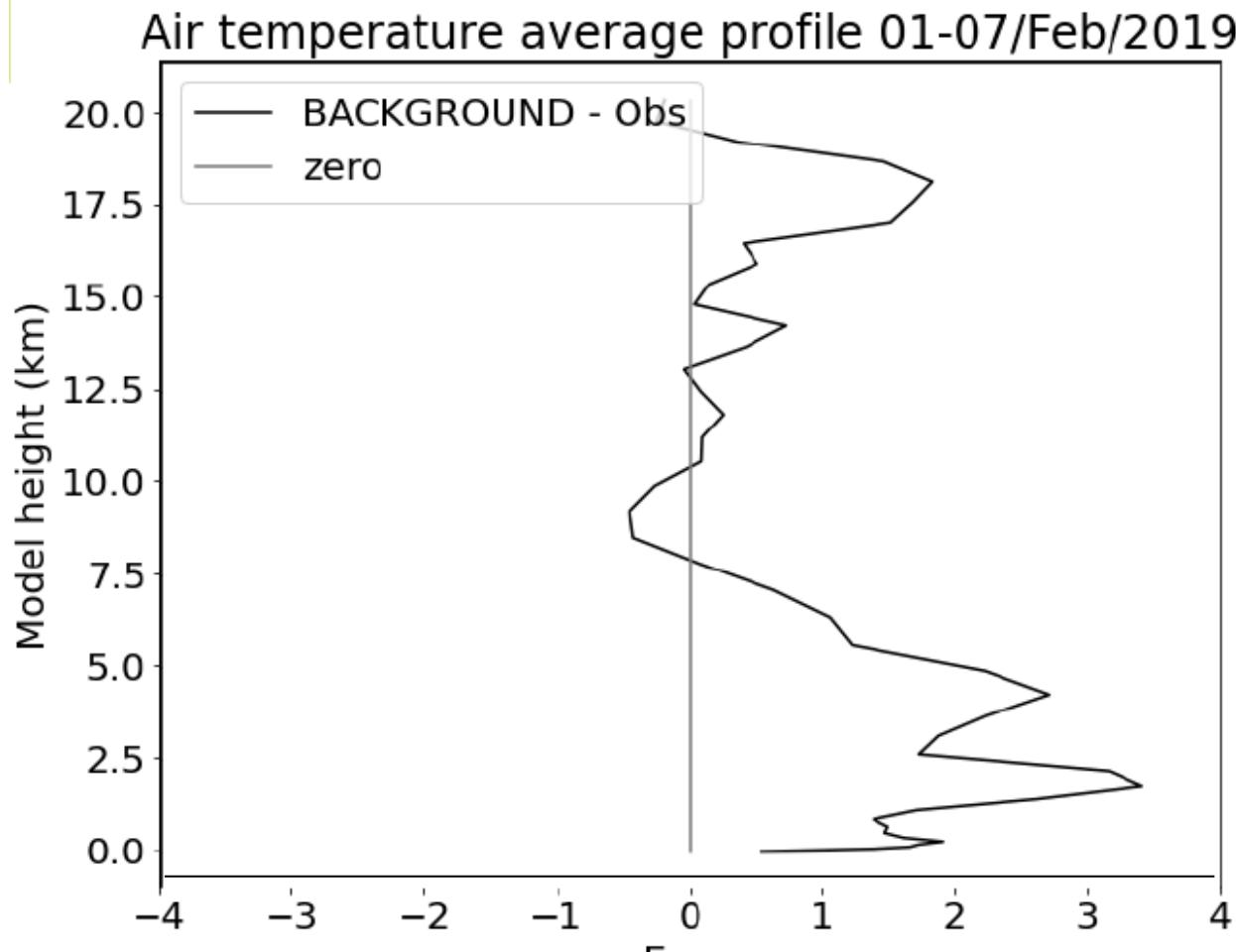
3dvar



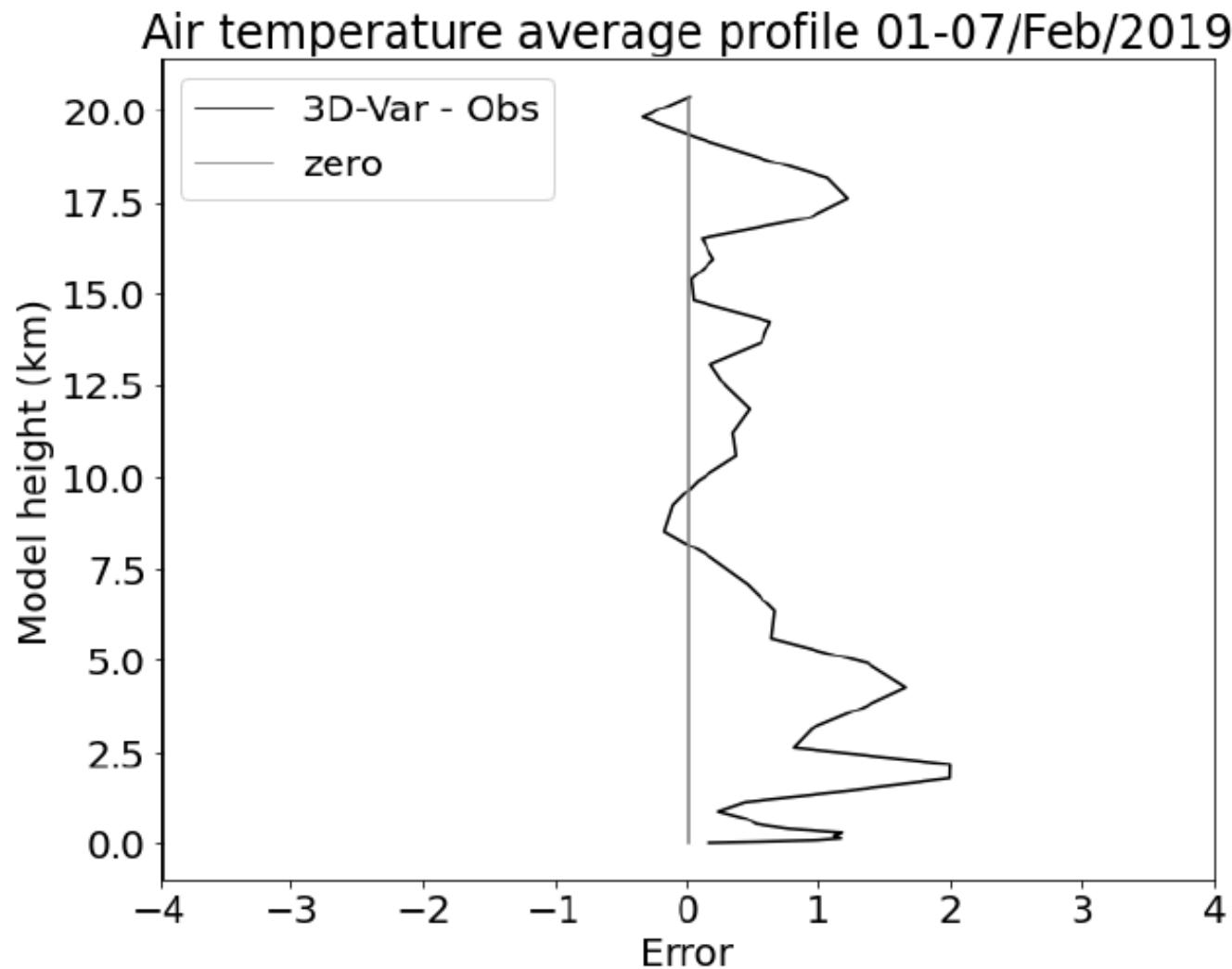
MPCA-3dvar



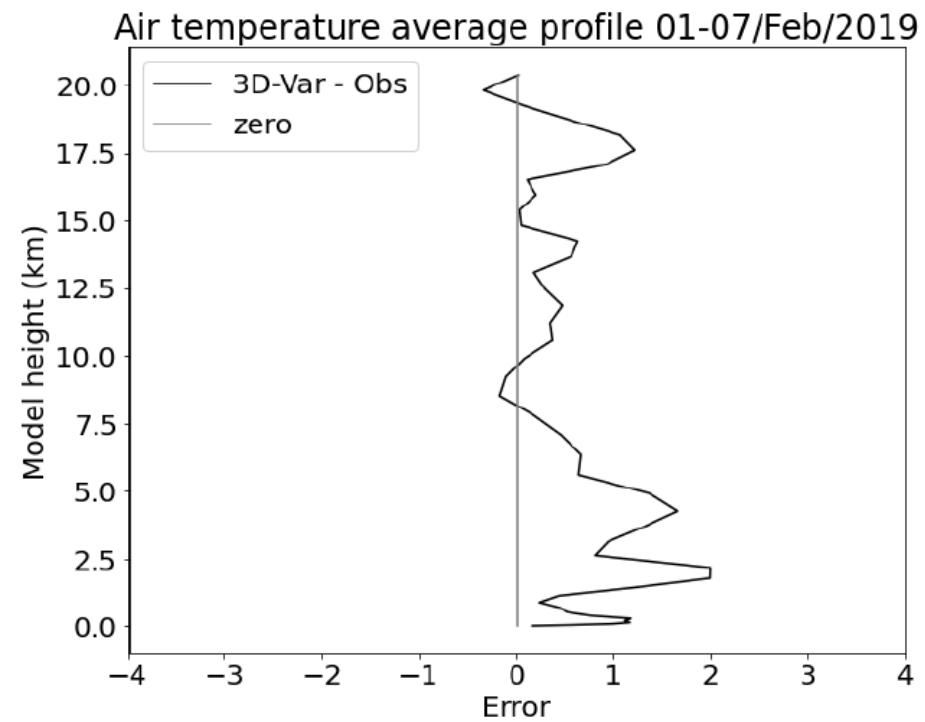
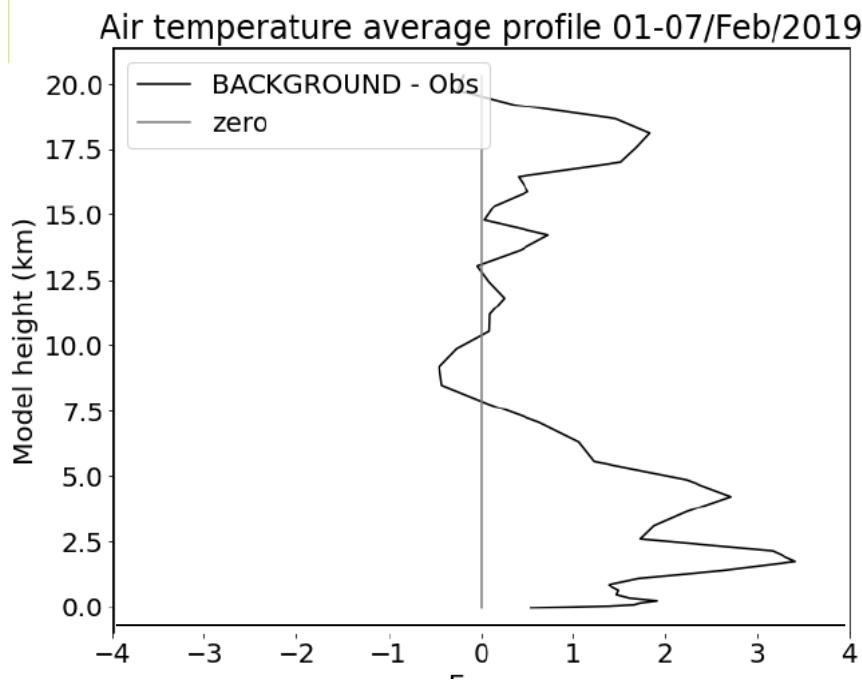
WRF-NCAR model



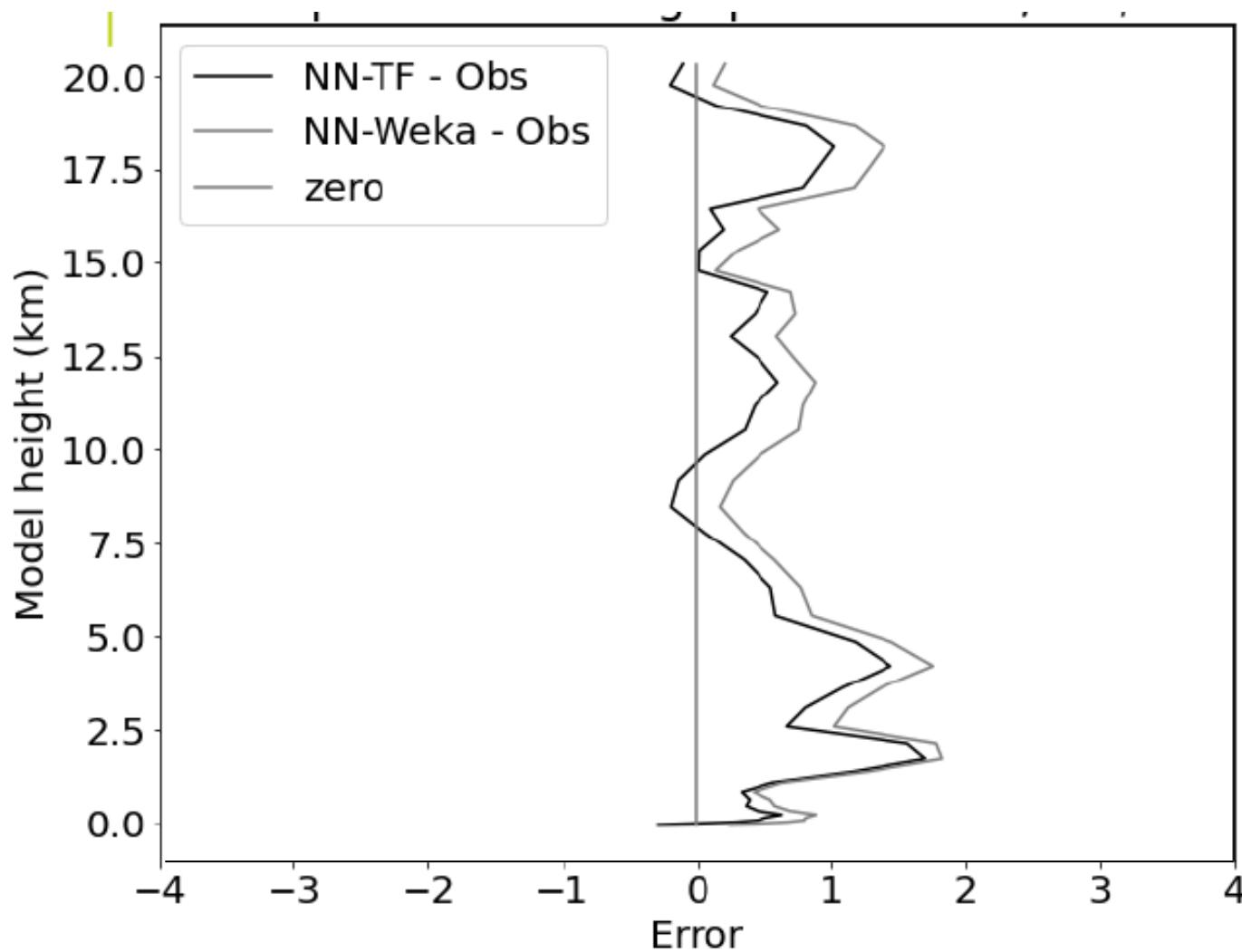
WRF-NCAR model



WRF-NCAR model



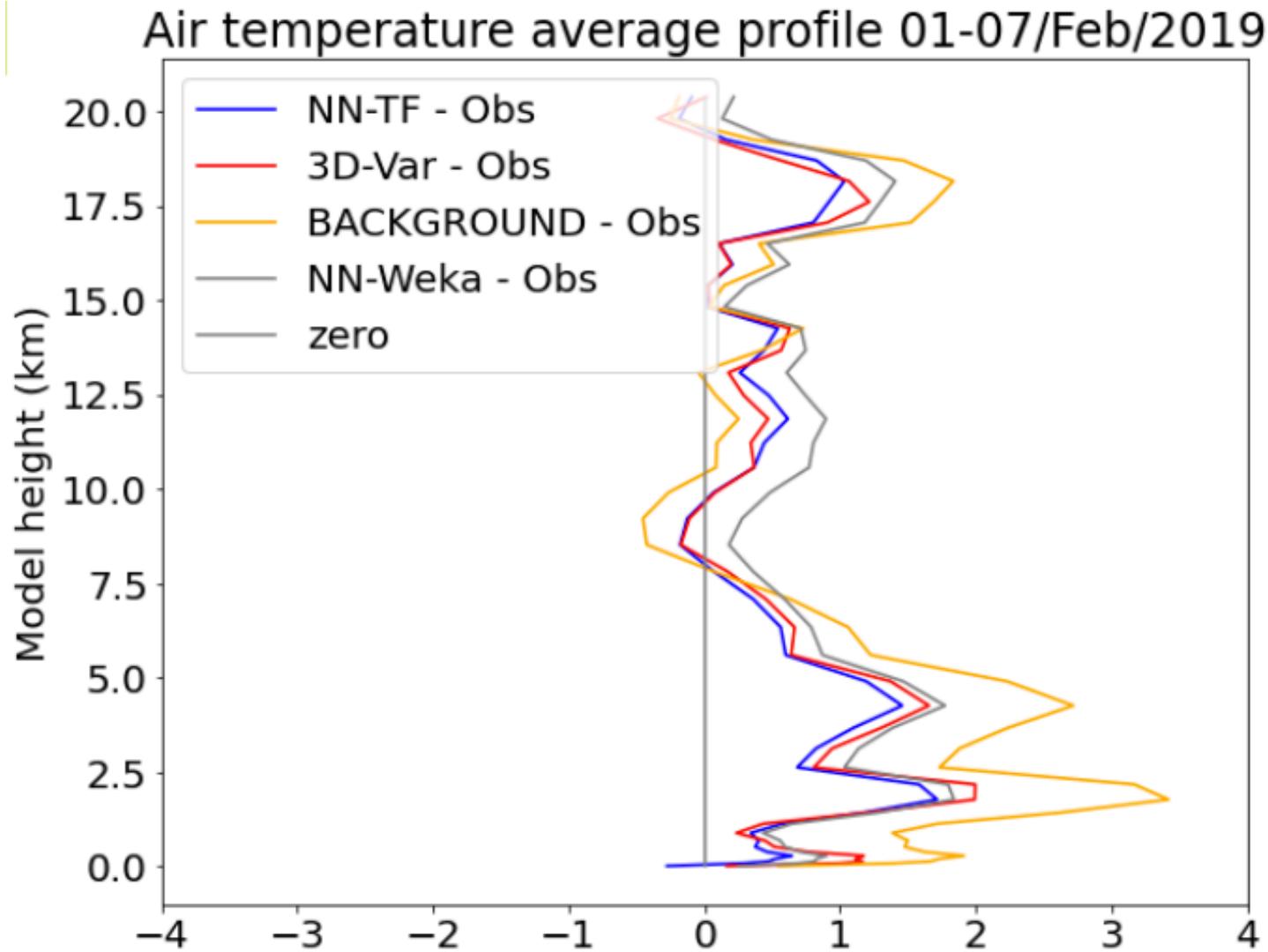
WRF-NCAR model



TensorFlow



WRF-NCAR model



WRF-NCAR model

- CPU-time

	Time/cycle	Total
3D-Var	00:01:11	00:33:08
NN-MPCA	00:00:01	00:00:28

71 times faster

Data assimilation: NN vs. “standard” methods

■ CPU-time

MODEL	SPEED (G)		COAPS-FSU (G)		WRF (R)	
Method	LEnTKF		NN	LEnTKF		NN
CPU-time	04:20:39 00:02:53		26:52:00 00:29:49		00:33:08 00:00:28	

95 times faster

55 times faster

71 times faster

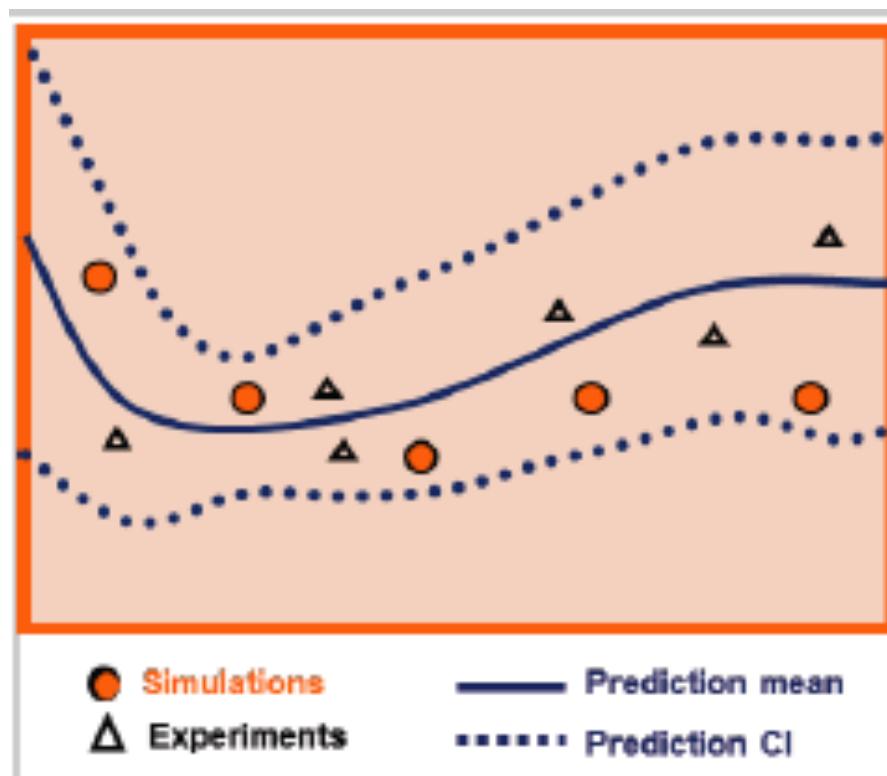
Predictability

How good is the prediction?

- Ensemble prediction
 - Data for statistical properties
 - Statistical tendencies
- Confidence interval
 - Large confidence interval: low predictability
 - Short confidence interval: high predictability

Predictability by ensemble prediction

- Ensemble prediction and confidence interval



Predictability by ensemble prediction

- Ensemble prediction and confidence interval

Proceedings of the joint ICVRAM ISUMA UNCERTAINTIES conference
Florianópolis, SC, Brazil, April 8-11, 2018



Data assimilation by neural networks with ensemble prediction

Cintra, Rosangela S.^{1,2}; Cocke, Steven² and Campos Velho, Haroldo F.¹

¹ National Institute for Space Research (INPE), São José dos Campos (SP), Brazil.

² Florida State University, Tallahassee (FL), USA.

Predictability by ensemble prediction

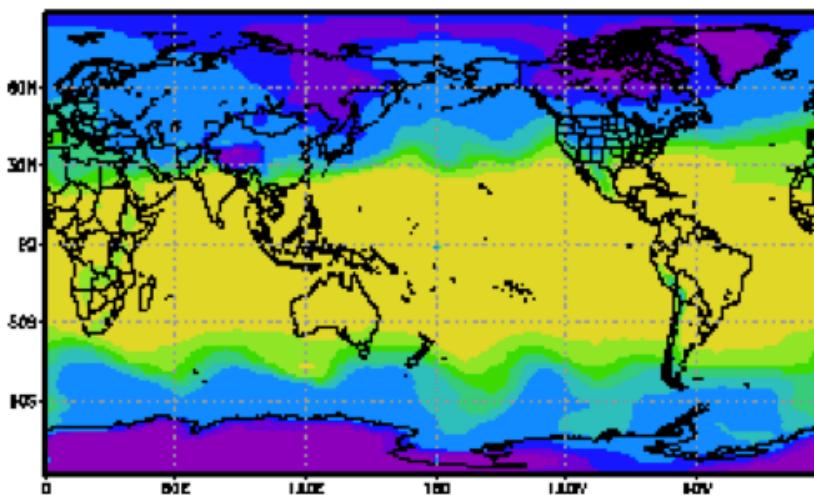
- Model execution by ensemble with 40 members
- Model resolution T63L27: 63 spherical harmonic components for horizontal resolution (~ 1.875), and 27 unevenly spaced vertical levels.
- Number of grid points: $96 \times 192 \times 27$
- Data assimilation with **96 MLP-NNs**
- Data assimilation cycle: **each 6 hours**
- Cray XE6 CPTEC: 24 nodes - 2 Opteron 12-cores

Ensemble prediction

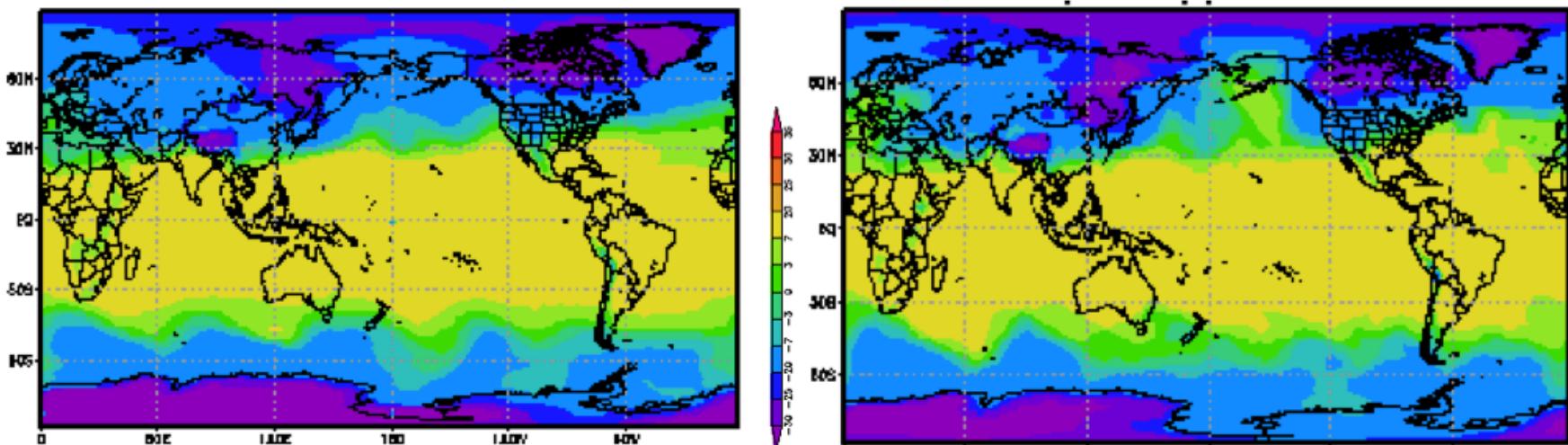
- FSU global model: January 2005

Temperature 500 hPa at 08/Jan/2005

LETKF



Control

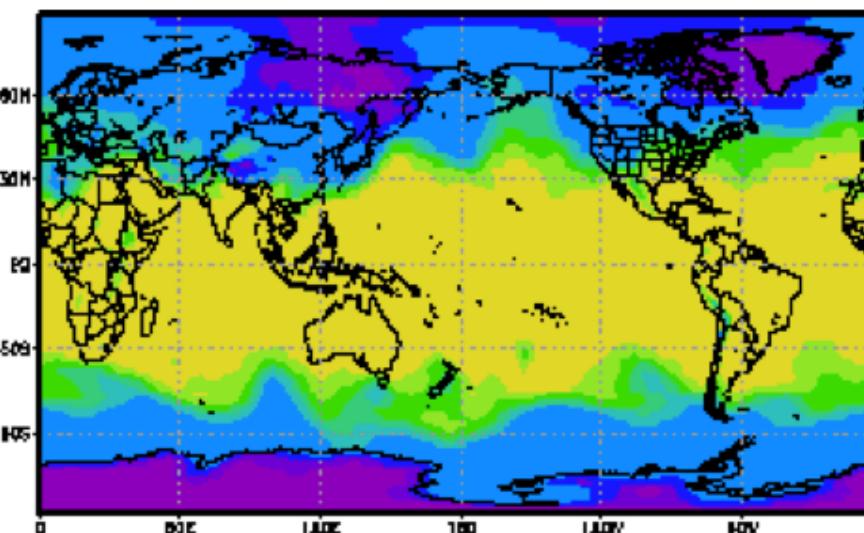


Ensemble prediction

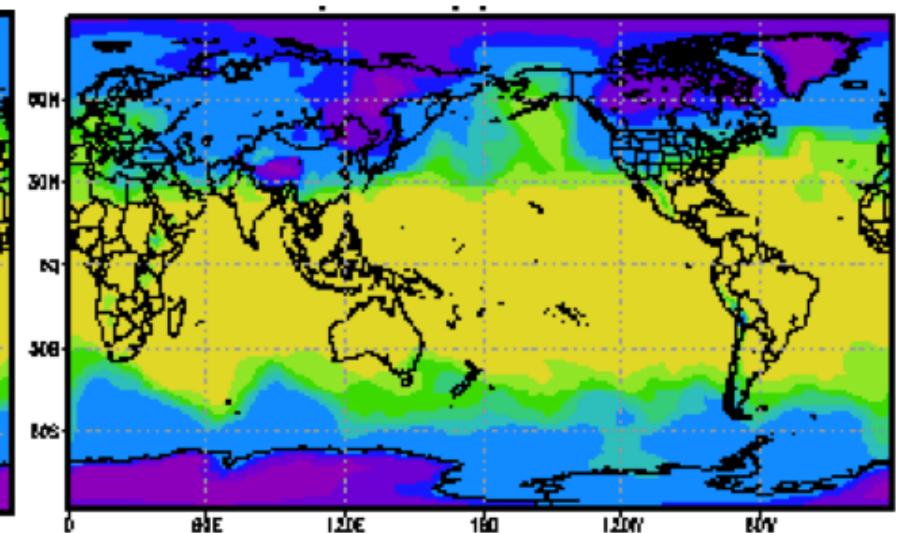
- FSU global model: January 2005

Temperature 500 hPa at 08/Jan/2005

NN-MLP



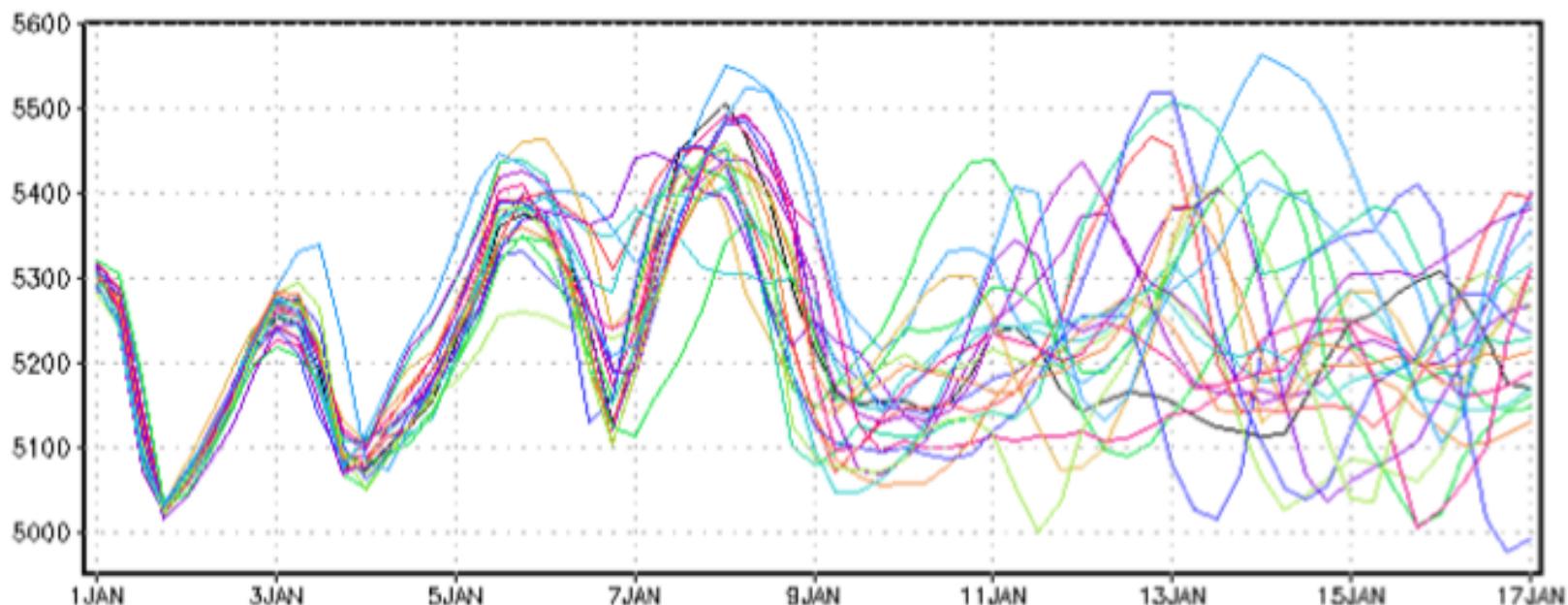
Control



Ensemble prediction

- FSU global model: January 2005

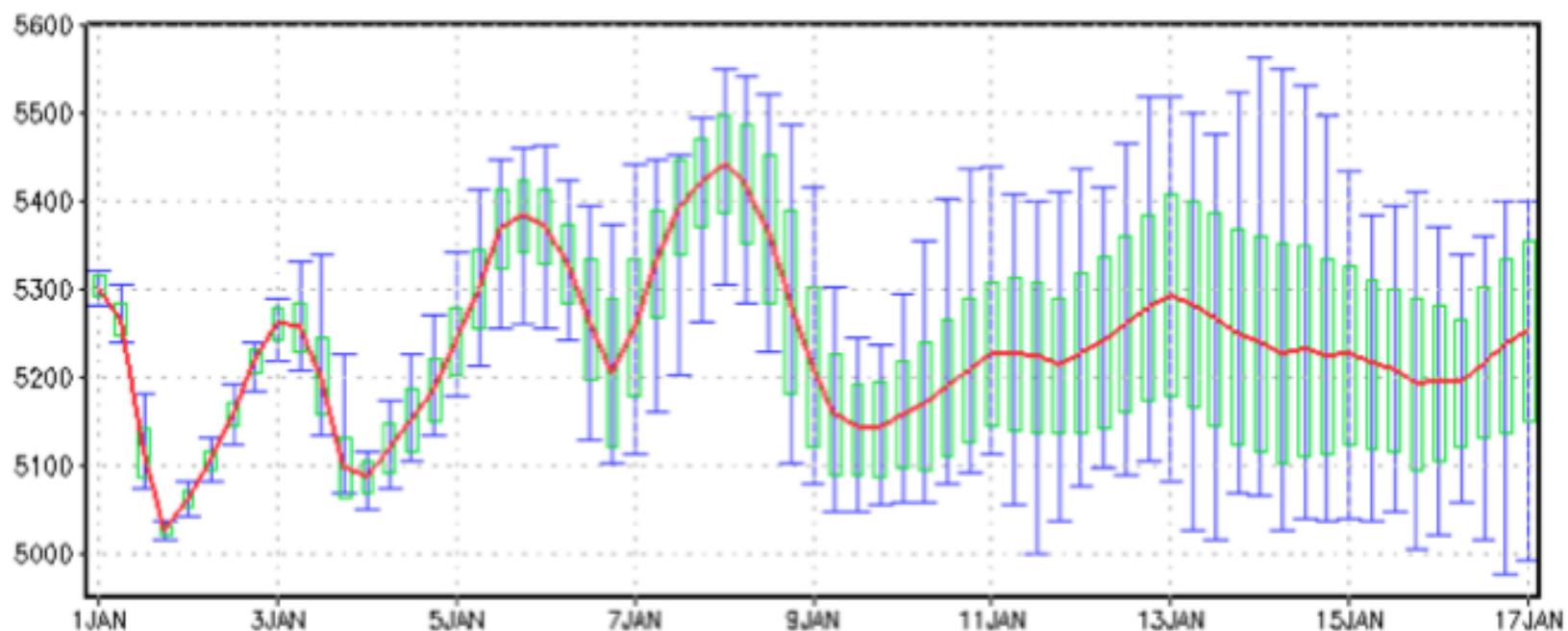
Spaghetti plots



Ensemble prediction

- FSU global model: January 2005

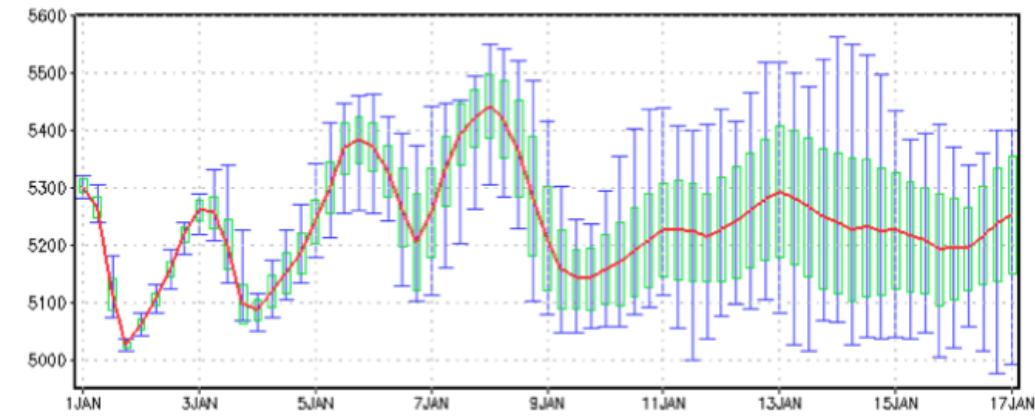
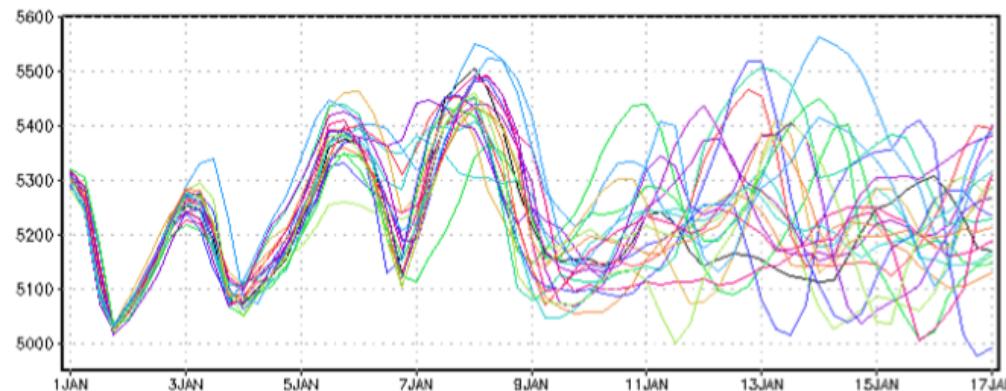
Confidence intervals



Ensemble prediction

- FSU global model: January 2005

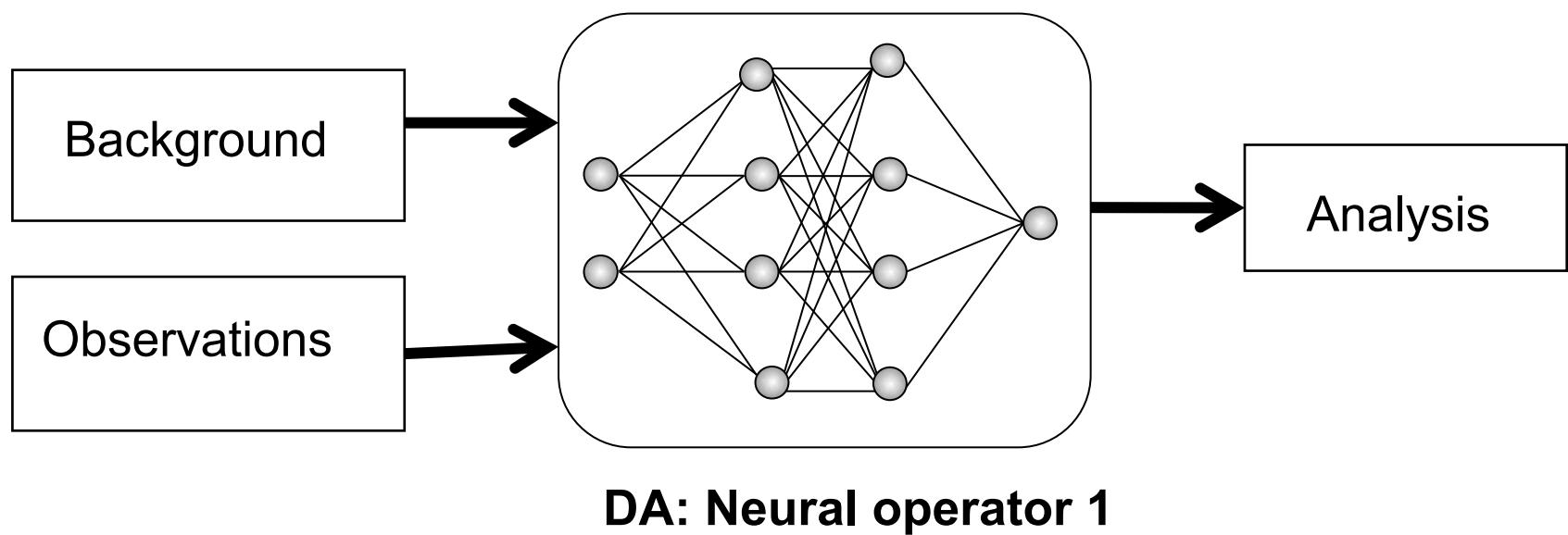
Spaghetti plots and confidence intervals



Uncertainty quantification by NN

Data assimilation: analysis by NN

Step-1: Data assimilation by NN



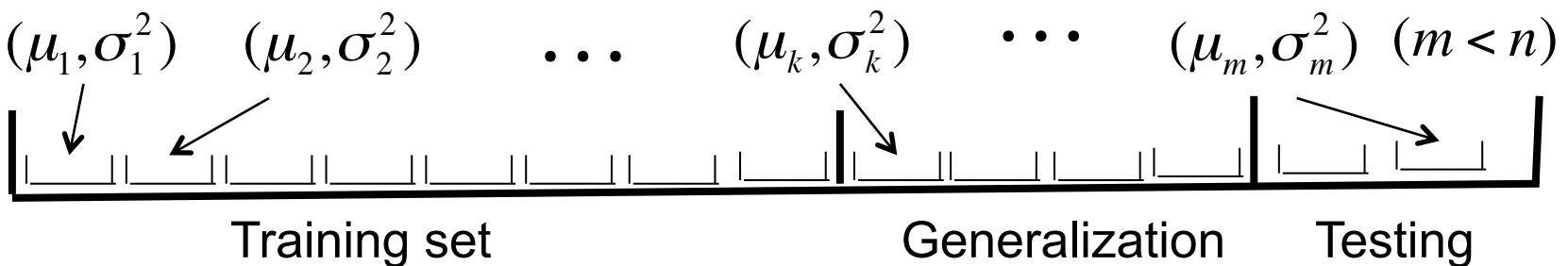
Uncertainty quantification by NN

Prediction: uncertainty quantification

Step-2: redesign the NN

A partition on the data-set used to define the neural fuser.

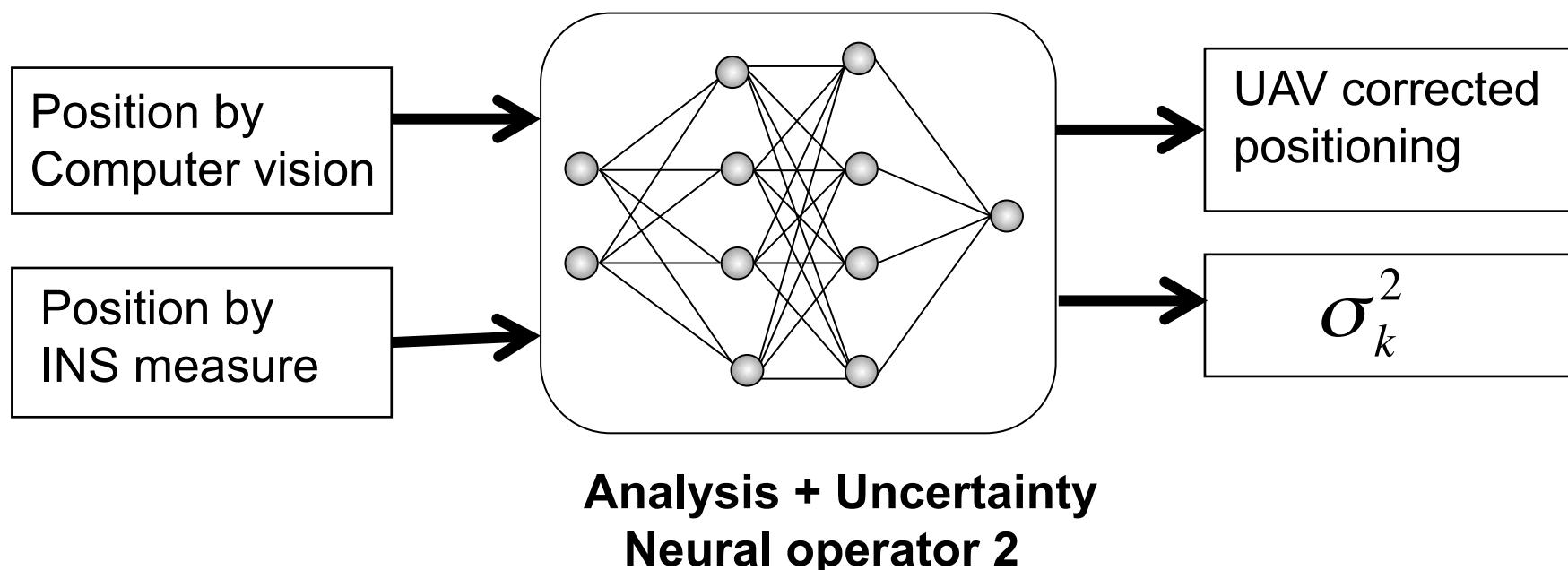
From the partition, with time series $\left\{(\mu_k, \sigma_k^2)\right\}_{k=1}^m$ new NN.



Drone positioning algorithm

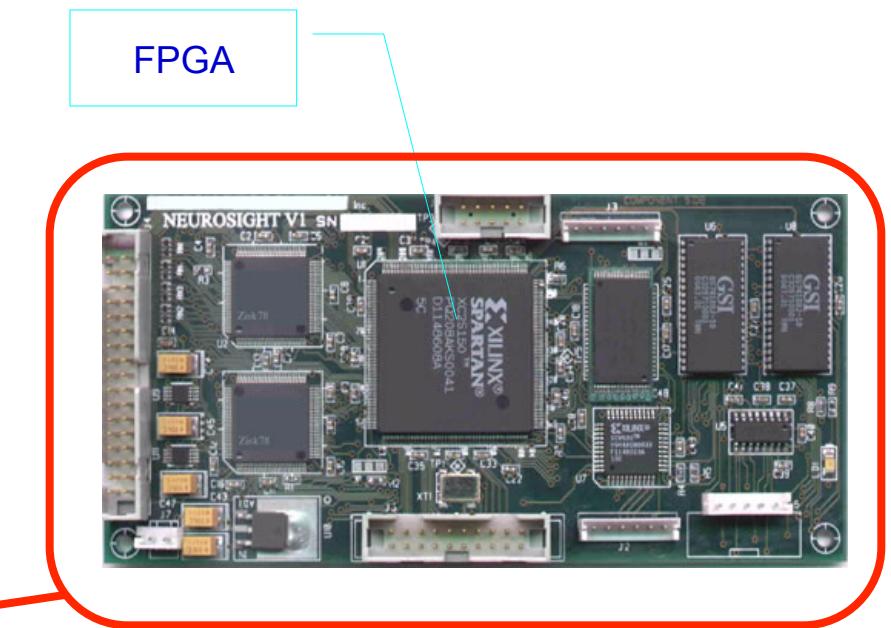
Positioning by NN: uncertainty quantification

Step-2: New neural fuser self-configured by MPCA



Data assimilation by NN: hardware components

The Cray XD1 - Reconfigurable Computing

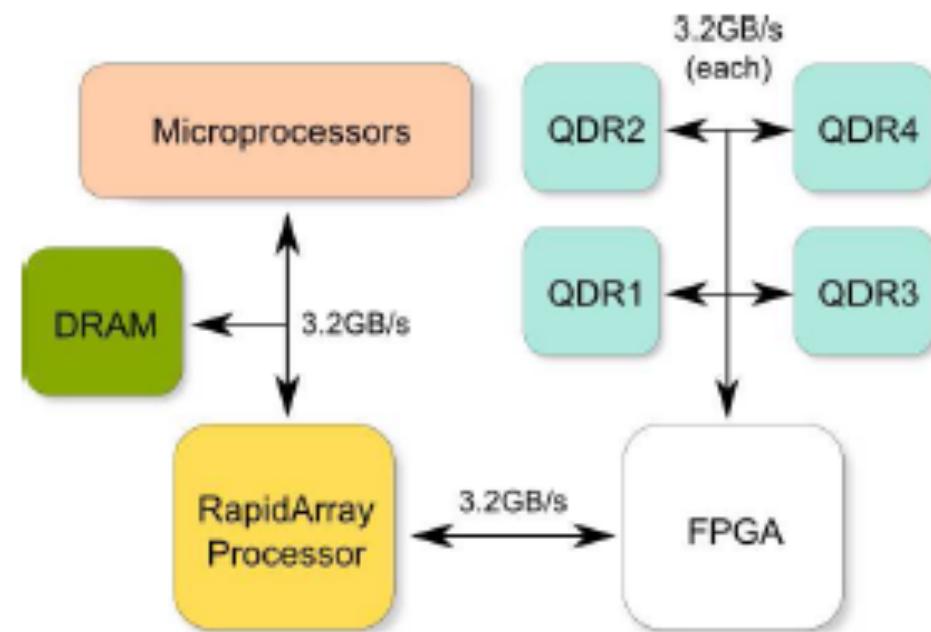


Hybrid computing with FPGA

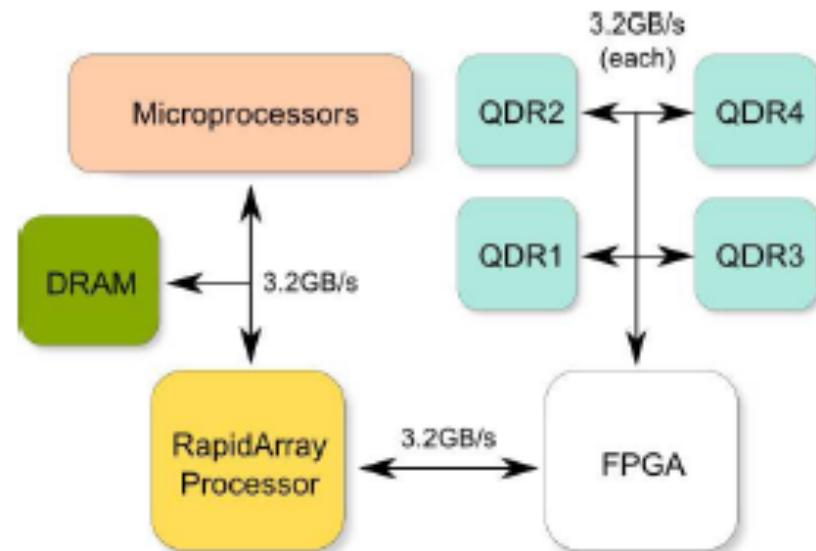
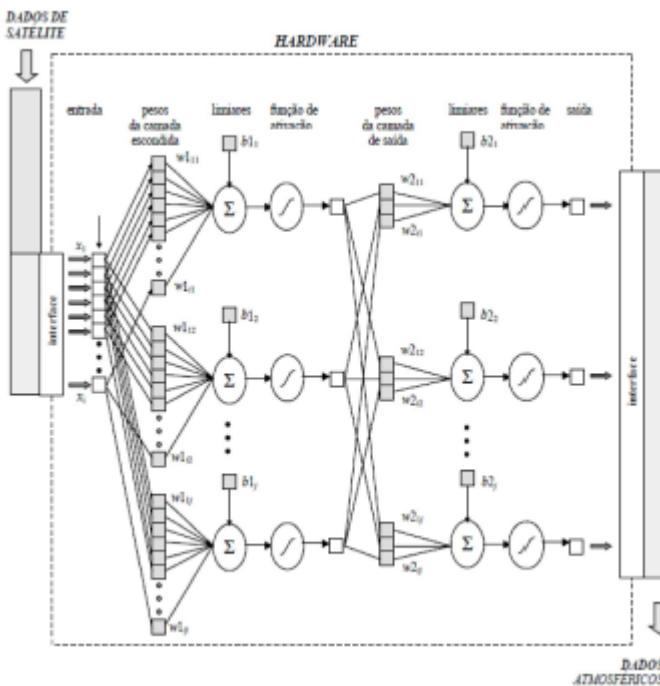
Blade
2 AMD Opteron 64bits 2.4GHz
1 FPGA Xilinx Virtex II Pro



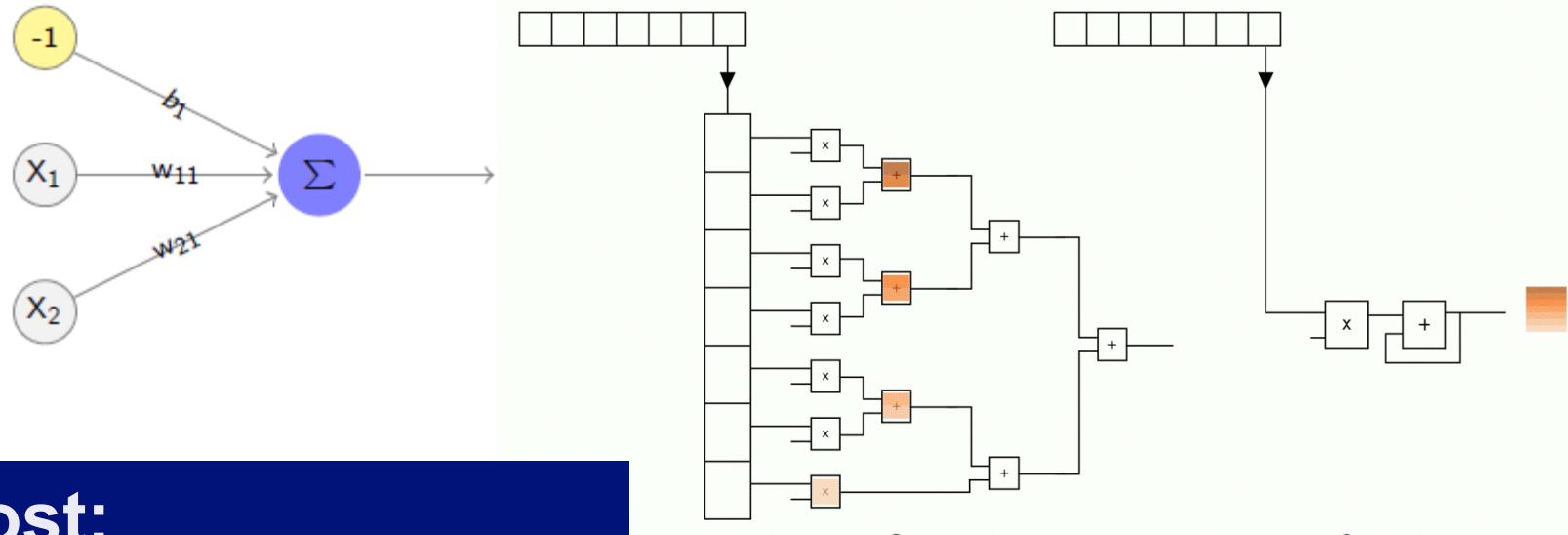
Cray XD1



Perceptron-NN for the Cray XD1



Perceptron-NN for the Cray XD1



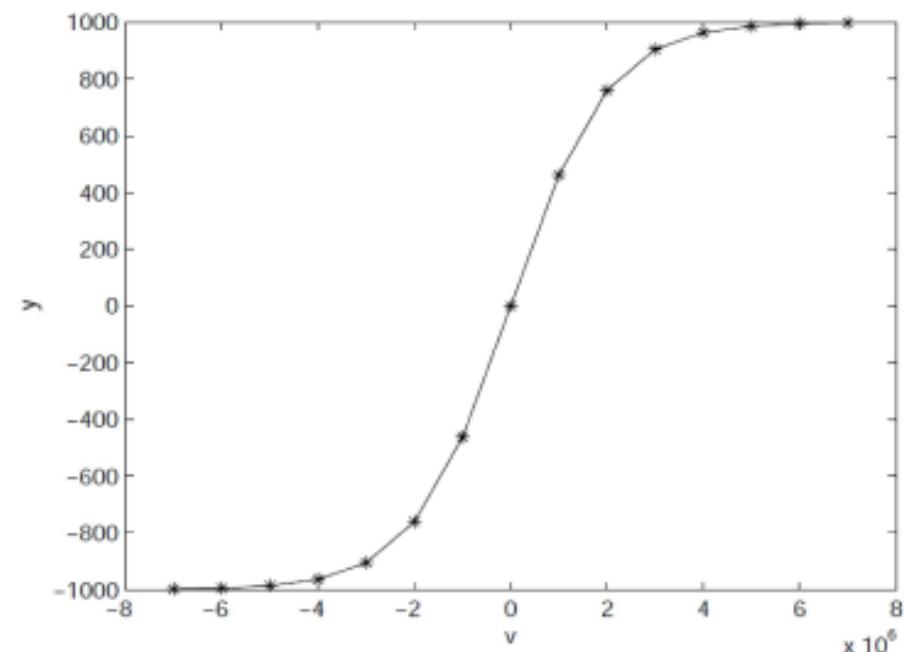
Cost:

- Multipliers: 7
- Summation: 1
- Cycles: $14 = 7 + 1 + 6$

Perceptron-NN for the Cray XD1

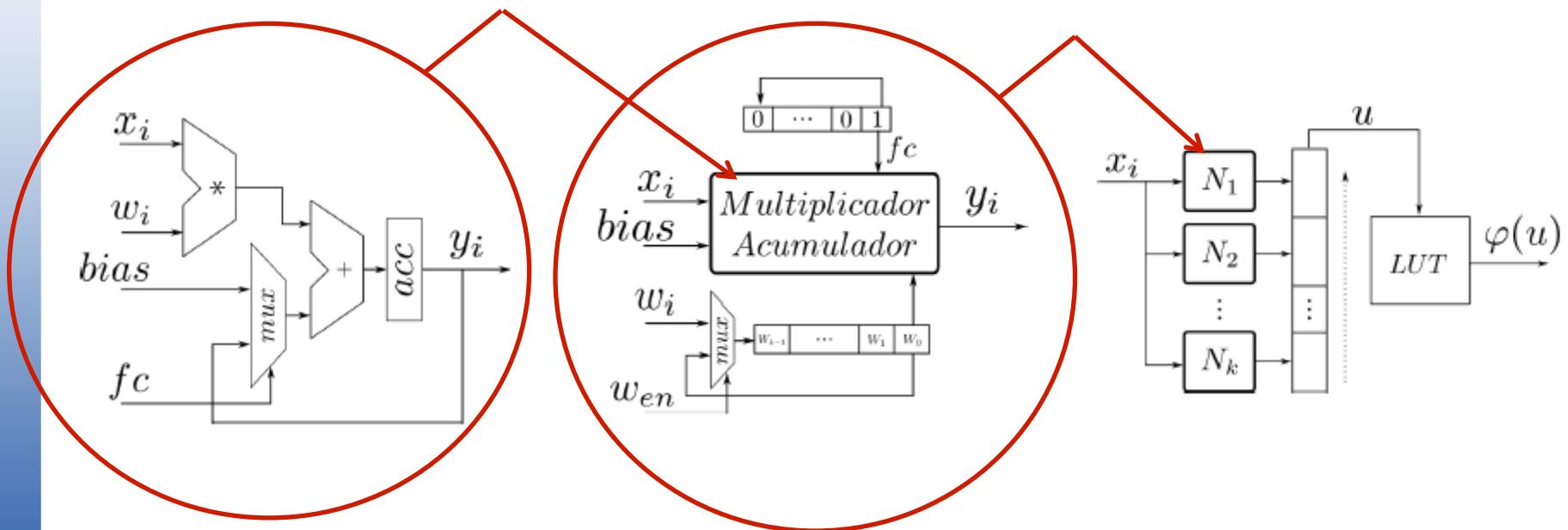
Activation function

- $\tanh(x)$
- Lookup Table (LUT)
- QDR: 1 M



Sigmoid function: $\tanh(x)$

Perceptron-NN for the Cray XD1

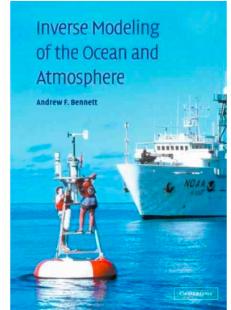


MAC:
Multiplier / accumulator
Input x weight
Stored on ACC or bias
(depending on fc signal)

Neuron
Uses of MAC

MLP-NN:
Combining neurons
Inputs connected by one bus
Ready to receive new data
Results to Lookup Table (LUT):
the pipeline

Shallow water 2D for ocean circulation



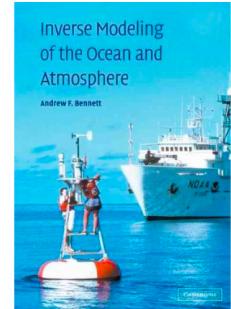
Process	Time (μs)
Software (CPU)	121709
Hardware (FPGA)	209187

$$\frac{\partial u}{\partial t} - fv + g \frac{\partial q}{\partial x} + r_u u = F_u$$

$$\frac{\partial v}{\partial t} + fu + g \frac{\partial q}{\partial y} + r_v v = F_v$$

$$\frac{\partial q}{\partial t} + H \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) + r_q q = 0$$

Shallow water 2D for ocean circulation



Process	Time (μs)
Software (CPU)	121709
CPU to FPGA	181365
FPGA	2
FPGA to CPU	9455
FPGA (Total)	209187

$$\frac{\partial u}{\partial t} - fv + g \frac{\partial q}{\partial x} + r_u u = F_u$$

$$\frac{\partial v}{\partial t} + fu + g \frac{\partial q}{\partial y} + r_v v = F_v$$

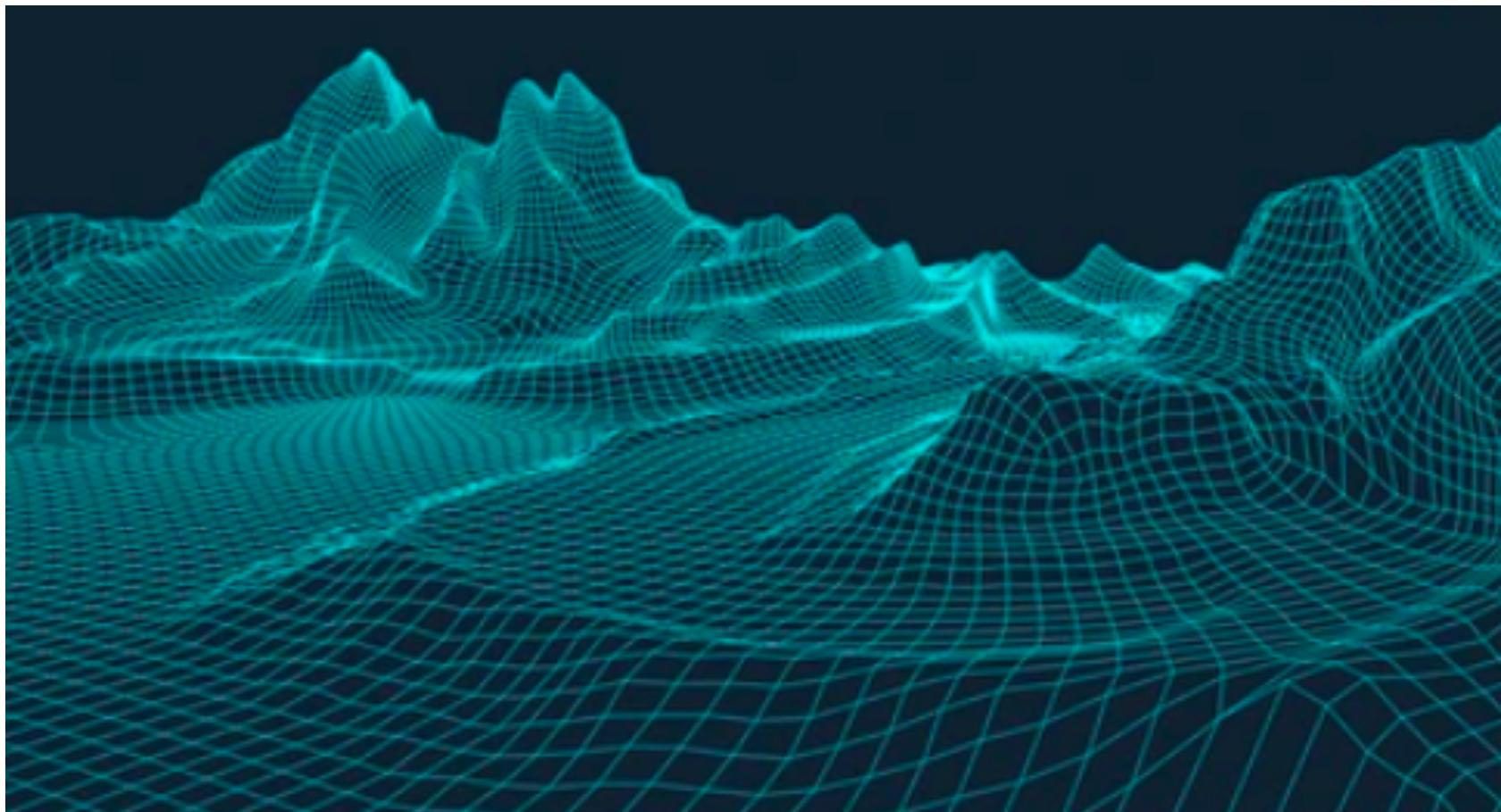
$$\frac{\partial q}{\partial t} + H \left(\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) + r_q q = 0$$

Weather and climate prediction

- Model (PDE) three components:
- Geophysical data
 - Topography
 - NDVI mapping
 - Soil type and soil moisture
- Dynamical core (Navie-Stokes equation "solver")
- Model physics
 - Surface model
 - Turbulence model
 - Radiative transfer model
 - Cloud formation and precipitation

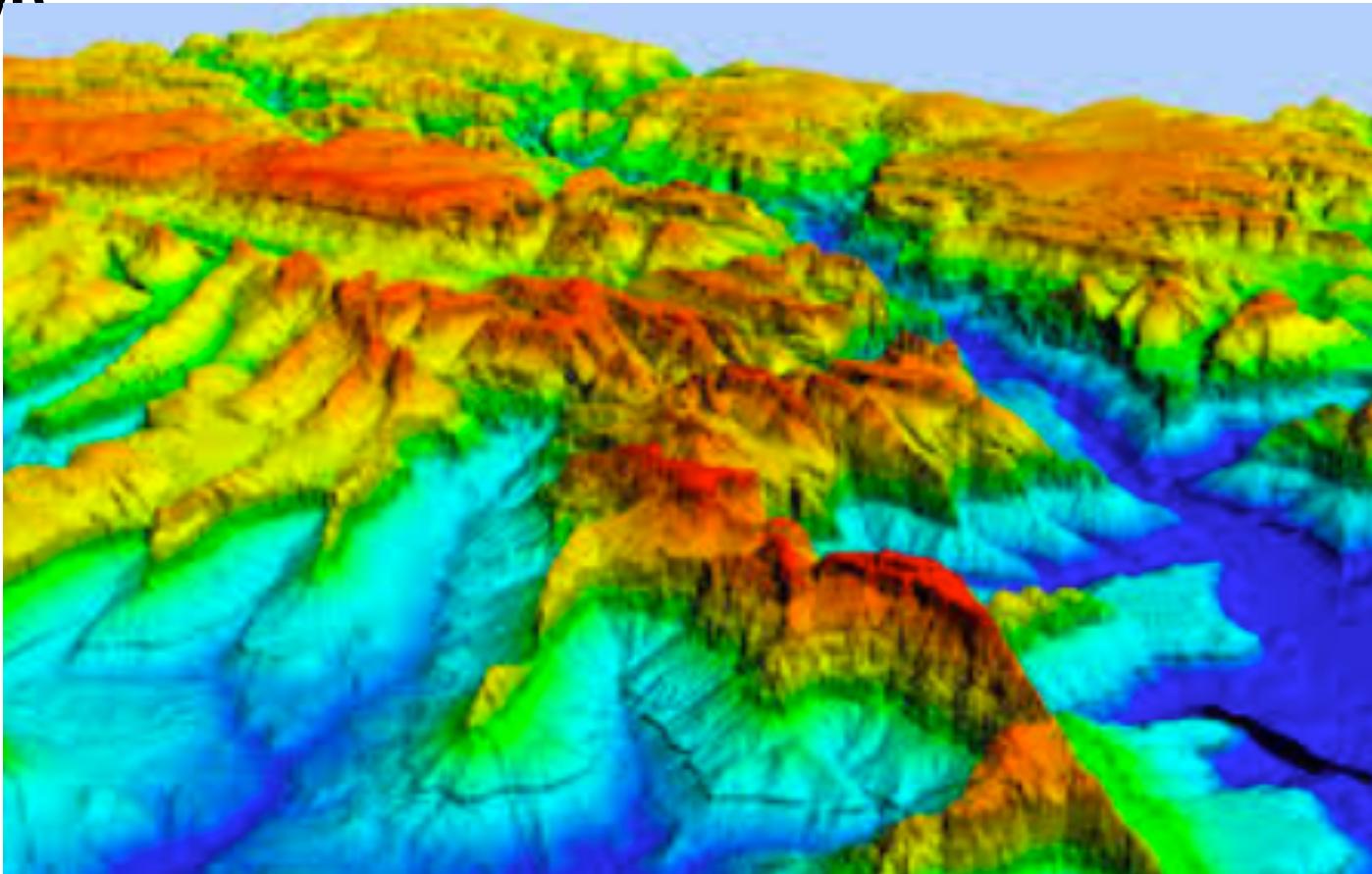
Weather and climate prediction

1.1 Topography data



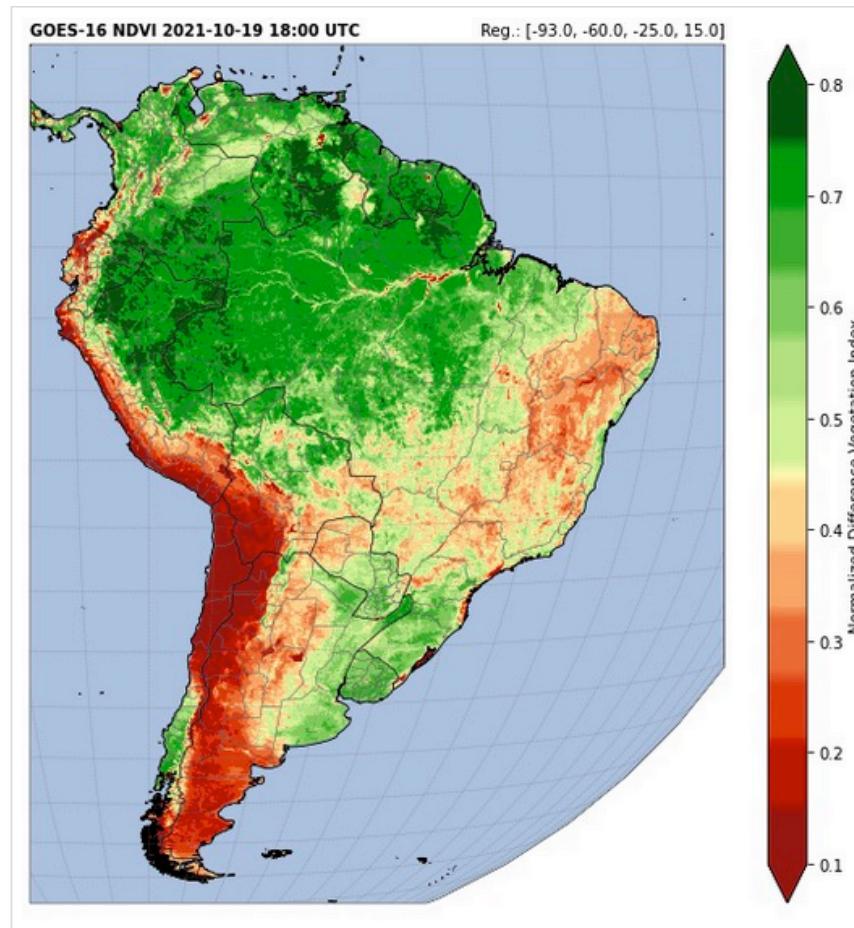
Weather and climate prediction

1.1/1.2 Topography data / surface covering map (NDV[“])



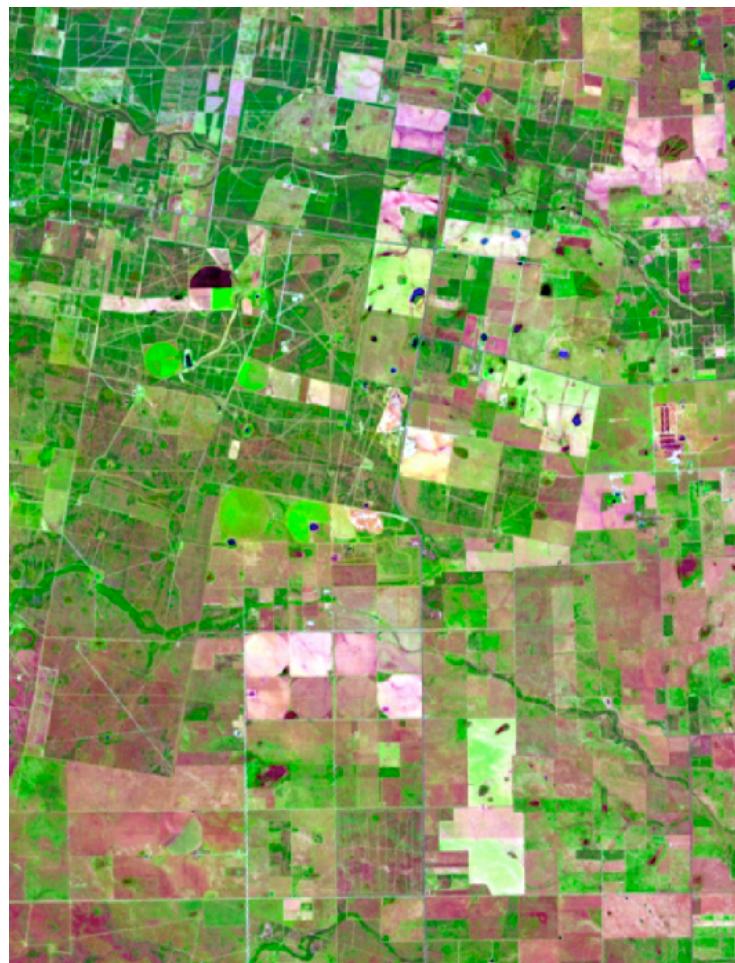
Weather and climate prediction

1.2 NDVI mapping



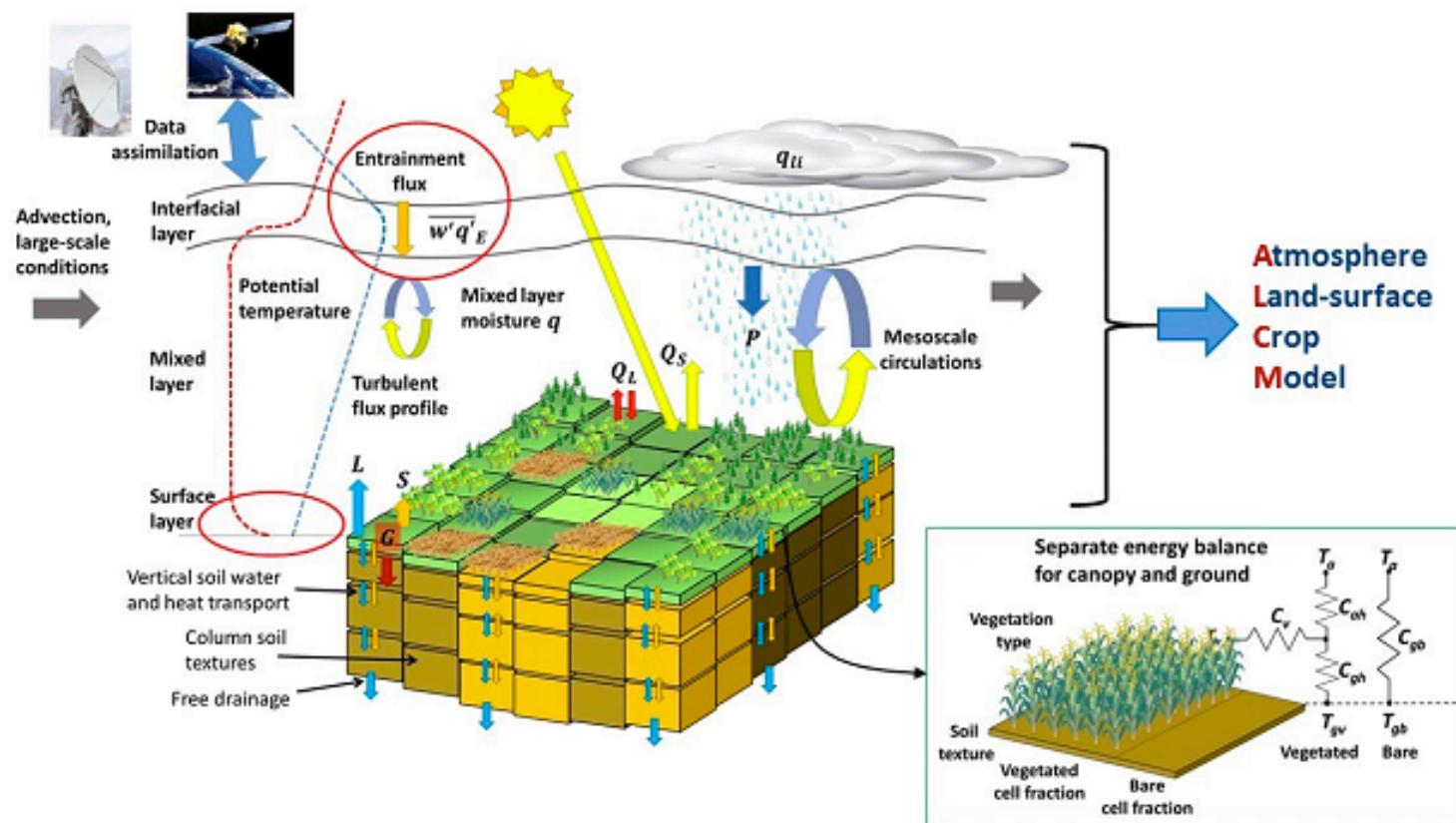
Weather and climate prediction

1.2 NDVI mapping



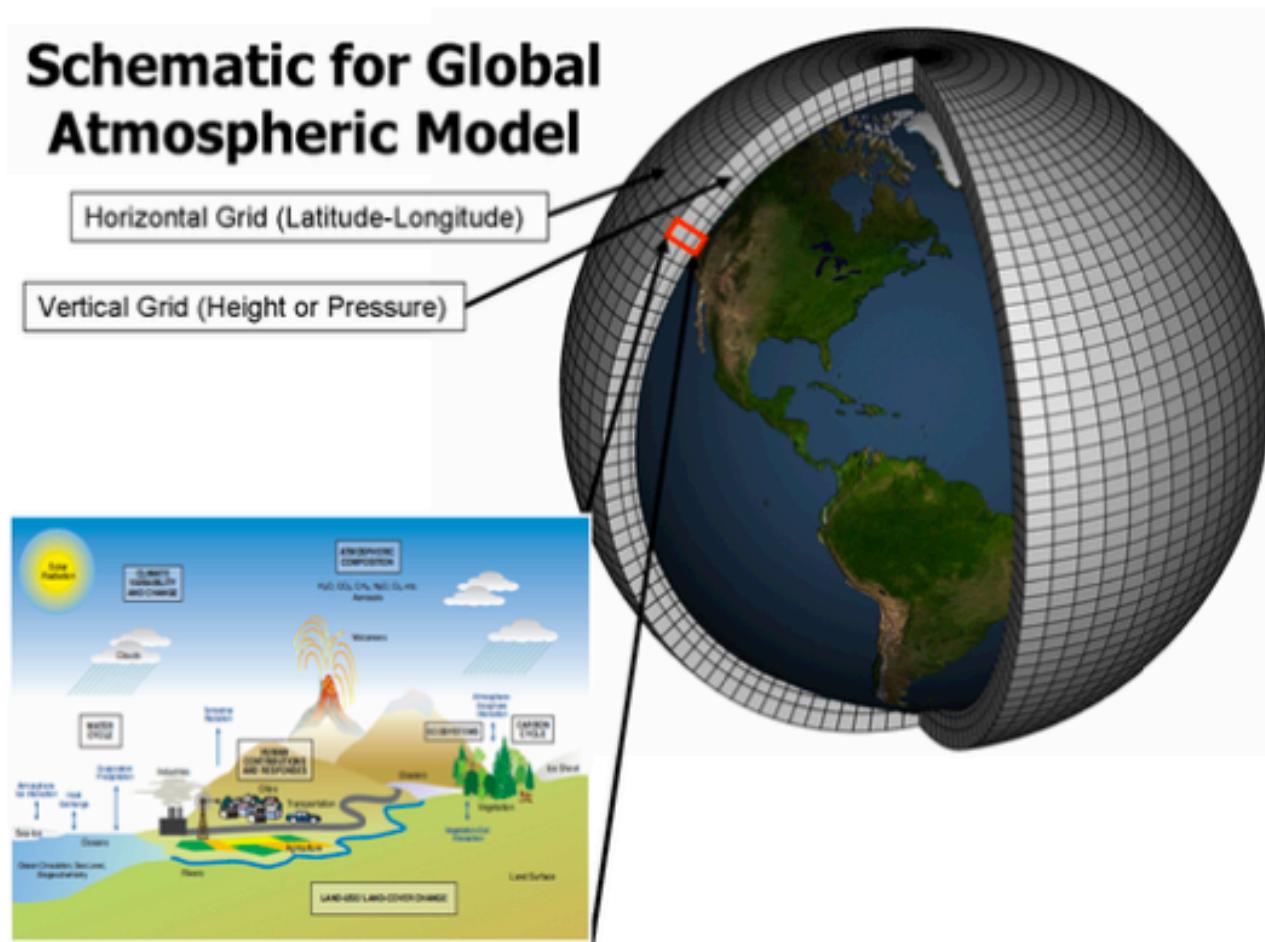
Weather and climate prediction

1.3 Soil type and soil moisture:



Weather and climate prediction

2. Dynamical core (Navie-Stokes equation "solver")



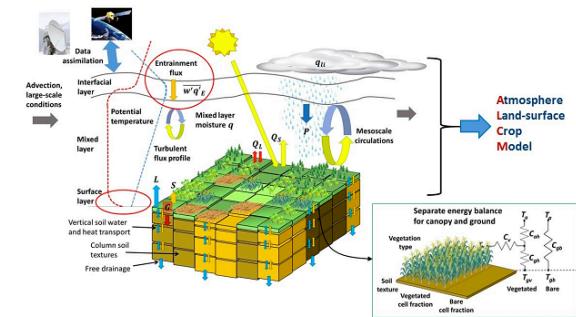
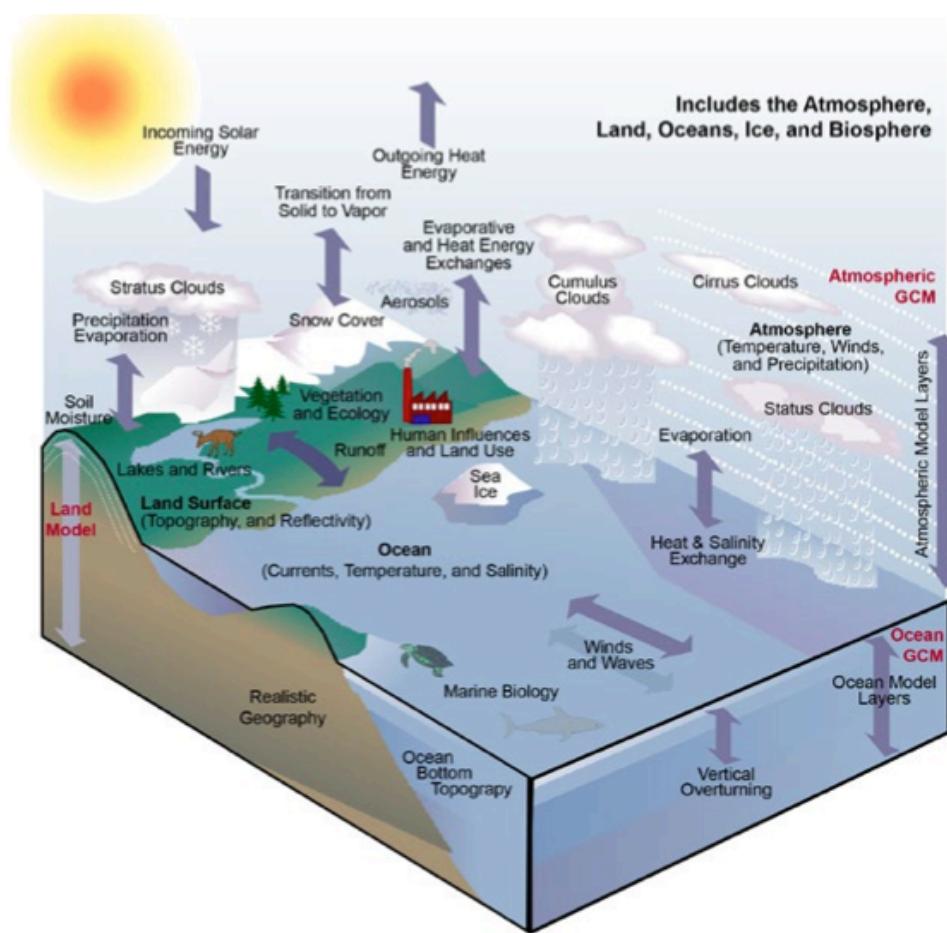
Weather and climate prediction

■ Dynamical core (Navie-Stokes equation "solver")

$$\begin{aligned}\frac{\partial \zeta}{\partial t} &= -\nabla \cdot (\zeta + f)\vec{v}_H - \vec{k} \cdot \nabla \times \left(RT\nabla q + \dot{\sigma} \frac{\partial \vec{c}_H}{\partial \sigma} - \vec{f} \right) \\ \frac{\partial D}{\partial t} &= \vec{k} \cdot \nabla \times (\zeta + f)\vec{v}_H - \nabla \cdot \left(RT\nabla q + \dot{\sigma} \frac{\partial \vec{c}_H}{\partial \sigma} - \vec{f} \right) - \nabla^2 \left(\phi + \frac{\vec{v}_H \cdot \vec{v}_h}{2} \right) \\ \frac{\partial T}{\partial t} &= -\nabla \cdot (T\vec{v}_H) + TD + \dot{\sigma}\gamma - \frac{RT}{c_p} \left(D + \frac{\partial \dot{\sigma}}{\partial \sigma} + H_T \right) \\ \frac{\partial q}{\partial t} &= -\vec{v}_H \cdot \nabla q - D - \frac{\partial \dot{\sigma}}{\partial \sigma} \quad \text{{with: } } q = \log(p_0) \\ \sigma \frac{\partial \phi}{\partial \sigma} &= -RT \quad \text{{with: } } \phi = gh \ ; \ \text{and: } \sigma = p/p_0 \\ \frac{\partial r}{\partial t} &= -\nabla \cdot (r\vec{v}_H) + rD - \dot{\sigma} \frac{\partial r}{\partial \sigma} + M\end{aligned}$$

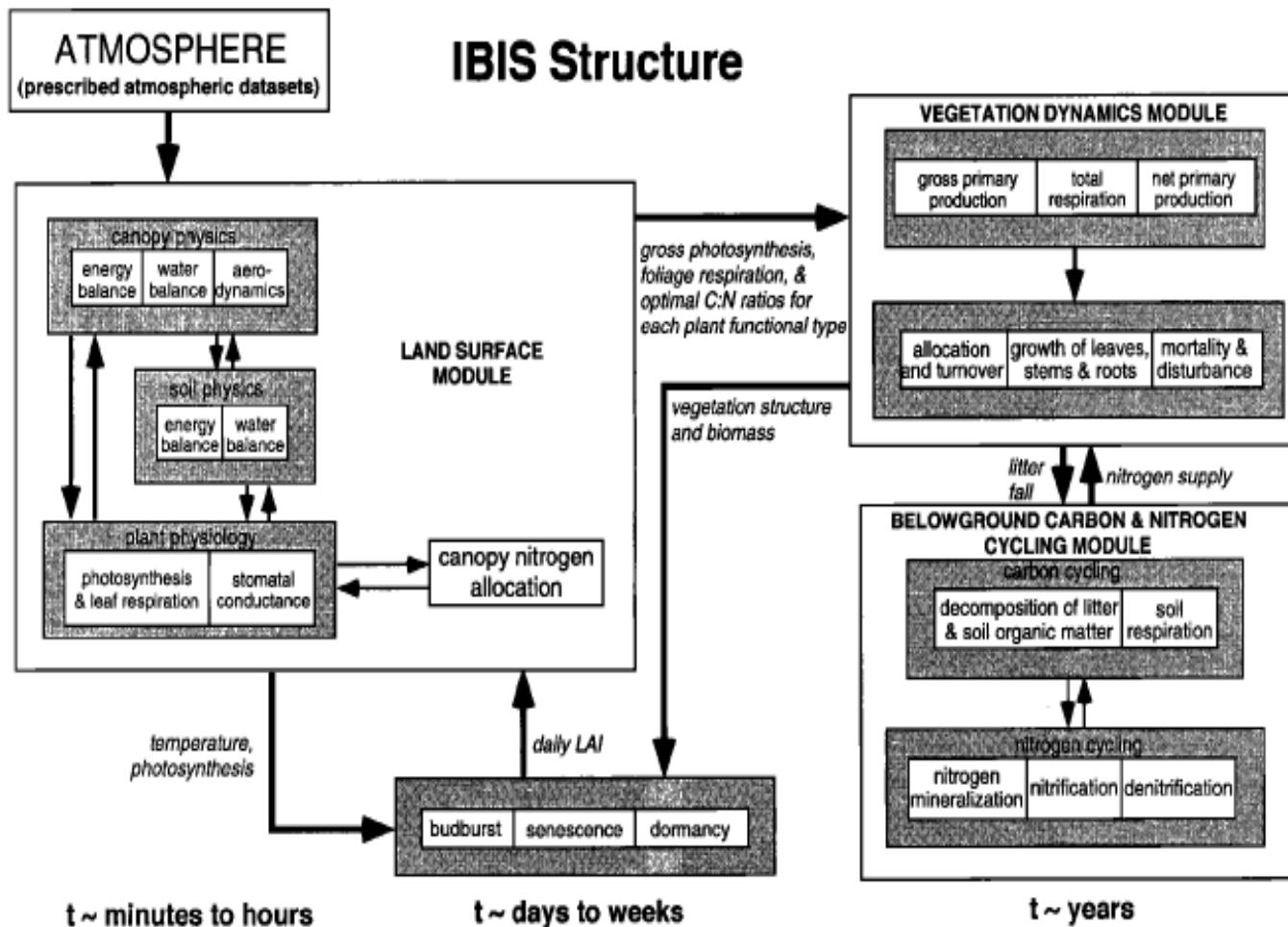
Weather and climate prediction

3.1 Model physics: Surface model



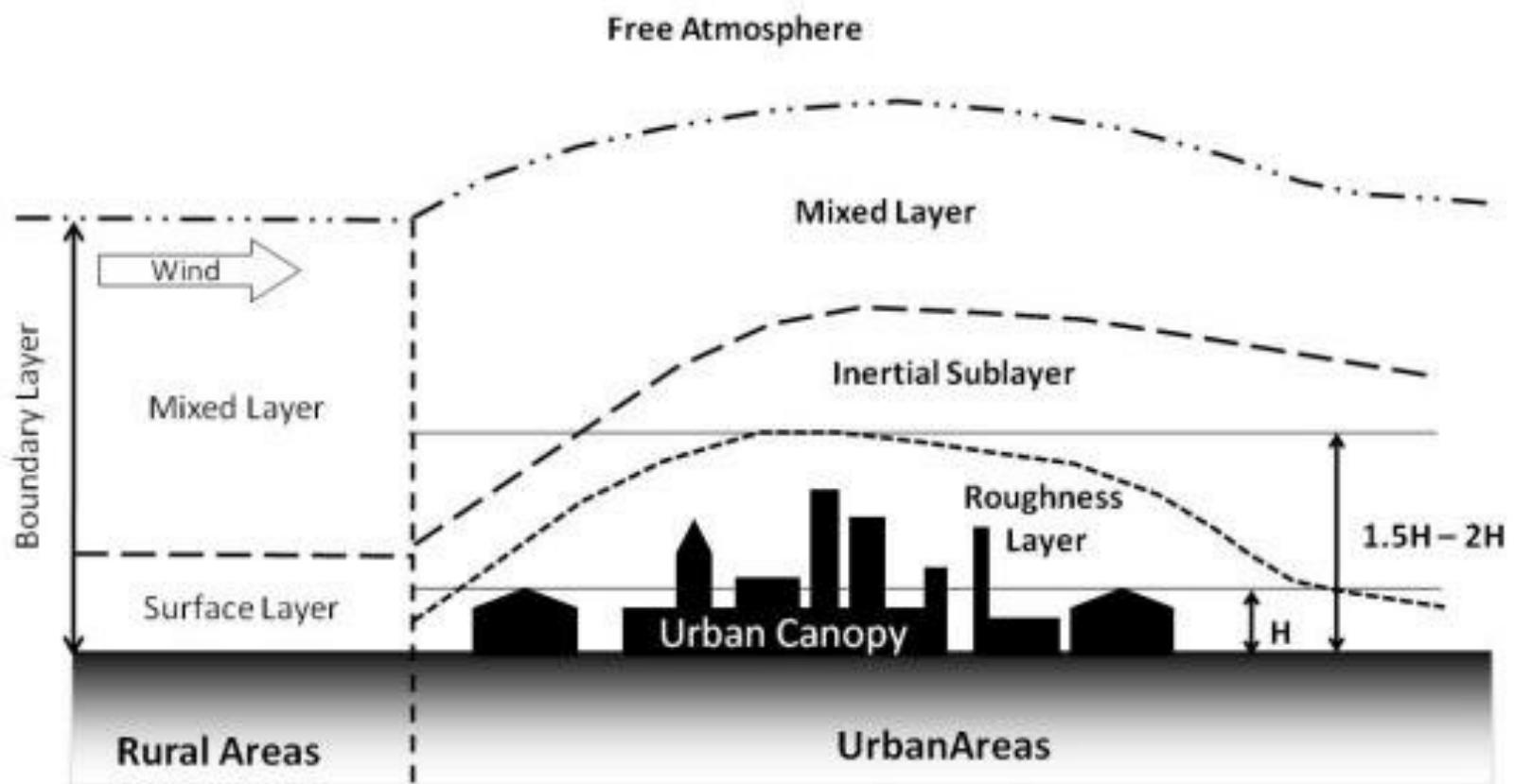
Weather and climate prediction

3.1 Model physics: Surface model



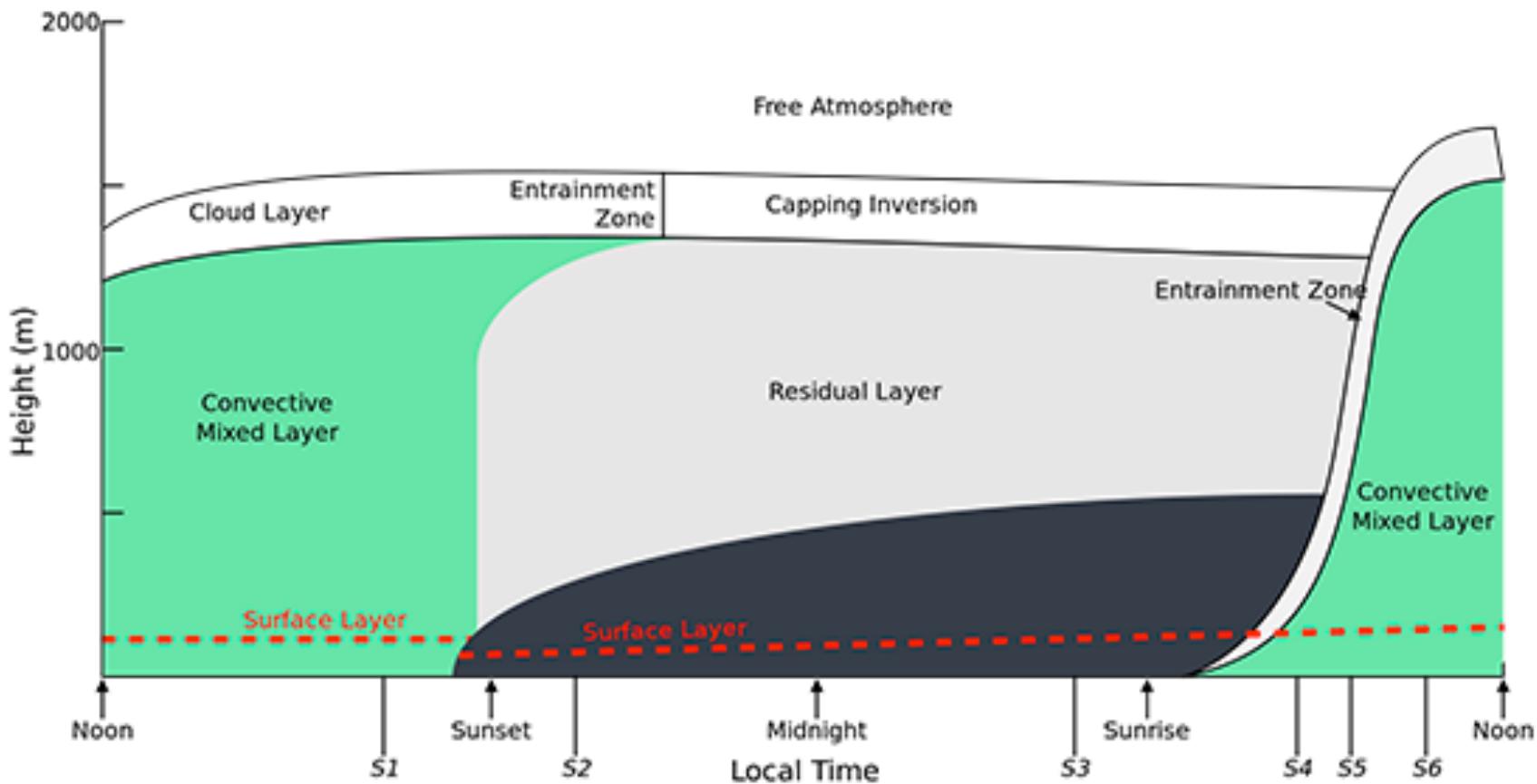
Weather and climate prediction

3.2 Model physics: Turbulence model



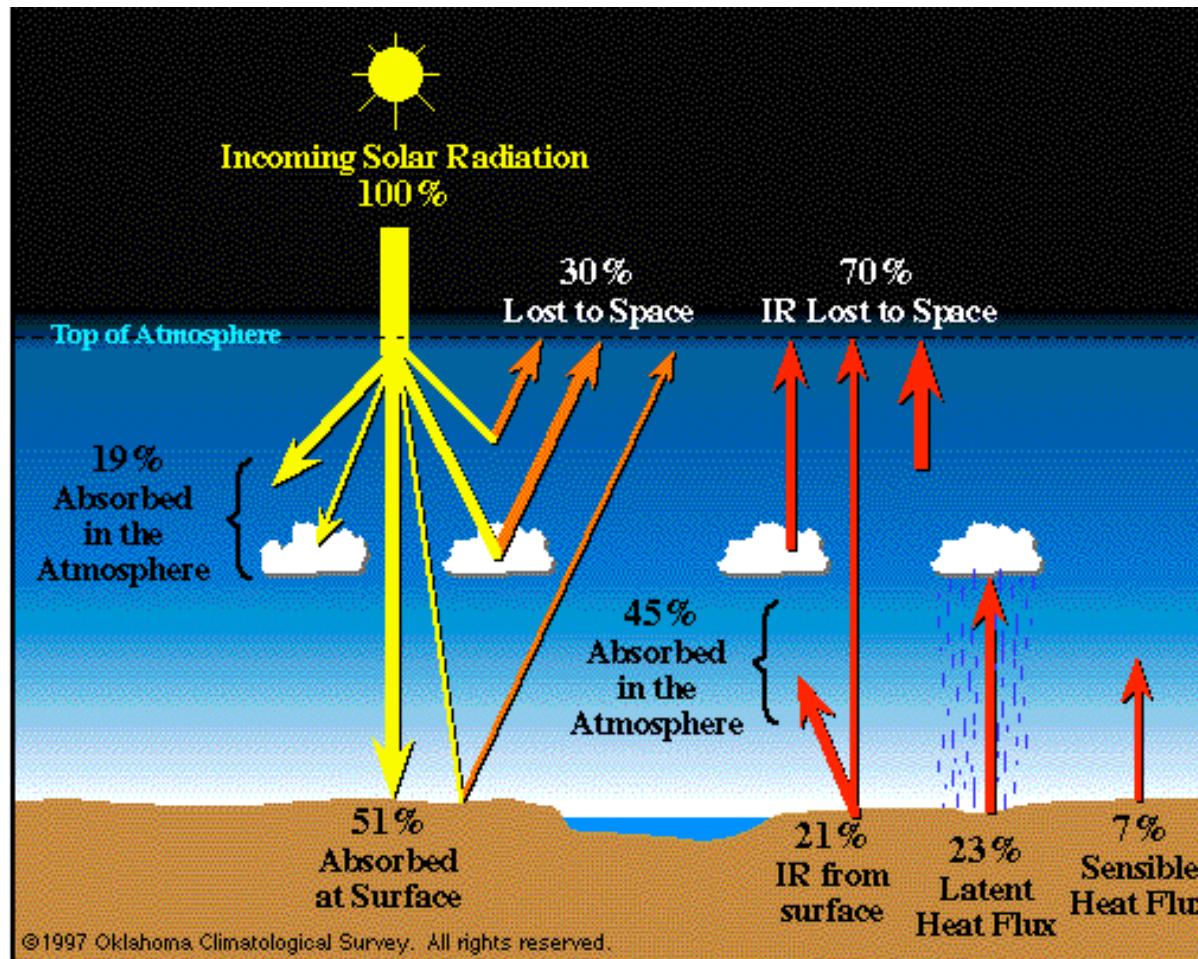
Weather and climate prediction

3.2 Model physics: Turbulence model



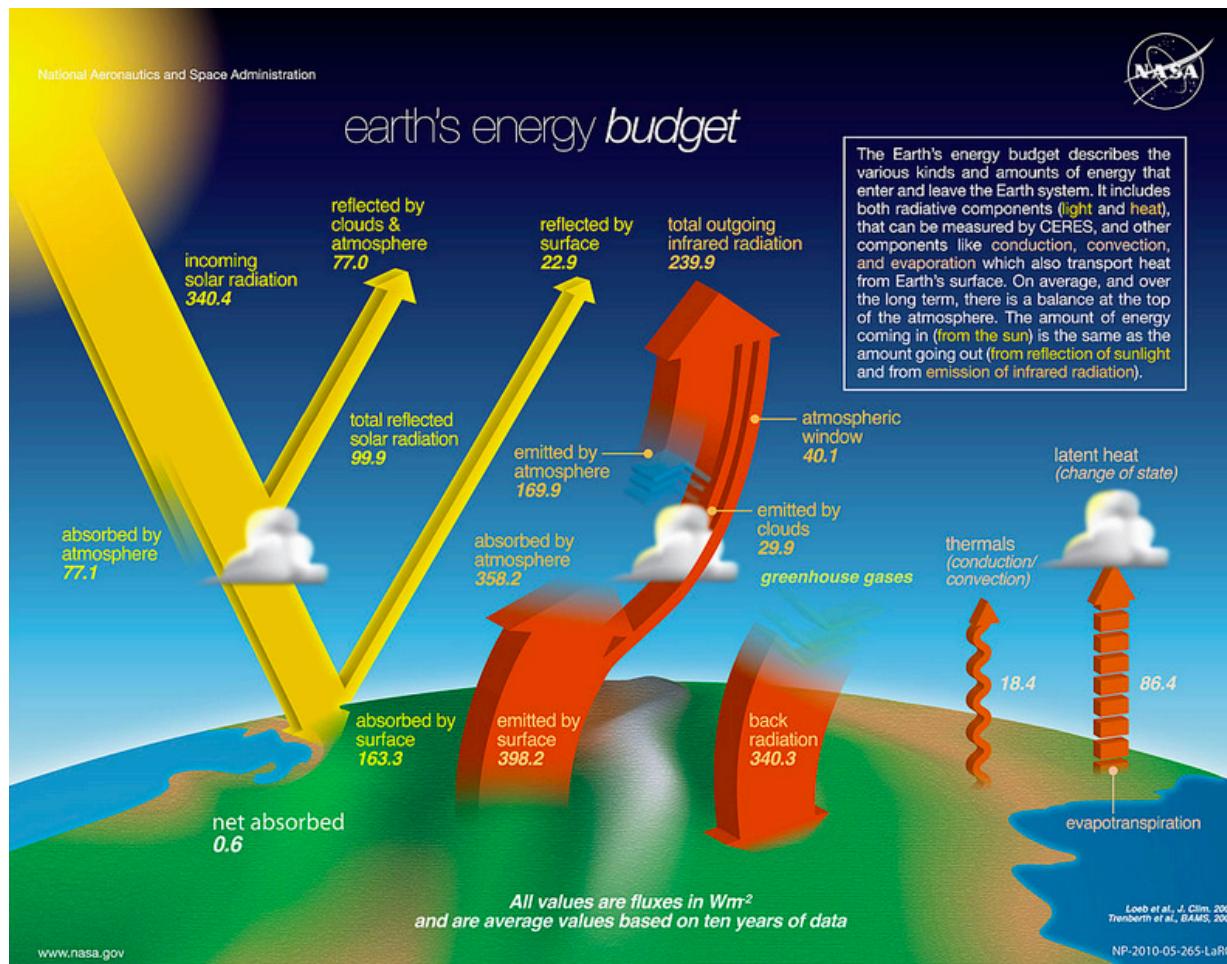
Weather and climate prediction

3.3 Model physics: Radiative transfer



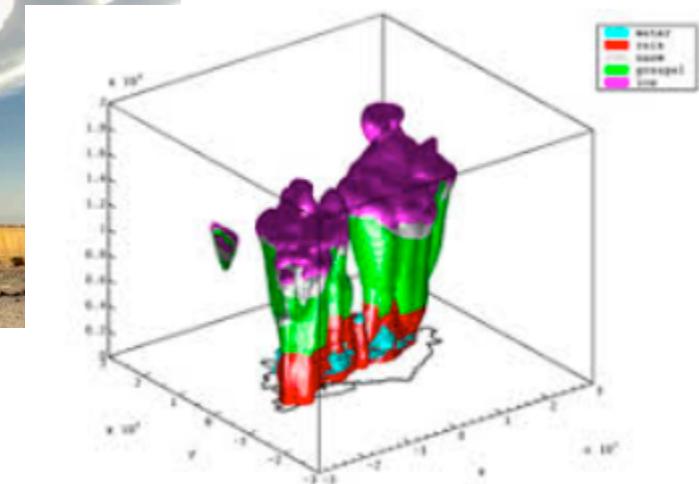
Weather and climate prediction

3.3 Model physics: Radiative transfer



Weather and climate prediction

3.3 Model physics: Cloud and precipitation



Data assimilation: what's that?

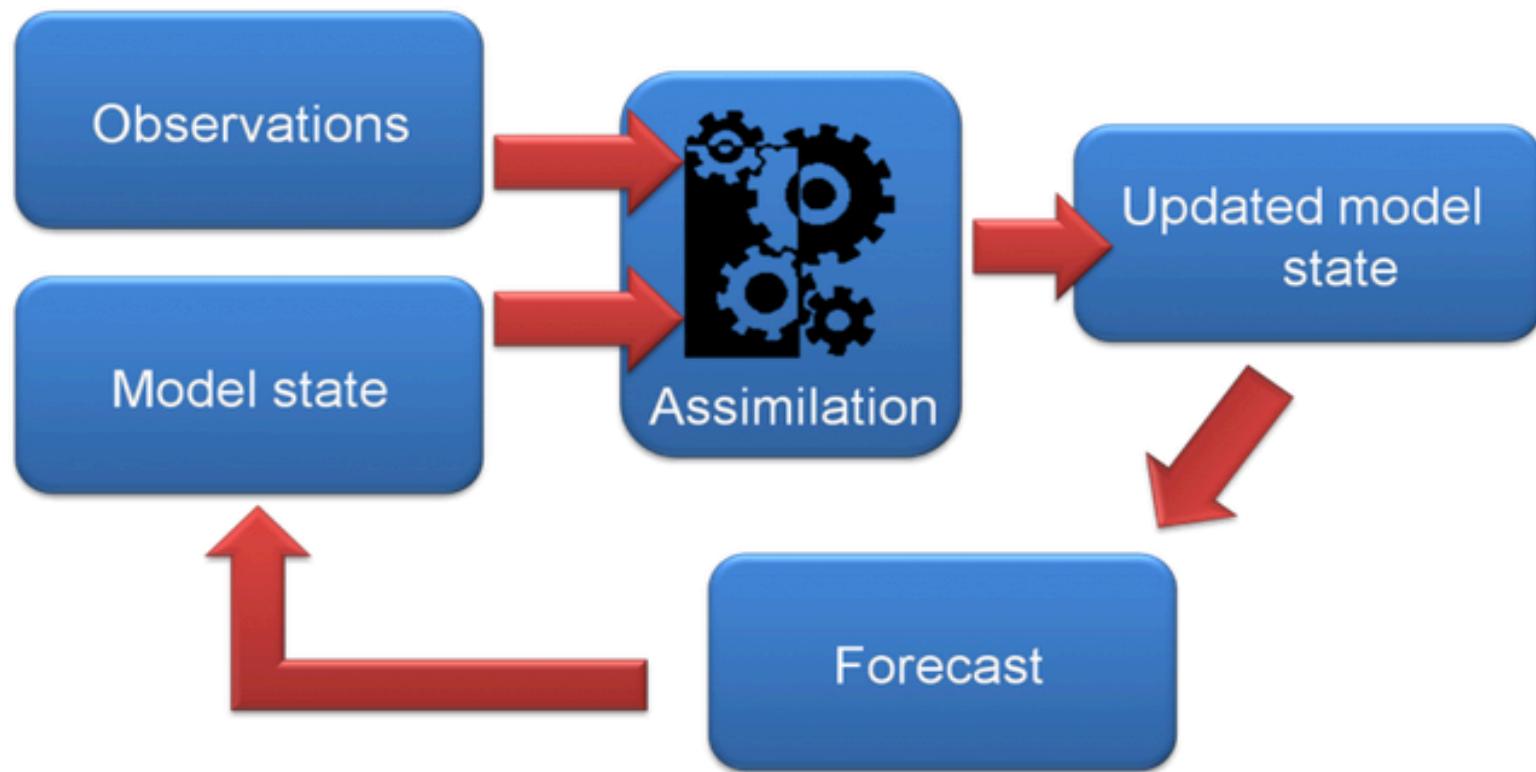


Figure Copyright: Prof. S. L. Dance
University of Reading 2022
Used with permission

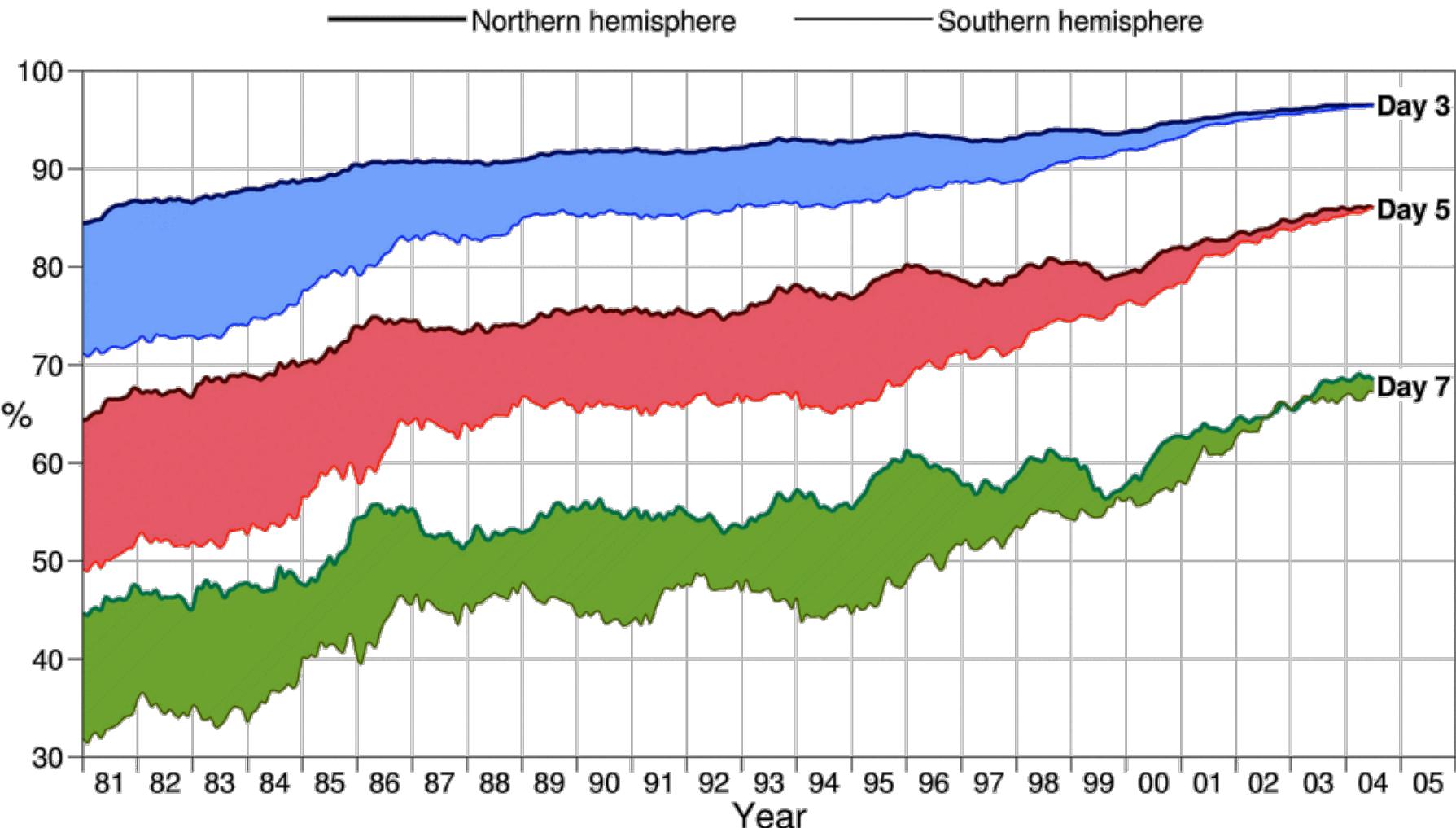
Data assimilation: what's that?



Forecasts Scores

ECMWF

Anomaly correlation of 500hPa height forecasts

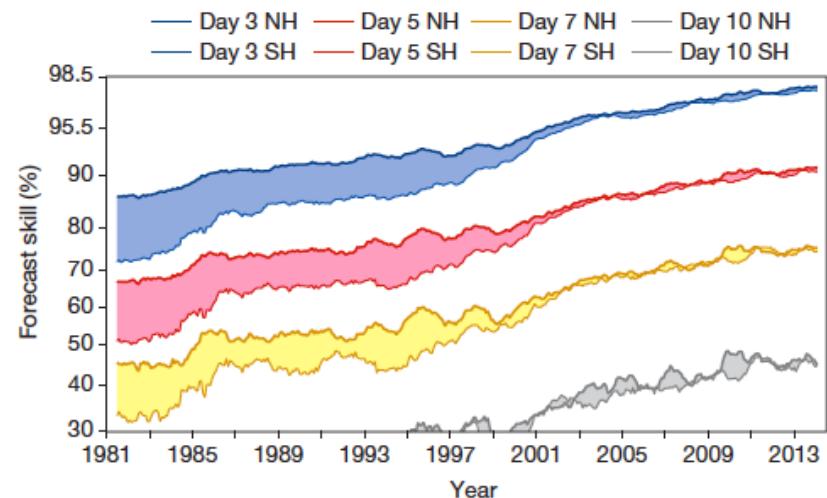


REVIEW

[doi:10.1038/nature14956](https://doi.org/10.1038/nature14956)

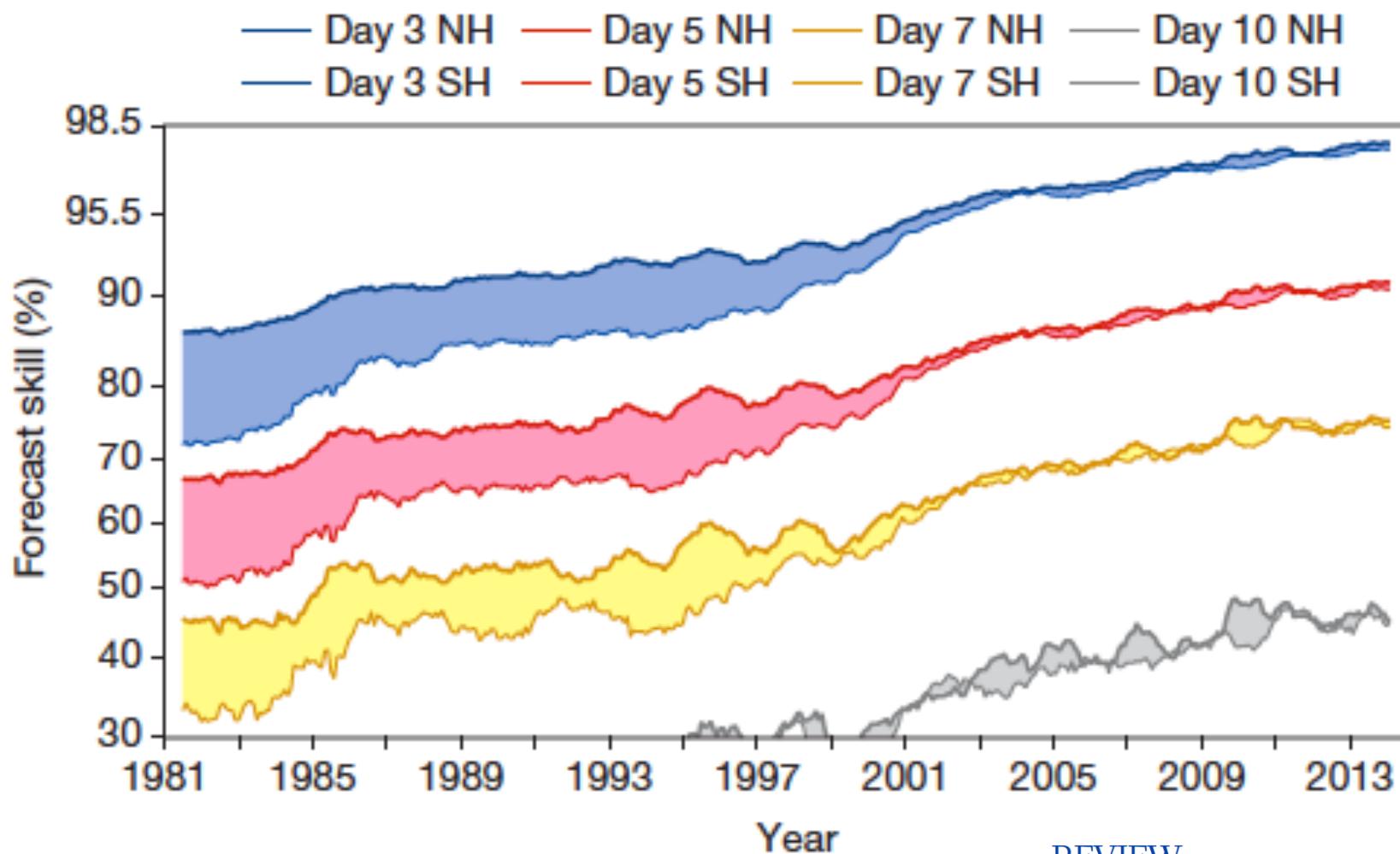
The quiet revolution of numerical weather prediction

Peter Bauer¹, Alan Thorpe¹ & Gilbert Brunet²



Forecasts Scores

ECMWF

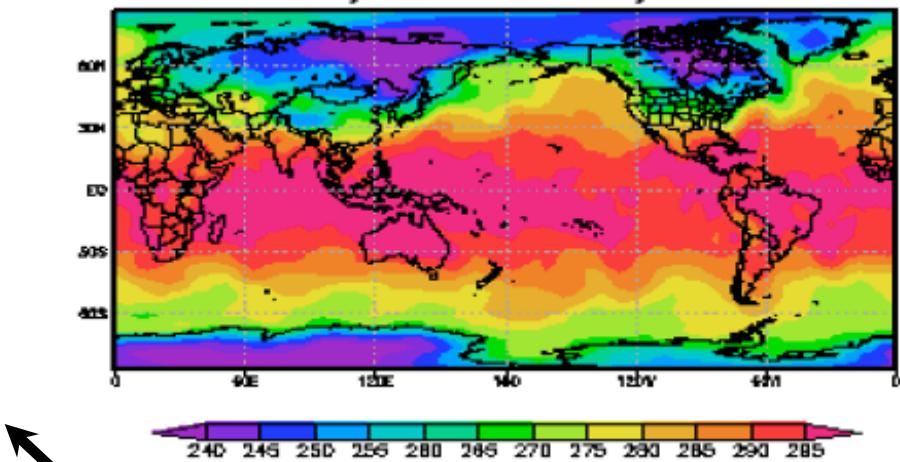
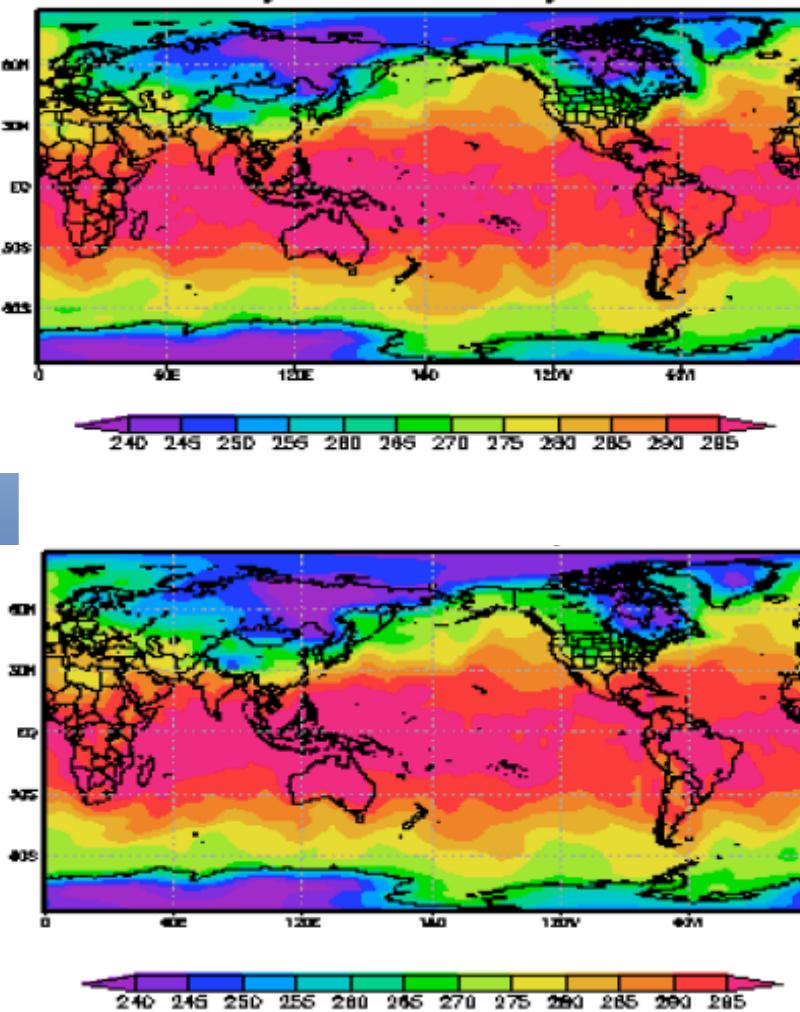


REVIEW

The quiet revolution of numerical weather prediction
Peter Bauer¹, Alan Thorpe¹ & Gilbert Brunet²

doi:10.1038/nature14956

Temperature: assimilation experiment

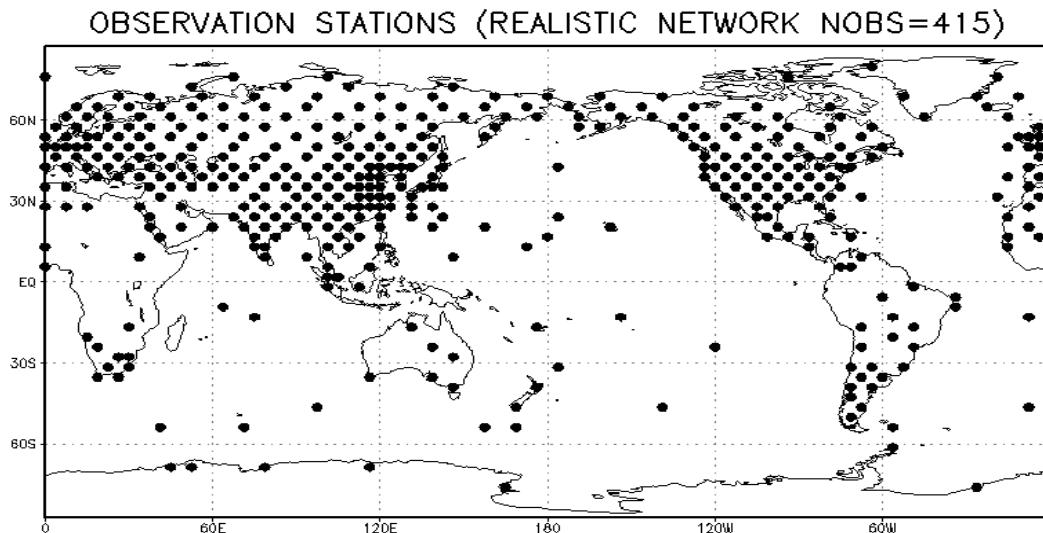


LETKF neural network

True

Results from Rosangela Cintra PhD thesis (2011)

Experiment: LETKF and neural network



Execution time	
LETKF method	ANN method
04:20:39	00:02:53
hours : minutes : seconds	

General atmospheric Circulation Modelo 3D (spectral model):

SPEEDY (Simplified Parameterizations primitivE Equation DYnamics)

Gaussian grid: 96 x 48 (horizontal) x 7 levels (vertical) = T30L7

Total grid points: 32.256 Total de variáveis: 133.632

Observations: (00, 06, 12, 18 UTC) – radiosondes “OMM stations”

Observations: 12035 (00 e 12 UTC) = $415 \times 4 \times 7 + 415$

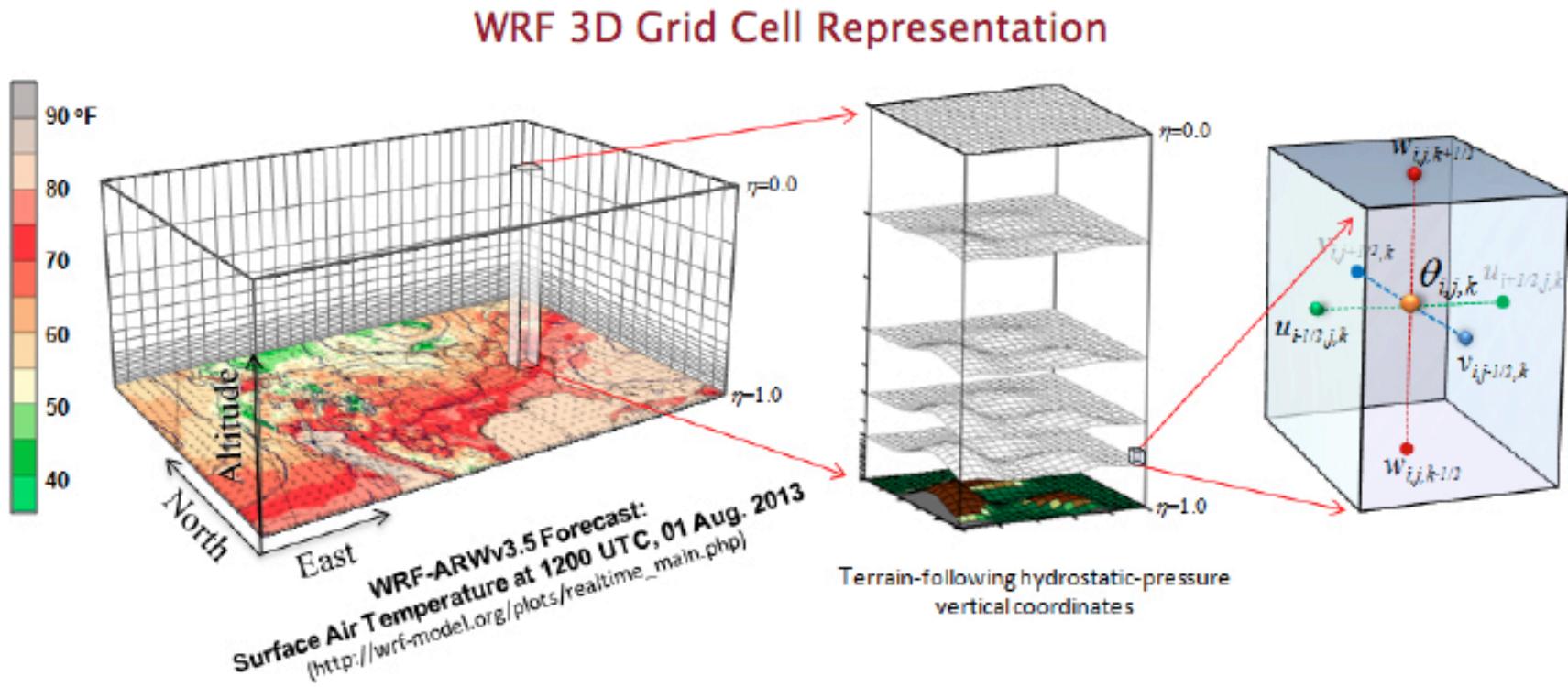
Observations: 2075 (00 e 12 UTC) = 415×5 (only surface)

Results from the Rosangela Cintra's PhD thesis (2011)

WRF: data assimilation 3D-Var x NN

■ Cooperation:

- CODPT-INPE (BR)
- Universities (BR): UFPel + IFI-Bagé + UFOPA + UFRJ
- LNCC (BR)



Thanks for our sponsors:

Brazilian agencies for research support:



*Conselho Nacional de Desenvolvimento
Científico e Tecnológico*



Thank you!