Study Notes

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List of Theorems

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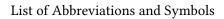
List of Definitions

A.1 Definition (Gaussian distribution) . . 27

LIST OF DEFINITIONS LIST OF DEFINITIONS

List of Abbreviations and Symbols

```
\begin{array}{lll} L & \text{Lagrangian. 25} \\ \hat{H} & \text{Hamiltonian. 25} \\ \mathbb{R} & \text{Real number. 10} \\ \vec{v} & \text{a vector. 10} \\ \end{array} GD Gradient Descent. 21
QFT Quantum Field Theory. 25
```



List of Abbreviations and Symbols

Preface

Contents

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0.1 Features of this template

TeX, stylized within the system as LTEX, is a typesetting system which was designed and written by Donald Knuth and first released in 1978. TeX is a popular means of typesetting complex mathematical formulae; it has been noted as one of the most sophisticated digital typographical systems.

- Wikipedia

0.1.1 crossref

different styles of clickable definitions and theorems

- nameref: Gaussian distribution
- autoref: Definition A.1, algorithm 1.5.1
- cref: Definition A.1,
- hyperref: Gaussian,

0.1.2 ToC (Table of Content)

- mini toc of sections at the beginning of each chapter
- list of theorems, definitions, figures
- the chapter titles are bi-directional linked

0.1.3 header and footer

fancyhdr

• right header: section name and link to the beginning of the section

- left header: chapter title and link to the beginning of the chapter
- footer: page number linked to ToC of the whole document

0.1.4 bib

- titles of reference is linked to the publisher webpage e.g., [Kit+02]
- backref (go to the page where the reference is cited) e.g., [Chi09]
- customized video entry in reference like in [Bab16]

0.1.5 preface, index, quote (epigraph) and appendix

index page at the end of this document...

0.1.6 symbol and glossary (abbreviation)

```
examples: \mathbb{R}, SVM, \vec{v}
```

usage

glossary package

```
pdflatex notes_template.tex
makeglossaries notes_template
pdflatex notes_template.tex
```

glossary-extra package and bib2gls

```
pdflatex notes_template.tex
bib2gls notes_template
pdflatex notes_template.tex
```

0.2 Related Tools

0.2.1 VSCode

Extension: Latex Workshop by James Yu

settings

0.2.2 lualatex and latexmk

```
.latexmkrc configuration file
```

To explain

```
# Also delete the *.glstex files from package glossaries-extra. Problem is,
# that that package generates files of the form "basename-digit.glstex" if
# multiple glossaries are present. Latexmk looks for "basename.glstex" and so
# does not find those. For that purpose, use wildcard.
$clean_ext = "%R-*.glstex";
push @generated_exts, 'glstex', 'glg';
add_cus_dep('aux', 'glstex', 0, 'run_bib2gls');
# PERL subroutine. $_[0] is the argument (filename in this case).
# File from author from here: https://tex.stackexchange.com/a/401979/120853
sub run_bib2gls {
    if ( $silent ) {
         my $ret = system "bib2gls --silent --group '$_[0]'"; # Original version
        my $ret = system "bib2gls --silent --group $_[0]"; # Runs in PowerShell
    } else {
        my $ret = system "bib2gls --group '$_[0]'"; # Original version
        my $ret = system "bib2gls --group $_[0]"; # Runs in PowerShell
    };
    my ($base, $path) = fileparse( $_[0] );
    if ($path && -e "$base.glstex") {
        rename "$base.glstex", "$path$base.glstex";
    }
    # Analyze log file.
    local *LOG;
    $LOG = "$ [0].glg";
    if (!$ret && -e $LOG) {
        open LOG, "<$LOG";
    while (<LOG>) {
            if (/^Reading (.*\.bib)\s$/) {
        rdb_ensure_file( $rule, $1 );
        }
    }
    close LOG;
    }
    return $ret;
}
```

0.2.3 Zotero and Better-bibtex

[todo] https://retorque.re/zotero-better-bibtex/ customized entry, e.g., Online Video

0.3 Copyright and License

- GitHub Repo: https://github.com/Jue-Xu/Latex-Template-for-Scientific-Style-Book
- Overleaf template: https://www.overleaf.com/latex/templates/latex-template-for-scientific-stylentprxjksmqxx

Part I Mathematics

Chapter 1

Discrete Math

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gls examples:

• Greatest Common Divisor (GCD); Greatest Common Divisor; GCD; Greatest Common Divisor (GCD)

1.1 Proof

Lemma 1.1.

Claim 1.1.

Theorem 1.1.

Example 1.1.

Fact 1.1.

Remark 1.1.

Exercise 1.1. Prove A iff B

Solution. By induction:

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1.2 Quantifier

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1.3 Graph

"Graph Isomorphism in Quasipolynomial Time" [Bab16]

1.4 Number theory

a Figure example

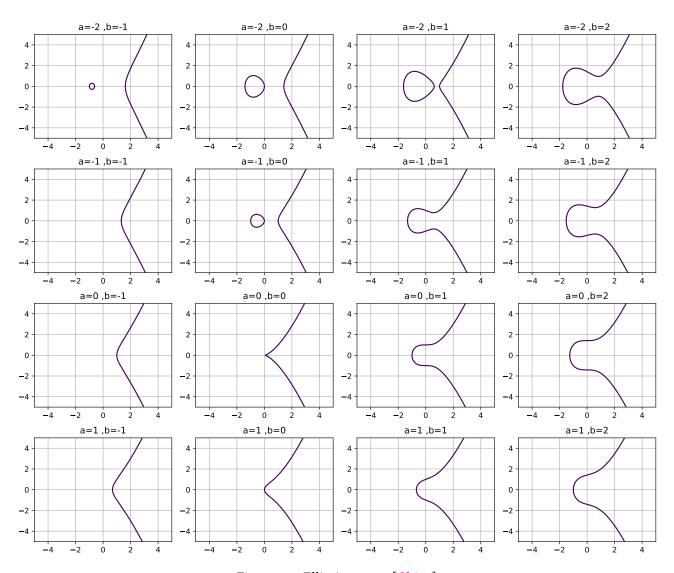


Figure 1.1: Elliptic curves [Chi09]

1.5 Algorithm

Part II Computer Science

Chapter 2

Machine Learning

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2.1	Reg	ression	
2.1.1	Gra	dient descent	
GD;			
2.2	Sup	port Vector Machine	
SVM;			



2.2 Support Vector Machine

Part III

Physics

Chapter 3

Quantum Mechanics

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3.1	Han	niltonian	
$\hat{H};$			
3.2 <i>L</i>	Patl	h Integral	
3.3	Qua	antum Field Theory	
QFT;			

Appendix A

Formulas

A.1 Gaussian distribution

Definition A.1 (Gaussian distribution). Gaussian distribution

Theorem A.1 (Central limit theorem).

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- [Bab16] László Babai. "Graph Isomorphism in Quasipolynomial Time". Jan. 19, 2016. arXiv: 1512.03547 [cs, math] (cit. on pp. 10, 17). Online video
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Alphabetical Index

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