

Accessing at given index -  $O(1)$ .

updating -  $O(1)$

inserting an item at beginning -  $O(n)$ .

Middle -  $O(n)$ .

End      ↗ Static -  $O(n)$

Dynamic -  $O(1)$

Removing Beginning -  $O(n)$

Middle -  $O(n)$

end -  $O(1)$

Copying an array -  $O(n)$ .

Sorting array -  $O(n \log n)$ .

→ static array  $\Rightarrow$  → fixed amount of memory to be used for storing the array's values.  
→ Appending values to array therefore involves copying the entire array and allocating new memory to it, Accounting for the extra space needed for newly appended value.  
↳ linear time operat'.

Dynam'ic Array : Pre-mtively allocates double the amount of memory needed to store the array's values. Appending values to the array is const time operation until the allocated memory is filled up. → if memory is filled up, array is copied & double the memory space is once again allocated for it.

↳ Amortized  $\text{Const}$  time insertion at end.

### ① Linear search

$\Rightarrow O(n, 1)$



input Key  $\rightarrow$  1      /      Key = 6  
 off  $\Rightarrow$  0      /      off = -1.

$\rightarrow$  loop over the array  
 till 0 to  $n-1$   
 if found return index

$\rightarrow$  return -1

### ② Binary Search.

$O(\log n, 1)$

↳ applicable only for sorted array.

key = 7

1	3	5	6	7
---	---	---	---	---

↑      ↑      ↑  
 Left      Mid      right  
 0                 $n-1$

while not ( $left < right$ )  
 left      right

$$mid = (\text{left} + \text{right}) // 2$$

if  $\text{arr}[mid] = \text{key}$  :  
 return mid.

else if  $\text{arr}[mid] < \text{key}$  :  
 left = mid + 1

else if  $\text{arr}[mid] > \text{key}$  :  
 right = mid - 1

### ③ largest elem in array

$O(n, 1)$

max = - infinite

loop through an array  $\rightarrow (0, n-1)$

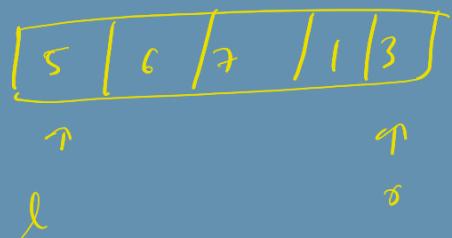
if  $\text{elem} < \text{max}$  :

    max = elem.

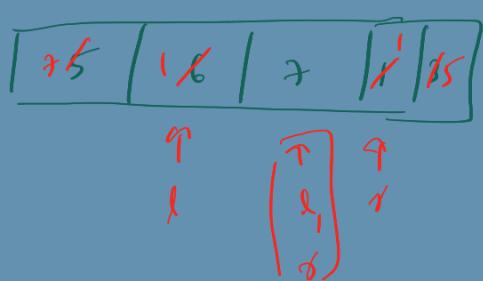
return max.

④

## Reverse Array.

 $O(n)$ 

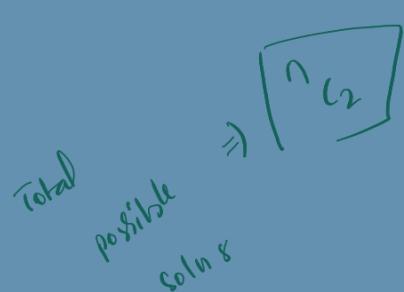
while  $l < r$ :  
swap  $\&$  nums, left, right



→ Pairs in an array

 $O(n^2)$ 

↳ combination .

 $(2, 4), (2, 6), (2, 8), (2, 10)$ ↳ nested loops.  
 $\sim O(n^2)$ . $(4, 6), (4, 8), (4, 10)$  $i \rightarrow 0 \rightarrow n-2$  $(6, 8), (6, 10)$  $j \rightarrow i+1 \rightarrow n-1$  $(8, 10)$ 

→ Subarrays

↳ continuous part of array

→  $O(n^2, 1)$

[ 2, 4, 6, 8, 10 ]

①

(2), (2, 4), (2, 4, 6), (2, 4, 6, 8), (2, 4, 6, 8, 10) - 5

4, (4, 6), (4, 6, 8), (4, 6, 8, 10) - 4

6, (6, 8), (6, 8, 10) - 3

8, (8, 10) - 2

Total sub arrays =  $\frac{n(n+1)}{2}$

10 - 1

• Maximum index difference.

(GFG)

$O(n^2, 1)$

[ 34, 8, 10, 3 ]

output ↗

→ conditions

↳  $i \leq j$

↳  $arr[i] \leq arr[j]$ .

Brute force:

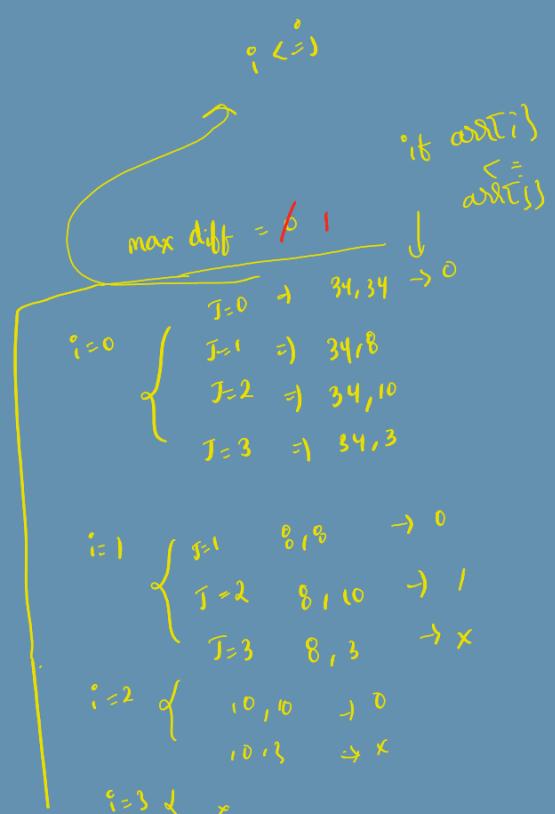
→  $O(n^2)$

[ 34, 8, 10, 3 ]

$i \rightarrow 0 \rightarrow n-1$

$j \rightarrow i, n-1$

if  $arr[i] \leq arr[j]$ :  
max diff:  
 $\max(\max \text{diff},$   
 $i, j))$



→ By Sliding window Approach.  $O(n), O(n)$

- conditions
- (1)  $i \leq j$
  - (2)  $\text{arr}[i] \leq \text{arr}[j]$

if condition satisfies  $\rightarrow$  increase window length / expand it ↑;  
else : decrease window length / contract it ↓  
by increasing  $i =$

{ 34, 8, 10, 3, 12, 80, 30, 33, 1 }

But how to check it

$\text{arr}[i] \leq \text{arr}[j] ??$

+ consider,

[ 10, 30  
 $i=2, j=6 \rightarrow \text{diff} = 6-2 = 4.$

maintain an arr for it.

II

if we take min elem from left to right our ans will be ↗ we can use prefix & suffix arrays  
optimum. ↘ left min ↘ right max.

[ 8, 30  
 $i=1, j=6 \rightarrow \text{diff} = 6-1 = 5$

Similarly if we take max elem from right to left it would be optim. ↗ maintain an array for it

[ 8, 33  
 $i=1, j=7 \rightarrow 7-1 = 6$

→ 34, 8, 10, 3, 12, 80, 33, 1  
start filling from left side choose the min elem.

$L_{\min} = \text{prefix arr} = [34, 18, 8, 3, 2, 2, 2, 1]$

$R_{\max} = \text{suffix arr} = [80, 80, 80, 80, 80, 33, 1]$

← it goes like this.



Theorem

- ① Winning state : State from which the current player can make  
(i) a move such that he directly wins or makes a  
(ii) move such that the opponent gets a losing state.
- ② Losing state : State from where no matter what move  
(i) you make the current player makes the  
opponent will always get a winning state.

1	1	1	1	0	1	1	1	1	0	1	1	1	1	0	1
↓	↖								↓						

As per  
losing state

Appd.

winning  
state part 2.

(oppo  
gft  
(losig  
state))

→ second largest elem of array:

→ sort array then choose last 2nd elem if sorted in ascending order.  
↳  $n \log n$ .

→ Optimal approach → 2 variables first, second.  
if no -ve num in arr.

first, second =  $\uparrow$  int::min value

for i in nums:

if  $i > \text{first}$ :

    second = first

    first = i

elif  $i > \text{second}$ :

    second = i

• Remove Duplicates from an array.

• if arr is sorted

$\boxed{1, 1, 2, 3, 3}$

check for before element.

$\Rightarrow \text{idx} = 1$

↳ start looping from first index

for i in range (1, n):

if arr[i-1] == arr[i]:

pass

else:

arr[idx] = arr[i]

idx += 1

O(n^2)

• if arr is not sorted.

↳ set  $\Rightarrow O(n, n)$

↳ default dict  $\rightarrow$  order is preserved  
 $\hookrightarrow O(n, n)$ .

↳ sort  $\Rightarrow O(n \log n, 1)$

order  
int  
preserved.

• Rotate Array - left by 1 step.

I/P = [ 10, 2, 5, 4, 2 ]

O/P = [ 2, 5, 4, 2, 10 ]

Approach  $\Rightarrow$

① copy the first element

temp = arr[0]

② loop through arr till

$\stackrel{n-1}{\equiv}$

not inclusive

for i in range (0, n-1):

arr[i] = arr[i+1]

③ set the last element

with temp.

arr[n-1] = temp

0  $\leftarrow 1$   
1  $\leftarrow 2$   
2  $\leftarrow 3$   
⋮  
n-1  $\leftarrow n$

• Rotate array - left by  $K$  steps.

$O(n+k, d)$ .

$$\text{arr} \Rightarrow \{1, 2, 3, 4, 5, 6, 7\}$$

$$K \Rightarrow 3$$

$$0 \mid P \Rightarrow 4, 5, 6, 7,$$

① Brute force.

↳ Store first  $3$  elements in temp array.

↳ Shift the elements ie, from  $K$  to  $\underbrace{n-1}_{[K, n)}$

↳ Put back those temp

$$\text{from } [n-K] \text{ to } n)$$

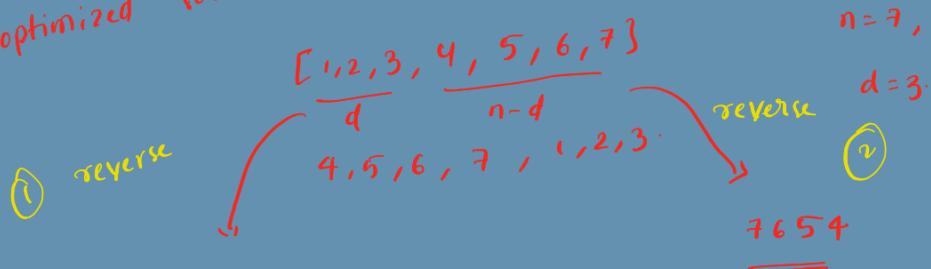
$i = n-K$  if we subtract  
↑ them from  
base index  $\Rightarrow i - (n-K)$

$0, 1, 2, \checkmark$

or  
we can use the  $T=0$   
in increment it as we

go

optimized (dn):



$$n=7,$$

$$d=3$$

$$\underline{\underline{7654}}$$

$$\underline{\underline{3,2,1}}$$

$$\rightarrow 3 \ 2 \ 1 \ 7 \ 6 \ 5 \ 4$$

$$4 \ 5 \ 6 \ 7 \ 1 \ 2 \ 3$$

(3) reverse it again  $\Rightarrow$

✓

→ Similar Approach for Right rotate By 1 & K.





