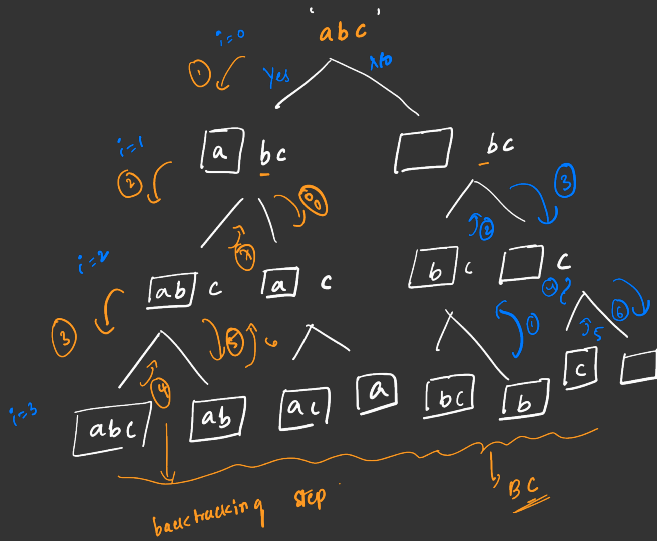


Finding * Subsets

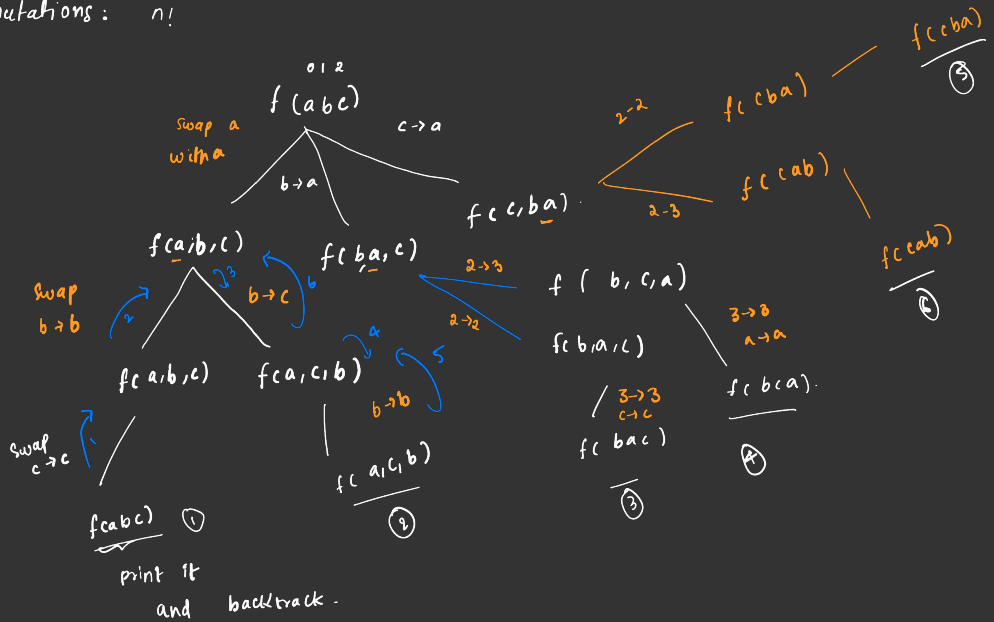
(2^n) subsets

of length n .

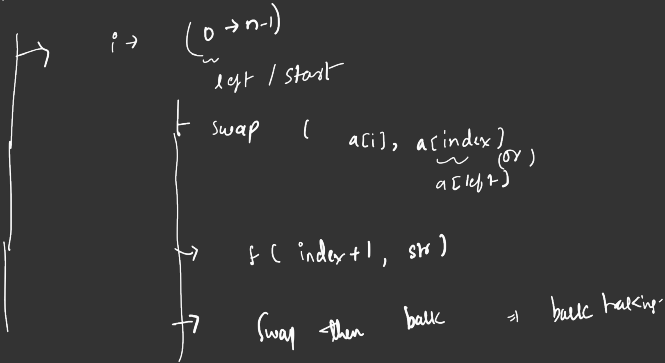
$abc \Rightarrow "", a, b, c, ab, bc, ac, abc.$



Permutations: $n!$



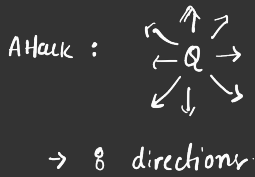
$f(index, str)$



N Queen.

↳ n queens puzzle is the problem of placing n queens on an $n \times n$ chess board such that no 2 queens attack each other.

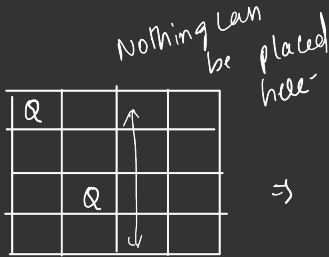
$N = 4$.



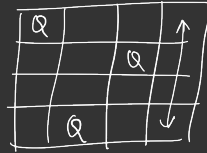
Rules :

- ① every row should have a queen
- ② every col should have a queen
- ③ None of them should attack each other.

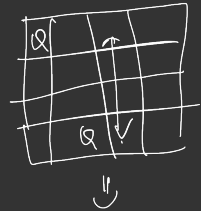
①



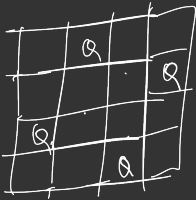
⇒



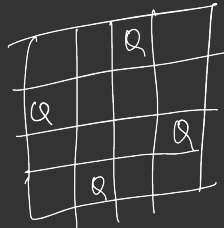
⇒



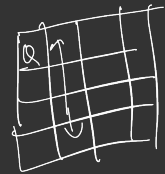
⇓



⇐



⇐



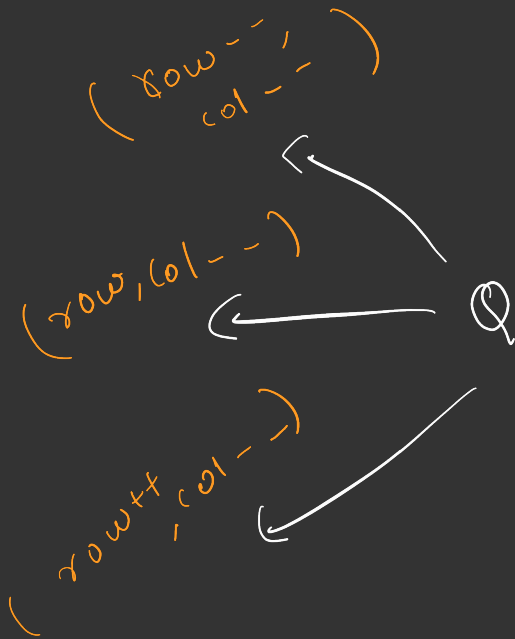
How & where to place Queen??

↑
Q
↓

This isn't req to
check as we are
going through col
wise.

Q →
↘

This side isn't
req to check
as we go
col by col



M coloring | Graph coloring

↳ Decision, enumeration problem.

Time complexity :

$$\underline{\underline{(N^m)}}$$

$$sc \Rightarrow \begin{array}{c} 0(N) \\ \text{recursi-} \end{array} + \begin{array}{c} 0(N) \\ \text{col} \end{array}$$

Grid ways :

Find num of ways to reach from
 $(0,0)$ to $(N-1, m-1)$ in $N \times M$
 grid.

Allowed moves \Rightarrow right, down.

•			1
			1
4	3	$1+1=2$	$1+0=1$
1	1	$0+1=1$	•

Cell (x,y)
 Right \swarrow down \searrow
 $(x, y+1)$ $(x+1, y)$

\downarrow \downarrow
 w_1 $+$ w_2
 ~~~~~

if  $src = (n-1, m-1)$  num of ways-  
 $\Rightarrow f(x,y) = f(x+1,y)$

$\underbrace{\text{down}}_{+} f(x, y+1)$   
 $\underbrace{\text{right}}$

|   |   |   |     |
|---|---|---|-----|
| 6 | 3 | 1 |     |
| 3 | 2 | 1 | → 0 |
| 1 | 1 | ! | ↓   |
|   |   |   | 0   |

$$T.C = 2^{(n+m)}$$

→ Sudoku.

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 5 | 3 |   | 6 | 7 | 8 | 9 |   | 2 |
| 6 | 7 | 2 | 1 | 9 | 5 | 3 | 4 | 8 |
|   | 9 | 8 | 3 | 4 | 2 | 5 | 6 | 7 |
| 8 | 5 | 9 | 7 | 6 | 1 | 4 | 2 | 3 |
| 4 | 2 | 6 | 9 | 5 | 3 | 7 | 9 | 1 |
| 7 | 1 | 3 | 9 |   | 4 | 8 | 5 | 6 |
| 9 | 6 |   | 5 | 3 | 7 | 2 | 9 | 4 |
| 2 | 8 | 7 | 4 | 1 | 9 | 6 | 3 | 5 |
| 3 | 4 | 5 | 2 | 8 | 9 | 1 | 7 | 9 |

Rules.

- ① The digit 1-9 shd appear only once in any level

row / col

- ② within 3x3 matrix it should appear once.



|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 5 | 3 |   | 6 | 7 | 8 | 9 |   | 2 |
| 6 | 7 | 2 | 1 | 9 | 5 | 3 | 4 | 8 |
|   | 9 | 8 | 3 | 4 | 2 | 5 | 6 | 7 |
| 8 | 5 | 9 | 7 | 6 | 1 | 4 | 2 | 3 |
| 4 | 2 | 6 | 8 | 5 | 3 | 7 | 9 | 1 |
| 7 | 1 | 3 | 9 |   | 4 | 8 | 5 | 6 |
| 9 | 6 |   | 5 | 3 | 7 | 2 | 8 | 4 |
| 2 | 8 | 7 | 4 | 1 | 9 | 6 | 3 | 5 |
| 3 | 4 | 5 | 2 | 8 | 9 | 1 | 7 | 9 |



|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 5 | 3 |   | 6 | 7 | 8 | 9 |   | 2 |
| 6 | 7 | 2 | 1 | 9 | 5 | 3 | 4 | 8 |
|   | 9 | 8 | 3 | 4 | 2 | 5 | 6 | 7 |
| 8 | 5 | 9 | 7 | 6 | 1 | 4 | 2 | 3 |
| 4 | 2 | 6 | 8 | 5 | 3 | 7 | 9 | 1 |
| 7 | 1 | 3 | 9 |   | 4 | 8 | 5 | 6 |
| 9 | 6 |   | 5 | 3 | 7 | 2 | 8 | 4 |
| 2 | 8 | 7 | 4 | 1 | 9 | 6 | 3 | 5 |
| 3 | 4 | 5 | 2 | 8 | 9 | 1 | 7 | 9 |

False  
remove  
1

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 5 | 3 | 4 | 6 | 7 | 8 | 9 |   | 2 |
| 6 | 7 | 2 | 1 | 9 | 5 | 3 | 4 | 8 |
|   | 9 | 8 | 3 | 4 | 2 | 5 | 6 | 7 |
| 8 | 5 | 9 | 7 | 6 | 1 | 4 | 2 | 3 |
| 4 | 2 | 6 | 8 | 5 | 3 | 7 | 9 | 1 |
| 7 | 1 | 3 | 9 |   | 4 | 8 | 5 | 6 |
| 9 | 6 |   | 5 | 3 | 7 | 2 | 8 | 4 |
| 2 | 8 | 7 | 4 | 1 | 9 | 6 | 3 | 5 |
| 3 | 4 | 5 | 2 | 8 | 9 | 1 | 7 | 9 |

(wait)

↳ After back track.

False  
remove  
the elem

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 5 | 3 | 1 | 6 | 7 | 8 | 9 | 9 | 2 |
| 6 | 7 | 2 | 1 | 9 | 5 | 3 | 4 | 8 |
|   | 9 | 8 | 3 | 4 | 2 | 5 | 6 | 7 |
| 8 | 5 | 9 | 7 | 6 | 1 | 4 | 2 | 3 |
| 4 | 2 | 6 | 8 | 5 | 3 | 7 | 9 | 1 |
| 7 | 1 | 3 | 9 |   | 4 | 8 | 5 | 6 |
| 9 | 6 |   | 5 | 3 | 7 | 2 | 8 | 4 |
| 2 | 8 | 7 | 4 | 1 | 9 | 6 | 3 | 5 |
| 3 | 4 | 5 | 2 | 8 | 9 | 1 | 7 | 9 |

True

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 5 | 3 | 4 | 6 | 7 | 8 | 9 | 1 | 2 |
| 6 | 7 | 2 | 1 | 9 | 5 | 3 | 4 | 8 |
| 1 | 9 | 8 | 3 | 4 | 2 | 5 | 6 | 7 |
| 8 | 5 | 9 | 7 | 6 | 1 | 4 | 2 | 3 |
| 4 | 2 | 6 | 8 | 5 | 3 | 7 | 9 | 1 |
| 7 | 1 | 3 | 9 | 2 | 4 | 8 | 5 | 6 |
| 9 | 6 | 1 | 5 | 3 | 7 | 2 | 8 | 4 |
| 2 | 8 | 7 | 4 | 1 | 9 | 6 | 3 | 5 |
| 3 | 4 | 5 | 2 | 8 | 9 | 1 | 7 | 9 |

for i → (0-9):

for j → (0-9):

if board[i][j] == '.':

for k (1-9):

if is valid (board, i, j, k):

board[i][j] = k

if solve (board):

return True.

else:

board[i][j] = '.'

return False.