

Rope Cutting problem: Worst case $\rightarrow O(3^n)$, $O(n)$ space
 ↳ if we traverse till end by considering each cut = 1

① I/P $\rightarrow n=5, a=2, b=5, c=1$.

O/P $\rightarrow 5$

Explanation: we can make max of 5 pieces of 1 length.

② I/P $\rightarrow n=11, a=12, b=9, c=11$

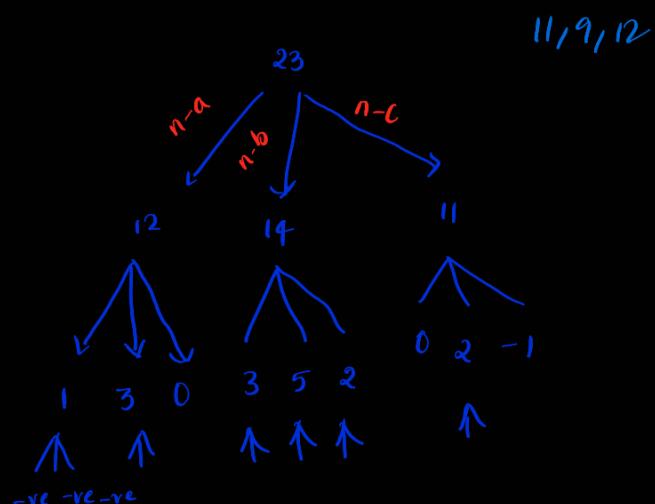
O/P $\rightarrow 2$

Explanation: we can make 2 pieces of length 11 & 12

③ I/P $\rightarrow 9, 2, 2, 2$

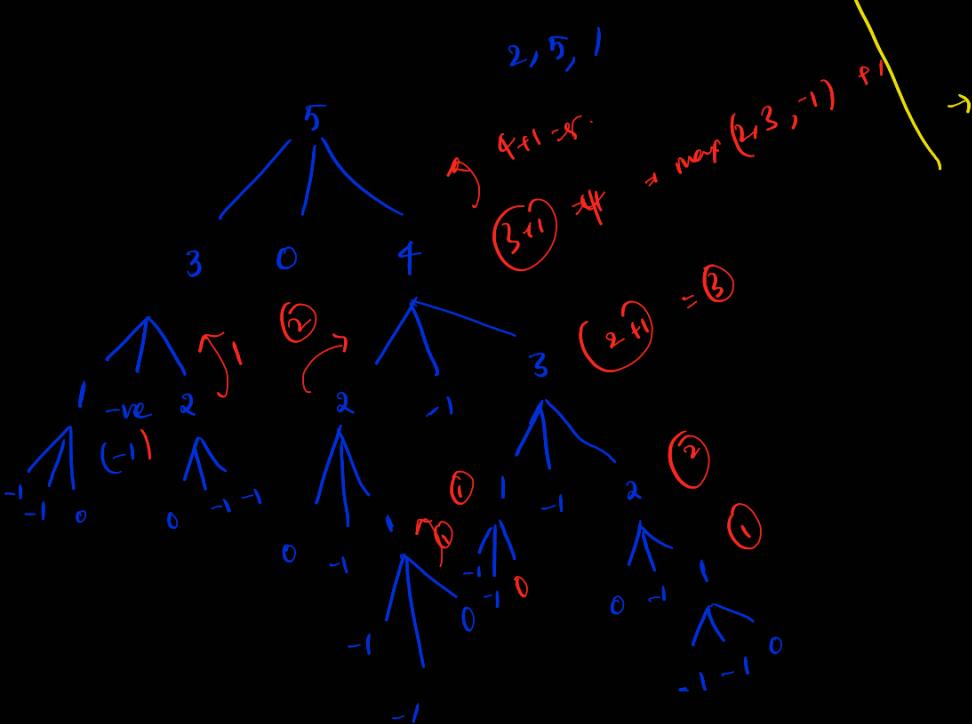
O/P $\rightarrow -1$

.. corner case...



11, 9, 12

→ if $n == 0$: return 0
 → if $n < 0$: return -1
 $\max(\text{fun}(n-a, a, b, c), \text{fun}(n-b, a, b, c), \text{fun}(n-c, a, b, c))$



Add 1 to result
 it's for count
 initially it will be zero
 as you make a cut
 we need to add 1
 to it
 for considering that
 new cut made

- Generate Subsets / subsequences of a string.

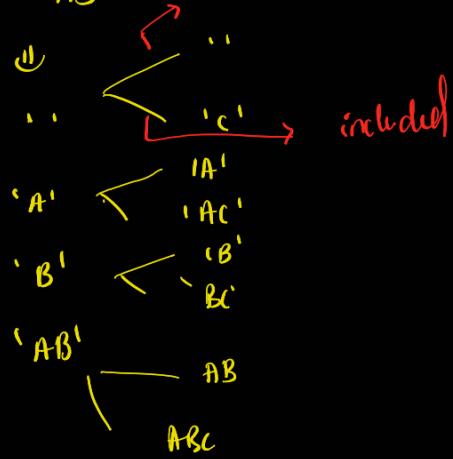
I/P = 'A,B'

O/P = ' ', 'A', 'B', 'AB'

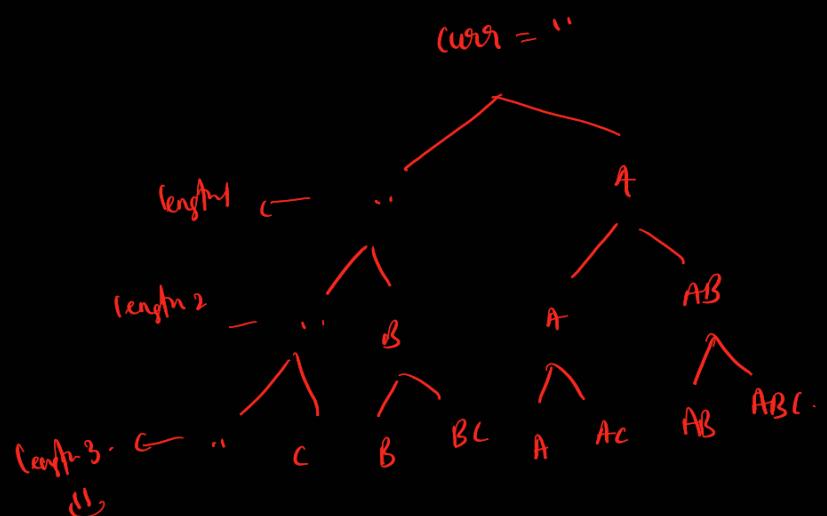
- All char's in input

string are distinct.

→ consider 'AB' not included



subsets of
ABC



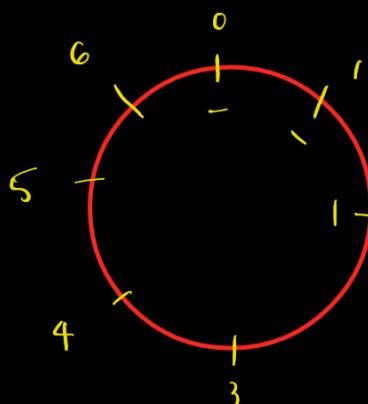
as we reached the str length we can
print curr & return .

Josephus

I/P \Rightarrow $n=7, k=3$, O/P = 3.

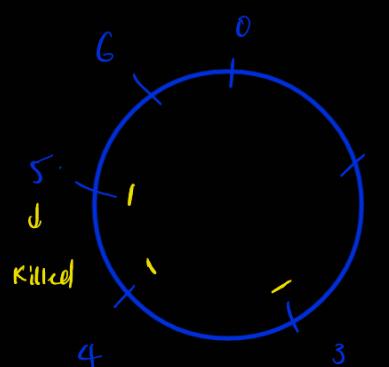
\downarrow kill every 3rd person.

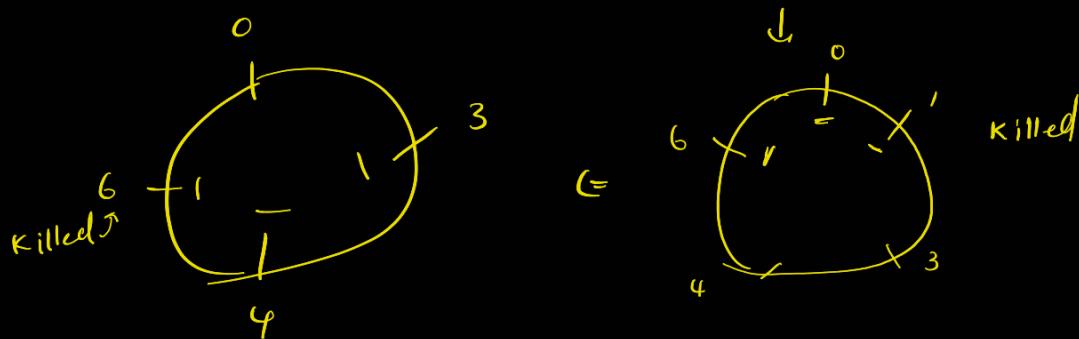
No. of persons in a circle.



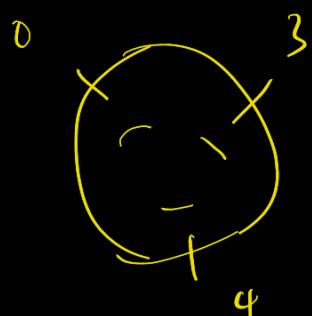
killed.

killed.





↓



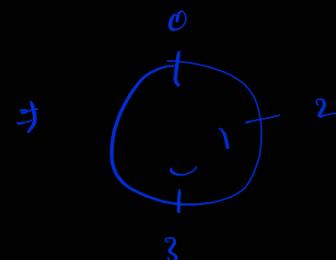
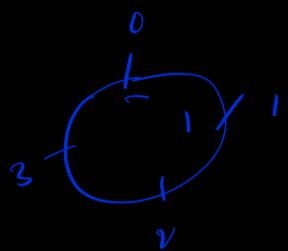
0



⇒ 3

}

∴ $n=4, K=2$



def fun(n, K):
if $n = 1$:
return 0

if $n = 1$ ⇒ 1

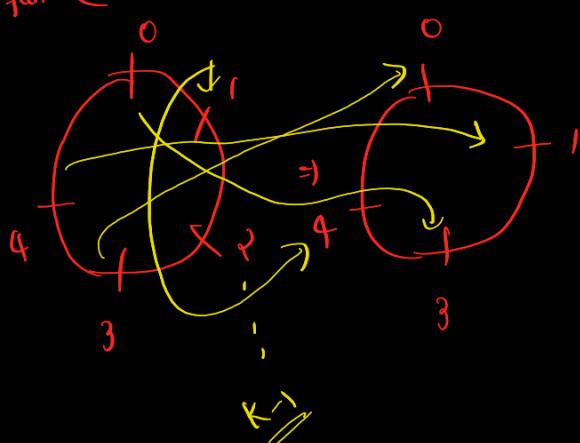
it will be killed

K_2
anything

return fun($n-1, K$)

↳ This will consider a recursive call
from 5, 4, 3 -- like this
(fun($n-1, K$) + K)

fun(5, 3)
fun(4, 3)



∴

$(5, 3)$	$(4, 3)$
3	0
4	1
0	2
1	3

n, K	$n-1, K$
K	0
$K+1$	1
$K+2$	2
$K+3$	3
⋮	⋮

But $K+i$ may become more than n

$n, n-1, \dots, 1, 0$ from 0 to n

so we will just need the numbers

so we need to modulo arithmetic

$$\left(\text{fun}(n-1, K) + F \right) \% n$$

Digital Root ..

$$\begin{array}{r} \text{IP} \quad 1 \\ \text{0 IP} \quad 1 \end{array} \quad \left| \quad \left| \quad \begin{array}{c} 99999 \\ \text{sum digits} \\ \overbrace{}^{45} \end{array} \quad = \quad 9 \\ \text{sum them} \\ \text{till we arrive} \\ \text{at single digit} \end{array}$$

def fun(n):
 if n < 10:
 return n

sum = 0
while n > 0:
 sum += n % 10
 n //= 10

fun(sum)

Lucky numbers are subset of integers. Rather than going into much theory, let us see the process of arriving at lucky numbers,

Take the set of integers

1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19,.....

First, delete every **second** number, we get following reduced set.

1, 3, 5, 7, 9, 11, 13, 15, 17, 19,.....

Now, delete every **third** number, we get

1, 3, 7, 9, 13, 15, 19,.....

Continue this process indefinitely.....

Any number that does **NOT** get deleted due to above process is called "**lucky**".

You are given a number **N**, you need to tell whether the number is lucky or not.

If the number is lucky return 1 otherwise 0.

Example 1:

Input:

N = 5

Output: 0

Explanation: 5 is not a lucky number as it gets deleted in the second iteration.

Example 2:

Input:

N = 19

Output: 1

Explanation: 19 is a lucky number because it does not get deleted throughout the process.

Your Task:

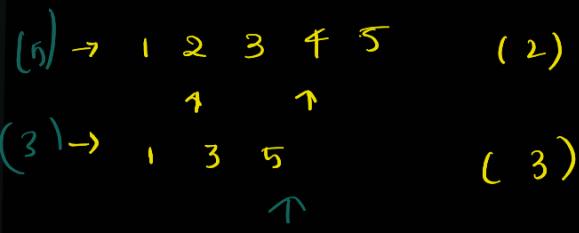
You don't need to read input or print anything. You only need to complete the function **isLucky()** that takes N as parameter and returns either False if the N is not lucky else True.

Expected Time Complexity: O(sqrt(N)).

Expected Auxiliary Space: O(1).

Constraints:

$1 \leq N \leq 10^5$



if $n \% K == 0$:
return False

→ 1 2 3 4 5 6 7 8 9 10, " (2)
(2), 13, 14, 15, 16, 17, 18, 19

→ 1, 3, 5, 7, 9, 11, 13, 15, (3)

17, 19

→ 1, 3, 7, 9, 13, 15, 19 (4)

→ 1, 3, 7, 13, 15, 19 (5)

→ 1, 3, 7, 13, 19 (6)

Base Case

if $n < K$:
return K.

fun (n - n / K , $K + 1$)

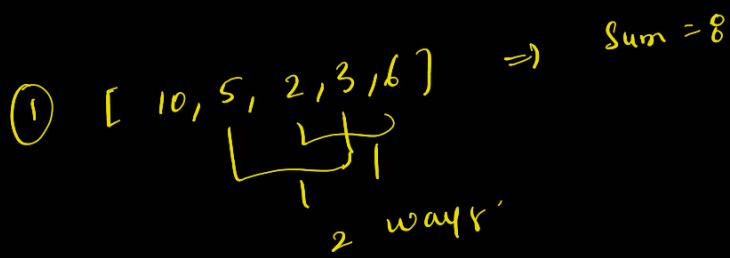
we will remove
these many
nums as go

if $n \% K == 0$
??

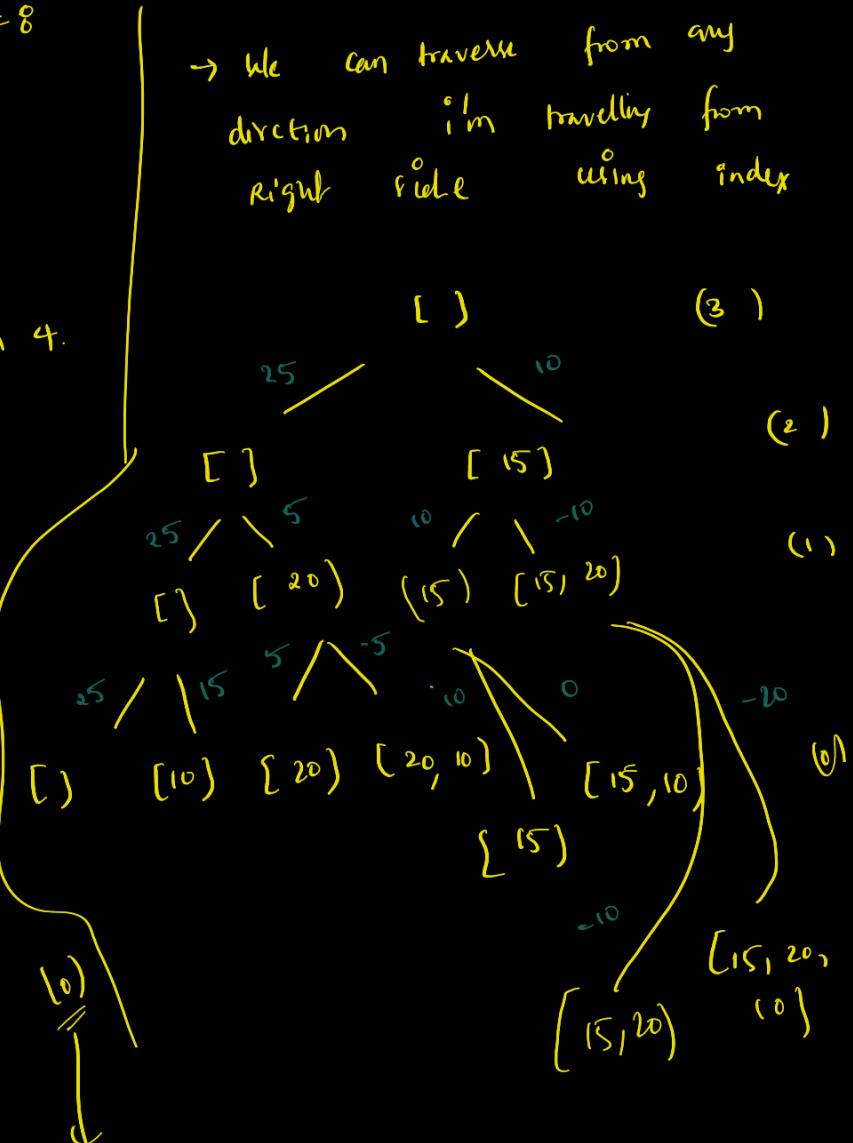
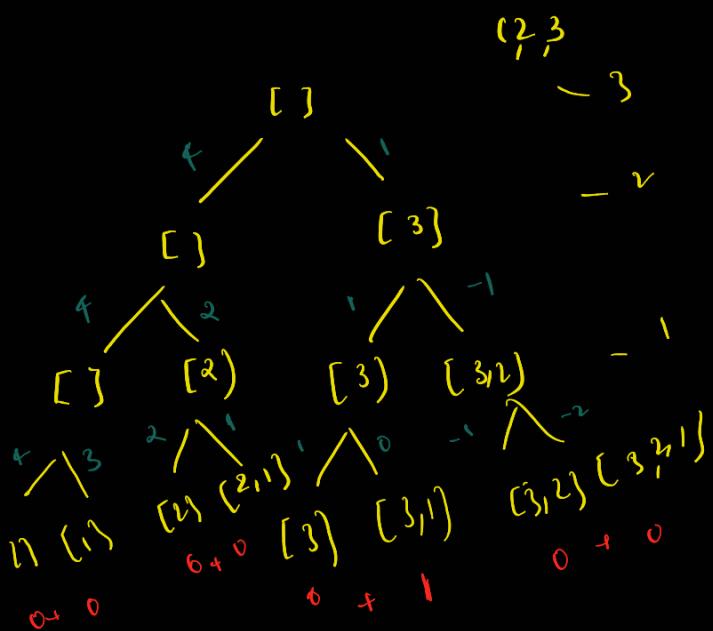
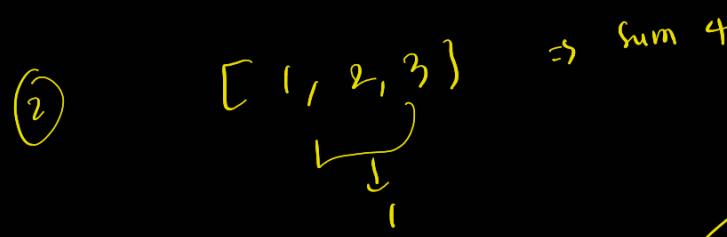
• Count subset sum: 0 (2^n)

10, 2015

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→ We can traverse from any direction in travelling from right side using index



If $n = -0$:

If $\text{sum} == 0$:
return 1

else:
return 0

Initial
exclude
return

include + exclude

combinational sum:

$\rightarrow \{2, 3, 6, 7\}$ target $\rightarrow (2^t \times k)$.

sum $\sum_{j=1}^{2^t} \{7\}$

$f(0, 7, \{\})$

$f(1, 7, \{\})$

