

Natural Language Processing

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Part 1: Generative Models for Word Alignment

Generative Model of Word Alignment

Word Alignments: IBM Model 3

Finding the best alignment: IBM Model 1

Learning Parameters: IBM Model 1

IBM Model 2

Back to IBM Model 3

Noisy Channel Model

Alignment Task

 $e \longrightarrow \mathsf{Program} \longrightarrow \mathsf{Pr}(e \mid f)$

Training Data

► Alignment Model: learn a mapping between fand e.

Training data: lots of translation pairs between fand e.

The IBM Models

- ► The first statistical machine translation models were developed at IBM Research (Yorktown Heights, NY) in the 1980s
- ► The models were published in 1993:

 Brown et. al. The Mathematics of Statistical Machine Translation.

 Computational Linguistics. 1993.
 - http://aclweb.org/anthology/J/J93/J93-2003.pdf
- ► These models are the basic SMT models, called: IBM Model 1, IBM Model 2, IBM Model 3, IBM Model 4, IBM Model 5 as they were called in the 1993 paper.
- We use eand f in the equations in honor of their system which translated from French to English.
 Trained on the Canadian Hansards (Parliament Proceedings)

Generative Model of Word Alignment

Word Alignments: IBM Model 3 Word Alignments: IBM Model 1

Finding the best alignment: IBM Model 1

Learning Parameters: IBM Model 1

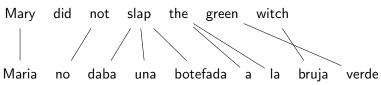
IBM Model 2

Back to IBM Model 3

Generative Model of Word Alignment

- ► English **e**: Mary did not slap the green witch
- ▶ "French" **f**: Maria no daba una botefada a la bruja verde
- Alignment **a**: $\{1, 3, 4, 4, 4, 5, 5, 7, 6\}$ e.g. $(f_8, e_{a_8}) = (f_8, e_7) = (bruja, witch)$

Visualizing alignment a



Generative Model of Word Alignment

Data Set

- ▶ Data set \mathcal{D} of N sentences: $\mathcal{D} = \{(\mathbf{f}^{(1)}, \mathbf{e}^{(1)}), \dots, (\mathbf{f}^{(N)}, \mathbf{e}^{(N)})\}$
- ▶ French **f**: $(f_1, f_2, ..., f_l)$
- ▶ English **e**: (e_1, e_2, \ldots, e_J)
- ▶ Alignment **a**: (a_1, a_2, \ldots, a_l)
- $length(\mathbf{f}) = length(\mathbf{a}) = I$

Generative Model of Word Alignment

Find the best alignment for each translation pair

$$\mathbf{a}^* = \arg\max_{\mathbf{a}} \Pr(\mathbf{a} \mid \mathbf{f}, \mathbf{e})$$

Alignment probability

$$Pr(\mathbf{a} \mid \mathbf{f}, \mathbf{e}) = \frac{Pr(\mathbf{f}, \mathbf{a}, \mathbf{e})}{Pr(\mathbf{f}, \mathbf{e})}$$

$$= \frac{Pr(\mathbf{e}) Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e})}{Pr(\mathbf{e}) Pr(\mathbf{f} \mid \mathbf{e})}$$

$$= \frac{Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e})}{Pr(\mathbf{f} \mid \mathbf{e})}$$

$$= \frac{Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e})}{\sum_{\mathbf{a}} Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e})}$$

Generative Model of Word Alignment

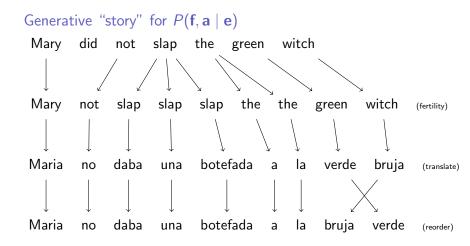
Word Alignments: IBM Model 3 Word Alignments: IBM Model 1

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Fertility parameter

$$n(\phi_j \mid e_j)$$
: $n(3 \mid slap)$; $n(0 \mid did)$

Translation parameter

$$t(f_i \mid e_{a_i}) : t(bruja \mid witch)$$

Distortion parameter

$$d(f_{pos} = i \mid e_{pos} = j, I, J) : d(8 \mid 7, 8, 6)$$

Generative model for $P(\mathbf{f}, \mathbf{a} \mid \mathbf{e})$

$$P(\mathbf{f}, \mathbf{a} \mid \mathbf{e}) = \prod_{i=1}^{I} n(\phi_{a_i} \mid e_{a_i})$$

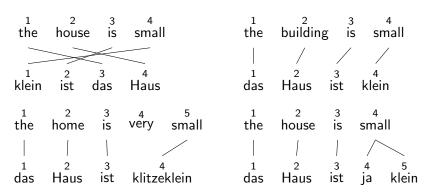
$$\times t(f_i \mid e_{a_i})$$

$$\times d(i \mid a_i, I, J)$$

Sentence pair with alignment $\mathbf{a} = (4, 3, 1, 2)$

If we know the parameter values we can easily compute the probability of this aligned sentence pair.

$$\mathsf{Pr}(\mathbf{f},\mathbf{a}\mid\mathbf{e}) =$$



Parameter Estimation

- ▶ What is $n(1 \mid \text{very}) = ?$ and $n(0 \mid \text{very}) = ?$
- ▶ What is $t(\text{Haus} \mid \text{house}) = ?$ and $t(\text{klein} \mid \text{small}) = ?$
- ▶ What is d(1 | 4, 4, 4) = ? and d(1 | 1, 4, 4) = ?

Parameter Estimation: Sum over all alignments

$$\sum_{\mathbf{a}} \Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e}) = \sum_{\mathbf{a}} \prod_{i=1}^{I} n(\phi_{a_i} \mid e_{a_i}) \times t(f_i \mid e_{a_i}) \times d(i \mid a_i, I, J)$$

Summary

- ► If we know the parameter values we can easily compute the probability Pr(a | f, e) given an aligned sentence pair
- ▶ If we are given a corpus of sentence pairs with alignments we can easily learn the parameter values by using relative frequencies.
- If we do not know the alignments then perhaps we can produce all possible alignments each with a certain probability?

IBM Model 3 is too hard: Let us try learning only $t(f_i \mid e_{a_i})$

$$\sum_{\mathbf{a}} \Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e}) = \sum_{\mathbf{a}} \prod_{i=1}^{I} n(\phi_{a_i} \mid e_{a_i}) \times t(f_i \mid e_{a_i}) \times d(i \mid a_i, I, J)$$

Generative Model of Word Alignment

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Alignment probability

$$Pr(\mathbf{a} \mid \mathbf{f}, \mathbf{e}) = \frac{Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e})}{\sum_{\mathbf{a}} Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e})}$$

Example alignment

$$\begin{aligned} \Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e}) &= \prod_{i=1}^{I} t(f_i \mid e_{a_i}) \\ \Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e}) &= \\ t(\text{das} \mid \text{the}) \times \\ t(\text{Haus} \mid \text{house}) \times \\ t(\text{ist} \mid \text{is}) \times \\ t(\text{klein} \mid \text{small}) \end{aligned}$$

$$\mathsf{Pr}(\mathbf{f}, \mathbf{a} \mid \mathbf{e}) = \prod_{i=1}^{l} t(f_i \mid e_{a_i})$$

Generative Model of Word Alignment

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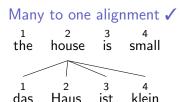
Finding the best word alignment: IBM Model 1

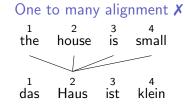
Compute the arg max word alignment

$$\hat{\mathbf{a}} = \arg\max_{\mathbf{a}} \mathsf{Pr}(\mathbf{a} \mid \mathbf{e}, \mathbf{f})$$

▶ For each f_i in $(f_1, ..., f_l)$ build $\mathbf{a} = (\hat{a_1}, ..., \hat{a_l})$

$$\hat{a}_i = \arg\max_{a_i} t(f_i \mid e_{a_i})$$





Generative Model of Word Alignment

Word Alignments: IBM Model 3 Word Alignments: IBM Model 1

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Learning parameters [from P.Koehn SMT book slides]

- ▶ We would like to estimate the lexical translation probabilities t(e|f) from a parallel corpus
- ... but we do not have the alignments
- Chicken and egg problem
 - if we had the alignments,
 - ightarrow we could estimate the *parameters* of our generative model
 - if we had the parameters,
 - ightarrow we could estimate the *alignments*

- Incomplete data
 - ▶ if we had *complete data*, we could estimate *model*
 - ▶ if we had *model*, we could fill in the *gaps in the data*
- Expectation Maximization (EM) in a nutshell
 - 1. initialize model parameters (e.g. uniform)
 - 2. assign probabilities to the missing data
 - 3. estimate model parameters from completed data
 - 4. iterate steps 2–3 until convergence

```
... la maison ... la maison blue ... la fleur ...

the house ... the blue house ... the flower ...
```

- Initial step: all alignments equally likely
- ▶ Model learns that, e.g., *la* is often aligned with *the*

```
... la maison ... la maison blue ... la fleur ...

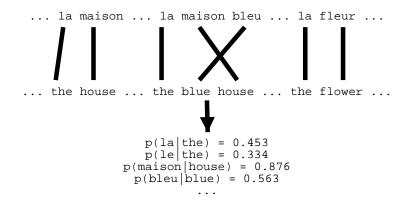
the house ... the blue house ... the flower ...
```

- After one iteration
- ▶ Alignments, e.g., between *la* and *the* are more likely



- After another iteration
- ▶ It becomes apparent that alignments, e.g., between *fleur* and *flower* are more likely (pigeon hole principle)

- Convergence
- ▶ Inherent hidden structure revealed by EM



Parameter estimation from the aligned corpus

IBM Model 1 and the EM Algorithm [from P.Koehn SMT book slides]

- EM Algorithm consists of two steps
- Expectation-Step: Apply model to the data
 - parts of the model are hidden (here: alignments)
 - using the model, assign probabilities to possible values
- ► Maximization-Step: Estimate model from data
 - take assign values as fact
 - collect counts (weighted by probabilities)
 - estimate model from counts
- Iterate these steps until convergence

IBM Model 1 and the EM Algorithm [from P.Koehn SMT book slides]

- ▶ We need to be able to compute:
 - Expectation-Step: probability of alignments
 - ► Maximization-Step: count collection

Alignment probability

$$Pr(\mathbf{a} \mid \mathbf{f}, \mathbf{e}) = \frac{Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e})}{Pr(\mathbf{f} \mid \mathbf{e})}$$

$$= \frac{Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e})}{\sum_{\mathbf{a}} Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e})}$$

$$= \frac{\prod_{i=1}^{I} t(f_i \mid e_{a_i})}{\sum_{\mathbf{a}} \prod_{i=1}^{I} t(f_i \mid e_{a_i})}$$

Computing the denominator

- ▶ The denominator above is summing over J^I alignments
- ▶ An interlude on how compute the denominator faster ...

Sum over all alignments

$$\sum_{\mathbf{a}} \Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e}) = \sum_{a_1=1}^{J} \sum_{a_2=1}^{J} \dots \sum_{a_l=1}^{J} \prod_{i=1}^{l} t(f_i \mid e_{a_i})$$

Assume (f_1, f_2, f_3) and (e_1, e_2)

$$\sum_{a_1=1}^2 \sum_{a_2=1}^2 \sum_{a_3=1}^2 t(f_1 \mid e_{a_1}) \times t(f_2 \mid e_{a_2}) \times t(f_3 \mid e_{a_3})$$

Assume
$$(f_1, f_2, f_3)$$
 and (e_1, e_2) : $I = 3$ and $J = 2$

$$\sum_{a_1=1}^2 \sum_{a_2=1}^2 \sum_{a_3=1}^2 t(f_1 \mid e_{a_1}) \times t(f_2 \mid e_{a_2}) \times t(f_3 \mid e_{a_3})$$

 $J^{\prime}=2^3$ terms to be added:

$$\begin{array}{l} t(f_1 \mid e_1) \; \times \; t(f_2 \mid e_1) \; \times \; t(f_3 \mid e_1) \; + \\ t(f_1 \mid e_1) \; \times \; t(f_2 \mid e_1) \; \times \; t(f_3 \mid e_2) \; + \\ t(f_1 \mid e_1) \; \times \; t(f_2 \mid e_2) \; \times \; t(f_3 \mid e_1) \; + \\ t(f_1 \mid e_1) \; \times \; t(f_2 \mid e_2) \; \times \; t(f_3 \mid e_2) \; + \\ t(f_1 \mid e_2) \; \times \; t(f_2 \mid e_1) \; \times \; t(f_3 \mid e_1) \; + \\ t(f_1 \mid e_2) \; \times \; t(f_2 \mid e_1) \; \times \; t(f_3 \mid e_2) \; + \\ t(f_1 \mid e_2) \; \times \; t(f_2 \mid e_2) \; \times \; t(f_3 \mid e_1) \; + \\ t(f_1 \mid e_2) \; \times \; t(f_2 \mid e_2) \; \times \; t(f_3 \mid e_2) \end{array}$$

Factor the terms:

$$\begin{array}{c} (t(f_{1}\mid e_{1})\times t(f_{2}\mid e_{1})) & \times & (t(f_{3}\mid e_{1})+t(f_{3}\mid e_{2})) & + \\ (t(f_{1}\mid e_{1})\times t(f_{2}\mid e_{2})) & \times & (t(f_{3}\mid e_{1})+t(f_{3}\mid e_{2})) & + \\ (t(f_{1}\mid e_{2})\times t(f_{2}\mid e_{1})) & \times & (t(f_{3}\mid e_{1})+t(f_{3}\mid e_{2})) & + \\ (t(f_{1}\mid e_{2})\times t(f_{2}\mid e_{2})) & \times & (t(f_{3}\mid e_{1})+t(f_{3}\mid e_{2})) & + \\ (t(f_{3}\mid e_{1})+t(f_{3}\mid e_{2})) & \begin{pmatrix} t(f_{1}\mid e_{1}) & \times & t(f_{2}\mid e_{1}) & + \\ t(f_{1}\mid e_{1}) & \times & t(f_{2}\mid e_{2}) & + \\ t(f_{1}\mid e_{2}) & \times & t(f_{2}\mid e_{1}) & + \\ t(f_{1}\mid e_{2}) & \times & t(f_{2}\mid e_{1}) & + \\ \end{pmatrix} \\ (t(f_{3}\mid e_{1})+t(f_{3}\mid e_{2})) & \begin{pmatrix} t(f_{1}\mid e_{1}) & \times & (t(f_{2}\mid e_{1})+t(f_{2}\mid e_{2})) & + \\ t(f_{1}\mid e_{2}) & \times & (t(f_{2}\mid e_{1})+t(f_{2}\mid e_{2})) & + \\ \end{pmatrix}$$

Assume
$$(f_1, f_2, f_3)$$
 and (e_1, e_2) : $I=3$ and $J=2$
$$\prod_{i=1}^3 \sum_{a_i=1}^2 t(f_i \mid e_{a_i})$$

 $I \times J = 2 \times 3$ terms to be added:

$$\begin{array}{cccccc} (t(f_1 \mid e_1) & + & t(f_1 \mid e_2)) & \times \\ (t(f_2 \mid e_1) & + & t(f_2 \mid e_2)) & \times \\ (t(f_3 \mid e_1) & + & t(f_3 \mid e_2)) & \end{array}$$

Alignment probability

$$Pr(\mathbf{a} \mid \mathbf{f}, \mathbf{e}) = \frac{Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e})}{Pr(\mathbf{f} \mid \mathbf{e})}$$

$$= \frac{\prod_{i=1}^{I} t(f_i \mid e_{a_i})}{\sum_{\mathbf{a}} \prod_{i=1}^{I} t(f_i \mid e_{a_i})}$$

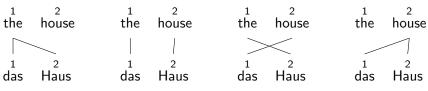
$$= \frac{\prod_{i=1}^{I} t(f_i \mid e_{a_i})}{\prod_{i=1}^{I} \sum_{j=1}^{J} t(f_i \mid e_j)}$$

Learning parameters t(f|e) when alignments are known

$$\begin{split} t(\textit{das} \mid \textit{the}) &= \frac{c(\textit{das}, \textit{the})}{\sum_{f} c(f, \textit{the})} & t(\textit{house} \mid \textit{Haus}) = \frac{c(\textit{Haus}, \textit{house})}{\sum_{f} c(f, \textit{house})} \\ t(\textit{ein} \mid \textit{a}) &= \frac{c(\textit{ein}, \textit{a})}{\sum_{f} c(f, \textit{a})} & t(\textit{Buch} \mid \textit{book}) = \frac{c(\textit{Buch}, \textit{book})}{\sum_{f} c(f, \textit{book})} \\ t(f \mid e) &= \sum_{s=1}^{N} \sum_{f \rightarrow e \in \mathbf{f}^{(s)}, \mathbf{e}^{(s)}} \frac{c(f, e)}{\sum_{f} c(f, e)} \end{split}$$



Learning parameters t(f|e) when alignments are unknown



Also list alignments for (the book, das Buch) and (a book, ein Buch)

```
Initialize t^0(f|e)

t(Haus \mid the) = 0.25 t(das \mid house) = 0.5

t(das \mid the) = 0.5 t(Haus \mid house) = 0.5

t(Buch \mid the) = 0.25 t(Buch \mid house) = 0.0
```

Compute posterior for each alignment

```
Initialize t^0(f|e)

t(Haus \mid the) = 0.25

t(das \mid house) = 0.5

t(Buch \mid the) = 0.25

t(Buch \mid house) = 0.05

t(Buch \mid house) = 0.00
```

Compute $Pr(\mathbf{a}, \mathbf{f} \mid \mathbf{e})$ for each alignment

the house 1 2 the house 1 2 das Haus	the house	the house 1 2 das Haus	the house 1 2 das Haus
0.5×0.25 0.125			$0.5 \times 0.5 \\ 0.25$

Compute
$$Pr(\mathbf{a} \mid \mathbf{f}, \mathbf{e}) = \frac{Pr(\mathbf{a}, \mathbf{f} \mid \mathbf{e})}{Pr(\mathbf{f} \mid \mathbf{e})}$$

 $Pr(\mathbf{f} \mid \mathbf{e}) = 0.125 + 0.25 + 0.125 + 0.25 = 0.75$

the house 1 2 the house 1 2 das Haus	the house 1 2 that 2 4 4 4 5 6 7 6 7 7 8 9 1 1 1 1 1 1 1 1 1 1	the house 1 2 das Haus	the house
0.125	0.25	$\begin{array}{c} 0.125 \\ \hline 0.75 \\ 0.167 \end{array}$	0.25
0.75	0.75		0.75
0.167	0.334		0.334

Compute fractional counts c(f, e)

$$c(Haus, the) = 0.125 + 0.125$$
 $c(das, house) = 0.125 + 0.25$ $c(das, the) = 0.125 + 0.25$ $c(Haus, house) = 0.25 + 0.25$ $c(Buch, the) = 0.0$ $c(Buch, house) = 0.0$

```
Expectation step: expected counts g(f, e)
 g(das, the) = 0.5
                          g(das, house) = 0.5
                       g(Haus, house) = 0.667
 g(Haus, the) = 0.334
 g(Buch, the) = 0.0
                          g(Buch, house) = 0.0
 total = 0.834
                                 total
                                         = 1.167
Maximization step: get new t^{(1)}(f \mid e) = \frac{g(f,e)}{\sum_{f} g(f,e)}
  t(Haus \mid the) = 0.4
                           t(das \mid house) = 0.43
  t(das, | the) = 0.6
                       t(Haus \mid house) = 0.57
                           t(Buch \mid house) = 0.0
  t(Buch \mid the) = 0.0
Keep iterating: Compute t^{(0)}, t^{(1)}, t^{(2)}, \dots until convergence
```

Parameter Estimation: IBM Model 1

EM learns the parameters $t(\cdot | \cdot)$ that maximizes the log-likelihood of the training data:

$$\arg \max_{t} L(t) = \arg \max_{t} \sum_{s} \log \Pr(\mathbf{f}^{(s)} \mid \mathbf{e}^{(s)}, t)$$

- Start with an initial estimate t₀
- ▶ Modify it iteratively to get $t_1, t_2,...$
- \blacktriangleright Re-estimate t from parameters at previous time step t_{-1}
- lacktriangle The convergence proof of EM guarantees that $L(t) \geq L(t_{-1})$
- ▶ EM converges when $L(t) L(t_{-1})$ is zero (or almost zero).

Statistical Machine Translation

Generative Model of Word Alignment

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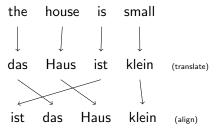
Finding the best alignment: IBM Model 1

Learning Parameters: IBM Model 1

IBM Model 2

Back to IBM Model 3

Generative "story" for Model 2

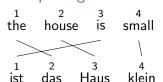


$$\Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e}) = \prod_{i=1}^{I} t(f_i \mid e_{a_i}) \times a(a_i \mid i, I, J)$$

Alignment probability

$$Pr(\mathbf{a} \mid \mathbf{f}, \mathbf{e}) = \frac{Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e})}{\sum_{\mathbf{a}} Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e})}$$
$$Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e}) = \prod_{i=1}^{I} t(f_i \mid e_{a_i}) \times a(a_i \mid i, I, J)$$

Example alignment



$$\begin{aligned} \mathsf{Pr}(\mathbf{f}, \mathbf{a} \mid \mathbf{e}) &= \\ t(\mathsf{das} \mid \mathsf{the}) \times a(1 \mid 2, 4, 4) \times \\ t(\mathsf{Haus} \mid \mathsf{house}) \times a(2 \mid 3, 4, 4) \times \\ t(\mathsf{ist} \mid \mathsf{is}) \times a(3 \mid 1, 4, 4) \times \\ t(\mathsf{klein} \mid \mathsf{small}) \times a(4 \mid 4, 4, 4) \end{aligned}$$

Alignment probability

$$Pr(\mathbf{a} \mid \mathbf{f}, \mathbf{e}) = \frac{Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e})}{Pr(\mathbf{f} \mid \mathbf{e})}$$

$$= \frac{\prod_{i=1}^{I} t(f_i \mid e_{a_i}) \times a(a_i \mid i, I, J)}{\sum_{\mathbf{a}} \prod_{i=1}^{I} t(f_i \mid e_{a_i}) \times a(a_i \mid i, I, J)}$$

$$= \frac{\prod_{i=1}^{I} t(f_i \mid e_{a_i}) \times a(a_i \mid i, I, J)}{\prod_{i=1}^{I} \sum_{j=1}^{J} t(f_i \mid e_j) \times a(j \mid i, I, J)}$$

Learning the parameters

- ► EM training for IBM Model 2 works the same way as IBM Model 1
- We can do the same factorization trick to efficiently learn the parameters
- The EM algorithm:
 - ▶ Initialize parameters *t* and *a* (prefer the diagonal for alignments)
 - Expectation step: We collect expected counts for t and a parameter values
 - Maximization step: add up expected counts and normalize to get new parameter values
 - Repeat EM steps until convergence.

Statistical Machine Translation

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Parameter Estimation: Sum over all alignments

$$\sum_{\mathbf{a}} \Pr(\mathbf{f}, \mathbf{a} \mid \mathbf{e}) = \sum_{\mathbf{a}} \prod_{i=1}^{I} n(\phi_{a_i} \mid e_{a_i}) \times t(f_i \mid e_{a_i}) \times d(i \mid a_i, I, J)$$

Sampling the Alignment Space[from P.Koehn SMT book slides]

- Training IBM Model 3 with the EM algorithm
 - ► The trick that reduces exponential complexity does not work anymore
 - → Not possible to exhaustively consider all alignments
- Finding the most probable alignment by hillclimbing
 - start with initial alignment
 - change alignments for individual words
 - keep change if it has higher probability
 - continue until convergence
- Sampling: collecting variations to collect statistics
 - all alignments found during hillclimbing
 - neighboring alignments that differ by a move or a swap

Higher IBM Models[from P.Koehn SMT book slides]

IBM Model 1	lexical translation
IBM Model 2	adds absolute reordering model
IBM Model 3	adds fertility model
IBM Model 4	relative reordering model
IBM Model 5	fixes deficiency

- Only IBM Model 1 has global maximum
 - training of a higher IBM model builds on previous model
- Computationally biggest change in Model 3
 - trick to simplify estimation does not work anymore
 - ightarrow exhaustive count collection becomes computationally too expensive
 - sampling over high probability alignments is used instead

Summary [from P.Koehn SMT book slides]

- ▶ IBM Models were the pioneering models in statistical machine translation
- Introduced important concepts
 - generative model
 - EM training
 - reordering models
- Only used for niche applications as translation model
- ... but still in common use for word alignment (e.g., GIZA++, mgiza toolkit)

Natural Language Processing

Anoop Sarkar anoopsarkar.github.io/nlp-class

Simon Fraser University

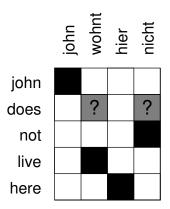
Part 2: Word Alignment

Word Alignment [from P.Koehn SMT book slides]

Given a sentence pair, which words correspond to each other?

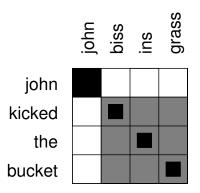
	michael	geht	davon	ans	•	dass	ē	Ξ	haus	bleibt
michael										
assumes										
that										
he										
will										
stay										
in										
the										
house		·								

Word Alignment? [from P.Koehn SMT book slides]



Is the English word *does* aligned to the German *wohnt* (verb) or *nicht* (negation) or neither?

Word Alignment? [from P.Koehn SMT book slides]



How do the idioms *kicked the bucket* and *biss ins grass* match up?

Outside this exceptional context, *bucket* is never a good translation for *grass*

Measuring Word Alignment Quality [from P.Koehn SMT book slides]

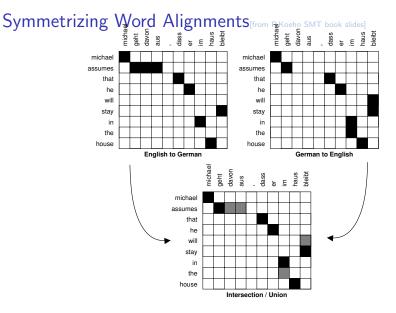
- ▶ Manually align corpus with sure (S) and possible (P) alignment points ($S \subseteq P$)
- Common metric for evaluation word alignments: Alignment Error Rate (AER)

$$AER(S, P; A) = \frac{|A \cap S| + |A \cap P|}{|A| + |S|}$$

- ► AER = 0: alignment A matches all sure, any possible alignment points
- However: different applications require different precision/recall trade-offs

Word Alignment with IBM Models [from P.Koehn SMT book slides]

- ► IBM Models create a many-to-one mapping
 - words are aligned using an alignment function
 - a function may return the same value for different input (one-to-many mapping)
 - a function can not return multiple values for one input (no many-to-one mapping)
- Real word alignments have many-to-many mappings



Intersection plus grow additional alignment points [Och and Ney, CompLing2003]

Growing heuristic [from P.Koehn SMT book slides]

```
grow-diag-final(e2f,f2e)
 1: neighboring = \{(-1,0),(0,-1),(1,0),(0,1),(-1,-1),(-1,1),(1,-1),(1,1)\}
 2: alignment A = intersect(e2f,f2e); grow-diag(); final(e2f); final(f2e);
grow-diag()
 1: while new points added do
 2:
        for all English word e \in [1...e_n], foreign word f \in [1...f_n], (e, f) \in A do
 3:
            for all neighboring alignment points (e_{new}, f_{new}) do
 4:
                if (e_{new} unaligned OR f_{new} unaligned) AND
                (e_{\text{new}}, f_{\text{new}}) \in \text{union(e2f,f2e)} then
                   add (e_{new}, f_{new}) to A
 5:
               end if
 6:
 7:
            end for
        end for
 8.
 9: end while
final()
 1: for all English word e_{\text{new}} \in [1...e_n], foreign word f_{\text{new}} \in [1...f_n] do
        if (e_{\text{new}} \text{ unaligned OR } f_{\text{new}} \text{ unaligned}) \text{ AND } (e_{\text{new}}, f_{\text{new}}) \in \text{union(e2f,f2e)}
        then
 3:
            add (e_{new}, f_{new}) to A
        end if
 4:
 5: end for
```

More Recent Work on Symmetrization [from P.Koehn SMT book slides]

- Symmetrize after each iteration of IBM Models [Matusov et al., 2004]
 - run one iteration of E-step for each direction
 - symmetrize the two directions
 - count collection (M-step)
- Use of posterior probabilities in symmetrization
 - generate n-best alignments for each direction
 - calculate how often an alignment point occurs in these alignments
 - use this posterior probability during symmetrization

Link Deletion / Addition Models[from P.Koehn SMT book slides]

- Link deletion [Fossum et al., 2008]
 - start with union of IBM Model alignment points
 - delete one alignment point at a time
 - uses a neural network classifiers that also considers aspects such as how useful the alignment is for learning translation rules
- Link addition [Ren et al., 2007] [Ma et al., 2008]
 - possibly start with a skeleton of highly likely alignment points
 - add one alignment point at a time

Discriminative Training Methods [from P.Koehn SMT book slides]

- Given some annotated training data, supervised learning methods are possible
- Structured prediction
 - not just a classification problem
 - solution structure has to be constructed in steps
- Many approaches: maximum entropy, neural networks, support vector machines, conditional random fields, MIRA, ...
- Small labeled corpus may be used for parameter tuning of unsupervised aligner [Fraser and Marcu, 2007]

Better Generative Models[from P.Koehn SMT book slides]

- Aligning phrases
 - ▶ joint model [Marcu and Wong, 2002]
 - problem: EM algorithm likes really long phrases

- Fraser and Marcu: LEAF
 - decomposes word alignment into many steps
 - similar in spirit to IBM Models
 - includes step for grouping into phrase

Summary[from P.Koehn SMT book slides]

- Lexical translation
- Alignment
- Expectation Maximization (EM) Algorithm
- Noisy Channel Model
- ► IBM Models 1–5
 - ▶ IBM Model 1: lexical translation
 - ▶ IBM Model 2: alignment model
 - ▶ IBM Model 3: fertility
 - ▶ IBM Model 4: relative alignment model
 - ► IBM Model 5: deficiency
- Word Alignment

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