Pseudo Relevance Feedback with Deep Language Models and Dense Retrievers: Successes and Pitfalls

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Pseudo Relevance Feedback (PRF) is known to improve the effectiveness of bag-of-words retrievers. At the same time, deep language models have been shown to outperform traditional bag-of-words rerankers. However, it is unclear how to integrate PRF directly with emergent deep language models. In this article, we address this gap by investigating methods for integrating PRF signals into rerankers and dense retrievers based on deep language models. We consider text-based and vector-based PRF approaches, and investigate different ways of combining and scoring relevance signals. An extensive empirical evaluation was conducted across four different datasets and two task settings (retrieval and ranking).

Text-based PRF results show that the use of PRF had a mixed effect on deep rerankers across different datasets. We found that the best effectiveness was achieved when (i) directly concatenating each PRF passage with the query, searching with the new set of queries, and then aggregating the scores; (ii) using Borda to aggregate scores from PRF runs.

Vector-based PRF results show that the use of PRF enhanced the effectiveness of deep rerankers and dense retrievers over several evaluation metrics. We found that higher effectiveness was achieved when (i) the query retains either the majority or the same weight within the PRF mechanism, and (ii) a shallower PRF signal (i.e., a smaller number of top-ranked passages) was employed, rather than a deeper signal. Our vector-based PRF method is computationally efficient; thus this represents a general PRF method others can use with deep rerankers and dense retrievers.

CCS Concepts: • **Information systems** → **Retrieval models and ranking**; **Query reformulation**; **Query representation**.

Additional Key Words and Phrases: Pseudo Relevance Feedback, Deep Language Model for Information Retrieval, Dense Retriever, BERT

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1 INTRODUCTION

Pseudo Relevance Feedback (PRF) assumes the top-ranked passages from any phase of retrieval contain relevant signals, and thus modifies the query by exploiting these signals in a bid to reduce the effect of query-passage vocabulary mismatch and improve search effectiveness [3]. Previous research has considered PRF in the context of traditional bag-of-words retrieval models such as probabilistic [43], vector space [44], and language models [23, 30, 59]. PRF

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methods such as Rocchio [44], relevance models [23], RM3 [28], and KL expansion models [59] analyse the top-ranked passages to expand the query or to modify the query weights. The query and the passage are represented as either text or vectors, hence the categorization of *text-based* and *vector-based* PRF approaches hereafter. Empirically, these approaches improve the initial retrieval effectiveness [3].

Recently, Transformer [47] based deep language models [9, 12, 41, 42, 53] have been adopted with promising results in information retrieval [17, 54]. Seminal in this context is the work of Nogueira and Cho [39] who fine tuned BERT [12] as a reranker on top of BM25. In this article, we investigate how to integrate PRF signals, effective for bag-of-words models, into deep language model rerankers, e.g. BERT (other models such as RoBERTa [27], query likelihood models [15, 62, 63] can be applied as well), and dense retrievers, such as ANCE [50] and RepBERT [60]; extensive evaluations are done towards the proposed PRF methods along the side.

In our experiments, we investigate two alternative paths to integrate PRF signals with deep language models: text-based and vector-based. The *text-based PRF* approach is an obvious direction as the concatenation of the query text and the PRF passages text is used as the new formulated query to feed into the deep language model (e.g., BERT). However, this approach has two major impediments: (i) the lengthy concatenated text would often exceed the allowed input size (input vector length) of these deep language models [14, 52] and (ii) it is computationally expensive or infeasible as it requires additional deep language model inferences at query time [18, 26]. To solve the first challenge, we propose three different text handling methods to generate text augmentations from the full concatenated text such that each of the augmentations is within the length limit of the deep language models. Because we split the concatenated text into augmentations, we also propose three different score aggregation methods (Average, Borda, and Max) to aggregate the scores from each augmentation to calculate the final scores for each passage.

To address the computational complexity challenge, we use model pre-generated embeddings to represent text [21, 40, 50, 60]. Query latency is, therefore, reduced to the time of generating the query embeddings because the passages embeddings are pre-generated. In the context of PRF, we further utilise these pre-generated passages embeddings to efficiently integrate the relevance signals while eliminating the input size limit of deep language models, which we refer to as *vector-based PRF* approach. In this approach, each feedback passage is pre-generated as embeddings (vectors). We adopt two different vector fusion methods (Average and Rocchio) to integrate the feedback vectors into the query vectors. The Rocchio method has two parameters: the query vector weight and feedback passage vector weight. We empirically investigate the influence of query and feedback passages through weighting within the Rocchio PRF approach.

To evaluate these PRF approaches, we use the TREC Deep Learning Track Passage Retrieval Task (TREC DL) 2019 [6] and 2020 [7], the TREC Conversational Assistance Track 2019 (TREC CAsT) [11], the Web Answer Passages (WebAP) [20], and the DL HARD [34]. TREC CAsT and WebAP are used for the passage retrieval task rather than their original tasks (e.g., for CAsT we do not consider the multi-turn conversational relationship between queries).

For the text-based PRF approach, we find that our models significantly outperform the baselines across several evaluation metrics on TREC DL 2019, while having mixed results on TREC DL 2020, TREC CAsT and WebAP. For DL HARD, the proposed approach does not have any significant improvements at all. The results suggest that TREC DL 2019 queries are easier – the results from the initial ranking contain less noise – hence, the PRF can add more relevant information to the queries. On the other hand, the queries of TREC DL 2020, TREC CAsT, and WebAP are harder—the results from the initial ranking contain more noise—hence, adding these PRF signals into the query will cause query drift and lead to worse performance. DL HARD is created by selecting queries from TREC DL 2019 and TREC DL 2020 based on the performance systems at TREC had (i.e., select queries for which systems cannot perform well), and the

characteristics of the queries [34]. Our results show that text-based PRF did not work on DL HARD, suggesting that the feedback passages do not contain relevant signals or contain more noise than valuable signals.

Another challenge for text-based PRF is its computational complexity for the full ranking pipeline. It requires at least two inferences, depending on the text augmentation method. This, at least, doubles the total run time in comparison to that of deep language rerankers without PRF.

For the vector-based PRF approach, we find that our models improve the respective baselines (RepBERT, ANCE) across all evaluation metrics and all datasets for the retrieval task; the proposed approach also outperforms the strong BM25+BERT ranker across several metrics. This result suggests that encoding the PRF feedback passages into embedding vectors better models the relevance signals to be exploited by the PRF mechanism. Unlike text-based PRF, the passage vectors are pre-generated and indexed, so the inference steps on passages is not required at retrieval or rerank time. This makes vector-based PRF very efficient: it takes only 1/20th of the time of the BM25+BERT reranker, and only about double the time of the simple bag-of-words BM25. In addition, since our proposed approach works directly with the vector embeddings of query and passages, they can be applied on top of any choice of dense retriever. For the reranking task, we find that our models outperform the BM25 and BM25+RM3 baselines across all metrics and datasets, while they have only mixed improvements over the strong BM25+BERT reranker. Overall, the vector-based PRF approach for retrieval tend to improve deep metrics, while for reranking they tend to improve shallow metrics.

To summarize in this article we make the following contributions:

- We thoroughly investigate the PRF effectiveness under different conditions, in particular how sensitive the effectiveness is to PRF depth, text handling/vector fusion, and score estimation;
- We conduct a thorough comparison of text-based and vector-based approaches within the same reranking task;
- We conduct a thorough comparison of different vector-based approaches within the same retrieval task;
- We study the efficiency of the proposed text-based and vector-based PRF approaches.

2 RELATED WORK

Pseudo-Relevance Feedback (PRF) is a classic query expansion method that modifies the original query in an attempt to address the mismatch between the query intent and the query representation [5, 48]. A typical PRF setting is to use the top-ranked passages from a retrieval system as relevant signal from which to select query terms to add to the original query and/or to set the weights for the query terms. PRF approaches including Rocchio [44], KL expansion [30, 59], query-regularized mixture model [46], RM3 [28], relevance-feedback matrix factorization [58], and relevance models [23] have been well studied. The use of PRF on top of efficient bag-of-words retrieval models is common in information retrieval systems and it has been shown to be an effective strategy for improving retrieval effectiveness [5, 23]. Traditional PRF approaches [23, 28, 44, 59] are simple, yet more effective, robust and generalisable, in comparison to more complex models [46, 58], which instead achieve marginal gains, may be harder to implement/reproduce, or may be problematic to instantiate across different datasets or domains from those in which they have been originally evaluated. In this study, we employ the most popular PRF method in existing research (RM3) as a baseline. The RM3 considers the original query and the feedback passages when creating new query by assigning different weights to the original query and feedback terms. RM3 is effective and robust compared to other query expansion methods [28], and it is used as a baseline in several pseudo relevance feedback studies [4, 29, 35].

Recent research has studied PRF in different settings. Lin [25] considered document ranking as a binary classification problem, combining PRF with text classification by introducing positive and negative pseudo labels. The positive pseudo

labels are obtained from the top-k documents, while the negative labels from the bottom-n documents. The final score is a linear interpolation of the classifier score and the retriever score. Li et al. [24] proposed a neural PRF framework, which was further extended by Wang et al. [49], that utilises a feed forward neural network to determine the target document's relevance score by aggregating the target query and the target feedback relevance scores. These proposed models, however, have achieved marginal improvements over the BM25 baseline. The efficiency (run time) of the proposed models have not been reported and thus it is difficult to establish whether these marginal improvements in effectiveness may be at the cost of efficiency.

Deep language models based on transformers [47], such as BERT [12], T5 [42], and RoBERTa [27], has surpassed the existing state-of-the-art effectiveness in different search tasks. BERT, in specific, has shown to improve over previous state-of-the-art for ad hoc retrieval [39]. Recent research has also considered integrating PRF with deep language models. Yu et al. [55] presented a framework that integrates PRF with a Graph-based Transformer (PGT). It represents each feedback passage as a node and the PRF signals are captured by using sparse attention between graph nodes. While this approach handles the input-size limit of deep language models, it achieves marginal improvements in comparison to the BERT reranker approach across most of the evaluation metrics, at the cost of efficiency. Specifically, compared to our results, PGT achieves a lower nDCG@10 than our simplest text-based PRF reranking approach; it also achieves lower effectiveness in reranking and similar effectiveness in retrieval compared to our vector-based PRF with ANCE, but at a much higher computational cost.

Wang et al. [48] argued that existing PRF research mainly consider relevance matching where terms are used to sort feedback documents. On the contrary, they propose a model that considers both relevance and semantic matching. The relevance score is obtained using BM25. For semantic matching, they split the top-k PRF documents into sentences. For each sentence, they use BERT to estimate the semantic similarity with the query. Scores from the top-m sentences of each document are considered as the semantic score for this document. The final scores of each document are calculated from a linear interpolation of the relevance and semantic scores. The expansion terms are then extracted from the reranked top-k PRF documents and added to the original query for a second retrieval stage. Although the improvements are marginal, they indeed demonstrate that BERT can identify relevance signals from the feedback documents, at sentence level, to enhance retrieval effectiveness. However, this marginal improvement is at the expense of efficiency because expansion terms are identified through BERT.

Zheng et al. [61] presented a three-phase BERT-based query expansion model: BERT-QE. The first phase is a standard BERT reranking [39] step. In the second phase, the top-k passages are selected as feedback passages, which are further split into overlapping partitions using a sliding window. These partitions, along with the original query, are fed into BERT to get the top-m partitions with the highest scores per passage. In the third phase, the top-m partitions and the candidate passage are fed into BERT. The score of a candidate passage in this phase is calculated as a weighted sum, where the weight is the relevance score of each partition in the top-m partitions from phase two, and the score is the relevance score between the top-m partitions and the candidate passage. The final score of a candidate passage is calculated by a linear interpolation of the first phase BERT relevance score between the query and the passage, and the third phase weighted sum score between the top-m partitions and the candidate passages. Although BERT-QE achieves significant improvements in effectiveness over BERT reranker, it requires 11.01x more computations than BERT, making it computationally infeasible in many practical applications.

It is clear that integrating PRF signals into deep language models implies a trade-off between effectiveness and efficiency. While current approaches ignored efficiency, the majority still achieved marginal improvements in effectiveness. In this study, we propose two approaches to integrate PRF signals with the aim to improve effectiveness while

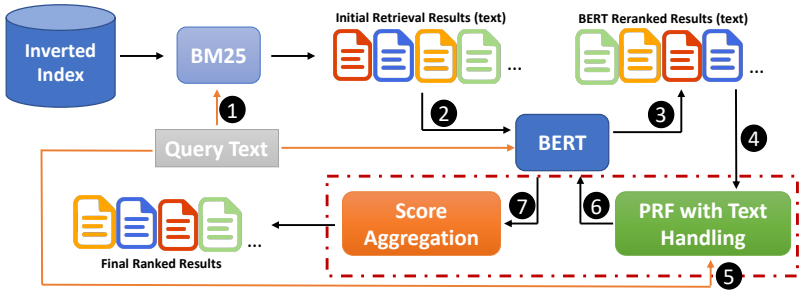


Fig. 1. The proposed architecture for integrating Text-Based Pseudo-Relevance Feedback into Deep Language Model rerankers with a bag-of-words initial retriever.

maintaining efficiency: (i) by concatenating the feedback passages with the original query to form the new queries that contain the relevant signals, (ii) by pre-generating passage collection embeddings and performing PRF in the vector space, because embeddings promise to capture the semantic similarity between terms [10, 13, 22, 36, 37, 45, 56, 57], which makes it feasible as a method for first stage retrieval as well.

3 METHODOLOGY

3.1 Text-Based Pseudo-Relevance Feedback

In this paper, we address the challenge of the input size limit of BERT by employing three text-based PRF methods on top of the BERT reranker:

(1) *Concatenate and Truncate*: append the query and the top-k *feedback* passages, then truncate to the length of 256 tokens. BERT has an input size limit of 512 tokens; we allocate 256 tokens to the new query and the remaining tokens are left to concatenate the *candidate* passage.
(2) *Concatenate and Aggregate*: append the query to each of the top-k feedback passages to form k new queries. For each new query, use BERT to perform another rerank, resulting in k new ranked lists. The final scores for the candidate passages are generated using different score estimation methods that combine the k ranked lists (but not the ranked list of the original query).
(3) *Sliding Window*: concatenate the top-k passages, then use a sliding window to split the aggregated text into overlapping partitions . Concatenate the query with each partition to create j new queries, then follow the same steps as Concatenate and Aggregate.

Methods 2 and 3 require the aggregation of multiple ranker lists to estimate the scores and obtain the final ranked list. For this, we aggregate the scores of a candidate passage using several methods:

(1) *Average*: calculate the average of all the scores per candidate passage.
(2) *Max*: consider only the highest score per candidate passage.
(3) *Borda*: employ the Borda voting rule [2, 33] to calculate the score of each candidate passage.

Figure 1 depicts the proposed architecture for integrating text-based PRF signals into BERT reranker. The initial retriever is a traditional bag-of-words BM25 followed by BERT reranker. As shown in step ❶, the query is passed to BM25 to retrieve the initial ranked results from the inverted index. Then the query text and initial retrieval results

are passed to BERT for reranking (❷). The top-k feedback passages from the reranked list are used as PRF relevance signals (❹), after mapping them back to their text representation (❸). Then, the query and feedback passage texts are combined together to form new query texts (❺) followed by another BERT-based scoring step (❻), and finally the individual scores are aggregated per candidate passage to form the final ranking (❼). The core components of this architecture, which are PRF with Text Handling and Score Estimation, are described in the next two sections.

3.1.1 Text-Based PRF with Text Handling. We consider three different approaches to handle the text length that exceeds the BERT input size limit:

Concatenate and Truncate (CT). A new query text is generated by concatenating the original query text with the top-k feedback passage texts, separated by a space (␣). If the length of the new query exceeds 256, it will be truncated to the first 256 tokens. Then, we run the new query through BERT reranker. The new query is constructed as follows:

$$Q_{new,l<=256} = \lceil Q_{original} + ␣ + p_1 + ... + ␣ + p_k \rceil_{256} \tag{1}$$

where Q_{new} and $Q_{original}$ represent the new query text and the original query text, respectively. $l <= 256$ represents the input size limit enforced, which is achieved by truncating the sequence (denoted with $\lceil . \rceil_{256}$). $p_1, ..., p_k$ represent the top-k feedback passages from the BERT reranker. ␣ is the space in between.

Concatenate and Aggregate (CA). This approach generates k new queries by concatenating the original query text with each of the top-k feedback passage texts, separated by a space (␣). Then, each of the new queries is run through another BERT reranking step resulting into k scores per candidate passage, which will be aggregated later to estimate the final score. The new queries are generated as follows:

$$\begin{aligned} Q_{1,new} &= Q_{original} + ␣ + p_1 \\ &... \\ Q_{k,new} &= Q_{original} + ␣ + p_k \end{aligned} \tag{2}$$

where $Q_{1,new}, ..., Q_{k,new}$ represent the k new queries. $Q_{original}$ represents the original query text. $p_1, .., p_k$ represent the top-k feedback passage texts. ␣ is the separation token in between.

Sliding Window (SW). In this approach, the top-k feedback passage texts are appended together, then a sliding window is applied to split the text into j overlapping partitions with different window size and stride according to different datasets' passage lengths [8], as below:

$$p_1 + ... + p_k \xrightarrow{SW} p_1, ..., p_j \tag{3}$$

where $p_1, ..., p_k$ represent the top-k feedback passage texts, SW represents the sliding window mechanism, $p_1, ..., p_j$ represent the j partitions. Similar to the CA approach, the set of j new queries is generated using Eq. 2.

Note that after generating each new query, the query/passage pair may exceed the BERT input size limit for the CT approach. Under this situation, if the length of the new query exceeds 256, we truncate the new query down to be of length 256. For CA and SW approaches, we also applied the same methodology to guarantee all the new queries are below the length of 256.

3.1.2 Text-Based with Score Estimation. CA and SW text-handling approaches generate k and j scores per candidate passage, respectively. To estimate a final score for each candidate passage, we consider the following estimation methods.

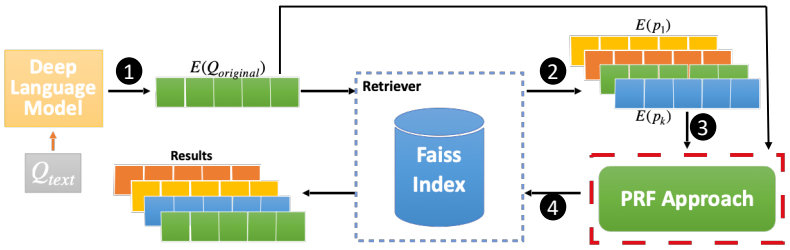


Fig. 2. The proposed architecture for integrating vector-based Pseudo-Relevance Feedback into Deep Language Model dense retrievers.

Average. The final score is estimated by calculating the mean of all scores:

$$S_{final} = Avg(S_1 + S_2 + ... + S_k) \tag{4}$$

where S_{final} represents the final ranking score for each candidate passage, and $S_1, ..., S_k$ represent the k ranking scores for each candidate passage based on each of the k new queries. For the rest of this paper, we refer to this method as Text-Average, represented by T-A for brevity.

Max. The final score is estimated by taking the highest score per candidate passage:

$$S_{final} = Max(S_1, S_2, ..., S_k) \tag{5}$$

where S_{final} represents the maximum score for each candidate passage, and $S_1, ..., S_k$ represent the k ranking scores for each candidate passage based on each of the k new queries. For the rest of this paper, we refer to this method as Max, represented by M for brevity.

Borda. The final score is estimated by using the Borda voting algorithm. The score of a candidate passage w.r.t a ranked list is the number of candidate passages in the ranked list that are ranked lower. Scores are summed over ranked lists as follows:

$$S_{final} = \sum_{L_i : p \in L_i} \frac{n - r_{L_i}(p) + 1}{n} \tag{6}$$

where L_i represents the $i\text{-}th$ ranked list produced using the $i\text{-}th$ new query, p represents the candidate passage, r is the rank of the candidate passage, and n represents the number of candidate passages in the ranked list. For the rest of this paper, we refer to this method as Borda, represented by B for brevity.

3.2 Vector-Based Pseudo-Relevance Feedback

Using two existing, efficient first stage Transformer models[1] (RepBERT [60] and ANCE [50]), we employ two vector-based PRF methods:

(1) *Average:* the mean of the original query embeddings and the feedback passage embeddings are used to generate the new query representation.
(2) *Rocchio:* different weights are assigned to the original query embeddings and the feedback passage embeddings following the intuition provided by the original Relevance Feedback mechanism proposed by Rocchio [44].

[1]Note that our methods are generally applicable to other efficient first stage Transformer models as well, such as TILDE [63], ColBERT [21], EPIC [32], CLEAR [16], and RocketQA [40].

Figure 2 depicts the proposed architecture for integrating vector-based PRF signals into deep language model dense retrievers, such as RepBERT and ANCE. A single deep language model is used to generate offline the embeddings for all passages, which are then stored in a Faiss index [19]. The deep language model is also used to generate the query embedding at inference time (step ❶). The query embedding is then passed to the dense retriever that exploits the Faiss index to perform the first pass of retrieval to obtain the initial ranked list (❷). The top-k feedback passage embeddings from the initial ranked list are used as PRF relevance signals (❸), using vector operations, and are then used to perform the subsequent retrieval to get the final ranked list (❹).

Figure 2 portraits the vector-based PRF approach when used for retrieval. This architecture can be adapted to the reranking task, where an initial ranking of passages is obtained from an inverted-index method, like BM25+BERT (as in Figure 1 and our experiments). In this case, ranked list of passages produced by the inverted index method is mapped to embeddings using the Faiss index, to obtain the ranked list at step ❷.

We describe the two proposed vector-based PRF approaches in the next two sections.

3.2.1 Vector-Based PRF with Average. A new query embedding is generated by averaging the original query embedding and the top-k feedback passage embeddings. The intuition is to treat the original query at par of the signal from the top-k feedback passages (i.e., the query weights as much as each passage). The new query embedding is computed as follows:

$$E_{Q_{new}} = Avg(E(Q_{original}), E(p_1), ..., E(p_k)) \tag{7}$$

where E represents the embeddings of either the query or the feedback passage, $E_{Q_{new}}$ represents the newly formulated query embeddings. We do not generate an actual text query in the vector-based PRF approaches: only the embedding of the new query is generated. $Q_{original}$ represents the original query, $p_1, ..., p_k$ represent the top-k passages retrieved by the first stage ranker. In the remainder of the paper we refer to this method as Vector Average, represented by V-A for brevity.

3.2.2 Vector-Based PRF with Rocchio. This method is inspired by the original Rocchio method for relevance feedback [44] but adapted to deep language models. The intuition is to transform the original query embedding towards the average of the top-k feedback passage embeddings by assigning different weights to query and (the combination of) feedback passages, thus controlling the contribution of each component toward the final score. Unlike in the original version of Rocchio, in this work we do not model the PRF with non-relevant passages: hence the negative portion of Rocchio is omitted. We note that this could be extended by identifying which passages in the initial ranked list could represent a negative relevance signal (e.g., the bottom passages) – however we leave this for future consideration.

Thus, our Rocchio PRF approach consists of interpolating the query embedding and the average PRF embedding:

$$E_{Q_{new}} = \alpha * E(Q_{original}) + \beta * Avg(E(p_1), ..., E(p_k)) \tag{8}$$

where α controls the weight assigned to the original query embedding and β the weight assigned to the PRF signal. In the remainder of the paper we refer to this method as Rocchio, represented by $\mathcal{RC}_{\alpha}$ and $\mathcal{RC}_{\alpha,\beta}$ for brevity.

Table 1. Statistics of the four datasets considered in our experiments. Where #Q represents the number of queries, #P represents the number of passages in the collection, Avg Len represents the average length of passages, Avg #J/Q represents the average number of judged passages per query, and #J represents the number of judged passages in total.

	#Q	#P	Avg Len	Avg #J/Q	#J
TREC DL 2019	43	8,841,823	64.7	215.3	9,260
TREC DL 2020	54	8,841,823	64.7	210.9	11,386
TREC CAsT 2019	502	38,618,941	68.6	63.2	31,713
WebAP	80	1,959,777	74.5	11858.8	948,700
DL HARD	50	8,841,823	64.7	85.1	4,256

4 EXPERIMENTAL SETUP

4.1 Datasets

Our experiments use the TREC Deep Learning Track Passage Retrieval Task 2019 [6] (DL 2019) and 2020 [7] (DL 2020), DL HARD [34], the TREC Conversational Assistance Track 2019 [11] (CAsT 2019), and the Web Answer Passages (WebAP) [20]. The detailed statistics for each dataset are listed in Table 1.

TREC DL 2019 and 2020 contain 200 queries each. However for 2019, only 43 queries have judgements; and thus the remaining 157 queries without judgements are discarded from our evaluation. In 2020, only 54 queries have judgements; and thus the remaining 146 queries are similarly discarded. The relevance judgements for both datasets range from 0 (not relevant) to 3 (highly relevant). The passage collection is the same as the MS MARCO passage ranking dataset [38], which is a benchmark English dataset for ad-hoc retrieval tasks with ≈8.8M passages. The difference between TREC DL and MS MARCO is that queries in TREC DL have several judgements per query (215.3/210.9 on average for 2019/2020), instead of an average of one judgement per query for MS MARCO. We do not use MS MARCO in this work for this reason: the very sparse relevance judgements would not be able to provide detailed, reliable information on the behaviour of the PRF approaches. DL HARD builds upon the TREC DL 2019/2020 queries: these queries are considered as hard queries on which previous methods do not perform well, and new judgements are provided for the added new queries (originally unjudged in TREC) [34]. While TREC CAsT 2019 is originally constructed for multi-turn conversational search, we treat each turn independently, and we use the manually rewritten topic utterances. WebAP is built from the TREC 2004 Terabyte Track collection, and it contains 80 queries[2] and about 2 Million passages (1,1858.8 judged passages per query, on average). The relevance judgements for TREC CAsT 2019 and WebAP ranged from 0 (not relevant) to 4 (highly relevant).

4.2 Evaluation Metrics

We employ MAP, nDCG@{1, 3, 10}, and Reciprocal Rank (RR)[3] for the reranking task on both text-based PRF and vector-based PRF. We select these metrics because they are the common measures reported for BERT based models and these datasets – thus allowing cross-comparison with previous and future work. For the retrieval task on vector-based PRF, we also report Recall@{1000}, but it is not considered for text-based PRF approaches because they are built on top of the BERT reranker where the Recall is limited by the initial retriever (BM25) to the top 1,000 passages. We report Recall for its diagnostic ability in informing whether a gain in e.g., MAP is produced because of a higher number of

[2]In addition to two queries without relevance judgements, which are excluded in our experiments
[3]If for a query no relevant passage is retrieved up to the considered standard cut-off (1,000), then we assign RR=0.

Table 2. Window size and stride size of the Sliding Window PRF approach for each dataset.

	window size	stride
TREC DL 2019	65	32
TREC DL 2020	65	32
TREC CAsT 2019	69	34
WebAP	75	37
DL HARD	65	32

retrieved relevant passages, or because of a better ranking (i.e. ordering of the same number of relevant passages). For all results, statistical significance is performed using two-tailed paired t-test.

4.3 Baselines

We consider the following baselines:

- `BM25`: traditional first stage retriever, implemented using the Anserini toolkit [51] with its default settings.
- `BM25+RM3`: RM3 pseudo relevance feedback method [1] on top of BM25, as implemented in Anserini. We use this approach as a representative bag-of-words PRF method, since previous research has found alternative bag-of-words PRF approaches achieve similar effectiveness [35]. We note that BM25+RM3 is a standard baseline for MS MARCO and TREC DL.
- `RepBERT (R)`: first stage dense retriever [60]. We use the implementation made available by the authors.
- `ANCE (A)`: first stage dense retriever [50]. We use the scripts provided by the authors for both data pre-processing and model implementation.
- `BM25+BERT (BB)`: A common two-stage reranker pipeline, first proposed by Nogueira and Cho [39], where the initial stage is BM25, and BERT is used to rerank the results from BM25. BERT is fine-tuned on MS MARCO Passage Retrieval Dataset [38]. In all of our experiments, we use the 12 layer uncased BERT-Base provided by Nogueira and Cho [39], unless stated otherwise, and we simply refer to it as BERT. In Section 5.5 we also use BERT-Large for the efficiency analysis.

4.4 Applying PRF to Rerankers

Text-Based Pseudo-Relevance Feedback for Reranking. We refer to this approach as BB+PRF, where BB represents BM25+BERT. For the Sliding Window approach, we use the average passage length as the window size, and half of the window size as the stride. Details of the Sliding Window parameters for each dataset are shown in Table 2. We experiment by using the top $k = 1, 3, 5, 10, 15, 20$ passages as pseudo relevance feedback.

Vector-Based Pseudo-Relevance Feedback for Reranking. We consider the vector representations (embeddings) generated by RepBERT and ANCE to apply PRF as a second stage ranker, represented as BB+PRF-R and BB+PRF-A, where BB represents BM25+BERT, R represents RepBERT, and A represents ANCE. To achieve this, the top-k passages IDs from BERT are mapped to their vector representations before estimating the final scores. For the Rocchio method, we experiment by assigning weights to the query and the feedback passage within the range of 0.1–1 with a step of 0.1. We experiment by using the top $k = 1, 3, 5, 10$ passages as pseudo relevance feedback.

4.5 Applying PRF to Retrievers

We choose RepBERT and ANCE as representative first stage dense retrievers because they achieve state-of-the-art effectiveness in previous work on MS MARCO (with ANCE being superior to RepBERT) [50]. We note that a host of alternative first stage dense retrievers have been recently proposed, including stronger ones like RocketQA [40], but most of these retrievers consider more complex training procedures than those selected in this study. We further note that the implementation of the current best first stage dense retriever, RocketQA, has only just been made available and is based on PaddlePaddle [31], thus uses a setup that differs from ours and is not selected for simplicity. We expect that findings that apply for RepBERT and ANCE are likely to translate to other dense retrievers, like RocketQA.

For RepBERT, instead of the original self-implemented dot product retrieval, we utilise the Faiss toolkit [19] to build the index and perform retrieval. We develop our PRF approaches on top of both RepBERT and ANCE. To be consistent with RepBERT, we truncate the query tokens to be of length 20, and the passage tokens to be of length 256. For ANCE, we truncate the query tokens to be of length 64, and passage tokens to be of length 512. For the rest of this paper, vector-based PRF with RepBERT as base model is represented by R+PRF-R, and with ANCE as base model is represented by A+PRF-A for the retrieval task.

4.6 Efficiency experiments

To measure the runtime of each method, we run our experiments on a Unix-based server with the Intel(R) Xeon(R) Gold 6132 CPU @ 2.60GHz for BM25 and BM25 + RM3. For RepBERT, ANCE, and our approaches, we use a Unix-based server equipped with a single Tesla V100 SMX2 32GB GPU.

5 RESULTS

The overarching research question we seek to answer with our experiments is: *What are the successes and pitfalls of integrating PRF into deep language model rerankers and dense retrievers in terms of effectiveness and efficiency?* Each of the following subsections addresses a more specific sub-question.

5.1 PRF Depth

RQ1: What is the impact of PRF depth on the effectiveness of reranking and retrieval? To answer this question, we vary the number of top-k passages while displaying the distribution of results over other parameters (text handling and score estimation).

5.1.1 Reranking with Different PRF Depths. Results of *text-based* PRF (BB+PRF) for reranking are shown in Figure 3. For TREC DL 2019, increased PRF depth is associated with a marginal improvement in effectiveness across most of the evaluation metrics, except for nDCG@10 and, to a minor extent, nDCG@3. On the other hand, increasing PRF depth decreases the effectiveness across the remaining datasets, and none of the PRF configurations is substantially better than the BB baseline. Results of *vector-based* PRF models (BB+PRF-R and BB+PRF-A) are shown in Figure 4. For TREC DL 2019, increased PRF depth is associated with substantial improvements in RR and nDCG@1 using both BB+PRF-R and BB+PRF-A, and marginally improvements in nDCG at depths 3–10. For TREC DL 2020 and TREC CAsT, increased PRF depth is associated with marginal improvements in nDCG@{1,3}. For the remaining datasets, increased PRF depth shows mixed results, but overall it appears to decrease the effectiveness over all metrics.

(a) TREC DL 2019

(b) TREC DL 2020

(c) TREC CAsT

(d) WebAP

(e) DL HARD

Fig. 3. Impact of PRF depth on the effectiveness of BM25+BERT+PRF(BB+PRF) for the task of reranking. Baseline BM25+BERT(BB) is marked with a dashed red line.

(a) TREC DL 2019

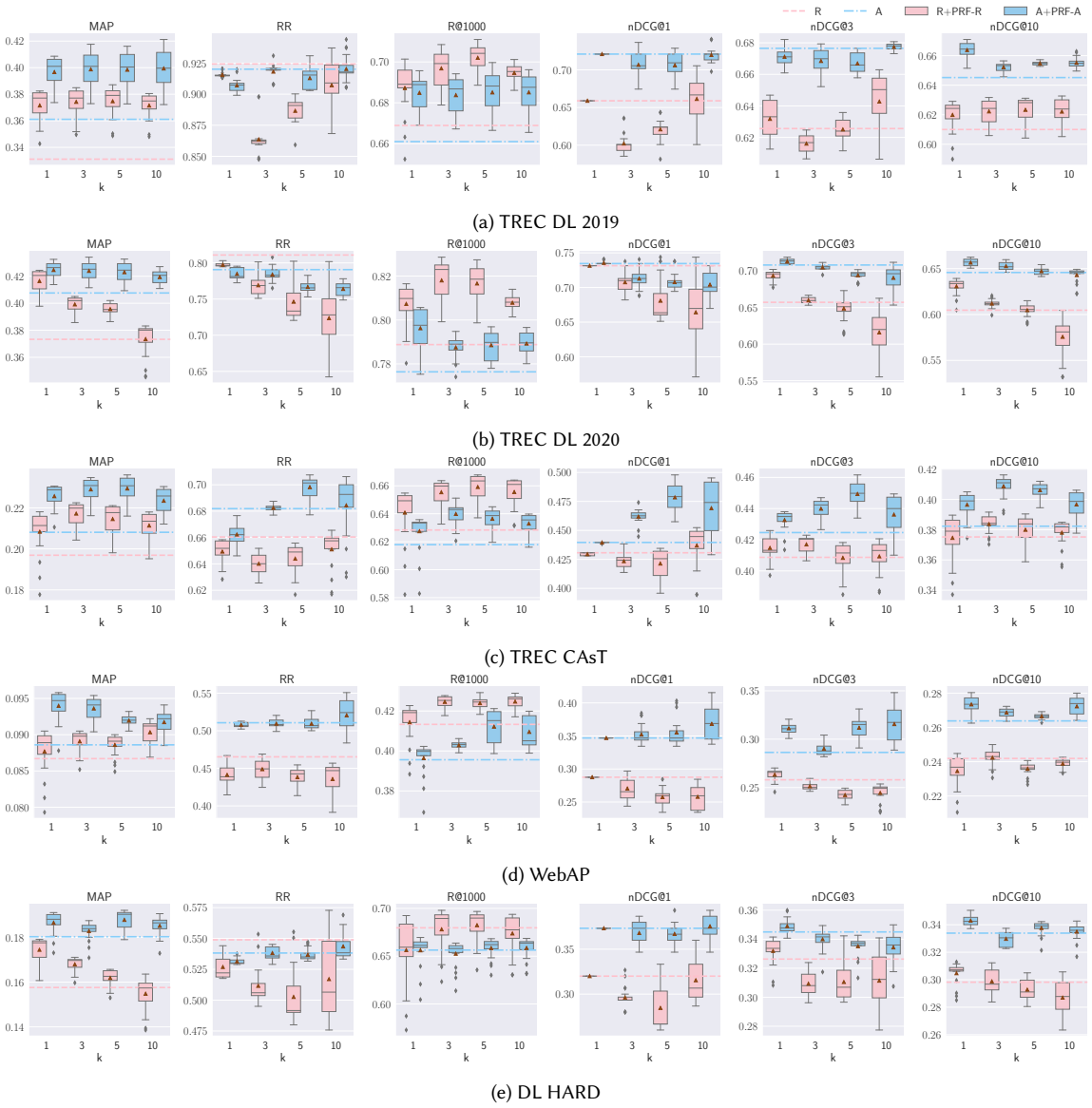
(b) TREC DL 2020

(c) TREC CAsT

(d) WebAP

(e) DL HARD

Fig. 4. Impact of PRF depth on the effectiveness of BM25+BERT+PRF-RepBERT(BB+PRF-R) and BM25+BERT+PRF-ANCE(BB+PRF-A) for the task of reranking. Baseline BM25+BERT(BB) is marked with a dashed red line.



(a) TREC DL 2019

(b) TREC DL 2020

(c) TREC CAsT

(d) WebAP

(e) DL HARD

Fig. 5. Impact of PRF depth on the effectiveness of RepBERT+PRF-RepBERT(R+PRF-R) and ANCE+PRF-ANCE(A+PRF-A) for the task of retrieval. Baseline RepBERT(R) is marked with a dashed red line, ANCE(A) is marked with a dash-dot blue line.

5.1.2 Retrieval with Different PRF Depths. Results of *vector-based* PRF (R+PRF-R and A+PRF-A) for retrieval are shown in Figure 5. For deep evaluation metrics (MAP, nDCG@10 and R@1000), increased PRF depth is associated with significant improvements in effectiveness over the baseline dense retrievers across all datasets, with few exceptions for DL HARD. Increased PRF depth is associated with decreased RR values across all datasets, with few exceptions for A+PRF-A where PRF at depth of 10 is on par or marginally better. For shallow metrics such as nDCG@{1, 3}, mixed

impact across datasets is witnessed with respect to changing PRF depths. For TREC DL 2019 and 2020, PRF of depth 1 is on par with the baselines. For TREC CAsT and WebAP, increased PRF depth is associated with significant increases of effectiveness of A+PRF-A, while PRF of depth 1 enhances the effectiveness of R+PRF-R. For DL Hard, all PRF depths perform on par with the ANCE(A) baseline, while PRF of depth 1 performs on par with the RepBERT(R) baseline.

5.1.3 Summary. To summarize, increasing PRF depth tends to enhance the effectiveness of vector-based models over shallow metrics (RR, nDCG@{1,3}) for reranking, and deep metrics (R@1000, nDCG@10 and MAP) for retrieval. On the other hand, PRF depth impacts the effectiveness of text-based reranking models negatively.

5.2 Text Handling

RQ2: What is the impact of text handling techniques on the effectiveness of reranking and retrieval? To answer this question, we vary the text handling techniques while displaying the distribution of results over other parameters (PRF depth and score estimation). We analyze the effectiveness under three text handling techniques: Concatenate and Truncate (CT), Concatenate and Aggregation (CA), and Sliding Window (SW); and two dense representations for text: RepBERT(R+PRF-R) and ANCE(A+PRF-A).

5.2.1 Reranking with Different Text Handling. Results are shown in Figure 6. For TREC DL 2019, CA substantially improves MAP, RR, and nDCG@1, and marginally improves nDCG@3. BB+PRF-A and BB+PRF-R substantially improve RR, while BB+PRF-A also substantially improves nDCG@1. On the other hand, BB+PRF-R is on par with the baseline over *nDCG*@1, and BB+PRF-A is on par with nDCG@{3, 10}. All other methods do not improve effectiveness. For TREC DL 2020, SW marginally improves nDCG@{1, 3}. BB+PRF-R is on par with the baseline for nDCG@1. All other methods do not improve over the baseline, and all methods, including SW and BB+PRF-R, hurt MAP.

For TREC CAsT 2019, unlike the previous datasets, no improvements can be observed for MAP and nDCG@10 across all methods. CT is on par with the baseline in terms of RR, and marginal improvements are present for nDCG@1. BB+PRF-A is on par with the baseline for nDCG@1. All other metrics are not improved when employing different text handling methods.

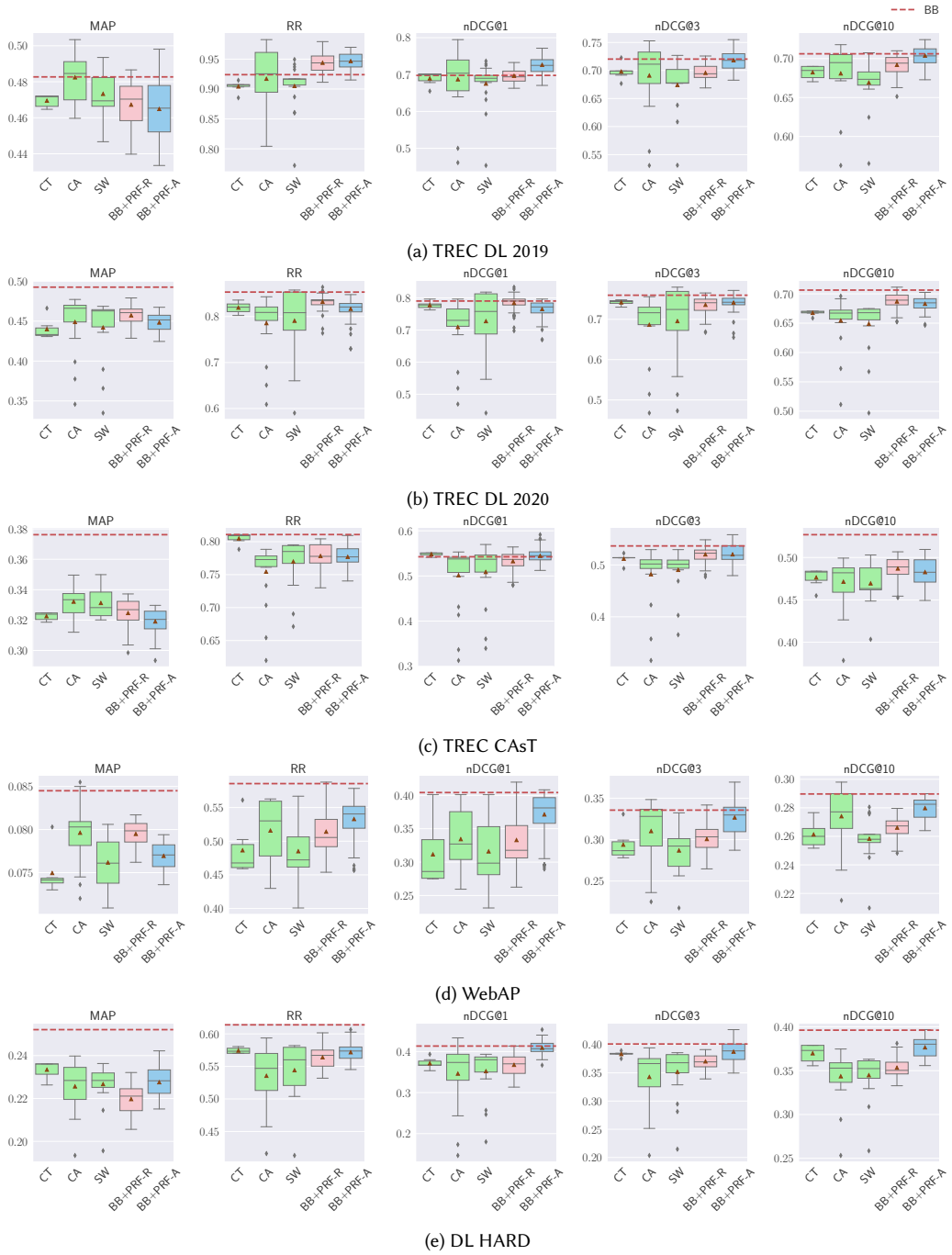
For WebAP, no substantial improvements are found, regardless of the metric, with the exception of nDCG@3, for which BB+PRF-A is on par with the baseline.

For DL HARD, all methods hurt MAP and RR. BB+PRF-A is on par with the baseline for nDCG@1. No substantial improvements on other metrics can be observed for the remaining methods.

5.2.2 Retrieval with Different Text Handling. Results are shown in Figure 7. For TREC DL 2019, both methods substantially outperform their respective baselines in terms of MAP, R@1000, and nDCG@10. No improvement can be observed for RR and nDCG@1. A+PRF-A does not outperform the baseline in terms of nDCG@3, but R+PRF-R does. For TREC DL 2020, both methods A+PRF-A and R+PRF-R substantially improve MAP and R@1000. On the other hand, they do not improve RR and nDCG@1. R+PRF-R is on par with the baseline for nDCG@{3, 10}. Marginal improvements can be observed for A+PRF-A in terms of nDCG@10.

For TREC CAsT 2019, both methods substantially improve the baseline in terms of MAP, R@1000, and nDCG@{3, 10}. Both A+PRF-A and R+PRF-R improve over the baseline in terms of nDCG@1, but A+PRF-A does so substantially; in addition A+PRF-A is on par with the baseline for RR. Both methods do not improve the baselines for other metrics.

For WebAP, similar trends can be observed for MAP, RR, and R@1000. R+PRF-R hurts the effectiveness over nDCG@{1, 3}, while A+PRF-A marginally improves nDCG@1 and substantially improves nDCG@3 and nDCG@10.



(a) TREC DL 2019

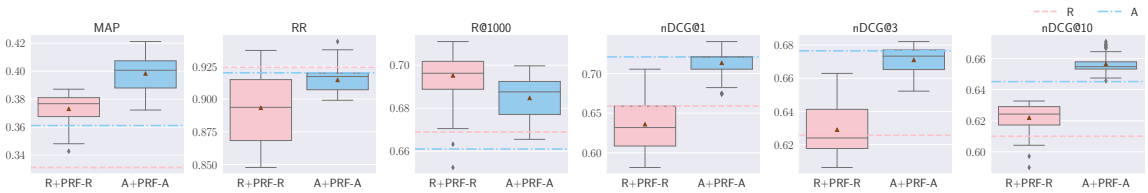
(b) TREC DL 2020

(c) TREC CAsT

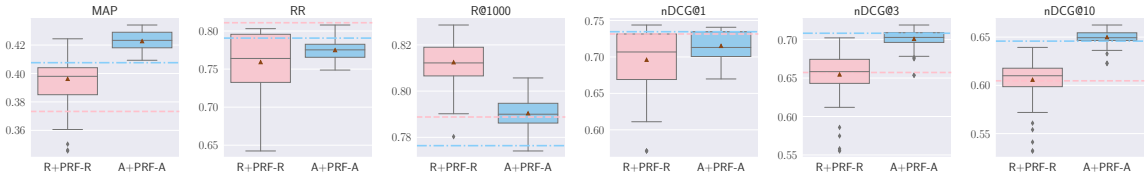
(d) WebAP

(e) DL HARD

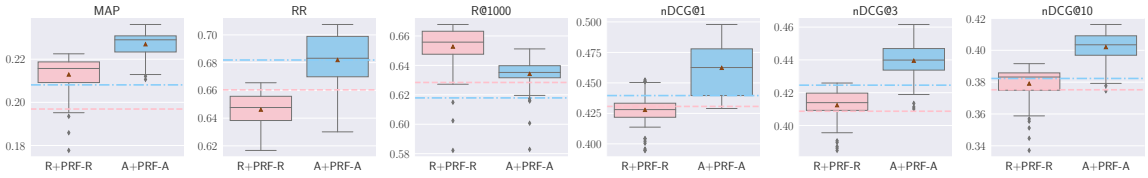
Fig. 6. Impact of text handling on the effectiveness of PRF approaches for the task of reranking, where CT, CA and SW represent the text handling methods Concatenate and Truncate, Concatenate and Aggregate and Sliding Window, respectively, while BM25+BERT+PRF-RepBERT(BB+PRF-R) and BM25+BERT+PRF-ANCE(BB+PRF-A) are the dense representations for text. Baseline BM25+BERT(BB) is marked with a dashed red line.



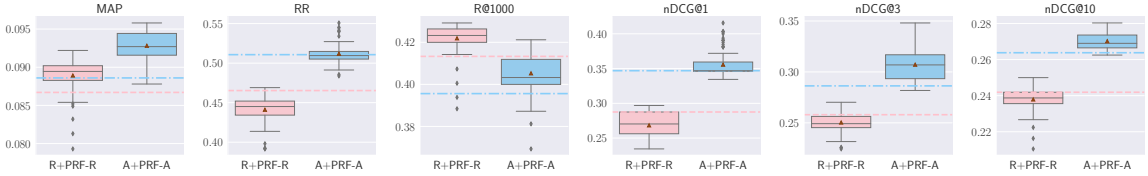
(a) TREC DL 2019



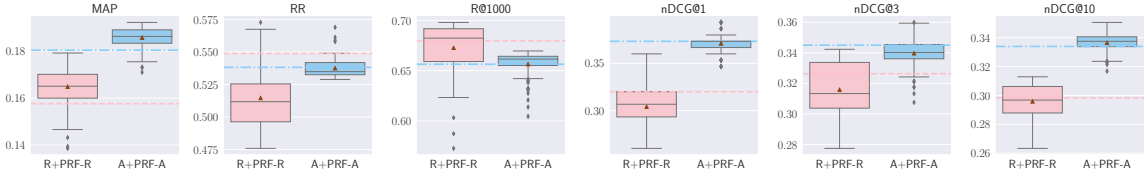
(b) TREC DL 2020



(c) TREC CAsT



(d) WebAP



(e) DL HARD

Fig. 7. Vector-based PRF retrieval effectiveness by using different dense retrieval models RepBERT(R+PRF-R) and ANCE(A+PRF-A). Baseline RepBERT(R) is marked with dashed red line, ANCE(A) is marked with dash-dot blue line.

For DL HARD, both methods substantially improve MAP; R+PRF-R also substantially improves R@1000. A+PRF-A is on par with the baseline for RR, R@1000, nDCG@1, and marginally improves nDCG@10. No improvements are observed for the remaining metrics for either method.

5.2.3 Summary. To summarize, when used for reranking, CA tends to improve more on MAP, BB+PRF-R tends to have more improvements for RR, and BB+PRF-A tends to improve more on nDCG@{1, 3, 10}. In general, all methods tend to improve more nDCG than RR or MAP.

When used for retrieval, A+PRF-A is, overall, a better representation, as it improves all metrics and outperforms all baselines. R+PRF-R performs worse than A+PRF-A. This is because RepBERT(R) baseline is worse than ANCE(A) baseline across most metrics, causing the top ranked results to contain less relevant passages compared to A: hence, the PRF mechanism receives a noisier relevance signal from the feedback passages.

5.3 Score Estimation

RQ3: What is the impact of score estimation methods on the effectiveness of reranking and retrieval? To answer this question, we vary the score estimation methods while displaying the distribution of results over other parameters (PRF depth and text handling). We analyze the effectiveness under three text-based score aggregation methods: Average (T-A), Borda (B) and Max (M); and three vector-based score fusion methods: Average (V-A), Rocchio with fixed α and varying β ($\mathcal{RC}_\beta$), and Rocchio with varying α and β ($\mathcal{RC}_{\alpha,\beta}$).

5.3.1 Reranking with Text Score Estimation and Vector Fusion. Results are shown in Figure 8. For TREC DL 2019, T-A outperforms the baseline in terms of MAP, RR, and nDCG@1, while B is only on par with the baseline for RR, and *M* hurts effectiveness across all metrics. BB+PRF-A with V-A is on par with the baseline across all metrics, except for marginal improvements found for RR. BB+PRF-R with V-A only improves RR marginally. Both BB+PRF-A and BB+PRF-R with $\mathcal{RC}_\beta$ and $\mathcal{RC}_{\alpha,\beta}$ substantially improve RR, while only BB+PRF-A with $\mathcal{RC}_{\alpha,\beta}$ substantially improves RR and nDCG@1, and is on par with the baseline A for nDCG@{3, 10}.

For TREC DL 2020, no score estimation method can outperform the baseline in terms of MAP. B, BB+PRF-R with $\mathcal{RC}_\beta$ and $\mathcal{RC}_{\alpha,\beta}$ are on par with the baseline for nDCG@{1, 3}. M is the worst estimation method for this dataset, as it only outperforms the baseline for nDCG@1, and all remaining methods decrease effectiveness.

For TREC CAsT 2019, M does not perform well across any metric, while T-A and B are on par with the baseline for nDCG@1. On the other hand, BB+PRF-A with V-A, $\mathcal{RC}_\beta$, and $\mathcal{RC}_{\alpha,\beta}$ is on par with the baseline for nDCG@1.

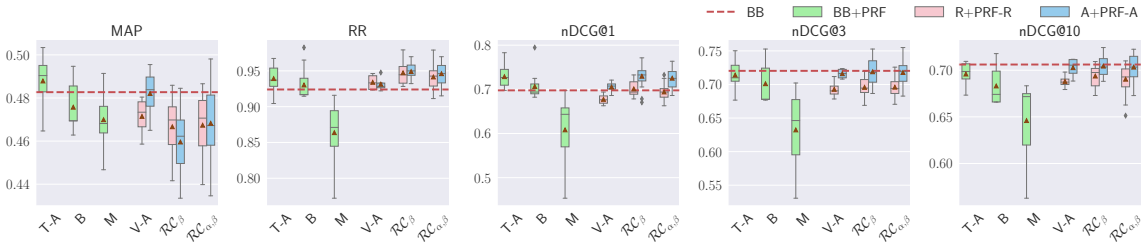
For WebAP, all methods are worse than the baseline in terms of MAP. For RR, only BB+PRF-A with $\mathcal{RC}_\beta$ is on par with the baseline for nDCG@3.

For DL HARD, all methods are worse than the baseline for MAP, RR, and nDCG@{3, 10}, except BB+PRF-A with $\mathcal{RC}_\beta$ and $\mathcal{RC}_{\alpha,\beta}$, which is on par with the baseline for nDCG@1.

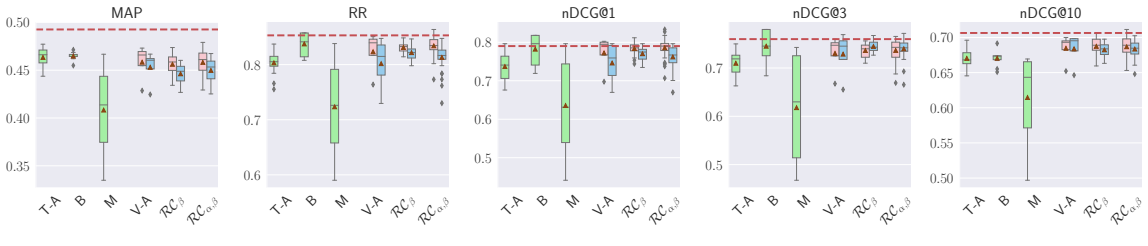
5.3.2 Retrieval with Vector Fusion. Results are shown in Figure 9. For TREC DL 2019, overall, A+PRF-A outperforms the baseline across MAP, R@1000, and nDCG@10, while it is worse than the baseline for RR, and nDCG@{1, 3}. R+PRF-R also substantially improves MAP, R@1000, and nDCG@10, and it is on par with the baseline for nDCG@3 when $\mathcal{RC}_{\alpha,\beta}$ is used.

For TREC DL 2020, R+PRF-R performs exceptionally well in terms of R@1000, but both A+PRF-A and R+PRF-R do not outperform the respective baselines in terms of RR. On the other hand, A+PRF-A also outperforms the A+PRF-A baseline for R@1000, although the improvement is smaller than it was for R+PRF-R. All methods with A+PRF-A are on par with the baseline in terms of nDCG@10; a similar result is obtained for R+PRF-R, except that marginal improvements can be observed with $\mathcal{RC}_\beta$.

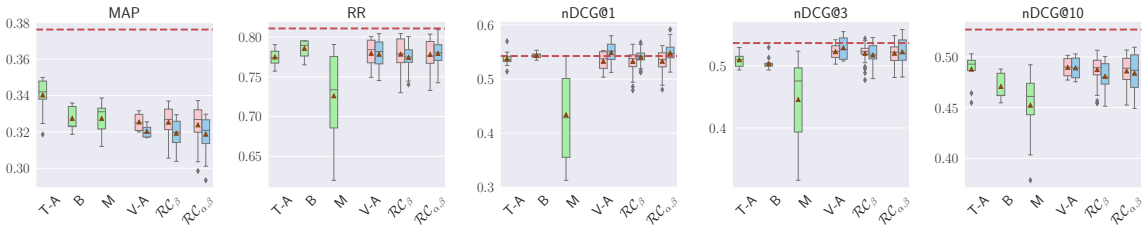
For TREC CAsT 2019, both A+PRF-A and R+PRF-R substantially outperform the respective baselines in terms of MAP. A+PRF-A achieves substantial improvements in terms of nDCG@{1, 3, 10}. Both A+PRF-A and R+PRF-R, combined with any of V-A, $\mathcal{RC}_\alpha$ or $\mathcal{RC}_{\alpha,\beta}$, are either on par or worse than other metrics of the baseline and the dense retrievers without PRF (R and A).



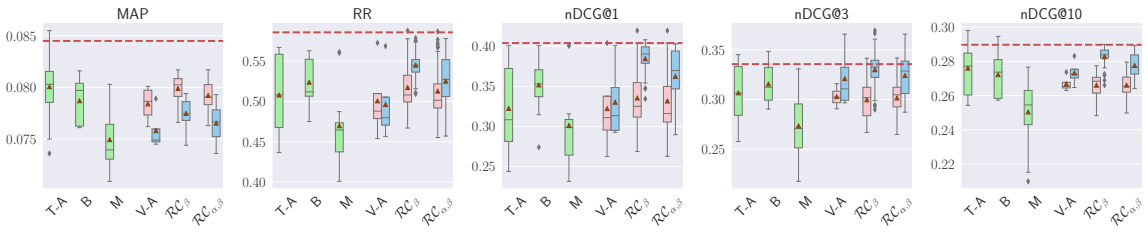
(a) TREC DL 2019



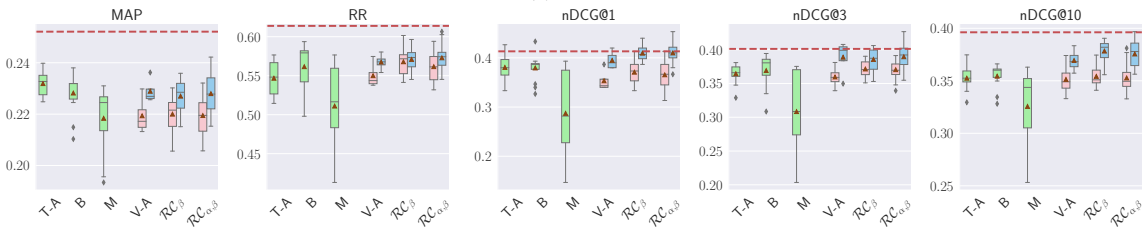
(b) TREC DL 2020



(c) TREC CAsT

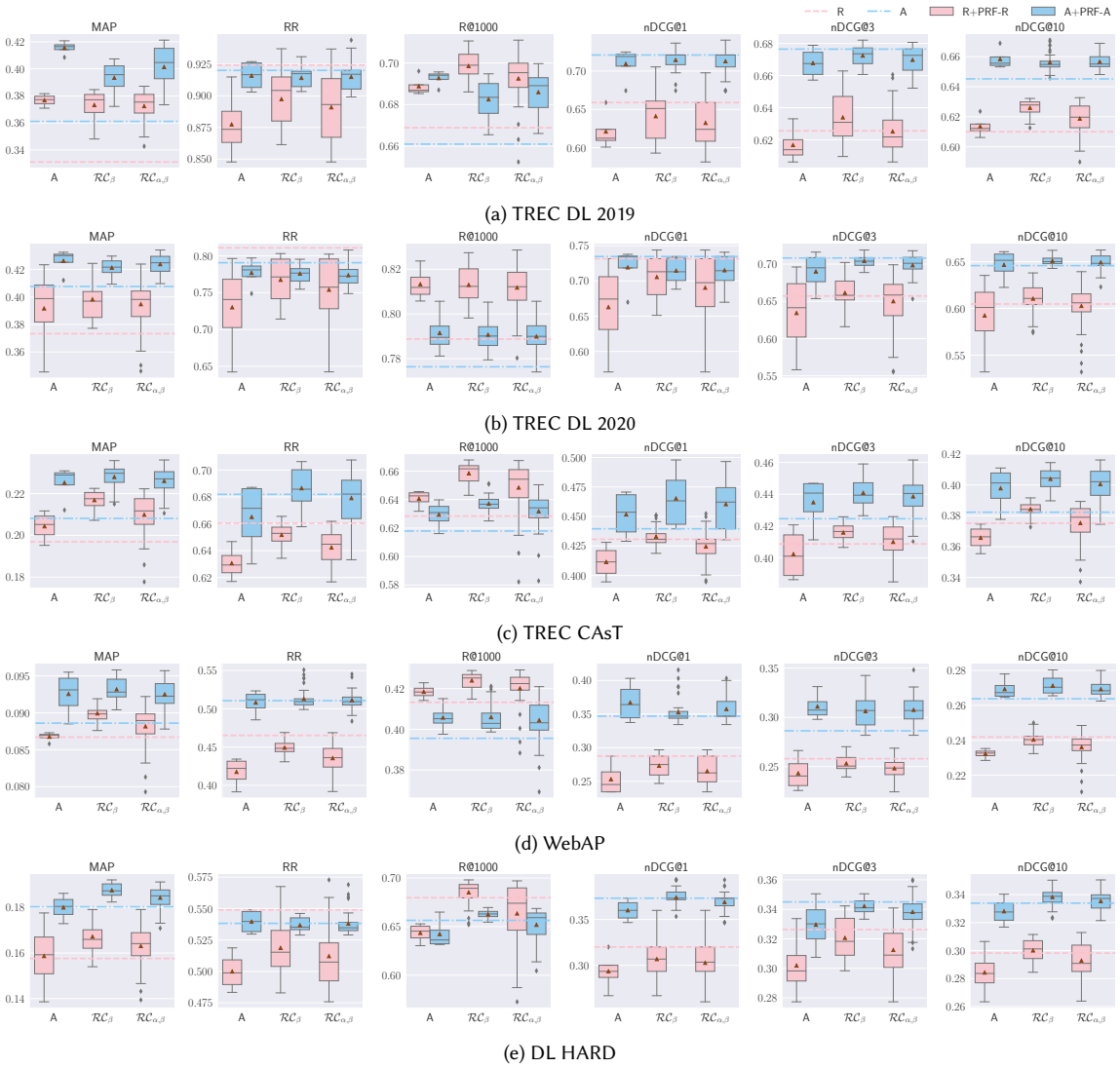


(d) WebAP



(e) DL HARD

Fig. 8. Reranking effectiveness by using different score estimation methods. Where T-A is Text Average, B is Borda, M is Max, V-A is Vector Average, $\mathcal{RC}_\beta$ is Rocchio with fixed α value, and $\mathcal{RC}_{\alpha,\beta}$ is Rocchio with α and β. Baseline BM25+BERT(BB) is marked with dashed red line.



(a) TREC DL 2019

(b) TREC DL 2020

(c) TREC CAsT

(d) WebAP

(e) DL HARD

Fig. 9. Vector-based PRF retrieval effectiveness by using different vector fusion methods. Where A is Vector Average, $\mathcal{RC}_\beta$ is Rocchio with fixed α value, and $\mathcal{RC}_{\alpha,\beta}$ is Rocchio with α and β. Baseline RepBERT(R) is marked with dashed red line, ANCE(A) is marked with dash-dot blue line.

For WebAP, both base models substantially improve MAP and R@1000, except R+PRF-R with A, which is on par with the baseline in terms of MAP. Overall, A+PRF-A is either on par with or improves the baseline across all metrics. On the other hand, R+PRF-R instead exhibits losses in terms of nDCG@{1, 3, 10}.

For DL HARD, A+PRF-A substantially improves MAP and nDCG@10 with $\mathcal{RC}_\beta$. R+PRF-R substantially improves MAP and R@1000 with $\mathcal{RC}_\beta$. All other metrics are either on par or worse than the baselines.

5.3.3 Summary. When the reranking task is considered, $\mathcal{RC}_{\alpha,\beta}$ is found to perform considerably well across all the metrics and datasets. B, T-A, and $\mathcal{RC}_{\beta}$ also perform well across several metrics and all datasets. M performs poorly across all metrics and datasets.

When the retrieval task is considered, $\mathcal{RC}_{\alpha,\beta}$ and $\mathcal{RC}_{\beta}$ perform the best in most circumstances. A+PRF-A with these methods is more likely to improve nDCG at early cut-offs, while R+PRF-R with these methods is more likely to improve deep recall.

5.4 Effectiveness of PRF

RQ4: What is the impact of PRF models on the effectiveness of reranking and retrieval? To answer this question, we consider only our best performing PRF models with the optimal values for all the parameters combined. Results are presented in Table 3. For each dataset, the middle three rows represent PRF rerankers(BB+PRF, BB+PRF-R and BB+PRF-A), and the last two rows represent PRF retrievers (R+PRF-R and A+PRF-A). BB, R, and A are abbreviations for BM25+BERT, RepBERT, and ANCE, respectively. R@1000 is considered only for the evaluation of retrieval, mainly where it is infeasible to employ BERT for retrieval.

5.4.1 Reranking with Text-Based PRF (BB+PRF). For TREC DL 2019, our model improves effectiveness over all metrics, with statistical significance mainly for shallow metrics (RR, nDCG@{1,3}). For TREC DL 2020, we observe improvements over shallow metrics only, although statistically not significant.

For TREC CAsT 2019, BB+PRF does not improve the effectiveness of BM25+BERT, except for nDCG@1. We speculate this is because BM25+BERT is trained with short passages, so it performs the best on CAsT (which consists of short passages).

For WebAP, improvements are observed over MAP and nDCG@{3,10}. Again, we believe this to be associated with the length of the passages in the dataset: here passages are longer and thus BM25+BERT (trained/fine-tuned on short passages) does not perform well.

For DL HARD, the improvement is only on nDCG@1, yet not significant, while nDCG@10 is significantly worse than the baseline. We speculate this is due to the poor relevance signals received by the PRF mechanism. Note that shallow metrics values on DL HARD are far below those in TREC DL 2019 and 2020 (which share the same passages): this means that the passages used for PRF are likely not relevant, thus possibly causing query drift.

To summarize, our proposed BB+PRF approach achieves substantially better results than BM25 and BM25+RM3. However, the improvements over BM25+BERT are more patchy, and are mostly achieved for shallow metrics. We put this down to the length of the text passages formed by the PRF methods: these are substantially longer than the passages used to train/fine-tune the BERT reranker.

5.4.2 Reranking with Vector-Based PRF (BB+PRF-R, BB+PRF-A). When RepBERT is used as the base model (BB+PRF-R), for TREC DL 2019, improvements are obtained for RR and nDCG@1, while no improvements are obtained on the remaining metrics. For TREC DL 2020, we observe improvements over shallow metrics only (RR, nDCG@{1, 10}). For TREC CAsT 2019, the improvements are observed at nDCG@{1, 3}, but nDCG@10 is significantly worse than the baseline, and so is MAP. For WebAP, we observe improvements in shallow metrics as well (RR, nDCG@{1, 3}). For DL HARD, there are no improvements over all reported metrics; on the contrary, it performs significantly worse than the baseline on MAP and nDCG@10.

Table 3. Results of PRF approaches for the tasks of reranking and retrieval across different datasets. For each parametric method, the settings that achieve optimal effectiveness over all metrics are reported. Statistical significance (paired t-test) with $p < 0.05$ between PRF models and BM25 is marked with ^{a}, between PRF models and BM25+RM3 is marked with ^{b}, between PRF and the corresponding baseline is marked with ^{c}. Best results with respect to each dataset and each metric are highlighted in **bold**.

	Model	MAP	RR	nDCG@1	nDCG@3	nDCG@10	R@1000
TREC DL 2019	BM25	.3773	.8245	.5426	.5230	.5058	.7389
	BM25+RM3	.4270	.8167	.5465	.5195	.5180	**.7882**
	BM25+BERT (BB)	.4827	.9240	.6977	.7203	.7061	.7389
	RepBERT (R)	.3311	.9243	.6589	.6256	.6100	.6689
	ANCE (A)	.3611	.9201	.7209	.6765	.6452	.6610
	BB+PRF(k = 10,CA,BORDA)	.4947^{ab}	**.9826**^{abc}	**.7946**^{abc}	**.7528**^{abc}	.7178^{ab}	–
	BB+PRF-R(k = 10, β = .3)	.4705^{a}	.9793^{ab}	.7326^{ab}	.6963^{ab}	.6993^{ab}	–
	BB+PRF-A(k = 10, α = .3, β = .7)	**.4955**^{ab}	.9690^{ab}	.7519^{ab}	.7385^{ab}	**.7210**^{ab}	–
	R+PRF-R(k = 10, β = .3)	.3669^{c}	.9368	.7054^{c}	.6559^{abc}	.6252^{ab}	.7012^{bc}
	A+PRF-A(k = 10, α = .4, β = .6)	.4151^{c}	.9440^{a}	.7403^{ab}	.6807^{ab}	.6629^{ab}	.6962^{bc}
TREC DL 2020	BM25	.2856	.6585	.5772	.5021	.4796	.7863
	BM25+RM3	.3019	.6360	.5648	.4740	.4821	**.8217**
	BM25+BERT (BB)	**.4926**	.8531	.7901	.7598	.7064	.7863
	RepBERT (R)	.3733	.8109	.7315	.6572	.6047	.7888
	ANCE (A)	.4076	.7907	.7346	.7082	.6458	.7764
	BB+PRF(k = 3,SW,BORDA)	.4644^{ab}	.8575^{ab}	.8179^{ab}	**.7798**^{ab}	.6739^{ab}	–
	BB+PRF-R(k = 5, α = .4, β = .6)	.4778^{ab}	**.8638**^{ab}	**.8333**^{ab}	.7544^{ab}	**.7111**^{ab}	–
	BB+PRF-A(k = 1, α = .5, β = .5)	.4606^{abc}	.8476^{ab}	.7963^{ab}	.7691^{ab}	.6984^{ab}	–
	R+PRF-R(k = 1, α = .6, β = .4)	.4239^{abc}	.7951^{ab}	.7315^{ab}	.6991^{ab}	.6393^{ab}	.8159^{c}
	A+PRF-A(k = 3, α = .4, β = .6)	.4341^{abc}	.8079^{ab}	.7407^{ab}	.7117^{ab}	.6598^{ab}	.7948
TREC CAST	BM25	.2936	.6502	.3631	.3542	.3526	**.8326**
	BM25+RM3	.3132	.6556	.3971	.3829	.3817	.8246
	BM25+BERT (BB)	**.3762**	**.8108**	.5425	.5366	**.5269**	**.8326**
	RepBERT (R)	.1969	.6604	.4307	.4087	.3752	.6284
	ANCE (A)	.2081	.6819	.4396	.4246	.3823	.6179
	BB+PRF(k = 10,CC)	.3247^{ac}	.8106^{ab}	.5510^{abc}	.5140^{ab}	.4838^{abc}	–
	BB+PRF-R(k = 3, α = .5, β = .5)	.3372^{ac}	.7985^{ab}	.5480^{ab}	.5468^{ab}	.5067^{abc}	–
	BB+PRF-A(k = 3, α = .3, β = .7)	.3274^{ac}	.8093^{ab}	**.5914**^{ab}	**.5583**^{ab}	.5055^{abc}	–
	R+PRF-R(k = 10, α = .8, β = .2)	.2150^{abc}	.6618	.4498^{a}	.4146^{a}	.3844^{c}	.6566^{abc}
	A+PRF-A(k = 3, β = .9)	.2347^{abc}	.6826	.4626^{a}	.4434^{abc}	.4138^{ac}	.6508^{abc}
WEBAP	BM25	.0436	.3099	.1667	.1604	.1404	.2944
	BM25+RM3	.0536	.2767	.1344	.1316	.1376	.3472
	BM25+BERT (BB)	.0845	.5856	.4042	.3356	.2897	.2944
	RepBERT (R)	.0867	.4653	.2875	.2580	.2419	.4133
	ANCE (A)	.0886	.5107	.3469	.2863	.2638	.3956
	BB+PRF(k = 15,CA,AVG)	.0855^{ab}	.5459^{ab}	.3271^{ab}	**.3444**^{ab}	**.2980**^{ab}	–
	BB+PRF-R(k = 1, α = .7, β = .3)	.0809^{ab}	**.5866**^{ab}	**.4198**^{ab}	.3418^{ab}	.2708^{ab}	–
	BB+PRF-A(k = 3, β = .8)	.0790^{abc}	.5502^{ab}	.4083^{ab}	.3394^{ab}	.2842^{ab}	–
	R+PRF-R(k = 3, β = .1)	.0887^{abc}	.4690^{ab}	.2969^{ab}	.2594^{ab}	.2433^{ab}	**.4206**^{abc}
	A+PRF-A(k = 3, β = .9)	**.0953**^{abc}	.5134^{ab}	.3563^{ab}	.2928^{ab}	.2710^{ab}	.4027^{ab}
DL-HARD	BM25	.1845	.5422	.3533	.3137	.2850	.6288
	BM25+RM3	.1925	.4381	.2467	.2508	.2555	.6522
	BM25+BERT (BB)	**.2521**	**.6139**	.4133	.4012	.3962	.6288
	RepBERT (R)	.1576	.5489	.3200	.3263	.2982	.6797
	ANCE (A)	.1803	.5382	.3733	.3450	.3339	.6564
	BB+PRF(k = 3,CA,BORDA)	.2380^{a}	.5937^{b}	**.4333**^{b}	.3944^{b}	.3550^{abc}	–
	BB+PRF-R(k = 5, α = .8, β = .2)	.2255^{c}	.5843^{ab}	.3867^{b}	.3861^{b}	.3646^{abc}	–
	BB+PRF-A(k = 5, α = .4, β = .6)	.2422^{a}	.5904^{ab}	**.4333**^{b}	**.4267**^{ab}	**.3968**^{ab}	–
	R+PRF-R(k = 5, α = .9, β = .1)	.1654	.5504^{b}	.3333	.3368	.3030	**.6929**^{c}
	A+PRF-A(k = 10, β = .4)	.1865	.5426	.3933^{b}	.3453	.3380^{b}	.6681^{c}

With ANCE as the base model (BB+PRF-A), for TREC DL 2019, all shallow metrics (RR, nDCG@{1, 3, 10}) and MAP are improved. For TREC DL 2020 and DL HARD, improvements are found at nDCG@{1, 3, 10}. For TREC CAsT and WebAP, we observe improvements over nDCG@{1, 3} for both datasets.

To summarize, the proposed vector-based PRF as reranker (BB+PRF-R, BB+PRF-A): (1) it improves the effectiveness over BM25+BERT across several metrics and for all datasets, (2) it achieves substantially better results than BM25, BM25+RM3, and RepBERT/ANCE, except on DL HARD, (3) it provides mixed results when compared with BM25+BERT, with no clear pattern of improvements (or deficiencies) across measures and datasets.

5.4.3 Retrieval with Vector-Based PRF (R+PRF-R, A+PRF-A). For R+PRF-R, results show similar trends on all datasets: improvements can be observed on all reported metrics (MAP, RR, R@1000, and nDCG@{1, 3, 10}, except on TREC DL 2020, where PRF performs worse than the RepBERT baseline for RR.

For A+PRF-A, PRF performs better than ANCE baseline on all evaluation metrics and across all datasets. The improvements in MAP are significant in TREC DL 2019, TREC DL 2020, TREC CAsT, and WebAP; the improvements for R@1000 are significant in TREC DL 2019, TREC CAsT, and DL HARD. Significant improvements in nDCG@{3, 10} are found only in TREC CAsT. Overall, A+PRF-A achieve higher effectiveness than R+PRF-R: ANCE per se is a stronger model than RepBERT, thus encoding more relevant information from the text. Hence, when PRF uses ANCE, it can better encode the additional relevance signals, leading to enhanced effectiveness.

To summarize, our proposed A+PRF-A and R+PRF-R models work well across all datasets and metrics. They also achieve substantial improvements over BM25 and BM25+RM3 baselines across almost all metrics, and they outperform the BM25+BERT baseline on several metrics.

5.4.4 Summary. To answer RQ4, our results suggest that PRF used for either reranking or retrieval can improve effectiveness as measured across several metrics. More specifically, compared to the respective baselines, R+PRF-R and A+PRF-A tend to deliver improvements across all metrics and datasets, except for RR on TREC DL 2020 with RepBERT as base model. On the other hand, BB+PRF tends to only improve shallow metrics, especially when compared to BM25, BM25+RM3, and dense retriever baselines; BB+PRF-R and BB+PRF-A exhibit similar trends.

5.5 Efficiency of PRF

RQ5: What is the impact of PRF models on the efficiency of reranking and retrieval?

To answer this question, we study the efficiency of the PRF approaches and the baseline models. Low query latency – the time required for a ranker to produce a ranking in answer to a query – is an essential feature for the deployment of retrieval methods into real-time search engines. The query latency of the investigated methods is summarised in Table 4.

The dense retrievers studied in this work (R and A) have a comparable query latency to BM25, with the latter being 10ms faster. Applying vector-based PRF to dense retrievers (R+PRF-R and A+PRF-A) has a comparable impact on query latency to BM25+RM3, with the latter being 23–34ms faster. The latency values measured in our experiments are compatible with the requirements of real-time search engines. On the other hand, applying vector-based PRF to BM25+BERT, as a reranking stage(BB+PRF-R and BB+PRF-A), has a high query latency, similar to that of BM25+BERT. Lastly, we found the two-stage BM25+BERT-Large to be the least efficient (up to 2 orders of magnitude slower than other methods) except the text-based PRF approaches(BB+PRF). While BERT and BERT-Large reranking models consider only the top 1,000 passages from BM25, their query latency remains impractical for real-time search engines, the BB+PRF approaches actually creates more queries from one original query, hence leads to worse query latency overall.

Table 4. Query latency of the investigated methods on TREC DL 2019: the lower latency, the better (faster).

	Models	Latency (ms/q)
Baselines	BM25 (Anserini)	81
	BM25 + RM3 (Anserini)	140
	RepBERT(R)	93
	ANCE(A)	94
Vector-based PRF Retriever	R+PRF-R-Average	163
	R+PRF-R-Rocchio	163
	A+PRF-A-Average	173
	A+PRF-A-Rocchio	174
Vector-based PRF Reranker	BB+PRF-R-Average	3,411
	BB+PRF-R-Rocchio	3,414
	BB+PRF-A-Average	3,409
	BB+PRF-A-Rocchio	3,414
Text-based PRF Reranker	BB+PRF($k = 5$)-CT	6,889
	BB+PRF($k = 5$)-CA	17,266
	BB+PRF($k = 5$)-SW	22,314
BERT Reranker	BM25 + BERT(BB)	3,246
	BM25 + BERT Large	9,209

We also analysed the relationship between query length (either original query, or query plus PRF signal) and latency. For BM25 and BM25+RM3, query latency increases with the increase of query length: the longer the query (including the PRF component), in fact, the more posting lists need to be traversed. On the other hand, query length does not affect the query latency of ANCE or RepBERT[4], because the query is converted to fixed length vectors: no matter how many words in the query, the generated query vector is always of the same length. This same reasoning applied for the vector-based PRF approaches: even when increasing the number of PRF passages considered (k), the query latency remains unchanged. As for the text-based PRF, we cut-off the query (including the revised query after PRF) to the length of 256 tokens, and before the query/passage pair is passed to BERT, the pair is padded to be of a total length of 512 tokens. Thus, no matter how long the query is (including possibly PRF), the sequence passed to BERT is always 512 tokens long. The reason for padding the input for BERT is that for each batch of query-passage pairs passed to BERT, the pairs in a batch need to be of the same length. The batching mechanism is useful for efficiently exploiting the GPU processing. In such cases, the query latency of the text-based PRF does not change with the increase of query length. A factor instead that does greatly affect the efficiency of text-based PRF with CA or SW is the depth of PRF. The more PRF passages, in fact, the more BERT inferences are required at run time, and thus the higher the query latency. For example, one original query with PRF depth at 5, the CA will generate 5 new queries, each for one feedback passage. So for each original query, it only needs one inference for BM25+BERT, but with the new queries from CA, it needs 5 more inferences, combined with BM25+BERT, it requires 6 inferences in total, similar for SW. (Table 4)

6 DISCUSSION

Integrating PRF with deep language models has two main challenges: computational cost and input size limit, which can be roughly mapped to efficiency and effectiveness, respectively. Previous research has focused mainly on effectiveness, and applying PRF as a second stage that considers a subset of the data collection, to mitigate the computational cost. For instance, Zheng et al. [61] proposed a PRF framework which is divided into three phases, each involving BERT, to

[4]If not just noticeably because more tokens need to be passed through the tokenizer.

rerank passages and chunks of text after the initial retrieval. Similarly, Wang et al. [48] applied PRF to the second stage retrieval, utilising BERT for reranking sentences. Other work that applied PRF to the first stage retrieval has limited the second phase of retrieval to a subset of the collection, either to depth of 500 [55] or 1000 [24]. We argue that the main limitation with these approaches is related to the first stage retrieval model they employed — if the first stage is basic bag-of-words then the overall method inherits many of this models limitations.

To address the applicability, effectiveness, and efficiency of text-based PRF and vector-based PRF approaches, we compared them over two different tasks, retrieval for vector-based PRF and reranking for both vector-based PRF and text-based PRF. While our proposed text-based PRF approach handles the input size limit effectively, we demonstrated that it enhances the ranking effectiveness marginally. This finding aligns with previous research, but we demonstrated it happens at the cost of efficiency. The BERT model is slow (ranking 1,000 passages for each query takes 9,209 ms), rendering text-based PRF approaches infeasible and inapplicable to real-time search engines for this task. On the other hand, our proposed vector-PRF approach is substantially more efficient for both reranking and retrieval tasks: it only takes 163-174 ms to process one query. In addition, it does so while also improving the effectiveness in terms of shallow metrics compared to BERT (for reranking), and in terms of all metrics compared to ANCE and RepBERT (for retrieval).

The BERT reranker used as a strong baseline in our experiments is an off-the-shelf model, originally produced by Nogueira and Cho [39]. This model is fine-tuned on the training set of the MS MARCO Passage Retrieval Dataset. The query length in this training set is much shorter than the newly formed queries from the text-based PRF approaches. This causes a mismatch between training and testing data. Theoretically, if the testing data is significantly different from the trained data data used to fine-tune the model, the model itself will be less effective. Despite this, in our experiments we found that the formed long PRF queries still significantly improve results for some metrics across several datasets (although improvements are often only marginal) – but in the majority of cases their effectiveness is worse than that of BM25+BERT. It will then be interesting to investigate whether the effectiveness of text-based PRF can be further improved by fine-tuning the BERT model with long PRF queries, hence eliminating the training/testing data mismatch. On the other hand, vector-based PRF is not affected by this issue, because the query vector is of fixed length: no matter how many PRF passages are added to the original query vector, the query vector formed via PRF maintains the same length, and thus no training/testing data mismatch occurs. Another advantage of vector-based PRF over the text-based is that, although its effectiveness might be improved significantly after fine-tuning on long PRF queries, the text-based PRF approach is still inefficient and it is infeasible to apply it to real-time settings.

7 CONCLUSION

This article investigated the integration of PRF within transformer-based deep language models and dense retrievers for retrieval and reranking. In this context, a text-based PRF approach, applicable to the reranking task only, and a vector-based PRF approach, applicable to both retrieval and reranking tasks, were proposed to leverage the relevance signals from the feedback passages. The proposed approaches are based on the BERT reranker and the dense retrievers ANCE and RepBERT. In this context, we studied the impact of vector representation (for vector-based PRF), PRF depth, text handling techniques (for text-based PRF), and different score estimation (vector fusion) methods (for vector-based PRF) .

When analysing results for the vector-based PRF approaches, we found they differed depending on whether we considered the task of retrieval or reranking.

In terms of *which vector-based representation is most effective* for retrieval, we empirically found that performing PRF using ANCE as a representation (A+PRF-A) is better than when using RepBERT (R+PRF-R) across metrics and datasets,

with the exception of R@1000. Indeed, our results show that R+PRF-R tends to improve deep metrics, while A+PRF-A tends to improve shallow metrics. When considering the reranking task, substantial improvements only occurred on a few datasets and for a limited amount of metrics, and overall ANCE-based PRF performs better than RepBERT-based.

In terms of the *impact of depth of PRF signal* for vector-based PRF, we found that when retrieval is considered, substantial improvements are recorded when 3 to 5 passages are given as feedback, while deeper feedback (10 passages) hurts effectiveness most of the times. When reranking is considered, PRF depth is not a factor substantially influencing effectiveness in a consistent manner across datasets and metrics.

In terms of *score estimation methods (vector fusion)* for the vector-based PRF, we found that, for the retrieval task, $\mathcal{RC}_{\beta}$ and $\mathcal{RC}_{\alpha,\beta}$ achieve the best effectiveness across all datasets. Moreover, R+PRF-R often performs best when using either approximately evenly distributed weights between query/feedback passages, or when the query retains most of the weight. This is similar for A+PRF-A, although for this method there are cases where the best effectiveness is achieved by giving a higher weight to feedback passages. When the task of reranking is considered, we found that $\mathcal{RC}_{\alpha}$ and $\mathcal{RC}_{\alpha,\beta}$ record the most improvements. Substantial improvements, however, only occur on TREC DL 2019 and for only MAP, RR, and nDCG@1.

The *text-based PRF* approaches were only applicable to the reranking task. In terms of *depth of PRF*, we found that, in most cases, substantial improvements are achieved when using 3, 5, and 10 passages for PRF. Deeper PRF signals (15 and 20 passages) were found to hurt effectiveness: this is likely because the addition of more feedback passages substantially contributed to query drift. In terms of *text handling methods*, we found that CA performs best in most cases, but only marginal improvements over the baselines are recorded across datasets and metrics.

Vector-based and text-based PRF approaches could be compared only in the reranking task. In terms of effectiveness, neither of these two types of approaches clearly and consistently outperformed the other across datasets and metrics. However, they greatly differed in terms of *efficiency (query latency)*. When the vector-based PRF was used for retrieval, latency was close to that of the bag-of-words PRF method BM25+RM3, and about double that of BM25. When used for reranking, the latency of the vector-based PRF remained the same. However, to this latency one needs to add that of the preceding part of the retrieval/ranking pipeline: in the case of our experiments that was the latency of BM25+BERT, which was substantial. On the other hand, the latency of text-based PRF was substantially higher. To the latency of the initial retrieval/ranking pipeline, in fact, the text-based PRF added the latency associated with the text handling methods (e.g., Concatenate and Aggregate) – and this operation involved the execution of many more, costly BERT inferences, rendering the overall latency prohibitive for real-time search engines.

The implementations of our PRF methods are made publicly available at http://ielab.io/publications/li-tois-2021, along with the full empirical results.

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