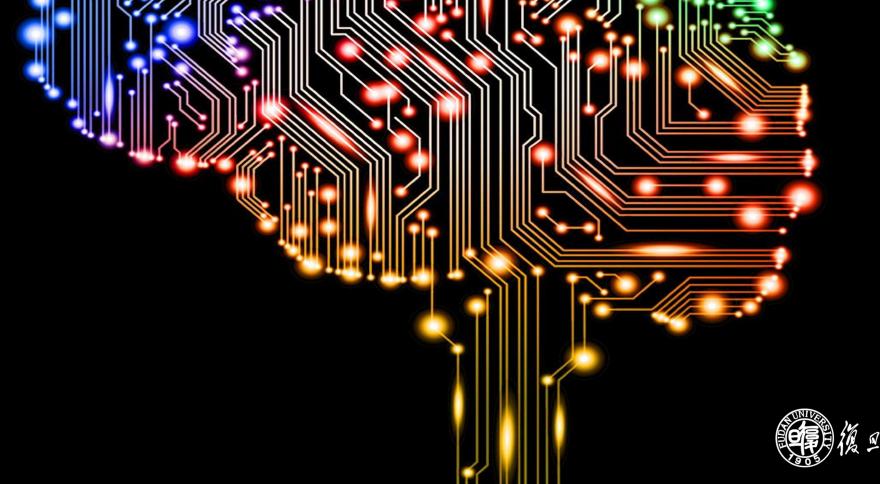
数据驱动的人工智能(3b)神经网络基础

Data Driven Artificial Intelligence

邬学宁 SAP硅谷创新中心 2017 / 03









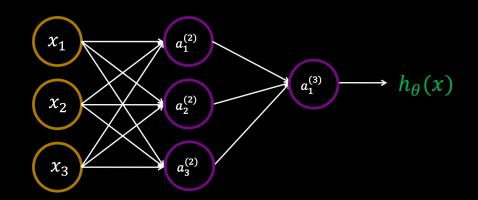


Feeding Forward MLP
Back Propagation
TensorFlow Introduction





ANN: Feeding Forward Vectorization



$$a_{1}^{(2)} = \sigma(\Theta_{10}^{(1)}x_{0} + \Theta_{11}^{(1)}x_{1} + \Theta_{12}^{(1)}x_{2} + \Theta_{13}^{(1)}x_{3})$$

$$a_{2}^{(2)} = \sigma(\Theta_{20}^{(1)}x_{0} + \Theta_{21}^{(1)}x_{1} + \Theta_{22}^{(1)}x_{2} + \Theta_{23}^{(1)}x_{3})$$

$$a_{3}^{(2)} = \sigma(\Theta_{30}^{(1)}x_{0} + \Theta_{31}^{(1)}x_{1} + \Theta_{32}^{(1)}x_{2} + \Theta_{33}^{(1)}x_{3})$$

$$h_{\theta}(x) = a_{1}^{(3)} = \sigma(\Theta_{10}^{(2)}a_{0}^{(2)} + \Theta_{11}^{(2)}a_{1}^{(2)} + \Theta_{12}^{(2)}a_{2}^{(2)} + \Theta_{13}^{(2)}a_{3}^{(2)})$$

$$x = \begin{bmatrix} 1 \\ x_1 \\ x_2 \\ x_3 \end{bmatrix} \quad z^{(2)} = \begin{bmatrix} z_0^{(2)} \\ z_0^{(2)} \\ z_0^{(2)} \\ z_0^{(2)} \end{bmatrix}$$

$$z^{(2)} = \Theta^{(1)} x$$
 $a^{(2)} = \sigma(z^{(2)})$
 $add \ a_0^{(2)} = 1$
 $z^{(3)} = \Theta^{(2)} a^{(2)}$
 $h_{\theta}(x) = a_1^{(3)} = \sigma(z^{(3)})$





Recap: Chain Rule

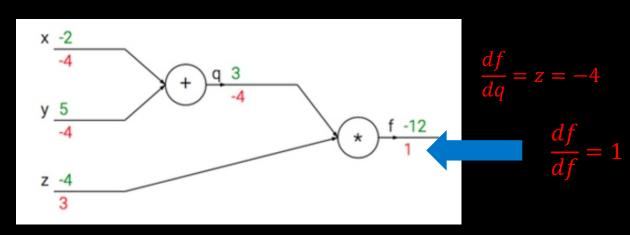
$$f(x,y,z) = (x+y)z$$
 可以写成 $f = qz$,其中 $q = x + y$

$$q = x + y$$
. $\frac{dq}{dx} = 1, \frac{dq}{dy} = 1$
 $f = qz$. $\frac{df}{dq} = z, \frac{df}{dz} = q$

$$\frac{df}{dx} = \frac{df}{dq} \frac{dq}{dx} = z = -4$$

$$\frac{df}{dy} = \frac{df}{dq} \frac{dq}{dy} = z = -4$$

$$\frac{df}{dz} = q = x + y = 3$$







Recap: Chain Rule

Case 1:
$$y = g(x); z = h(y)$$

 $\Delta x \to \Delta y \to \Delta z$

$$\frac{dz}{dx} = \frac{dz}{dy}\frac{dy}{dx}$$

Case 2:
$$x = g(s)$$
; $y = h(s)$; $z = k(x, y)$

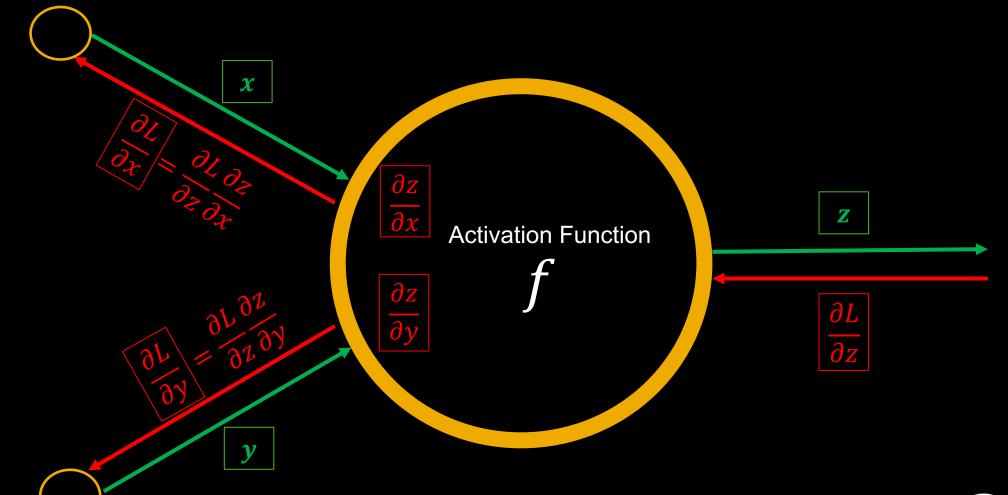
$$\Delta x \rightarrow \Delta y \rightarrow \Delta z$$

$$\frac{dz}{ds} = \frac{dz}{dx}\frac{dx}{ds} + \frac{dz}{dy}\frac{dy}{ds}$$





Activation Function: Back Propagation (BP)

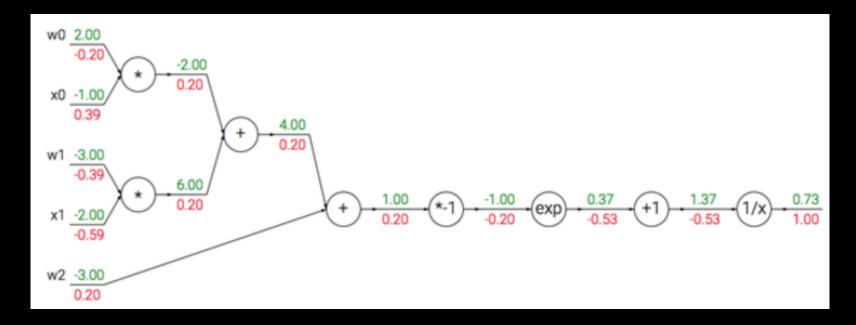






Back Propagation Example

$$f(w,x) = \frac{1}{1 + e^{-(w_0 x_0 + w_1 x_1 + w_2)}}$$



$$f(x) = \frac{1}{x} \qquad \frac{d}{dx}f(x) = -\frac{1}{x^2}$$

$$f(x) = c + x \qquad \frac{d}{dx}f(x) = 1$$

$$f(x) = e^x \qquad \frac{d}{dx}f(x) = e^x$$

$$f(x) = ax \qquad \frac{d}{dx}f(x) = a$$

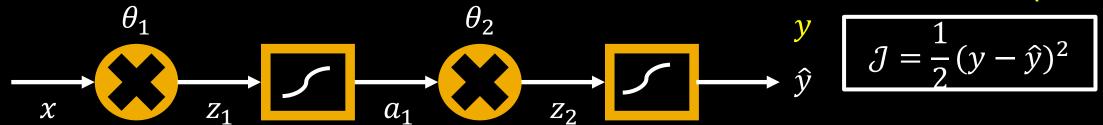
$$-0.53e^{x} = -0.53e^{-1} = -0.20 \qquad (-\frac{1}{x^{2}})(1.00) = -\frac{1}{1.37^{2}} = -0.53$$





← Back Propagation (永远求偏导)

Cost Function (1 row):



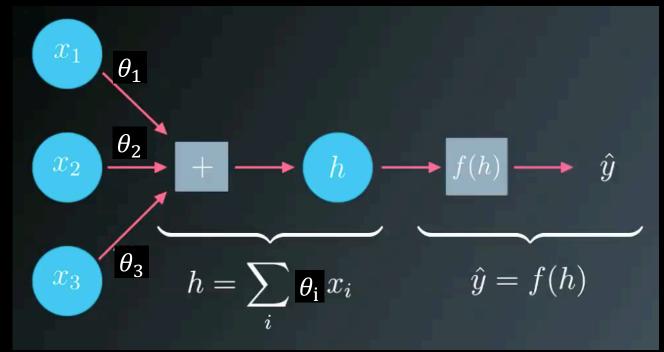
$$\frac{\partial \mathcal{J}}{\partial \theta_2} = \frac{\partial \mathcal{J}}{\partial \hat{y}} \frac{\partial \hat{y}}{\partial \theta_2} = \frac{\partial \mathcal{J}}{\partial \hat{y}} \frac{\partial \hat{y}}{\partial z_2} \frac{\partial z_2}{\partial \theta_2} = 2 \frac{1}{2} (y - \hat{y}) \frac{\partial}{\partial \hat{y}} (y - \hat{y}) \frac{\partial \hat{y}}{\partial z_2} \frac{\partial z_2}{\partial \theta_2}$$

$$= -(y - \hat{y})\hat{y}(1 - \hat{y})a_1$$

$$\frac{\partial \mathcal{J}}{\partial \theta_1} = \frac{\partial \mathcal{J}}{\partial z_2} \frac{\partial z_2}{\partial \theta_1} = \frac{\partial \mathcal{J}}{\partial z_2} \frac{\partial z_2}{\partial a_1} \frac{\partial a_1}{\partial z_1} \frac{\partial z_1}{\partial \theta_1} = -(y - \hat{y})\hat{y}(1 - \hat{y}) \theta_2 a_1 (1 - a_1) x$$







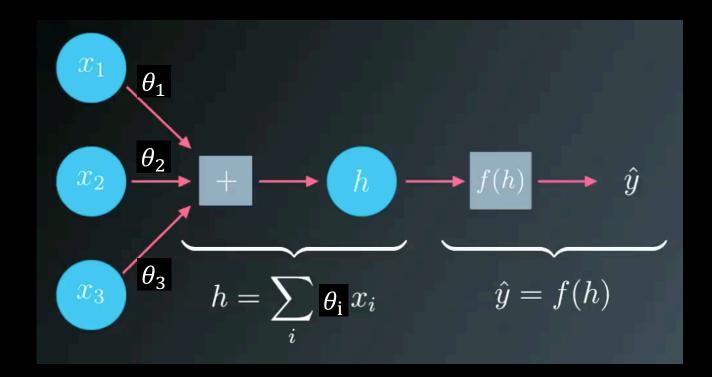
$$\mathcal{J} = \frac{1}{2} \sum_{i} (y^{(i)} - \hat{y}^{(i)})^{2}$$
$$= \frac{1}{2} \sum_{i} (y^{(i)} - f(\sum_{j} \theta_{j} x_{j}^{(i)}))^{2}$$

为了简化问题,我们假设只有一个数据样本,和一个输出节点:

$$\mathcal{J} = \frac{1}{2}(y - \hat{y})^2 = \frac{1}{2}(y - f(\sum_{j} \theta_j x_j)^2)$$







$$\mathcal{J} = \frac{1}{2} (y - f \left(\sum_{j} \theta_{j} x_{j} \right))^{2}$$

$$\theta_{j} = \theta_{j} + \Delta \theta_{j}$$

$$\theta_{j} \propto -\frac{\partial \mathcal{J}}{\partial \theta_{j}}$$

$$\theta_{j} = -\alpha \frac{\partial \mathcal{J}}{\partial \theta_{i}}$$

$$\frac{\partial \mathcal{J}}{\partial \theta_j} = \frac{\partial}{\partial \theta_j} \frac{1}{2} (y - \hat{y})^2 = (y - \hat{y}) \frac{\partial}{\partial \theta_j} (y - \hat{y}) = -(y - \hat{y}) \frac{\partial}{\partial \theta_j} f(\sum_j \theta_j x_j)$$



$$= -(y - \hat{y}) f'(h)x_j$$
 where $h = \sum_j \theta_j x_j$



$$\frac{\partial \mathcal{J}}{\partial \theta_i} = -(y - \hat{y})f'(h)x_i \qquad \Delta \theta_i = \alpha(y - \hat{y})f'(h)x_i$$

为了方便,我们定义: $\delta = (y - \hat{y})f'(h)$

* 对于Sigmoid 激活函数: f'(h) = f(h)(1 - f(h))

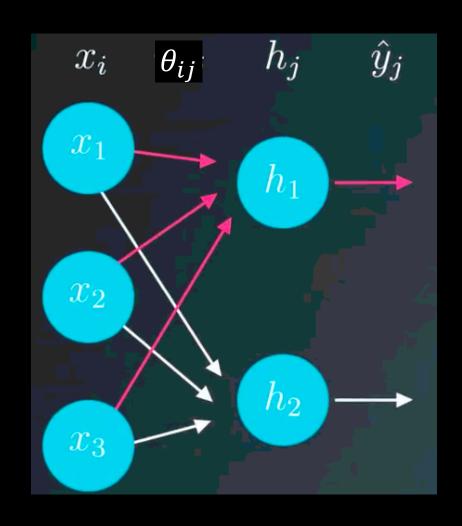
所以,我们可将权重更新公式重写为:

$$\theta_i = \theta_i + \alpha \delta x_i$$





△ 反向传播与梯度下降(多输出节点)



$$\delta = (y - \hat{y})f'(h)$$

$$\delta_j = (y_j - \widehat{y_j})f'(h_j)$$

$$\Delta\theta_i = \alpha\delta x_i$$

$$\Delta\theta_{ij} = \alpha\delta_j x_i$$





```
import numpy as np
def sigmoid(x):
    return 1/(1+np.exp(-x))
def sigmoid_prime(x):
    return sigmoid(x) * (1 - sigmoid(x))
# Input/output/weights data
x = np.array([0.1, 0.3])
   0.2
weights = np.array([-0.8, 0.5])
learnrate = 0.5
```

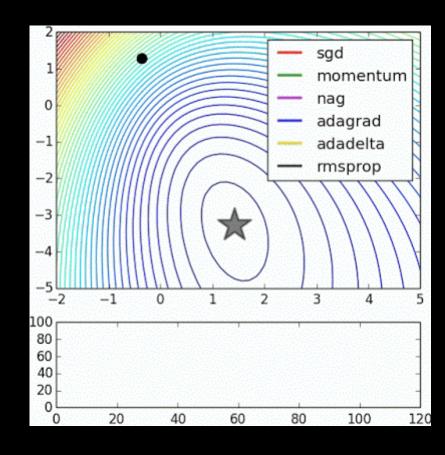
```
\delta_j = (y_j - \widehat{y_j})f'(h_j)
\Delta\theta_{ii} = \alpha\delta_i x_i
```

```
# the linear combination performed by the node
h = np.dot(x, weights)
# The neural network output (y-hat)
nn output = sigmoid(h)
# output error (y - y-hat)
error = y - nn_output
# output gradient (f'(h))
output_grad = sigmoid_prime(h)
# error term (lowercase delta)
delta = error * output_grad
# Gradient descent step
del_w = learnrate * delta * x
print(del_w)
```





▲ 参数更新



logistic regression on noisy moons







1st Example of Keras

```
from keras.models import Sequential
from keras.layers import Dense
model = Sequential()
model.add(Dense(10, input_dim=20, kernel_initializer = 'random_uniform'))
```

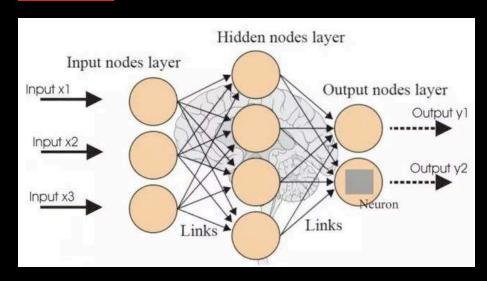
- Sequential: the simplest model, a sequential Keras model is a linear pipeline (a stack) of neural networks layer.
- model.add define a single layer with 10 artificial neurons, and it expects 20 features
- Each neuron can be initialized with random_uniform (-0.05, 0.05).
- Weights can also be initialized with random_normal and zero.
- Dense means each neuron in a layer is connected to all neurons located in the previous layer and to all the neurons in the following layer.

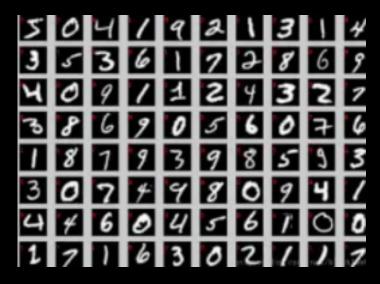






Multilayer Perceptron (MLP) & MNIST





- Perceptron are usually single layer.
- *MNIST*, a database of handwritten digits (Gray Scale) made up of 60,000 examples and a test set of 10,000 examples. Each image contains 28x28 pixels.
- The training examples are annotated by humans with correct answer (Supervised Learning).







Sample Code 1 (Base Line)

```
# Imports
import keras
from keras.datasets import mnist
from keras.models import Sequential
from keras.layers import Dense, Activation, Dropout
from keras.optimizers import SGD
# Hyperparameters
NB EPOCHS = 10
BATCH_SIZE = 128
NB CLASSES = 10
VALIDATION SPLIT = 0.2
# Load Data
# X_train is 60000 rows of 28*28 values, X_test is 10000 rows of 28*28
(X_train, y_train),(X_test, y_test) = mnist.load_data()
# flatten and convert to float32 for normalization
X train = X train.reshape(60000, 784)
X_{\text{test}} = X_{\text{test.reshape}}(10000, 784)
X_train = X_train.astype('float32')
X_test = X_test.astype('float32')
```







Sample Code 2 (Base Line)

```
# Normalize
X_train /= 255
X_test /= 255
```

```
# Convert class into one-hot encoding
Y_train = keras.utils.to_categorical(y_train, NB_CLASSES)
Y_test = keras.utils.to_categorical(y_test, NB_CLASSES)
```

```
# Build the model
model = Sequential()
model.add(Dense(NB_CLASSES, input_shape=(784,)))
model.add(Activation('softmax'))
```

- Softmax is the generalization of logistic regression!
- Softmax squash a k-dimensional vector of arbitrary value into a same dimensional real value vectors in the range of (0,1) and add up to 1.

model.compile(loss='categorical_crossentropy',optimizer=SGD(), metrics=['accuracy'])

- Cost / Objective Functions
 - MSE
 - Binary Cross-entropy
 - Categorical Cross-entropy

- Evaluation Metrics:
 - Accuracy
 - Precision / Recall







44 K Accuracy / Precision / Recall

			PREDI true	CTION false	
	X.I.I.	true	4		
	REALIT	fallse	c		
accuracy: "what percent of the prediction were correct?"					(*+b) (*+b+b+b)
precision: "what percent of positive predictions were correct?"					(1+1)
recall: "what percent of positive cases were caught?"					(a) (a+b)







Sample Code 2 (Base Line)

```
history = model.fit(X_train, Y_train, batch_size = BATCH_SIZE, epochs = NB_EPOCHS, verbose = 1,
                   validation_data=(X_test,Y_test))
score = model.evaluate(X_test, Y_test, verbose=0)
print(score)
```

- Epochs: the number of times the model is exposed to the training set, at each iteration, the optimizers tries to adjust the weights to minimize the objective function.
- Batch Size: The number of training instance observed before the optimizer performs a weight update.







Sample Code 2 (Base Line)







Hidden layer Added (Relu)

```
# Build the model
model = Sequential()

model.add(Dense(512, activation='relu', input_shape=(784,)))

model.add(Dense(512, activation='relu'))

model.add(Dense(10, activation='softmax'))
```

- Add 2 hidden layers
- Reduce the Epoch to 20

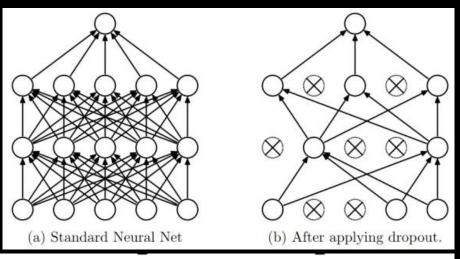






Hidden layer Added (Dropout)

```
model = Sequential()
model.add(Dense(512, activation='relu', input_shape=(784,)))
model.add(Dropout(0.2))
model.add(Dense(512, activation='relu'))
model.add(Dense(512, activation='relu'))
model.add(Dropout(0.2))
model.add(Dense(10, activation='softmax'))
```



```
Epoch 15/20
60000/60000 [=============] - 7s - loss: 0.1700 - acc: 0.9499 - val_loss: 0.1384 - val_acc: 0.9572
Epoch 16/20
60000/60000 [=============] - 7s - loss: 0.1620 - acc: 0.9521 - val_loss: 0.1343 - val_acc: 0.9580
Epoch 17/20
60000/60000 [=============] - 7s - loss: 0.1554 - acc: 0.9539 - val_loss: 0.1290 - val_acc: 0.9589
Epoch 18/20
60000/60000 [==============] - 7s - loss: 0.1493 - acc: 0.9564 - val_loss: 0.1244 - val_acc: 0.9608
Epoch 19/20
60000/60000 [================] - 7s - loss: 0.1424 - acc: 0.9580 - val_loss: 0.1207 - val_acc: 0.9616
Epoch 20/20
60000/60000 [===============] - 7s - loss: 0.1383 - acc: 0.9598 - val_loss: 0.1166 - val_acc: 0.9625
```







Regularization Implementation

```
from keras import regularizers
model.add(Dense(64, input_dim = 64, kernel_regularizer=regularizers.l2(0.01)))
```







Advance Optimizer (RMSprop & Adam)

from keras.optimizers import

RMSprop, Adam

RMSprop and Adam includes the concept of *Momentum*.

model.compile(loss='categorical_crossentropy'

optimizer=RMSprop(), met

metrics=['accuracy'])

```
SGD
Momentum
NAG
Adagrad
Adadelta
Rmsprop
```

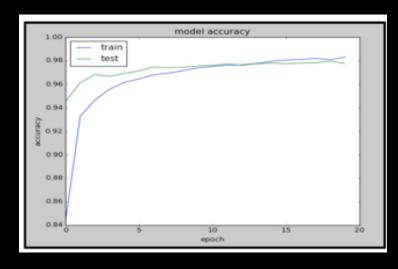
```
Epoch 19/20
60000/60000 [=========] - 7s - loss: 0.0429 - acc: 0.9917 - val_loss: 0.1144 - val_acc: 0.9840
Epoch 20/20
60000/60000 [==========] - 8s - loss: 0.0382 - acc: 0.9927 - val_loss: 0.1089 - val_acc: 0.9846
```

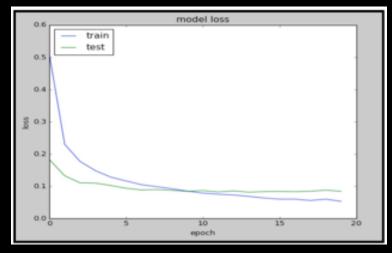


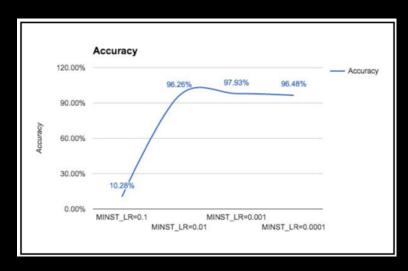


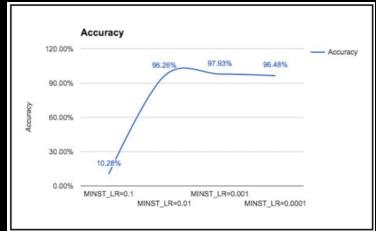


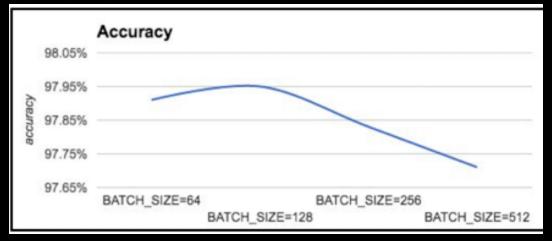
Hyper parameters

















Hello World!

```
import tensorflow as tf
hello_constant = tf.constant('Hello World!')
with tf.Session() as sess:
    output = sess.run(hello_constant)
    print(output)
```







Linear Regression

```
numpy - as - np
       tensorflow as tf
       sklearn
       matplotlib.pyplot as plt
learning_rate = 0.01
training_epochs = 1000
display_steps = 100
train_X = np.array([3.3,4.4,5.5,6.71,6.93,4.168,9.779,6.182,7.59,2.167,7.042,10.791,5.313,7.997,5.654,9.27,3.1])
train_Y = np.array([1.7, 2.76, 2.09, 3.19, 1.694, 1.573, 3.366, 2.596, 2.53, 1.221, 2.827, 3.465, 1.65, 2.904, 2.42, 2.94, 1.3])
n_samples = train_X.shape[0]
X = tf.placeholder("float")
Y = tf.placeholder("float")
W = tf.Variable(np.random.randn(), name = 'weight')
b = tf.Variable(np.random.randn(), name = 'bias')
pred = tf.add(tf.mul(X,W),b)
cost = tf.reduce_sum(tf.pow(pred-Y,2))/2/n_samples
optimizer = tf.train.GradientDescentOptimizer(learning_rate).minimize(cost)
      tf.Session()
init = tf.global_variables_initializer()
sess.run(init)
    epoch in range(training_epochs):
        (x,y) in zip(train_X,train_Y):
        sess.run(optimizer, feed_dict={X:x,Y:y})
       epoch % 100 = 0:
        c = sess.run(cost, feed_dict={X:x,Y:y})
        -print('epoch=',epoch,'cost=',c,'weight=',sess.run(W),'bias=',sess.run(b))
print('Optimization Finished')
```







Logistic/Softmax Regression

```
import tensorflow as tf
from tensorflow.examples.tutorials.mnist import input_data
mnist = input_data.read_data_sets("/tmp/data/", one_hot=True)
learning_rate = 0.01
training_epochs = 25
batch size = 100
display_step = 1
x = tf.placeholder(tf.float32, [None, 784])
y = tf.placeholder(tf.float32, [None, 10])
W = tf.Variable(tf.random_normal([784,10]))
b = tf.Variable(tf.random_normal([10]))
    = tf.nn.softmax(tf.matmul(x, W) + b)
cost = tf.reduce_mean(-tf.reduce_mean(y*tf.log(pred), reduction_indices=1))
optimizer = tf.train.GradientDescentOptimizer(learning_rate).minimize(cost)
init = tf.global_variables_initializer()
sess = tf.Session()
sess.run(init)
for epoch in range(training_epochs):
    num_batch = int(mnist.train.num_examples/batch_size)
    for i in range(num batch):
        batch xs,batch ys = mnist.train.next batch(batch size)
        c = sess.run([optimizer, cost], feed_dict ={x: batch_xs, y:batch_ys})
```







Thank you!

Contact information:

邬学宁 (i025497)

Chief Data Scientist, SAP Silicon Valley Innovation Center

Address: No. 1001, Chenghui Road, Shanghai, 201023

Phone number: +8621-6108 5287

Email: x.wu@sap.com