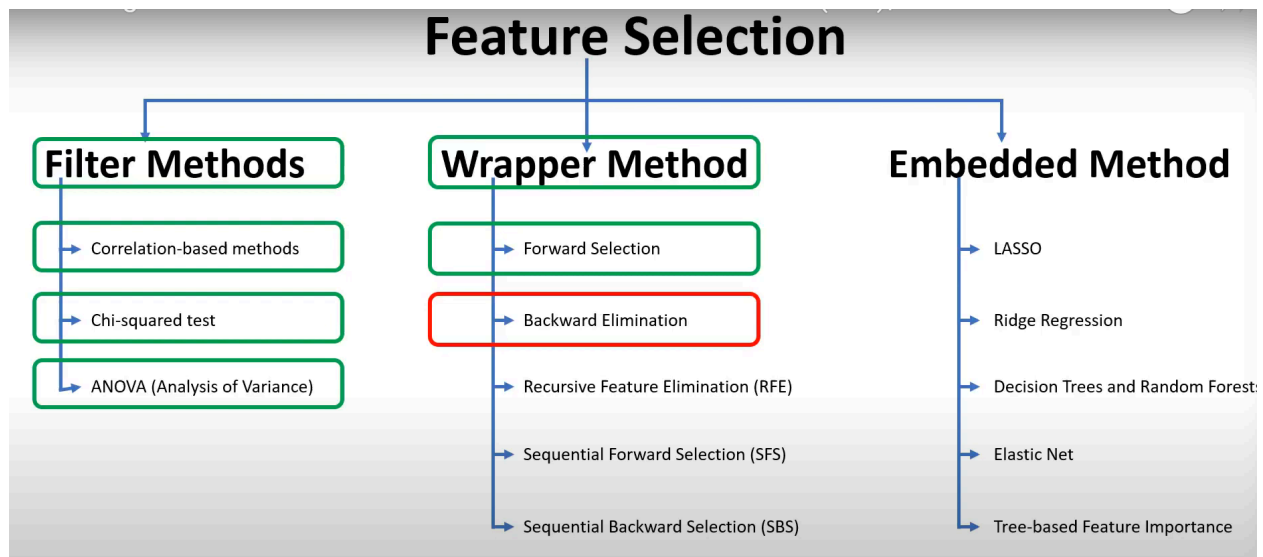


Feature Selection (Filter Methods) (VVIMP-Interview)



- **Feature selection** is the process of choosing a subset of relevant features (variables) for use in a model.
- This is important because not all features contribute to the model's performance, and irrelevant or redundant features can lead to overfitting, increased complexity, and slower computation.
- If your data has 10-15 columns, there's not much need do the feature selection.

Why Feature Selection?

- **Improve Model Performance:** Focuses the model on meaningful patterns.
- **Reduce Overfitting:** Minimizes noise from irrelevant features.
- **Speed Up Training:** Fewer features mean faster computations.
- **Enhance Interpretability:** Simplifies understanding of model decisions.

- **Curse of dimensionality:** As the dimensions increase, the distance between points also increase and therefore it is not reliable if there are too many dimensions.

Types of Feature Selection Methods

1. **Filter Methods**
2. **Wrapper Methods**
3. **Embedded Methods**
4. Hybrid



a. Filter Methods

- **Approach:** Use statistical measures to score feature relevance.
- **Pros:** Fast and model-agnostic.
- **Cons:** Ignores feature interactions.
- **Techniques:**
 - **Correlation:** Pearson's, Spearman's.
 - **Variance Thresholding:** Remove low-variance features.
 - **Chi-Squared Test:** For categorical data.
 - **Mutual Information:** Measures dependency.

b. Wrapper Methods

- **Approach:** Evaluate feature subsets based on model performance.
- **Pros:** Considers feature interactions.
- **Cons:** Computationally expensive.
- **Techniques:**
 - **Forward Selection:** Add features one by one.

- **Backward Elimination:** Remove features one by one.
- **Recursive Feature Elimination (RFE):** Iteratively removes the least important features.

c. Embedded Methods

- **Approach:** Feature selection during model training.
- **Pros:** Balances efficiency and accuracy.
- **Techniques:**
 - **Lasso (L1 Regularization):** Shrinks less important coefficients to zero.
 - **Tree-Based Models:** Use feature importance (e.g., Random Forest, XGBoost).

1. Filter Methods

- Individually studies each feature with statistical techniques like correlation or variance and decides if to keep it or not.
- Focuses on 1 feature at a time
- **Pros:** Fast and model-agnostic.
- **Cons:** Ignores feature interactions.

Common techniques:

- **Correlation Matrix:** Select features that are **not highly correlated** with each other.
- **Chi-Square Test:** Tests the independence between features and the target variable (used for categorical data).
- **Variance Threshold:** Removes features with low variance, assuming low variance means little to no information.
- **ANOVA**

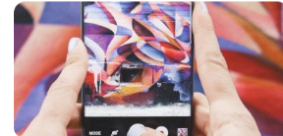
- **Mutual Info**

Dataset Used:

- <https://www.kaggle.com/datasets/uciml/human-activity-recognition-with-smartphones>

Human Activity Recognition with Smartphones

Recordings of 30 study participants performing activities of daily living



Data Card Code (426) Discussion (14) Suggestions (0)

Columns → **563**

AIM : Reduce 563 → 100 without losing the results

No linear regression → Because output is classification (we'll use logistic regression)

```
df = pd.read_csv(r'Human_Activity\train.csv').drop(columns='subject')
df.head()
```

	tBodyAcc-mean()-X	tBodyAcc-mean()-Y	tBodyAcc-mean()-Z	tBodyAcc-std()-X	tBodyAcc-std()-Y	tBodyAcc-std()-Z	tBodyAcc-mad()-X	tBodyAcc-mad()-Y	tBodyAcc-mad()-Z	tBodyAcc-max()-X	...	fBodyBodyGyroJerkMag-skewness()
0	0.288585	-0.020294	-0.132905	-0.995279	-0.983111	-0.913526	-0.995112	-0.983185	-0.923527	-0.934724	...	-0.298676
1	0.278419	-0.016411	-0.123520	-0.998245	-0.975300	-0.960322	-0.998807	-0.974914	-0.957686	-0.943068	...	-0.595051
2	0.279653	-0.019467	-0.113462	-0.995380	-0.967187	-0.978944	-0.996520	-0.963668	-0.977469	-0.938692	...	-0.390748
3	0.279174	-0.026201	-0.123283	-0.996091	-0.983403	-0.990675	-0.997099	-0.982750	-0.989302	-0.938692	...	-0.117290
4	0.276629	-0.016570	-0.115362	-0.998139	-0.980817	-0.990482	-0.998321	-0.979672	-0.990441	-0.942469	...	-0.351471

5 rows × 562 columns

- We dropped 'Subject' as we're dealing with categorical variables
- All these values are **scaled (-1 to +1)**
- **Output → Activity**

```
df['Activity'].value_counts()
```

```
Activity
LAYING      1407
STANDING    1374
SITTING     1286
WALKING     1226
WALKING_UPSTAIRS  1073
WALKING_DOWNSTAIRS  986
Name: count, dtype: int64
```

```
print(df.shape)
```

Output: (7352, 562)

First, apply logistic regression

```
from sklearn.preprocessing import LabelEncoder #CAT → Numeric
from sklearn.model_selection import train_test_split
from sklearn.linear_model import LogisticRegression
from sklearn.metrics import accuracy_score
```

```
# Separate features and target
```

```
X = df.drop('Activity', axis=1)
```

```
y = df['Activity']
```

```
# Encode target labels
```

```
le = LabelEncoder()
```

```
y = le.fit_transform(y)
```

```
# Split data into training and testing sets
```

```
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2, random_state=42)
```

LabelEncoder : This is used to **convert categorical labels** (like 'cat', 'dog', 'fish') into numerical values (e.g., 0, 1, 2) so that they can be used in machine learning models that require numerical inputs.

```
print(X_train.shape)
print(X_test.shape)
```

Output:

```
(5881, 561)
```

```
(1471, 561)
```

Apply Logistic Regression:

```
# Initialize and train logistic regression model
log_reg = LogisticRegression(max_iter=1000) # Increase max_iter if it doesn't
converge
log_reg.fit(X_train, y_train)
```

```
# Make predictions on the test set
y_pred = log_reg.predict(X_test)
```

```
# Calculate and print accuracy score
accuracy = accuracy_score(y_test, y_pred)
print("Test accuracy:", accuracy)
```

Output:

```
Test accuracy: 0.9809653297076818
```

- **Accuracy score** is used here because the problem is a **classification task**, where the goal is to predict **categories** (e.g., 'yes' or 'no').
- Accuracy measures how many predictions match the true labels.
- On the other hand, **R² (R-squared)** is used for **regression tasks**, where the goal is to predict continuous values.

Delete Duplicate Columns

```
def get_duplicate_columns(df):

    duplicate_columns = {}
    seen_columns = {}

    for column in df.columns:
        current_column = df[column]

        # Convert column data to bytes
        try:
            current_column_hash = current_column.values.tobytes()
        except AttributeError:
            current_column_hash = current_column.to_string().encode()

        if current_column_hash in seen_columns:
            if seen_columns[current_column_hash] in duplicate_columns:
                duplicate_columns[seen_columns[current_column_hash]].append(column)
            else:
                duplicate_columns[seen_columns[current_column_hash]] = [column]
        else:
            seen_columns[current_column_hash] = column

    return duplicate_columns
```

Simpler Code to delete Duplicates

```
def remove_duplicate_columns(df):  
    # Transpose the DataFrame to compare columns as rows  
    transposed_df = df.T  
  
    # Find duplicate rows (which are the original columns)  
    duplicate_columns = transposed_df[transposed_df.duplicated()].index.tolist()  
()  
  
    # Drop duplicate columns from the original DataFrame  
    df_cleaned = df.drop(columns=duplicate_columns)  
  
    return df_cleaned
```

.index : In Pandas, every DataFrame or Series has an **index** property, which stores the row labels. In the case of a transposed DataFrame (**df.T**), the **index** represents the column names from the original DataFrame.

.tolist() : This method converts the Pandas Index object (which holds column names) into a standard Python list.

So when we call

transposed_df[transposed_df.duplicated()].index.tolist() , it identifies the index labels (which are the original column names) of the rows that are duplicated. These column names are returned as a list.

```
X_train=remove_duplicate_columns(X_train)
```


	tBodyAcc-mean()-X	tBodyAcc-mean()-Y	tBodyAcc-mean()-Z	tBodyAcc-std()-X	tBodyAcc-std()-Y	tBodyAcc-std()-Z	tBodyAcc-mad()-X	tBodyAcc-mad()-Y	tBodyAcc-mad()-Z	t
57	0.278007	-0.017803	-0.108965	-0.994425	-0.994873	-0.994886	-0.994939	-0.993994	-0.995450	t
4154	0.237617	-0.000782	-0.114476	-0.326331	0.069663	-0.224321	-0.343326	0.039623	-0.256327	t
6945	0.290924	-0.050878	-0.073518	-0.026220	-0.032163	0.393109	-0.118256	-0.030279	0.432861	t
527	0.275268	-0.015050	-0.114204	-0.981092	-0.901124	-0.960423	-0.984417	-0.901405	-0.965788	t
4196	0.278790	-0.018585	-0.106908	-0.997380	-0.983893	-0.984482	-0.997331	-0.985196	-0.983768	t
...	t
5191	0.278897	-0.030306	-0.096043	-0.555352	-0.104055	-0.438064	-0.572530	-0.112149	-0.429688	t
5226	0.289183	-0.049248	-0.125083	-0.290043	-0.212102	-0.469731	-0.307317	-0.209558	-0.528635	t
5390	0.293946	-0.018341	-0.119916	-0.627198	-0.216566	-0.424764	-0.648666	-0.253814	-0.417569	t
860	0.280475	-0.018976	-0.113756	-0.994825	-0.985314	-0.965857	-0.995170	-0.984285	-0.963293	t
7270	0.263582	0.006928	-0.095320	-0.368655	-0.142631	-0.151250	-0.426026	-0.130656	-0.149079	t
5881 rows × 540 columns										

do the same for X_test

```
X_test= remove_duplicate_columns(X_test)
```

✓ 0.1s

	tBodyAcc-mean()-X	tBodyAcc-mean()-Y	tBodyAcc-mean()-Z	tBodyAcc-std()-X	tBodyAcc-std()-Y	tBodyAcc-std()-Z
4525	0.283203	-0.047024	-0.168986	0.384949	0.176898	-0.310332
1446	0.256904	-0.036623	-0.133856	0.201409	-0.154142	0.344183
5995	0.291316	-0.001065	-0.072461	-0.336609	-0.279162	-0.303323
4222	0.276116	-0.010909	-0.102886	-0.992196	-0.982169	-0.981127
6754	0.256382	0.000428	-0.113664	0.075014	0.046502	-0.369482
...
3704	0.288089	-0.024497	-0.095596	-0.947145	-0.835807	-0.895158
705	0.276959	-0.003011	-0.116333	-0.975745	-0.876568	-0.932322
1650	0.284576	-0.020942	-0.106882	-0.994198	-0.988329	-0.990618
2260	0.277980	-0.019820	-0.109165	-0.997517	-0.982207	-0.974343
5907	0.283935	-0.020993	-0.115315	-0.997183	-0.989286	-0.993926
1471 rows × 540 columns						

Variance Threshold

```
from sklearn. feature_selection import VarianceThreshold
```

- Removes features with low variance, assuming low variance means little to no information.

A	B	C
1	1	X
2	1	N
3	1	X

- Here, B is constant
- It doesn't play any role in prediction
- We can drop such columns
- If values of 95% columns is 1 and remaining 5% is → It's Quasi Constant column
 - Its variance is close to 0

Steps

- Normalize data*
- Decide a **threshold (eg. 0.1)**
 - 0.01 to 0.1**
 - Calculate **variance** for every column
 - Check** which columns' threshold is **less than our decided threshold**
 - Drop em 🙌

```
from sklearn.feature_selection import VarianceThreshold
sel = VarianceThreshold(threshold=0.05)
sel.fit(X_train)
```

Check which columns' threshold is **more**:

```
sum(sel.get_support())
```

Output: 349

Output: 349

- `sel.get_support()` → returns boolean values: True/False

```
sel.get_support()
```

✓ 0.0s

```
array([False, False, False, True, True, True, True, True, True,  
       True, True, True, True, True, True, True, True, False,  
       False, True, True, True, True, True, True, True, True,  
       True, True, True, False, False, False, True, False, True,  
       True, True, True, True, True, True, True, False, False,  
       False, False, False, False, True, True, True, True, True,  
       True, True, True, True, True, False, False, False, True,  
       True, True, False, False, False, False, True, True, True,  
       True, True, True, True, True, True, True, True, False,  
       False, False, True, True, True, True, True, True, True,  
       True, True, True, True, True, True, True, False, True,  
       True, True, True, True, True, True, True, False, True,
```

False = columns' threshold is **less** than our decided one

To see the column names:

```
columns = X_train.columns[sel.get_support()]
columns
```

```
Index(['tBodyAcc-std()-X', 'tBodyAcc-std()-Y', 'tBodyAcc-std()-Z',
      'tBodyAcc-mad()-X', 'tBodyAcc-mad()-Y', 'tBodyAcc-mad()-Z',
      'tBodyAcc-max()-X', 'tBodyAcc-max()-Y', 'tBodyAcc-max()-Z',
      'tBodyAcc-min()-X',
      ...,
      'fBodyBodyGyroJerkMag-meanFreq()', 'fBodyBodyGyroJerkMag-skewness()',
      'fBodyBodyGyroJerkMag-kurtosis()', 'angle(tBodyAccMean,gravity)',
      'angle(tBodyAccJerkMean,gravityMean)',
      'angle(tBodyGyroMean,gravityMean)',
      'angle(tBodyGyroJerkMean,gravityMean)', 'angle(X,gravityMean)',
      'angle(Y,gravityMean)', 'angle(Z,gravityMean)'],
      dtype='object', length=349)
```

Let's insert these columns in X_train & X_test:

```
X_train = sel.transform(X_train)
X_test = sel.transform(X_test)
```

```
X_train = pd.DataFrame(X_train, columns=columns)
X_test = pd.DataFrame(X_test, columns=columns)
```

`X_train = sel.transform(X_train)` : This is where the actual feature selection happens for your training data.

- The `sel.transform(X_train)` → It deletes all columns except the above ones
- But it returns a **(NumPy array)** containing only the *selected* features (columns) - those that had a variance greater than 0.05.

Why we used `pd. DataFrame (X_train, columns=columns)` ?

- **NumPy arrays → Pandas DataFrames**
- After `sel.transform(X_train)` and `sel.transform(X_test)`, `X_train` and `X_test` are no longer Pandas DataFrames. They become NumPy arrays.
- To convert them back into Pandas DataFrames (which are often easier to work with, especially if you want to keep column names), you use

```
pd.DataFrame() .
```



New sklearn: `.set_output()` → Get the output as DataFrame

`fit` VS `transform` VS `fit_transform`

- `fit` is used on the **training data** to avoid any potential data leakage.
- `transform` is then used on both the training and test data to ensure the same features are selected in both.
- Using `fit_transform` on the test set would improperly use test data during training, which violates the principles of machine learning and can lead to biased results.

```
print(X_train.shape)
print(X_test.shape)
```

Output:

```
(5881, 349)
```

```
(1471, 349)
```

Points to Consider whiles using variance threshold:

It:

- Ignores Target Variable
- Ignores Feature Interactions
- Sensitive to Data Scaling
- Arbitrary Threshold Value

Correlation

- Pearson

Disadvantages of Correlation:

1. **Linearity Assumption:** Only measures **linear** relationships, not non-linear ones.
2. **Limited to Two Variables:** Doesn't capture **complex relationships** involving more than two variables.
3. **Threshold Determination:** Defining what's considered a "**high**" correlation is **subjective**.
4. **Sensitive to Outliers:** A few extreme values can **skew** the correlation coefficient.

```
X_train.corr()
```

	tBodyAcc-std()-X	tBodyAcc-std()-Y	tBodyAcc-std()-Z	tBodyAcc-mad()-X	tBodyAcc-mad()-Y	tBodyAcc-mad()-Z	tBodyAcc-max()-X	tBodyAcc-max()-Y
tBodyAcc-std()-X	1.000000	0.927247	0.850268	0.998631	0.920936	0.845200	0.981284	0.977614
tBodyAcc-std()-Y	0.927247	1.000000	0.895065	0.922627	0.997384	0.894128	0.917831	0.911863
tBodyAcc-std()-Z	0.850268	0.895065	1.000000	0.842986	0.890973	0.997414	0.852711	0.852711
tBodyAcc-mad()-X	0.998631	0.922627	0.842986	1.000000	0.916201	0.838010	0.973704	0.973704
tBodyAcc-mad()-Y	0.920936	0.997384	0.890973	0.916201	1.000000	0.890707	0.911283	0.911283
tBodyAcc-mad()-Z	0.845200	0.894128	0.997414	0.838010	0.890707	1.000000	0.852711	0.852711
tBodyAcc-max()-X	0.981284	0.917831	0.852711	0.973704	0.911283	0.852711	1.000000	0.999999
tBodyAcc-max()-Y	0.977614	0.911863	0.852711	0.973704	0.911283	0.852711	0.999999	1.000000
tBodyAcc-max()-Z	0.977614	0.911863	0.852711	0.973704	0.911283	0.852711	0.999999	0.999999
...
tBodyGyroMean,gravityMean	0.023914	-0.002241	-0.010535	0.024098	-0.005865	-0.014838	0.029230	-0.000000
tBodyGyroJerkMean,gravityMean	-0.035176	-0.028881	-0.016002	-0.035629	-0.026679	-0.016949	-0.038935	-0.000000
angle(X,gravityMean)	-0.374114	-0.383095	-0.344114	-0.370629	-0.379578	-0.346350	-0.386159	-0.000000
angle(Y,gravityMean)	0.472605	0.524945	0.475241	0.467965	0.526803	0.476498	0.482312	0.000000
angle(Z,gravityMean)	0.393209	0.432180	0.480824	0.389139	0.430548	0.477627	0.404088	0.000000

Here, we can take 2 approaches:

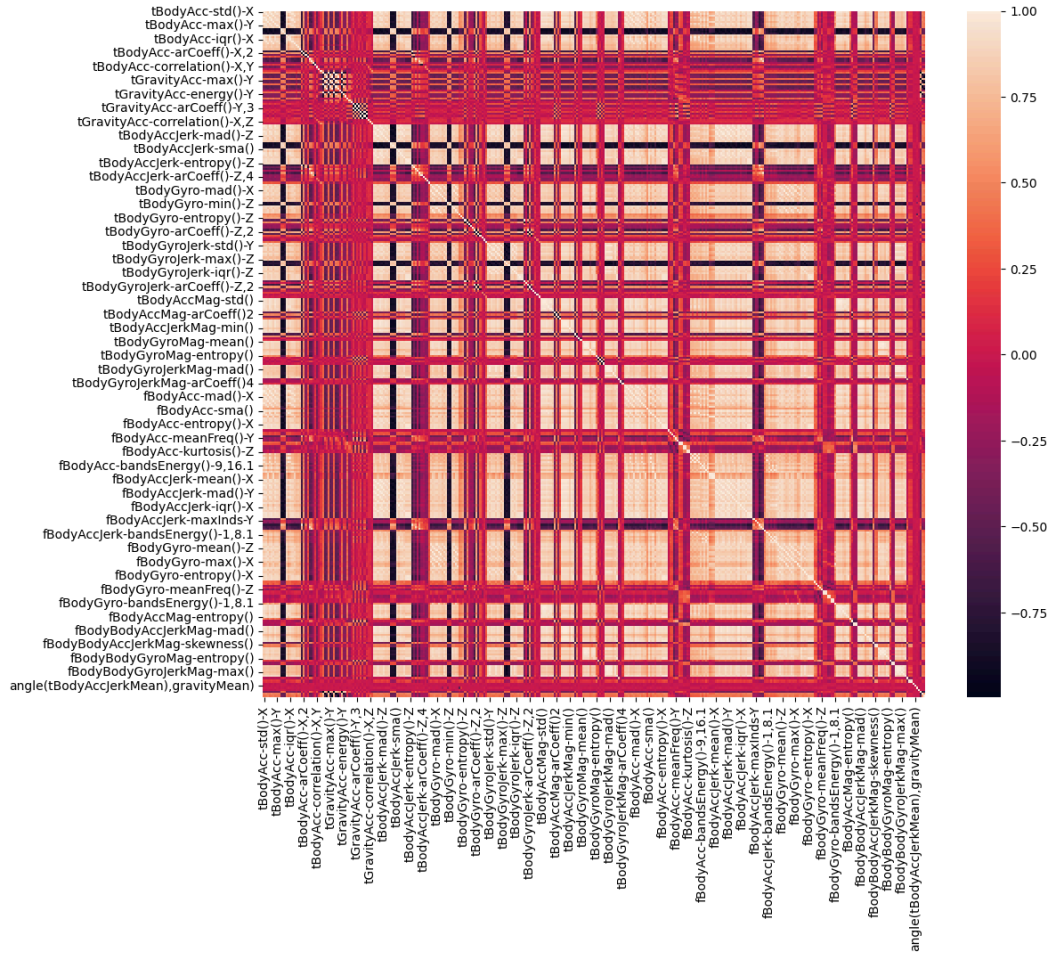
1. Find out corr with y

- Decide a range - eg. -0.3 to +0.3
 - If it's below -0.3 or above 0.3, keep the column
2. Find corr **between columns**
- Select a threshold
 - If Corr is above absolute value, drop that column
 - This is to check **multicollinearity**
 - This is mostly used approach

What's our approach?

- Find out corr between columns
- If it's more than 0.95 → drop 1 of the columns

```
import matplotlib.pyplot as plt
plt.figure(figsize=(12,10))
sns.heatmap(X_train.corr())
```



```
corr_matrix = X_train.corr()
```

```
# Get the column names of the DataFrame
```

```
columns = corr_matrix.columns
```

```
# Create an empty list to keep track of columns to drop
```

```
columns_to_drop = []
```

```
# Loop over the columns
```

```
for i in range(len(columns)):
```

```
    for j in range(i + 1, len(columns)):
```

```
        # Access the cell of the DataFrame
```



```
if corr_matrix.loc[columns[i], columns[j]] > 0.95:
    columns_to_drop.append(columns[j])
```

```
print(len(columns_to_drop))
```

`columns = corr_matrix.columns` : This line extracts the column names

```
for i in range(len(columns)):
    for j in range(i + 1, len(columns)):
```

Starting

`j` from `i + 1` ensures we only iterate through the *upper triangle* of the correlation matrix (excluding the diagonal and the lower triangle), thus avoiding redundant comparisons and also avoiding comparing a column with itself.

Remember

```
corr_matrix.loc[columns[0], columns[1]]
```

This will access this value:

	tBodyAcc-std()-X	tBodyAcc-std()-Y	tBodyAcc-std()-Z
tBodyAcc-std()-X	1.000000	0.927247	0.850268
tBodyAcc-std()-Y	0.927247	1.000000	0.895065
tBodyAcc-std()-Z	0.850268	0.895065	1.000000
tBodyAcc-mad()-X	0.998631	0.922627	0.842986
tBodyAcc-mad()-Y	0.920936	0.997384	0.890973

- `columns[0]` which is `'tBodyAcc-std()-X'` is used as the **row label**.
- `columns[1]` which is `'tBodyAcc-std()-Y'` is used as the **column label**.

How It Avoids Duplicate Checking:

- The key part is `for j in range(i + 1, len(columns))`.
 - When `i = 0`, `j` will start from **1**, so it compares column 0 with column 1, column 2, and so on.
 - When `i = 1`, `j` will start from **2**, so it compares column 1 with column 2, column 3, and so on.
 - When `i = 2`, `j` will start from **3**, so it compares column 2 with column 3, column 4, and so on.



It will go through the upper triangle.

```
if corr_matrix.loc[columns[i], columns[j]] > 0.95:  
    columns_to_drop.append(  
        columns[j] )
```

- If two features have a correlation **greater than 0.95**, the second feature (`columns[j]`) is marked for removal.

```
columns_to_drop = set(columns_to_drop)  
len(columns_to_drop)
```

Output: 197 #columns to drop

- We converted the list in set to avoid duplicates

Drop all these columns:

```
X_train.drop(columns = columns_to_drop, axis = 1, inplace=True)  
X_test.drop(columns = columns_to_drop, axis = 1, inplace=True)
```

```
print(X_train.shape)
print(X_test.shape)
```

Output:

(5881, 152)

(1471, 152)

- Now we have 152 columns left.

ANOVA

- ANOVA is used when:
 - Input: Numeric
 - Output: Categorical (Usually 2+)
- Can also be used when output is numeric

How does ANOVA work?

- You take 1 column & study its relationship with output column
- You calculate F-stats/F-ratio

$$F = \frac{\text{Between Group Variance}}{\text{Within Group Variance}}$$



There is a less difference between
groups

ANOVA using sklearn Python:

```
from sklearn.feature_selection import f_classif
from sklearn.feature_selection import SelectKBest
```

```
sel = SelectKBest(f_classif, k=100).fit(X_train, y_train)
```

```
# display selected feature names
X_train.columns[sel.get_support()]
```

```
Index(['tBodyAcc-std()-X', 'tBodyAcc-std()-Y', 'tBodyAcc-std()-Z',
      'tBodyAcc-max()-Z', 'tBodyAcc-min()-X', 'tBodyAcc-min()-Y',
      'tBodyAcc-min()-Z', 'tBodyAcc-entropy()-X', 'tBodyAcc-entropy()-Y',
      'tBodyAcc-entropy()-Z', 'tBodyAcc-arCoeff()-X,1',
      'tBodyAcc-arCoeff()-X,2', 'tBodyAcc-arCoeff()-X,3',
      'tBodyAcc-arCoeff()-Y,1', 'tBodyAcc-arCoeff()-Z,1',
      'tBodyAcc-correlation()-X,Y', 'tBodyAcc-correlation()-Y,Z',
      'tGravityAcc-mean()-X', 'tGravityAcc-mean()-Y', 'tGravityAcc-mean()-Z',
      'tGravityAcc-sma()', 'tGravityAcc-energy()-Y', 'tGravityAcc-energy()-Z',
      'tGravityAcc-entropy()-X', 'tGravityAcc-entropy()-Y',
      'tGravityAcc-arCoeff()-Y,1', 'tGravityAcc-arCoeff()-Y,2',
      'tGravityAcc-arCoeff()-Z,1', 'tGravityAcc-arCoeff()-Z,2',
      'tGravityAcc-correlation()-Y,Z', 'tBodyAccJerk-std()-Z',
      'tBodyAccJerk-min()-X', 'tBodyAccJerk-min()-Y', 'tBodyAccJerk-min()-Z',
      'tBodyAccJerk-entropy()-X', 'tBodyAccJerk-arCoeff()-X,3',
```

`f_classif` → f classification

- calculates the **ANOVA F-value** for each feature

`SelectKBest` → Select the best features (in this case, 100 based on a scoring function (here, `f_classif`)).

- Here, **we'll calculate ANOVA for all 152 columns & select best 100**

```
columns = X_train.columns[sel.get_support()]
```

- Now, transform the data

```
X_train = sel.transform(X_train)
X_test = sel.transform(X_test)

X_train = pd.DataFrame(X_train, columns=columns)
X_test = pd.DataFrame(X_test, columns=columns)
```

```
print(X_train.shape)
print(X_test.shape)
```

Output:
(5881, 100)
(1471, 100)

Disadvantages of ANOVA

- Assumption of Normality
- Assumption of Homogeneity of Variance
- Independence of Observations
- Effect of Outliers
- Doesn't Account for Interactions

NOW, APPLY LOGISTIC REGRESSION AGAIN WITH NEW DATA

```
# Initialize and train logistic regression model
log_reg = LogisticRegression(max_iter=1000) # Increase max_iter if it doesn't
converge
log_reg.fit(X_train, y_train)

# Make predictions on the test set
y_pred = log_reg.predict(X_test)
```

```
# Calculate and print accuracy score
accuracy = accuracy_score(y_test, y_pred)
print("Test accuracy:", accuracy)
```

Output: Test accuracy: 0.9694085656016316

Chi-square Test

Formula

The Chi-Square statistic is calculated as:

$$\chi^2 = \sum \frac{(O_{ij} - E_{ij})^2}{E_{ij}}$$

Where:

- O_{ij} : Observed frequency in cell (i, j) .
- E_{ij} : Expected frequency in cell (i, j) , calculated as:

$$E_{ij} = \frac{(\text{Row Total}) \times (\text{Column Total})}{\text{Grand Total}}$$

Degrees of Freedom

$$df = (r - 1) \times (c - 1)$$

Where:

- r : Number of rows.
- c : Number of columns.

Chi Square

- Used when **both input & output** columns are **categorical**
- We'll use Titanic dataset

```
titanic = pd.read_csv('titanic/train.csv')[['Pclass','Sex','SibSp','Parch','Embarked','Survived']]
titanic.head()
```

	Pclass	Sex	SibSp	Parch	Embarked	Survived
0	3	male	1	0	S	0
1	1	female	1	0	C	1
2	3	female	0	0	S	1
3	1	female	1	0	S	1
4	3	male	0	0	S	0

- Survived will be output

How Chi Square works

- We'll ask question: Is there any relationship between the columns sex & survived?
 - If no → we'll drop the sex column
- You form a contingency table like: 📌

Contingency Table			
	Boy	Girl	Sum
like Snickers	43	30	73
doesn't like Snickers	8	19	27
Sum	51	49	100

- We can do the same in python with `pd.crosstab()`

```
ct = pd.crosstab(titanic['Survived'],titanic['Sex'],margins=True)
```

ct

Sex	female	male	All
Survived			
0	81	468	549
1	233	109	342
All	314	577	891

- You can this 🙌 observed value
- You make one more table **"Expected"** with ideal data

Suppose you have a 2x2 contingency table with the following observed values:

	Category A	Category B	Total
X	30	10	40
Y	20	40	60
Total	50	50	100

For the cell at row X and column Category A, the expected value would be:

$$E_{X,A} = \frac{(R_X \times C_A)}{N} = \frac{(40 \times 50)}{100} = 20$$

```
ct2= pd.crosstab(titanic['Survived'],titanic['Sex'])
ct2
```

```
from scipy.stats import chi2_contingency
chi2_contingency(ct2)
```


Output:

```
Chi2ContingencyResult(statistic=260.71702016732104, pvalue=1.1973570627755645e-58, dof=1, expected_freq=array([[193.47474747, 355.52525253], [120.52525253, 221.47474747]]))
```

- We used ct2 **without the call column** because the all column interferes with results
- Run a loop and calculate `chi2_contingency` for each column

```
score = []
```

```
for feature in titanic.columns[:-1]:
```

```
    # create contingency table
```

```
    ct = pd.crosstab(titanic['Survived'], titanic[feature])
```

```
    # chi_test
```

```
    p_value = chi2_contingency(ct)[1]
```

```
    score.append(p_value)
```

`titanic.columns[:-1]` → All columns except last one i.e. "Survived"

`chi2_contingency(ct)[1]` → p-value

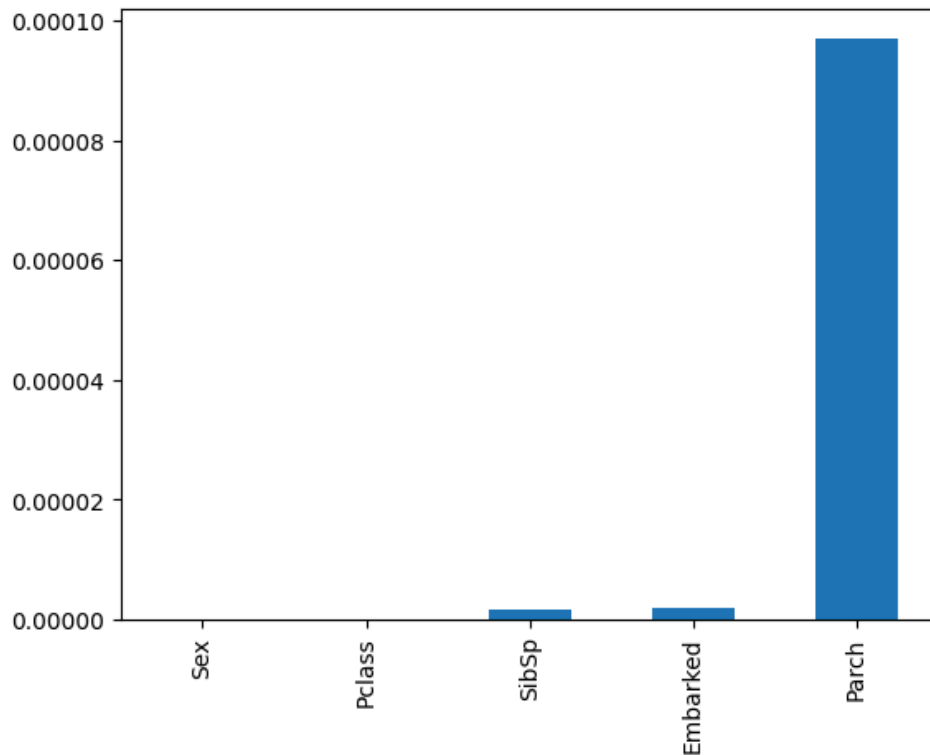
```
score
```

Output:

```
[4.549251711298793e-23,  
 1.1973570627755645e-58,  
 1.5585810465902118e-06,  
 9.703526421039996e-05,  
 1.769922284120912e-06]
```

- Plot these on graph

```
pd.Series(score, index=titanic.columns[:-1]).sort_values(ascending=True).plot  
(kind='bar')
```



- More the p-value, less the importance of the feature.

Alternate code with **sklearn**

```
from sklearn.preprocessing import LabelEncoder  
from sklearn.feature_selection import chi2  
import matplotlib.pyplot as plt
```

```
# assuming titanic is your DataFrame and 'Survived' is the target column
```

```
# Encode categorical variables
le = LabelEncoder()
titanic_encoded = titanic.apply(le.fit_transform)

X = titanic_encoded.drop('Survived', axis=1)
y = titanic_encoded['Survived']

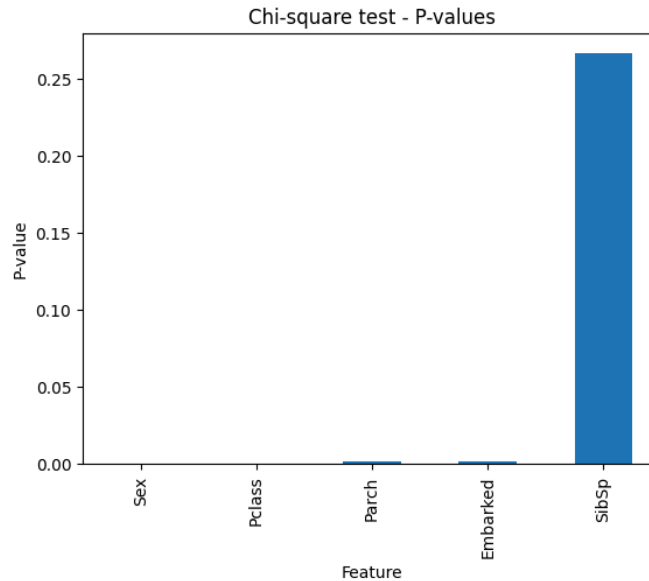
# Calculate chi-squared stats
chi_scores = chi2(X, y)

# chi_scores[1] are the p-values of each feature.
p_values = pd.Series(chi_scores[1], index = X.columns)
p_values.sort_values(inplace = True)

# Plotting the p-values
p_values.plot.bar()

plt.title('Chi-square test - P-values')
plt.xlabel('Feature')
plt.ylabel('P-value')

plt.show()
```



```
le = LabelEncoder()
titanic_encoded = titanic.apply(le.fit_transform)
```

- In this method, you have to convert the variables into Category
- This above code works with `SelectKBest`

`.apply(...)`: This is a Pandas DataFrame method that applies a function to each column (or row, depending on the `axis` argument, which defaults to columns if not specified) of the DataFrame.

`chi2(X, y)` returns → **Chi2 statistics & p_values**

Advantages and Disadvantages of Filter Methods

Advantages

- Simplicity
- Speed
- Scalability
- Pre-processing Step:

- They can serve as a pre-processing step for other feature selection methods.
- For instance, you could use a filter method to remove irrelevant features before applying a more computationally expensive method, such as a wrapper method.

Disadvantages

- Lack of Feature Interaction
- Model Agnostic:
 - This means that the selected features might not necessarily contribute to the accuracy of the specific model you want to use.
 - Can work well for one model & might not give that accurate results for another model.
- Statistical Measures Limitation:
 - For example, correlation is a measure of linear relationship and might not capture non-linear relationships effectively.
 - Similarly, variance-based methods might keep features with high variance but low predictive power.
- Threshold Determination