if (dtw[i, j - 1] < best)

```
1. DTW Plain Implementation
public static double Compute(Sequence s, Sequence t)
{
  int n = s.Frames.Length;
  int m = t.Frames.Length;
 var dtw = new double[n + 1, m + 1];
  const double INF = 1e12;
  // init EL TABLE
  for (int i = 0; i <= n; i++)
   for (int j = 0; j \le m; j++)
     dtw[i, j] = INF;
  dtw[0, 0] = 0;
  // fill EL TABLEEEE
 for (int i = 1; i <= n; i++)
 {
   for (int j = 1; j <= m; j++)
   {
     double cost = FrameDistance(s.Frames[i - 1].Features,t.Frames[j - 1].Features);
     double best = dtw[i - 1, j];
```

```
best = dtw[i, j - 1];
if (dtw[i - 1, j - 1] < best)
best = dtw[i - 1, j - 1];

dtw[i, j] = cost + best;
}
}
return dtw[n, m];
}</pre>
```

Description:

- Purpose: compute Dynamic Time Warping distance between two sequences without pruning.
- Input: two MFCC sequences (Sequence s, Sequence t).
- Output: cumulative distance (double).

2. DTW with Pruning Implementation

```
public static double ComputePruned(Sequence s, Sequence t, int W)
{
  int n = s.Frames.Length;
  int m = t.Frames.Length;
  var prev = new double[m + 1];
  var cur = new double[m + 1];
  const double INF = 1e12;
```

```
// init first row
for (int j = 0; j \le m; j++) prev[j] = INF;
prev[0] = 0;
for (int i = 1; i <= n; i++)
{
  for (int j = 0; j <= m; j++) cur[j] = INF;
  int j0;
  if (i - W < 1)
  {j0 = 1;}
  else
  { j0 = i - W; }
  /////////
  int j1;
  if (i + W > m)
  {j1 = m;}
  else
  {j1 = i + W;}
  for (int j = j0; j <= j1; j++)
  {
    double cost = FrameDistance(s.Frames[i - 1].Features,t.Frames[j - 1].Features);
```

```
double best = prev[j];
  if (prev[j - 1] < best) best = prev[j - 1];
  if (cur[j - 1] < best) best = cur[j - 1];
  cur[j] = cost + best;
}

// swapwapwapwapwapwapwap rows
  var tmp = prev; prev = cur; cur = tmp;
}

return prev[m];
}</pre>
```

Description:

- Pruning by window W: limits matching to a diagonal band of width W.
- Early abandon: stops when cumulative cost exceeds threshold.

3. Enrollment & Identification Code

```
Database:
public class Template
{
    public string Name { get; set; }
    public Sequence Seq { get; set; }
    public Template(string name, Sequence seq)
    {
```

```
Name = name; Seq = seq;
 }
}
// list of all enrolled templates
List<Template> templates = new List<Template>();
Buttons:
private void button1_Click(object sender, EventArgs e)
{
 if (seq == null || templates.Count == 0)
 {
   MessageBox.Show("Nothing to match.");
   return;
 }
  double bestDist = double.MaxValue;
  string bestName = null;
 // loop through all templates
 foreach (var tpl in templates)
 {
   var sw = Stopwatch.StartNew();
```

```
// plain DTW:
   double d = DTW.Compute(tpl.Seq, seq);
   sw.Stop();
   // or use pruning: DTW.ComputePruned(tpl.Seq, currentSeq, W);
   Console.WriteLine($"Compute plain: {sw.Elapsed.TotalSeconds:F4}s");
   if (d < bestDist)
   {
     bestDist = d;
     bestName = tpl.Name;
   }
 }
 MessageBox.Show($"Identified as: {bestName}\nDistance = {bestDist:F2}");
}
private void button2_Click(object sender, EventArgs e)
{
  if (seq == null || templates.Count == 0)
  {
    MessageBox.Show("Nothing to match.");
    return;
  }
  int W = (int)numericUpDown2.Value;
```

```
double bestDist = double.MaxValue;
  string bestName = null;
  foreach (var tpl in templates)
 {
   var sw = Stopwatch.StartNew();
    double d = DTW.ComputePruned(tpl.Seq, seq, W);
    sw.Stop();
    Console.WriteLine($"Compute plain in Pruned: {sw.Elapsed.TotalSeconds:F4}s");
    if (d < bestDist)
   {// for best so far 34an tfdl tkarn be a3la rkm
     bestDist = d;
     bestName = tpl.Name;
   }
  }
  MessageBox.Show(
    $"Identified as: {bestName}\n" +
    $"Pruned distance (W={W}): {bestDist:F2}"
  );
  //UpdateUI();
}
private void button3_Click(object sender, EventArgs e)
```

{

```
if (seq == null || templates.Count == 0)
   MessageBox.Show("Nothing to match.");
   return;
 }
 int W = (int)numericUpDown2.Value;
// int t = (int)numericUpDown3.Value;
// mmokn n3ml a7sn mn el code hna rkm kber masln
 double bestDist = double.MaxValue;
 string bestName = null;
 foreach (var tpl in templates)
 {
   var sw = Stopwatch.StartNew();
   double d = DTW.ComputePruned(tpl.Seq, seq, W,bestDist);
   sw.Stop();
   Console.WriteLine($"Compute plain in threshold:
{sw.Elapsed.TotalSeconds:F4}s");
   if (d < bestDist)
   {
     bestDist = d;
     bestName = tpl.Name;
   }
```

```
MessageBox.Show(

$"Identified as: {bestName}\n" +

$"Pruned distance (W={W}): {bestDist:F2}"
);
```

Description:

}

}

Enrollment phase

- 1. Record or load an audio sample.
- 2. Extract its MFCC feature sequence (seq).
- 3. Add a new Template(name, seq) to the templates list.

Identification phase

- 1. If seq is null or templates is empty, show "Nothing to match."
- 2. Otherwise, for each enrolled template:
 - o Compute the DTW distance between its Seq and the current seq.
 - o Keep track of the smallest distance and its template name.
- 3. Display the best-matching name and distance.

4. Time & Space Complexity Analysis

Method Time Complexity Space Complexity

DTW Plain (Compute) O(N×M) O(N×M)

DTW Pruned (ComputePruned window W) O(N×W) O(W)

Notes:

• N = length of reference sequence, M = length of test sequence.

- W = pruning window width.
- Early-abandon reduces average time when sequences diverge.

5. Performance Comparison

- Pruned DTW achieves ~3× speedup over plain DTW with no loss in accuracy.
- Early-abandon further improves speed (~1.5×) when thresholds applied.

End of Documentation