

# Exam 20 December

**Due** Dec 20 at 5pm      **Points** 30      **Questions** 30

**Available** Dec 20 at 4pm - Dec 20 at 5:05pm about 1 hour

**Time Limit** 50 Minutes

## Instructions

Notation:  $\_$  denotes the blank symbol in questions on configurations

## Attempt History

	Attempt	Time	Score
LATEST	<a href="#">Attempt 1</a>	48 minutes	21 out of 30

⚠ Correct answers are hidden.

Score for this quiz: **21** out of 30

Submitted Dec 20 at 4:49pm

This attempt took 48 minutes.

### Question 1

1 / 1 pts

$f(n)=3\log_8 n$ ,  $g(n)=5\log_2 n$ .

Claim1:  $f(n)=\Omega(g(n))$ .

Claim 2:  $g(n)=\Omega(f(n))$ .

Which one of the 2 claims holds?

- ☐ Claim 1 only
- ☐ Claim 2 only
- ☒ both claims hold
- ☐ none of the two claims holds

Incorrect

### Question 2

0 / 1 pts

Let  $f$  and  $g$  be  $\mathbf{N} \rightarrow \mathbf{R}_0^+$  functions. Suppose, that the limit of the sequence  $f/g$  does not exist (as  $n \rightarrow +\infty$ ).

Which of the following statements follows from this assumption?

1st statement:  $f(n) = \Omega(g(n))$  does not hold.

2nd statement:  $g(n) = \Omega(f(n))$  does not hold.

- ☐ Only the 1st statement follows.
- ☐ Only the 2nd statement follows.
- ☒ Both statements follow.
- ☐ None of the two statements follows.

Incorrect

### Question 3

0 / 1 pts

Let  $M = (Q, \Sigma, \Gamma, \delta, q_0, q_a, q_r)$  be a 2-tape Turing machine. Which one is the starting configuration for input word  $abb$ ?

- ☐  $(q_0, \lambda, abb, \lambda, \_)$
- ☐  $(q_0, abb, \_)$
- ☐  $(q_0, \lambda, abb, \lambda, \lambda)$
- ☒  $(q_0, abb, \lambda)$

### Question 4

1 / 1 pts

Which one of the following two words can be a configuration of one-tape Turing machine  $M = (\{q_0, q_1, q_2\}, \{a, b\}, \Gamma, \delta, q_0, q_a, q_r)$  ?

$q_1aab$  or  $aabq_1$ ?

☒  $q_1aab$  only

☐  $aabq_1$  only

☐ both of the two words

☐ none of the two words

### Question 5

1 / 1 pts

Let  $M$  be a nondeterministic Turing machine and let  $\vdash$  and  $\vdash^*$  denote its one-step and multi-step transition relation, respectively..

Which one of the following statements holds?

1st statement: If  $K$  is a configuration of  $M$  then  $K \vdash^* K$  holds.

2nd statement: If  $K$  and  $K'$  are configurations of  $M$  and  $K \vdash K'$  holds, then  $K \vdash^* K'$  holds as well.

☐ Only the 1st statement holds.

☐ Only the 2nd statement holds.

☒ Both statements hold.

☐ None of the two statements holds.

### Question 6

1 / 1 pts

Suppose, that  $L$  can be decided by an  $f(n)=2n\log_2 n$  time bounded deterministic Turing machine.

Which one of the following statments follows from this assumption?

1st statement:  $L$  is in  $P$ .

2nd statement:  $L$  is not in  $P$ .

- ☒ Only the 1st statement follows.
- ☐ Only the 2nd statement follows.
- ☐ Both statements follow.
- ☐ None of the two statements follows.

Incorrect

**Question 7****0 / 1 pts**

Suppose, that  $L$  can be decided by an  $f(n)=3^n+2n^2$  time bounded deterministic Turing machine.

Which one of the following statments follows from this assumption?

1st statement:  $L$  is in  $P$ .

2nd statement:  $L$  is not in  $P$ .

- ☐ Only the 1st statement follows.
- ☒ Only the 2nd statement follows.
- ☐ Both statements follow.
- ☐ None of the two statements follows.

**Question 8****1 / 1 pts**

Which one of the following statments hold?

1st statement: If  $L \in \text{NTIME}(f(n))$  then  $L \in \text{TIME}(2^{O(f(n))})$ .

2nd statement: If  $L \in \text{TIME}(f(n))$  then  $L \in \text{NTIME}(f(n))$ .

- ☐ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.

- ☒ Both statements hold.
- ☐ None of the two statements holds.

**Question 9****1 / 1 pts**

Suppose, that  $L$  can be decided by an  $f(n)=2n+3\log_2 n$  time bounded deterministic Turing machine.

Which one of the following statments follows from this assumption?

1st statement:  $L$  is in  $P$ .

2nd statement:  $L$  is in  $NP$ .

- ☐ Only the 1st statement follows.
- ☐ Only the 2nd statement follows.
- ☒ Both statements follow.
- ☐ None of the two statements follows.

**Incorrect****Question 10****0 / 1 pts**

Which one of the following statements can be stated as being TRUE?

1st statement: Let  $M$  be a nondeterministic Turing machine of  $f(n)=n^3$  time complexity. Then there exist a deterministic Turing machine of  $O(n^7)$  time complexity equivalent with  $M$ .

2nd statement: Let  $M$  be a deterministic 2-tape Turing machine of  $f(n)=n^3$  time complexity. Then there exist a deterministic 1-tape Turing machine of  $O(n^7)$  time complexity equivalent with  $M$ .

- ☐ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☒ Both statements hold.

- ☐ None of the two statements holds.

Incorrect

### Question 11

0 / 1 pts

Which one of the following statements can not be stated as being TRUE?

- ☐ For every deterministic Turing machine there exist an equivalent nondeterministic one.
- ☐ For every nondeterministic Turing machine there exist an equivalent deterministic one.
- ☒ For every deterministic 3-tape Turing machine of polynomial time complexity there exists an equivalent deterministic 2-tape Turing machine of polynomial time complexity.
- ☐ For every nondeterministic Turing machine of polynomial time complexity there exists an equivalent deterministic Turing machine of polynomial time complexity.

Incorrect

### Question 12

0 / 1 pts

Which one of the following two statements holds?

1st statement: No bijection exists between  $\{L \mid L \subseteq \{0,1\}^*\}$  and the set of Turing machines of input alphabet  $\{0,1\}$ .

2nd statement: No bijection exists between  $\{0,1\}^*$  and the set of real numbers of the  $[0,1]$  interval.

- ☒ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.

- ☐ Both statements hold.
- ☐ None of the two statements holds.

**Question 13****1 / 1 pts**

Which one of the following statements holds?

1st statement: Every language is recognizable by a Turing machine.

2nd statement:  $RE \subset R$

- ☐ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☐ Both statements hold.
- ☒ None of the two statements holds.

**Question 14****1 / 1 pts**

Which one of the following statements holds?

1st statement: The complement language of  $L_{diag}$  is undecidable.

2nd statement:  $L_{diag}$  is reducible to a Turing-recognizable language.

- ☒ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☐ Both statements hold.
- ☐ None of the two statements holds.

**Question 15****1 / 1 pts**

Which one of the following statements can be stated being TRUE?

1st statement: The language of satisfiable conjunctive normal forms of propositional logic is in P.

2nd statement: The language of satisfiable formulas of first order logic is not in P.

- ☐ Only the 1st statement.
- ☒ Only the 2nd statement.
- ☐ Both statements.
- ☐ None of the two statements.

**Incorrect****Question 16****0 / 1 pts**

Consider a first order logic including a predicate symbol  $q$  and a function symbol  $f$ , both of arity 2.

Which one of the following is a string representation of a first order formula? ( $x$  and  $y$  are variables)

1.  $\forall y f(y, y)$

2.  $q(x, y) \vee q(f(x, y))$

- ☒ only the 1st one
- ☐ only the 2nd one
- ☐ both
- ☐ none of them

**Question 17****1 / 1 pts**



Let  $D = \{(u,v), (w,x), (y,z)\}$  ( $u,v,w,x,y,z \in \Sigma^+$ ) be an instance of the Post Correspondence Problem. (There are 3 dominos, the first one has  $u$  at the top and  $v$  at the bottom, the second one has  $w$  at the top and  $x$  at the bottom, the third one has  $y$  at the top and  $z$  at the bottom. )

Which one of the following statements holds?

1. If  $uwuu = vxvv$  then  $D$  has a solution.
2. All solutions of  $D$  is a sequence of at most 3 dominos.

☒ Only the 1st statement holds.

☐ Only the 2nd statement holds.

☐ Both statements hold.

☐ None of the 2 statement holds.

### Question 18

1 / 1 pts

Which one of the following statements holds?

1st statement: According to Rice's Theorem it is undecidable whether a Turing machine recognizes the language  $\{01, 11, 101\}$ .

2nd statement: According to Rice's Theorem it is undecidable whether a Turing machine recognizes a recursively enumerable language.

☒ Only the 1st statement holds.

☐ Only the 2nd statement holds.

☐ Both statements hold.

☐ None of the two statements holds.

### Question 19

1 / 1 pts

Which one of the following languages is not in NP?

- ☐ REACHABILITY
- 
- ☒ VALIDITYPRED
- 
- ☐ 2SAT
- 
- ☐ INDEPENDENT SET

**Question 20****1 / 1 pts**

Which one of the following formulas is a 3CNF?

1.  $((\neg p \vee q \vee \neg r) \wedge (\neg p \vee \neg r \vee \neg s)) \vee (q \wedge r \wedge s)$

2.  $(\neg p \vee q) \wedge (\neg r \vee \neg q)$

(p,q,r,s are atomic variables)

- ☐ only the 1st one
- 
- ☐ only the 2nd one
- 
- ☐ both
- 
- ☒ none of them

**Question 21****1 / 1 pts**

Which one of the following statements holds?

1st statement: If 2-COLORING is in P, then  $P=NP$ .

2nd statement: If VERTEX COVER is in P, then  $P=NP$ .

- ☐ Only the 1st statement holds.
- 
- ☒ Only the 2nd statement holds.
- 
- ☐ Both statements hold.

- ☐ None of the two statements holds.

**Question 22****1 / 1 pts**

Let  $G$  be a simple undirected graph of 20 vertices.

Which one of the following statements holds?

1st statement: If  $G$  has a vertex cover of size 8 then  $G$  has an independent set of size 12.

2nd statement: If  $G$  has an independent set of size 12, then  $G$  has a clique of size 8.

- ☒ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☐ Both statements hold.
- ☐ None of the two statements holds.

**Question 23****1 / 1 pts**

Which one of the following statements holds?

1st statement: If  $L_1 \leq_p L_2$  then  $L_1 \leq L_2$ .

2nd statement: If  $L_1 \leq_p L_2$  then the complement of  $L_1 \leq_p$  the complement of  $L_2$ .

- ☐ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☒ Both statements hold.
- ☐ None of the two statements holds.

**Question 24****1 / 1 pts**

Which one of the following statements can be stated being TRUE?

1st statement: All NP-intermediate problems are in PSPACE.

2nd statement: GRAPH ISOMORPHISM is an NP-intermediate problem.

- 
- ☒ Only the 1st statement.
- 
- ☐ Only the 2nd statement.
- 
- ☐ Both statements.
- 
- ☐ None of the two statements.

**Question 25****1 / 1 pts**

Which one of the following statements holds?

1st statement:  $\text{coNP} \subseteq \text{R}$ .

2nd statement: Time complexity class coNP is the complement of time complexity class NP.

- 
- ☒ Only the 1st statement holds.
- 
- ☐ Only the 2nd statement holds.
- 
- ☐ Both statements hold.
- 
- ☐ None of the two statements holds.

**Question 26****1 / 1 pts**

Which one of the following statements holds?

1st statement: REACHABILITY can be decided by a nondeterministic Turing machine in polynomial time.

2nd statement: REACHABILITY is recursively enumerable.

- ☐ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☒ Both statements hold.
- ☐ None of the two statements holds.

### Question 27

1 / 1 pts

Which one of the following statements can be stated being TRUE?

1st statement:  $\text{TIME}(n^2) \subseteq \text{NSPACE}(n^2)$

2nd statement:  $\text{SPACE}(n^2) \subseteq \text{NTIME}(n^2)$

- ☒ Only the 1st statement.
- ☐ Only the 2nd statement.
- ☐ Both statements.
- ☐ None of the two statements.

Incorrect

### Question 28

0 / 1 pts

Which one of the following statements holds?

1st statement: Every type 2 language (according to Chomsky's hierarchy) can be recognized by a linear bounded automaton.

2nd statement: Every language which can be recognized by a linear bounded automaton is a type 2 language.

- ☐ Only the 1st statement holds.

- ☐ Only the 2nd statement holds.
- ☐ Both statements hold.
- ☒ None of the two statements holds.

Incorrect

**Question 29****0 / 1 pts**

Which one of the following statements holds?

1st statement: Every language  $L$ , that can be generated by a type 1 grammar (according to Chomsky's classification) can be recognized by a nondeterministic Turing machine.

2nd statement: Every language  $L$ , that can be recognized by a nondeterministic Turing machine can be generated by a type 1 grammar.

- ☐ Only the 1st statement.
- ☐ Only the 2nd statement.
- ☒ Both statements.
- ☐ None of the two statements.

**Question 30****1 / 1 pts**

Which one of the following statements can be stated being TRUE?

1st statement: Every PSPACE-complete language is in NPSPACE.

2nd statement: 3SAT is PSPACE-complete.

- ☒ Only the 1st statement.
- ☐ Only the 2nd statement.
- ☐ Both statements.

☐ None of the statements.

Quiz Score: **21** out of 30