

# Exam 29 December

**Due** Dec 29 at 11am **Points** 30 **Questions** 30**Available** Dec 29 at 10am - Dec 29 at 11:05am about 1 hour**Time Limit** 50 Minutes

## Instructions

Notation: \_ denotes the blank symbol in questions on configurations

## Attempt History

|        | Attempt                   | Time       | Score        |
|--------|---------------------------|------------|--------------|
| LATEST | <a href="#">Attempt 1</a> | 50 minutes | 22 out of 30 |

! Correct answers are hidden.

Score for this quiz: **22** out of 30

Submitted Dec 29 at 10:50am

This attempt took 50 minutes.

### Question 1

1 / 1 pts

$$f(n)=9n^4+5n \quad g(n)=2^{n-2}$$

Which one of the following statements holds?

1st statement:  $f(n)=O(g(n))$ .2nd statement:  $g(n)=O(f(n))$ .

- ☒ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☐ Both statements hold.
- ☐ None of the two statements holds.

**Question 2****1 / 1 pts**

$$f(n)=n^4+2n \quad g(n)=(2/3)^n$$

Which one of the following statements holds?

1st statement:  $f(n)=\Omega(g(n))$ .

2nd statement:  $g(n)=\Omega(f(n))$ .

- ☒ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☐ Both statements hold.
- ☐ None of the two statements holds.

**Question 3****1 / 1 pts**

Let  $M = (Q, \Sigma, \Gamma, \delta, q_0, q_a, q_r)$  be a 2-tape Turing machine. Which one is the starting configuration for input word  $abb$ ?

- ☒  $(q_0, \lambda, abb, \lambda, \_)$
- ☐  $(q_0, abb, \_)$
- ☐  $(q_0, \lambda, abb, \lambda, \lambda)$
- ☐  $(q_0, abb, \lambda)$

**Question 4****1 / 1 pts**

Which one of the following two words can be a configuration of one-tape Turing machine  $M = (\{q_0, q_1, q_2\}, \{a, b\}, \Gamma, \delta, q_0, q_a, q_r)$  ?

$q_1aab$  or  $aabq_1$ ?

- ☒  $q_1aab$  only
- ☐  $aabq_1$  only
- ☐ both of the two words
- ☐ none of the two words

Incorrect

### Question 5

0 / 1 pts

Let  $M = (Q, \Sigma, \Gamma, \delta, q_0, q_a, q_r)$  be a 2-tape Turing machine and let  $\_$  denote the blank symbol.

Which one of the following statements holds?

1st statement:  $(q_0, \lambda, \lambda, \lambda, \lambda)$  is the starting configuration for input  $\lambda$ .

2nd statement:  $(q_r, \lambda, \_, \lambda, \_)$  is a rejecting configuration.

- ☐ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☒ Both statements hold.
- ☐ None of the two statements holds.

Incorrect

### Question 6

0 / 1 pts

Let  $M = (\{q_0, q_a, q_r\}, \{a, c\}, \{a, b, c, \_ \}, \delta, q_0, q_a, q_r)$ , where the transitions are

$\delta(q_0, a) = (q_a, b, S)$ ,

$\delta(q_0, b) = (q_a, b, S)$ ,

$\delta(q_0, c) = (q_r, \_, L)$ ,

$\delta(q_0, \_) = (q_a, \_, L)$ .

Is it true, that  $b \in L(M)$ ? Is it true, that  $c \in L(M)$ ?

- ☒  $b \in L(M)$  only
- ☐  $c \in L(M)$  only
- ☐ both  $b \in L(M)$  and  $c \in L(M)$  holds
- ☐ none of  $b \in L(M)$  and  $c \in L(M)$  holds

## Question 7

1 / 1 pts

Which one of the following statements can be stated as being TRUE?

1st statement: Let  $M$  be an  $n^3$  time bounded nondeterministic Turing machine. Then there exist a deterministic  $O(n^7)$  time bounded deterministic Turing machine equivalent with  $M$ .

2nd statement: Let  $M$  be an  $n^3$  time bounded deterministic 2-tape Turing machine. Then there exist a deterministic  $O(n^7)$  time bounded 1-tape deterministic Turing machine equivalent with  $M$ .

- ☐ Only the 1st statement holds.
- ☒ Only the 2nd statement holds.
- ☐ Both statements hold.
- ☐ None of the two statements holds.

Incorrect

**Question 8**

0 / 1 pts

Which one of the following statements can not be stated as being TRUE?

☒

For every deterministic Turing machine there exist an equivalent nondeterministic one.

☐

For every nondeterministic Turing machine there exist an equivalent deterministic one.

☐

For every deterministic 3-tape Turing machine of polynomial time complexity there exists an equivalent deterministic 2-tape Turing machine of polynomial time complexity.

☐

For every nondeterministic Turing machine of polynomial time complexity there exists an equivalent deterministic Turing machine of polynomial time complexity.

Incorrect

**Question 9**

0 / 1 pts

Let  $L$  be a language and  $M$  be a nondeterministic Turing machine, such that  $L(M)=L$  holds.

Which one of the following statements follows from this assumption?

1st statement:  $L \in \text{RE}$

2nd statement:  $L \in \text{R}$

☐

Only the 1st statement follows.

- ☐ Only the 2nd statement follows.
- ☐ Both statements follow.
- ☒ None of the two statements follows.

Incorrect

**Question 10****0 / 1 pts**

Which one of the following sequences is NOT a code of 3-state ( $q_0, q_r, q_a$ ) 1-tape deterministic Turing machine according to the coding given on the lecture? [Before assigning a specific machine for non-codes.]

- ☐ 0101000100010001101001000100010001101000100010001000
- ☒ 0101010001000110100100100010001101000100101000
- ☐ 0101010101101001010101101000101010
- ☐ 0101010001011110100100100010001101001001010100

**Question 11****1 / 1 pts**

Which one of the following statements holds?

1st statement: The cardinality of  $\{L \mid L \subseteq \{0,1\}^*\} \setminus RE$  is countably infinite.

2nd statement: The cardinality of  $RE \setminus R$  is countably infinite.

- ☐ Only the 1st statement.
- ☒ Only the 2nd statement.
- ☐ Both statements.

☐ None of the two statements.

**Question 12****1 / 1 pts**

Which one of the following statements holds?

1st statement:  $L_h$  can be reduced to a decidable language.

2nd statement: The complement language of  $L_h$  is in RE.

☐ Only the 1st statement holds.

☐ Only the 2nd statement holds.

☐ Both statements hold.

☒ None of the two statements holds.

**Question 13****1 / 1 pts**

Which one of the following statements holds?

1st statement: TSP can be reduced to a decidable language.

2nd statement: The complement language of TSP is in RE.

☐ Only the 1st statement holds.

☐ Only the 2nd statement holds.

☒ Both statements hold.

☐ None of the two statements holds.

Incorrect

**Question 14****0 / 1 pts**

Which one of the following statements holds (using the concepts of Rice's theorem)?

1st statement:  $\{ L \mid L \subseteq \{0,1\}^* \text{ and } L \text{ is finite} \}$  is a non-trivial property of the recursively enumerable languages.

2nd statement:  $\emptyset$  is a trivial property of the recursively enumerable languages.

- ☒ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☐ Both statements hold.
- ☐ None of the two statements holds.

**Question 15****1 / 1 pts**

Which one of the following statements can be stated being TRUE?

1st statement: The language of unsatisfiable formulas of propositional logic is in P.

2nd statement: The language of valid formulas of first order logic is undecidable.

- ☐ Only the 1st statement.
- ☒ Only the 2nd statement.
- ☐ Both statements.
- ☐ None of the two statements.



**Question 16****1 / 1 pts**

Consider a first order logic including a predicate symbol  $p$  and a function symbol  $f$ , both of arity 2.

Which one of the following is a string representation of a first order formula? ( $x$  and  $y$  are variables)

1.  $\forall x f(x, y)$

2.  $p(x, y) \vee p(f(y, y), x)$

☐ only the 1st one

☒ only the 2nd one

☐ both

☐ none of them

**Question 17****1 / 1 pts**

Let  $D = \{(u, v), (w, x)\}$  ( $u, v, w, x \in \Sigma^+$ ) be an instance of the Post Correspondence Problem. (There are 3 dominos, the first one has  $u$  at the top and  $v$  at the bottom, the second one has  $w$  at the top and  $x$  at the bottom. )

Which one of the following statements holds?

1. All solutions of  $D$  is a sequence of at most 2 dominos.

2. If  $|u| > |v|$  and  $|w| > |x|$  then  $D$  has no solution

☐ Only the 1st statement holds.

☒ Only the 2nd statement holds.

☐ Both statements hold.

- ☐ None of the 2 statement holds.

**Question 18****1 / 1 pts**

Which one of the following statements holds?

1st statement: For every nondeterministic Turing machine  $M$  there exists a grammar generating  $L(M)$ .

2nd statement: For every grammar  $G$  there exists a nondeterministic Turing machine recognizing  $L(G)$ .

- ☐ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☒ Both statements hold.
- ☐ None of the two statements holds.

**Question 19****1 / 1 pts**

Which one of the following statements holds?

1st statement: For every nondeterministic Turing machine  $M$  there exists a context sensitive grammar generating  $L(M)$ .

2nd statement: For every context sensitive grammar  $G$  there exists a nondeterministic Turing machine recognizing  $L(G)$ .

- ☐ Only the 1st statement.

- ☒ Only the 2nd statement.
- ☐ Both statements.
- ☐ None of the two statements.

Incorrect

**Question 20****0 / 1 pts**

Which one of the following languages can be a language not in P?

- ☐ PERFECT MATCHING
- ☐ REACHABILITY
- ☐ GRAPH ISOMORPHISM
- ☒ 2SAT

**Question 21****1 / 1 pts**

Which one of the following languages is not in NP?

- ☐ GRAPH ISOMORPHISM
- ☐ SUBGRAPH ISOMORPHISM
- ☒ UNSATPRED
- ☐ SAT

**Question 22****1 / 1 pts**

Which one of the following two propositional formulas is a Horn formula?

1.  $(\neg x \vee y) \wedge (\neg x \vee \neg z) \wedge y$
2.  $(\neg x \vee y \vee \neg z) \wedge (\neg x \vee \neg z \vee \neg w)$

(x,y,z,w are atomic variables)

☐ only the 1st one

☐ only the 2nd one

☒ both of them

☐ none of them

**Question 23****1 / 1 pts**

Complete the sentence to make it true.

If ..... then  $P=NP$ .

☐ REACHABILITY is in NP

☐ there is an NP-complete problem in NP

☒ there are no NP-intermediate problems in NP

☐ every problem in NP is reducible to an NP-complete problem

**Question 24****1 / 1 pts**

Let G be a simple undirected graph of 20 vertices.

Which one of the following statements holds?

1st statement: If  $G$  is 4-colorable, then  $G$  is 5-colorable.

2nd statement: If  $G$  has a vertex cover of size 7, then  $G$  has a vertex cover of size 8.

- ☐ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☒ Both statements hold.
- ☐ None of the two statements holds.

### Question 25

1 / 1 pts

Let  $L$  and  $L'$  be languages and assume that  $L$  is in NP. Then the following proves NP-completeness of  $L$ .

- ☐  $L \leq L'$  and  $L'$  is NP-complete
- ☐  $L \leq_p L'$  and  $L'$  is NP-complete
- ☒  $L' \leq_p L$  and  $L'$  is NP-complete
- ☐  $L' \leq L$  and  $L'$  is NP-complete

### Question 26

1 / 1 pts

Which one of the following statements holds?

1st statement: If  $P=NP$  is FALSE, then there exists a non-NP-complete language in  $NP \setminus P$ .

2nd statement: If  $P=NP$ , then PRIME FACTORIZATION is not NP-intermediate.

- ☐ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☒ Both statements hold.
- ☐ None of the two statements holds.

### Question 27

1 / 1 pts

Which one of the following statements holds?

1st statement: Space complexity class  $coNL$  is the complement of space complexity class  $NL$ .

2nd statement:  $NL \subseteq coNL$ .

- ☐ Only the 1st statement holds.
- ☒ Only the 2nd statement holds.
- ☐ Both statements hold.
- ☐ None of the two statements holds.

### Question 28

1 / 1 pts

Which one of the following statements can be stated being TRUE?

1st statement:  $TIME(n^2) \subseteq NSPACE(n^2)$

2nd statement:  $\text{SPACE}(n^2) \subseteq \text{NTIME}(n^2)$

- ☒ Only the 1st statement.
- ☐ Only the 2nd statement.
- ☐ Both statements.
- ☐ None of the two statements.

### Question 29

1 / 1 pts

Which one of the following statements holds?

1st statement: There is a language which can be decided by nondeterministic offline Turing machine of  $O(n \log n)$  space complexity, but can not be decided by a deterministic offline Turing machine of polynomial space complexity.

2nd statement: There is a language in NP which can not be decided by a deterministic offline Turing machine of polynomial space complexity.

- ☐ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☐ Both statements hold.
- ☒ None of the two statements holds.

Incorrect

### Question 30

0 / 1 pts

Which one of the following statements can be stated being TRUE?

1st statement: Every PSPACE-complete language is in NPSPACE.

2nd statement: 3SAT is PSPACE-complete.

☐ Only the 1st statement.

☐ Only the 2nd statement.

☒ Both statements.

☐ None of the statements.

Quiz Score: **22** out of 30