

# Exam 29 December

**Due** Dec 29 at 11am**Points** 30**Questions** 30**Available** Dec 29 at 10am - Dec 29 at 11:05am about 1 hour**Time Limit** 50 Minutes

## Instructions

Notation: \_ denotes the blank symbol in questions on configurations

## Attempt History

	Attempt	Time	Score
LATEST	<a href="#">Attempt 1</a>	49 minutes	18 out of 30

❗ Correct answers are hidden.

Score for this quiz: **18** out of 30

Submitted Dec 29 at 10:59am

This attempt took 49 minutes.

### Question 1

1 / 1 pts

$$f(n)=10n^4+2n \quad g(n)=2^{n-2}$$

Which one of the following statements holds?

1st statement:  $f(n)=\Omega(g(n))$ .

2nd statement:  $g(n)=\Omega(f(n))$ .

☐ Only the 1st statement holds.

☒ Only the 2nd statement holds.

☐ Both statements hold.

☐ None of the two statements holds.

### Question 2

1 / 1 pts

$$f(n)=n^4+2n \quad g(n)=(2/3)^n$$

Which one of the following statements holds?

1st statement:  $f(n)=\Omega(g(n))$ .

2nd statement:  $g(n)=\Omega(f(n))$ .

- ☒ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☐ Both statements hold.
- ☐ None of the two statements holds.

### Question 3

1 / 1 pts

Let  $M = (Q, \Sigma, \Gamma, \delta, q_0, q_a, q_r)$  be a 2-tape Turing machine. Which configuration follows  $(q, u, av, xe, by)$  if  $\delta(q, a, b) = (r, c, d, R, L)$  ?

$(u, v, x, y \in \Gamma^*, v, y \neq \lambda, a, b, c, d, e \in \Gamma)$

- ☒  $(r, uc, v, x, edy)$
- ☐  $(r, uc, v, xe, dy)$
- ☐  $(r, ua, v, x, eby)$
- ☐  $(r, uc, v, xed, y)$

### Question 4

1 / 1 pts

Let  $M = (Q, \Sigma, \Gamma, \delta, q_0, q_a, q_r)$  be a 2-tape Turing machine. Which one is the starting configuration for input word  $abb$ ?

- ☒  $(q_0, \lambda, abb, \lambda, \_)$
- ☐  $(q_0, abb, \_)$

☐  $(q_0, \lambda, \text{abb}, \lambda, \lambda)$

☐  $(q_0, \text{abb}, \lambda)$

Incorrect

### Question 5

0 / 1 pts

Let  $M = (Q, \Sigma, \Gamma, \delta, q_0, q_a, q_r)$  be a 2-tape Turing machine and let  $\_$  denote the blank symbol.

Which one of the following statements holds?

1st statement:  $(q_0, \lambda, \lambda, \lambda, \lambda)$  is the starting configuration for input  $\lambda$ .

2nd statement:  $(q_r, \lambda, \_, \lambda, \_)$  is a rejecting configuration.

☐ Only the 1st statement holds.

☐ Only the 2nd statement holds.

☒ Both statements hold.

☐ None of the two statements holds.

Incorrect

### Question 6

0 / 1 pts

Let  $M = (\{q_0, q_a, q_r\}, \{a, c\}, \{a, b, c, \_\}, \delta, q_0, q_a, q_r)$ , where the transitions are

$\delta(q_0, a) = (q_a, b, S)$ ,

$\delta(q_0, b) = (q_a, b, S)$ ,

$\delta(q_0, c) = (q_0, \_, L)$ ,

$\delta(q_0, \_) = (q_a, \_, L)$ .

Is it true, that  $b \in L(M)$ ? Is it true, that  $c \in L(M)$ ?

☐  $b \in L(M)$  only

☐  $c \in L(M)$  only

- ☒ both  $b \in L(M)$  and  $c \in L(M)$  holds
- ☐ none of  $b \in L(M)$  and  $c \in L(M)$  holds

**Question 7****1 / 1 pts**

Which one of the following statements can be stated as being TRUE?

1st statement: Let  $M$  be an  $n^3$  time bounded nondeterministic Turing machine. Then there exist a deterministic  $O(n^7)$  time bounded deterministic Turing machine equivalent with  $M$ .

2nd statement: Let  $M$  be an  $n^3$  time bounded deterministic 2-tape Turing machine. Then there exist a deterministic  $O(n^7)$  time bounded 1-tape deterministic Turing machine equivalent with  $M$ .

- ☐ Only the 1st statement holds.
- ☒ Only the 2nd statement holds.
- ☐ Both statements hold.
- ☐ None of the two statements holds.

**Incorrect****Question 8****0 / 1 pts**

Let  $L$  be a language and  $M$  be a nondeterministic Turing machine, such that  $L(M)=L$  holds.

Which one of the following statements follows from this assumption?

1st statement:  $L \in R$

2nd statement:  $L \in RE$

- ☐ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.

☒ Both statements hold.

☐ None of the two statements holds.

Incorrect

### Question 9

0 / 1 pts

Which one of the following statements holds?

1st statement: Every recursively enumerable language can be recognized by a nondeterministic Turing machine.

2nd statement: Every NP-complete language can be decided by a deterministic Turing machine.

☐ Only the 1st statement holds.

☐ Only the 2nd statement holds.

☐ Both statements hold.

☒ None of the two statements holds.

Incorrect

### Question 10

0 / 1 pts

Which one of the following sequences is NOT a code of 3-state ( $q_0, q_r, q_a$ ) 1-tape deterministic Turing machine according to the coding given on the lecture? [Before assigning a specific machine for non-codes.]

☐ 0101010001000110100100100010001101000100101000

☒ 01010001010110100100100010011010001001010

☐ 0101010001011110100100100010001101001001010100

☐ 0101000100010001101001000100010001101000100010001000

Incorrect

## Question 11

0 / 1 pts

Which one of the following statements holds?

1st statement: The cardinality of the family of undecidable languages is countably infinite.

2nd statement: The cardinality of  $\{L \mid L \subseteq \{0,1\}^*\} \setminus \text{RE}$  is countably infinite.

- ☐ Only the 1st statement.
- ☐ Only the 2nd statement.
- ☒ Both statements.
- ☐ None of the two statements.

## Question 12

1 / 1 pts

Which one of the following statements holds?

1st statement:  $L_h$  can be reduced to a decidable language.

2nd statement: The complement language of  $L_h$  is in RE.

- ☐ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☐ Both statements hold.
- ☒ None of the two statements holds.

Incorrect

## Question 13

0 / 1 pts

Which one of the following statements holds?

1st statement: VALIDITYPRED can be reduced to a decidable language.

2nd statement: The complement language of VALIDITYPRED is in R.

- ☐ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☒ Both statements hold.
- ☐ None of the two statements holds.

Incorrect

**Question 14****0 / 1 pts**

Which one of the following statements holds (using the concepts of Rice's theorem)?

1st statement:  $\{ L \mid L \subseteq \{0,1\}^* \text{ and } L \text{ is finite} \}$  is a non-trivial property of the recursively enumerable languages.

2nd statement:  $\emptyset$  is a trivial property of the recursively enumerable languages.

- ☒ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☐ Both statements hold.
- ☐ None of the two statements holds.

**Question 15****1 / 1 pts**

Which one of the following statements can be stated being TRUE?

1st statement: The language of unsatisfiable formulas of propositional logic is in NP.

2nd statement: The language of valid formulas of first order logic is in R.

- ☒ Only the 1st statement.

- ☐ Only the 2nd statement.
- ☐ Both statements.
- ☐ None of the two statements.

**Question 16****1 / 1 pts**

Consider a first order logic including a predicate symbol  $q$  and a function symbol  $f$ , both of arity 2.

Which one of the following is a string representation of a first order formula? ( $x$  and  $y$  are variables)

1.  $\forall y f(y, y)$
2.  $q(x, y) \vee q(f(y), x)$

- ☐ only the 1st one
- ☐ only the 2nd one
- ☐ both
- ☒ none of them

**Question 17****1 / 1 pts**

Let  $D = \{(u, v), (w, x), (y, z)\}$  ( $u, v, w, x, y, z \in \Sigma^+$ ) be an instance of the Post Correspondence Problem. (There are 3 dominos, the first one has  $u$  at the top and  $v$  at the bottom, the second one has  $w$  at the top and  $x$  at the bottom, the third one has  $y$  at the top and  $z$  at the bottom. )

Which one of the following statements holds?

1. If  $uwuu = vxvv$  then  $D$  has a solution.
2. All solutions of  $D$  is a sequence of at most 3 dominos.

- ☒ Only the 1st statement holds.



☐ Only the 2nd statement holds.

☐ Both statements hold.

☐ None of the 2 statement holds.

Incorrect

### Question 18

0 / 1 pts

Which one of the following statements holds?

1st statement: For every nondeterministic Turing machine  $M$  there exists a grammar generating  $L(M)$ .

2nd statement: For every grammar  $G$  there exists a nondeterministic Turing machine recognizing  $L(G)$ .

☐ Only the 1st statement holds.

☒ Only the 2nd statement holds.

☐ Both statements hold.

☐ None of the two statements holds.

### Question 19

1 / 1 pts

Which one of the following statements holds?

1st statement: For every nondeterministic Turing machine  $M$  there exists a context sensitive grammar generating  $L(M)$ .

2nd statement: For every context sensitive grammar  $G$  there exists a nondeterministic Turing machine recognizing  $L(G)$ .

☐ Only the 1st statement.

☒ Only the 2nd statement.

☐ Both statements.

☐ None of the two statements.

### Question 20

1 / 1 pts

Which one of the following languages can be a language not in P?

☐ HORNSAT

☐ 2-COLORING

☐ PRIMES

☒ PRIME FACTORIZATON

### Question 21

1 / 1 pts

Which one of the following languages is not in NP?

☐ GRAPH ISOMORPHISM

☐ SUBGRAPH ISOMORPHISM

☒ UNSATPRED

☐ SAT

Incorrect

### Question 22

0 / 1 pts

Which one of the following two propositional formulas is a Horn formula?

1.  $(\neg x \vee y) \wedge (\neg x \vee \neg z) \wedge y$

2.  $(\neg x \vee y \vee \neg z) \wedge (\neg x \vee \neg z \vee \neg w)$

(x,y,z,w are atomic variables)

☐ only the 1st one

☐ only the 2nd one

☐ both of them

☒ none of them

### Question 23

1 / 1 pts

Complete the sentence to make it true.

If ..... then  $P=NP$ .

☐ REACHABILITY is in NP

☐ there is an NP-complete problem in NP

☒ there are no NP-intermediate problems in NP

☐ every problem in NP is reducible to an NP-complete problem

Incorrect

### Question 24

0 / 1 pts

Let  $G$  be a simple undirected graph of 20 vertices.

Which one of the following statements holds?

1st statement: If  $G$  is 5-colorable, then  $G$  is 4-colorable.

2nd statement: If  $G$  has an independent set of size 7, then  $G$  has an independent set of size 8.

☐ Only the 1st statement holds.

- ☐ Only the 2nd statement holds.
- ☒ Both statements hold.
- ☐ None of the two statements holds.

Incorrect

**Question 25**

0 / 1 pts

Let  $L$  and  $L'$  be languages and assume that  $L$  is in NP. Then the following proves NP-completeness of  $L$ .

- ☐  $L \leq L'$  and  $L'$  is NP-complete
- ☒  $L \leq_p L'$  and  $L'$  is NP-complete
- ☐  $L' \leq_p L$  and  $L'$  is NP-complete
- ☐  $L' \leq L$  and  $L'$  is NP-complete

**Question 26**

1 / 1 pts

Which one of the following statements holds?

1st statement: If  $P=NP$  is FALSE, then there exists a non-NP-complete language in  $NP \setminus P$ .

2nd statement: If  $P=NP$ , then PRIME FACTORIZATION is not NP-intermediate.

- ☐ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☒ Both statements hold.
- ☐ None of the two statements holds.

**Question 27****1 / 1 pts**

Which one of the following statements holds?

1st statement: Space complexity class  $\text{coNL}$  is the complement of space complexity class  $\text{NL}$ .

2nd statement:  $\text{NL} \subseteq \text{coNL}$ .

- ☐ Only the 1st statement holds.
- ☒ Only the 2nd statement holds.
- ☐ Both statements hold.
- ☐ None of the two statements holds.

**Question 28****1 / 1 pts**

Which one of the following statements holds?

1st statement: REACHABILITY can be decided by a nondeterministic Turing machine in polynomial time.

2nd statement: REACHABILITY is recursively enumerable.

- ☐ Only the 1st statement holds.
- ☐ Only the 2nd statement holds.
- ☒ Both statements hold.
- ☐ None of the two statements holds.

**Question 29****1 / 1 pts**

Which one of the following statements holds?

1st statement: There is a language which can be decided by nondeterministic offline Turing machine of  $O(n \log n)$  space complexity, but can not be decided by a deterministic offline Turing machine of polynomial space complexity.

2nd statement: There is a language in NP which can not be decided by a deterministic offline Turing machine of polynomial space complexity.

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- ☐ Only the 1st statement holds.
- 
- ☐ Only the 2nd statement holds.
- 
- ☐ Both statements hold.
- 
- ☒ None of the two statements holds.

**Question 30****1 / 1 pts**

Which one of the following statements can be stated being TRUE?

1st statement: Every PSPACE-complete language is in NPSPACE.

2nd statement: 3SAT is PSPACE-complete.

- 
- ☒ Only the 1st statement.
- 
- ☐ Only the 2nd statement.
- 
- ☐ Both statements.
- 
- ☐ None of the statements.

**Quiz Score: 18 out of 30**