

# Midterm test - quiz

**Due** Apr 16, 2021 at 5:02pm

**Points** 30

**Questions** 15

**Available** until Apr 16, 2021 at 5:02pm

**Time Limit** 40 Minutes

This quiz is no longer available as the course has been concluded.

## Attempt History

	Attempt	Time	Score
LATEST	<a href="#">Attempt 1</a>	26 minutes	30 out of 30

! Correct answers are hidden.

Score for this quiz: **30** out of 30

Submitted Apr 16, 2021 at 4:58pm

This attempt took 26 minutes.

### Question 1

2 / 2 pts

$A=[1..4]$  is the base-statespace of program  $S$ .

$$S = \left\{ \begin{array}{l} 1 \rightarrow \langle 1, 2 \rangle, 1 \rightarrow \langle 1, 4, 2, 3 \rangle, 1 \rightarrow \langle 1, 4 \rangle \\ 2 \rightarrow \langle 2, fail \rangle, 2 \rightarrow \langle 2 \rangle \\ 3 \rightarrow \langle 3, 1 \rangle, 3 \rightarrow \langle 3, 2 \rangle, 3 \rightarrow \langle 3 \rangle, 3 \rightarrow \langle 3, 4 \rangle, \\ 4 \rightarrow \langle 4 \rangle, 4 \rightarrow \langle 4, 4, \dots \rangle \end{array} \right\}$$

Select all the true statements!

☐  $(4,4) \in p(S)$

☐  $(2,2) \in p(S)$

☒  $(1,4) \in p(S)$

☐ None of the other statements is true.

☒  $2 \in p(S)(1)$

**Question 2****2 / 2 pts**

$A = [1..4]$  is the base-statespace of program  $S$ .

We do not know the program  $S$ , but we know that  $p(S) = \{ (1,1), (3,1) \}$ .

$F = \{ (3,2), (3,1), (1,W) \}$  is a problem over  $A$ , where  $W \in A$ .

Which state of  $A$  would you choose as  $W$  in order to satisfy the following condition:

- program  $S$  solves problem  $F$

☐  $w$  can be either 1 or 3, but it cannot be 2 or 4

☐  $w$  can be any state of  $A$

☐ there is no state in  $A$  that makes the given condition true

☒  $w$  can be nothing else but 1

**Question 3****2 / 2 pts**

$H = [1..10]$

$A = (x:H)$

Let  $S$  denote the loop over the statespace  $A$ , where the program  $x := x - 3$  is the body of the loop, and the logical function  $x > 3$  is the loop condition.

Select all the true statements!

☒ State  $\{x:2\}$  is in the domain of relation  $p(S)$ .

☐ None of the other statements is true.



Starting its execution from the state  $\{x:10\}$ , program  $S$  terminates faultlessly.

☒ The pair  $(\{x:7\}, \{x:1\})$  is in set  $p(S)$ .

- ☒ State  $\{x:2\}$  is in set  $p(S)(\{x:8\})$ .

### Question 4

2 / 2 pts

$A=[1..4]$  is the base-statespace of program  $S$ .

$$S = \{ \begin{array}{l} 1 \rightarrow \langle 1, 2 \rangle, 1 \rightarrow \langle 1, 4, 2, 3 \rangle, 1 \rightarrow \langle 1, 4 \rangle \\ 2 \rightarrow \langle 2, fail \rangle, 2 \rightarrow \langle 2 \rangle \\ 3 \rightarrow \langle 3, 1 \rangle, 3 \rightarrow \langle 3, 2 \rangle, 3 \rightarrow \langle 3 \rangle, 3 \rightarrow \langle 3, 4 \rangle, \\ 4 \rightarrow \langle 4 \rangle, 4 \rightarrow \langle 4, 4, \dots \rangle \end{array} \}$$

Select all the true statements!

☐  $(2,2) \in p(S)$

☒  $(3,3) \in p(S)$

☒  $4 \notin p(S)$

☒  $1 \in p(S)(3)$

☐ None of the other conditions is true.

### Question 5

2 / 2 pts

$H = [1..10]$

$A = (x:H)$

Let  $S$  denote the program  $x := x-3$  over the base-statespace  $A$ .

How many elements does the set  $D_{p(S)}$  have?

☐ 0

☐ 6

☐ infinite number of elements

☒ 7

☐ 8

### Question 6

2 / 2 pts

$H = [1..10]$

$A = (x:H)$

Let  $S$  denote the loop over the statespace  $A$ , where the program  $x := x - 3$  is the body of the loop, and the logical function  $x > 3$  is the loop condition.

How many elements does the set  $D_p(S)$  have?

☐ 7

☒ 10

☐ 0

☐ 8

### Question 7

2 / 2 pts

How many of the following sequences can be in the range of a program over the base-statespace  $A = [1..4]$ ?

$\langle 1, 1, 1, 1, \dots \rangle$

$\langle 3, \text{fail} \rangle$

$\langle 4, (4, \text{false}), 1 \rangle$

3

**Question 8****2 / 2 pts** $H = [1..10]$  $A = (x:H)$ 

Let  $S$  denote the loop over the statespace  $A$ , where the program  $x := x-3$  is the body of the loop, and the logical function  $x > 3$  is the loop condition.

How many executions program  $S$  have, that end in the state *fail* ?

☒ 0☐ 2☐ 3☐ 10**Question 9****2 / 2 pts**

$A=[1..4]$  is the base-statespace of program  $S$ .

We do not know the program  $S$ , but we know that  $p(S)=\{(3,2), (3,1)\}$ .

$F=\{(3,2), (3,1), (1,w)\}$  is a problem over  $A$ , where  $w \in A=[1..4]$ .

Which state of  $A$  would you choose as  $w$  in order to satisfy the following condition:

- program  $S$  solves problem  $F$

☒ there is no state in  $A$  that makes the given condition true☐  $w$  can be any state of  $A$ ☐ the given information is not sufficient to answer the question☐  $w$  can be nothing else but 1

**Question 10****2 / 2 pts**

$$A = (x:\mathbb{N}^+, y:\mathbb{N}^+)$$

Given a problem F in the following way:

$$F = \{ (a,b) \in A \times A \mid 3 \cdot x(a) + 2 \cdot y(b) < 10 \}$$

How many elements does problem F have?

☐ 6☐ 3☒ 4☐ 5**Question 11****2 / 2 pts**

$$A = (x:\mathbb{N}, y:[1..100])$$

Consider the following problem over statespace A:

$$F = \{ (a,b) \in A \times A \mid x(a)=x(b) \wedge 2 \cdot y(b) < x(a) \}$$

Is the pair ( {x:8, y:10}, {x:8, y:3} ) in the problem F?

☒ True☐ False**Question 12****2 / 2 pts**

$$A = (x:\mathbb{N}, y:\mathbb{N}, z:\mathbb{N})$$

$$B = (x':\mathbb{N}, y':\mathbb{N})$$

$Q = (x=x' \wedge y=y')$  $R = (Q \wedge x < z \wedge z < y \wedge \text{prime}(z))$ 

$\text{prime}(z)$  is true if  $z$  is a prime number.

Consider the specification given above.

How many elements does the truth set of  $R\{x':20, y':25\}$  have?

☐ infinite number of elements

☐ 3

☐ 0

☒ 1

### Question 13

2 / 2 pts

$A = \{1,2\}$  is the base-statespace of program  $S$ .

$S = \{1 \rightarrow \langle 1,2 \rangle, 2 \rightarrow \langle 2,2,2,\dots \rangle\}$

Given two problems  $F1$  and  $F2$ :

$F1 = \{(1,1)\}$

$F2 = \{\}$

Which problem does the program  $S$  solve?

☐  $S$  solves both  $F1$  and  $F2$ .

☐  $S$  solves  $F1$ , but does not solve  $F2$ .

☐  $S$  does not solve  $F1$ , and  $S$  does not solve  $F2$ .

☒  $S$  solves  $F2$ , but does not solve  $F1$ .

### Question 14

2 / 2 pts

$A = (x:[1..10])$

How many elements are there in the truth set of the following function?

$wp(x:=x-3, x < 5)$

4

### Question 15

2 / 2 pts

$A = (x:\mathbb{N}, y:[1..100])$

Consider the following problem over statespace A:

$F = \{ (a,b) \in A \times A \mid x(a)=x(b) \wedge 2 \cdot y(b) < x(a) \}$

Is the pair  $(\{x:8, y:10\}, \{x:8, y:3\})$  in the problem F?

☒ True

☐ False

Quiz Score: **30** out of 30