

CSEN 102: Introduction to Computer Science
Winter Semester 2013-2014
 Midterm Exam

Instructions: Read carefully before proceeding.

- Good Luck!**

[illegible]

Exercise 1 Sequential algorithms
Wooden Boxes

(5 Marks)

A factory manufactures wooden boxes (a box is a cuboid with six faces). The price of the wood is 10LE/m². Write an algorithm that, given the three dimensions of the box in meters, calculates and prints the total surface area of the box and the price of the wood needed.

Solution:

```
1 get width, length, height
2 set area to length * width * 2 + length * height * 2 + height * width * 2
3 set cost to area * 10
4 print "The_area_is_"
5 print area
6 print "The_cost_is_"
7 print cost
```

Exercise 2 Conditional operations
BMI

(10 Marks)

The body mass index (BMI) is the ratio of the weight of a person (in kilograms) to the square of the height (in meters). Write an algorithm that given the weight and height, computes the BMI, and prints out the corresponding BMI category:

- Starvation: less than 15
- Anorexic: less than 17.5
- Underweight: less than 18.5
- Ideal: greater than or equal to 18.5 but less than 25
- Overweight: greater than or equal to 25 but less than 30
- Obese: greater than or equal to 30 but less than 40
- Morbidly Obese: greater than or equal to 40

You algorithm should test the least number of conditions once it is executed.

Solution:

```
1  get weight
2  get height
3  set ratio to (weight/(height * height))
4  if (ratio >= 40)
5      then print "Morbidly_Obese"
6  else
7      if (ratio >= 30)
8          then print "Obese"
9      else
10         if (ratio >= 25)
11             then print "Overweight"
12         else
13             if (ratio >= 18.5)
14                 then print "Ideal"
15             else
16                 if (ratio >= 17.5)
17                     print "Underweight"
18                 else
19                     if (ratio >= 15)
20                         then print "Anorexic"
21                     else
22                         print "Starvation"
23                     endif
24                 endif
25             endif
26         endif
27     endif
28 endif
```

**Exercise 3 Conditional
 Chinese Zodiac**

(10 Marks)

Chinese tradition assigns one of twelve zodiac signs to each year. After a twelve year circle, the signs are repeated in the same order. The order is: Rat—Ox—Tiger—Rabbit—Dragon—Snake—Horse—Sheep—Monkey—Rooster—Dog—Pig. Chinese New Year is usually in the beginning of February, so a Chinese year can be approximately identified with a Western calendar year. The last year of the Rat coincided with 2008.

Write a program that, given a year after 2013, gives the zodiac sign of the coinciding Chinese year.

You are not allowed to use any else statements.

Solution:

```
1  get year
2  set year to year - 2008
3  set year to year%12
4
5  if (year = 0) then
6      print "The_year_of_the_Rat."
7  endif
8
9  if (year = 1) then
10     print "The_year_of_the_Ox."
11 endif
12
13 if (year = 2) then
14     print "The_year_of_the_Tiger."
15 endif
16
17 if (year = 3) then
18     print "The_year_of_the_Rabbit."
19 endif
20
21 if (year = 4) then
22     print "The_year_of_the_Dragon."
23 endif
24
25 if (year = 5) then
26     print "The_year_of_the_Snake."
27 endif
28
29 if (year = 6) then
30     print "The_year_of_the_Horse."
31 endif
32
33 if (year = 7) then
34     print "The_year_of_the_Sheep."
35 endif
36
37 if (year = 8) then
38     print "The_year_of_the_Monkey."
39 endif
40
41 if (year = 9) then
42     print "The_year_of_the_Rooster."
43 endif
44
45 if (year = 10) then
```

```
46     print "The_year_of_the_Dog."
47 endif
48
49 if (year = 11) then
50     print "The_year_of_the_Pig."
51 endif
```

Exercise 4 Conditional operations
Letter Grade

(4+2+8=14 Marks)

Some schools use a scale like the following to determine the proper letter grade to assign to a student. The letter grade is based on a percentage representing a weighted average of all of the work for the term. Based on the following table, all percentage values must be in the range of 0.0 through 100.0:

Value of Percentage	Assigned Grade
$90.0 \leq \text{percentage} \leq 100.0$	A
$80.0 \leq \text{percentage} < 90.0$	B
$70.0 \leq \text{percentage} < 80.0$	C
$60.0 \leq \text{percentage} < 70.0$	D
$0.0 \leq \text{percentage} < 60.0$	F

An algorithm to determine where the range `weightedAverage` falls into could be implemented with unnecessarily long separate if statements.

```

get weightedAverage
set result to ""
if (weightedAverage > 100)
then set result to "The average is out of range"
endif
if (weightedAverage >= 90.0)
then set result to "A"
endif
if (weightedAverage >= 80.0 AND weightedAverage <= 90.0)
then set result to "B"
endif
if (weightedAverage >= 70.0 AND weightedAverage < 80.0)
then set result to "C"
endif
if (weightedAverage >= 60.0 AND weightedAverage < 70.0)
then set result to "D"
endif
if (weightedAverage >= 0.0 AND weightedAverage < 60.0)
then set result to "F"
endif
print result

```

- (a) The algorithm has two errors/missing statements that you should find and fix.

Solution:

- There is a missing condition in the second if statement to avoid that the result A will be printed for number that are out of range.

```
if (weightedAverage >= 90.0 AND weightedAverage <= 100)
```

- The second mistake is the overlap of the second and third conditions of the if statements. In case `weightedAverage` is equal to 90, the algorithm would print A and then B.

```
if (weightedAverage >= 80.0 AND weightedAverage < 90.0)
```

- (b) What is the main disadvantage of the algorithm above after fixing the two errors/missing statements?

Solution:

Independent of the value of `weightedAverage` all conditions of the if statements have to be checked once the algorithm is executed. This leads to an inefficient algorithm.

- (c) Rewrite the algorithm to avoid the disadvantage you mentioned in the previous question. **You are not allowed to use compounded conditions.**

Solution:

```
1  Get wa
2  if( wa > 100 ) then
3      print "out "
4  else
5      if(wa >= 90) then
6          print "A"
7      else
8          if(wa>=80) then
9              print "B"
10         else
11             if(wa>=70) then
12                 print "C"
13             else
14                 if(wa>=60) then
15                     print "D"
16                 else
17                     print "F"
18                 endif
19             endif
20         endif
21     endif
22 endif
```

Exercise 5 Iteration
Rotation

(10 Marks)

Write an algorithm that rotates the digits of a 4-digit number (m), n places to the right and displays the output.

For example

- if m is 9732 and n is 1, the output should be 2973.
- if m is 1234 and n is 2, the output should be 3412.
- if m is 5814 and n is 3, the output should be 8145.

Solution:

```
1  get m
2  get n
3
4  set i to 1
5
6  while (i <= n)
7  {
8      set ones to m%10
9      set num to INT(m/10)
10     set m to ones*1000 + num
11     set i to i+1
12 }
13
14 print m
```


Exercise 6 Iterative algorithms
ISBN

(15 Marks)

The International Standard Book Number (ISBN) is a 10 digit code that uniquely specifies a book. The rightmost digit is a checksum digit which can be uniquely determined from the other 9 digits from the condition that $d_1 + 2d_2 + 3d_3 + \dots + 10d_{10}$ must be a multiple of 11 (here d_i denotes the i th digit from the right).

The checksum digit d_1 can be any value from 0 to 10; the ISBN convention is to use the value X to denote 10.

Example: the checksum digit corresponding to 020131452 is 5 since it is the only value of d_1 between 0 and 10 for which $d_1 + 2 * 2 + 3 * 5 + 4 * 4 + 5 * 1 + 6 * 3 + 7 * 1 + 8 * 0 + 9 * 2 + 10 * 0$ is a multiple of 11.

Write an algorithm that takes a 9-digit integer and computes the checksum, and prints it out. Your algorithm should print X if the checksum digit is 10.

Solution:

```

1  get n
2  set sum to 0
3  set i to 2
4  while (i <= 10) {
5      set digit to n % 10
6      set sum to sum + i * digit
7      set n to INT(n / 10)
8  }
9
10 if (sum % 11 == 1)
11 then print "X"
12 else if (sum % 11 == 0)
13     then print "0"
14     else
15         print 11 - (sum % 11)
16     endif
17 endif

```

Exercise 7 Conditional operations
Tracing

(4+4+6=14 Marks)

Given the following fragment of a Java program

```
int a = 7; int b = 22; int c = 4;
if (b < a) { int t = b; b = a; a = t; }
if (c < b) { int t = c; c = b; b = t; }
if (b < a) { int t = b; b = a; a = t; }
System.out.println(" " + a + " " + b + " " + c);
```

- (a) Trace the algorithm above and write out what it will print.

Solution:

The algorithm prints

4 7 22

- (b) What does the algorithm do for any three variables a, b and c.

Solution:

The algorithm sorts the three numbers in ascending order.

- (c) Write an algorithm that will do the same for 5 variables a, b, c, d and e. The algorithm should look similar to the one above for three variables.

Solution:

```
1 public class Sorting {
2     public static void main(String[] args) {
3         int A = 5;
4         int B = 22;
5         int C = 3;
6         int D = 13;
7         int E = 1;
8         int t;
9
10        if (A > B) { t = A; A = B; B = t; }
11        if (B > C) { t = B; B = C; C = t; }
12        if (A > B) { t = A; A = B; B = t; }
13        if (C > D) { t = C; C = D; D = t; }
14        if (B > C) { t = B; B = C; C = t; }
15        if (A > B) { t = A; A = B; B = t; }
16        if (D > E) { t = D; D = E; E = t; }
17        if (C > D) { t = C; C = D; D = t; }
18        if (B > C) { t = B; B = C; C = t; }
19        if (A > B) { t = A; A = B; B = t; }
20
21        System.out.println(" " + A + " " + B + " " + C + " " + D + " " + E);
22    }
23 }
```

Exercise 8 Iterative operations
Tracing

(6+4+4=14 Marks)

Given the following algorithm

```
get n
set x to 1
set c to 0
while (n >= 1) {
    print x
    set c to c + 1
    set x to 2 * x
    set n to INT(n/2)
}
print c
```

- (a) Draw the tracing table for $n=19$ and write out what the algorithm will print.

Solution:

The algorithm prints the following sequence

1 2 4 8 16

and prints then 5 which is the length of the sequence.

- (b) What is the sequence printed by the algorithm for any n ?

Solution:The algorithm prints the power of 2 from 1 to n .

- (c) What is the value of c in terms of n ?

Solution: $c = \lfloor \log_2(n) \rfloor + 1$ where $\lfloor \cdot \rfloor$ corresponds to the floor function.

Exercise 9 Java

(2+2+2+2+4(Bonus)=8 Marks)

- (a) What does the compiler do if you try to write the following expression:

```
double x;  
System.out.println(x);
```

Solution:

It is a compile error since the variable is not initialized with a value.

- (b) Suppose that `a` and `b` are `int` values. What does the following sequence of statements do?

```
int t = a;  
b = t;  
a = b;
```

Solution:

The variables `a` and `b` will be assigned to the initial value of `a`.

- (c) What does the following statement do where `grade` is a variable of type `int`?

```
boolean isA = (90 <= grade <= 100);
```

Solution:

It is a compile error. It has to be written with a compounded condition.

```
boolean isA = (grade >= 90 && grade <= 100);
```

- (d) What is wrong with the following if statement?

```
boolean done = false;  
if (done = false) {  
    ...  
}
```

Solution:

A comparison should be done with `==`.

- (e) Write the **shortest** Java program you can that takes an integer `N` and print true if $(1 + 2 + \dots + N)^2$ is equal to $(1^3 + 2^3 + \dots + N^3)$.

Solution:

```
public static void main(String[] args) {  
    System.out.println(true);  
}
```

Exercise 10 Iterative operations
Tracing

(6+4=10 Marks)

Given the following Java program

```
public static void main(String[] args) {
    int N = 5;
    String s = "";
    int i = 1;
    while (i <= N) {
        if (i % 2 == 0)
        {
            s = s + i + s;
        }
        else
        {
            s = i + s + i;
        }
        i = i + 1;
    }
    System.out.println(s);
}
```

- (a) Draw the tracing table for N=5 and mention what will be printed at the end of the execution of the Java program.

Solution:

The algorithm will print 53112113431121135.

- (b) The algorithm prints for any N a string with a specific feature. Mention the feature of this string.

Solution:

The string is a palindrome, i.e. a word that reads the same forward as backward.