Heuristics

Question 1a

The Euclidian Distance is the distance between two points calculated with: $\frac{(x_2-x_1)^2+(y_2-y_1)^2}$ for points (x_1, y_1) and (x_2, y_2) . Usually used when the movement is unrestricted (up, down, left, right, diagonal).

Question 1b

The Manhattan Distance is the distance between two points calculated with: $|x_2-x_1|+|y_2-y_1|$ for points (x_1, y_1) and (x_2, y_2) . Usually used when the movement is restricted to a grid (up, down, left, right).

Question 2a

- Visited = []; Unvisited = [A, B, C, D, E, F, Z]
- initial state

Vertex	Distance	Previous	
Α	0	-	
В	∞	-	
С	∞	-	
D	∞	-	
Е	∞	-	
F	∞	-	
Z	∞	-	

- Visited = [A]; Unvisited = [B, C, D, E, F, Z]
- from A to B: 0+4=4
- from A to C: 0+3=3

Vertex	Distance	Previous
А	0	-
В	4	А
С	3	А
D	∞	_
Е	∞	-
F	∞	_

Vertex	Distance	Previous
Z	∞	-

- Visited = [A, C]; Unvisited = [B, D, E, F, Z]
- from C to D: 3+7=10
- from C to E: 3+10=13

Vertex	Distance	Previous
Α	0	-
В	4	А
С	3	А
D	10	С
Е	13	С
F	∞	_
Z	∞	-

- Visited = [A, C, B]; Unvisited = [D, E, F, Z]
- from B to E: 4+12=16
- from B to F: 4+5=9

Vertex	Distance	Previous	
Α	0	-	
В	4	А	
С	3	А	
D	10	С	
Е	13	С	
F	9	В	
Z	∞	-	

- Visited = [A, C, B, F]; Unvisited = [D, E, Z]
- from F to Z: 9+16=25

Vertex	Distance	Previous	
Α	0	-	
В	4	A	
С	3	A	

Vertex	Distance	Previous C	
D	10		
Е	13	С	
F	9	В	
Z	25	F	

- Visited = [A, C, B, F, D]; Unvisited = [E, Z]
- from D to E: 10+2=12

Vertex	Distance	Previous	
Α	0	-	
В	4	Α	
С	3	Α	
D	10	С	
E	12	D	
F	9	В	
Z	25	F	

- Visited = [A, C, B, F, D, E]; Unvisited = [Z]
- from E to Z: 12+5=17

Vertex	Distance	Previous
А	0	-
В	4	Α
С	3	А
D	10	С
Е	12	D
F	9	В
Z	17	E

- Visited = [A, C, B, F, D, E, Z]; Unvisited = []
- No more vertices to visit

Vertex	Distance	Previous	
Α	0	-	

Vertex	Distance	Previous	
В	4	А	
С	3	А	
D	10	С	
Е	12	D	
F	9	В	
Z	17	Е	

• Shortest path: A -> C -> D -> E -> Z; Cost: 17

Question 2b

- Initial state: G=0, H=14, F=14
- open = [A]; closed = []
- Expand A (F=14)
- Examine B, C
- open = [B, C]; closed = [A]

Node	G	Н	F	Previous
В	4	12	16	Α
С	3	11	14	Α

- Expand C (F=14)
- Examine D, E
- open = [B, D, E]; closed = [A, C]

Node	G	Н	F	Previous
В	4	12	16	А
С	3	11	14	А
D	10	6	16	С
Е	13	4	17	С

- Expand B (F=16)
- Examine E, F
- open = [D, E, F]; closed = [A, C, B]

Node	G	Н	F	Previous
В	4	12	16	А

Node	G	Н	F	Previous
С	3	11	14	А
D	10	6	16	С
Е	13	4	17	С
F	9	11	20	В

- Expand D (F=16)
- Examine E
- open = [E, F]; closed = [A, C, B, D]

Node	G	Н	F	Previous
В	4	12	16	А
С	3	11	14	А
D	10	6	16	С
Е	12	4	16	D
F	9	11	20	В

- Expand E (F=16)
- Examine Z
- open = [F, Z]; closed = [A, C, B, D, E]

Node	G	Н	F	Previous
В	4	12	16	А
С	3	11	14	А
D	10	6	16	С
Е	12	4	16	D
F	9	11	20	В
Z	17	0	17	E

• Shortest path: A -> C -> D -> E -> Z; Cost: 17