

Q1

(1) $C^+ = \{C\}$, $J \notin C^+$ so $C \rightarrow J \notin F^+$

(2) $F' = \{A \rightarrow B, A \rightarrow C, E \rightarrow A, E \rightarrow D, BD \rightarrow E, CE \rightarrow D, CE \rightarrow H, H \rightarrow G, EI \rightarrow J\}$

$BD \rightarrow E$, $B^+ = \{B\}$, Hence, $BD \rightarrow E$ cannot be replaced by $B \rightarrow E$

$D^+ = \{D\}$, Hence, $BD \rightarrow E$ cannot be replaced by $D \rightarrow E$

so $BD \rightarrow E$ cannot be replaced

$CE \rightarrow D$, $C^+ = \{C\}$, Hence, $CE \rightarrow D$ cannot be replaced by $C \rightarrow D$

$E^+ = \{A, B, C, D\}$, Hence, $CE \rightarrow D$ can be replaced by $E \rightarrow D$

$CE \rightarrow H$, $C^+ = \{C\}$, Hence, $CE \rightarrow H$ cannot be replaced by $C \rightarrow H$

$E^+ = \{A, B, C, D\}$, Hence, $CE \rightarrow H$ can be replaced by $E \rightarrow H$

$EI \rightarrow J$, $E^+ = \{A, B, C, D\}$, Hence, $EI \rightarrow J$ cannot be replaced by $E \rightarrow J$

$I^+ = \{I\}$, Hence, $EI \rightarrow J$ cannot be replaced by $I \rightarrow J$

so $F'' = \{A \rightarrow B, A \rightarrow C, E \rightarrow A, E \rightarrow D, BD \rightarrow E, CE \rightarrow H, H \rightarrow G, EI \rightarrow J\}$

$A^+|_{F'' - \{A \rightarrow B\}} = \{A, C\}$, so $A \rightarrow B$ is not redundant

$A^+|_{F'' - \{A \rightarrow C\}} = \{A, B\}$, so $A \rightarrow C$ is not redundant

$E^+|_{F'' - \{E \rightarrow A\}} = \{E, D\}$, so $E \rightarrow A$ is not redundant

$E^+|_{F'' - \{E \rightarrow D\}} = \{E, A\}$, so $E \rightarrow D$ is not redundant

$H^+|_{F'' - \{H \rightarrow G\}} = \{H\}$, so $H \rightarrow G$ is not redundant

so $F'' = F_{min} = \{A \rightarrow B, A \rightarrow C, E \rightarrow A, E \rightarrow D, BD \rightarrow E, E \rightarrow H, H \rightarrow G, EI \rightarrow J\}$

(3) $U = \{A, B, C, D, E, G, H, I, J, K\}$

$R_1 = \{A, B, C, D, E\}$ so $U_1 = \{A, B, C, D, E\}$

$R_2 = \{E, G, H\}$ so $U_2 = \{E, G, H\}$

$R_3 = \{E, I, J, K\}$ so $U_3 = \{E, I, J, K\}$

A	B	C	D	E	G	H	I	J	K
a_1	a_2	a_3	a_4	a_5	b_{16}	b_{17}	b_{18}	b_{19}	b_{110}
b_{21}	b_{22}	b_{23}	b_{24}	a_5	a_6	a_7	b_{28}	b_{29}	b_{210}
b_{31}	b_{32}	b_{33}	b_{34}	a_5	b_{36}	b_{37}	a_8	a_9	a_{10}

A	B	C	D	E	G	H	I	J	K
a_1	a_2	a_3	a_4	a_5	a_6	a_7	a_8	a_9	a_{10}
b_{21}	b_{22}	b_{23}	b_{24}	a_5	a_6	a_7	b_{28}	b_{29}	b_{210}
b_{31}	b_{32}	b_{33}	b_{34}	a_5	b_{36}	b_{37}	a_8	a_9	a_{10}

There is a row which has all the set in U , so R_1, R_2, R_3 of R is loss-less-join.

(4) left hand side of F is $X = \{A, E, B, D, C, H, I\}$

step1:

$A^+ = \{A, B, C\}$

$E^+ = \{A, B, C, D, E, H, G\}$

$B^+ = \{B\}$

$D^+ = \{D\}$

$$H^+ = \{G\}$$

$$I^+ = \{I\}$$

step2:

$$EI^+ = \{A, B, C, D, E, H, G, I, J\}$$

step3:

$$EIK^+ = \{A, B, C, D, E, H, G, I, J, K\}$$

So, super key are $\{EIK\}, \{BDIK\}, \{EIKH\}, \{EIKA\}, \{EIKB\}$

(5) $p = \{R1 = \{EIK\}, R2 = \{EIJ\}, R3 = \{EAD\}, R4 = \{ADH\}, R5 = \{HG\}, R6 = \{ABC\}\}$

A	B	C	D	E	G	H	I	J	K
				a			a		a
				a			a	a	
a			a	a					
a			a			a			
					a	a			
a	a	a							
a	a	a	a	a	a	a	a	a	a

So, this BCNF relations is lossless-join, but it cannot be dependency-preserving since there is no $BD \rightarrow E$.

Q2:

(1) undo T1, T3 and redo T2

(2) undo T1, T3.

Q3:

(1)

Data pages: P3, P4, P8, P7, P1

Queries:

Q1: read: P3, P4, P8, P7

Q2: read: P1, P8

Buffer: 3

FIFO:

Q1:

3	4	8
7	4	8

STEP:4

Q2:

7	4	8
7	1	8

STEP:1

FIFO: TOTAL STEP:1+4=5

MRU:

3	4	8
3	4	7

STEP:4

Q2

3	4	7
3	4	1
3	4	8

STEP:2

MRU: TOTAL STEP:4+2=6

So FIFO buffer replacement policy is better than MRU buffer replacement policy.

(2)

Data pages: P3, P4, P8, P7, P6

Queries:

Q1: read: P3, P4, P8, P7

Q2: read: P7, P6

Q3: read: P4, P6

Buffer: 3

FIFO:

Q1:

3	4	8
7	4	8

STEP:4

Q2:

7	4	8
7	6	3

STEP:2

Q3:

7	6	3
4	6	3

STEP:1

FIFO: TOTAL STEP:4+2+1=7

LRU:

3	4	8
7	4	8

STEP:4

Q2

7	4	8
7	6	3

STEP:2

Q3

7	6	3
7	4	6

STEP:2

LRU: TOTAL STEP: $4+2+2=8$

So FIFO buffer replacement policy is better than LRU buffer replacement policy.