

Week 12 Problem Set

Random Variables and Expectation

[\[Show with no answers\]](#) [\[Show with all answers\]](#)

Congratulations on reaching the end of this course!

Just one exercise for the last lecture. A sample solution will be posted on Friday (week 13).

1. (Expectation, variance)

You randomly draw one card at a time from a deck of 52 Poker cards: $\{2, 3, \dots, 10, J, Q, K, A\} \times \{\spadesuit, \clubsuit, \heartsuit, \diamondsuit\}$.

- a. Assume that the cards are not put back into the deck after each drawing.
 - i. Is the event of drawing a specific card independent of the previous draw?
 - ii. Calculate the expected number of drawing attempts until a card other than an ace is drawn.
 - iii. Calculate the expected number of drawing attempts until the sum of the cards drawn is ≥ 5 . (2–10 are counted as their numeric value; J, Q, K are counted as 10; A is counted as 11).
 - iv. Calculate the variances of the two random variables considered in questions (ii) and (iii).
- b. Answer questions (i)–(iii) for the case when the cards are put back after each drawing.

[\[show answer\]](#)