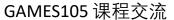
#### Lecture 06+

# Learning-based Character Animation (cont.)

#### Libin Liu

School of Intelligence Science and Technology Peking University





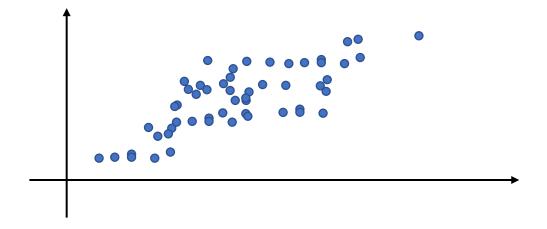


VCL @ PKU

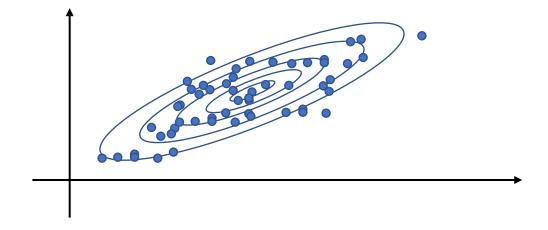
#### Outline

- Learning-based Character Animation (cont.)
  - Motion Models
  - Autoregressive models: PFNN
  - Generative models

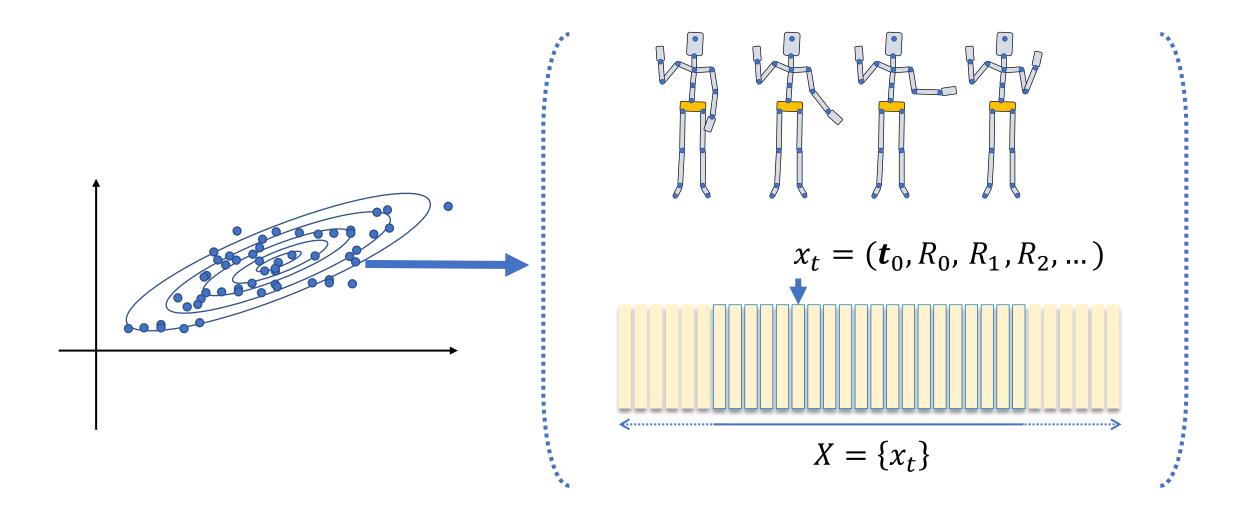
Given a set of example motions  $\{x_i\} \sim p(x)$ 

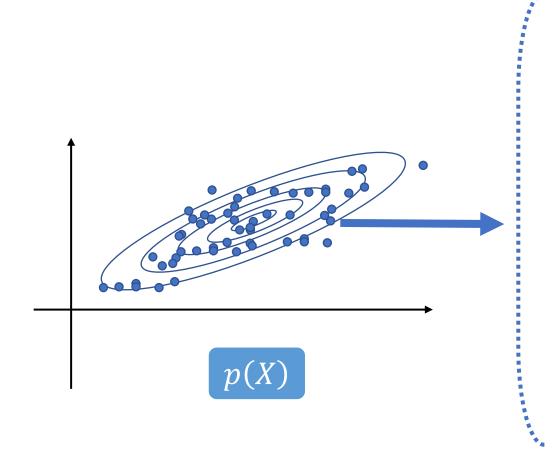


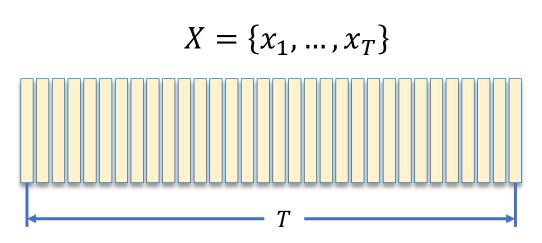
Given a set of example motions  $\{x_i\} \sim p(x)$ 



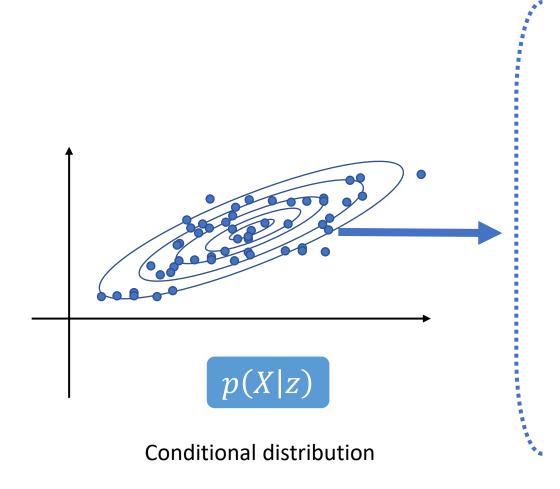
p(x): probability that x is a natural motion

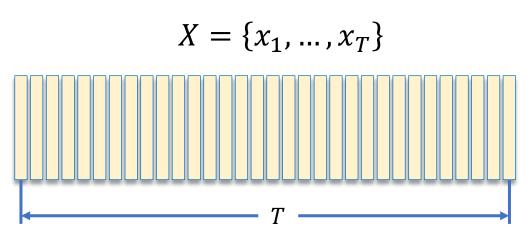






$$p(X) = p(x_1, \dots, x_T)$$

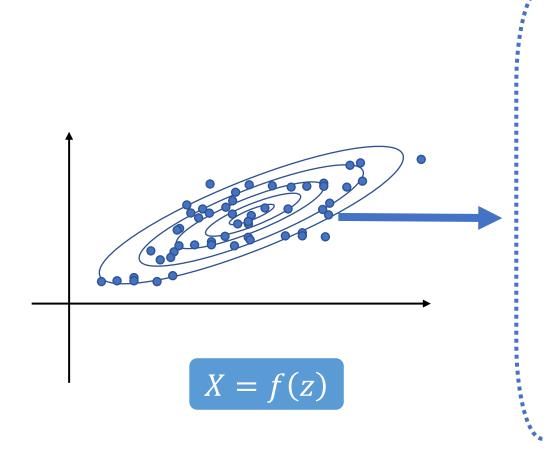


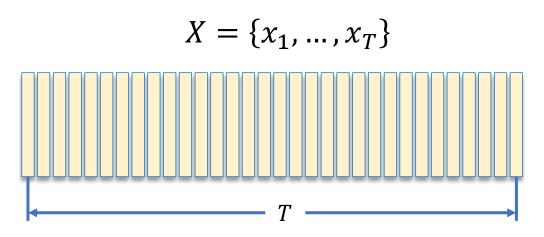


$$p(X|\mathbf{z}) = p(x_1, ..., x_T|\mathbf{z})$$

z: control parameterslatent variables

• • • • • •

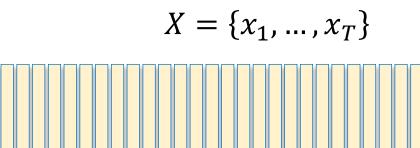




$$(x_1, \dots, x_T) = f(\mathbf{z})$$

z: control parameterslatent variables

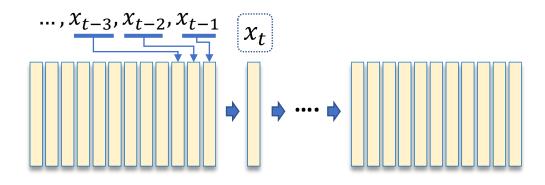
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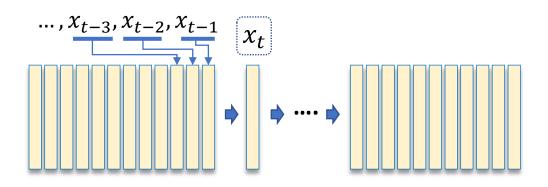




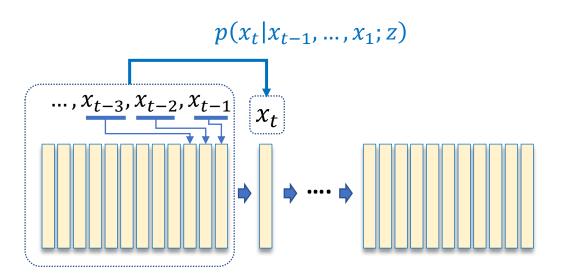


$$X = f(\mathbf{z})$$



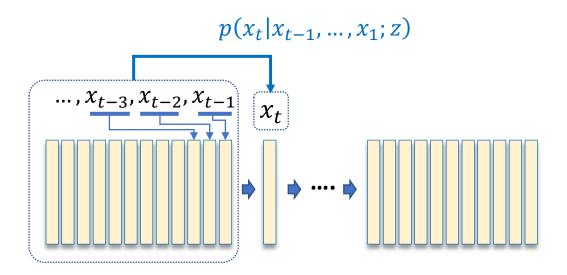


$$p(X|\mathbf{z}) = p(x_1, ..., x_T|\mathbf{z})$$



$$p(X|\mathbf{z}) = p(x_1, ..., x_T|\mathbf{z})$$

$$= p(x_1) \prod_{t} p(x_t | x_{t-1}, ..., x_1; z)$$

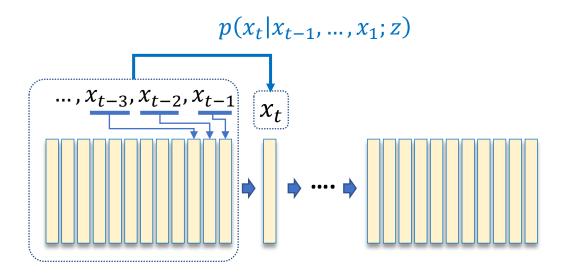


$$p(X|\mathbf{z}) = p(x_1, ..., x_T|\mathbf{z})$$

$$= p(x_1) \prod_{t} p(x_t | x_{t-1}, ..., x_1; z)$$

\*The chain rule of conditional probabilities:

$$p(x_1, x_2) = p(x_2|x_1)p(x_1)$$



$$p(X|\mathbf{z}) = p(x_1, ..., x_T|\mathbf{z})$$

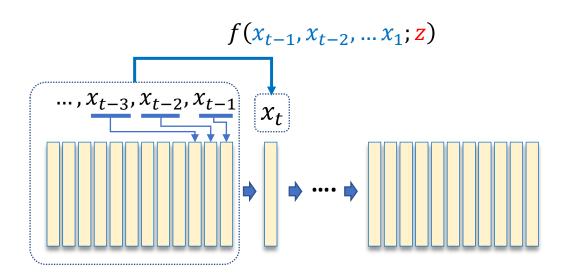
$$= p(x_1) \prod_{t} p(x_t | x_{t-1}, ..., x_1; z)$$

\*The chain rule of conditional probabilities:

$$p(x_1, x_2) = p(x_2|x_1)p(x_1)$$

$$p(x_1, x_2, x_3) = p(x_2, x_3|x_1)p(x_1)$$

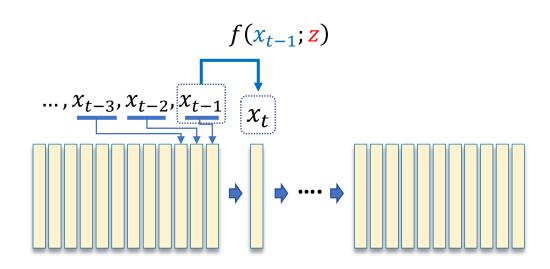
 $= p(x_3|x_2,x_1)p(x_2|x_1)p(x_1)$ 



$$p(X|\mathbf{z}) = p(x_1, ..., x_T|\mathbf{z})$$

$$= p(x_1) \prod_t p(x_t|x_{t-1}, ..., x_1; \mathbf{z})$$

$$x_t = f(x_{t-1}, x_{t-2}, ... x_1; \mathbf{z})$$

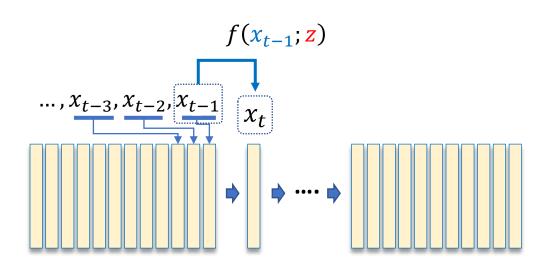


**Markov Property** 

$$p(X|z) = p(x_1, ..., x_T|z)$$

$$= p(x_1) \prod_t p(x_t|x_{t-1}, ..., x_1; z)$$

$$x_t = f(x_{t-1}, x_t, ..., x_1; z)$$



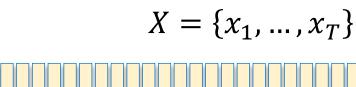
**Markov Property** 

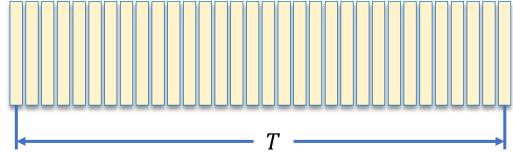
$$p(X|\mathbf{z}) = p(x_1, \dots, x_T|\mathbf{z})$$

$$= p(x_1) \prod_t p(x_t|x_{t-1};z)$$



$$x_t = f(x_{t-1}; \mathbf{z})$$

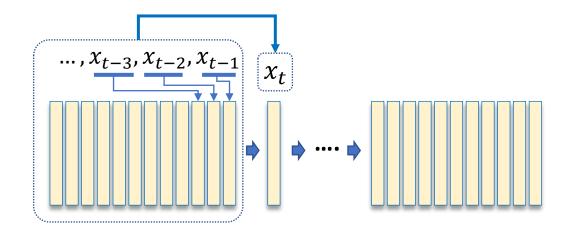








$$X = f(\mathbf{z})$$



$$p(x_t|x_{t-1},\ldots,x_1;z)$$



$$x_t = f(x_{t-1}, x_{t-2}, ...; z)$$

$$x_t = f(x_{t-1}; \mathbf{z})$$

Markov Property

$$x_t = f(x_{t-1}, x_{t-2}, ...; z)$$
  
 $x_t = f(x_{t-1}; z)$ 

$$x_t = f(x_{t-1}, x_{t-2}, \dots; z)$$
$$x_t = f(x_{t-1}; z)$$

$$x_t = f(x_{t-1}; \mathbf{z})$$

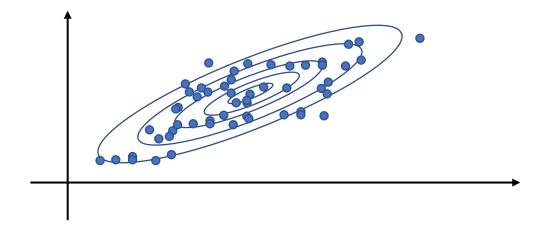
z: control parameterslatent variables

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$$x_t = f(x_{t-1})$$

$$x_t = f(x_{t-1})$$

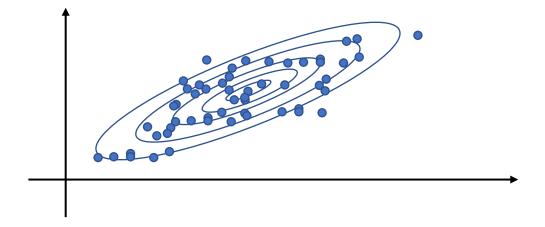
Given a set of example motions  $\{X_i\} \sim p(X)$ 

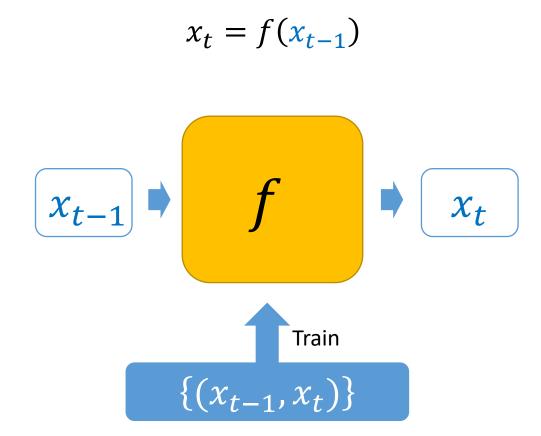


$$x_t = f(x_{t-1})$$

Given a set of example transitions

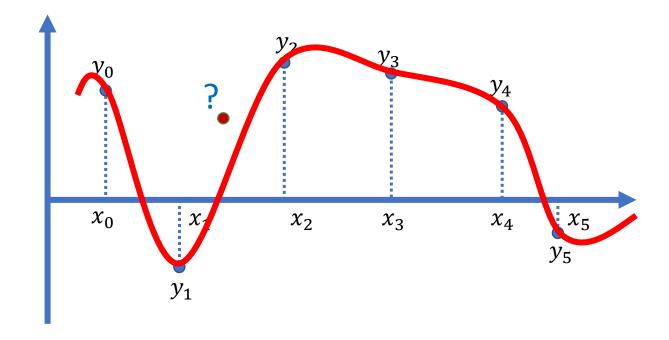
$$\{(x_{t-1},x_t)\} \sim p(X)$$

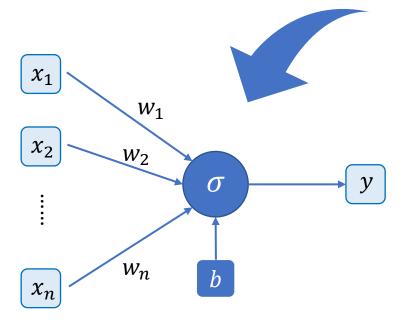


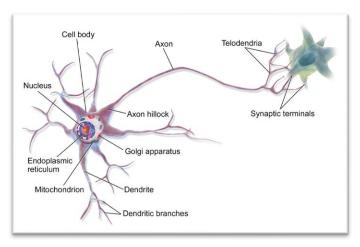


# Interpolation

$$f(x_i) = y_i \qquad \qquad f(x) = ?$$

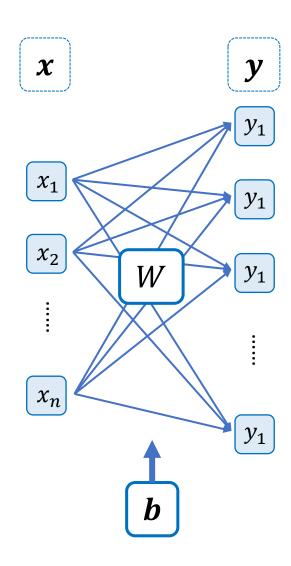




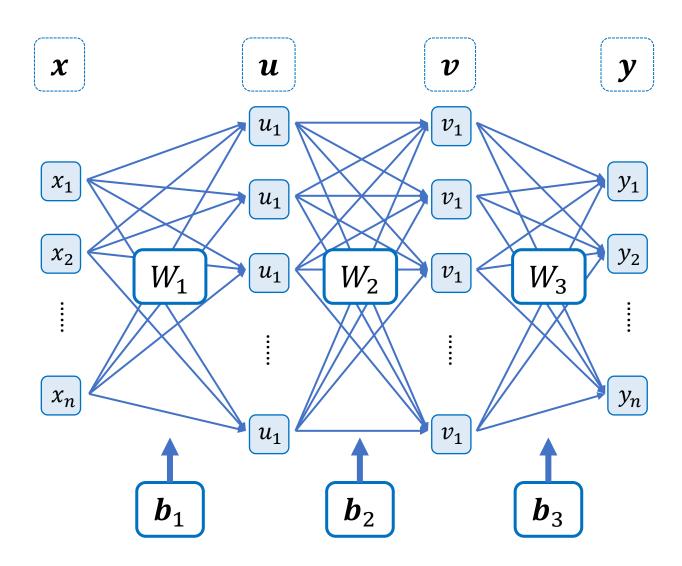


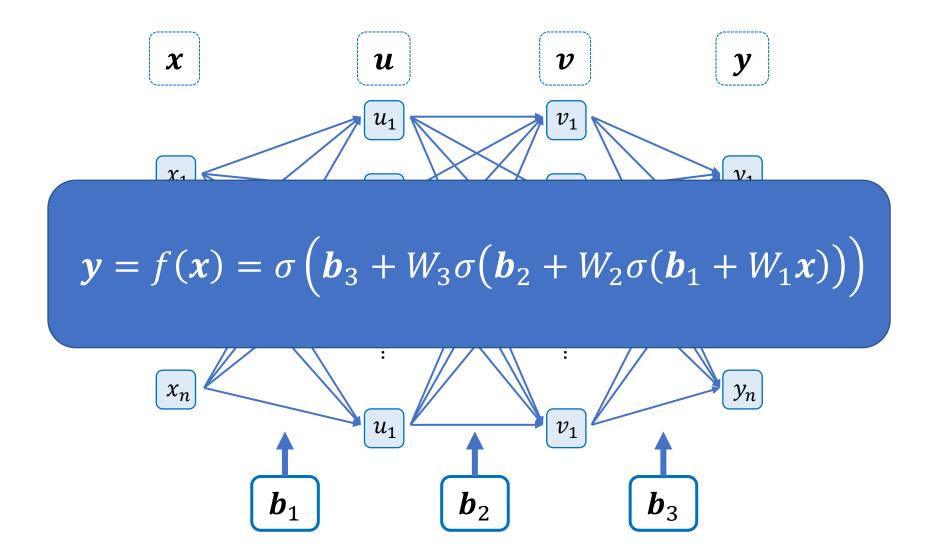
A Multipolar Neuron

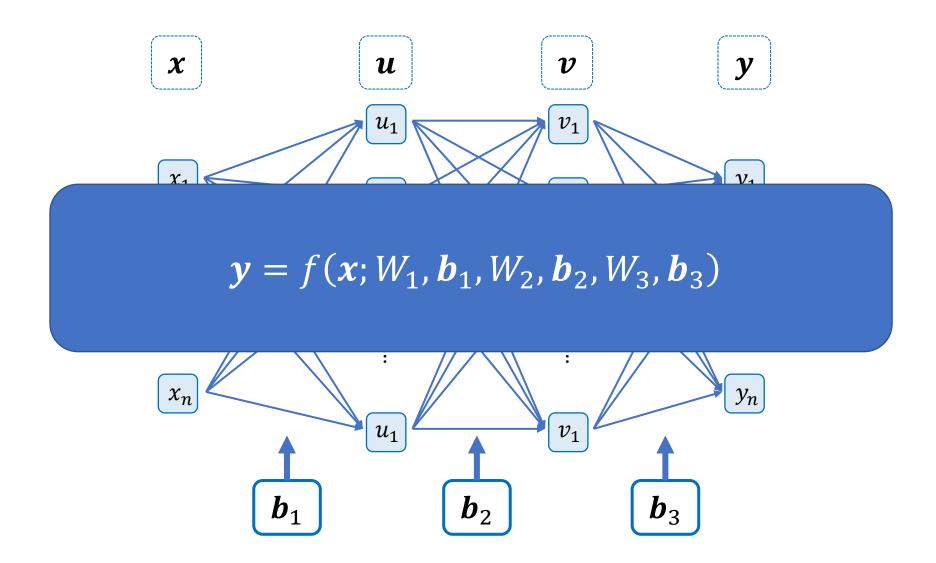
$$y = \sigma \left( \sum_{i} w_{i} x_{i} + b \right)$$



$$y = \sigma(Wx + b)$$







$$x_{t} = f(x_{t-1}; \theta)$$

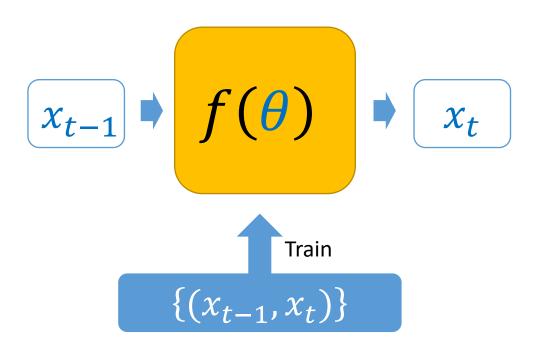
$$\theta = (W_{1}, \boldsymbol{b}_{1}, W_{2}, \boldsymbol{b}_{2}, \dots)$$

$$f(\theta) \qquad \qquad \boldsymbol{x}_{t}$$

$$x_{t-1} \qquad \qquad \boldsymbol{x}_{t}$$

$$\{(x_{t-1}, x_{t})\}$$

$$x_t = f(x_{t-1}; \boldsymbol{\theta})$$
  
$$\boldsymbol{\theta} = (W_1, \boldsymbol{b}_1, W_2, \boldsymbol{b}_2, \dots)$$



Given a set of example transitions

$$\{(x_{t-1},x_t)\} \sim p(X)$$

Find  $\theta = (W_1, \boldsymbol{b}_1, W_2, \boldsymbol{b}_2, ...)$  that minimizes

$$F(\theta) = \sum_{(x_{t-1}, x_t)} ||f(x_{t-1}; \theta) - x_t||$$

#### **Stochastic Gradient Descent:**

For a batch of random sample 
$$\left\{ (x_{t-1}^{(i)}, x_t^{(i)}) \right\} \sim \left\{ (x_{t-1}, x_t) \right\}$$

Compute the approximate gradient

$$\nabla_{\theta} F(\theta) \approx \sum_{i} \nabla_{\theta} \left( \left\| f\left(x_{t-1}^{(i)}; \theta\right) - x_{t}^{(i)} \right\| \right)$$

update 
$$\theta = (W_1, b_1, W_2, b_2, ...)$$
 as

$$\theta \leftarrow \theta - \alpha \nabla_{\theta} F(\theta)$$

#### Stochastic Gradient Descent:

For a batch of random sample 
$$\left\{ (x_{t-1}^{(i)}, x_t^{(i)}) \right\} \sim \left\{ (x_{t-1}, x_t) \right\}$$

Compute the approximate gradient

$$\nabla_{\theta} F(\theta) \approx \sum_{i} \nabla_{\theta} \left( \left\| f\left(x_{t-1}^{(i)}; \theta\right) - x_{t}^{(i)} \right\| \right)$$

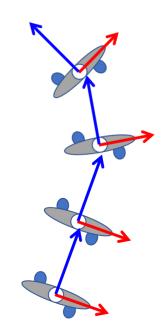
using backpropagation

update 
$$\theta = (W_1, b_1, W_2, b_2, ...)$$
 as

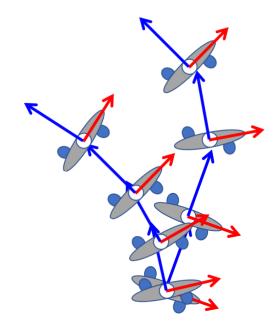
$$\theta \leftarrow \theta - \alpha \nabla_{\theta} F(\theta)$$

# Ambiguity Issue

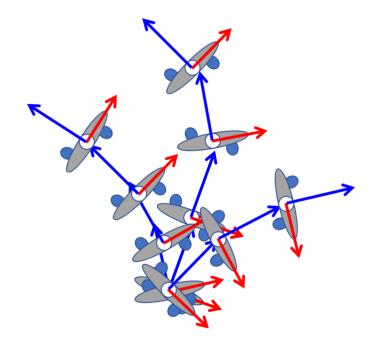
$$x_t = f(x_{t-1})$$



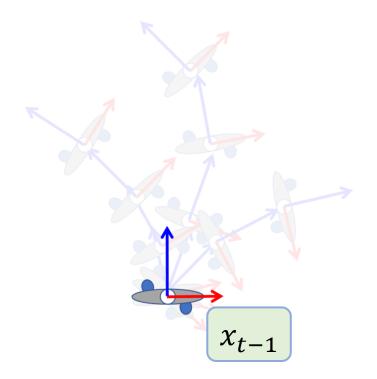
$$x_t = f(x_{t-1})$$



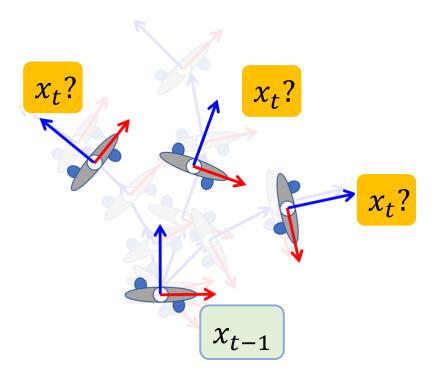
$$x_t = f(x_{t-1})$$



$$x_t = f(x_{t-1})$$

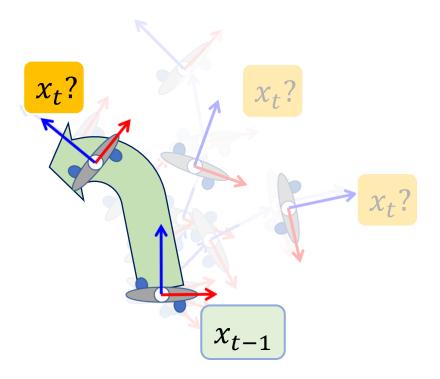


$$x_t = f(x_{t-1})$$

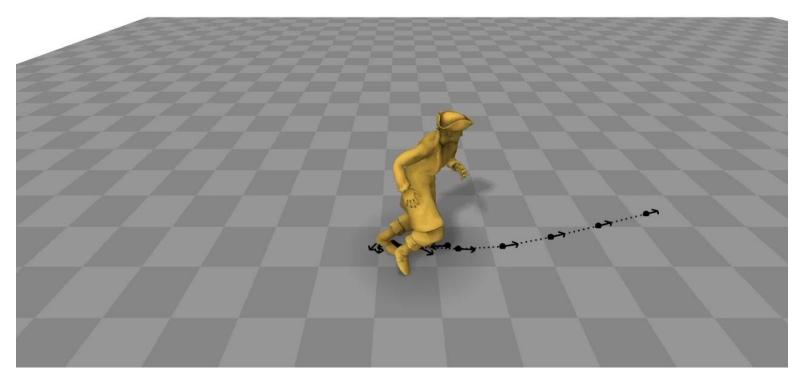


## Hidden Variables

$$x_t = f(x_{t-1}; \mathbf{z})$$







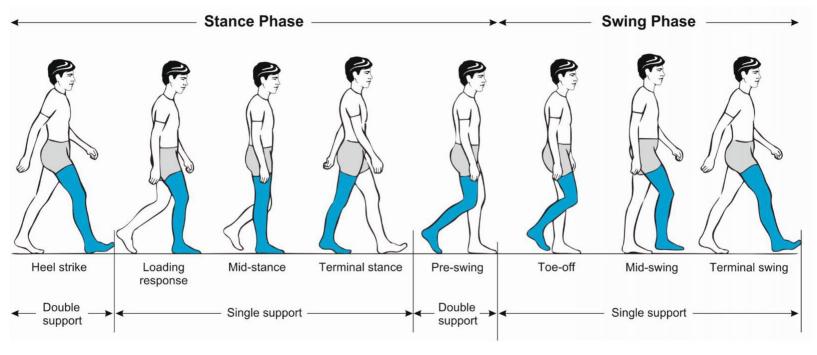
Phase-Functioned Neural Networks for Character Control

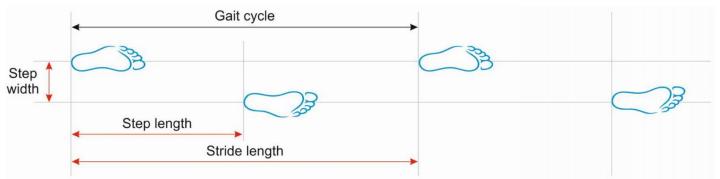
DANIEL HOLDEN, University of Edinburgh TAKU KOMURA, University of Edinburgh JUN SAITO, Method Studios

\*SIGGRAPH 2017

$$x_t = f(x_{t-1}; \mathbf{z_t})$$

$$z_t \rightarrow \begin{array}{c} \text{control parameters} \\ \text{phase parameter} \end{array}$$

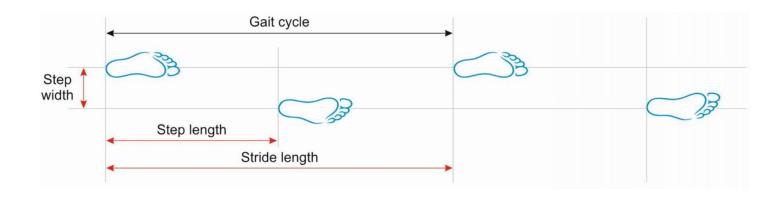




phases of a walking gait cycle

Pirker and Katzenschlager 2017. Gait disorders in adults and the elderly.

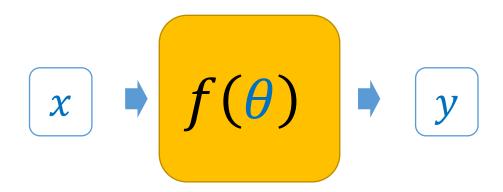
$$x_t = f(x_{t-1}; z_t) \qquad z_t = (c_t, \phi_t)$$



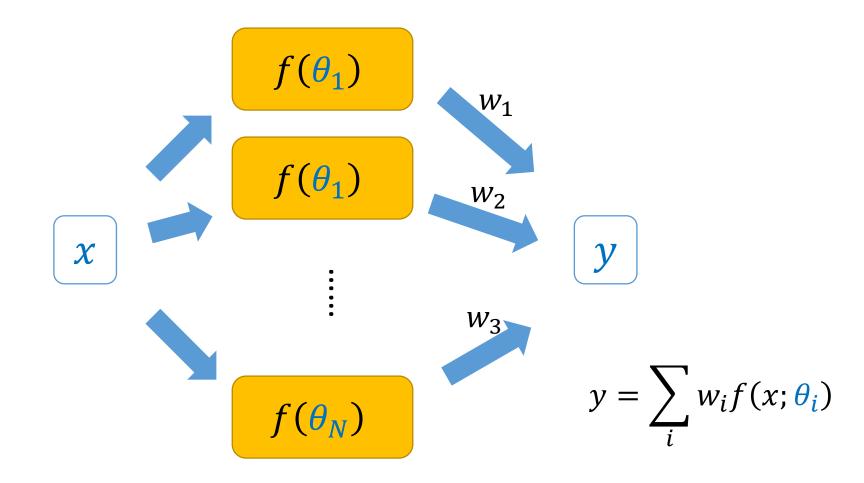
$$\phi = 0.0 \longrightarrow 0.5 \longrightarrow 1.0$$

$$0.0 \longrightarrow 0.5 \longrightarrow 1 \longrightarrow$$

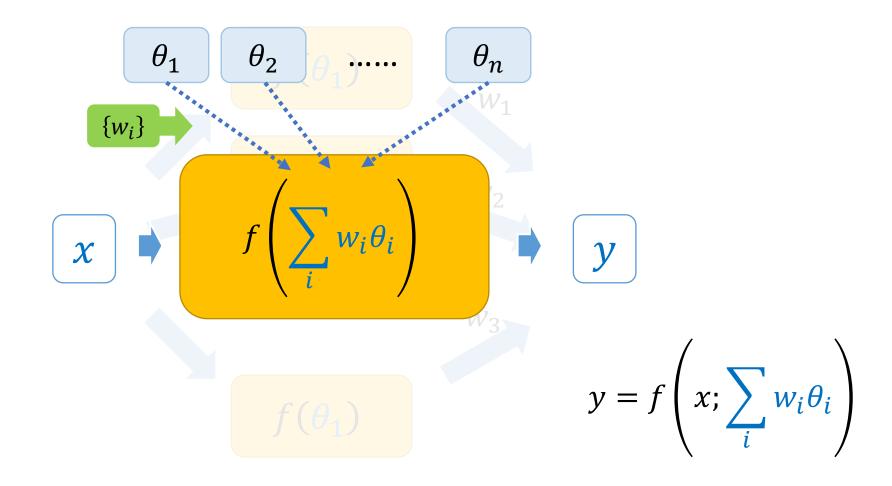
# Mixture of Experts



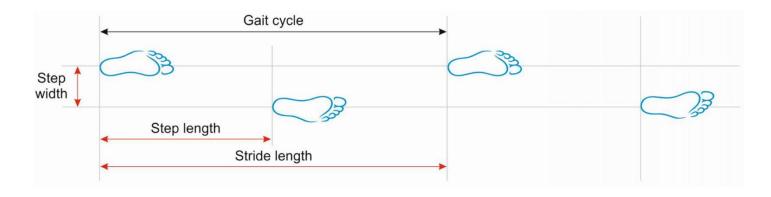
# Mixture of Experts



# Weighted-Blended Mixture of Experts



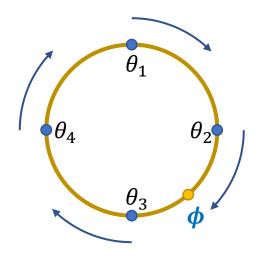
$$x_t = f\left(x_{t-1}; c_t, \theta_t = \sum_i w_i(\phi_t)\theta_i\right)$$



$$\phi = 0.0 \longrightarrow 0.5 \longrightarrow 1.0$$

$$0.0 \longrightarrow 0.5 \longrightarrow 1 \longrightarrow$$

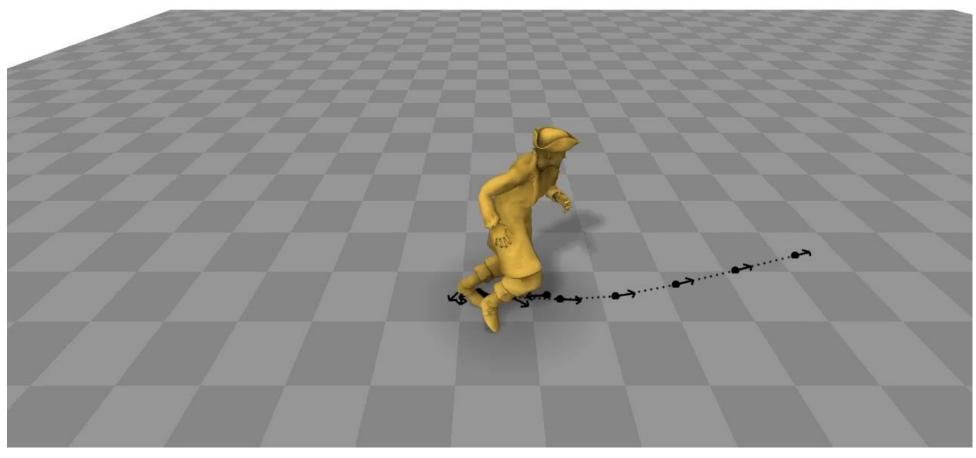
$$x_t = f\left(x_{t-1}; c_t, \theta_t = \sum_i w_i(\phi_t)\theta_i\right)$$



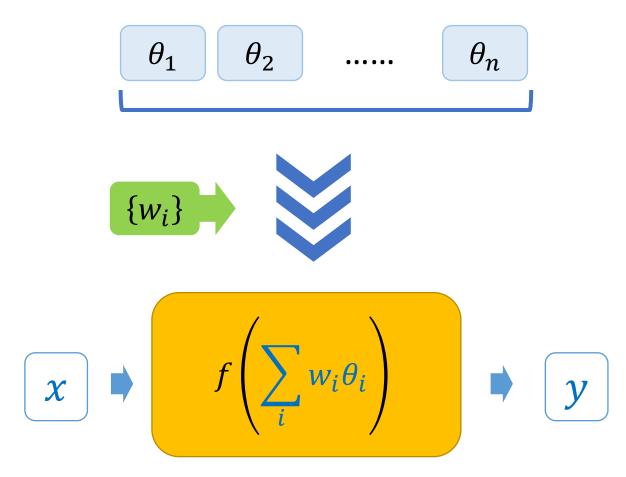
#### Cubic Catmull-Rom Spline:

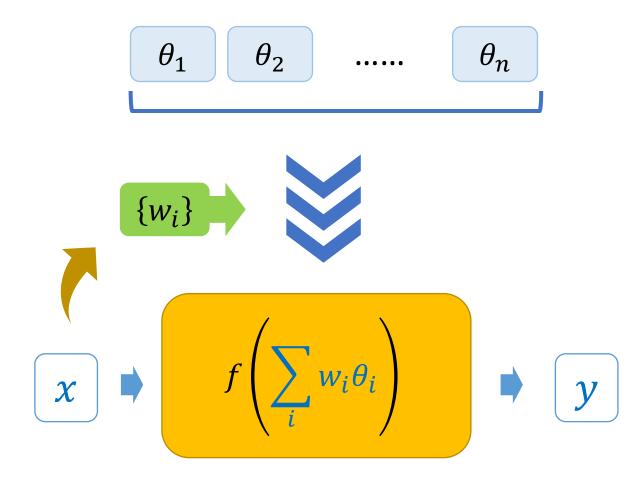
$$\begin{split} \theta_t &= \theta_2 \\ &+ \phi \left( -\frac{1}{2}\theta_1 + \frac{1}{2}\theta_3 \right) \\ &+ \phi^2 \left( \theta_1 - \frac{5}{2}\theta_2 + 2\theta_3 - \frac{1}{2}\theta_4 \right) \\ &+ \phi^3 \left( -\frac{1}{2}\theta_1 + \frac{3}{2}\theta_2 - \frac{3}{2}\theta_3 + \frac{1}{2}\theta_4 \right) \end{split}$$

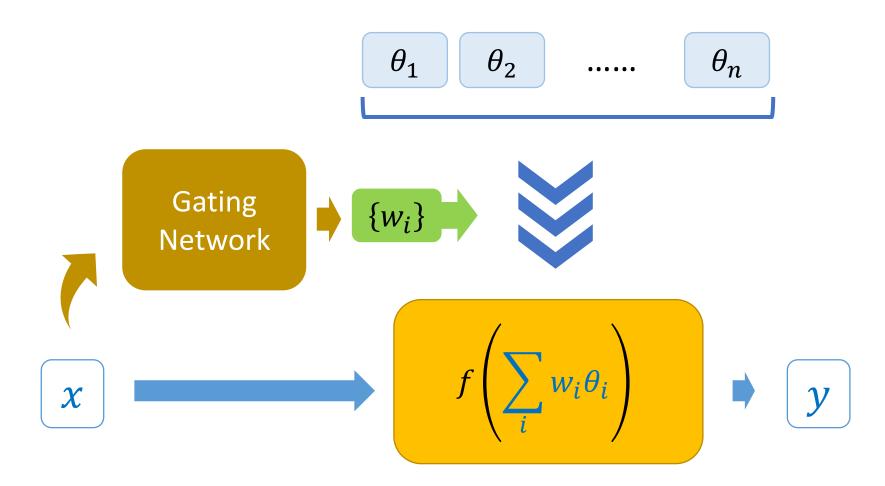


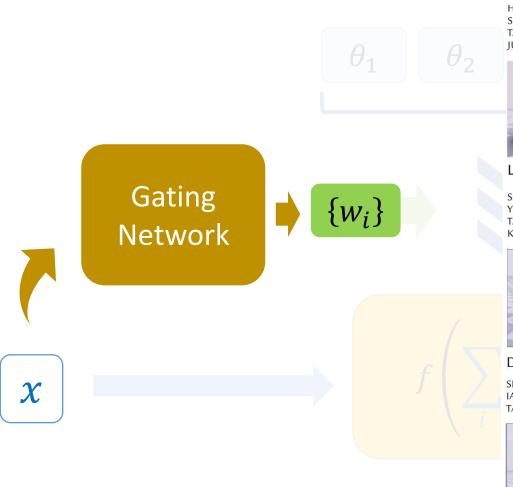


[Holden et al. 2017]









#### Mode-Adaptive Neural Networks for Quadruped Motion Control

HE ZHANG<sup>†</sup>, University of Edinburgh SEBASTIAN STARKE†, University of Edinburgh TAKU KOMURA, University of Edinburgh JUN SAITO, Adobe Research



\*SIGGRAPH 2018

#### Local Motion Phases for Learning Multi-Contact Character Movements

SEBASTIAN STARKE, University of Edinburgh, UK and Electronic Arts, USA YIWEI ZHAO, Electronic Arts, USA TAKU KOMURA, University of Edinburgh, UK KAZI ZAMAN, Electronic Arts, USA



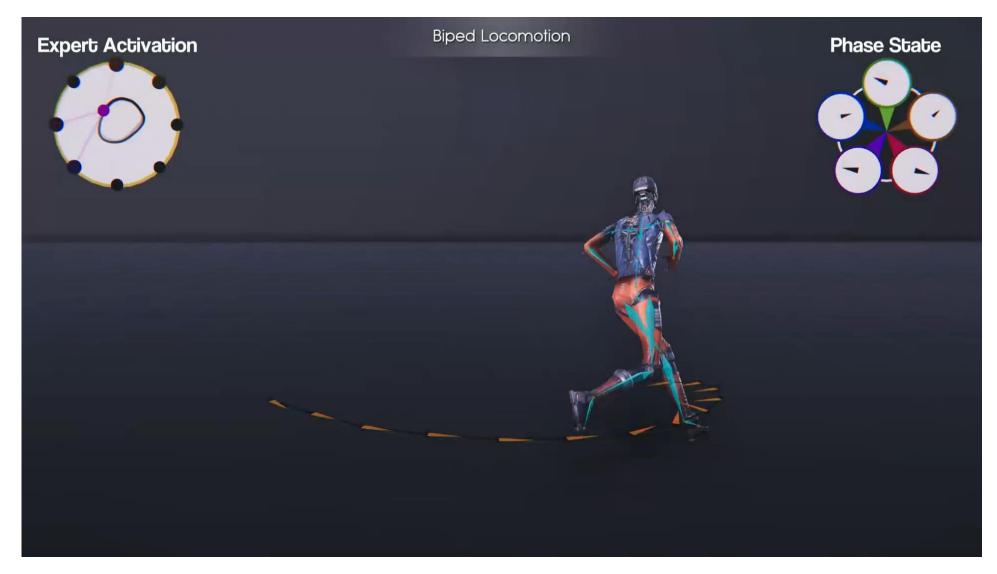
\*SIGGRAPH 2020

DeepPhase: Periodic Autoencoders for Learning Motion Phase Manifolds

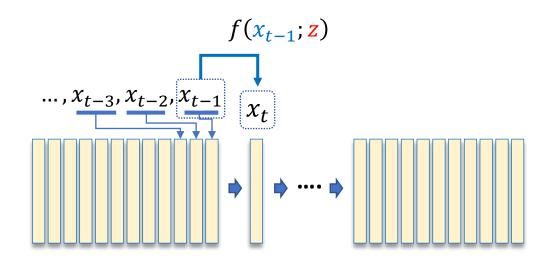
SEBASTIAN STARKE, The University of Edinburgh, UK and Electronic Arts, USA IAN MASON, The University of Edinburgh, UK TAKU KOMURA, The University of Hong Kong, Hong Kong



\*SIGGRAPH 2022



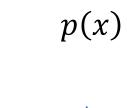
[Starke et al. 2022]

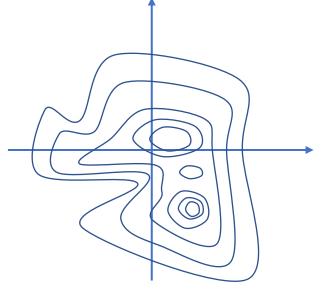


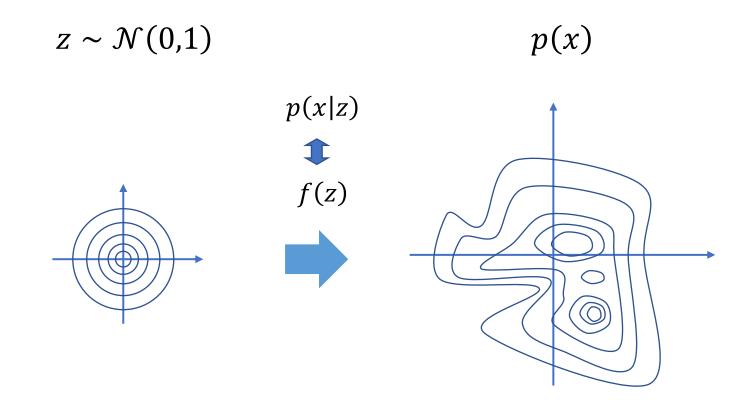
$$p(X|\mathbf{z}) = p(x_1, \dots, x_T|\mathbf{z})$$

$$= p(x_1) \prod_{t} p(x_t|x_{t-1};z)$$

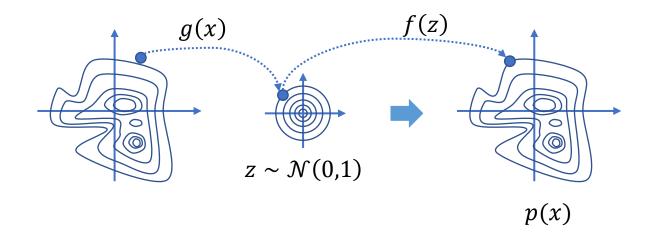




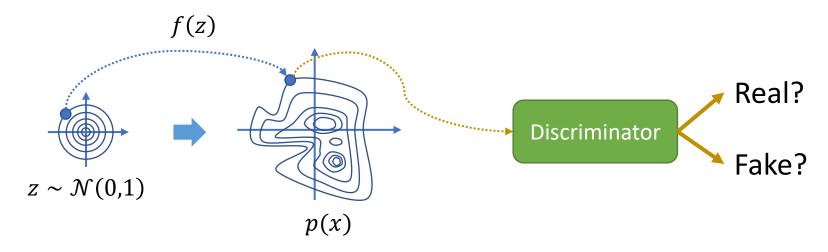


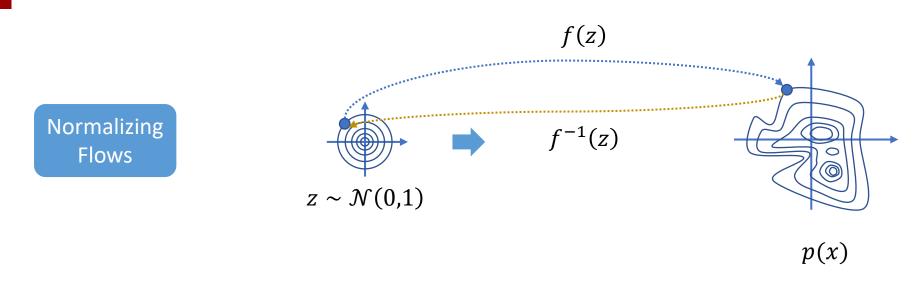


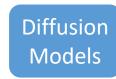
Variational Autoencoders

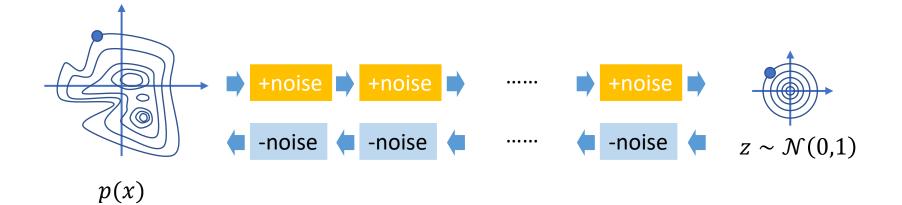


Generative Adversarial Network



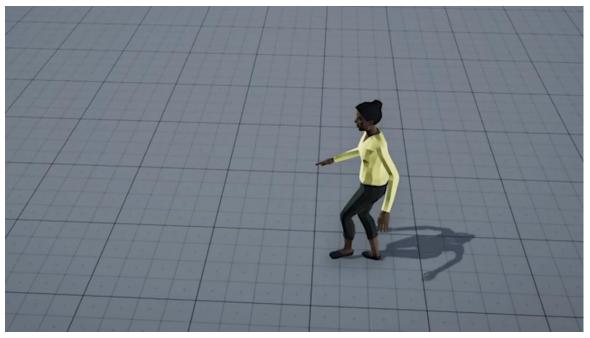




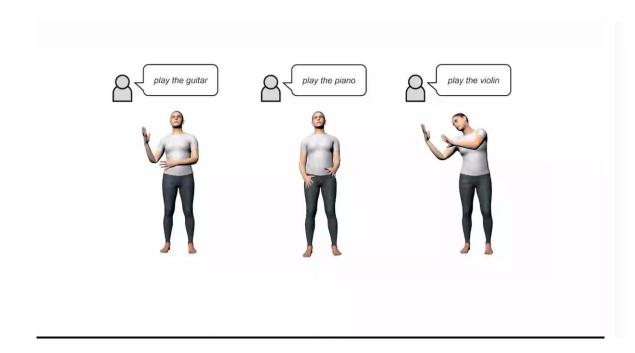


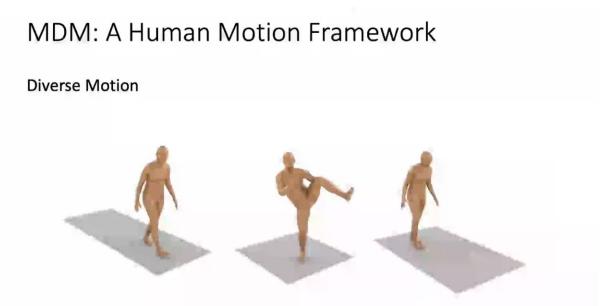


[Ling et al. 2021 Character Controllers Using Motion VAEs]



[Henter et al. 2020, MoGlow: Probabilistic and Controllable Motion Synthesis Using Normalising Flows]





[Zhang et al. 2022, arXiv, MotionDiffuse: Text-Driven Human Motion Generation with **Diffusion Model**]

[Tevet et al. 2022, arXiv, MDM: Human Motion Diffusion Model

## Outline

- Learning-based Character Animation (cont.)
  - Motion Models
  - Autoregressive models: PFNN
  - Generative models

# Questions?

