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1.Reverse number
def reverse_number(num, rev=0):
  if num == 0:
    return rev
  else:
    return reverse_number(num // 10, rev * 10 + num % 10)
num = 12345
print(reverse_number(num))
2.Perfect number
def is_perfect(n):
  sum_divisors = 0
  for i in range(1, n // 2 + 1):
    if n % i == 0:
      sum_divisors += i
  return sum_divisors == n
n = 28
print(is_perfect(n))
3.Demonstrate Usage of Big-O Notation
def constant_time(n):
  return n + 1
def linear_time(arr):
  total = 0
  for num in arr:
    total += num
  return total
def quadratic_time(arr):
  for i in range(len(arr)):
    for j in range(len(arr)):
      print(i, j)
print(constant_time(5))
print(linear_time([1, 2, 3, 4, 5]))
quadratic_time([1, 2, 3])
4. Mathematical Analysis of Non-Recursive and Recursive Algorithms
def linear_search(arr, target):
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for i in range(len(arr)):
    if arr[i] == target:
      return i
  return -1
def factorial(n):
  if n == 0 or n == 1:
    return 1
  else:
    return n * factorial(n - 1)
print(linear_search([1, 2, 3, 4, 5], 4))
print(factorial(5))
5. Solving Recurrence relations
def master_theorem(n):
  if n == 1:
    return 1
  return 2 * master_theorem(n // 2) + n
print(master_theorem(8))
def substitution_method(n):
  if n == 1:
    return 1
  return substitution_method(n - 1) + 1
print(substitution_method(5))
def iteration_method(n):
  if n == 1:
    return 1
  return 2 * iteration_method(n // 2) + n
6.Intersection unique
def intersection_unique(nums1, nums2):
  return list(set(nums1) & set(nums2))
nums1 = [1, 2, 2, 1]
nums2 = [2, 2]
print(intersection_unique(nums1, nums2))
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7.intersection multiset
def intersection_multiset(nums1, nums2):
  counts1 = Counter(nums1)
  counts2 = Counter(nums2)
  intersection = []
  for num in counts1:
    if num in counts2:
       intersection.extend([num] * min(counts1[num], counts2[num]))
  return intersection
nums1 = [1, 2, 2, 1]
nums2 = [2, 2]
print(intersection_multiset(nums1, nums2))
8.merge sort
def merge_sort(arr):
  if len(arr) > 1:
    mid = len(arr) // 2
    L = arr[:mid]
    R = arr[mid:]
    merge_sort(L)
    merge_sort(R)
    i = j = k = 0
    while i < len(L) and j < len(R):
      if L[i] < R[j]:
        arr[k] = L[i]
        i += 1
       else:
        arr[k] = R[j]
        j += 1
       k += 1
    while i < len(L):
      arr[k] = L[i]
      i += 1
      k += 1
    while j < len(R):
       arr[k] = R[j]
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j += 1
      k += 1
  return arr
nums = [5, 2, 3, 1]
print(merge_sort(nums))
9.sort\ half\_odd\ and\ half\_even
def sort_half_odd_half_even(nums):
 odd_index = 0
  even_index = 1
  n = len(nums)
  while odd_index < n and even_index < n:
    if nums[odd_index] % 2 == 0:
      while even_index < n and nums[even_index] % 2 == 0:
        even_index += 2
      if even_index < n:
        nums[odd_index], nums[even_index] = nums[even_index], nums[odd_index]
    odd_index += 2
  return nums
nums = [4, 1, 2, 3, 6, 7, 8, 5]
print(sort_half_odd_half_even(nums))
10.sorted array
def sort_array_by_parity(nums):
  odd_index = 1
  even_index = 0
  n = len(nums)
  while odd_index < n and even_index < n:
    if nums[even_index] % 2 == 0:
      even_index += 2
    elif nums[odd_index] % 2 == 1:
      odd_index += 2
    else:
     nums[even_index], nums[odd_index] = nums[odd_index], nums[even_index]
      even_index += 2
      odd index += 2
  return nums
nums = [4, 1, 2, 3, 6, 7, 8, 5]
print(sort_array_by_parity(nums))
```