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Sec → KRG 1-A

Q1 → Given the three integers m, a and b , find the n^{th} magical number.

A number X is magical if it is either divisible by a or b .

If answer is very large, return it modulo 10^{9+7} .

$$n=1, a=2, b=3$$

$$\text{ans} \rightarrow 2$$

$$n=4, a=2, b=3$$

$$\text{ans} \rightarrow 86$$

$$n \approx 10^9$$

Approach ↴

Binary search ↴

Lower limit of binary search $\rightarrow \min(a, b)$.

Upper limit of binary search $\rightarrow n \times \min(a, b)$.

of others $\times 0.6$,

If we want to find the number of multiples, from 2 to X ,
we can calculate it through ↴

$$\text{Number of multiples of } a \text{ or } b \text{ till } X \rightarrow \frac{X}{a} + \frac{X}{b} - \frac{X}{\text{lcm}(a,b)}$$

Calculate number of multiples at every mid and compare with n .
 \rightarrow Apply binary search accordingly.

```

using namespace std;

#define long ll long long

#define mod 1000000007

int solve(int n, int a, int b) {
    ll low = min(a, b);
    ll high = ll * n * min(a, b);
    ll lcm = ll (a * b) / -gcd(a, b);
    while (low < high) {
        ll mid = low + (high - low) / 2;
        ll cnt = mid / a + mid / b - mid / lcm;
        if (cnt < n) low = mid + 1;
        else high = mid;
    }
    return (low * 1L * mod);
}

int main() {
    int n, a, b;
    cin >> n >> a >> b;
    cout << solve(n, a, b) << endl;
}

```