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Sec → KRG-1-A

Q1 → Given the three integers m, a and b , find the n^{th} magical number.

A number x is magical if it is either divisible by a or b .

If answer is very large, return it modulo 20^9+7 .

$n=1, a=2, b=3$

ans → 2

$n=4, a=2, b=3$

ans → 86

$n \approx 10^9$

Approach ↴

Binary Search ↴

Lower limit of binary search → $\min(a, b)$.

max^m limit of binary search → $n \times \min(a, b)$.

If we want to find the number of multiples, ^{of either a or b ,} from 1 to x ,

we can calculate it through ↴

$$\begin{array}{l} \text{Number of multiples of} \\ a \text{ or } b \text{ till } x \end{array} \rightarrow \frac{x}{a} + \frac{x}{b} - \frac{x}{\text{lcm}(a, b)}$$

Calculate number of multiples at every mid and compare with n .
→ Apply binary search accordingly.

```
using namespace std;
```

```
#define long long long
```

```
#define mod 1000000007
```

```
int solve (int n, int a, int b) {
```

```
    ll low = min(a, b);
```

```
    ll high = 1LL * n * min(a, b);
```

```
    ll lcm = 1LL * (a * b) / __gcd(a, b);
```

```
    while (low < high) {
```

```
        ll mid = low +  $\frac{(high - low)}{2}$ ;
```

```
        ll cnt =  $\frac{mid}{a} + \frac{mid}{b} - \frac{mid}{lcm}$ ;
```

```
        if (cnt < n) { low = mid + 1;
```

```
            else high = mid;
```

```
    }
```

```
    return (low * 1LL * mod);
```

```
}
```

```
int main() {
```

```
    int n, a, b;
```

```
    cin >> n >> a >> b;
```

```
    cout << solve(n, a, b) << endl;
```

```
}
```