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# Problem H. How many inversions?

Input: standard Output: standard

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Humbertov Moralov in his student days, he is attended system engineering at "University of missing hill". He was evaluated in its first course of Analysis of Algorithms (at the first half of 1997) with the following topics and questions:

#### Inversions:

Let A[1 ... n] an array of distinct integers of size n. If i < j and A[i] > A[j], then the pair (i, j) is called an **inversion** of A.

Given the above definition about an inversion, *Humbertov Moralov* must answer the following questions:

- 1. List all inversions in (3, 2, 8, 1, 6).
- 2. What array of size n, with all the numbers from the set  $1, 2, 3, \ldots, n$  has the largest amount of inversions? How many inversions?
- 3. Write an algorithm to determine the number of inversions in any permutation of n elements with  $\theta(n \log n)$  in the worst case run time.

Humbertov Moralov answered questions 1. and 2. without any problem, but he was not able to solve the question 3 at time. Days later he thought the following solution:

```
1: inv \leftarrow 0
 2: function Merge(A[], p, q, r)
         n_1 \leftarrow q - p + 1
 3:
         n_2 \leftarrow r - q
 4:
         create arrays L[1 ... n_1 + 1] and R[1 ... n_2 + 1]
 5:
 6:
         for i = 1 to n_1 do
              L[i] \leftarrow A[p+i-1]
 7:
         end for
 8:
         for j = 1 to n_2 do
 9:
              R[j] \leftarrow A[q+j]
10:
11:
         end for
         L[n_1+1] \leftarrow \infty
12:
         R[n_2+1] \leftarrow \infty
13:
         i \leftarrow 1
14:
         j \leftarrow 1
15:
16:
         for k = p to r do
              if L[i] \leq R[j] then
17:
                  A[k] \leftarrow L[i]
18:
                  i \leftarrow i + 1
19:
20:
                   A[k] \leftarrow R[j]
21:
22:
                  j \leftarrow j + 1
```

```
\mathbf{inv} \leftarrow \mathbf{inv} + \mathbf{n_1} - \mathbf{i} + \mathbf{1}
23:
             end if
24:
        end for
25:
26: end function
27: function MergeSort(A[], p, r)
        if p < r then
28:
             q \leftarrow \lfloor (p+r)/2 \rfloor
29:
             MERGESORT(A[], p, q)
30:
             MERGESORT(A[], q + 1, r)
31:
             MERGE(A[], p, q, r)
32:
33:
        end if
34: end function
```

Will this code solve the problem? Just adding the lines 1 and 23 will be enough to solve the problem?

Please help *Humbertov Moralov* to validate this solution! For this, you must implement this solution in any of the programming languages accepted by the ACM-ICPC and verify if the expected results are generated.

#### Input

The input may contain several test cases. Each input case begins with a positive integer n  $(1 \le n \le 10^6)$  denoting the length of A, followed by n distinct lines. Each line contains a positive integer from array A. For  $i \in [1, n]$ , will meet that  $0 \le A[i] \le 10^8$ . The input ends with a test case in which n is zero, and this case must not be processed.

### Output

For each test case, your program must print a positive integer representing the total number of inversions in the array A. Each valid test case must generate just one output line.

## Example

Input	Output
5	5
3	10
2	0
8	
1	
6	
5	
5	
4	
3	
2	
1	
1	
10	
0	

Use faster I/O methods