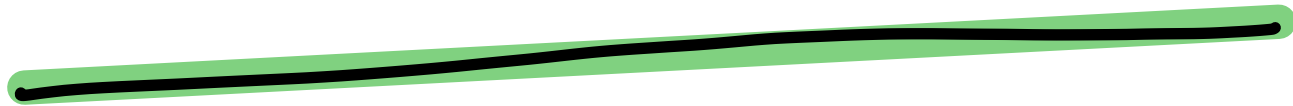




# CENTRAL LIMIT THEOREM

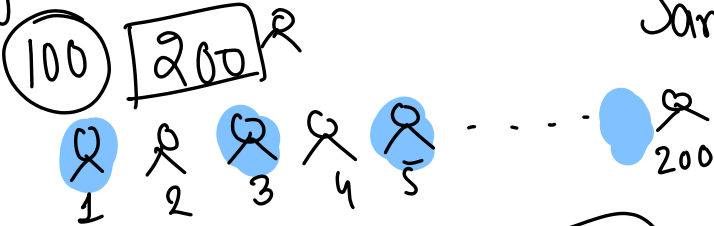


- ① CLT  $\rightarrow$  (Today)
- ② CI  $\rightarrow$  Confidence Interval (Next)

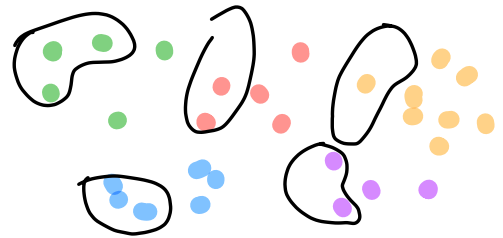
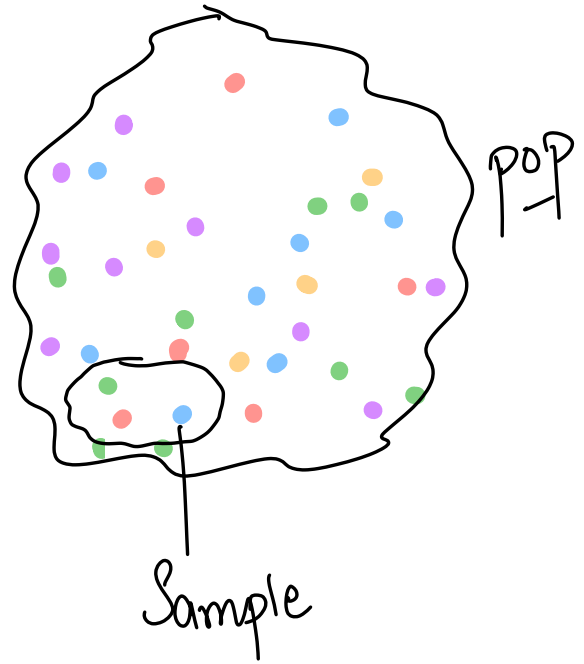
## Sampling Techniques

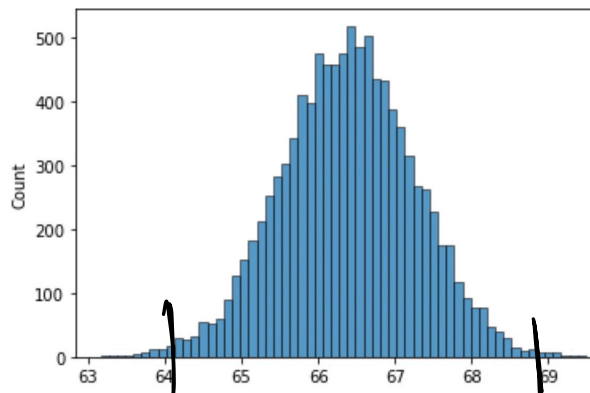
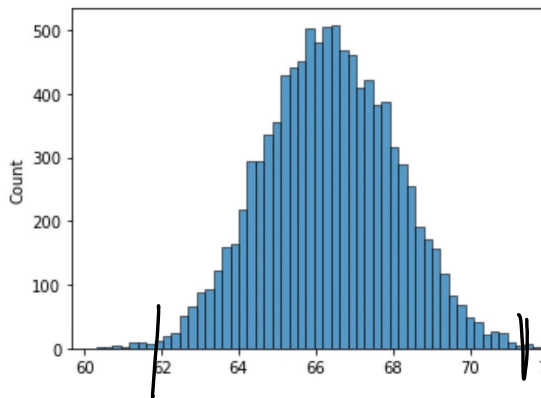
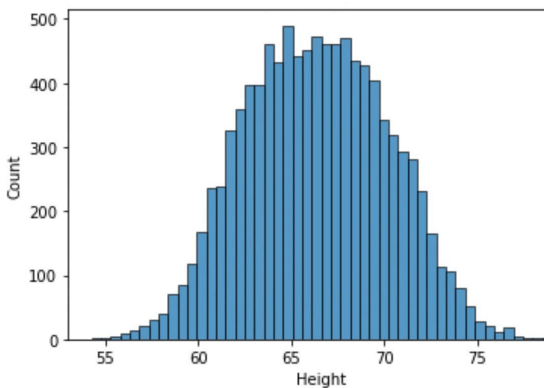
① Random Sampling

② Systematic Sampling



③ Stratified Sampling  
Cluster based Sampling





Normal Distribution

Sample size = 5

$\mu = 66.34$

$\sigma_5 = 1.709$

Sample size = 20

$\mu = 66.38$

$\sigma_{20} = 0.849$

$\mu = 66.36$   
 $\sigma = 3.8475$

$\sigma > \sigma_5 > \sigma_{20}$

# Central Limit Theorem

If "n" denotes sample size

& "σ" denotes population standard deviation

$\left\{ \begin{array}{l} n=5 \\ n=10 \\ 20 \\ 30 \\ \vdots \end{array} \right\}$

then Standard deviation of distribution of sampling means

$$\sigma = \frac{\sigma}{\sqrt{n}}$$

AKA

"Standard Error"

$$\bar{X} = \frac{X_1 + X_2 + X_3 + X_4 + X_5 + \dots + X_n}{n}$$

$\bar{X}$  is  
Random  
Variable.

↳ deriving sample means (RV)

$\bar{X}$  follow Gaussian Distribution  
Normal Distribution

• Mean / Expectation  $E[\bar{X}] = \mu$

• Std of  $\bar{X} = \frac{\sigma}{\sqrt{n}}$

$$\bar{X} \sim N\left(\mu, \frac{\sigma}{\sqrt{n}}\right)$$

$$n > 30$$

\* If our original pop<sup>n</sup> is normally distributed.

$n$  doesn't matter

$$n=1$$

$$n=2$$

$$\bar{X} \sim N$$

$$\bar{X} \sim N$$

Z test  $\rightarrow n > 30$

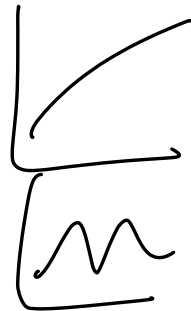
t test  $\rightarrow n < 30$

$\hookrightarrow$  t student's distribution

\* If our original pop<sup>n</sup> is not normally distributed.

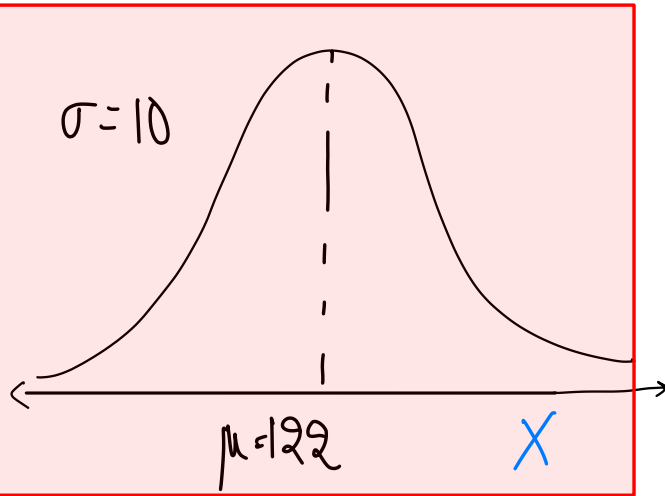
$$\bar{X} \sim N$$

$$n > 30$$



Systolic blood pressure of a group of people is known to have an average of 122 mmHg and a standard deviation of 10 mmHg

Calculate the probability that the average blood pressure of 16 people will be greater than 125 mmHg.

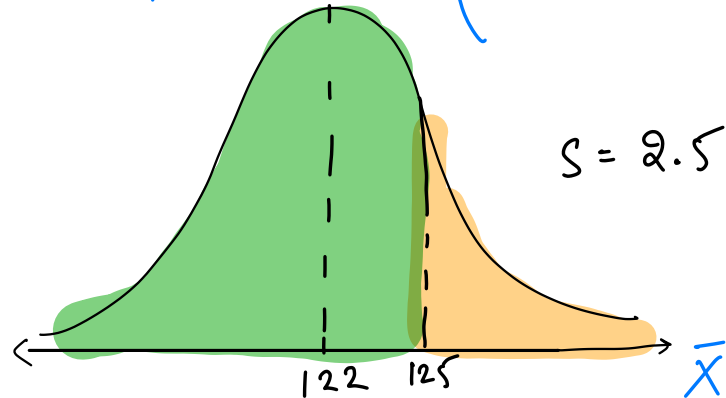


$$P[X > 125] = 1 - \underbrace{P[X < 125]}_{\text{norm.cdf}(z \text{ score})}$$

$$\bar{X} \sim N\left(\mu, \frac{\sigma}{\sqrt{n}}\right) \quad n=16$$

*sample mean*

$$\bar{X} \sim N(122, 2.5)$$





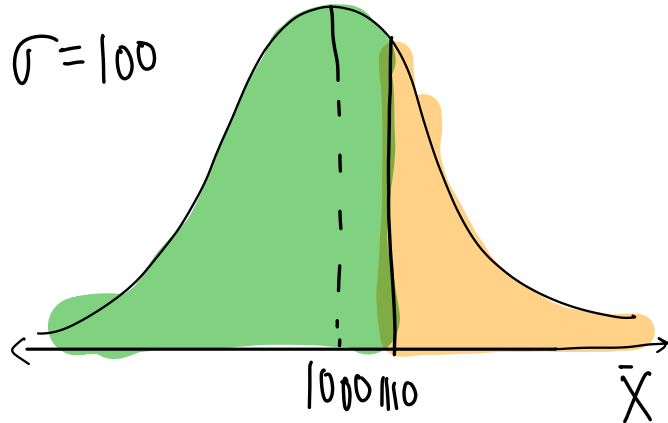
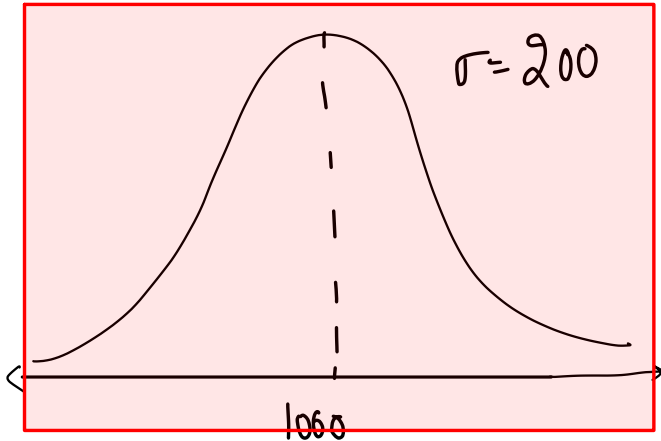
Weekly toothpaste sales have a mean 1000 and std dev 200. What is the probability that the average weekly sales next month is more than 1110?

32 users have participated

A	0.29	28%
<input checked="" type="radio"/> B	0.13	41%
C	0.11	22%
D	0.08	9%

$$\bar{X} = \frac{X_1 + X_2 + X_3 + X_4}{4} \quad \hookrightarrow n=4$$

$$\bar{X} \sim N\left(1000, \frac{200}{\sqrt{4}}\right)$$



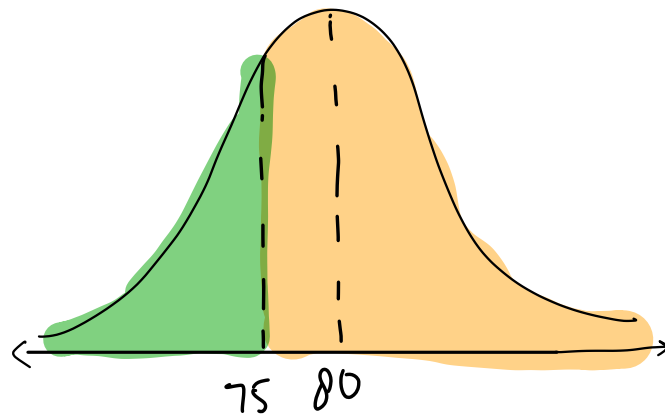
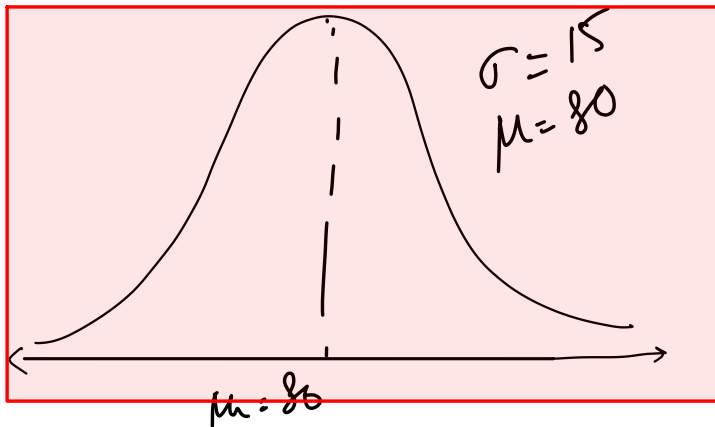
In an e-commerce website, the average purchase amount per customer is \$80 with a standard deviation of \$15. If we randomly select a sample of 50 customers, what is the probability that the average purchase amount in the sample will be less than \$75?

23 users have participated

A	0.36	13%
B	0.18	30%
C	0.01	13%
<input checked="" type="checkbox"/> D	0.009	43% ✓

$$\bar{X} \sim N\left(80, \frac{15}{\sqrt{50}}\right) \quad n = 50$$

$$0.009$$



Adapt

Manual

↳ ML (1)

↳ DL NN

