

ANOVA

a :	[25 25 27 30 23 20]	$\mu_A = 25$	H_0 : No difference $\mu_1 = \mu_2 = \mu_3$
b :	[30 30 21 24 26 28]	$\mu_B = 26.5$	
c :	[18 30 29 29 24 26]	$\mu_C = 26$	

H_a : At least 1 is different
 $\mu_1 \neq \mu_2 \neq \mu_3$

Step 1 . Compute individual grps means .

Step 2 : Compute means of means of grps .

$$\bar{m} = \frac{\mu_A + \mu_B + \mu_C}{3} = \frac{25 + 26.5 + 26}{3} = 25.83$$

a	:	[25 25 27 30 23 20]	$\mu_A = 25$
b	:	[30 30 21 24 26 28]	$\mu_B = 26.5$
c	:	[18 30 29 29 24 26]	$\mu_C = 26$

Step 3: compute variance
b/w groups.

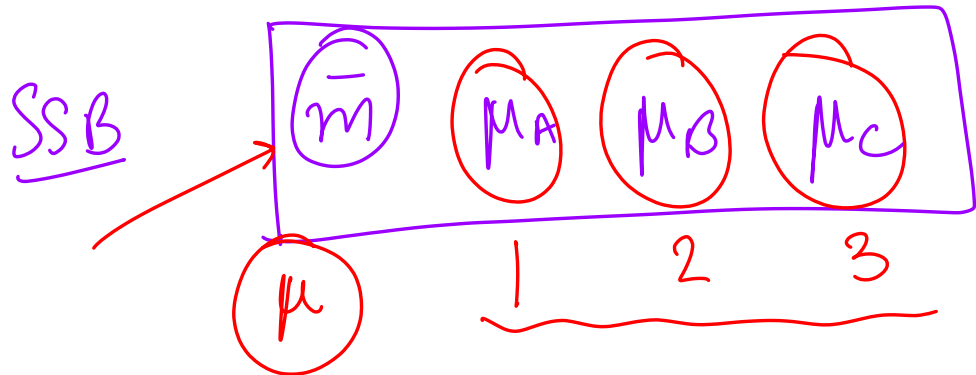
SSB. Sum of squares between

$$\sum n_i (\mu_i - \bar{m})^2$$

$$= 6(25 - 25.83)^2 + 6(26.5 - 25.83)^2 + 6(26 - 25.83)^2$$

$$= 7.0002$$

$$\text{DOF}_B = 2$$



Step 4:

MSB

Mean Sum of Squared between groups

$$MSB = \frac{SSB}{DOF_B} = 3.501$$

$$MSW = \frac{SSW}{DOF_W} = \frac{223.5}{15} = 14.9$$

Mean of Sum of Squared within groups.

a : [25 25 27 30 23 20] $\mu_A = 25$
b : [30 30 21 24 26 28] $\mu_B = 26.5$
c : [18 30 29 29 24 26] $\mu_C = 26$

Step 5 = Compute variance within groups.

SSW: Sum of Squared within group.

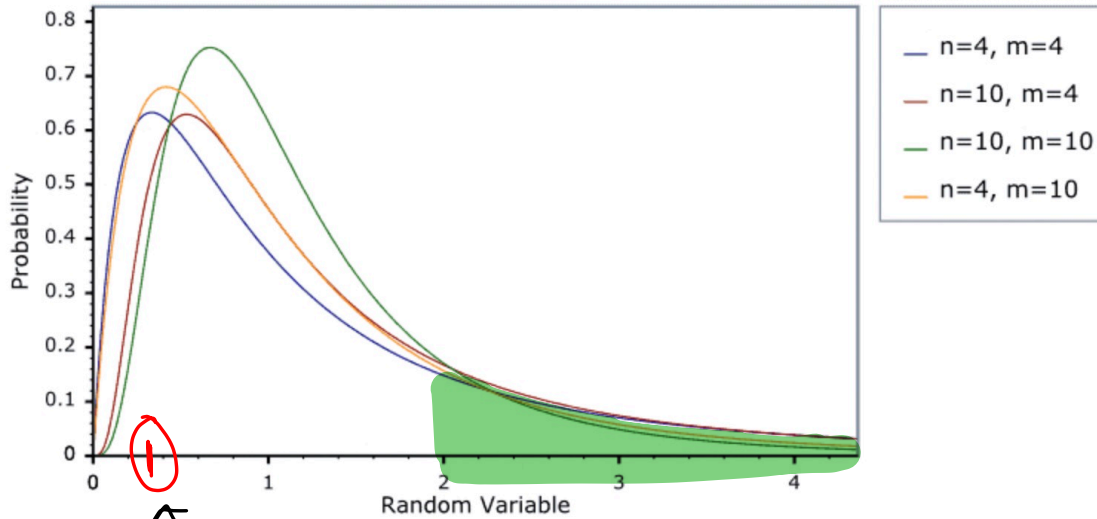
$$\begin{aligned}
 & (25 - 25)^2 + (25 - 25)^2 + \dots + (20 - 25)^2 \quad \left. \begin{array}{l} \text{A} \\ \text{B} \\ \text{C} \end{array} \right\} (x_i - \mu_i)^2 \\
 & (30 - 26.5)^2 + (30 - 26.5)^2 + \dots + (28 - 26.5)^2 \\
 & (18 - 26)^2 + (30 - 26)^2 + \dots + (26 - 26)^2
 \end{aligned}
 \rightarrow \text{SSW}$$

223.5

$$DOF_w = 15$$

$$F_{ratio} = \frac{\text{Variance b/w groups}}{\text{Variance within groups}} = \frac{MSB}{MSW}$$
$$= \frac{3.501}{14.9} = 0.2348$$

F Distribution PDF

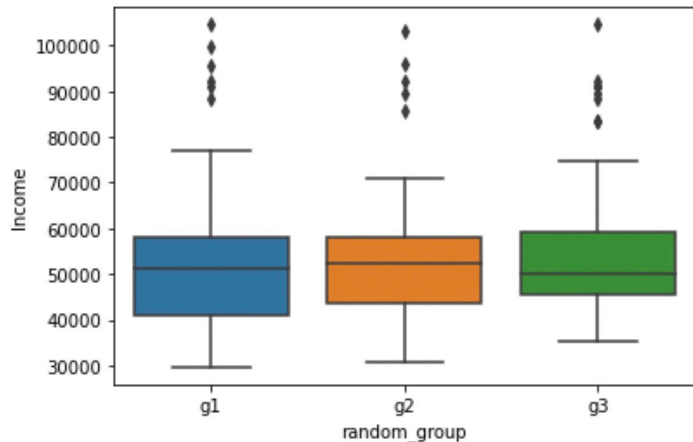


Right tailed
Test

$$F_{ratio} = 0.2348$$

$$p_{value} = 1 - f.cdf(0.2348, df_{\text{between}} = 2, df_{\text{within}} = 15)$$

①

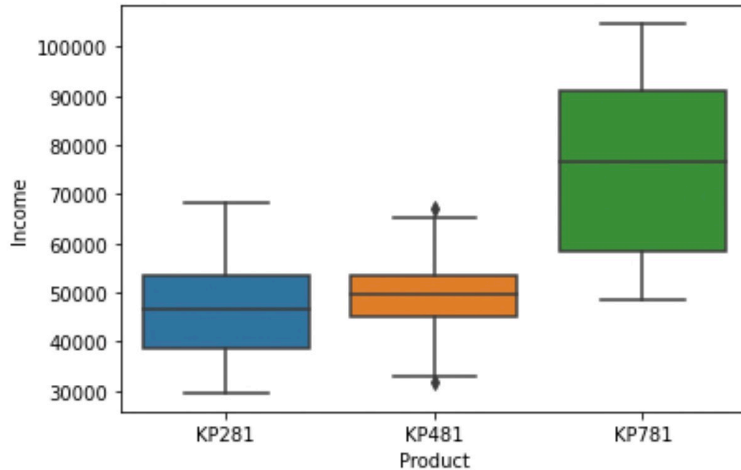


Similar / H_0 /

$H_0 = \mu_1 = \mu_2 = \mu_3$ (Groups are similar)

$H_a = \mu_1 \neq \mu_2 \neq \mu_3$ (" " not similar)

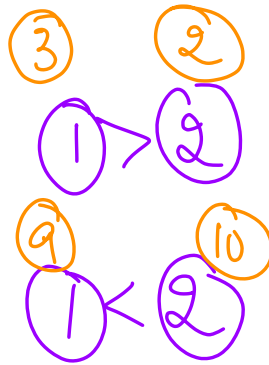
②



Different / H_a /

Variance within groups.

Variance b/w groups



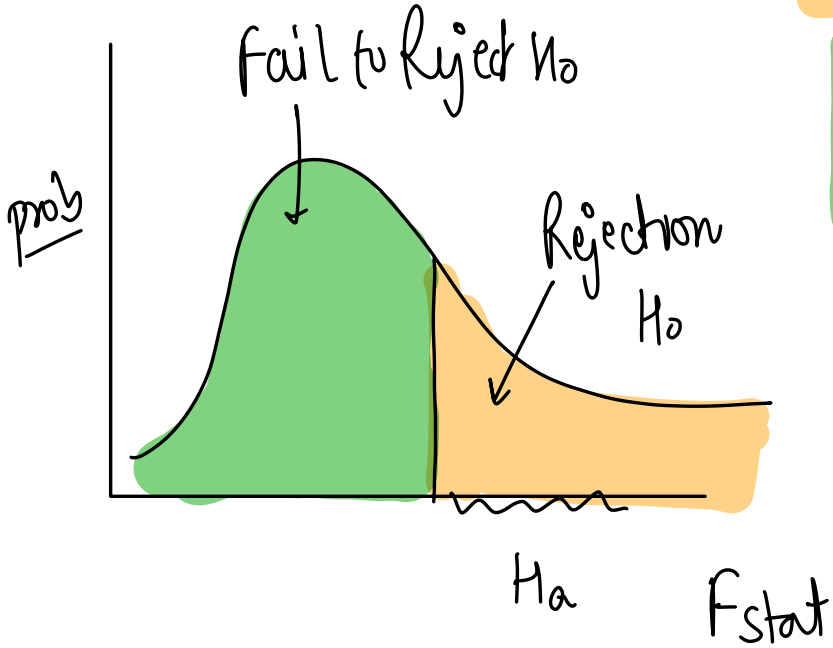
Fratio: $\frac{b/w}{\text{Within}}$

$$\text{Fratio} = \frac{10}{2} = 5$$

(2nd) H_a

$$\text{Fratio} = \frac{9}{3} = 3$$

1st setup H_0



Right tailed test

ASSUMPTIONS

- ① Data should be Gaussian
 - ② Independent.
 - ③ Equal Variances among diff group.
- Visualise
→ Q Q Plot
- Test
→ Wilkin Shapiro Test
- Levene Test

If these condⁿ are not met / don't hold true









KRUSKAL'S TEST

Next Class

① Gaussian \rightarrow Test \leftarrow ECDFs

② Gaussian \rightarrow QQ Plot

③ Business Understanding of ANOVA \rightarrow Feature Engineering

	1	2	3	
A				
B				
C				
				

$$\begin{aligned}
 &(n-1)(m-1) \\
 &= (3-1)(2-1) \\
 &= 2 \times 1
 \end{aligned}$$

$$\begin{aligned}
 H_0 &= \mu_1 = \mu_2 \\
 H_a &=
 \end{aligned}$$

t-test - rel →

Inter
Rejection

$H_0 : \mu_1 = \mu_2$
 $H_a :$
~~Session had no effect~~
~~Rejection had no effect~~

Amazon

X_1

