Hopfield Networks in C++

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1 Hopfield Networks in C++	1
1.1 Introduction	1
1.2 Theoretical Background	1
2 Hopfield Networks in C++: Requirements and Installation instructions	5
2.1 Requirements	5
2.2 Installation	5
2.3 Running the example and tests	5
3 Class Documentation	7
3.1 HopfieldNetwork Class Reference	7
3.1.1 Constructor & Destructor Documentation	7
<b>3.1.1.1 HopfieldNetwork()</b> [1/2]	8
<b>3.1.1.2 HopfieldNetwork()</b> [2/2]	8
3.1.1.3 ~HopfieldNetwork()	8
3.1.2 Member Function Documentation	8
3.1.2.1 build_random_patterns()	8
3.1.2.2 build_weights()	8
3.1.2.3 cur_overlap()	9
3.1.2.4 get_alpha()	9
3.1.2.5 get_Energy() [1/2]	9
3.1.2.6 get_Energy() [2/2]	9
3.1.2.7 get_M()	9
3.1.2.8 get_N()	9
3.1.2.9 get_T()	9
3.1.2.10 glauber_evolve()	10
<b>3.1.2.11</b> init_on_corrupted_pattern() [1/2]	10
<b>3.1.2.12</b> init_on_corrupted_pattern() [2/2]	10
3.1.2.13 init_spins_randomly()	10
3.1.2.14 max_overlap()	10
3.1.2.15 overlaps()	10
3.1.2.16 push_back_pattern()	11
3.1.2.17 set_alpha()	11
3.1.2.18 set_M()	11
3.1.2.19 set_temperature()	11
4 File Documentation	13
4.1 source/HopfieldNetwork.h File Reference	13
4.1.1 Detailed Description	14
4.1.2 Macro Definition Documentation	14
4.1.2.1 N_PARALLEL_THREADS	14
4.1.3 Function Documentation	14
4.1.3.1 overlap()	14

	4.1.3.2 random_spin()	 		14						
4.2 Hopfield	dNetwork.h	 		15						
Bibliography										19
Index										21

### **Chapter 1**

## Hopfield Networks in C++

#### 1.1 Introduction

This header-only library implements a Hopfield Network in C++, aiming for a lightweight implementation that makes use of parallelism whenever possible. The time evolution is performed according to a parallel version of the conventional Glauber algorithm. Albeit being quite simple in its definition, the Hopfield Model can be regarded as a minimal version of a recurrent neural network implementing an associative, content addressed memory. Moreover, the study of the properties of the model in the presence of noise can be carried out in the framework of Statistical Physics, thus providing a paradigmatic example of the physical properties of a disordered system.

The implementation of parallel procedures is achieved via the OpenMP #pragma directives, so to exploit a secure and complete interface to the parallel features of C++. The default number of parallel threads can be set at compile time, so to meet the specifics of the available architecture, while for some methods also runtime specification is made possible, as detailed in the following documentation.

#### 1.2 Theoretical Background

The Hopfield Model or Hopfield Network is a very simple model for an associative memory. First put forward by William Little in 1974 and then developed by John Hopfield, it was devised to explain in a simplified context, the associative nature of memory in the brain, e.g. the fact that the recognition of an object can be triggered also by a partial or modified version of the memory itself. The model is very simplistic from the point of view of biological realism, the neurons being represented by McCulloch-Pitts binary units, which can only be in one of two states: +1, active or -1, inactive. Considering discretised units of time, each corresponding ideally to the average refractory period of a biological neuron, and representing the internal state of neuron i at time instant t as  $\sigma_i^t$ , the McCulloch-Pitts update rule for each neuron in a network containing N is defined as

$$\sigma_i^{t+1} = \operatorname{sgn}\left(\sum_{j=1}^N W_{ij}\sigma_j^t\right)$$

where the  $W_{ij}$  are called the synaptic weights, and  $\operatorname{sgn}$  is the sign function. The choice of which, and how many, spins to update per time unit is part of the implementation, as in general the details tend not to affect the final equilibrium state.

To have the Network work as an associative memory we need to store into it a number p of memories, in the form of spin patterns. The idea is that an associative memory, if put in a configuration close to one of the stored patterns

(e.g. a corrupted version of it), should reconstruct it during its time evolution, i.e. relax to a configuration  $\vec{\sigma}$  of the spins equal to the closest stored pattern.

To do so, with the previously defined dynamics, it can be proved that it is sufficient to define the weights  $W_{ij}$  as follows. Letting the patterns  $\xi_i^\mu$  be indexed by a greek index such as  $1 \le \mu \le p$  and the spins within each pattern with a regular latin index such as  $1 \le i \le N$ , we define the  $W_{ij}$  as

$$W_{ij} = \frac{1}{N} \sum_{\mu=1}^{p} \xi_{i}^{\mu} \xi_{j}^{\mu}$$

This choice of weights is called *Hebbian rule*, from the connectionist psychologist Donald Hebb, and it is generally summarised by the phrase *fire together*, *bind together*, meaning that the synapses connecting neurons which activate together are reinforced, while those connecting neurons that seldom fire together are weakened.

It can be proved [1] that under very simple hypotheses (symmetric weights), that the function

$$\mathcal{H}(\sigma) = -\frac{1}{2} \sum_{i=1}^{N} W_{ij} \sigma_i \sigma_j$$

, \* is a Lyapunov function (i.e. non-decreasing along the system's orbits) for the deterministic dynamics. From a physicist's viewpoint, we are saying that the deterministic dynamics tends to minimise a Ising-like spin Hamiltonian.

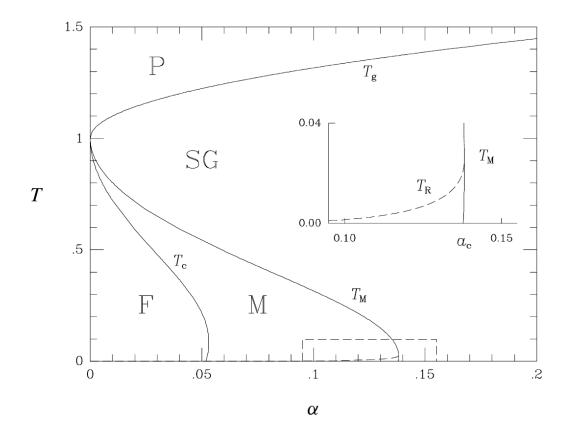
It can be proved similarly [1], that the deterministic dynamics can lead the network into spurious minima, i. $\leftarrow$  e. minima which correspond to the combination of a finite number of memories, *spurious mixtures*, or even an extensive number of memories, *glassy states* (Of course to access this kind of states it is necessary to have an extensive number of available memories, i.e. we need to have the scaling  $p = \alpha N$ ).

To avoid these states, or to render them unstable (repulsive) equilibria, we can introduce a stochastic dynamics into the system. A sensible choice would be to introduce a temperature and select a dynamics which is compatible with the Boltzmann-Gibbs equilibrium distribution induced by the spin Hamiltonian, this way we have a natural parametrisation for the noise level and can employ the machinery of Statistical Physics to characterise the macroscopic states of the system. To do so, we can select as update rule any method from the Monte Carlo techniques applied to spin systems. We choose *Glauber dynamics*, which amount to selecting a spin at random and flipping it with probability

$$\mathbb{P}(\sigma_i \to -\sigma_i) = \frac{1}{1 + e^{\beta \Delta \mathcal{H}_i}}$$

where by  $\Delta \mathcal{H}_i = 2 \sum_j W_{ij} \sigma_j \sigma_i$  we denote the energy change caused by a flip of spin *i*.

This dynamics is compatible with the Boltzmann-Gibbs equilibrium distribution and so we can set out to determine the phase diagram of the model using the tools of Statistical Physics. In particular we are interested in the case in which the number of patterns is extensive with N, so  $p=\alpha N$ , and we want to characterise the working features of the network as an associative memory in function of the noise level (temperature) T and the load parameter  $\alpha$ . The Statistical Mechanical treatment of the problem is very interesting and makes use of Replica Methods to deal with the *quenched disorder* brought on by the distribution of the memories. The resulting phase diagram is presented in the figure below (from [1]).

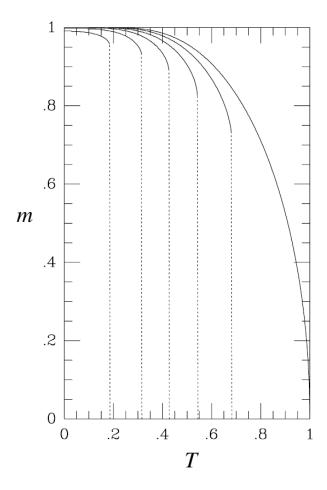


The different phases correspond to the case in which the recall states are absolute minima of the system free energy (F), local minima (M) or neither, due to the glassy nature of the free energy landscape (SG). The P phase corresponds to a paramagnetic fully disordered phase. The regions in which the network is considered to be working as an associative memory are F and M, since provided that the initial state is not too corrupted, the network will reconstruct the original pattern with its dynamics. To measure this property the pattern overlaps (also known as Mattis magnetisations) are introduced, the overlap between spin configuration  $\sigma$  and pattern  $\xi^{\mu}$  being defined as

$$m^{\mu}(\sigma) = \frac{1}{N} \sum_{i=1}^{N} \sigma_i \xi_i^{\mu}$$

where if the  $\sigma$  is omitted it is implied that the overlap is to be taken with the current spin state of the network.

Recall states, also known as pure states, correspond to a value of the appropriate  $m^\mu=1$ , and with a pure state ansatz one can obtain a self consistent equation for the amplitude  $m^\mu$  as a function of  $T,\,\alpha$ , yielding the following plot (from [1])



Where the various lines correspond, from top to bottom, to values of  $\alpha=0,\ldots,\,0.125$  in increments of 0.025, and dashed lines indicate the vanishing temperature for the amplitude at the given  $\alpha$ .

By inspecting the graph we can clearly see that for low levels of noise the Network has recalls very close to 1, thus proving that an amount of noise can be beneficial in Network operation by allowing it to better explore its configuration space, but without detriment to the quality of its functioning.

## **Chapter 2**

# Hopfield Networks in C++: Requirements and Installation instructions

#### 2.1 Requirements

To use the class implemented in this header it is necessary to have a compiler with support for C++ standard 2011 and OpenMP.

Most compilers come already equipped with these features, in particular no installing of further packages was required during development and testing, on Ubuntu 20.04 using g++ version 9.4.0.

For more information and full documentation please refer to the Manual.

#### 2.2 Installation

To be able to instantiate <code>HopfieldNetwork</code> objects as implemented in this project, you will need to copy the header file to a directory of your convenience, and <code>#include</code> it in your programs according to the usual inclusion rules of C++.

Then compile the project with

```
g++ my_program.C -fopenmp -DN_PARALLEL_THREADS=N -Ofast -o my_program.out
```

where  ${\tt N}$  should be the desired default number of parallel threads to use in parallel code sections.

#### 2.3 Running the example and tests

To run the example and the tests, please create a <code>Hopfieldcpp/build</code> directory first. The example program and the tests can be compiled by navigating to <code>Hopfieldcpp/source/</code> and launching

```
cmake -D N_PARALLEL_THREADS=N CMakeLists.txt
```

where N should be the desired default number of parallel threads to use in parallel code sections (N defaults to the result of the nproc command in absence of the -D option).

The output of cmake should follow, after that pass make to build the example or make test to run the automated tests

The example program can be run by passing ./build/example from the Hopfieldcpp directory.

The example program consists of a program that calculates the pure state amplitude graph, it has the following calling signature

```
./example N_spins alpha T_lower_bound T_upper_bound T_steps measurements_← per_step iterations_per_measurement output_filepath (optional)
```

and produces a table to standard output, and if output\_filepath is specified, to file.

Notice that since the repeated measurements at each temperature step are performed using the different patterns in a given network instance, it is necessary that  $measurements\_per\_step <= M = round(alpha * N)$ , otherwise an exception is raised to avoid a segmentation violation.

## **Chapter 3**

## **Class Documentation**

#### 3.1 HopfieldNetwork Class Reference

#### **Public Member Functions**

- HopfieldNetwork (int \_N, int \_M, double \_T)
- HopfieldNetwork (int \_N, double \_alpha, double \_T)
- ∼HopfieldNetwork ()
- int get N ()
- double get\_alpha ()
- double get\_T ()
- int get\_M ()
- void init\_spins\_randomly ()
- void init\_on\_corrupted\_pattern (spin\_pattern pattern, double probability)
- void init\_on\_corrupted\_pattern (int i, double probability)
- void set temperature (double newT)
- void build\_random\_patterns (int n\_patterns=-1)
- void push\_back\_pattern (spin\_pattern p)
- void set\_M (int newM)
- void set\_alpha (double newalpha)
- void build\_weights ()
- void glauber\_evolve (unsigned int niter, unsigned int nflips=N\_PARALLEL\_THREADS)
- double get\_Energy (spin \*state)
- double get\_Energy ()
- std::vector< double > overlaps ()
- double cur overlap (int i)
- std::pair< int, double > max\_overlap ()

#### 3.1.1 Constructor & Destructor Documentation

8 Class Documentation

#### 3.1.1.1 HopfieldNetwork() [1/2]

```
HopfieldNetwork::HopfieldNetwork (
    int _N,
    int _M,
    double _T ) [inline]
```

Construct a Hopfield Network with N spins, able to store M patterns of N spins, with initial temperature T.

#### 3.1.1.2 HopfieldNetwork() [2/2]

```
HopfieldNetwork::HopfieldNetwork (
    int _N,
    double _alpha,
    double _T ) [inline]
```

Construct a Hopfield Network with N spins, able to store  $\alpha$  N patterns of N spins, with initial temperature T.  $\alpha$  is generally known in literature as the load parameter.

#### 3.1.1.3 ~HopfieldNetwork()

```
HopfieldNetwork::~HopfieldNetwork ( ) [inline]
```

Destroy a Hopfield Network instance. A handwritten destructor is needed for the raw pointers.

#### 3.1.2 Member Function Documentation

#### 3.1.2.1 build\_random\_patterns()

```
void HopfieldNetwork::build_random_patterns ( int n_patterns = -1 ) [inline]
```

Build and store a number n\_patterns of randomly built patterns in the network. If nothing or -1 is passed, build and store M patterns. This method is useful as a benchmark since the most simple theoretical results have been proved for random patterns.

#### 3.1.2.2 build\_weights()

```
void HopfieldNetwork::build_weights ( ) [inline]
```

Construct the matrix of weights from the patterns stored in this->patterns and store it in this-> $\mathbb{W}$ . This is the matrix generally indicated in the literature with  $J_{ij}$ .

#### 3.1.2.3 cur\_overlap()

```
double HopfieldNetwork::cur_overlap ( \quad \text{int } i \text{ ) } \quad [\text{inline}]
```

Return the overlap between the current spin configuration of the network (the one stored in this->spins) and the i-th pattern stored in the network.

#### 3.1.2.4 get\_alpha()

```
double HopfieldNetwork::get_alpha ( ) [inline]
```

Getter for the load parameter.

#### 3.1.2.5 get\_Energy() [1/2]

```
double HopfieldNetwork::get_Energy ( ) [inline]
```

Return the energy of the Network for the current internal state of this->spins.

#### 3.1.2.6 get\_Energy() [2/2]

Return the Energy of the Network evaluated for the spin configuration pointed by state. state must point to N instances of spin.

#### 3.1.2.7 get\_M()

```
int HopfieldNetwork::get_M ( ) [inline]
```

Getter for the number of patterns.

#### 3.1.2.8 get\_N()

```
int HopfieldNetwork::get_N ( ) [inline]
```

Getter for the network size.

#### 3.1.2.9 get\_T()

```
double HopfieldNetwork::get_T ( ) [inline]
```

Getter for the temperature.

10 Class Documentation

#### 3.1.2.10 glauber\_evolve()

```
void HopfieldNetwork::glauber_evolve (
          unsigned int niter,
          unsigned int nflips = N_PARALLEL_THREADS ) [inline]
```

Evolve the network using a parallel version of the Glauber algorithm. Run niter evolution steps, in each of which nflips spins are evolved, default value is N\_PARALLEL\_THREADS.

#### 3.1.2.11 init\_on\_corrupted\_pattern() [1/2]

Initialise the spins with a corrupted version of the i-th pattern of the M stored in the network, where each of the spins may have been flipped with probability probability. Note that pattern must point to M spins.

#### 3.1.2.12 init\_on\_corrupted\_pattern() [2/2]

Initialise the spins with a corrupted version of the pattern pointed by pattern, where each of the spins may have been flipped with probability probability.

#### 3.1.2.13 init\_spins\_randomly()

```
void HopfieldNetwork::init_spins_randomly ( ) [inline]
```

Initialise all the spins in a random configuration, using random\_spin().

#### 3.1.2.14 max\_overlap()

```
std::pair< int, double > HopfieldNetwork::max_overlap ( ) [inline]
```

Return a std::pair<int, double> containing the index of the most condensed pattern and the corresponding Mattis magnetisation. They can be easily accessed through the .first and .second members of the std::pair.

#### 3.1.2.15 overlaps()

```
std::vector< double > HopfieldNetwork::overlaps ( ) [inline]
```

Return a std::vector of M elements, containing the memory overlaps of the current internal state of the network. The  $\mu$ -th element being the overlap with pattern  $\mu$ , a.k.a. the Mattis magnetisation  $m^{\mu}$ .

#### 3.1.2.16 push\_back\_pattern()

Store another pattern in the Network. This method falsifies the internal switch initialised\_weights so that launching a simulation before calling the function build\_weights() throws. This method throws if one attempts to push back a pattern of size() different from N.

#### 3.1.2.17 set\_alpha()

Set a new value for the load parameter  $\alpha$ . Defining newM = round(newalpha \* N), one of the following three cases can apply.

If newM = M, nothing is changed, if newM < M, (M - newM) patterns are popped back from the tail of the patterns vector. If newM > M, (newM-M) new random patterns are pushed back to the patterns vector.

Calling this method falsifies the internal switch initialised\_weights so that launching a simulation without calling the function build weights() throws an exception.

#### 3.1.2.18 set\_M()

Set a new value for the number of stored patterns. Depending on the value of newM, one of the following three cases can apply.

If newM = M, nothing is changed, if newM < M, (M - newM) patterns are popped back from the tail of the patterns vector. If newM > M, (newM-M) new random patterns are pushed back to the patterns vector.

Calling this method falsifies the internal switch initialised\_weights so that launching a simulation without calling the function build weights() throws an exception.

#### 3.1.2.19 set\_temperature()

Set the network operation temperature to newT.

The documentation for this class was generated from the following file:

· source/HopfieldNetwork.h

12 Class Documentation

## **Chapter 4**

## **File Documentation**

#### 4.1 source/HopfieldNetwork.h File Reference

```
#include <algorithm>
#include <cmath>
#include <random>
#include <stdexcept>
#include <utility>
#include <vector>
```

#### **Classes**

• class HopfieldNetwork

#### **Macros**

• #define N\_PARALLEL\_THREADS 1

#### **Typedefs**

- typedef signed char **spin** 
  - Signed char used to represent a single Ising spin which can only take the values +1 or -1 to optimize memory usage.
- typedef std::vector< spin > spin\_pattern

Shorthand to represent a pattern of spins to store in the Network.

#### **Functions**

- spin random\_spin ()
- double overlap (spin \*a, spin \*b, int N)

14 File Documentation

#### 4.1.1 Detailed Description

**Author** 

Giulio Colombini

Hopfield Network with built-in parallel Monte Carlo Glauber evolution.

This header contains the full implementation of a Hopfield Network, along with some useful functions to work with it.

#### 4.1.2 Macro Definition Documentation

#### 4.1.2.1 N\_PARALLEL\_THREADS

```
#define N_PARALLEL_THREADS 1
```

The number of parallel threads used to run the program defaults to 1, but can be set at compile time depending on the possibilities of the available machine by passing  $-DN\_PARALLEL\_THREADS=N$ , where N is the number of desired threads.

#### 4.1.3 Function Documentation

#### 4.1.3.1 overlap()

Returns the overlap between spin configuration  $\sigma^a$  and  $\sigma^b$ , both of which must be of size N, amounting to

Overlap
$$(\sigma^a, \sigma^b) = \frac{1}{N} \sum_{i=1}^{N} \sigma_i^a \sigma_i^b$$
.

. When calculated between the current spin configuration and one of the memories, this quantity is often called the *Mattis magnetisation* and indicated, e.g. for memory  $\mu$ , by  $m^{\mu}$ .

#### 4.1.3.2 random\_spin()

```
spin random_spin ( ) [inline]
```

Returns a spin which has value +1 or -1 with equal probability 1/2.

4.2 HopfieldNetwork.h 15

#### 4.2 HopfieldNetwork.h

Go to the documentation of this file.

```
114 #include <algorithm>
115 #include <cmath>
116 #include <random>
117 #include <stdexcept>
118 #include <utility>
119 #include <vector>
120
121 #ifndef N_PARALLEL_THREADS
124
        #define N_PARALLEL_THREADS 1
125 #endif
126
128 typedef signed char spin;
129
131 typedef std::vector<spin> spin_pattern;
132
133
135 static std::default_random_engine re;
137 static std::uniform_int_distribution<short int> coin_toss(0,1);
139 static std::uniform_real_distribution<double> rnd(0.0,1.0);
140
141 inline spin random_spin()
142
145 {return 2 * coin_toss(re) - 1;}
146
147 double overlap (spin \star a, spin \star b, int N)
154 {
155
         double ret = 0:
         for (int i = 0; i < N; ++i) ret += a[i]*b[i];</pre>
156
158
          return ret/N;
159 }
160
161 class HopfieldNetwork
162 {
163
164
          double T = 0.;
                                                                    // System temperature
165
         double alpha;
                                                                    // System load parameter
                                                                    // Number of spins/neurons
166
         int N:
                                                                    // Number of memories/patterns
// Pointer to the state of the Network Spins
167
         int M;
168
         spin * spins;
169
          std::vector<spin_pattern> patterns;
                                                                    // Vector containing the patterns stored in the
        double ** W; // Interaction weights between neurons std::uniform_int_distribution<int> spin_picker; // Distribution used for selecting spins to update bool initialised_weights = false; // Keep track of weight initialisations, to avoid running simulations without uninitialised parameters in the model.
170
171
172
173
174
175
176
         HopfieldNetwork(int _N, int _M, double _T): T{_T}, N{_N}, M{_M}
180
181
               alpha = double(M/N);
182
              spins = new spin[N];
183
              patterns = std::vector<spin_pattern>(M, spin_pattern());
184
               W = new double * [N];
              #pragma omp parallel for num_threads(N_PARALLEL_THREADS)
for(int i = 0; i < N; ++i) W[i] = new double[N];</pre>
185
186
              spin_picker = std::uniform_int_distribution<int>(0, N-1);
187
188
         }
189
190
         HopfieldNetwork(int _N, double _alpha, double _T): T{_T}, alpha{_alpha}, N{_N}
195
196
              M = int(std::round(alpha * N));
197
              spins = new spin[N];
198
              patterns = std::vector<spin_pattern>(M, spin_pattern());
199
               W = \text{new double } * [N];
               #pragma omp parallel for num_threads(N_PARALLEL_THREADS)
200
201
               for(int i = 0; i < N; ++i) W[i] = new double[N];
202
               \label{eq:spin_picker} \verb|spin_picker| = \verb|std::uniform_int_distribution<int>(0, N-1);
203
         }
204
205
          ~HopfieldNetwork()
209
210
              delete[] spins;
for(int i = 0; i < N; ++i) delete[] W[i];</pre>
211
212
              delete[] W;
213
214
215
216
          // Getters
219
          int get_N() {return N;};
```

16 File Documentation

```
222
        double get_alpha(){return alpha;};
225
        double get_T() {return T;};
228
        int get_M() {return M; };
229
230
        void init_spins_randomly()
{for(int i = 0; i < N; ++i) spins[i] = random_spin();}</pre>
234
235
236
        void init_on_corrupted_pattern(spin_pattern pattern, double probability)
241
            #pragma omp parallel for num_threads(N_PARALLEL_THREADS)
2.42
            for(int i = 0; i < N; ++i){spins[i] = rnd(re) < probability? -1 * pattern[i] : pattern[i];}}</pre>
243
244
245
        void init on corrupted pattern(int i, double probability)
250
251
            #pragma omp parallel for num_threads(N_PARALLEL_THREADS)
252
            patterns[i][j];}}
253
254
255
        // Parametric setters
256
257
        void set_temperature(double newT)
2.58
        {T = newT; }
2.61
262
263
        // Memory setters
264
265
        void build_random_patterns(int n_patterns = -1)
269
        if (n_patterns == -1) n_patterns = M; // Defaults to the number specified at construction
270
271
272
        #pragma omp parallel for num_threads(N_PARALLEL_THREADS)
273
274
        for (int p = 0; p < M; ++p)
275
276
            patterns[p].resize(N);
            for(int n = 0; n < N; ++n) patterns[p][n] = random_spin();</pre>
277
278
279
        initialised_weights = false;
280
281
2.82
        void push_back_pattern(spin_pattern p)
287
288
            if (p.size() == (unsigned)N) {this->patterns.push_back(p);}
            else {throw std::runtime_error("The length of each pattern must be equal to the number of spins
289
       in the system!");}
290
            this->M = this->patterns.size();
291
            this->alpha = double(this->M / this->N);
292
            initialised_weights = false;
293
        }
294
295
        void set_M(int newM)
305
306
            int deltaM = newM - this->M;
            if(deltaM > 0)
307
308
309
                spin_pattern tmp(N, 0);
310
                for (int i = 0; i < deltaM; ++i)
311
312
                    for(int j = 0; j < N; ++j) tmp[j] = random_spin();
313
                    this->patterns.push_back(tmp);
314
315
                this->M = newM;
316
                this->alpha = double(this->M/this->N);
317
                initialised_weights = false;
318
319
            if (deltaM == 0) return;
            if (deltaM < 0)</pre>
320
321
            {
322
                for(int i = 0; i < std::abs(deltaM); ++i) this->patterns.pop_back();
323
                this->M = newM;
324
                this->alpha = double(this->M/this->N);
325
                initialised_weights = false;
326
327
328
        }
329
330
        void set_alpha(double newalpha)
340
            int newM = int(std::round(newalpha * this->N));
341
342
            set M(newM);
343
344
345
        // Weights initialiser
346
        void build_weights()
347
352
```

```
353
        #pragma omp parallel for num_threads(N_PARALLEL_THREADS)
354
355
        for(int i = 0; i < N; ++i)
356
357
             for (int j = 0; j \le i; ++j)
358
359
                 W[i][j] = 0;
360
                  or(int w = 0; w < M; ++w) W[i][j] += (double)patterns[w][i] * patterns[w][j] / N;
                 W[j][i] = W[i][j];
361
362
363
364
        initialised weights = true;
365
366
367
        // Evolution step function
368
        void glauber_evolve(unsigned int niter, unsigned int nflips = N_PARALLEL_THREADS)
373
374
375
        for(auto it : patterns) if(it.size() != (unsigned)N) throw std::runtime_error("Simulation was
       launched with uninitialised patterns.");
376
377
        if (not initialised_weights) throw std::runtime_error("Simulation was launched with uninitialised
       weights.");
378
379
        for(unsigned int iter = 0; iter < niter; ++iter)</pre>
380
381
             int flip_candidates[nflips];
382
             for(unsigned int i = 0; i < nflips; ++i) flip_candidates[i] = spin_picker(re);</pre>
383
384
             #pragma omp parallel for num_threads(N_PARALLEL_THREADS)
385
386
             for(unsigned int i = 0; i < nflips; ++i)</pre>
387
388
                 double 1f = 0;
389
                 for (int j = 0; j < N; ++j) lf+= W[flip_candidates[i]][j]*spins[j];
390
                double dE = 2 * 1f * spins[flip_candidates[i]];
double thr = 1/(1+std::exp(dE/T));
391
392
393
394
                 if(rnd(re) < thr)</pre>
395
                         spins[flip_candidates[i]] *= -1;
396
397
398
399
400
401
402
        double get_Energy(spin * state)
406
407
            double ret = 0:
408
409
             #pragma omp parallel for reduction (-:ret) num_threads(N_PARALLEL_THREADS)
410
             for (int i = 0; i < N; ++i)
411
                 for(int j = i+1; j < N; ++j) ret -= W[i][j]*state[i]*state[j];</pre>
412
413
414
415
            return ret;
416
417
418
        double get_Energy()
422
423
            return get_Energy(this->spins);
424
425
426
        std::vector<double> overlaps()
431
             std::vector<double> overlaps(N, 0.);
432
433
             for(int o = 0; o < M; ++o) overlaps[o] = overlap(spins, patterns[o].data(), N);</pre>
434
            return overlaps;
435
436
437
        double cur_overlap(int i)
442
443
            return overlap(this->spins, patterns[i].data(), this->N);
444
445
446
        std::pair<int, double> max_overlap()
451
             auto overlaps = this->overlaps();
452
             int argmax = std::distance(overlaps.begin(), std::max_element(overlaps.begin(),
453
       overlaps.end()));
454
            return std::pair<int, double>(argmax, overlaps[argmax]);
455
456 };
```

18 File Documentation

## **Bibliography**

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20 BIBLIOGRAPHY

## Index

$\sim$ HopfieldNetwork HopfieldNetwork, 8	init_spins_randomly HopfieldNetwork, 10
build_random_patterns HopfieldNetwork, 8	max_overlap HopfieldNetwork, 10
build_weights HopfieldNetwork, 8	N_PARALLEL_THREADS HopfieldNetwork.h, 14
cur_overlap HopfieldNetwork, 8	overlap  HopfieldNetwork.h, 14
get_alpha HopfieldNetwork, 9	overlaps HopfieldNetwork, 10
get_Energy HopfieldNetwork, 9	push_back_pattern
get_M HopfieldNetwork, 9	HopfieldNetwork, 10 random_spin
get_N HopfieldNetwork, 9 get_T	HopfieldNetwork.h, 14
HopfieldNetwork, 9 glauber_evolve	set_alpha HopfieldNetwork, 11
HopfieldNetwork, 9	set_M HopfieldNetwork, 11
HopfieldNetwork, 7  ~HopfieldNetwork, 8	set_temperature HopfieldNetwork, 11 source/HopfieldNetwork.h, 13, 15
<pre>build_random_patterns, 8 build_weights, 8 cur_overlap, 8</pre>	Source/Hopheldivetwork.ii, 13, 13
get_alpha, 9 get_Energy, 9	
get_M, 9 get_N, 9	
get_T, 9 glauber_evolve, 9	
HopfieldNetwork, 7, 8 init_on_corrupted_pattern, 10	
init_spins_randomly, 10 max_overlap, 10 overlaps, 10	
push_back_pattern, 10 set_alpha, 11	
set_M, 11 set_temperature, 11	
HopfieldNetwork.h N_PARALLEL_THREADS, 14	
overlap, 14 random_spin, 14	
init_on_corrupted_pattern HopfieldNetwork, 10	