

Data Structure

Chapter 3: Sorting

Main

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3.1 Introduction

- ◆ Record（记录）： Multiple data items
- ◆ Key (关键字)： *The items* used to sort records
- ◆ RecordType:

```
typedef struct {  
    KeyType key;           // 关键字项  
    .....                // 其它数据项  
} RecordType, RcdType;    // 记录类型
```

3.1.1 Concepts

- ◆ Example:

(175, 85, 260, 63, 412, 504, 840, 518, 630, 950)

Sorting:

(63, 85, 175, 260, 412, 504, 518, 630, 840, 950)

- ◆ The important critical properties of sorting algorithm:

(排序算法的两大关键步骤)

- **Number of comparisons to be made** (比较)

- **Number of data movements** (移动)

3.1.1 Concepts

◆ The objectives of sorting algorithm:

- (1) Minimize the number of movements of data
- (2) Movements of data from secondary storage to main memory in large blocks
- (3) Retaining all the data items in the main memory

◆ The factors for choosing a sorting methods:

- (1) Programming time
- (2) Execution time of the program
- (3) Memory or auxiliary storage space needed for programming environment.

RcdSqlList

Elem saved in RcdSqlList:

```
typedef struct {  
    KeyType key;           // 关键字项  
    .....                // 其它数据项  
} RecordType, RcdType;    // 记录类型
```

The RcdSqlList:

```
typedef struct {  
    RcdType *rcd;    // 存储空间基址  
    int length;      // 当前长度  
    int size;        // 存储容量  
} RcdSqlList; // 记录的顺序表
```

注意： SqlList
的0号位闲置
或用作 **sentry**
post(哨位)

3.1.1 Concepts

◆ SORTing: the arrangement of a set of DATA in some order *Ascending* 升序 or *Descending* 降序

◆ Two categories sorting:

(1) Internal Sorting :

Sorting of data items in the Main memory

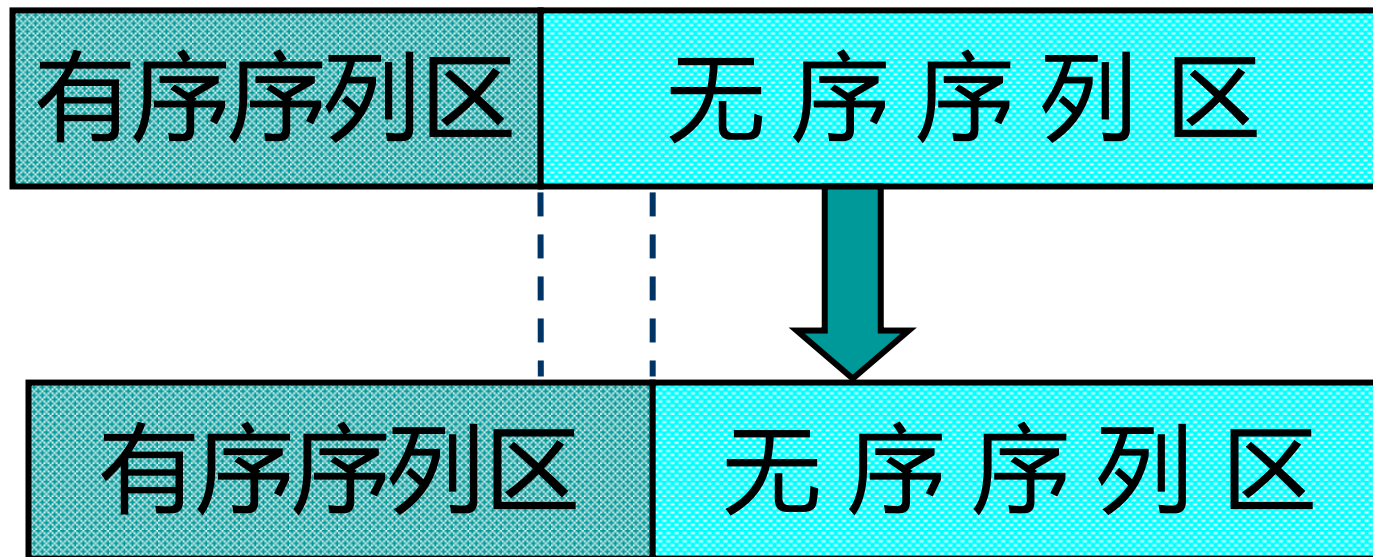
(2) External Sorting :

Sorting of data items partly in the main memory and partly in Auxiliary memory

Classification of internal sorting

- ◆ Five categories : Exchange sort, selection sort, insertion sort, merge sort and cardinality sort.

(交换排序、选择排序、插入排序、归并排序和基数排序)



Classification of internal sorting

- ◆ **Array storage (internal store)**
Files storage (external store)

- (1) Insertion
- (2) Selection
- (3) Bubble (冒泡)
- (4) Shell
- (5) Quick
- (6) Binary
- (7) Heap
- (8) Radix (基数)
- (9) Merge

Sort (Internal Sorting)

Records r_1, r_2, \dots, r_n

**With KEY values k_1, k_2, \dots, k_n ,
respectively**



SORTed

Records $r_{i1}, r_{i2}, \dots, r_{in}$

**with KEY values $k_{i1} \leq k_{i2} \leq \dots \leq k_{in}$,
respectively**

Internal sorting

◆ The objectives of sorting algorithm:

- (1) Minimize the number of movements of data
- (2) Movements of data from secondary storage to main memory in large blocks
- (3) Retaining all the data items in the main memory

◆ The factors for choosing a sorting methods:

- (1) Programming time
- (2) Execution time of the program
- (3) Memory or auxiliary storage space needed for programming environment.

Complexity of Internal Sorting Algorithm

Algorithm	Worst (Time)	Average (Time)	Best (Time)	Auxiliary Space	Stability
Insertion	$O(n^2)$	$O(n^2)$	$O(n-1)$	$O(1)$	Yes
Selection	$O(n^2)$	$O(n^2)$	$O(n^2)$	$O(1)$	No
Bubble	$O(n^2)$	$O(n^2)$	$O(n^2)$	$O(1)$	Yes
Shell	$\sim O(n)$	$O(n(\log_2 n)^2)$	$\sim O(n)$	$O(1)$	No
Quick	$O(n^2)$	$O(\log_2 n)$	$O(\log_2 n)$	$O(\log n)$	No
BinaryTree	$O(n^2)$	$O(n \log n)$	$O(n \log n)$		Yes
Heap	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$	$O(1)$	No
Radix	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$	$O(n+r)$	Yes
Merge	$O(n \log n)$	$O(n \log n)$	$O(n \log n)$	$O(n)$	Yes

Stability 算法稳定性:

◆ Stability:

Before Sorting:

If $\text{Rec}(K_i) > \text{Rec}(K_j)$ for KEY $K_i = K_j$

After Sorting:

Sort is STABLE: if $\text{Rec}(K_i) > \text{Rec}(K_j)$

Sort is UNStable: if $\text{Rec}(K_i) < \text{Rec}(K_j)$

3.2 Simple Insertion Sort (直接插入排序)

◆ The key sequence: (56, 68, 25, 45, 90, 38, 10, 72)

初始序列: [56] 68 25 45 90 38 10 72

第一趟排序结果: [56 68] 25 45 90 38 10 72

第二趟排序结果: [25 56 68] 45 90 38 10 72

第三趟排序结果: [25 45 56 68] 90 38 10 72

第四趟排序结果: [25 45 56 68 90] 38 10 72

第五趟排序结果: [25 38 45 56 68 90] 10 72

第六趟排序结果: [10 25 38 45 56 68 90] 72

第七趟排序结果: [10 25 38 45 56 68 72 90]



算法实现分析

- ◆ Find Insert Position

`j = 0; do { j++; } while (L.rcd[j].key < L.rcd[i+1].key);` // 从前到后查找
插入位置

- ◆ Move record to empty insertion position

`L.rcd[0] = L.rcd[i+1];` // 先将记录 `L.rcd[i+1]` 保存在空闲的0号单元

`k = i+1; do { k--; L.rcd[k+1] = L.rcd[k]; } while(k > j);` // 从后到前移动
记录

- ◆ Use Sentry and sentry post:

`L.rcd[0] = L.rcd[i+1];` // 置入哨位，作为哨兵

`j = i+1; do{ j--; L.rcd[j+1] = L.rcd[j]; }`

`while(j > 1 && L.rcd[0].key < L.rcd[j-1].key);`

// 从后到前查找并移动记录

- ◆ Set up sentry
- ◆ Find Insert Position. Move records to empty insertion position
- ◆ Insert a Record

Simple Insertion Sort

void InsertSort (RcdSqList &L)

0	1	j			i	i+1		
38	25	45	56	68	90	38	10	72

```

void InsertSort(RcdSqList &L) { // 对顺序表L作直接插入排序。
    int i, j;
    for(i = 1; i < L.length; ++i)
        if(L.rcd[i+1].key < L.rcd[i].key) { // 需将L.rcd[i+1]插入有序序列
            L.rcd[0] = L.rcd[i+1]; // 先将记录L.rcd[i+1]保存在空闲的0号单元
            j = i+1;
            do { j--; L.rcd[j+1] = L.rcd[j]; // 记录后移
            } while(L.rcd[0].key < L.rcd[j-1].key); // 判断是否需要继续移动
            L.rcd[j] = L.rcd[0]; // 插入
        }
}

```

Complexity of Algorithm

- ◆ The time consumption of Insertion sort is mainly related to the frequency of records compared with key and moved.

- ◆ **Best case (data are in order)**

“比较” 的次数:

$$\sum_{i=1}^{n-1} 1 = n - 1$$

“移动” 的次数:

$$0$$

- ◆ **Worst case (data are in reverse order)**

“比较” 的次数:

$$\sum_{i=1}^{n-1} (i+1) = \frac{(n+2)(n-1)}{2}$$

“移动” 的次数:

$$\sum_{i=1}^{n-1} (i+2) = \frac{(n+4)(n-1)}{2}$$

- ◆ **Best case : $O(n)$, Worst case : $O(n^2)$ 。**

Average case (data are in random order)

- ◆ Only one record auxiliary space is required. Space complexity $O(1)$

3.3 Shell sort (希尔排序)

◆ Shell sort : diminishing increment sort

The items are Divided into smaller Segments (e.g., k segment), then these segments are Sorted separately using Insertion sorting.

1	2	3	4	5	6	7	8	9	10											
<hr/>																				
(13	,	27	,	49	,	55	,	04	,	49	,	38	,	65	,	97	,	76)

3.3 Steps of Shell sort

- ◆ Set up Increment d , dividing the list into smaller segments
- ◆ Sorting separately these smaller Segments using Insertion sorting.
- ◆ Continuously decrease increment d , Repeat the above steps until d is reduced to 1.

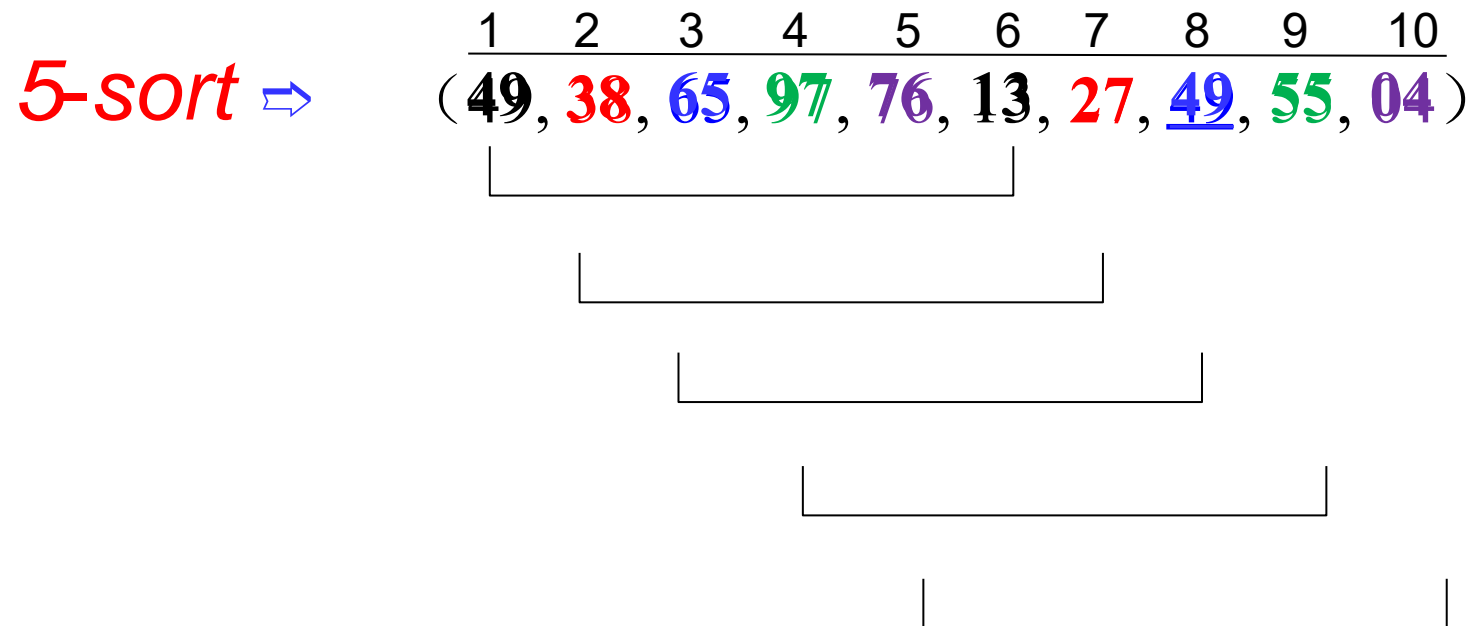
The value sequence of increment d is called *increment sequence*. sorting operation can be marked *d-sort* .

ShellSort is also named **diminishing increment sort** (缩小增量排序)

Example of Shell sort

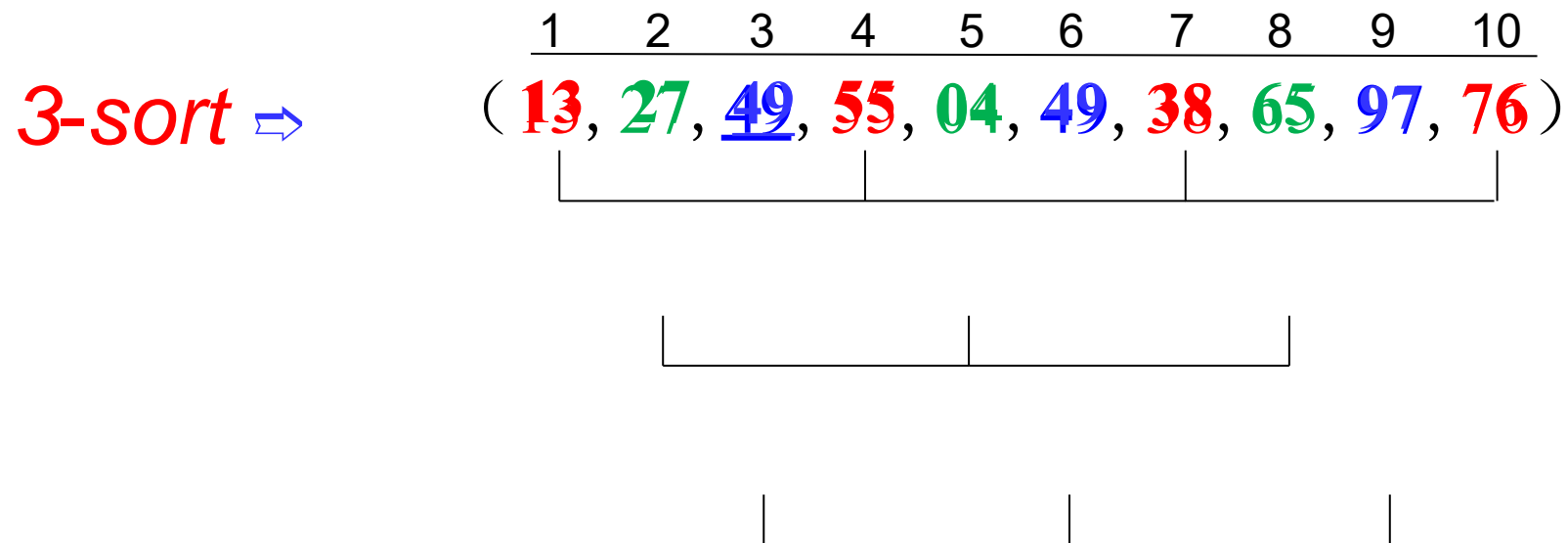
- ◆ Original sequence: (49, 38, 65, 97, 76, 13, 27, 49, 55, 04)
- ◆ *Increment sequence* : $d = (5, 3, 1)$

The first: $d_1 = 5$:



The result : (13, 27, 49, 55, 04, 49, 38, 65, 97, 76)

◆ The second : $d_2 = 3$



The result : (13, 04, 49, 38, 27, 49, 55, 65, 97, 76)

◆ The third : $d_3 = 1$ **1-sort :**

(04, 13, 27, 38, 49, 49, 55, 65, 76, 97)

- ◆ 暂存待插入记录
- ◆ 按增量 dk 查找插入位置, 移动记录空出插入位置
- ◆ 插入记录

一趟希尔排序

`void ShellInsert(RcdSqList &L, int dk)`

0	i-3			i			i+3			
38	13	04	<u>49</u>	55	27	49	38	65	97	76
				j						

```

void ShellInsert(RcdSqList &L, int dk) { // 对顺序表L作一趟希尔排序, 增量为dk
    int i, j;
    for(i = 1; i <= L.length-dk; ++i)
        if(L.rcd[i+dk].key < L.rcd[i].key) { // 需将L.rcd[i+dk]插入有序序列
            L.rcd[0] = L.rcd[i+dk]; // 暂存在L.rcd[0]
            j = i+dk;
            do{ j-=dk; L.rcd[j+dk] = L.rcd[j]; // 记录后移
            }while(j-dk>0 && L.rcd[0].key<L.rcd[j-dk].key); // 判断是否需要继续移动
            L.rcd[j] = L.rcd[0]; // 插入
        }
    }
}

```

希尔排序

```
void ShellSort(RcdSqList &L, int d[], int t) {  
    // 按增量序列d[0..t-1]对顺序表L作希尔排序  
    int k;  
    for( k = 0; k<t; ++k )  
        ShellInsert(L, d[k]); //一趟增量为d[k]的插入排序  
}
```

Time Complexity : $O(n^{1.5})$

Stability: Shell sort is unstable.