

Physics formula booklet

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Constants and unit conversions

Gas constant	$R = 8.314 \text{ J/(mol K)}$ $= 0.082057 \frac{\text{L atm}}{\text{mol K}}$
Converting between rpm and rad/s	$1 \text{ rpm} = \frac{2\pi}{60} \text{ rad/s}$
Gravitational constant	$G = 6.67 \cdot 10^{-11} \text{ Nm}^2/\text{kg}^2$
Converting between Kelvin and Celsius temperatures	$T_K = T_C + 273.15$
Converting between atmospheres and Pascals	$1 \text{ atm} = 1.013 \cdot 10^5 \text{ Pa}$
Stefan-Boltzmann constant	$\sigma = 5.67 \cdot 10^{-8} \text{ W/(m}^2\text{K}^4)$
Avogadro's number	$N_A = 6.02 \cdot 10^{23} \text{ mol}^{-1}$
Boltzmann constant	$k = 1.38 \cdot 10^{-23} \text{ J/K} = \frac{R}{N_A}$

Vectors (Chapter 1)

Scalar/dot product	$\vec{A} \cdot \vec{B} = \vec{A} \vec{B} \cos(\theta) = A_x B_x + A_y B_y + A_z B_z$
Vector/cross product	$\vec{A} \times \vec{B} = \begin{bmatrix} A_y B_z - A_z B_y \\ A_z B_x - A_x B_z \\ A_x B_y - A_y B_x \end{bmatrix}$ $ \vec{A} \times \vec{B} = \vec{A} \vec{B} \sin(\theta)$

1D motion (Chapter 2)

Average and instantaneous velocity	$\langle v \rangle = \frac{\Delta x}{\Delta t}$ $v = \frac{dx}{dt}$ <p>The angle brackets denote an average</p>
Average and instantaneous acceleration	$\langle a \rangle = \frac{\Delta v}{\Delta t}$ $a = \frac{dv}{dt}$
Equations for straight line motion with constant acceleration	$v_x = v_{0x} + a_x t$ $x = x_0 + v_{0x} t + \frac{1}{2} a_x t^2$ $v_x^2 = v_{0x}^2 + 2a_x(x - x_0)$ $x - x_0 = \frac{1}{2}(v_{0x} + v_x)t$
Straight line motion with varying acceleration	$v_x = v_{0x} + \int_0^t a_x dt$ $x = x_0 + \int_0^t v_x dt$

2D motion (Chapter 3)

Projectile motion	$x = v_{0x} t$ $y = v_{0y} t - \frac{1}{2} g t^2$ $v_y = v_{0y} - g t$
Centripetal acceleration	$a_c = \frac{v^2}{R} = \frac{4\pi^2 R}{T^2}$ <p>where R is the radius of the circle in which the object is moving</p>

Relative velocity	$v_{P/A-x} = v_{P/B-x} + v_{B/A-x}$ $\vec{v}_{P/A} = \vec{v}_{P/B} + \vec{v}_{B/A}$ <p>where $\vec{v}_{P/A}$ means the velocity of P relative to A</p>
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Newton's Laws (Chapters 4 and 5)

Net force	$\vec{F}_{net} = \vec{F}_1 + \vec{F}_2 + \vec{F}_3 + \dots$
Newton's second law	$\vec{F}_{net} = m\vec{a}$ $F_{net,x} = ma_x$ $F_{net,y} = ma_y$ $F_{net,z} = ma_z$
Gravitational force (weight)	$F_g = mg$
Newton's third law	$\vec{F}_{A \text{ on } B} = -\vec{F}_{B \text{ on } A}$
Kinetic friction	$F_k = \mu_k N$ <p>where μ_k is the coefficient of kinetic friction and N is the normal force acting on the object</p>
Static friction	$F_s \leq \mu_s N$ <p>where μ_s is the coefficient of static friction and N is the normal force acting on the object</p>

Work and kinetic energy (Chapter 6)

Work	$W = \vec{F} \cdot \vec{s} = Fs \cos(\theta)$ <p>where \vec{s} is the displacement vector and θ is the angle between the force and displacement vectors</p>
Kinetic energy	$E_{kin} = \frac{1}{2}mv^2$
Work-energy theorem	$W_{tot} = \Delta E_{kin}$
Work done by a varying force or on a curved path	$W = \int_{x_1}^{x_2} F_x dx$ $W = \int_{P_1}^{P_2} \vec{F} \cdot d\vec{s} = \int_{P_1}^{P_2} F \cos(\theta) ds = \int_{P_1}^{P_2} F_{\parallel} ds$ <p>where P_1 is the initial position, P_2 is the final position, and \vec{s} is displacement</p>

Power	$\langle P \rangle = \frac{\Delta W}{\Delta t}$ $P = \frac{dW}{dt}$ $P = \vec{F} \cdot \vec{v} = F \cdot v \cdot \cos(\theta)$ <p>where $\langle P \rangle$ is average power and P is instantaneous power</p>
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Potential energy (Chapter 7)

Gravitational potential energy	$E_{pot,g} = mgh$
Elastic potential energy	$E_{pot,s} = \frac{1}{2}kx^2$ <p>where k is the spring constant and x is the displacement from the equilibrium position</p>
Work done by gravity or a spring	$W_g = -\Delta E_{pot,g}$ $W_s = -\Delta E_{pot,s}$
Mechanical energy	$E_{mec} = E_{kin} + E_{pot}$ <p>where E_{pot} is the sum of all the different potential energies involved</p>
Work-mechanical energy theorem	$\Delta E_{mec} = W_{nc}$ $E_{mec,i} + W_{nc} = E_{mec,f}$ <p>where W_{nc} is the work done by non-conservative forces. "i" means initial and "f" means final</p>

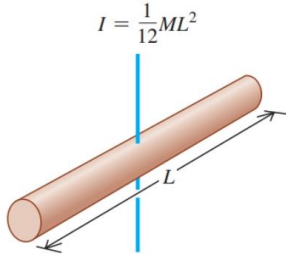
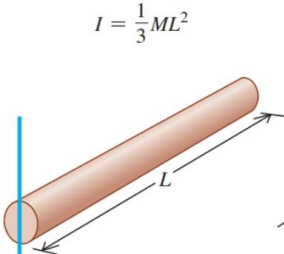
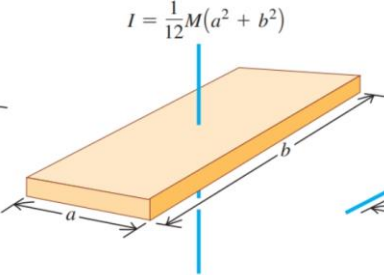
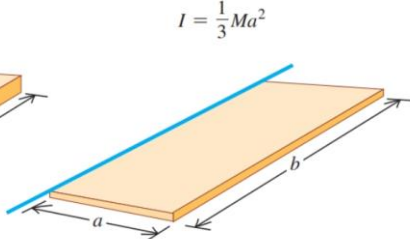
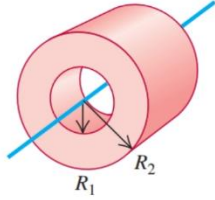
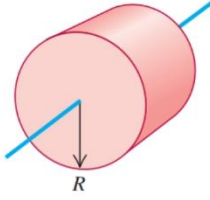
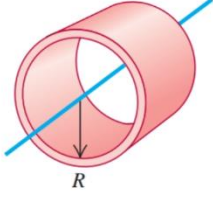
Momentum (Chapter 8)

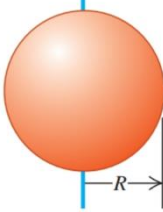
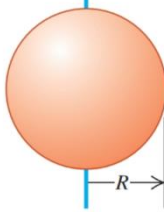
Momentum	$\vec{p} = m\vec{v}$
Newton's second law in terms of momentum	$\vec{F}_{net} = \frac{d\vec{p}}{dt}$
Impulse	$\vec{J} = \Delta\vec{p}$ $\vec{J} = \langle \vec{F}_{net} \rangle \Delta t$ $\vec{J} = \int_{t_1}^{t_2} \vec{F}_{net} dt$ <p>where $\langle \vec{F}_{net} \rangle$ is the average net force and \vec{F}_{net} is the instantaneous net force</p>

Conservation of momentum	$\vec{P} = \vec{p}_A + \vec{p}_B + \dots = m_A \vec{v}_A + m_B \vec{v}_B + \dots$ $\vec{P}_i = \vec{P}_f$ <p>The sum of the momenta of the objects that make up a system is constant if the net external force on the system is 0. "i" means initial and "f" means final</p>
Kinetic energy in terms of momentum	$E_{kin} = \frac{p^2}{2m}$
Center of mass	$\vec{r}_{cm} = \frac{\sum_i m_i \vec{r}_i}{\sum_i m_i}$
Total momentum and net force using center of mass	$\vec{P} = M \vec{v}_{cm}$ $\vec{F}_{net,external} = M \vec{a}_{cm}$
Force of thrust on a rocket	$F_{thrust} = -v_{ex} \frac{dm}{dt}$ <p>where v_{ex} is the exhaust <i>speed</i> (positive) and $\frac{dm}{dt}$ is the rate of change of mass of the rocket as it loses fuel (negative)</p>
Speed of a rocket after launch	$v_f = v_i + v_{ex} \ln\left(\frac{m_i}{m}\right)$ <p>where v_i is the initial speed, v_{ex} is the exhaust speed (positive), m_i is the initial mass of the rocket, and m is the mass of the rocket at the time when you want to find its speed</p>

Rotation of rigid bodies (Chapter 9)

Angular velocity	$\omega_z = \frac{d\theta}{dt}$
Angular acceleration	$\alpha_z = \frac{d\omega_z}{dt}$
Equations for angular motion with constant angular acceleration	$\theta = \theta_0 + \omega_{0z}t + \frac{1}{2}\alpha_z t^2$ $\theta - \theta_0 = \frac{1}{2}(\omega_{0z} + \omega_z)t$ $\omega_z = \omega_{0z} + \alpha_z t$ $\omega_z^2 = \omega_{0z}^2 + 2\alpha_z(\theta - \theta_0)$
Linear speed and angular speed	$v = r\omega$ <p>where r is the distance of a particle from the rotation axis</p>
Tangential acceleration and angular acceleration	$a_{tan} = r\alpha$

Radial (centripetal) acceleration and angular speed	$a_{rad} = \frac{v^2}{r} = \omega^2 r$
Moment of inertia	$I = \sum_i m_i r_i^2$
Rotational kinetic energy	$E_{kin, rot} = \frac{1}{2} I \omega^2$
Moment of inertia for various shapes	<div> <div> <p>(a) Slender rod, axis through center</p> $I = \frac{1}{12} ML^2$  </div> <div> <p>(b) Slender rod, axis through one end</p> $I = \frac{1}{3} ML^2$  </div> <div> <p>(c) Rectangular plate, axis through center</p> $I = \frac{1}{12} M(a^2 + b^2)$  </div> <div> <p>(d) Thin rectangular plate, axis along edge</p> $I = \frac{1}{3} Ma^2$  </div> <div> <p>(e) Hollow cylinder</p> $I = \frac{1}{2} M(R_1^2 + R_2^2)$  </div> <div> <p>(f) Solid cylinder</p> $I = \frac{1}{2} MR^2$  </div> <div> <p>(g) Thin-walled hollow cylinder</p> $I = MR^2$  </div> <p>(continued on next page)</p> </div>

	<div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;"> <p>(h) Solid sphere</p> $I = \frac{2}{5}MR^2$  </div> <div style="text-align: center;"> <p>(i) Thin-walled hollow sphere</p> $I = \frac{2}{3}MR^2$  </div> </div>
Parallel-axis theorem	$I_P = I_{cm} + Md^2$ <p>where I_{cm} is the moment of inertia around an axis through the center of mass, I_P is the moment of inertia around an axis parallel to that axis, d is the distance between the two axes, and M is the mass of the body</p>

Dynamics of rotational motion (Chapter 10)

Torque	$\tau = Fl = rF \sin(\phi) = F_{tan}r$ <p>l is the length of the lever arm</p> <p>r is the distance of the point where the force is applied from the axis of rotation</p> <p>ϕ is the angle between the force vector and the position vector \vec{r} of the point where the force is applied with respect to the axis of rotation</p> <p>F_{tan} is the tangential force component</p> <p>In vector form,</p> $\vec{\tau} = \vec{r} \times \vec{F}$
Rotational analog of Newton's second law	$\tau_{z, net} = I\alpha_z$
Kinetic energy in combined translation and rotation	$E_{kin} = \frac{1}{2}Mv_{cm}^2 + \frac{1}{2}I_{cm}\omega^2$
Condition for rolling without slipping	$v_{cm} = R\omega$
Work done by a torque	$W = \int_{\theta_1}^{\theta_2} \tau_z d\theta$ <p>For a constant torque,</p> $W = \tau_z \Delta\theta$

Work-kinetic energy theorem for rotational motion	$W_{tot} = \frac{1}{2}I\omega_f^2 - \frac{1}{2}I\omega_i^2$
Power of a torque	$P = \tau_z \omega_z$
Angular momentum	<p>For a particle:</p> $\vec{L} = \vec{r} \times \vec{p} = \vec{r} \times m\vec{v}$ $L_z = rp \sin(\theta) = rmv \sin(\theta)$ <p>For a rigid body rotating about its axis of symmetry:</p> $\vec{L} = I\vec{\omega}$ $L_z = I\omega_z$
Rotational analog of Newton's second law with angular momentum	$\vec{\tau}_{net} = \frac{d\vec{L}}{dt}$
Precession angular speed for a gyroscope	$\Omega = \frac{F_g r}{I\omega}$ <p>F_g is the gravitational force acting on the gyroscope and r is the radius of precession</p>

Equilibrium and elasticity (Chapter 11)

Conditions for equilibrium	$\vec{F}_{net} = \mathbf{0}$ $\vec{\tau}_{net} = \mathbf{0} \text{ about any point}$
Hooke's law in general	Elastic modulus = $\frac{\text{Stress}}{\text{Strain}}$
Tensile and compressive stress	$Y = \frac{\sigma}{\varepsilon} = \frac{F_{\perp}/A}{\Delta l/l_0}$ <p>where Y is Young's modulus, σ is tensile/compressive stress, ε is tensile/compressive strain, and F_{\perp} is the normal force component applied to opposite sides</p>
Bulk stress	$B = -\frac{\Delta p}{\Delta V/V_0}$ <p>where B is the bulk modulus and Δp is the pressure change</p>

Shear stress	$S = \frac{\tau}{\gamma} = \frac{F_{\parallel}/A}{x/h}$ <p>S is the shear modulus</p> <p>τ is shear stress</p> <p>γ is shear strain</p> <p>F_{\parallel} is the parallel force component applied to opposite sides</p> <p>x is the displacement of one side</p> <p>h is the transverse dimension, or height</p>
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Fluid mechanics (Chapter 12)

Density	$\rho = \frac{m}{V}$
Pressure at a point in a fluid	$p = \frac{dF_{\perp}}{dA}$ <p>where F_{\perp} is the normal force applied on both sides of the area A</p>
Pressure in a fluid at rest	$p_2 - p_1 = -\rho g(h_2 - h_1)$ <p>where h_1 and h_2 are elevations</p> $p = p_0 + \rho gh$ <p>where p_0 is the pressure at the surface of the fluid and h is the distance from the surface</p>
Force of buoyancy	$F_B = F_{g, \text{fluid}} = V_{\text{object}} \rho_{\text{fluid}} g$ <p>The force of buoyancy on an object is the weight of the fluid that was displaced, or the volume of the object times the fluid density times g</p>
Continuity equation for a fluid in motion	$A_1 v_1 = A_2 v_2$
Volume flow rate	$\dot{V} = \frac{dV}{dt} = Av$
Bernoulli's equation	$p + \rho gh + \frac{1}{2} \rho v^2 = \text{constant}$ <p>where h is elevation</p>
Pressure difference required for viscous flow in a circular tube	$\Delta P = \frac{8\eta L}{\pi r^4} \cdot \dot{V}$ <p>where r is the radius of the flow tube, L is its length, and η is the fluid viscosity</p>

Reynold's number for determining flow type in a circular tube	$N_R = \frac{2r\rho v}{\eta}$ <p>where r is the radius of the flow tube and η is the fluid viscosity</p> <p>If $N_R < 2000$, the flow is laminar</p> <p>If $N_R > 3000$, the flow is turbulent</p> <p>If $2000 < N_R < 3000$, it needs to be tested</p>
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Gravitation (Chapter 13)

Law of gravitation	$F_g = \frac{Gm_1m_2}{r^2}$ <p>G is the gravitational constant, $6.67 \cdot 10^{-11} \text{ Nm}^2/\text{kg}^2$</p> <p>$m_1$ and m_2 are the masses of two objects</p> <p>r is the distance between the two objects</p>
Acceleration due to gravity at the surface of a planet	$g = \frac{GM}{R^2}$ <p>where M is the mass of the planet and R is its radius</p>
Gravitational potential energy	$E_{\text{pot, g}} = -\frac{Gm_1m_2}{r}$
Speed in circular orbit	$v = \sqrt{\frac{GM}{r}}$ <p>where M is the mass of the planet and r is the radius of orbit</p>
Period in circular orbit	$T = \frac{2\pi r}{v} = \frac{2\pi r^{\frac{3}{2}}}{\sqrt{GM}}$ <p>where v is the speed of orbit, M is the mass of the planet, and r is the radius of orbit</p>

Periodic motion (Chapter 14)

Period and frequency	$T = \frac{1}{f}$
Angular frequency	$\omega = 2\pi f = \frac{2\pi}{T}$
Condition for simple harmonic motion (SHM)	$F_x = -kx$

Acceleration in SHM as a function of position	$a_x = -\frac{k}{m}x$
Angular frequency, frequency, and period in SHM	$\omega = \sqrt{\frac{k}{m}}$ $f = \frac{1}{2\pi} \sqrt{\frac{k}{m}}$ $T = 2\pi \sqrt{\frac{m}{k}}$
Position, velocity, and acceleration in SHM as functions of time	$x = A \cos(\omega t + \phi)$ $v_x = -\omega A \sin(\omega t + \phi)$ $a_x = -\omega^2 A \cos(\omega t + \phi)$ <p>where A is the amplitude and ϕ is the phase angle. v_x oscillates between ωA and $-\omega A$, and a_x oscillates between $\omega^2 A$ and $-\omega^2 A$</p>
Energy in SHM	$E_{mec} = \frac{1}{2}mv_x^2 + \frac{1}{2}kx^2 = \frac{1}{2}kA^2 = \text{constant}$
Angular SHM	$\omega = \sqrt{\frac{\kappa}{I}}$ $f = \frac{1}{2\pi} \sqrt{\frac{\kappa}{I}}$ <p>where κ is the torsion constant and I is the moment of inertia</p>
Simple pendulum	$\omega = \sqrt{\frac{g}{L}}$ $f = \frac{1}{2\pi} \sqrt{\frac{g}{L}}$ $T = 2\pi \sqrt{\frac{L}{g}}$
Physical pendulum	$\omega = \sqrt{\frac{mgd}{I}}$ $T = 2\pi \sqrt{\frac{I}{mgd}}$ <p>where d is the distance between the center of gravity and the axis of rotation and I is the moment of inertia about the axis</p>

Damped oscillations	$x = Ae^{-\left(\frac{b}{2m}\right)t} \cos(\omega't + \phi)$ $\omega' = \sqrt{\frac{k}{m} - \frac{b^2}{4m^2}}$ <p> A is the initial amplitude b is the damping constant ω' is the angular frequency of the damped oscillations ϕ is the phase angle k is the force constant of the restoring force </p>
Types of damped oscillations	<p>Underdamping: $b < 2\sqrt{km}$</p> <p>Critical damping: $b = 2\sqrt{km}$</p> <p>Overdamping: $b > 2\sqrt{km}$</p>
Resonance	$A = \frac{F_{max}}{\sqrt{(k - m\omega_d^2)^2 + b^2\omega_d^2}}$ <p> ω_d is the driving frequency k is the force constant of the restoring force b is the damping constant </p>

Temperature and Heat (Chapter 17)

Thermal expansion	<p>Linear:</p> $\Delta L = \alpha L_0 \Delta T$ <p>Volume:</p> $\Delta V = \beta V_0 \Delta T$ <p>where α is the coefficient of linear thermal expansion and β is the coefficient of volume thermal expansion. In solids,</p> $\beta = 3\alpha$
Tensile stress from thermal expansion	$\sigma = \frac{F}{A} = -Y\alpha\Delta T$ <p>where Y is Young's modulus</p>
Heat required for a temperature change	$Q = mc\Delta T$ $Q = nC\Delta T$ <p>where Q is heat, c is specific heat capacity, C is molar heat capacity, and n is number of moles</p>

Heat required for a phase change	$Q = \pm mL$ <p>where L is the latent heat of fusion, vaporization, or sublimation. If only part of the substance undergoes a phase change,</p> $Q = \pm x mL$ <p>where x is the fraction that undergoes a phase change</p>
Calorimetry equation	$\sum Q = 0$ <p>for heat flow between objects isolated from their surroundings</p>
Heat current in conduction	$H = \frac{dQ}{dt} = kA \frac{T_H - T_C}{L}$ <p>H is heat current A is the area through which the heat flows L is the length of the heat flow path T_H is the temperature of the hot end T_C is the temperature of the cold end k is the thermal conductivity of the material</p>
Heat current through materials in series	$H_1 = H_2 = H_3 = \dots$
Heat current through materials in parallel	$H_{total} = H_1 + H_2 + H_3 + \dots$
Heat current in radiation	$H = Ae\sigma T^4$ $H_{net} = Ae\sigma(T^4 - T_s^4)$ <p>A is the surface area of the object e is the emissivity of the object σ is the Stefan-Boltzmann constant, $5.67 \cdot 10^{-8} \text{ W}/(\text{m}^2\text{K}^4)$ T is the temperature of the object T_s is the temperature of the surroundings</p>

Thermal properties of matter (Chapter 18)

Ideal gas equation	$pV = nRT$
Comparing two states of a constant mass of ideal gas	$\frac{p_1 V_1}{T_1} = \frac{p_2 V_2}{T_2}$

Moles	$m_{total} = nM$ $M = N_A m_{molecule}$ <p>where n is the number of moles, M is molar mass, and N_A is Avogadro's number, $6.02 \cdot 10^{23} \text{ mol}^{-1}$</p>
Total translational kinetic energy of the molecules in an ideal gas	$E_{kin, tr} = \frac{3}{2} nRT$
Average translational kinetic energy of a single molecule in an ideal gas	$\langle E_{kin, tr} \rangle = \frac{1}{2} m \langle v^2 \rangle = \frac{3}{2} kT$ <p>where $\langle v^2 \rangle$ is the average squared speed and k is the Boltzmann constant, $1.38 \cdot 10^{-23} \text{ J/K} = R/N_A$</p>
Root-mean-square speed of molecules in an ideal gas	$v_{rms} = \sqrt{\langle v^2 \rangle} = \sqrt{\frac{3kT}{m}}$
Mean free path of molecules in an ideal gas	$\lambda = v t_{mean} = \frac{V}{4\pi\sqrt{2}r^2N}$ <p>where t_{mean} is the mean free time, r is the molecular radius, and N is the number of molecules</p>
Theoretical heat capacities	<p>Monatomic gas:</p> $C_V = \frac{3}{2} R$ <p>Diatomic gas:</p> $C_V = \frac{5}{2} R$ <p>Monatomic solid:</p> $C_V = 3R$ <p>where R is the gas constant, 8.314 J/(mol K)</p>

First law of thermodynamics (Chapter 19)

Work in a thermodynamic process	$W = \int_{V_1}^{V_2} p dV$
The first law of thermodynamics	$\Delta E_{int} = Q - W$ <p>where E_{int} is the internal energy of a system, Q is the heat added to the system, and W is the work done by the system</p>

Types of thermodynamic processes	Adiabatic: No heat transfer, $Q = 0$ Isochoric: Constant volume, $W = 0$ Isobaric: Constant pressure, $W = p\Delta V$ and $Q = nC_p\Delta T$ Isothermal: Constant temperature
Work/heat in an isothermal process in an ideal gas	$W = Q = nRT \ln\left(\frac{V_2}{V_1}\right) = nRT \ln\left(\frac{p_1}{p_2}\right)$
Internal energy change in an ideal gas	$\Delta E_{int} = nC_v\Delta T$
Relationship between heat capacities in an ideal gas	$C_p = C_v + R$ where C_p is the molar heat capacity at constant pressure, C_v is the molar heat capacity at constant volume, and R is the gas constant, 8.314 J/K mol
Ratio of heat capacities	$\gamma = \frac{C_p}{C_v}$ For air, $\gamma = 1.4$
Adiabatic processes in ideal gases	$T_1V_1^{\gamma-1} = T_2V_2^{\gamma-1}$ $p_1V_1^\gamma = p_2V_2^\gamma$ $p_1^{1-\gamma}T_1^\gamma = p_2^{1-\gamma}T_2^\gamma$
Work done in an adiabatic process in an ideal gas	$W = nC_v(T_1 - T_2)$ $= \frac{C_v}{R}(p_1V_1 - p_2V_2)$ $= \frac{1}{\gamma - 1}(p_1V_1 - p_2V_2)$

Second law of thermodynamics (Chapter 20)

Efficiency in a heat engine	$e = \frac{W}{Q_H} = 1 + \frac{Q_C}{Q_H} = 1 - \left \frac{Q_C}{Q_H}\right $
Efficiency in the Otto cycle	$e = 1 - \frac{1}{r^{\gamma-1}}$
Coefficient of performance of a refrigerator	$K = \frac{ Q_C }{ W } = \frac{ Q_C }{ Q_H - Q_C }$
Heat transfer in a Carnot engine	$\frac{Q_C}{Q_H} = -\frac{T_C}{T_H}$
Efficiency of a Carnot engine	$e_{Carnot} = 1 - \frac{T_C}{T_H} = \frac{T_H - T_C}{T_H}$

Coefficient of performance of a Carnot refrigerator	$K_{Carnot} = \frac{T_C}{T_H - T_C}$
Entropy change for a reversible process	$\Delta S = \int_1^2 \frac{dQ}{T}$ <p>where 1 and 2 are the initial and final states. If the process is isothermal,</p> $\Delta S = \frac{Q}{T}$
Entropy change for an object undergoing a temperature change	$\Delta S = mc \ln\left(\frac{T_2}{T_1}\right)$
Entropy in terms of microstates	$S = k \ln(w)$ <p>where k is the Boltzmann constant, $1.38 \cdot 10^{-23}$ J/K and w is the number of microstates</p>
Entropy change in terms of microstates	$\Delta S = k \ln\left(\frac{w_2}{w_1}\right)$