

Lecture 1  
Computing Lab II  
CS 252A

Sandeep K. Shukla

Indian Institute of Technology Kanpur

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# Acknowledgement

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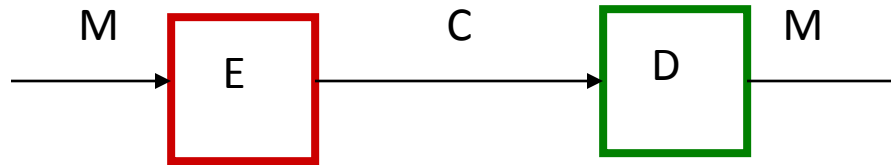
# Outline

- How cryptography works
- Secret key cryptography
- Public key cryptography
- Digital signature
- Message digest
- Distribution of public keys

# Cryptography: Basic Terminology

- Plaintext (or cleartext)
  - The message.
  - Denoted by M or P.
- Encryption (encipher)
  - Encoding of message.
  - Denoted by E.
- Ciphertext
  - Encrypted message.
  - Denoted by C.
- Decryption (decipher)
  - decoding of ciphertext
  - denoted by D.

# Encryption and Decryption



The following identity must hold true:

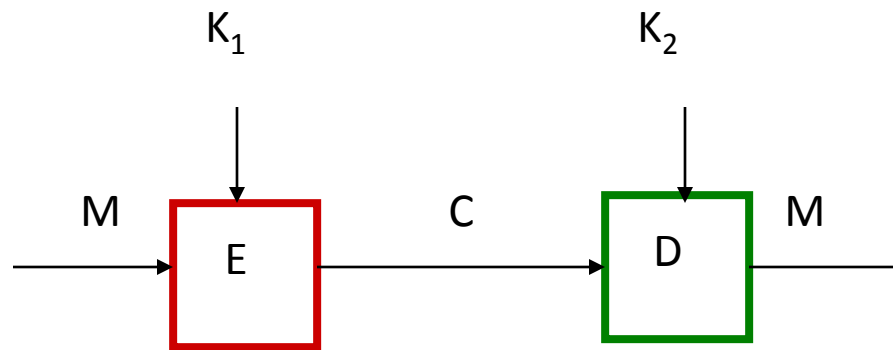
$$D(C) = M, \text{ where } C = E(M)$$

$$M = D(E(M))$$

# Cryptography: Algorithms and Keys

- A method of encryption and decryption is called a **cipher**.
- Generally there are two related functions: one for encryption and other for decryption.
- Some cryptographic methods rely on the secrecy of the algorithms.
- Such methods are mostly of historical interest these days.
- All modern algorithms use a **key** to control encryption and decryption.
- Encryption key may be different from decryption key.

# Key Based Encryption/Decryption



**Symmetric Case:** both keys are the same or derivable from each other

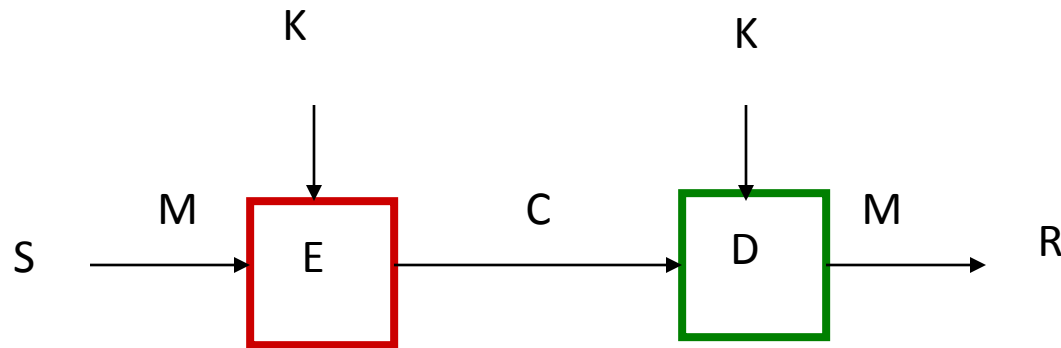
$$K_1 = K_2.$$

**Asymmetric Case:** keys are different and not derivable from each other

$$K_1 \neq K_2$$



# 1. Secret Key Cryptography

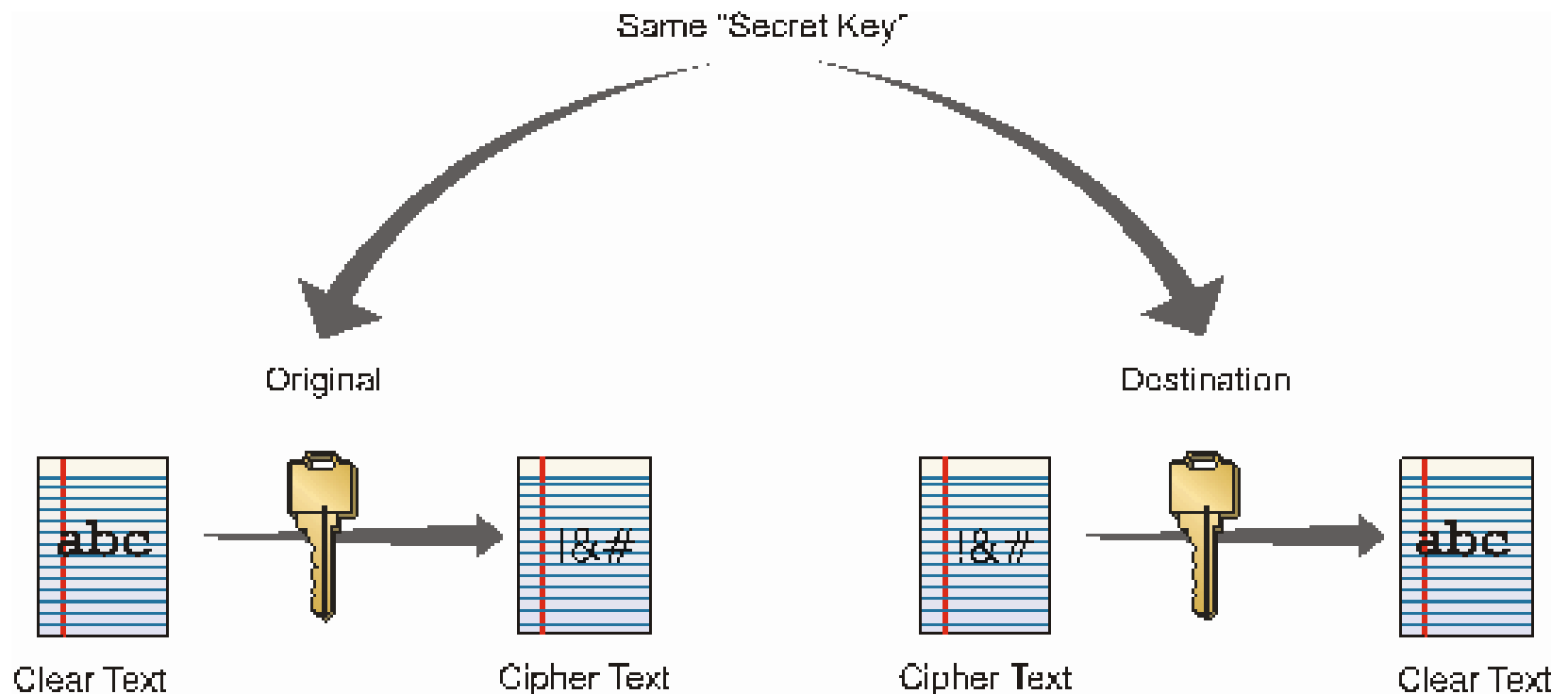


K is the secret key shared by both the sender (S) and receiver (R).

# Secret Key Cryptography

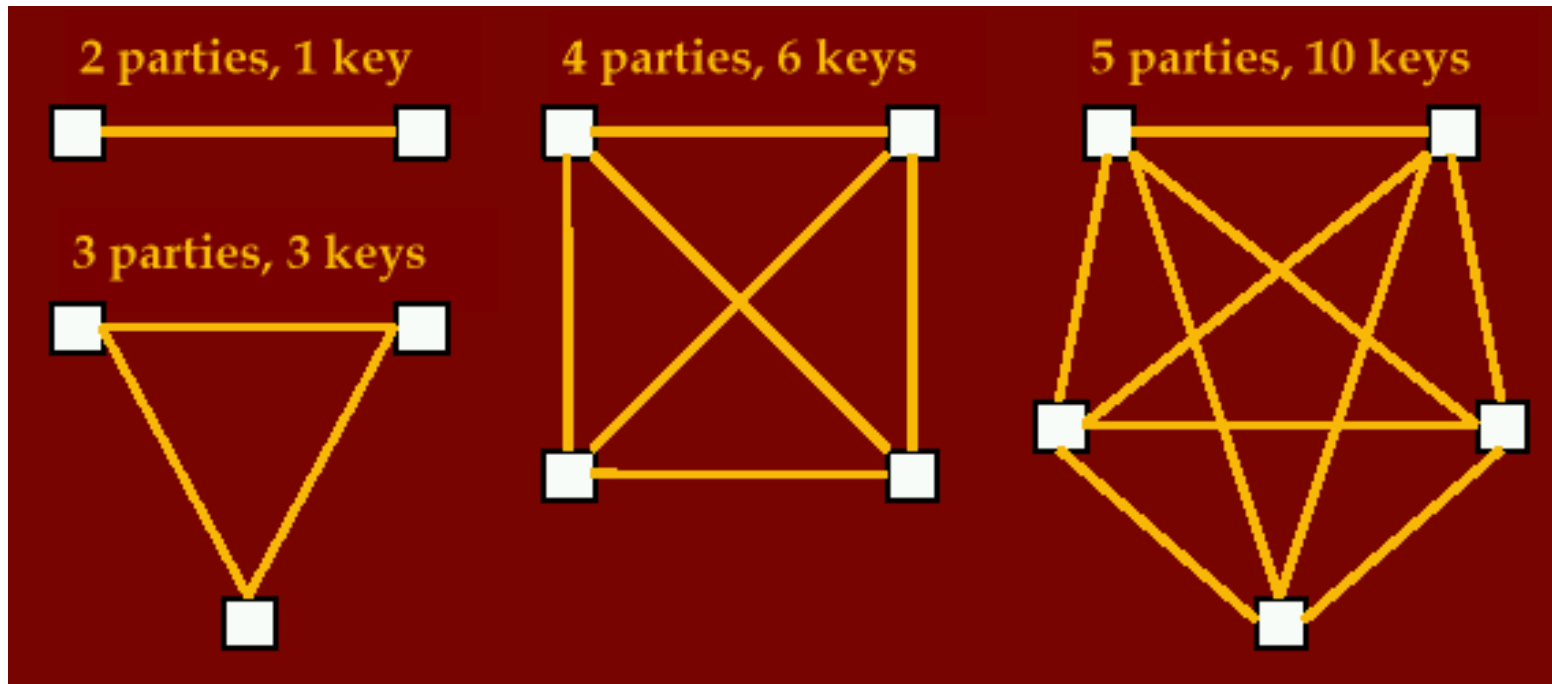
- Also called **symmetric** or single-key algorithms.
- The encryption and the decryption key are the same.
- Techniques based on a combination of substitution and permutation.
- **Stream ciphers**: operate on single bit or byte.
- **Block ciphers**: operate on blocks (typically 64 bits)
- Advantage: simple, fast.
- Disadvantage: ***key exchange, key management***.
- Examples: DES, RC4, IDEA, Blowfish, AES, etc.

# Private Key Cryptosystem (Symmetric)



# Symmetric Key - Issues

Key management, keys required =  $(p*(p-1))/2$  or:



# Secrete Key Assurances

- Confidentiality
  - is assurance that only owners of a shared secrete key can decrypt a message that has been encrypted with the shared secrete key
- Authentication
  - is assurance of the identify of the person at the other end of the line (use challenge and response protocols)
- Integrity
  - is assurance that a message has not been changed during transit and is also called message authentication (use message fingerprint)
- Non-repudiation
  - is assurance that the sender cannot deny a file was sent. This cannot be done with secrete key alone (need trusted third party or public key technology)

# Example: non-repudiation

- Scenario 1:
  - Alice sends a stock buy request to Bob
  - Bob does not buy and claims that he never received the request
- Scenario 2:
  - Alice sends a stock buy request to Bob
  - Bob sends back an acknowledge message
  - Again, Bob does not buy and claims that he never received it
  - Alice presents the ack message as proof
- Can she prove that the ack message was created by him?

# DES (Data Encryption Standard)

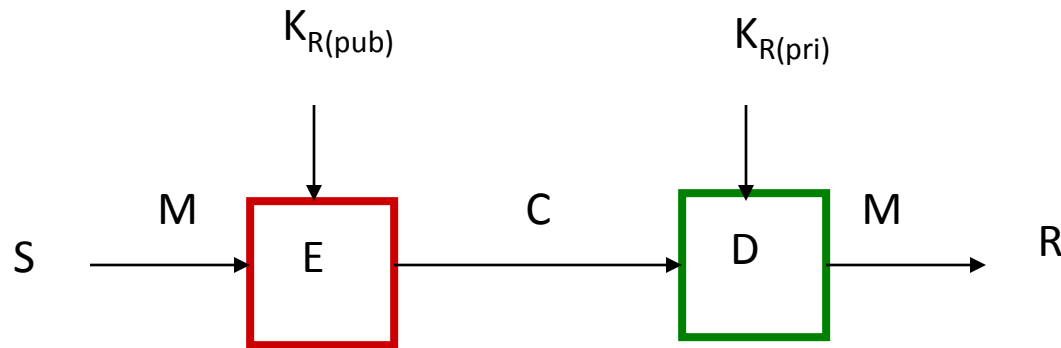
- In 1972, NIST (National Institute of Standards and Technology) decide to assist the development of a secure cryptographic method.
- In 1974, it settled on DES, which was submitted by IBM and is the Data Encryption Algorithm developed by Horst Feistel.
- NSA shortened the secrete key to 56 bits from 128 bits originally proposed by IBM.
- Initially intended for 10 years. DES reviewed in 1983, 1987, 1993.
- In 1997, NIST solicited candidates for a new secrete key encryption standard, Advanced Encryption Standard (AES).
- In Oct 2000, NIST selected Rijndael. ([www.nist.gov/AES](http://www.nist.gov/AES))

# Cycling through DES keys

- In 1977, a 56-bit key was considered good enough.
  - Takes 1,000 years to try all keys with 56 1's and 0's at one million keys per second
- In Jan 1997, RSA Data Security Inc. issued “DES challenge”
  - DES cracked in 96 days
  - In Feb 1998, distributed.net cracked DES in 41 days
  - In July 1998, the Electronic Frontier Foundation (EFF) and distributed.net cracked in 56 hours using a \$250K machine
  - In Jan 1999, the team did in less than 24 hours
- Double and Triple DES
  - Double DES only gives  $2^{57} = 2 \times 2^{56}$ , instead of  $2^{112}$ , due to *meet-in-the-middle* attack.
  - Triple DES recommended, but managing three keys more difficult

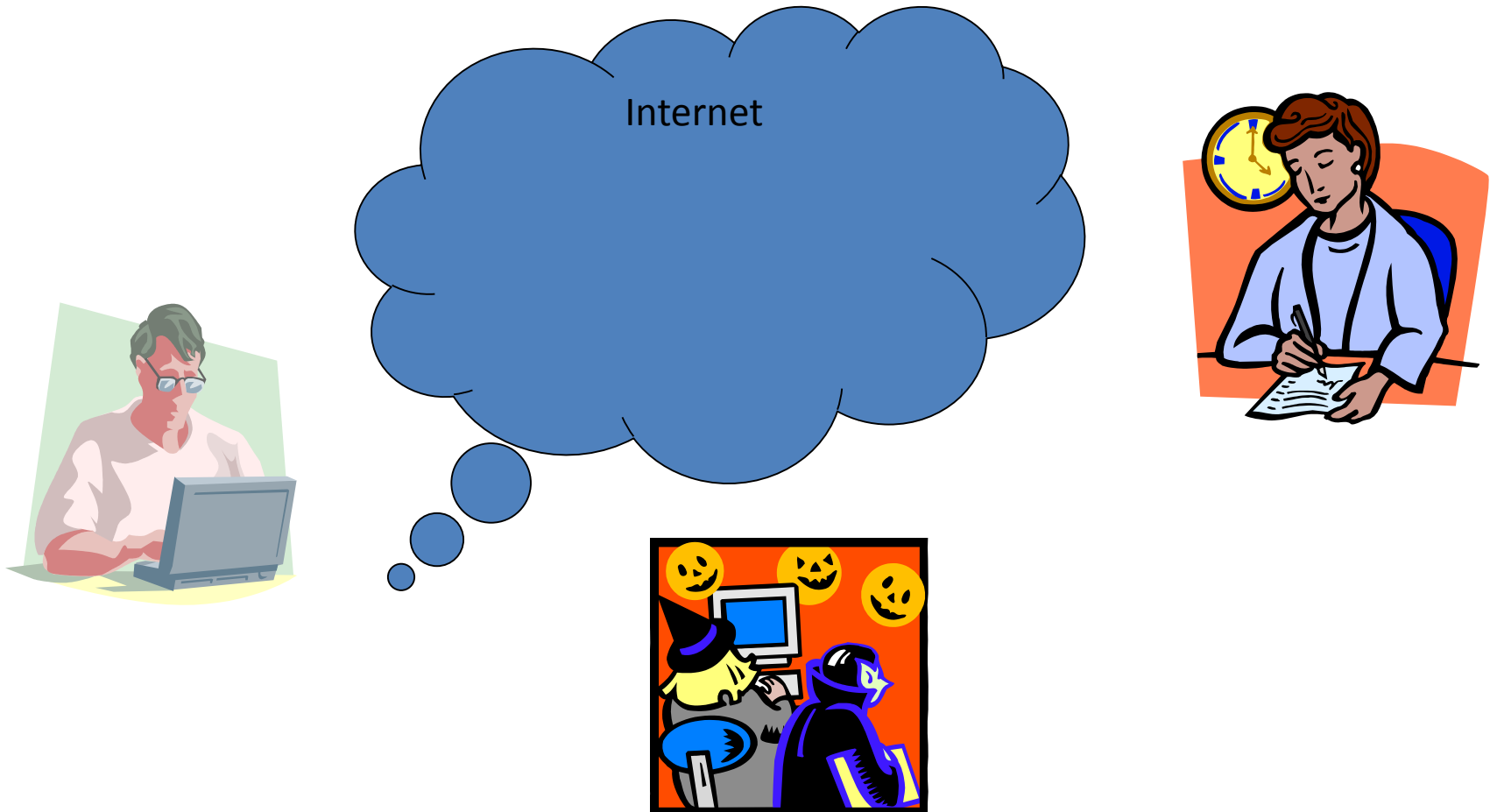


## 2. Public Key Cryptography



$K_{R(pub)}$  is Receiver's public key and  $K_{R(pri)}$  is Receiver's private key.

# Establishing Shared Secrete

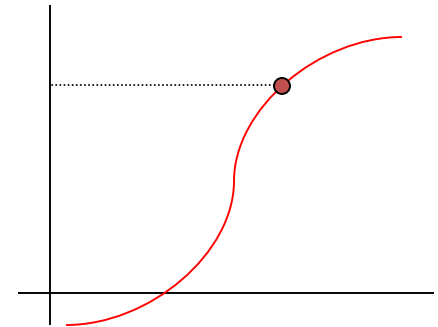


# Problem Statement

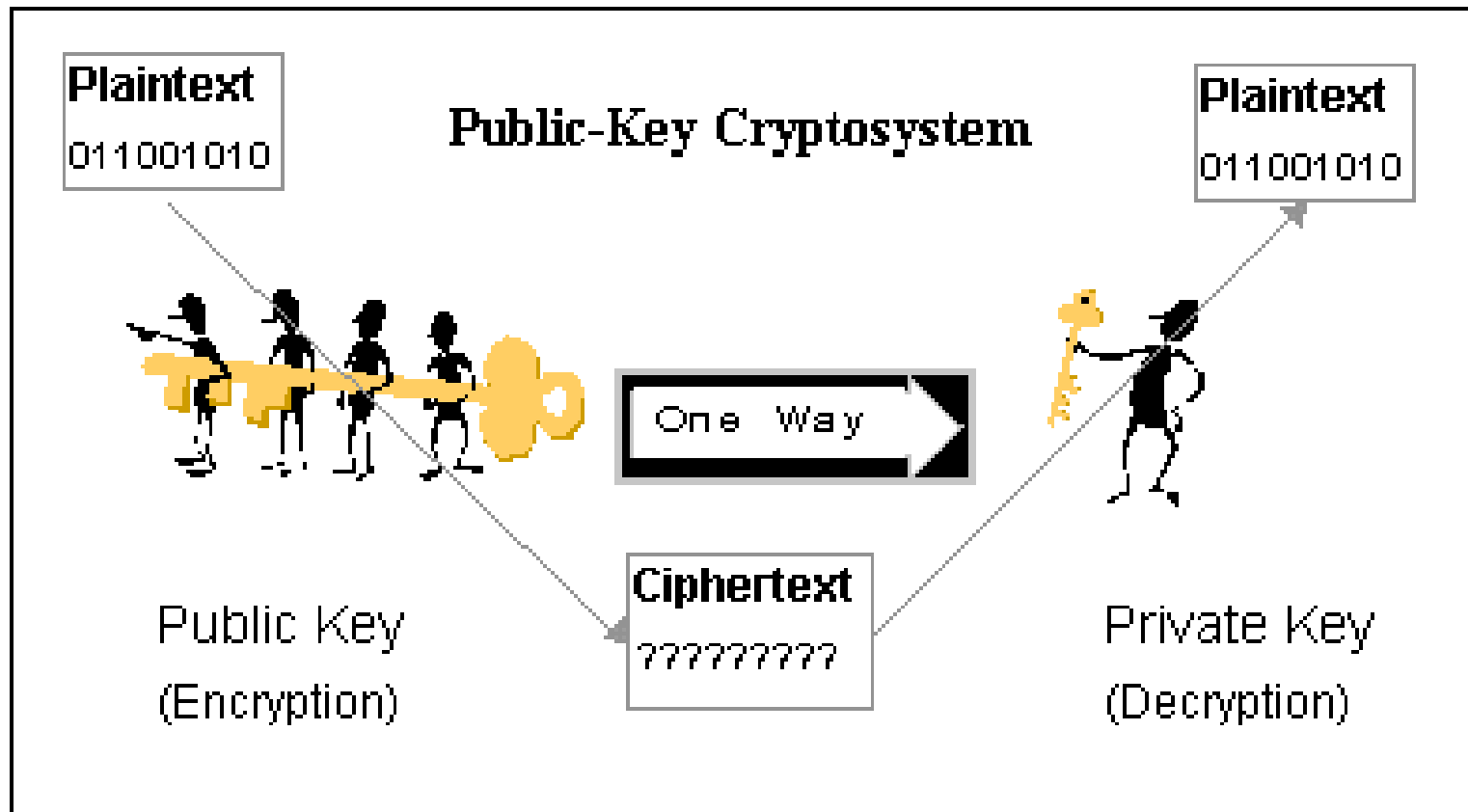
- Suppose Alice has an channel for communicating with Bob.
- Alice and Bob wish to use this channel to establish a shared secret.
- However, Eve is able to learn everything sent over the channel.
- If Alice and Bob have no other channel to use, can they establish a shared secret that Eve does not know?

# Public Key Cryptographic Algorithms

*Find a hard math problem, that is easy to compute in the forward direction, but is difficult to solve in the reverse direction, unless you have some special knowledge.*



# Public Key Cryptosystem



# General Strategy

- A public key is used to encrypt a message that can be decrypted only by the matching private key.
- Bob can use Alice's public key to encrypt messages. Only Alice can decrypt the message.
- Similarly, Alice can also use Bob's public key.
- Alice and Bob exchange information, each keeping a secret to themselves.
- The secrets that they keep allow them to compute a shared secret.
- Since Eve lacks either of these secrets she is unable to compute the shared secret.

# Simplified Math Tricks

- Public key cryptography is based on the mathematical concept of multiplicative inverse.
- Multiplicative inverses are two numbers that when multiplied equals one (e.g.,  $7 \times 1/7 = 1$ )
- In modular mathematics, two whole numbers are inverses if they multiplies to 1 (e.g.,  $3 \times 7 \bmod 10 = 1$ )
- Use modular inverse pairs to create public and private keys.
- Example
  - Message is 4
  - To scramble it, use  $4 \times 3 \bmod 10 = 2$
  - To recover it, use  $2 \times 7 \bmod 10 = 4$
- The security of public key systems depends on the difficulty of calculating inverses.

# Asymmetric Algorithms

- Also called public-key algorithms.
- Encryption key is different from decryption key.
- Furthermore, one cannot be calculated from other.
- Encryption key is often called the **public key** and decryption key is often called the **private key**.
- Advantages: better key management.
- Disadvantages: slower, more complex.
- Both techniques are complementary.
- Examples: RSA, Diffie-Hellman, El Gamal, etc.



# RSA Public Keys

- Named for Ron Rivest, Adi Shamir, and Len Adleman, published in 1978.
- Most widely known and used public key system.
- No shared secret is required.
- Based on some number-theoretic facts/results.
- Strength lies in the difficulty of determining the prime factors of a (large) number.
- Hardware improvements will not weaken RSA as long as appropriate key lengths are used.

# RSA Key Generation

- Pick large random primes  $p, q$ .
- Let  $p * q = n$  and  $\phi = (p-1)(q-1)$ .
- Choose a random number  $e$  such that:  $1 < e < \phi$  and  $\gcd(e, \phi) = 1$ . (relative primes)
- Calculate the unique number  $d$  such that  $1 < d < \phi$  and  $d * e \equiv 1 \pmod{\phi}$ . ( $d$  is inverse of  $e$ )
- The public key is  $\{e, n\}$  and the private key is  $\{d, n\}$ .
- The factors  $p$  and  $q$  may be kept private or destroyed.

# Encryption and Decryption

- Suppose Alice wants to send a message  $m$  to Bob.
- Alice computes  $c = m^e \bmod n$ , where  $\{e, n\}$  is Bob's public key.
- She sends  $c$  to Bob.
- To decrypt, Bob computes  $m = c^d \bmod n$ , where  $\{d, n\}$  is Bob's private key.
- The mathematical relationship between  $e$  and  $d$  ensures that Bob correctly recovers  $m$ .
- Since only Bob knows  $d$ , only he can decrypt.

# RSA - Authentication

- Suppose Alice wants to send a message  $m$  to Bob and ensure him that the message is indeed from her.
- Alice computes signature  $s = m^d \bmod n$ , where  $\{d, n\}$  is Alice's private key.
- She sends  $m$  and  $s$  to Bob.
- To verify the signature, Bob computes using  $\{e, n\}$   $m = s^e \bmod n$  and checks that it is recovered.
- In practice, RSA is combined with a symmetric key cryptosystem (e.g., DES) to encrypt.
- RSA is usually combined with a hash function to sign a message.

# Why Does it Work?

- It is secure because it is difficult to find  $\phi$  or  $d$  using only  $e$  and  $n$ . Finding  $d$  is equivalent in difficulty to factoring  $n$  as  $p \cdot q$ .
- It is feasible to encrypt and decrypt because:
  - It is possible to find large primes.
  - It is possible to find relative primes and their inverses.
  - Modular exponentiation is feasible.

# RSA - Example

- Let  $p = 47$  and  $q = 71$
- then  $n = p * q = 3337$
- $(p-1)*(q-1) = 3220 = \Phi_n$
- Choose (at random)  $e = 79$  [check using GCD (Greatest Common Divisor) that  $\Phi_n$  and  $e$  are relatively prime.]
- Compute  $d = 79^{-1} \bmod 3220 = 1019$
- Private key:  $\{79, 3337\}$
- Public key:  $\{1019, 3337\}$
- Let message  $m$  be 6882326879666683.
- To encrypt, first break it into blocks  $< n$ . [required condition]

# RSA - Example (continued)

- Let message consists of the following blocks:
  - 688, 232, 687, 966, 668, 003
- For the first block
  - $688^{79} \bmod 3337 = 1570 = c_1$
- For the entire message we have
  - 1570, 2756, 2091, 2276, 2423, 158
- To decrypt first block
  - $1570^{1019} \bmod 3337 = 688$
- The rest of the message can be recovered in the same manner.

# More on RSA

- RSA has been implemented in hardware.
- In hardware, RSA is about 1000 times slower than DES.
- In software, it is about 100 times slower.
- These numbers may change, but RSA can never approach the speed of symmetric algorithms.
- RSA encryption goes faster if  $e$  is chosen appropriately.
- Security of RSA depends on the problem of factoring large numbers. Though it has never been proven that one needs to factor  $n$  to calculate  $m$  from  $c$  and  $e$ .
- Most public key systems use at least 2048-bit key.
-



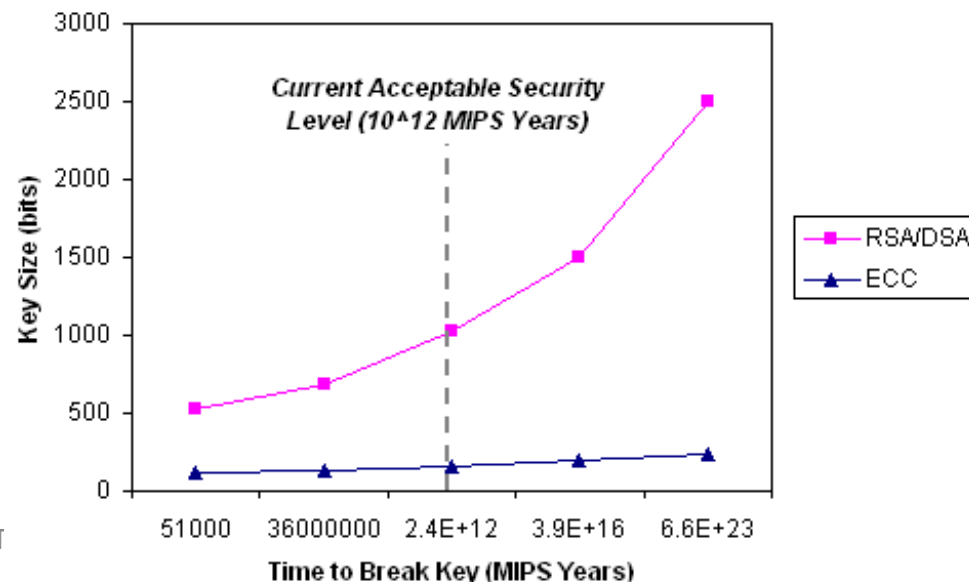
# Key Lengths

- The longer the key, the longer it takes to do an exhaustive key search. The problem space is to find the private key.
- The longer the key, the greater the computational power required to perform cryptographic operations.
- This means a tradeoff between security and time/power.
- Time and power become important for portable devices (cell phones, smart cards, ...).

## Popular key lengths:

- DES = 56 bits
- 3-DES = 168 bits
- RSA = 2048 bits
- ECC < RSA for comparable cryptographic security.

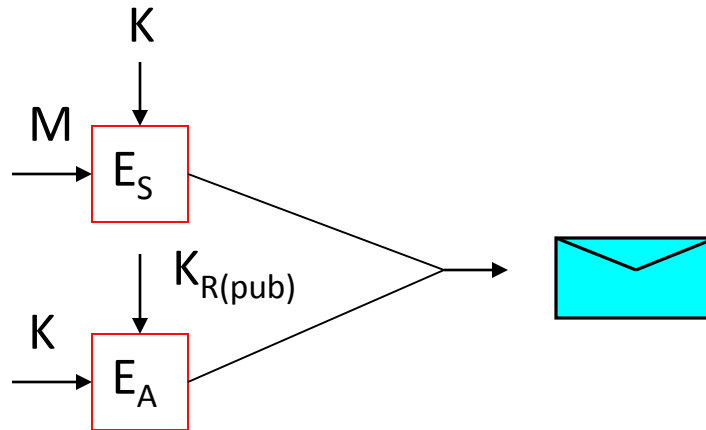
COMPARISON OF SECURITY LEVELS of  
ECC and RSA & DSA



# 3. Hybrid Cryptosystems

- In practice, public-key cryptography is used to secure and distribute **session keys**.
- These keys are used with symmetric algorithms for communication.
- Sender generates a random session key, encrypts it using receiver's public key and sends it.
- Receiver decrypts the message to recover the session key.
- Both encrypt/decrypt their communications using the same key.
- Key is destroyed in the end.

# Digital Envelope



$K$  is a random session key and  $E_S$  is a symmetric encryption algorithm and  $E_A$  is an asymmetric encryption algorithm. The receiver recovers the secret key from the digital envelope using his/her private key. He/she then uses the secret key to decrypt the message.

# 4. Digital Signatures

- A digital signature is a protocol that produces the same effect as a real signature.
  - It is a mark that only sender can make
  - Other people can easily recognize it as belonging to the sender.
- Digital signatures must be:
  - Unforgeable: If P signs message M with signature  $S(P,M)$ , it is impossible for someone else to produce the pair  $[M, S(P,M)]$ .
  - Authentic: R receiving the pair  $[M, S(P,M)]$  can check that the signature is really from P.

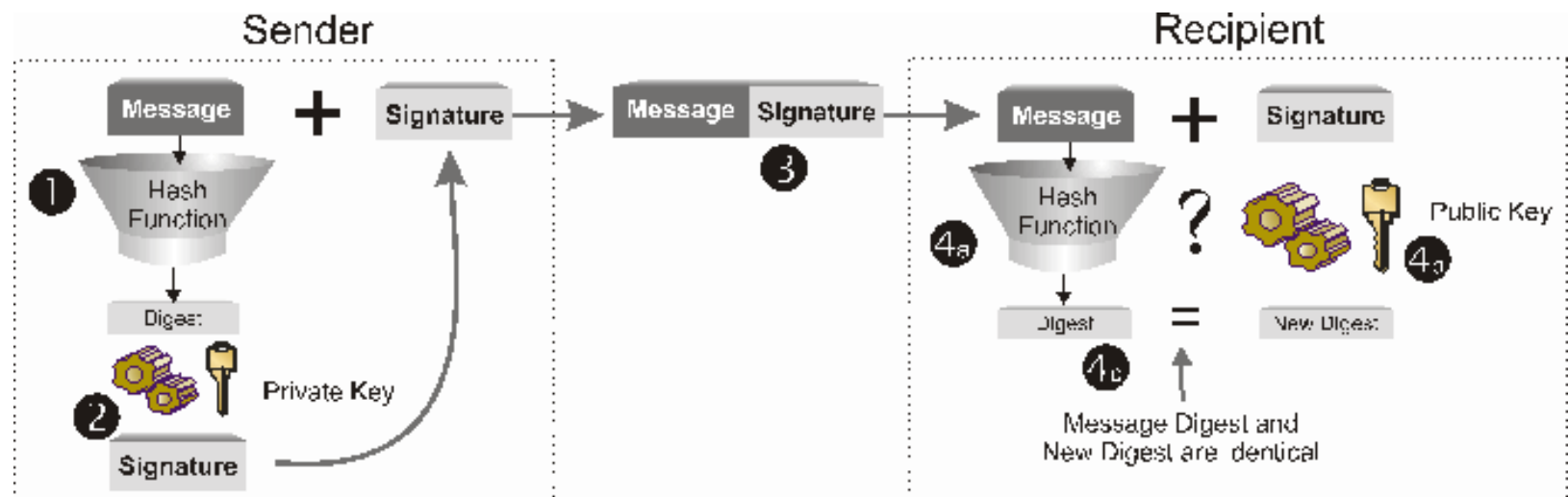
# Digital Signatures: Symmetric Key

- Under private key encryption system, the secrecy of the key guarantees the authenticity of the message as well as its secrecy.
- It does not prevent forgery, however.
- There is no protection against repudiation (denial of sending a message).
- An arbitrator (a trusted third party) is needed to prevent forgery.

# Digital Signatures - Public Key

- Public key encryption systems are ideally suited to digital signatures.
- Reverse of public key encryption/decryption.
- To sign a message, use your private key to encrypt the message.
- Send this signature together with the message.
- The receiver can verify the signature using your public key.
- Only you could have signed the message since your private key belongs to you and only you.
- The receiver saves the message and signature and anyone else can verify should you claim forgery.

# Digital Signature Process



# 5. Message Digest

- How to assure integrity
  - Alice makes a message digest from a plaintext message.
  - Alice signs the message digest and sends the signed digest and plaintext to Bob
  - Bob re-computes the message digest from the plaintext.
  - Bob decrypts the signed digest with Alice's public key.
  - Bob verifies that message is authentic if the message digest he computed is identical to the decrypted digest signed by Alice.



# Possible Scenarios

- Message
  - Plaintext, can be altered
- Message, E(Message-digest, pub-key)
  - Plaintext, encrypted msg digest
- E(message,sym-key), E(message-digest, pub-key)
  - Cipher-text, encrypted msg digest

# Cryptographic Hash Functions

- Hash functions are used in creating “digital fingerprint” of a large message.
- Requirements of such hash functions are:
  - easy to compute (i.e., reduce a message of variable size to a small digest of fixed size)
  - one-way, that is, hard to invert
  - collision-free (the probability that a randomly chosen message maps to an n-bit hash should ideally be  $\frac{1}{2^{**n}}$ )
- To sign a message, first apply a hash function to create a message digest, encrypt the digest using private key and send it along with the message.

# Uses for Hashing Algorithms

- Hash functions without secret keys are used:
  - To condense a message for digital signature.
  - To check the integrity of an input if the hash has been previously recorded.
- Such functions are called Modification Detection Codes (MDC's).
- Hash functions that use secret keys are called Message Authentication Codes (MAC's).
  - They are used for data origin authentication.
- MD5, SHA, SHA-2, SHA-3, SHA-256 etc.

## 6. Public Key Distribution

- Every user has his/her own public key and private key.
- Public keys are all published in a database.
- Sender and receiver agree on a cryptosystem.
- Sender gets receiver's public key from the db.
- Sender encrypts the message and sends it.
- Receiver decrypts it using his/her private key.
- What can be a problem?

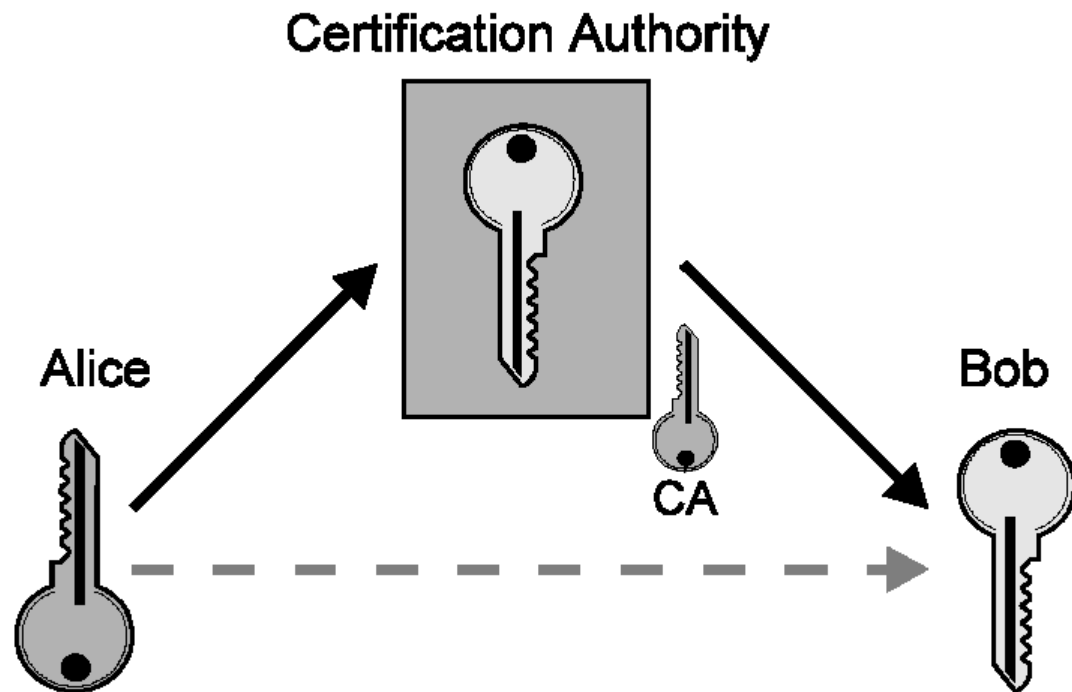
# Matching keys to owners

- Insecurity of TCP/IP
  - No authentication
  - No privacy/confidentiality
  - Repudiation possible
- Public key cryptography not enough
- Need to match keys to owners
- Need *infrastructure* and *certificate authorities*

# Public Key Infrastructure (PKI)

- As defined by Netscape:
  - *“Public-key infrastructure (PKI) is the combination of software, encryption technologies, and services that enables enterprises to protect the security of their communications and business transactions on the Internet.”*
  - Integrates digital certificates, public key cryptography, and certification authorities
- Two major frameworks
  - X.509
  - PGP (Pretty Good Privacy)

# Certification Authorities (CAs)



# Certification Authorities (cont.)

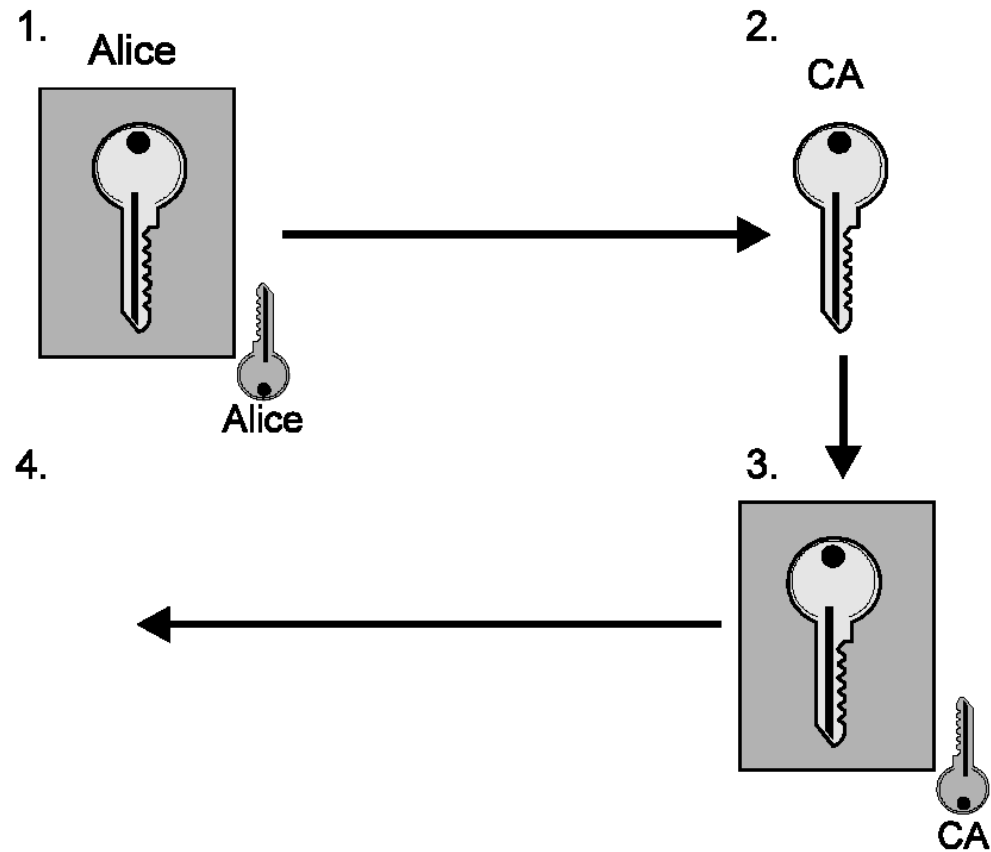
- Guarantee connection between public key and end entity
  - Man-In-Middle no longer works undetected
  - Guarantee authentication and non-repudiation
  - Privacy/confidentiality not an issue here
    - Only concerned with linking key to owner
- Distribute responsibility
  - Hierarchical structure



# Digital Certificates

- Introduced by IEEE-X.509 standard (1988)
- Originally intended for accessing IEEE-X.500 directories
  - Concerns over misuse and privacy violation gave rise to need for access control mechanisms
  - X.509 certificates addressed this need
- From X.500 comes the Distinguished Name (DN) standard
  - Common Name (CN)
  - Organizational Unit (OU)
  - Organization (O)
  - Country (C)
- Supposedly enough to give every entity on Earth a unique name

# Obtaining Certificates



# Obtaining Certificates

- 1. Alice generates  $A_{\text{priv}}$ ,  $A_{\text{pub}}$  and  $A_{\text{ID}}$ ; Signs  $\{A_{\text{pub}}, A_{\text{ID}}\}$  with  $A_{\text{priv}}$ 
  - Proves Alice holds corresponding  $A_{\text{priv}}$
  - Protects  $\{A_{\text{pub}}, A_{\text{ID}}\}$  en route to CA
- 2. CA verifies signature on  $\{A_{\text{pub}}, A_{\text{ID}}\}$ 
  - Verifies  $A_{\text{ID}}$  offline (optional)
- 3. CA signs  $\{A_{\text{pub}}, A_{\text{ID}}\}$  with  $CA_{\text{priv}}$ 
  - Creates certificate
  - Certifies binding between  $A_{\text{pub}}$  and  $A_{\text{ID}}$
  - Protects  $\{A_{\text{pub}}, A_{\text{ID}}\}$  en route to Alice
- 4. Alice verifies  $\{A_{\text{pub}}, A_{\text{ID}}\}$  and CA signature
  - Ensures CA didn't alter  $\{A_{\text{pub}}, A_{\text{ID}}\}$
- 5. Alice and/or CA publishes certificate

# PKI: Benefits

- Provides authentication
- Verifies integrity
- Ensures privacy
- Authorizes access
- Authorizes transactions
- Supports non-repudiation

# PKI: Risks

- Certificates only as trustworthy as their CAs
  - Root CA is a single point of failure
- PKI only as secure as private signing keys
- DNS not necessarily unique
- Server certificates authenticate DNS addresses, not site contents
- CA may not be authority on certificate contents
  - i.e., DNS name in server certificates
- ...