## HW6

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#### Considerations

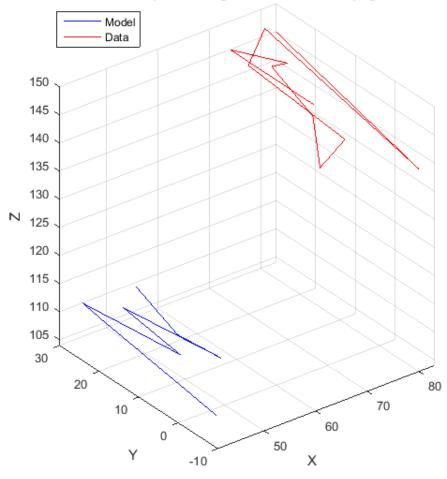
- 1. Simulation developed in MATLAB R2015b
- 2. Calling ICP code developed by Jakob Wilm & Hans Martin KjerAll, Copyright (c) 2012
- 3. First, the data from table1, Page 249 from "A method for Registration of 3-D Shapes" are simulated. It is considered 1, 6 and 10 iterations
- 4. Second, it is considered an array with the initial 200.000 data of the files "pointcloud1.fuse" and "pointcloud2.fuse" with 1, 6 and 10 iterations
- 5. Third, it is considered an array of all data of the files "pointcloud1.fuse" and "pointcloud2.fuse" with 1, 6 and 10 iterations
- 6. Attached the scripts used



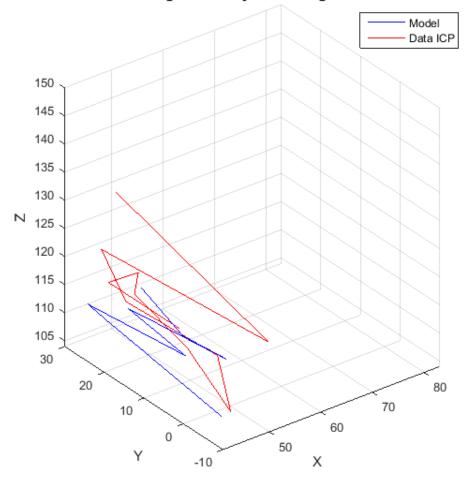


### Data Table 1, page 249

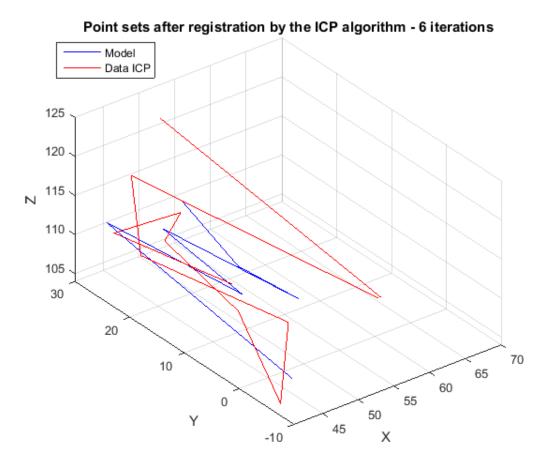


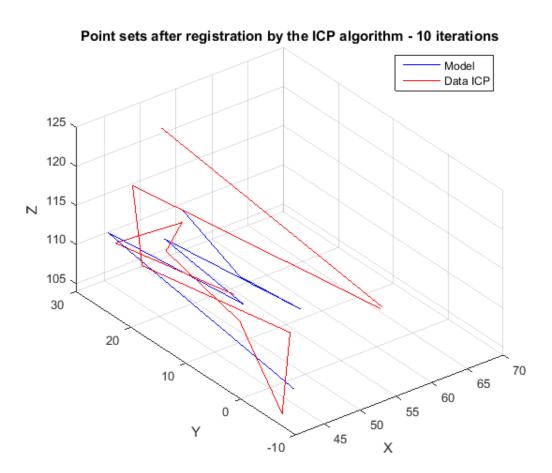


#### Point sets after registration by the ICP algorithm - 1 iterations



#### Data Table 1, page 249





#### **Preliminary**

 $Data_{ICP} = Rotation \times Data^{T} + Translation$ 

Data  $_{ICP}$  = Data after registration by ICP algorithm

Rotation = Rotation Matrix

Data = Data 'pointcloud2.fuse'

Translation = Translation Matrix

Model = Data 'pointcloud1.fuse'

FORMAT DATA		
X	Υ	Z
Intensity		
48,8588580000000 29	2,29952500000000	76,9953100000000
48,8588580000000 18	2,29952900000000	77,0080510000000
48,8588580000000 11	2,29953200000000	77,0017480000000
48,8588580000000 38	2,29953400000000	77,0020830000000
48,8588580000000 13	2,29953600000000	77,0057770000000
48,8588580000000 20	2,29953800000000	77,0790320000000
48,8588580000000	2,29954000000000	77,1124920000000

\*T= transposed matrix

# Partial data 200.000 points – Transformation Matrix (3x3)

$$\mathsf{Rotation}_{(\mathsf{iteration=1})} = \begin{bmatrix} 0.998647819 & 0.051985904 & -2.87E - 06 \\ -0.0519859 & 0.998647819 & -3.67E - 07 \\ 2.85E - 06 & 5.16E - 07 & 1 \end{bmatrix}$$

Translation<sub>(iteration=1)</sub> = 
$$\begin{bmatrix} -0.053225429 \\ 2.543121366 \\ 0.003359531 \end{bmatrix}$$

Runtime routine = 481.68s

$$Rotation_{(iteration=6)} = \begin{bmatrix} 0.991058266 & 0.133429809 & -1.51E - 06 \\ -0.13342981 & 0.991058266 & -3.99E - 07 \\ 1.45E - 06 & 5.97E - 07 & 1 \end{bmatrix}$$

Translation<sub>(iteration=6)</sub> = 
$$\begin{bmatrix} 0.130213226 \\ 6.539833942 \\ 0.015613276 \end{bmatrix}$$

Runtime routine = 10941.39s

$$Rotation_{(iteration=10)} = \begin{bmatrix} 0.991715012 & 0.12845752 & -1.50E - 06 \\ -0.12845752 & 0.991715012 & -2.88E - 07 \\ 1.45E - 06 & 4.79E - 07 & 1 \end{bmatrix}$$

Translation<sub>(iteration=10)</sub> = 
$$\begin{bmatrix} 0.109557569 \\ 6.295374314 \\ 0.021844462 \end{bmatrix}$$

Runtime routine = 29244.90s

#### Partial data 200.000 points – Transformation Matrix (4x4)

$$\text{Rotation}_{(\text{iteration}=1)} = \begin{bmatrix} 0.998647819 & 0.051985904 & -2.87E - 06 & 0 \\ -0.0519859 & 0.998647819 & -3.67E - 07 & 0 \\ 2.85E - 06 & 5.16E - 07 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \qquad \text{Translation}_{(\text{iteration}=1)} = \begin{bmatrix} -0.053225429 \\ 2.543121366 \\ 0.003359531 \\ 0 \end{bmatrix}$$

$$Translation_{(iteration=1)} = \begin{bmatrix} -0.053225429 \\ 2.543121366 \\ 0.003359531 \\ 0 \end{bmatrix}$$

$$\text{Rotation}_{(\text{iteration}=6)} = \begin{bmatrix} 0.991058266 & 0.133429809 & -1.51E - 06 & 0 \\ -0.13342981 & 0.991058266 & -3.99E - 07 & 0 \\ 1.45E - 06 & 5.97E - 07 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \qquad \text{Translation}_{(\text{iteration}=6)} = \begin{bmatrix} 0.130213226 \\ 6.539833942 \\ 0.015613276 \\ 0 \end{bmatrix}$$

$$Translation_{(iteration=6)} = \begin{bmatrix} 0.130213226 \\ 6.539833942 \\ 0.015613276 \\ 0 \end{bmatrix}$$

$$\text{Rotation}_{(\text{iteration}=10)} = \begin{bmatrix} 0.991715012 & 0.12845752 & -1.50E - 06 & 0 \\ -0.12845752 & 0.991715012 & -2.88E - 07 & 0 \\ 1.45E - 06 & 4.79E - 07 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \qquad \text{Translation}_{(\text{iteration}=10)} = \begin{bmatrix} 0.109557569 \\ 6.295374314 \\ 0.021844462 \\ 0 \end{bmatrix}$$

Translation<sub>(iteration=10)</sub> = 
$$\begin{bmatrix} 0.109557569 \\ 6.295374314 \\ 0.021844462 \\ 0 \end{bmatrix}$$

#### **Total data— Transformation Matrix (3x3)**

$$Rotation_{(iteration=1)} = \begin{bmatrix} 0.9999996 & -0,000894269 & -4,44E-06 \\ 0.000894269 & 0.9999996 & 9.31E-06 \\ 4.43E-06 & -9.31E-06 & 1 \end{bmatrix} \qquad Translation_{(iteration=1)} = \begin{bmatrix} 0.002443756 \\ -0.044463646 \\ -0.000178517 \end{bmatrix}$$

$$Translation_{(iteration=1)} = \begin{bmatrix} 0.002443756 \\ -0.044463646 \\ -0.000178517 \end{bmatrix}$$

Runtime routine = 14674.54s

Rotation<sub>(iteration=6)</sub> = 
$$\begin{bmatrix} 0.999370169 & -0.035486131 & -5.95E - 06 \\ 0.035486131 & 0.999370169 & 1.15E - 05 \\ 5.54E - 06 & -1.17E - 05 & 1 \end{bmatrix}$$

Translation<sub>(iteration=6)</sub> = 
$$\begin{bmatrix} 0.112855976 \\ -1.733340549 \\ -0.000145098 \end{bmatrix}$$

Runtime routine = 320394.18s

$$Rotation_{(iteration=10)} = \begin{bmatrix} 0.9985364 & -0.054083795 & -6.28E - 06 \\ 0.054083795 & 0.9985364 & 1.14E - 05 \\ 5.66E - 06 & -1.17E - 05 & 1 \end{bmatrix}$$

Translation<sub>(iteration=10)</sub> = 
$$\begin{bmatrix} 0.196380473 \\ -2.640073794 \\ -8.48E - 05 \end{bmatrix}$$

*Runtime routine* = 811621.64 s

#### **Total data— Transformation Matrix (4x4)**

$$Rotation_{(iteration=1)} = \begin{bmatrix} 0.9999996 & -0,000894269 & -4,44E-06 & 0 \\ 0.000894269 & 0.9999996 & 9.31E-06 & 0 \\ 4.43E-06 & -9.31E-06 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \qquad Translation_{(iteration=1)} = \begin{bmatrix} 0.002443756 \\ -0.044463646 \\ -0.000178517 \\ 0 \end{bmatrix}$$

$$Translation_{(iteration=1)} = \begin{bmatrix} 0.002443756 \\ -0.044463646 \\ -0.000178517 \\ 0 \end{bmatrix}$$

$$\text{Rotation}_{(\text{iteration}=6)} = \begin{bmatrix} 0.999370169 & -0.035486131 & -5.95E - 06 & 0 \\ 0.035486131 & 0.999370169 & 1.15E - 05 & 0 \\ 5.54E - 06 & -1.17E - 05 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \qquad \text{Translation}_{(\text{iteration}=6)} = \begin{bmatrix} 0.112855976 \\ -1.733340549 \\ -0.000145098 \\ 0 \end{bmatrix}$$

$$Translation_{(iteration=6)} = \begin{bmatrix} 0.112855976 \\ -1.733340549 \\ -0.000145098 \\ 0 \end{bmatrix}$$

$$\text{Rotation}_{(\text{iteration}=10)} = \begin{bmatrix} 0.9985364 & -0.054083795 & -6.28E - 06 & 0 \\ 0.054083795 & 0.9985364 & 1.14E - 05 & 0 \\ 5.66E - 06 & -1.17E - 05 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \qquad \text{Translation}_{(\text{iteration}=10)} = \begin{bmatrix} 0.196380473 \\ -2.640073794 \\ -8.48E - 05 \\ 0 \end{bmatrix}$$

Translation<sub>(iteration=10)</sub> = 
$$\begin{bmatrix} 0.196380473 \\ -2.640073794 \\ -8.48E - 05 \\ 0 \end{bmatrix}$$