

# Ames Albedo Reconstruction Software

*Part of the NASA NeoGeography Toolkit*

Version 0.1

Ara Nefian  
Oleg Alexandrov  
Zachary Moratto

Intelligent Robotics Group  
NASA Ames Research Center

April 22, 2014

# Contents

1	Overview . . . . .	2
2	Compiling and running the albedo software . . . . .	2
3	Sample runs . . . . .	3
4	Running the software on multiple machines . . . . .	3
5	The settings file . . . . .	3
6	Requirements for the input . . . . .	5
7	Modeling and the algorithm . . . . .	6
8	Advanced usage . . . . .	7
9	Retrieving the input data from ISIS cubes . . . . .	8
A-1	A sample settings file . . . . .	8

# 1 Overview

The albedo reconstruction software takes the following inputs:

1. A set of DRG (Digital Raster Graphic) images of the Moon in the GeoTIFF format
2. A set of DEM (Digital Elevation Model) images in the GeoTIFF format
3. The Sun and spacecraft position at the moment each DRG image was taken.

The algorithm uses the Sun/spacecraft position and DEM data to correct for the illumination conditions in the DRG images, thus computing Moon's true albedo.

In addition to creating albedo images, the software can also be used for generating image mosaics (see the parameter REFLECTANCE\_TYPE in section 5). In that case, the DEM images and Sun/spacecraft positions are not required.

## 2 Compiling and running the albedo software

The albedo reconstruction software needs to be fetched from GitHub, using the command:

```
git clone https://github.com/NeoGeographyToolkit/PhotometryTK.git
```

This will create a directory named **PhotometryTK**. The **INSTALL** file in that directory has instructions for how to compile and install the software and its pre-requisites.

The albedo reconstruction software can be called by using the script *reconstruct.sh* in the directory **PhotometryTK/src/tools**.

The script is called as follows:

```
reconstruct.sh settings.txt labelStr
```

Here, *settings.txt* is the settings file (section 5), and *labelStr* is a string label. The output of running this command will be stored in the directory *albedo\_labelStr*. This directory will have several subdirectories, with the following names and data:

- *albedo* – a set of albedo tiles in the GeoTIFF format with pixel values between 0 and 255; the size of the tiles is specified in the settings file (section 5)
- *albedo\_sub4* – the albedo tiles at 1/4th the original resolution, together with a kml tree at this resolution that can be visualized in Google Earth<sup>1</sup>
- *error* – the error map for each albedo tile (if COMPUTE\_ERRORS is set to 1, see section 5)
- *DEM* – the averaged DEM values for each albedo tile
- *exposure* – the estimated exposure time for each input DRG image (section 7)
- *weight* – the weights for each image

---

<sup>1</sup>This directory is not generated when the software is run on multiple machines (section 4) as kml generation is hard to parallelise and is best done offline.

### 3 Sample runs

Two *sample runs* (settings files and other necessary input data) are available in the directory PhotometryTK/src/photk/tests. They are executed automatically if the user runs *make check* in PhotometryTK/build.

### 4 Running the software on multiple machines

The albedo reconstruction software can be distributed over a very large number of computing nodes (using GNU parallel), as long as those nodes use the same filesystem. The computing nodes need to be specified in a file, with one machine name per line, and the environmental variable PBS\_NODEFILE should be set to the path to this file.<sup>2</sup> If this variable is not defined, the jobs are only run on the current machine.

The parameter NUM\_PROCESSES in the settings file (section 5) can be used to control how many processes to start on a given computing node. This number depends on the number of cores available on the node, the amount of memory available, and the resolution of the input images (higher resolution requires more memory and therefore fewer processes can be run simultaneously on a node).

### 5 The settings file

The parameters controlling the albedo reconstruction software are specified in a settings file (a sample settings file is shown in the appendix). It has the following entries:

DRG_DIR	The path to the directory of DRG images.
DEM_DIR	The path to the directory of DEM images.
SUN_POSITION_FILE	The Sun position file.
SPACECRAFT_POSITION_FILE	The spacecraft position file.
NUM_PROCESSES	How many simultaneous processes to start on a given computing node.
TILE_SIZE	Output albedo tile size, in degrees (usually 4 by 4 degrees).
SIMULATION_BOX	The region in which to compute the albedo, in the format lon_min : lon_max : lat_min : lat_max. If this parameter is not provided, the region will be assumed to be the entire Moon.

---

<sup>2</sup>On NASA's Pleiades Supercomputer the variable PBS\_NODEFILE is set automatically.

REFLECTANCE_TYPE	The reflectance type. Values: 0 – the reflectance is not be used, the result of albedo reconstruction is just an image mosaic, 1 – the Lambertian reflectance model is used, 2 – the Lunar-Lambertian reflectance model (Equation 2) is used.
SHADOW_THRESH	Shadow threshold, with values between 0 to 255 (the input DRG images have values between 0 to 255, see section 6). Its use depends on the parameter SHADOW_TYPE.
SHADOW_TYPE	Determines how to classify which input DRG image pixels are in the shadow (section 7). Values: 0 – no pixels are in the shadow, 1 – pixels in the shadow are those with values below SHADOW_THRESH, this is the default. Advanced values: 2 – pixels in the shadow satisfy $I/(R \cdot T) < t^3$ , 3 – analogous to option 2, but use the Lunar-Lambertian reflectance model (Equation 2) instead of the Lambertian model.
TR_CONST	A constant which determines how bright the albedo will be, a larger value will make the albedo appear darker.
PHASE_COEFF_C1	The coefficient $c_1$ in reflectance formula (Equation 2).
PHASE_COEFF_C2	The coefficient $c_2$ in the same expression.
MAX_NUM_ITER	Maximum number of albedo update iterations. If it is equal to 0, the image exposure, phase coefficients, and the albedo itself will only be initialized, and no subsequent iterations will take place to improve the initial values (see the algorithm in section 7).
NO_DEM_DATA_VAL	The value used in the DEM images to denote that no data is available at the current pixel. This number is normally stored within the DEM images; only if it absent there will the value specified here be used.

---

<sup>3</sup> $I$  is the image value,  $R$  is the Lambertian reflectance,  $T$  is the image exposure, and  $t$  is the shadow threshold.

USE_WEIGHTS	If to use weights to seamlessly blend the albedo values obtained from individual images (1 means true, and 0 means false). See section 7.
USE_NORMALIZED_COST_FUN	If to enforce that the sum of weights over all images add up to 1 at each pixel. If true, all pixels will contribute in equal amount to the cost function (Equation 1). This flag makes a difference only if multiple albedo iterations are performed ( $\text{MAX\_NUM\_ITER} > 0$ ). Turning this on incurs a significant performance hit.
COMPUTE_ERRORS	If at the end of the algorithm to compute the albedo error map (Equation 7), showing at each pixel what the error was in computing the albedo at that pixel.

## 6 Requirements for the input

As mentioned in section 1, the inputs to the albedo reconstruction software are a set of DRG images, a set of DEM images, and the Sun and spacecraft position for each DRG image. Here we specify the exact requirements for the data as expected by the software.

1. The DRG images should be in a directory and stored in the GeoTIFF format. It is assumed that the intensity values for each image pixel are between 0 and 255 (uint8). The first 11 characters of each image in that directory should be unique, and will be the means by which we will later look up the Sun and spacecraft position for that image. For example, given the image:

DRG\_input\_sub64/AS15-M-0074\_0075-DRG.tif

the lookup key is the 11-character string: AS15-M-0074.

2. The DEM images should be in a directory and stored in the GeoTIFF format. They may or may not overlap. If the DEM images overlap, the values from all images at a given pixel will be averaged. It is expected that the DEM images are either in int16 or float format. If the images lack the No Data Value, it should be explicitly set in the settings file using the parameter NO\_DEM\_DATA\_VAL (section 5).
3. The Sun positions for the DRG images should be listed in a text file, with one line in the file for each DRG image. The same should hold for the spacecraft position. Each line in these lists needs to be in the format:

lookup\_key x y z

where lookup\_key is the 11-character string that identifies the DRG image, and x, y, and z are the coordinates of the Sun (spacecraft) in the Cartesian coordinate system whose origin is the center of the Moon. The values should be in kilometers. An example entry for the Sun position is

AS15-M-0074 -1345328.6130903 151849061.51791 689530.60102555

4. The directories containing the DRG and DEM images should be user-writeable, as the software will create in those directories a list of the GeoTIFF images contained within them, together with the coordinates of the corners of each image. These lists are created only once and speed up subsequent computations.

Sample runs with the inputs satisfying these requirements are available (section 3).

## 7 Modeling and the algorithm

In section we describe the mathematical modeling underlying the albedo reconstruction software.

Let  $I_{ij}^k, A_{ij}, R_{ij}^k, T^k$  be the observed image value, albedo, reflectance, and exposure time. Here,  $(i, j)$  are pixel indices, and  $k$  is the image index.

We would like to determine the set  $\tilde{A}_{ij}, \tilde{T}^k, \tilde{c}_l = \arg \min_{A_{ij}, T^k, c_l} \mathbf{Q}$  where

$$\mathbf{Q} = \sum_k \sum_{ij} \left[ (I_{ij}^k - A_{ij} T^k R_{ij}^k)^2 S_{ij}^k w_{ij}^k \right] \quad (1)$$

Here,  $S_{ij}^k$  is a shadow binary variable,  $S_{ij}^k = 0$  when the pixel  $(i, j)$  is in the shadow and 1 otherwise. The weights  $w_{ij}^k$  are chosen such that they have linearly decreasing values from the center of the image ( $w_{ij}^k = 1$ ) to the image boundaries ( $w_{ij}^k = 0$ ). The choice of these weighs insures that the reconstructed albedo mosaic is seamless.

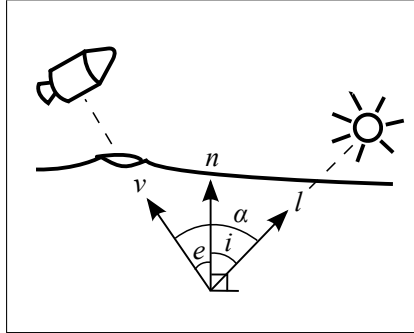


Figure 1: Illumination and viewing angles used by the Lunar-Lambertian reflectance model.

In the above equation the reflectance is computed using the Lunar-Lambertian model and is given by

$$R_{ij}^k = (e^{-c_1 \alpha} + c_2) \left[ (1 - L(\alpha)) \cos(\mathbf{i}_{ij}^k) + 2L(\alpha) \frac{\cos(\mathbf{i}_{ij}^k)}{\cos(\mathbf{i}_{ij}^k) + \cos(\mathbf{e}_{ij}^k)} \right] \quad (2)$$

where  $L(\alpha) = 1 + A\alpha + B\alpha^2 + C\alpha^3$  is a weighting factor between the Lunar and Lambertian reflectance models that depends on the phase angle ( $\alpha$ ),  $\mathbf{i}_{ij}^k$  and  $\mathbf{e}_{ij}^k$  are the incident and emission angles at image  $k$  and pixel  $(i, j)$  (see Figure 1). The numbers  $c_1$  and  $c_2$  are called the *phase coefficients*.

Determining the best albedo reconstruction from a set of images and the corresponding DEM (digital elevation map) is formulated as a cost function minimization problem for the albedo  $A_{ij}$ , image exposures  $T_k$ , and phase coefficients  $c_1$  and  $c_2$ . (Equation 1). An iterative solution to the above least square problem is given by the Gauss-Newton updates described below.

- **Step 1 (initialization):** Compute the average DEM and the weights. Normalize the weights so that the sum of weights at each pixel is 1 if the parameter `USE_NORMALIZED_COST_FUN` is set to 1 in the settings file (section 5). Initialize the exposure time as inversely proportional to the average image reflectance. Initialize the phase coefficients  $c_1$  and  $c_2$  to some reasonable values. Initialize the albedo as the argmin of the cost function  $\mathbf{Q}$  for fixed exposure time and phase coefficients

$$A_{ij} = \frac{\sum_k I_{ij}^k T^k R_{ij}^k S_{ij}^k w_{ij}^k}{\sum_k (T^k R_{ij}^k)^2 S_{ij}^k w_{ij}^k} \quad (3)$$

- **Step 2:** Re-estimate the exposure time using

$$\tilde{T}^k = T^k + \frac{\sum_{ij} (I_{ij}^k - A_{ij} T^k R_{ij}^k) A_{ij} R_{ij}^k S_{ij}^k w_{ij}^k}{\sum_{ij} (A_{ij} R_{ij}^k)^2 S_{ij}^k w_{ij}^k} \quad (4)$$

- **Step 3:** Re-estimate the phase coefficients using

$$\tilde{c}_1 = c_1 + \frac{\sum_{ijk} (I_{ij}^k - A_{ij} T^k R_{ij}^k) A_{ij} T^k \frac{\partial R_{ij}^k}{\partial c_1} S_{ij}^k w_{ij}^k}{\sum_{ijk} \left( A_{ij} T^k \frac{\partial R_{ij}^k}{\partial c_1} \right)^2 S_{ij}^k w_{ij}^k} \quad (5)$$

and analogously for  $c_2$ . The partial derivatives  $\partial R_{ij}^k / \partial c_1$  and  $\partial R_{ij}^k / \partial c_2$  are computed from Equation 2.

- **Step 4:** Re-estimate the albedo using

$$\tilde{A}_{ij} = A_{ij} + \frac{\sum_k (I_{ij}^k - A_{ij} T^k R_{ij}^k) T^k R_{ij}^k S_{ij}^k w_{ij}^k}{\sum_k (T^k R_{ij}^k)^2 S_{ij}^k w_{ij}^k} \quad (6)$$

- **Step 5:** Compute the error cost function  $\mathbf{Q}$  for the re-estimated values of the albedo and exposure time.
- **Convergence:** If the convergence error between the consecutive iterations falls below a fixed threshold then stop. Otherwise return to step 2.
- **Step 6:** Estimate the accuracy of the albedo reconstruction at each pixel using the formula

$$E_{ij} = \frac{\sum_k (I_{ij}^k / (T^k R_{ij}^k) - A_{ij})^2 S_{ij}^k w_{ij}^k}{\sum_k w_{ij}^k} \quad (7)$$

## 8 Advanced usage

The script *reconstruct.sh* computes the albedo by performing a series of calls to the executable *PhotometryTK/build/src/tools/reconstruct*. Advanced users may call this program directly to execute a certain stage of the algorithm (section 7).

The *reconstruct* executable takes the following options:



```

-s [ --settings-file ] arg      Settings file
-r [ --results-directory ] arg  Results directory
-f [ --images-list ] arg        The list of images
-t [ --tiles-list ] arg         The list of albedo tiles
-i [ --image-file ] arg         Current image or tile
--initial-setup                 Initial setup
--save-weights                  Save the weights
--compute-weights-sum          Compute the sum of weights at each pixel
--init-dem                     Initialize the DEM
--init-exposure                 Initialize the exposure times
--init-albedo                   Initialize the albedo
--update-exposure               Update the exposure times
--update-tile-phase-coeffs      Update the phase coefficients per tile
--update-phase-coeffs           Update the phase coefficients by combining the
                                results over all tiles
--update-albedo                 Update the albedo
--compute-errors                Compute the errors in albedo
--is-last-iter                  Is this the last iteration
-h [ --help ]                   Display this help message

```

For example, to initialize the exposure times for a given image, one may issue the command:

```

reconstruct -s settings.txt -r albedo_run -f albedo_run/imagesList.txt -t albedo_run/albedoTilesList.txt
-init-exposure -i DRG_DIR/AS16-M-2961.tif

```

Each time the *reconstruct* executable is run, it echoes the precise command and options which were used to call it, so these calls can be inferred by looking at the output of *reconstruct.sh*.

## 9 Retrieving the input data from ISIS cubes

The albedo reconstruction software assumes that the input DRG images are in GeoTIFF format, and that the sun and spacecraft positions are in text files (section 1). This section describes how to get this data from ISIS cubes.

The DRG images can be obtained by orthoprojecting the ISIS cubes onto the terrain data (a set of DEM tiles) using the script named *orthoproject\_cube.sh* in the directory PhotometryTK/src/tools. The script assumes that the following packages are installed: Ames Stereo Pipeline, ISIS libraries, and the GDAL tools. The paths to them can be set in the script. It can be called as:

```

orthoproject_cube.sh input.cub input_isis_adjust DEM_dir mpp num_proc output.tif

```

The arguments passed to it are, respectively, the cube file to orthoproject, the ISIS adjust file storing the adjusted camera position, the directory containing the DEM tiles to orthoproject onto, the desired output resolution in meters per pixel, the number of processors to use, and the name of the output image.

To get the sun and spacecraft position from a list of ISIS cubes, the script *get\_sun\_or\_spacecraft\_position.pl* is used, also located in PhotometryTK/src/tools. The usage is:

```

get_sun_or_spacecraft_position.pl sun-or-spacecraft inputCubesList.txt outputPositionList.txt

```

## A-1 A sample settings file

```

# Files/directories

```

DRG_DIR	DIM_input_2560mpp
DEM_DIR	DEM_tiles_sub64
SUN_POSITION_FILE	meta/sunpos.txt
SPACECRAFT_POSITION_FILE	meta/spacecraftpos.txt

#### # Constants

NUM_PROCESSES	8
TILE_SIZE	4.0
SIMULATION_BOX	-180:180:-180:180
REFLECTANCE_TYPE	2
SHADOW_THRESH	40
SHADOW_TYPE	1
TR_CONST	1.5
PHASE_COEFF_C1	1.7
PHASE_COEFF_C2	0.4
MAX_NUM_ITER	0
NO_DEM_DATA_VAL	-32767

#### # Actions

USE_WEIGHTS	1
USE_NORMALIZED_COST_FUN	0
COMPUTE_ERRORS	1

# Bibliography

- [1] M. J. Broxton, Z. M. Moratto, A. Nefian, M. Bunte, and M. S. Robinson. Preliminary Stereo Reconstruction from Apollo 15 Metric Camera Imagery. *40th Lunar and Planetary Science Conference*, 2009.
- [2] Ara V. Nefian, Kyle Husmann, Michael J. Broxton, Vinh To, Michael Lundy, and Matthew Hancher. A Bayesian Formulation for Sub-pixel Refinement in Stereo Orbital Imagery. *IEEE International Conference on Image Processing*, 85, November 2009.
- [3] Michael J. Broxton, Ara V. Nefian, Zachary Moratto, Taemin Kim, Michael Lundy, and Aleksandr V. Segal. 3D Lunar Terrain Reconstruction from Apollo Images. *International Symposium on Visual Computing*, 2009.