A Tour of TensorFlow

Proseminar Data Mining

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Abstract—Deep learning is a branch of artificial intelligence employing deep neural network architectures that has significantly advanced the state-of-the-art in computer vision, speech recognition, natural language processing and other domains. In November 2015, Google released TensorFlow, an open source deep learning software library for defining, training and deploying machine learning models. In this paper, we review TensorFlow and put it in context of modern deep learning concepts and software. We discuss its basic computational paradigms and distributed execution model, its programming interface as well as accompanying visualization toolkits. We then compare TensorFlow to alternative libraries such as Theano, Torch or Caffe on a qualitative as well as quantitative basis and finally comment on observed use-cases of TensorFlow in academia and industry.

Index Terms—Artificial Intelligence, Machine Learning, Neural Networks, Distributed Computing, Open source software, Software packages

I. INTRODUCTION

Modern artificial intelligence systems and machine learning algorithms have revolutionized approaches to scientific and technological challenges in a variety of fields. We can observe remarkable improvements in the quality of state-of-the-art computer vision, natural language processing, speech recognition and other techniques. Moreover, the benefits of recent breakthroughs have trickled down to the individual, improving everyday life in numerous ways. Personalized digital assistants, recommendations on e-commerce platforms, financial fraud detection, customized web search results and social network feeds as well as novel discoveries in genomics have all been improved, if not enabled, by current machine learning methods.

A particular branch of machine learning, *deep learning*, has proven especially effective in recent years. Deep learning is a family of representation learning algorithms employing complex neural network architectures with a high number of hidden layers, each composed of simple but non-linear transformations to the input data. Given enough such transformation modules, very complex functions may be modeled to solve classification, regression, transcription and numerous other learning tasks [1].

While deep learning algorithms and individual architectural components such as representation transformations, activation functions or regularization methods may initially be expressed in mathematical notation, they must eventually be transcribed into a computer program for real world usage.

For this purpose, there exist a number of open source as well as commercial machine learning software libraries and frameworks. Among these are Theano [5], Torch [6], scikit-learn [7] and many more, which we review in further detail in Section II of this paper. In November 2015, this list was extended by *TensorFlow*, a novel machine learning software library released by Google [8]. As per the initial publication, TensorFlow aims to be "an interface for expressing machine learning algorithms" in "large-scale [...] on heterogeneous distributed systems" [8].

The remainder of this paper aims to give a thorough review of TensorFlow and put it in context of the current state of machine learning. In detail, the paper is further structured as follows. Section ?? will provide a brief overview and history of machine learning software libraries, listing but not comparing projects similar to TensorFlow. Subsequently, Section II discusses in depth the computational paradigms underlying TensorFlow. In Section III we explain the current programming interface in the various supported languages. To inspect and debug models expressed in TensorFlow, there exist powerful visualization tools, which we examine in Section IV. Section V then gives a comparison of TensorFlow and alternative deep learning libraries on a qualitative as well as quantitative basis. Before concluding our review in Section VII, Section VI studies current real world use cases of TensorFlow in literature and industry.

II. THE TENSORFLOW PROGRAMMING MODEL

In this section we provide an in-depth discussion of the abstract computational principles underlying the TensorFlow software library. We begin with a thorough examination of the basic structural and architectural decisions made by the TensorFlow development team. Subsequently, we study TensorFlow's execution model and provide insight into the way TensorFlow graphs are assigned to available hardware units in a local as well as distributed environment. Lastly, we investigate how TensorFlow implements back-propagation, a crucial step for many machine learning algorithms.

A. Computational Graph Architecture

In TensorFlow, machine learning algorithms are represented as *computational graphs*. A computational or *dataflow* graph is a form of directed graph where *vertices* or *nodes* describe operations, while *edges* or *arcs* represent data flowing between

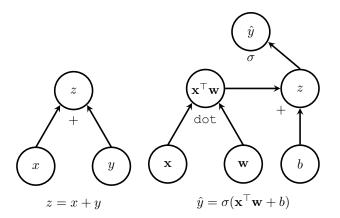


Fig. 1: Examples of computational graphs. The left graph displays a very simple computation, consisting of just an addition of the two input variables x and y. In this case, z is the result of the operation +, as the annotation suggests. The right graph gives a more complex example of computing a logistic regression variable \hat{y} in for some example vector \mathbf{x} , weight vector \mathbf{w} as well as a scalar bias b. As shown in the graph, \hat{y} is the result of the *sigmoid* or *logistic* function σ .

these operations. If an output variable z is the result of applying a binary operation to two inputs x and y, then we draw directed edges from x and y to an output node representing z and annotate the vertex with a label describing the performed computation. Examples for computational graphs are given in Figure 1. The following paragraphs discuss the principle elements of such a dataflow graph, namely *operations*, *tensors*, *variables* and *sessions* in further detail.

1) Operations: The major benefit of representing an algorithm in form of a graph is not only the intuitive (visual) expression of dependencies between units of a computational model, but also the fact that the definition of a *node* within the graph can be kept very general. In TensorFlow, nodes represent *operations*, which in turn express the combination or transformation of data flowing through the graph [8]. An operation can have *zero or more* inputs and produce *zero or more* outputs. As such, an operation may represent a mathematical equation, a variable or constant, a control flow directive, a file I/O operation or even a network communication port. Table ?? gives an overview of different kinds of operations that may be declared in a TensorFlow graph.

Any operation must be backed by an associated implementation. In [8] such an implementation is referred to as the operation's *kernel*. A particular kernel is always specifically

Category	Examples
Element-wise operations	Add, Mul, Exp
Matrix operations	MatMul, MatrixInverse
Value-producing operations	Constant, Variable
Neural network units	SoftMax, ReLU, Conv2D
Checkpoint operations	Save, Restore

TABLE I: Examples for TensorFlow operations [8].

built for execution on a certain kind of device, such as a CPU, GPU or other hardware unit.

- 2) Tensors: In TensorFlow, edges represent data flowing from one operation to another and are referred to as tensors. In the mathematical sense, a tensor is a multi-dimensional collection of homogeneous values with a fixed, static type. In terms of the computational graph, a tensor can be seen as a symbolic handle to one of the outputs of an operation. A tensor itself does not hold or store values in memory, but provides only an interface for retrieving the value referenced by the tensor. When creating an operation in the TensorFlow programming environment, such as for the expression x+y, a tensor object is returned. This tensor may then be supplied as input to other computations, thereby connecting the source and destination operations with an edge. By these means, data flows through a TensorFlow graph.
- 3) Variables: In a typical situation, such as when performing stochastic gradient descent (SGD), the graph of a machine learning model is executed from start to end multiple times for a single experiment. Between two such invocations, the majority of tensors in the graph are destroyed and do not persist. However, it is often necessary to maintain state across evaluations of the graph, such as for the weights and parameters of a neural network. For this purpose, there exist variables in TensorFlow, which are simply special operations that can be added to the computational graph.

In detail, variables can be described as persistent, mutable handles to in-memory buffers storing tensors. As such, variables are characterized by a certain shape and a fixed type. To manipulate and update variables manually (as opposed to implicitly by certain library routines), TensorFlow provides the assign family of graph operations.

4) Sessions: In TensorFlow, the execution of operations and evaluation of tensors may only be performed in a special environment referred to as session. One of the responsibilities of a session is to encapsulate the allocation and management of resources such as variable buffers. Moreover, the Session interface of the TensorFlow library provides a run routine, which is the primary entry point for executing parts or the entirety of a computational graph. This method takes as input the nodes in the graph whose tensors should be computed and returned. Moreover, an optional mapping from arbitrary nodes in the graph to respective replacement values — referred to as feed nodes — may be supplied to run as well [8].

Upon invocation of run, TensorFlow will start at the requested output nodes and work backwards, examining the graph dependencies and computing the full transitive closure of all nodes that must be executed. These nodes are then assigned to one or many physical execution units (CPUs, GPUs etc.) on one or many machines. The rules by which this assignment takes place are determined by TensorFlow's placement algorithm, discussed in detail in Subsection ??. Furthermore, as there exists the possibility to specify explicit orderings of node evaluations, called control dependencies, the execution algorithm will ensure that these dependencies are maintained.

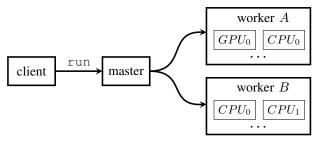


Fig. 2: A visualization of the different execution agents in a multi-machine, multi-device hardware configuration.

B. Execution Model

To execute computational graphs composed of the various elements just discussed, TensorFlow divides the tasks for its implementation among four distinct groups: the *client*, the *master*, a set of *workers* and lastly a number of *devices*. When the client requests evaluation of a TensorFlow graph via a Session's run routine, this query is sent to the master process, which in turn delegates the task to one or more worker processes and coordinates their execution. Each worker is subsequently responsible for overseeing one or more devices, which are the physical processing units for which the kernels of an operation are implemented.

Within this model, there are two degrees of scalability. The first degree pertains to scaling the number of machines on which a graph is executed. The second degree refers to the fact that on each machine, there may then be more than one device, such as, for example, five independent GPUs and/or three CPUs. For this reason, there exist two "versions" of TensorFlow, one for local execution on a single machine (but possibly many devices), and one supporting a *distributed* implementation across many machines and many devices. Figure 2 visualizes a possible distributed setup. While the initial release of TensorFlow supported only single-machine execution, the distributed version was open-sourced on April 13, 2016 [16].

- 1) Devices: Devices are the smallest, most basic entities in the TensorFlow execution model. All nodes in the graph, that is, the kernel of each operation, must eventually be mapped to an available device to be executed. In practice, a device will most often be either a CPU or a GPU. However, TensorFlow supports registration of further kinds of physical execution units by the user. For example, in May 2016, Google announced its Tensor Processing Unit (TPU), a custom built ASIC (application-specific-integrated-circuit) optimized specifically for fast tensor computations [17]. It is thus understandably easy to integrate new device classes as novel hardware emerges.
- 2) Placement Algorithm: To determine what nodes to assign to which device, TensorFlow makes use of a placement algorithm. The placement algorithm simulates the execution of the computational graph and traverses its nodes from input tensors to output tensors. To decide on which of the available devices $\mathbb{D} = \{d_1, \dots, d_n\}$ to place a given node

 ν encountered during this traversal, the algorithm consults a cost model $C_{\nu}(d)$. This cost model takes into account four pieces of information to determine the optimal device $\hat{d} = \arg\min_{d \in \mathbb{D}} C_{\nu}(d)$ on which to place the node during execution:

- Whether or not there exists an implementation (kernel) for a node on the given device at all. For example, if there is no GPU kernel for a particular operation, any GPU device would automatically incur an infinite cost.
- 2) Estimates of the size (in bytes) for a node's input and output tensors.
- 3) The expected execution time for the kernel on the device.
- 4) A heuristic for the cost of cross-device (and possibly cross-machine) transmission of the input tensors to the operation, in the case that the input tensors have been placed on nodes different from the one currently under consideration.
- 3) Cross-Device Execution: If the hardware configuration of the user's system provides more than one device, the placement algorithm will often distribute a graph's nodes among these devices. This can be seen as partitioning the set of nodes into classes, one per device. As a consequence, there may be cross-device dependencies between nodes that must be handled via a number of additional steps. Let us consider for this two devices A and B with particular focus on a node ν on device A. If ν 's output tensor forms the input to some other operations α , β on device B, there conceptually exist cross-device edges $\nu \to \alpha$ and $\nu \to \beta$ from device A to device B. This is visualized in Figure 3a.

In practice, there must be some means of transmitting ν 's output tensor from A, say a GPU device, to B — maybe a CPU device. For this reason, TensorFlow replaces the two edges $\nu \to \alpha$ and $\nu \to \beta$ by two new nodes. On device A, a send node is placed and connected to ν . In tandem, on device B, a recv node is instantiated and attached to α and β . The send and recv nodes are then connected by an additional edge. This is shown in Figure 3b. During execution of the graph, cross-device communication of data occurs exclusively via these special nodes. When the devices are located on separate machines, transmission between the worker processes on these machines may involve remote communication protocols such as TCP or RDMA.

C. Back-Propagation in TensorFlow

In a large number of deep learning and other machine learning algorithms, it is necessary to compute the gradients of particular nodes of the computational graph with respect to one or many other nodes. In [18], two approaches for back-propagating gradients through a computational graph are described. The first, which the authors refer to as *symbolto-number differentiation*, receives a set of input values and then computes the *numerical values* of the gradients at those input values. It does so by explicitly traversing the graph first in the forward order (forward-propagation) to compute the cost, then in reverse order (back-propagation) to compute the gradients via the chain rule. Another approach, more relevant

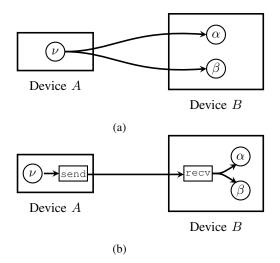


Fig. 3: A conceptual and practical visualization of cross-device communication. Figure 3a shows the conceptual connections between nodes on different devices. Figure 3b gives a more practical overview of how data is actually transmitted across devices using send and recy nodes.

to TensorFlow, is what [18] calls *symbol-to-symbol derivatives* and [8] terms *automatic gradient computation*. In this case, gradients are not computed by an explicit implementation of the back-propagation algorithm. Rather, special nodes are added to the computational graph that calculate the gradient of each operation and thus ultimately the chain rule. To perform back-propagation, these nodes must then simply be executed like any other nodes by the graph evaluation engine. As such, this approach does not produce the desired derivatives as a numeric value, but only as a *symbolic handle* to compute those values.

When TensorFlow needs to compute the gradient of a particular node ν with respect to some other tensor α , it traverses the graph in reverse order from ν to α . Each operation o encountered during this traversal represents a function depending on α and is one of the "links" in the chain $(\nu \circ \ldots \circ o \circ \ldots)(\alpha)$ producing the output tensor of the graph. Therefore, TensorFlow adds a *gradient node* for each such operation o that takes the gradient of the previous link (the outer function) and multiplies it with its own gradient. At the end of the traversal, there will be a node providing a symbolic handle to the overall target derivative $\frac{d\nu}{d\alpha}$, which implicitly implements the back-propagation algorithm. Figure 4 shows how a computational graph may look before and after gradient nodes are added.

III. THE TENSORFLOW PROGRAMMING INTERFACE

Having conveyed the abstract concepts of TensorFlow's computational model in Section II, we will now concretize those ideas and speak to TensorFlow's programming interface. We begin with a brief discussion of the available language interfaces. Then, we provide a more hands-on look at TensorFlow's Python API by walking through a simple practical example.

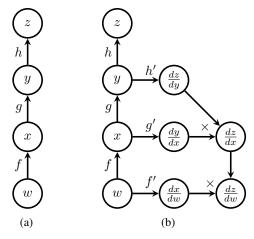


Fig. 4: A computational graph before (4a) and after (4b) gradient nodes are added. In this *symbol-to-symbol* approach, the gradient $\frac{dz}{dw}$ is just simply an operation like any other and therefore requires no special handling by the graph evaluation engine.

A. Interfaces

There currently exist two programming interfaces, in C++ and Python, that permit interaction with the TensorFlow backend. The Python API boasts a very rich feature set for creation and execution of computational graphs. As of this writing, the C++ interface (which is really just the core backend implementation) provides a comparatively much more limited API, allowing only to execute graphs built with Python and serialized to Google's Protocol Buffer¹ format. While there is experimental support for also building computational graphs in C++, this functionality is currently not as extensive as in Python.

B. Walkthrough

In the following paragraphs we give a step-by-step walk-through of a practical, real-world example of TensorFlow's Python API. We will train a simple multi-layer perceptron (MLP) with one input and one output layer to classify handwritten digits in the MNIST² dataset. In this dataset, the examples are small images of 28×28 pixels depicting handwritten digits in $\in \{0,\ldots,9\}$. We receive each such example as a flattened vector of $28 \times 28 = 784$ gray-scale pixel intensities. The label for each example is a *one-hot-encoded* vector $(d_1,\ldots,d_{10})^{\top}$ where the *i*-th component is set to one while all others are zero if the image shows the digit *i*.

To begin our walkthrough, we first import the TensorFlow library:

import tensorflow as tf

Next, we create a new computational graph via the tf.Graph constructor. To add operations to this graph, we must register it as the *default graph*. The way the TensorFlow

¹https://developers.google.com/protocol-buffers/

²http://yann.lecun.com/exdb/mnist/

API is designed, library routines that create new operation nodes always attach these to the current default graph. We register our graph as the default by using it as a Python context manager in a with-as statement:

```
# Create a new graph
graph = tf.Graph()

# Register the graph as the default one to add nodes
with graph.as_default():
    # Add operations ...
```

We are now ready to populate our computational graph with operations. We begin by adding two placeholder nodes examples and labels. Placeholders are special variables that *must* be replaced with concrete tensors upon graph execution. That is, they must be supplied in the feed_dict argument to Session.run(), mapping tensors to replacement values. For each such placeholder, we specify a shape and data type. An interesting feature of TensorFlow at this point is that we may specify the Python keyword None for the first dimension of each placeholder shape. This allows us to later on feed a tensor of variable size in that dimension. For the column size of the example placeholder, we specify the number of features for each image, meaning the $28 \times 28 = 784$ pixels. The label placeholder should expect 10 columns, corresponding to the 10-dimensional one-hot-encoded vector for each label digit:

```
# Using a 32-bit floating-point data type tf.float32
examples = tf.placeholder(tf.float32, [None, 784])
labels = tf.placeholder(tf.float32, [None, 10])
```

Given an example matrix $\mathbf{X} \in \mathbb{R}^{n \times 784}$ containing n images, the learning task then applies an affine transformation $\mathbf{X} \cdot \mathbf{W} + \mathbf{b}$, where \mathbf{W} is a *weight* matrix $\in \mathbb{R}^{784 \times 10}$ and \mathbf{b} a *bias* vector $\in \mathbb{R}^{10}$. This yields a new matrix $\mathbf{Y} \in \mathbb{R}^{n \times 10}$, containing the *scores* or *logits* of our model for each example and each possible digit. To transform the logits into a valid probability distribution, we then pass them through the softmax function:

```
# Draw random weights for symmetry breaking
weights = tf.Variable(tf.random_uniform([784, 10]))
# Slightly positive initial bias
bias = tf.Variable(tf.constant(0.1, shape=[10]))
# tf.matmul performs the matrix multiplication XW
# Note how the + operator is overloaded for tensors
logits = tf.matmul(examples, weights) + bias
# Applies the operation element-wise on tensors
estimates = tf.nn.softmax(logits)
```

Next, we compute our objective function, producing the error or *loss* of the model given its current trainable parameters \mathbf{W} and \mathbf{b} . We do this by calculating the *cross entropy* $H(\mathbf{L},\mathbf{Y})_i = -\sum_j \mathbf{L}_{i,j} \cdot \log(\mathbf{Y}_{i,j})$ between the probability distributions of our estimates \mathbf{Y} and the one-hot-encoded labels \mathbf{L} . More precisely, we consider the mean cross entropy over all examples as the loss:

```
# Computes the cross-entropy and sums the rows
cross_entropy = -tf.reduce_sum(
   labels * tf.log(estimates), [1])
loss = tf.reduce_mean(cross_entropy)
```

Now that we have an objective function, we can run (stochastic) gradient descent to update the weights of our model. For this, TensorFlow provides a GradientDescentOptimizer class. It is initialized with the learning rate of the algorithm and provides an operation minimize, to which we pass our loss tensor. This is the operation we will run repeatedly in a Session environment to train our model:

```
# We choose a learning rate of 0.5
gdo = tf.train.GradientDescentOptimizer(0.5)
optimizer = gdo.minimize(loss)
```

Finally, we can actually train our algorithm. For this, we enter a session environment using a tf.Session as a context manager. We pass our graph object to its constructor, so that it knows which graph to manage. To then execute nodes, we have several options. The most general way is to call Session.run() and pass a list of tensors we wish to compute. Alternatively, we may call eval() on tensors and run() on operations directly. Before evaluating any other node, we must first ensure that the variables in our graph are initialized. For this, we use the tf.initialize_all_variables() utility operation provided by TensorFlow, which in turn executes the initializer operation for each Variable in the graph. Then, we can perform a certain number of iterations of stochastic gradient descent, fetching an example and label mini-batch from the MNIST dataset each time and feeding it to the run function of our optimizer. At the end, our loss will (hopefully) be small:

The full code listing for this example, along with some additional implementation to compute an accuracy metric at each time step is given in Appendix I.

IV. VISUALIZATION OF TENSORFLOW GRAPHS

Deep learning models often employ neural networks with a highly complex and intricate structure. For example, [19] reports of a deep convolutional network based on the Google *Inception* model with more than 36,000 individual units, while [8] states that certain long short-term memory (LSTM) architectures can span over 15,000 nodes. *TensorBoard*, a web interface for graph visualization built directly into TensorFlow, allows the user to maintain a clear overview of such complex structures and facilitates model debugging.

The core feature of TensorBoard is the lucid visualization of computational graphs, exemplified in Figure ??. Graphs

Library	Forward (ms)	Backward (ms)
TensorFlow	26	55
Torch	25	46
Caffe	121	203

TABLE II: The result of Soumith Chintala's benchmarks for TensorFlow, Torch and Caffe (not Theano) on an AlexNet ConvNet model [22], [23].

with complex topologies and many layers can be displayed in a clear and organized manner, allowing the user to understand exactly how data flows through it. Especially useful is TensorBoard's notion of *name scopes*, whereby nodes or entire subgraphs may be grouped into one visual block, such as a single neural network layer. Such name scopes can then be expanded interactively to show the grouped units in more detail. Figure ?? shows the expansion of one the name scopes of Figure ??.

Furthermore, TensorBoard allows the user to track the development of individual tensor values over time. For this, you can attach two kinds of summary operations to nodes of the computational graph: scalar summaries and histogram summaries. Scalar summaries show the progression of a scalar tensor value, which can be sampled at certain iteration counts. In this way, you could, for example, observe the accuracy or loss of your model with time. Histogram summary nodes allow the user to track value distributions, such as those of neural network weights or the final softmax estimates. Figures ?? and ?? give examples of scalar and histogram summaries, respectively. Lastly, TensorBoard also allows visualization of images. This can be useful to show the images sampled for each mini-batch of an image classification task, or to visualize the kernel filters learned for a convolutional neural network [8].

V. COMPARISON WITH OTHER DEEP LEARNING FRAMEWORKS

Next to TensorFlow, there exist a number of other open source deep learning software libraries, the most popular being Theano, Torch and Caffe. In this section, we review two sources of quantitative comparisons between TensorFlow and other deep learning libraries, providing a summary of the most important results of each work.

The first source in our collection is the *convnet-benchmarks* repository on GitHub by Soumith Chintala [22], a research engineer at Facebook. The commit we reference³ is dated April 25, 2016. Chintala provides an extensive set of benchmarks for a variety of convolutional network models. Inter alia, Chintala gives the forward and backward-propagation time of TensorFlow, Torch and Caffe — but not Theano — for the AlexNet CNN model [23]. In these benchmarks, TensorFlow performs second-best in both measures behind Torch, with Caffe lagging relatively far behind. We reproduce the relevant results in Table II.

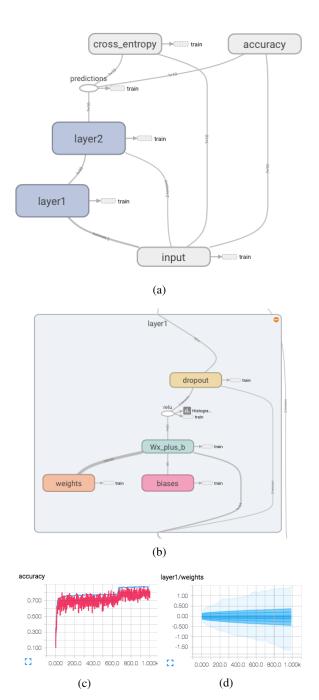


Fig. 5: A demonstration of TensorBoard's graph visualization features. Figure ?? shows the complete graph, while Figure ?? displays the expansion of Layer 1. Figures ?? and ?? give examples for scalar and histogram summaries, respectively.

Further benchmarks were published by the Theano development team in [5] on May 9, 2016. We focus on their results for an LSTM network operating on the Penn Treebank dataset [24]. Their comparisons measure words processed per second for a small model consisting of a single 200-unit hidden layer, and a large model with two 650-unit hidden layers. Moreover, they used cuDNN v4 for all libraries included in their benchmarks, which are TensorFlow, Torch and Theano. Results for

³Commit hash: 84b5bb1785106e89691bc0625674b566a6c02147

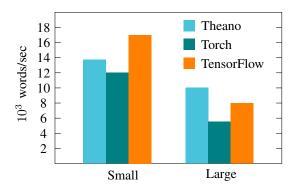


Fig. 6: The results of [5], showing a comparison of Tensor-Flow, Theano and Torch on an LSTM model for the Penn Treebank dataset [24]. On the left the authors tested a small model with a single hidden layer of 200 units; on the right they use two layers with 650 units each.

Caffe are not given. In their benchmarks, TensorFlow performs best among all three for the small model, followed by Theano and then Torch. For the large model, TensorFlow is placed second behind Theano, while Torch remains in last place. Table 5 shows these results.

VI. USE CASES OF TENSORFLOW TODAY

In this section, we investigate where TensorFlow is already in use today. Given that TensorFlow was released only little over 6 months ago as of this writing, its adoption in academia and industry is not yet widespread. The one exception is, of course, Google, which has already deployed TensorFlow for a variety of learning tasks [19], [25]–[27].

The first noteworthy mention of TensorFlow in literature is [29], published by Szegedy, Ioffe and Vanhoucke of the Google Brain Team in February 2016. In their work, the authors use TensorFlow to improve on the *Inception* model [19], which achieved best performance at the 2014 ImageNet classification challenge. The authors report a 3.08% top-5 error on the ImageNet test set.

In [25], Ramsundar et al. discuss massively "multitask networks for drug discovery" in a joint collaboration work between Stanford University and Google, published in early 2016. In this paper, the authors employ deep neural networks developed with TensorFlow to perform virtual screening of potential drug candidates. This is intended to aid pharmaceutical companies and the scientific community in finding novel medication and treatments for human diseases.

August and Ni apply TensorFlow to create recurrent neural networks for optimizing dynamic decoupling, a technique for suppressing errors in quantum memory [30]. With this, the authors aim to preserve the coherence of quantum states, which is one of the primary requirements for building universal quantum computers.

Lastly, we make note of the decision of Google DeepMind, an AI division within Google, to move from Torch7 to TensorFlow [28]. A related source, [17], states that DeepMind

made use of TensorFlow for its *AlphaGo*⁴ model, alongside Google's newly developed Tensor Processing Unit (TPU), which was built to integrate especially well with TensorFlow. In a correspondence of the authors of this paper with a member of the Google DeepMind team, the following four reasons were revealed to us as to why TensorFlow is advantageous to DeepMind:

- 1) TensorFlow is included in the Google Cloud Platform⁵, which enables easy replication of DeepMind's research.
- 2) TensorFlow's support for TPUs.
- 3) TensorFlow's main interface, Python, is one of the core languages at Google, which implies a much greater internal tool set than for Lua.
- 4) The ability to run TensorFlow on many GPUs.

VII. CONCLUSION

We have discussed TensorFlow, a novel open source deep learning library based on computational graphs. Its ability to perform fast automatic gradient computation, its inherent support for distributed computation and specialized hardware as well as its powerful visualization tools make it a very welcome addition to the field of machine learning. Its low-level programming interface gives fine-grained control for neural net construction, while abstraction libraries such as TFLearn allow for rapid prototyping with TensorFlow. In the context of other deep learning toolkits such as Theano or Torch, TensorFlow adds new features and improves on others. Its performance was inferior in comparison at first, but is improving with new releases of the library.

We note that very little investigation has been done in literature to evaluate TensorFlow's qualities with respect to distributed execution. We esteem this one of its principle strong points and thus encourage in-depth study by the academic community in the future.

TensorFlow has gained great popularity and strong support in the open-source community with many third-party contributions, making Google's move a sensible decision already. We believe, however, that it will not only benefit its parent company, but the greater scientific community as a whole; opening new doors to faster, larger-scale artificial intelligence.

APPENDIXI

```
#!/usr/bin/env python
# -*- coding: utf-8 -*-
""" A one-hidden-layer-MLP MNIST-classifier. """
from __future__ import absolute_import
from __future__ import division
from __future__ import print_function

# Import the training data (MNIST)
from tensorflow.examples.tutorials.mnist import
    input_data
import tensorflow as tf
```

⁴https://deepmind.com/alpha-go

⁵https://cloud.google.com/compute/

```
# Possibly download and extract the MNIST data set.
# Retrieve the labels as one-hot-encoded vectors.
mnist = input_data.read_data_sets("/tmp/mnist",
    one_hot=True)
# Create a new graph
graph = tf.Graph()
# Set our graph as the one to add nodes to
with graph.as_default():
   # Placeholder for input examples (None =
       variable dimension)
   examples = tf.placeholder(shape=[None, 784],
       dtype=tf.float32)
   # Placeholder for labels
   labels = tf.placeholder(shape=[None, 10],
       dtype=tf.float32)
   weights =
       tf. Variable (tf.truncated_normal(shape=[784,
       10], stddev=0.1))
   bias = tf.Variable(tf.constant(0.1, shape=[10]))
   # Apply an affine transformation to the input
       features
   logits = tf.matmul(examples, weights) + bias
   estimates = tf.nn.softmax(logits)
   # Compute the cross-entropy
   cross_entropy = -tf.reduce_sum(labels *
       tf.log(estimates),
                          reduction indices=[1])
   # And finally the loss
   loss = tf.reduce_mean(cross_entropy)
   # Create a gradient-descent optimizer that
       minimizes the loss.
   # We choose a learning rate of 0.01
   optimizer =
       tf.train.GradientDescentOptimizer(0.5).minimize(lossomputation of mathematical expressions," ArXiv e-prints, May 2016.
   # Find the indices where the predictions were
       correct
   correct_predictions = tf.equal(
      tf.argmax(estimates, dimension=1),
      tf.argmax(labels, dimension=1))
       tf.reduce_mean(tf.cast(correct_predictions,
       tf.float32))
with tf.Session(graph=graph) as session:
   tf.initialize_all_variables().run()
   for step in range(1001):
      example_batch, label_batch =
          mnist.train.next_batch(100)
      feed_dict = {examples: example_batch, labels:
          label_batch}
      if step % 100 == 0:
         _, loss_value, accuracy_value =
             session.run(
           [optimizer, loss, accuracy],
          feed_dict=feed_dict
         print("Loss at time {0}: {1}".format(step,
             loss_value))
         print("Accuracy at time {0}:
             {1}".format(step, accuracy_value))
```

optimizer.run(feed_dict)

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